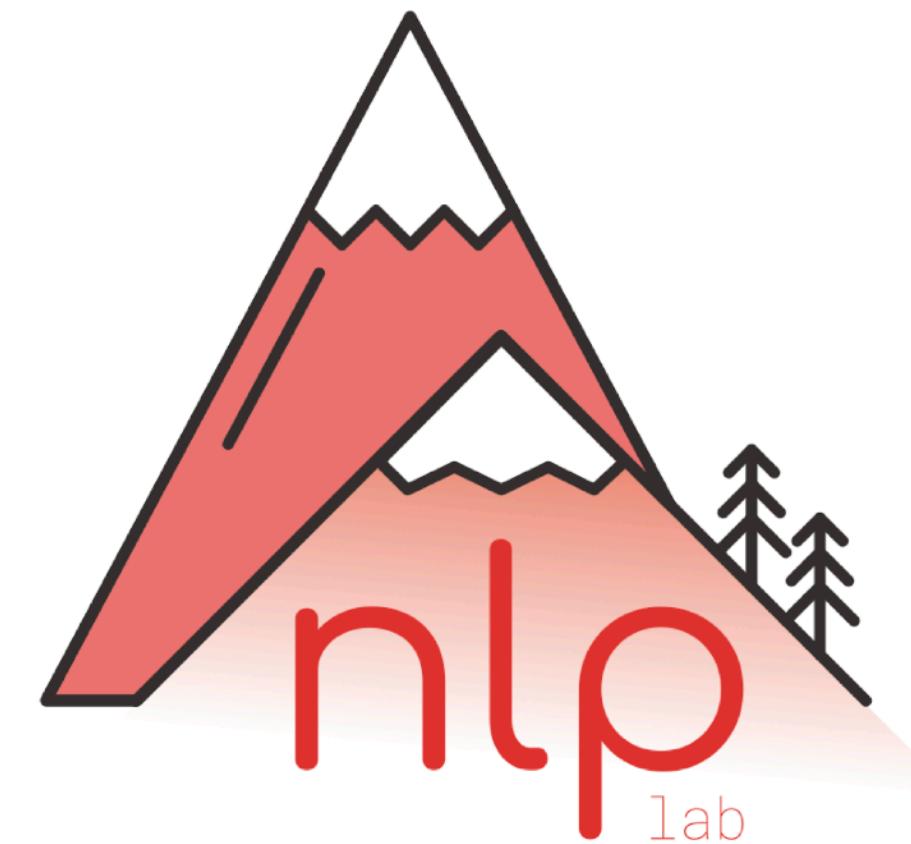


# Neural Word Embeddings

Antoine Bosselut



# Announcements

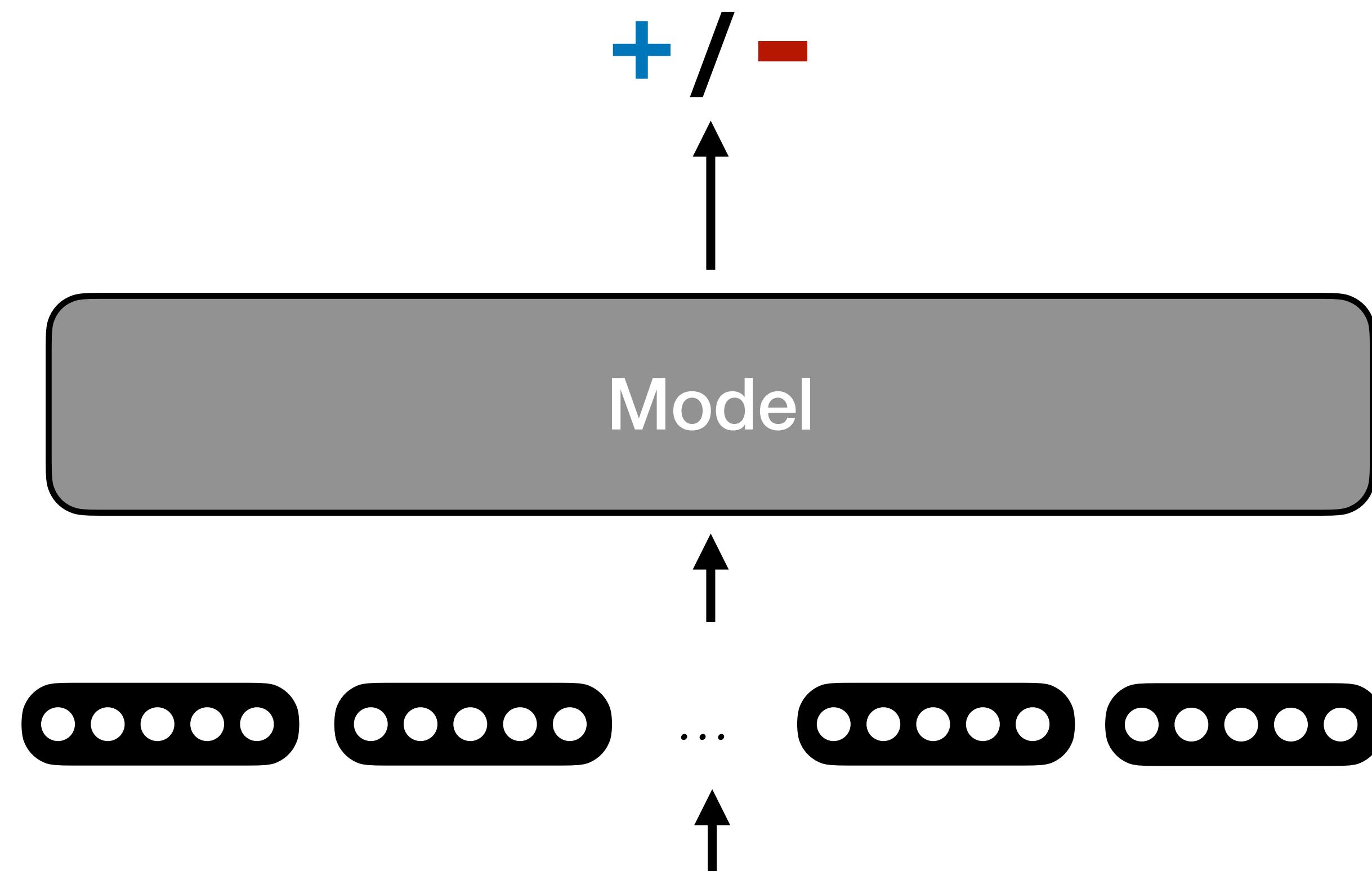
- Lectures are being recorded and MediaSpace channel is posted to the course website.
  - Make sure to see lectures marked [2026]
  - First lectures should be online by next week
- You can audit the class, but you can't take the midterm and project milestones won't be graded. We also can't guarantee access to resources

# Today's Outline

- **Recap:** Words are vectors!
- **New:** Learning self-supervised vector representations - CBOW, Skipgram, GloVe, fastText

# Word Representations

- How do we represent natural language sequences for NLP problems?



In neural natural  
language processing,  
**words are vectors!**

*I really enjoyed the movie we watched on Saturday!*

# Three Parts in our System

- **Embeddings:** how do we represent sequences of discrete words ?
- **Model:** how do we compose these embeddings to get sequence-level meaning representations?
- **Prediction:** how do we map our model's representation of a sequence to a task-relevant prediction?

**Today, let's talk about embeddings in more detail !**

# Choosing a vocabulary

- Language contains many words (e.g., ~600,000 in English)
  - **What about other tokens:** Capitalisation? Accents ? Typos!? Words in other languages!? In other scripts!? Emojis !? Unicode !?
  - **Millions of potential unique tokens!** Most rarely appear in our training data (Zipfian distribution)
  - Model has limited capacity
- How should we select which tokens we want our model to process?
  - Next week - tokenisation!
  - For now, initialize a vocabulary  $V$  of tokens that we can represent as a vector
  - Any token not in this vocabulary  $V$  is mapped to a special <UNK> token (i.e., “unknown”).

# How to represent words: sparse embeddings

- Define a vocabulary  $V$
- Each word in the vocabulary is represented by a sparse vector
- Dimensionality of sparse vector is size of vocabulary (e.g., thousands, possibly millions)

$$x_i \in \{0,1\}^V$$

I	→	[ 0 ... 0 0 0 1 ... 0 0 ]
really	→	[ 0 ... 1 ... 0 0 0 0 ]
enjoyed	→	[ 0 ... 0 0 0 1 0 ... 0 ]
the	→	[ 0 ... 0 1 0 0 0 ... 0 ]
movie	→	[ 0 ... 0 0 0 0 0 ... 1 ]
!	→	[ 1 ... 0 0 0 0 0 0 0 ]

# Problem: sparse embeddings

**With sparse vectors, similarity is a function of common words!**

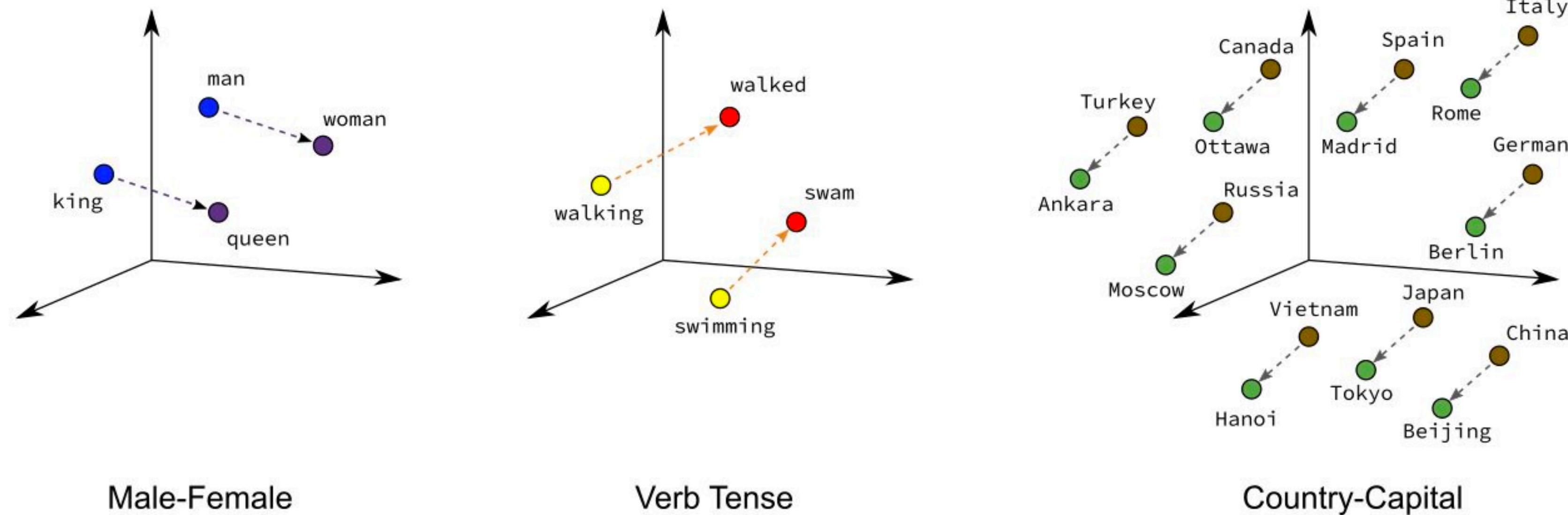
**How do you learn learn similarity between words?**

