Swap test equations

Abstract

Equations typed in \LaTeX to explain swap test circuit implemented with Qiskit in python. Complete description available here.

Equations

$$\begin{split} \frac{1}{\sqrt{2}}(|q_1q_20\rangle+|q_1q_21\rangle) \\ \frac{1}{\sqrt{2}}(|q_1q_20\rangle+|q_2q_11\rangle), \text{ notice that } |q_1\rangle \text{ and } |q_2\rangle \text{ are swapped in the case that } |a_0\rangle=|1\rangle \\ \frac{1}{2}(|q_1q_20\rangle+|q_1q_21\rangle+|q_2q_10\rangle-|q_2q_11\rangle) \\ \frac{1}{2}(|q_1q_21\rangle+|q_1q_20\rangle+|q_2q_11\rangle-|q_2q_10\rangle) \\ \frac{1}{2}(|qq1\rangle+|qq0\rangle+|qq1\rangle-|qq0\rangle) = \frac{1}{2}(2\,|qq1\rangle)=|qq1\rangle \\ \frac{1}{2}(|011\rangle+|010\rangle+|101\rangle-|100\rangle), \text{ and nothing can be simplified} \end{split}$$