enjoyed → [ 0 ... 0 0 1 ... 0 0 ]

loved → [ 0 ... 1 ... 0 0 0 0 ]

$$\text{sim( enjoyed, loved )} = 0$$

# Embeddings Goal



**How do we train semantics-encoding embeddings of words?**

# Dense Embeddings

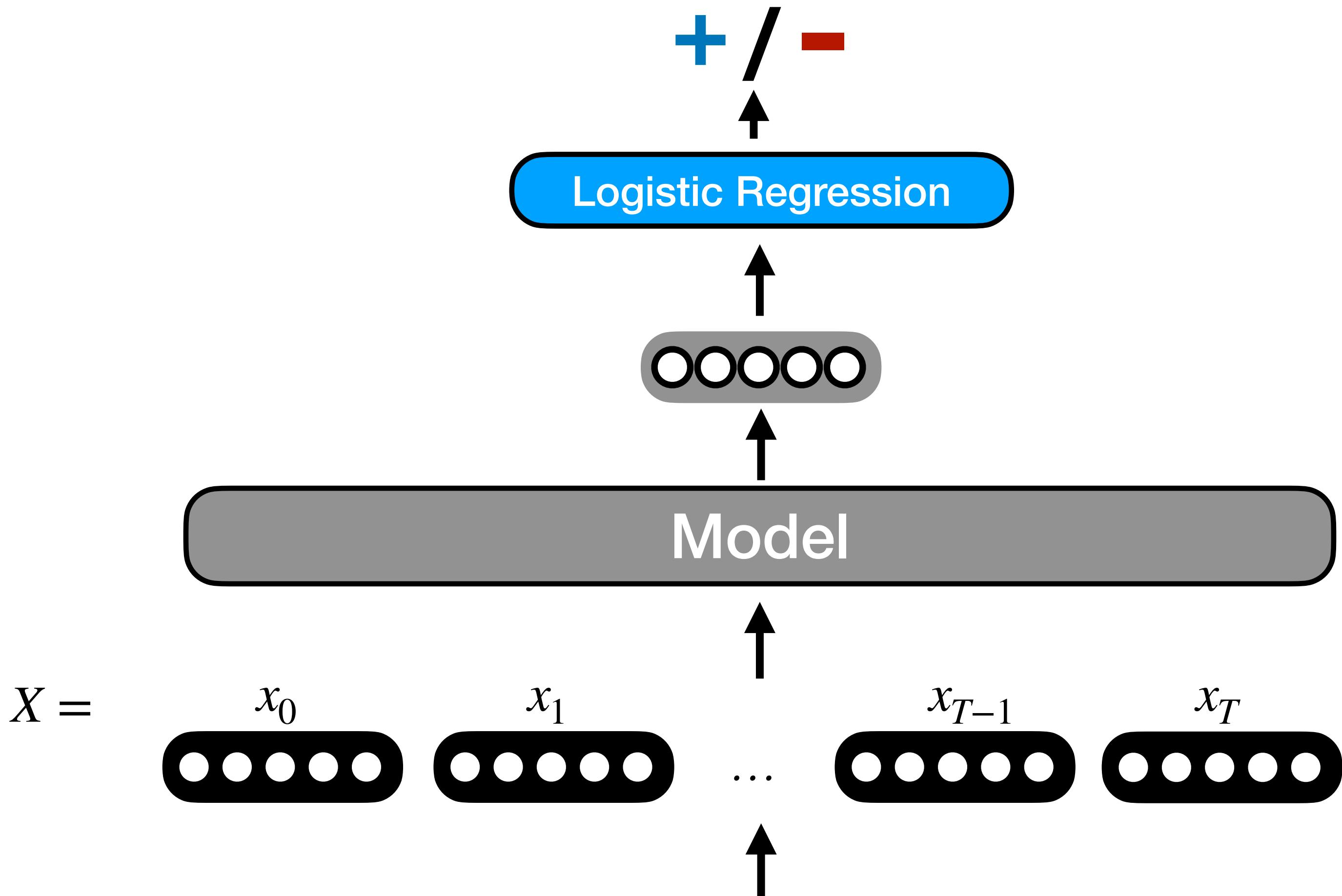
- Represent each word as a high-dimensional\*, **real-valued** vector
  - \*Low-dimensional compared to V-dimension sparse representations, but still usually  $O(10^2 - 10^3)$

I	→	[ 0.113 -0.782 1.893 0.984 6.349 ... ]
really	→	[ 0.906 0.661 -0.214 -0.894 -0.880 ... ]
enjoyed	→	[ -0.842 0.647 -0.882 0.045 0.029 ... ]
the	→	[ 0.100 0.765 -0.333 -0.538 -0.150 ... ]
movie	→	[ 0.104 -0.054 -0.268 -0.877 0.005 ... ]
!	→	[ 0.439 -0.577 -0.727 0.261 0.699 ... ]

word vectors  
word embeddings  
neural embeddings  
dense embeddings  
others...

- Similarity of vectors represents similarity of meaning for particular words

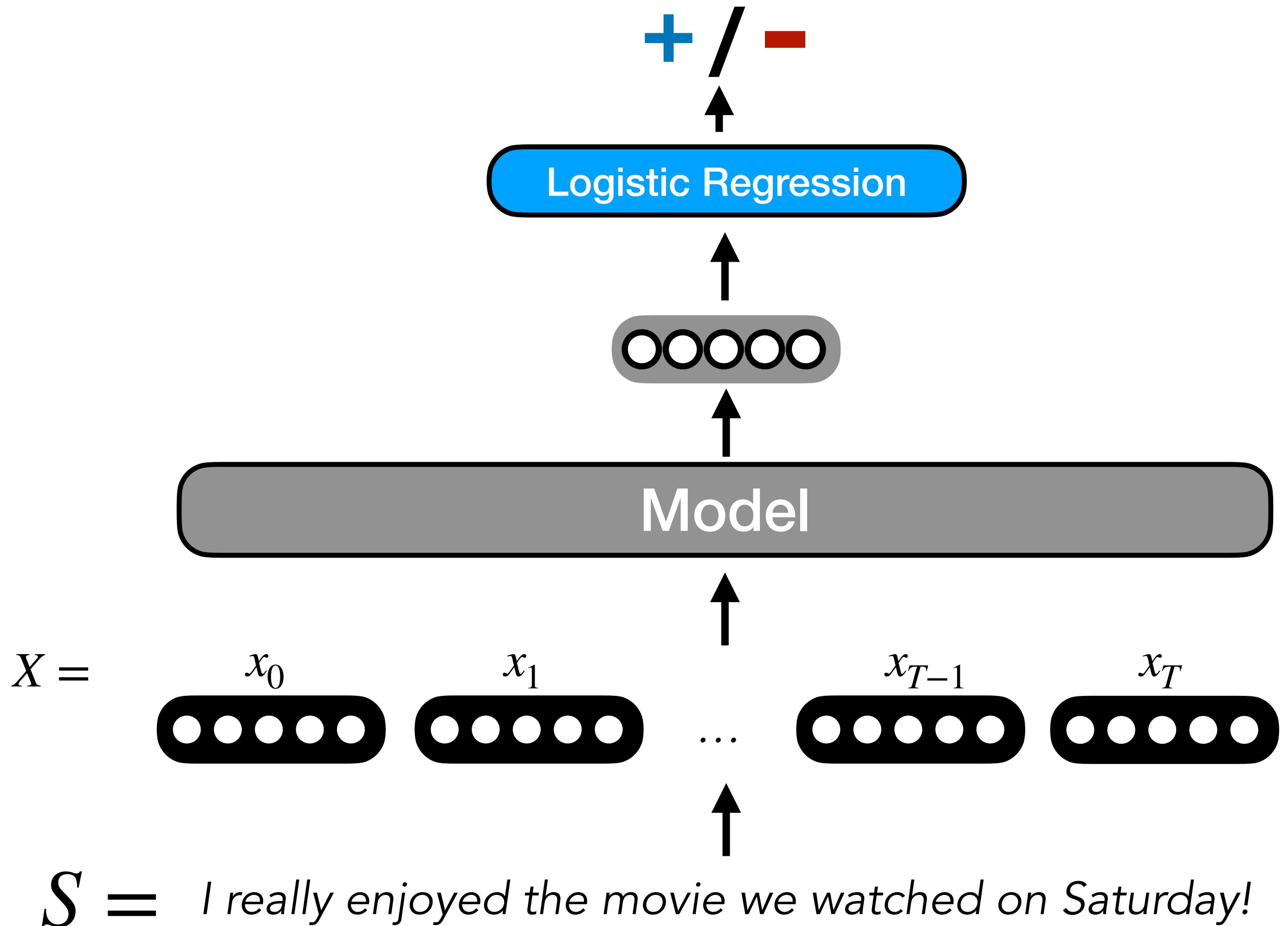
# Learn embeddings from the task!



Learn using **backpropagation**:  
compute gradients of loss with  
respect to initial embeddings  $X$

Learn embeddings that allow you  
to do the task successfully!

# Learn embeddings from the task!



- Supervised learning with a task-specific objective
  - Learn word embeddings that help complete the task
- **Q: Downsides of learning embeddings this way?**
  - Data scarcity (clean labeled data is expensive to collect)
  - Embeddings are optimised for this task — maybe not others!

# Question

**What could be a better way to learn word embeddings?**

# Self-supervised learning

“You shall know a word by the company it keeps”

*–J.R. Firth, 1957*

# Context Representations

**Solution:**

**Rely on the context in which words occur to learn their meaning**

Context is the **set of words** that occur **nearby**

*I really enjoyed the \_\_\_\_ we watched on Saturday!*

*The \_\_\_\_ growled at me, making me run away.*

*I need to go to the \_\_\_\_ to pick up some dinner.*

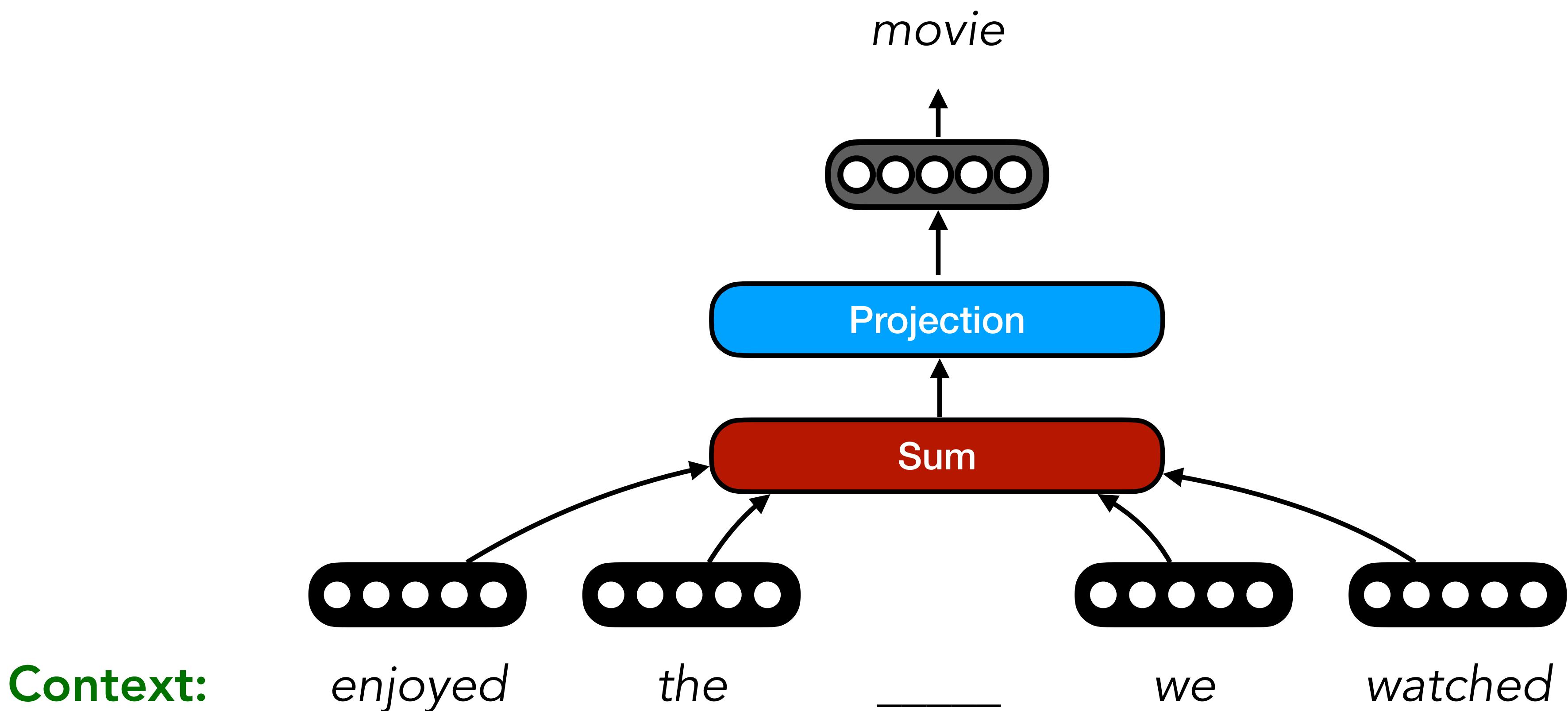
**Foundation of distributional semantics**

# Learning Word Embeddings

- Many options, huge area of research, but three standard approaches
- **Word2vec - Continuous Bag of Words (CBOW)**
  - Learn to predict missing word from surrounding window of words
- **Word2vec - Skip-gram**
  - Learn to predict surrounding window of words from given word
- **GloVe**
  - Learn to predict global co-occurrence statistics

# Continuous Bag of Words (CBOW)

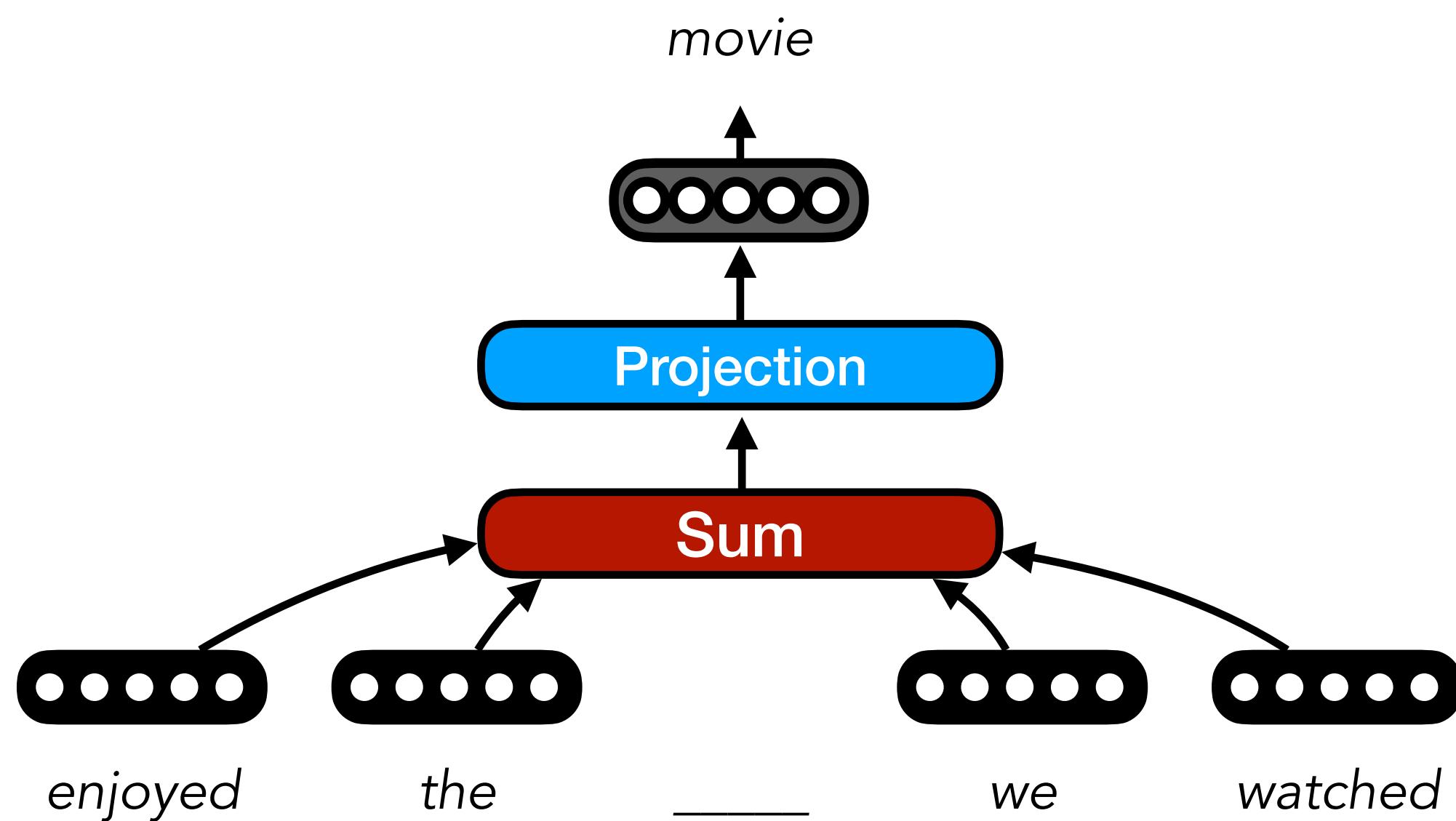
- Predict the missing word from a window of surrounding words



# Continuous Bag of Words (CBOW)

- Predict the missing word from a window of surrounding words

$$\max P(\text{movie} \mid \text{enjoyed}, \text{the}, \text{we}, \text{watched})$$

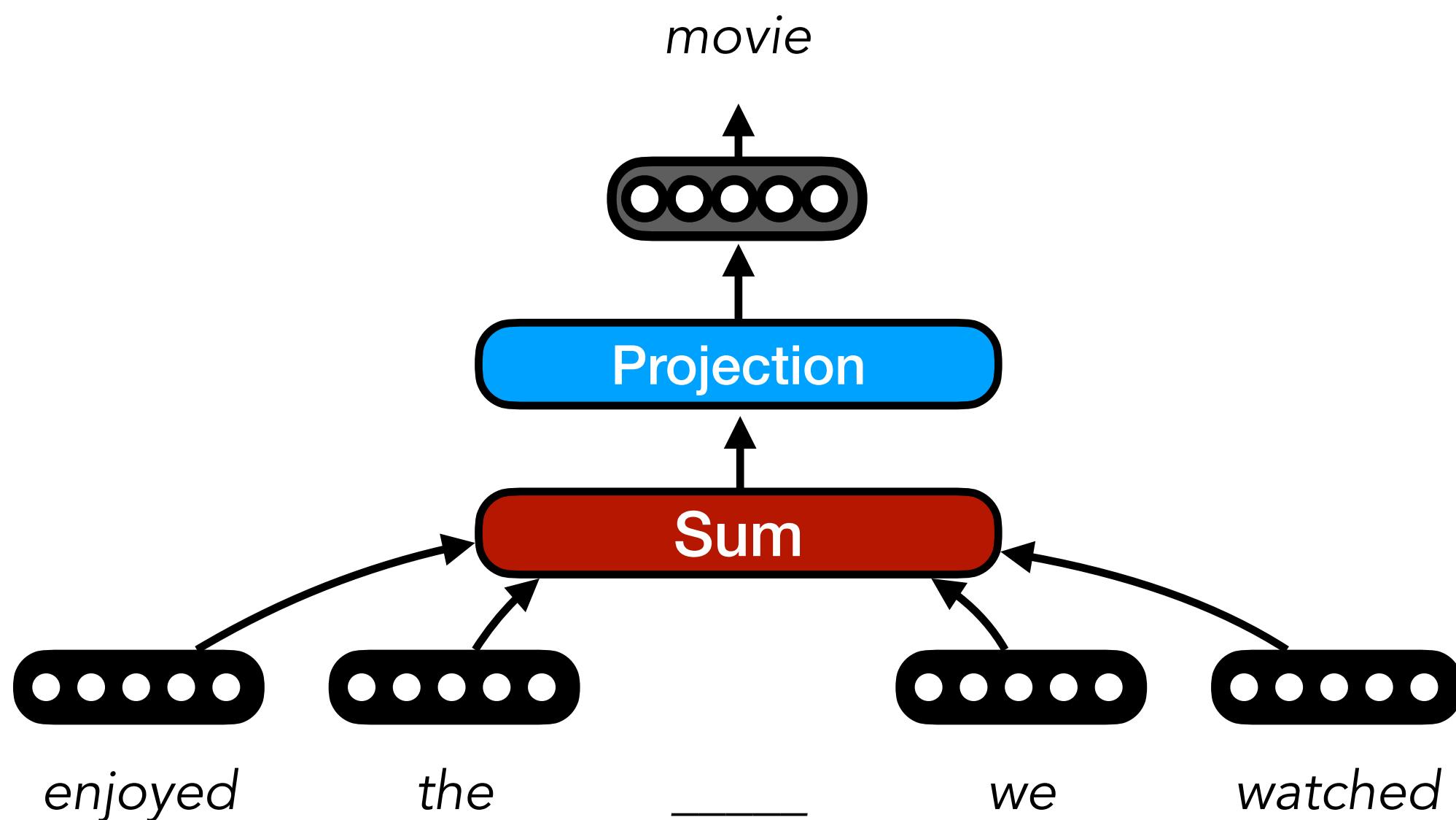


$$\max P(x_t \mid x_{t-2}, x_{t-1}, x_{t+1}, x_{t+2})$$

$$\max P(x_t \mid \{x_s\}_{s=t-2}^{s=t+2})$$

# Continuous Bag of Words (CBOW)

- Predict the missing word from a window of surrounding words



$$P(x_t | \{x_s\}_{s=t-2}^{s=t+2}) = \text{softmax}\left(\mathbf{U} \sum_{\substack{s=t-2 \\ s \neq t}}^{t+2} \mathbf{x}_s\right)$$

$$\mathbf{x}_s \in \mathbb{R}^{1 \times d}$$

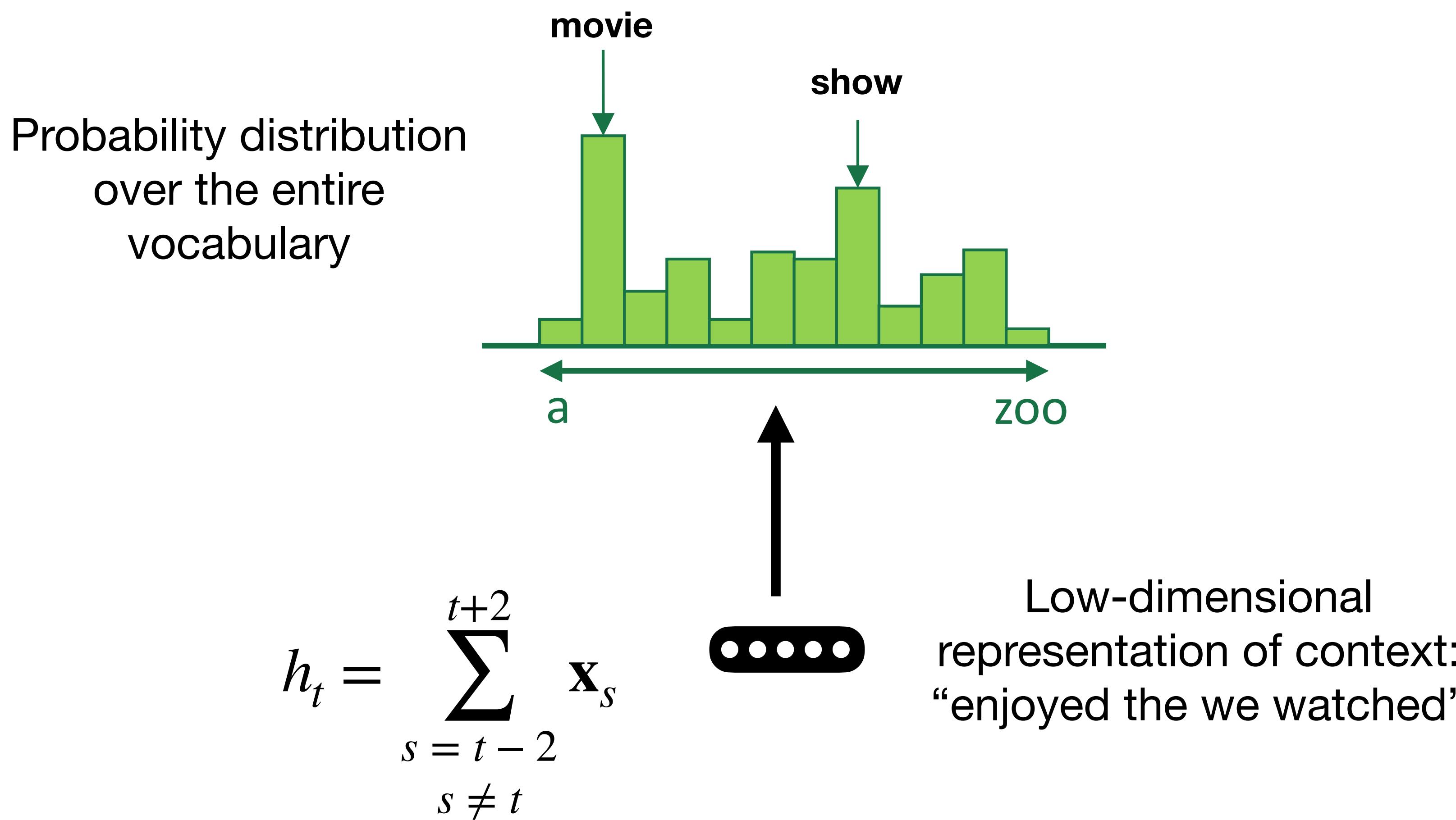
$$\dots$$

$$\mathbf{U} \in \mathbb{R}^{d \times V}$$

Projection

# Vocabulary Space Projection

$P(w_i | \text{vector for "enjoyed the we watched"})$



Let's say our output vocabulary consists of just four words: "movie", "show", "book", and "shelf".

$$h_t = \sum_{\substack{s=t-2 \\ s \neq t}}^{t+2} \mathbf{x}_s \quad \dots$$

Low-dimensional representation of context:  
"enjoyed the we watched"

Let's say our output vocabulary consists of just four words: "movie", "show", "book", and "shelf".

movie show book shelf  
 $<0.6, 0.2, 0.1, 0.1>$

We want to get a probability distribution over these four words



Low-dimensional representation of context:  
"enjoyed the we watched"

Let's say our output vocabulary consists of just four words: "movie", "show", "book", and "shelf".

$$\mathbf{U} = \begin{Bmatrix} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{Bmatrix}$$

first, we'll project our 3-d context representation to 4-d with a matrix-vector product

$$h_t = <-2.3, 0.9, 5.4>$$



Here's an example 3-d prefix vector

# How do we get there?

$$\mathbf{U} = \begin{Bmatrix} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{Bmatrix}$$

$$h_t = <-2.3, 0.9, 5.4>$$

intuition: each dimension of  $h_t$  corresponds to a *feature* of the context

# How do we get there?

$$\mathbf{U} = \left\{ \begin{array}{l} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{array} \right\}$$

movie  
show  
book  
shelf

intuition: each row of **U** contains *feature weights* for a corresponding word in the vocabulary

$$h_t = <-2.3, 0.9, 5.4>$$

intuition: each dimension of  $h_t$  corresponds to a *feature* of the context

$$\mathbf{U}h_t = \langle 1.8, -11.9, 12.9, -8.9 \rangle$$

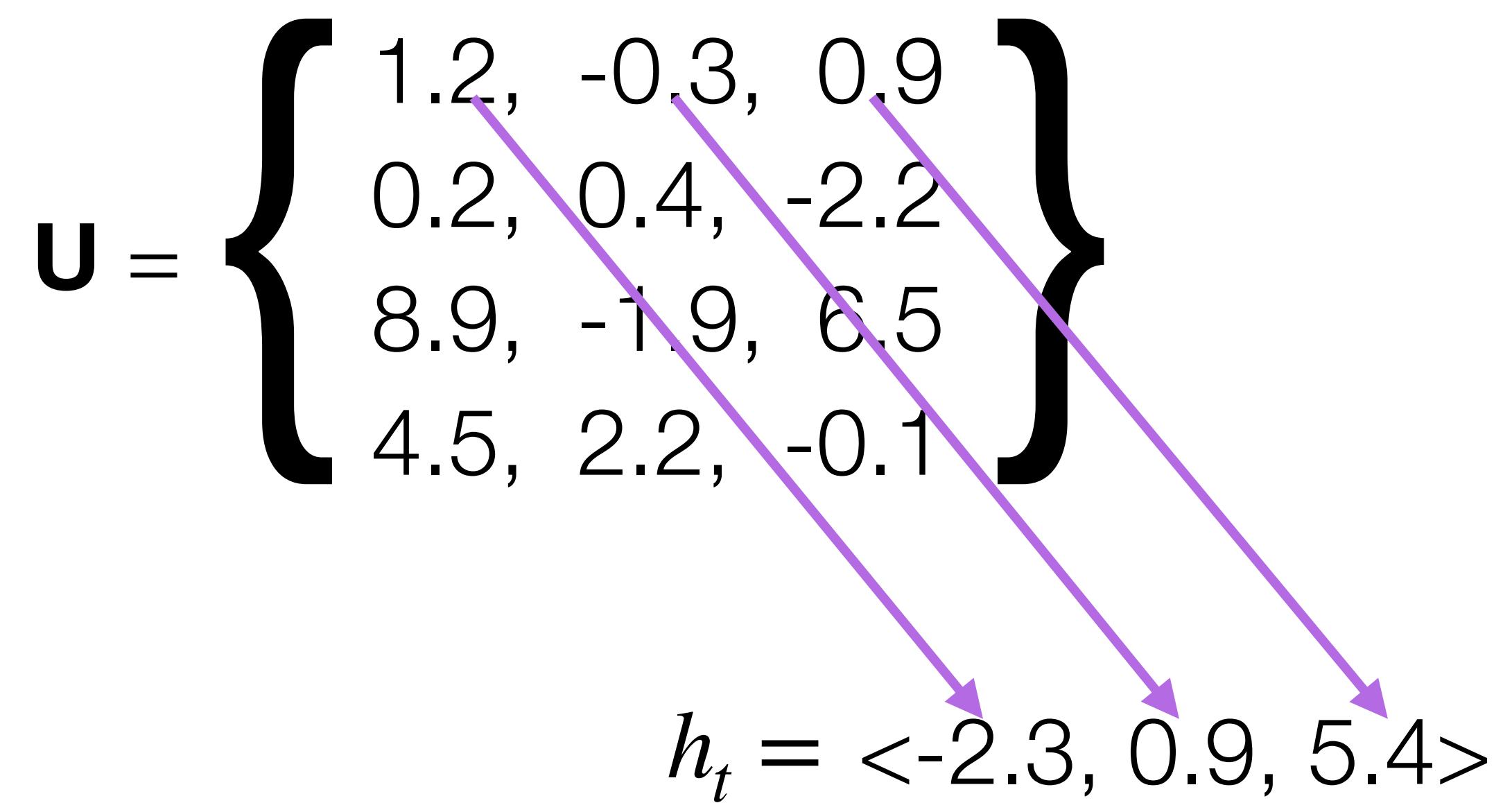
How did we compute this?  
It's just the dot product of  
each row of  $\mathbf{U}$  with  $h_t$

$$\mathbf{U} = \left\{ \begin{array}{l} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{array} \right\}$$

$$h_t = \langle -2.3, 0.9, 5.4 \rangle$$

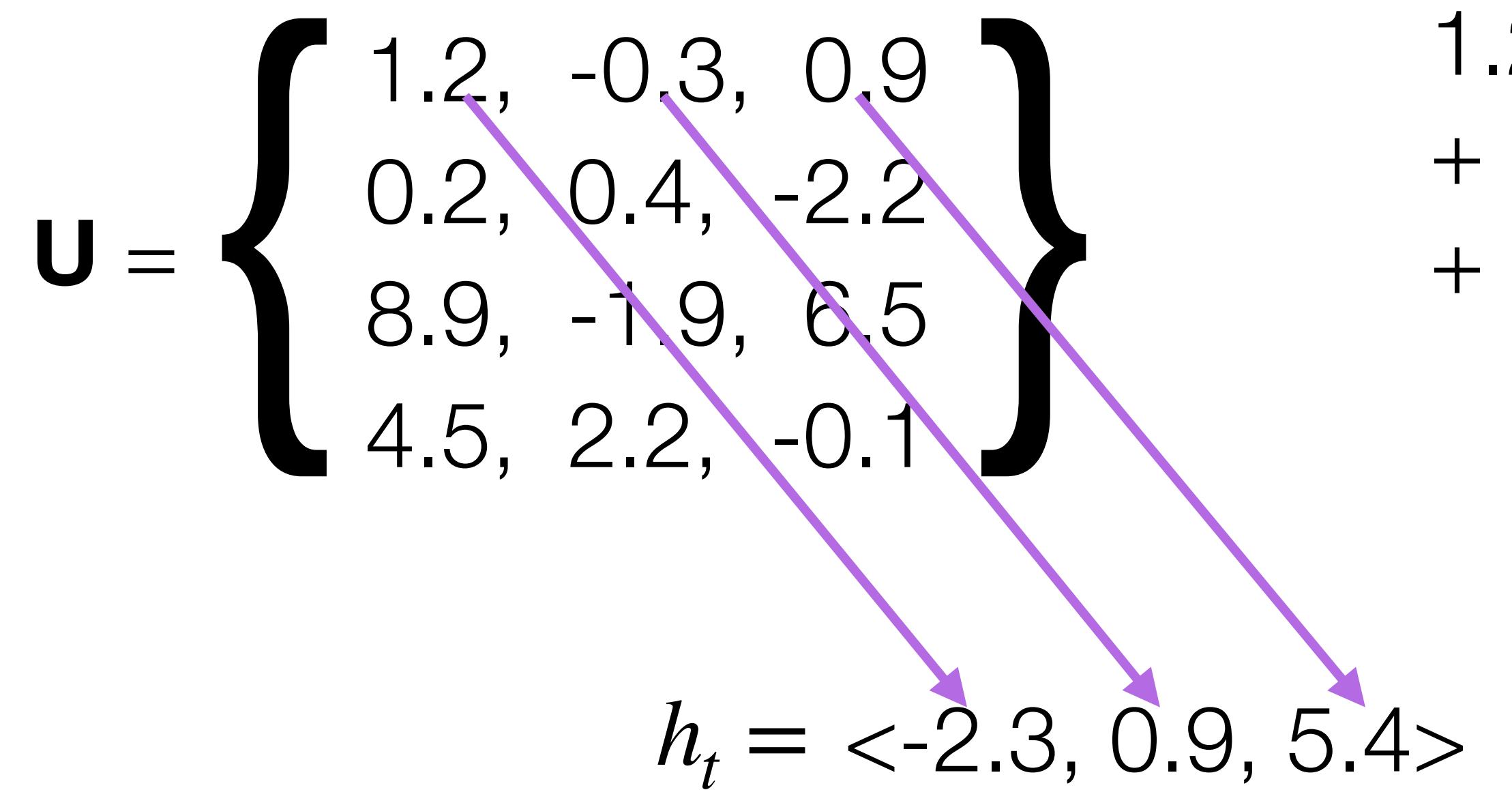
$$\mathbf{U}h_t = \langle 1.8, -11.9, 12.9, -8.9 \rangle$$

How did we compute this?  
It's just the dot product of  
each row of  $\mathbf{U}$  with  $h_t$

$$\mathbf{U} = \left\{ \begin{array}{l} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{array} \right\}$$
$$h_t = \langle -2.3, 0.9, 5.4 \rangle$$


$$\mathbf{U}h_t = \langle 1.8, -11.9, 12.9, -8.9 \rangle$$

How did we compute this?  
It's just the dot product of  
each row of  $\mathbf{U}$  with  $h_t$

$$\mathbf{U} = \left\{ \begin{array}{l} 1.2, -0.3, 0.9 \\ 0.2, 0.4, -2.2 \\ 8.9, -1.9, 6.5 \\ 4.5, 2.2, -0.1 \end{array} \right\}$$
$$h_t = \langle -2.3, 0.9, 5.4 \rangle$$


$$\begin{aligned} & 1.2 * -2.3 \\ & + -0.3 * 0.9 \\ & + 0.9 * 5.4 \end{aligned}$$

# Softmax

- The **softmax** function generates a probability distribution from the elements of the vector it is given

$$\text{softmax}(\mathbf{a})_i = \frac{e^{a_i}}{\sum_{j=1}^{|a|} e^{a_j}}$$

- $\mathbf{a}$  is a vector
- $a_i$  is dimension  $i$  of  $\mathbf{a}$
- each dimension  $i$  of the softmaxed output represents the probability of class  $i$

# Softmax

- The **softmax** function generates a probability distribution from the elements of the vector it is given

$$\text{softmax}(\mathbf{a})_i = \frac{e^{a_i}}{\sum_{j=1}^{|a|} e^{a_j}}$$

- $\mathbf{a}$  is a vector
- $a_i$  is dimension  $i$  of  $\mathbf{a}$
- each dimension  $i$  of the softmaxed output represents the probability of class  $i$

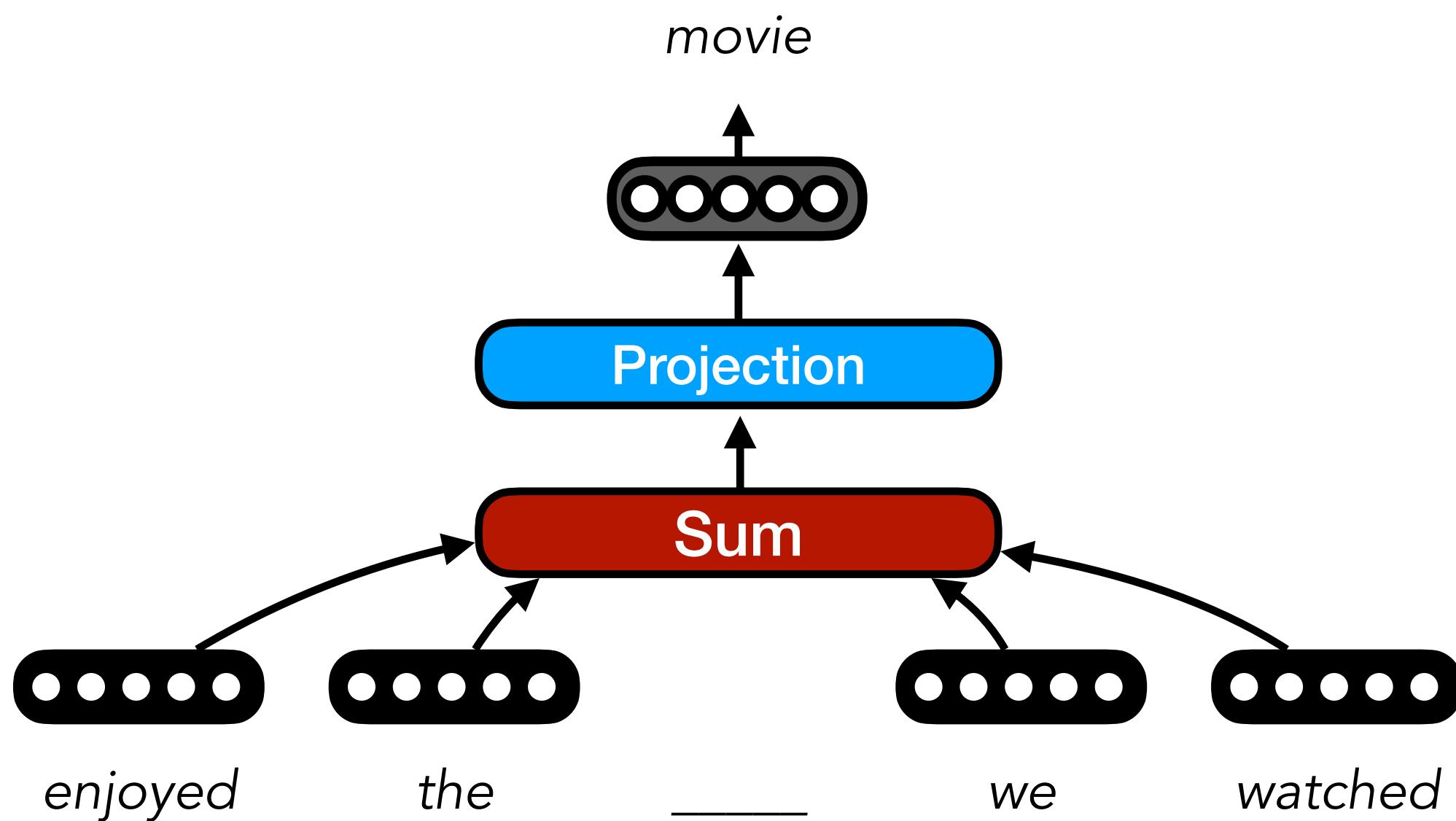
$$\mathbf{U}h_t = <1.8, -1.9, 2.9, -0.9>$$

$$\text{softmax}(\mathbf{U}h_t) = <0.24, 0.006, 0.73, 0.02>$$

Softmax will keep popping up, so be sure to understand it!

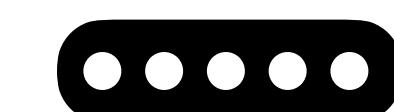
# Continuous Bag of Words (CBOW)

- Predict the missing word from a window of surrounding words



$$P(x_t | \{x_s\}_{s=t-2}^{s=t+2}) = \text{softmax}\left(\mathbf{U} \sum_{\substack{s=t-2 \\ s \neq t}}^{t+2} \mathbf{x}_s\right)$$

$$\mathbf{x}_s \in \mathbb{R}^{1 \times d}$$

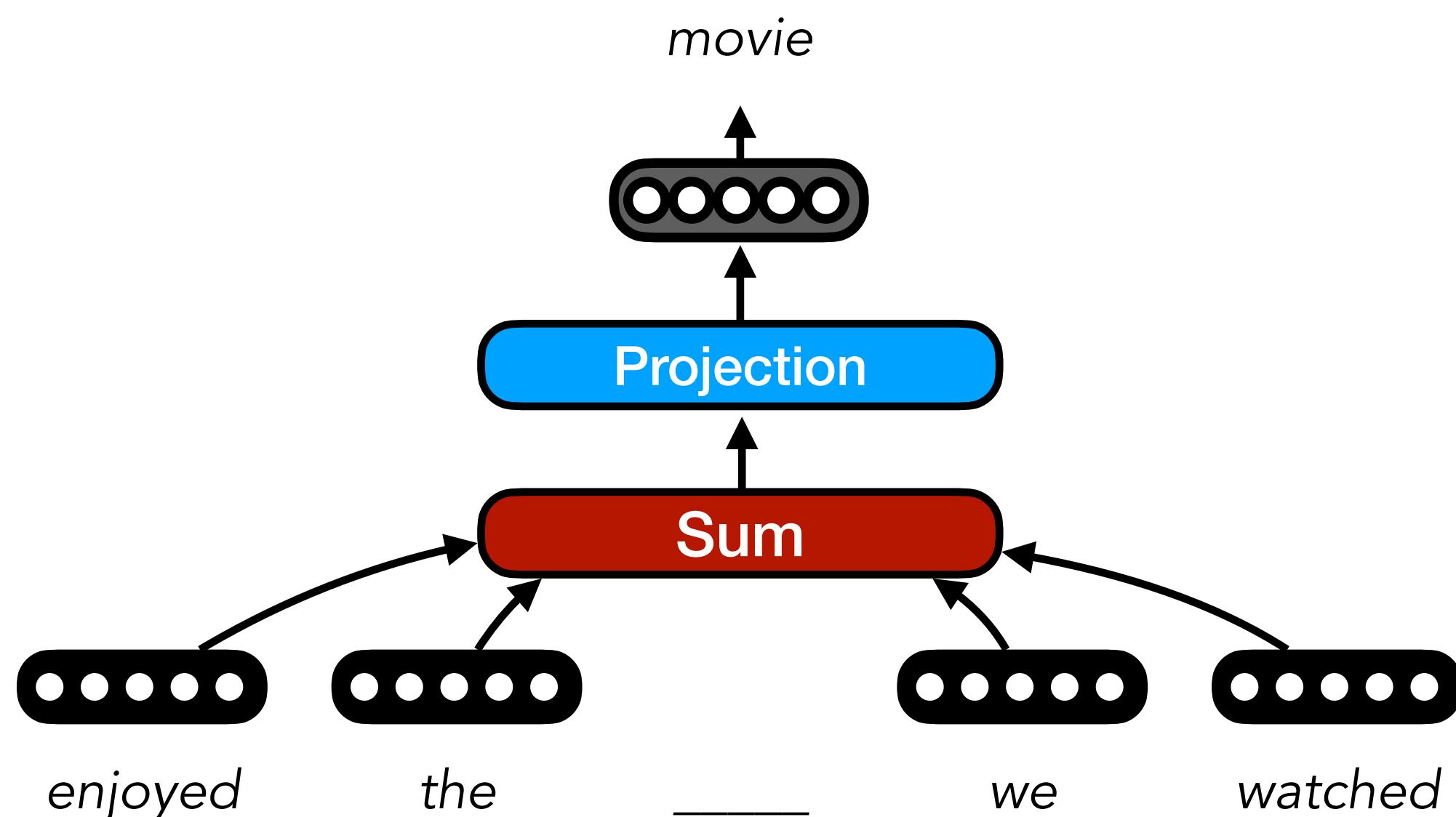


$$\mathbf{U} \in \mathbb{R}^{d \times V}$$

Projection

# Continuous Bag of Words (CBOW)

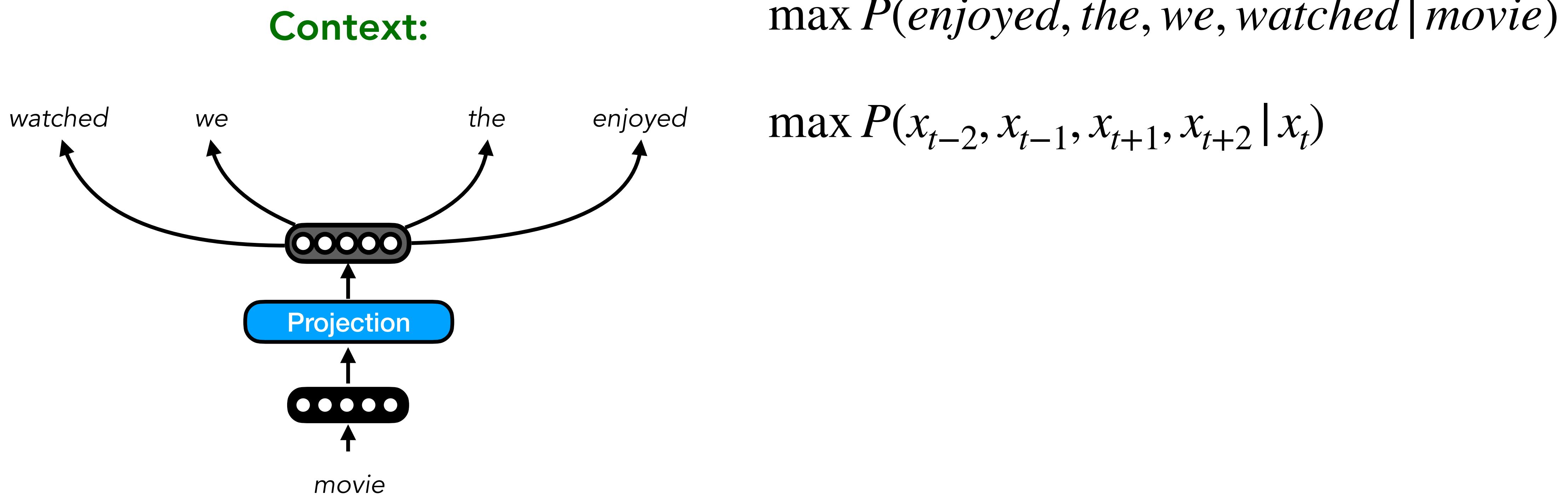
$$P(x_t | \{x_s\}_{s=t-2}^{s=t+2}) = \text{softmax} \left( \mathbf{U} \sum_{\substack{s=1 \\ s \neq t}}^{t+2} \mathbf{x}_s \right)$$



- Model is trained to **maximise** the **probability** of the missing word
  - For computational reasons, the model is typically trained to **minimise** the **negative log probability** of the missing word
- Here, we use a window of **N=2**, but the window size is a **hyperparameter**
- For computational reasons, a **hierarchical softmax** used to compute distribution (Eisenstein, 14.5.3)

# Skip-gram

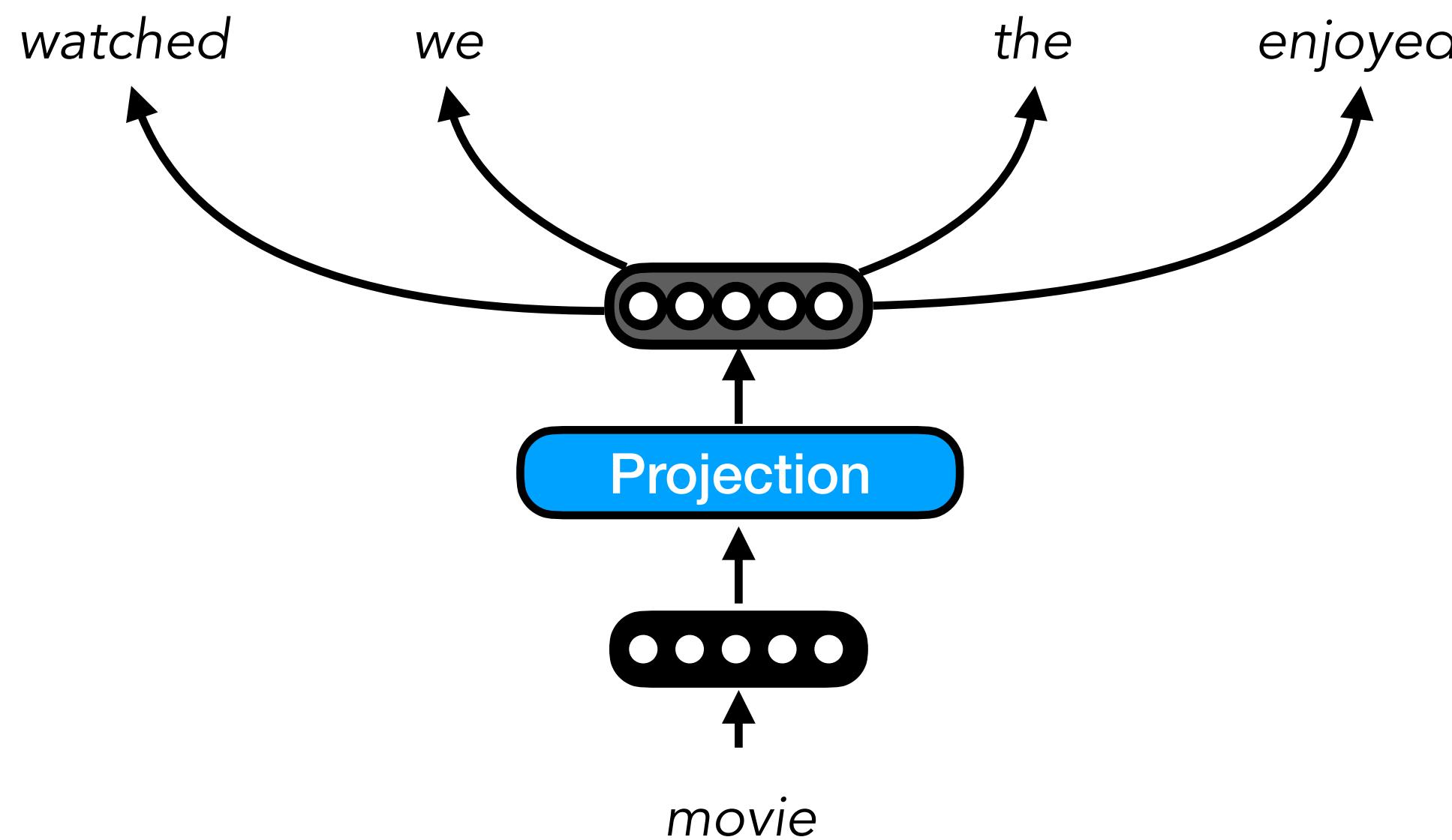
- We can also learn embeddings by predicting the surrounding context from a single word



# Skip-gram

- We can also learn embeddings by predicting the surrounding context from a single word

**Context:**



$$\max P(\text{enjoyed}, \text{the}, \text{we}, \text{watched} | \text{movie})$$

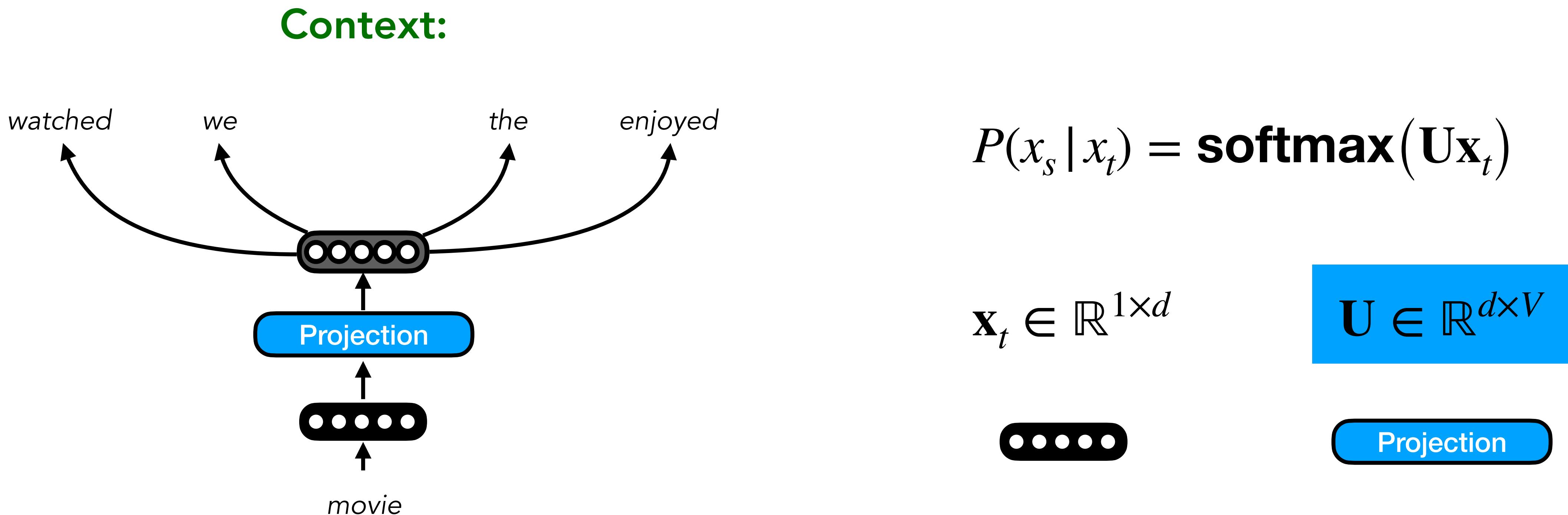
$$= \max P(x_{t-2}, x_{t-1}, x_{t+1}, x_{t+2} | x_t)$$

$$= \max \log P(x_{t-2}, x_{t-1}, x_{t+1}, x_{t+2} | x_t)$$

$$\begin{aligned} &= \max \left( \log P(x_{t-2} | x_t) + \log P(x_{t-1} | x_t) \right. \\ &\quad \left. + \log P(x_{t+1} | x_t) + \log P(x_{t+2} | x_t) \right) \end{aligned}$$

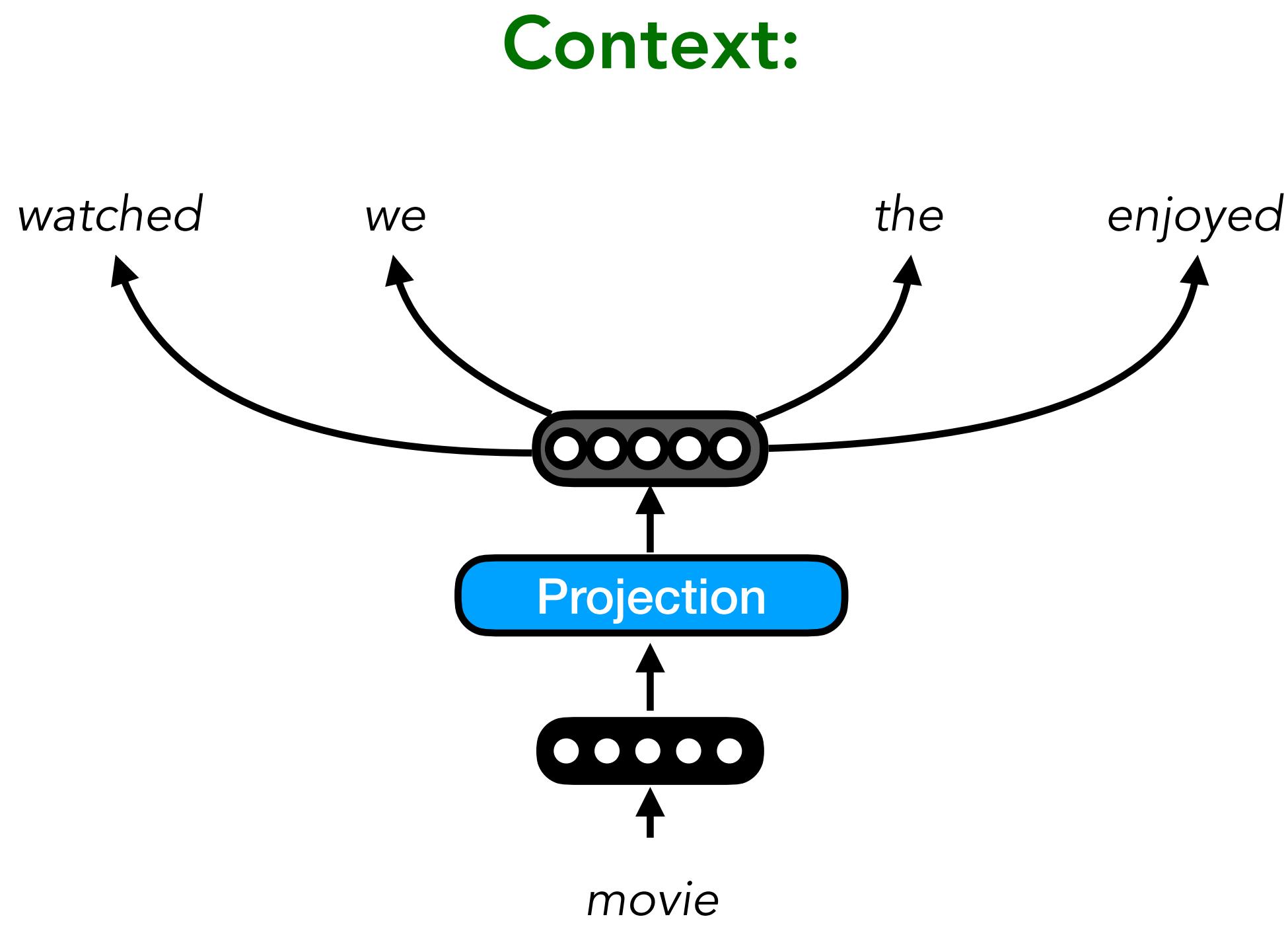
# Skip-gram

- We can also learn embeddings by predicting the surrounding context from a single word



# Skip-gram

- We can also learn embeddings by predicting the surrounding context from a single word



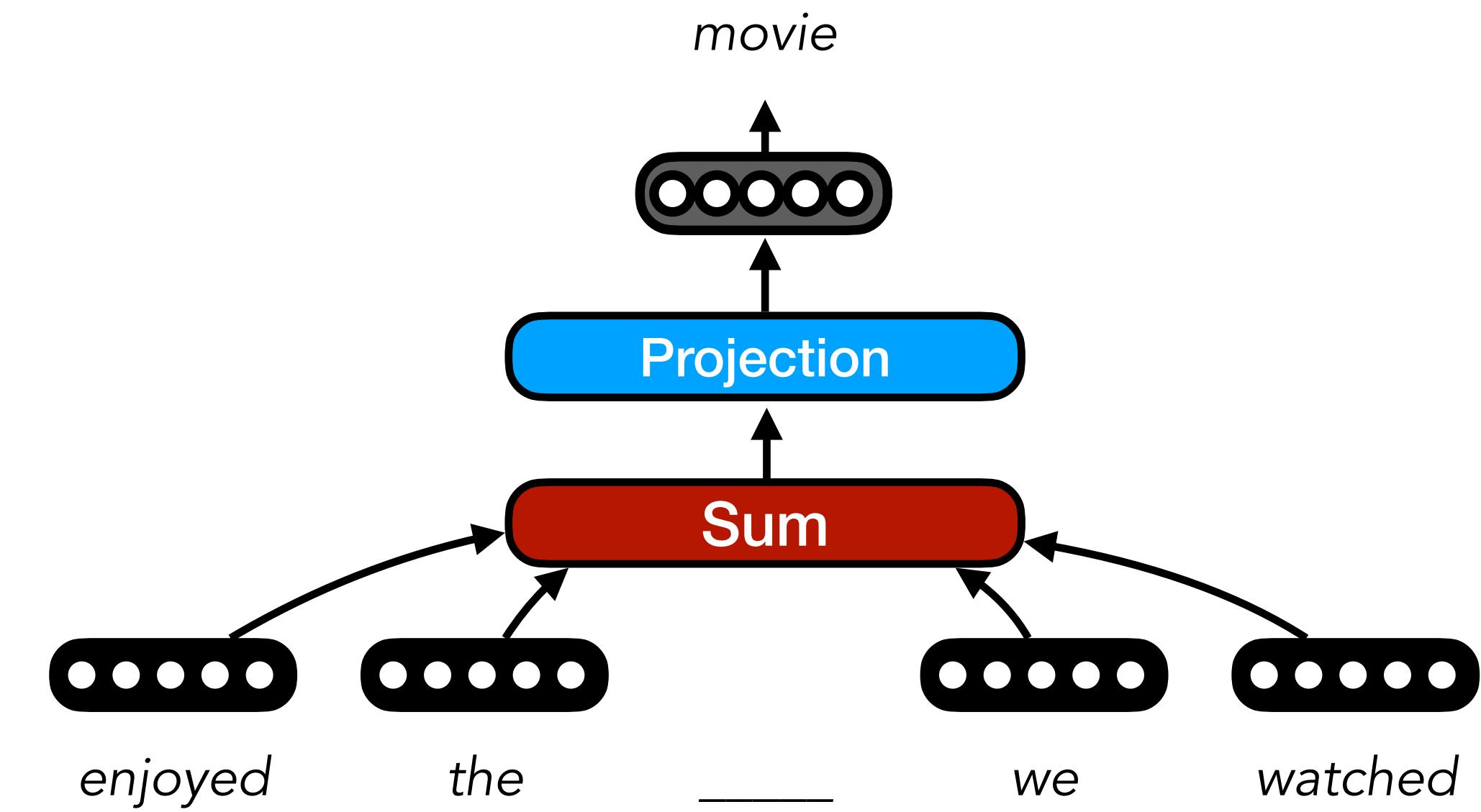
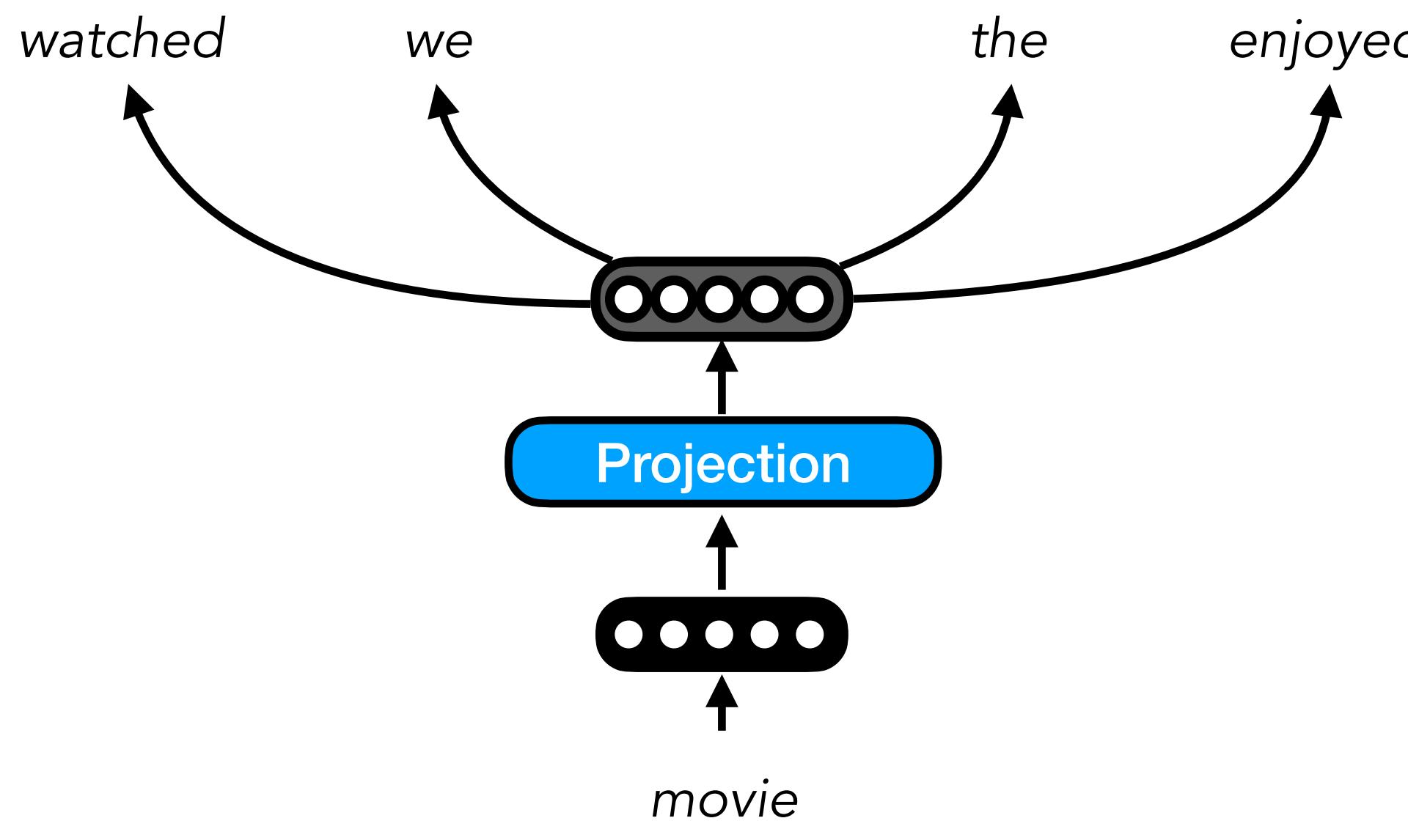
- Model is trained to **minimise the negative log probability** of the surrounding words
- Here, we use a window of **N=2**, but the window size is a **hyperparameter**.
  - Larger window = more information about related words in embedding
- Typically, set large window (**N=10**), but randomly select  $i \in [1, N]$  as dynamic window size so that closer words contribute more to learning

# Question

**What is the major conceptual difference between the CBOW and Skipgram methods for training word embeddings?**

# Skip-gram vs. CBOW

- **Question:** Do you expect a difference between what is learned by CBOW and Skipgram methods?



# Example

## CBOW

```
[ ] top_cbow = cbow.wv.most_similar('cut', topn=10)

print(tabulate(top_cbow, headers=["Word", "Similarity"],
```

Word	Similarity
slice	0.662173
crosswise	0.650036
score	0.630569
tear	0.618827
dice	0.563946
lengthwise	0.557231
cutting	0.557228
break	0.551517
chop	0.541566
carve	0.537967

## Skip-gram

```
[ ] top_sg = skipgram.wv.most_similar('cut', topn=10)

print(tabulate(top_sg, headers=["Word", "Similarity"],
```

Word	Similarity
crosswise	0.72921
score	0.702693
slice	0.696898
crossways	0.680091
1/2-inch-thick	0.678496
diamonds	0.671814
diagonally	0.670319
lengthwise	0.665378
cutting	0.66425
wise	0.656825

# Question

**What do Skipgram and CBOW have in common ?**

**They both learn word representations from predicting  
many local context windows around those words.**

**Can we do something else?**

# GloVe: Global Vectors

- **Problem:** Skip-gram and CBOW optimize local prediction objective and never explicitly model global corpus co-occurrence statistics.
- **Solution:** Build a global word–context co-occurrence matrix  $\mathbf{X} \in \mathbb{R}^{V \times V}$  and learn embeddings that approximate log co-occurrence counts.

$$\min \sum_{i,j} f(X_{i,j}) \left( w_i^T w_j + b_i + b_j - \log X_{ij} \right)^2$$

In GloVe, embeddings are learned s.t. their dot products approximate log co-occurrence counts.

—> **Embedding differences encode probability ratios, which capture semantic distinctions (Firth)**

# Other Resources of Interest

- **FastText** Embeddings (Bojanowski et al., 2017; Mikolov et al., 2018)
  - Enhancement of Skip-gram model that handles morphology
  - Divide words into character n-grams of size  $n$  — <where> = <wh, whe, her, ere, re>
- Retrofitting word vectors to semantic lexicons (Faruqui et al., 2014)
  - Training word vectors to encode relationships (e.g., synonymy) from high-level semantic resources: WordNet, PPDB, and FrameNet

- S: (n) **sofa**, couch, lounge (an upholstered seat for more than one person)
  - direct hyponym / full hyponym
  - direct hypernym / inherited hypernym / sister term
    - S: (n) **seat** (furniture that is designed for sitting on)
  - derivationally related form

# Recap

- **Problem:** Learning word embeddings from scratch using labeled data for a task is data-inefficient!
- **Solution:** Word embeddings can be learned in a self-supervised manner from large quantities of raw text
- **Three main algorithms:** Continuous Bag of Words (CBOW), Skip-gram, and GloVe

# Resources

- **word2vec**: <https://code.google.com/archive/p/word2vec/>
- **GloVe**: <https://nlp.stanford.edu/projects/glove/>
- **FastText**: <https://fasttext.cc/>
- **Gensim**: <https://radimrehurek.com/gensim/>

## Download pre-trained word vectors

- Pre-trained word vectors. This data is made available under the [Public Domain Dedication and License](http://www.opendatacommons.org/licenses/pddl/1.0/) v1.0 whose full text can be found at: <http://www.opendatacommons.org/licenses/pddl/1.0/>.
  - [Wikipedia 2014 + Gigaword 5](#) (6B tokens, 400K vocab, uncased, 50d, 100d, 200d, & 300d vectors, 822 MB download): [glove.6B.zip](#)
  - Common Crawl (42B tokens, 1.9M vocab, uncased, 300d vectors, 1.75 GB download): [glove.42B.300d.zip](#)
  - Common Crawl (840B tokens, 2.2M vocab, cased, 300d vectors, 2.03 GB download): [glove.840B.300d.zip](#)
  - Twitter (2B tweets, 27B tokens, 1.2M vocab, uncased, 25d, 50d, 100d, & 200d vectors, 1.42 GB download): [glove.twitter.27B.zip](#)
- Ruby [script](#) for preprocessing Twitter data

# References

- Firth, J.R. (1957). A Synopsis of Linguistic Theory, 1930-1955.
- Mikolov, T., Chen, K., Corrado, G.S., & Dean, J. (2013a). Efficient Estimation of Word Representations in Vector Space. *International Conference on Learning Representations*.
- Mikolov, T., Sutskever, I., Chen, K., Corrado, G.S., & Dean, J. (2013b). Distributed Representations of Words and Phrases and their Compositionality. *ArXiv*, abs/1310.4546.
- Pennington, J., Socher, R., & Manning, C.D. (2014). GloVe: Global Vectors for Word Representation. *Conference on Empirical Methods in Natural Language Processing*.
- Bojanowski, P., Grave, E., Joulin, A., & Mikolov, T. (2017). Enriching word vectors with subword information. *Transactions of the association for computational linguistics*.
- Mikolov, T., Grave, E., Bojanowski, P., Puhrsch, C., & Joulin, A. (2018). Advances in pre-training distributed word representations. *International Conference on Language Resources and Evaluation*.