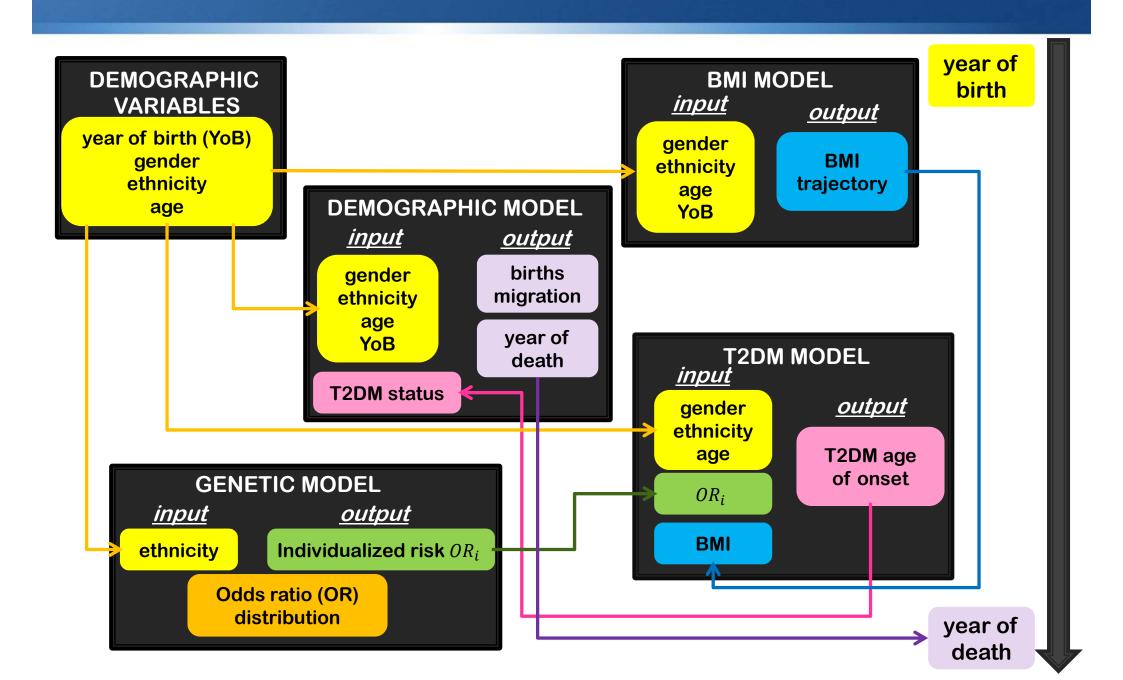


Thao Phan

OVERVIEW OF DEMOS



DEMOGRAPHIC DATA

SINGSTAT published data (1990-2010)

- Census
- Number of residents by 5-year age groups, race and sex
- Mortality rates and fertility rates by 5-year age groups
- Life-table (2003-2010)
- Number of deaths (including foreigners)
- TFR in 3 main races
- Crude birth and death rates by race

MORTALITY SUBMODEL

For age 0-84 (IMPROVED MODEL)

Lee-Carter model

$$\tau_{g,a}(t) = \tau_{g,a}(t-1) + \delta_t \times \gamma_a$$

Assume that γ_a is the same within each 5-year age group and δ_t is random walk with drift

MORTALITY SUBMODEL

For older age (a>85)

Coale-Kisker extrapolation method:

$$\kappa_{g,a} = \tau_{g,a}(0) - \tau_{g,a-1}(0)$$

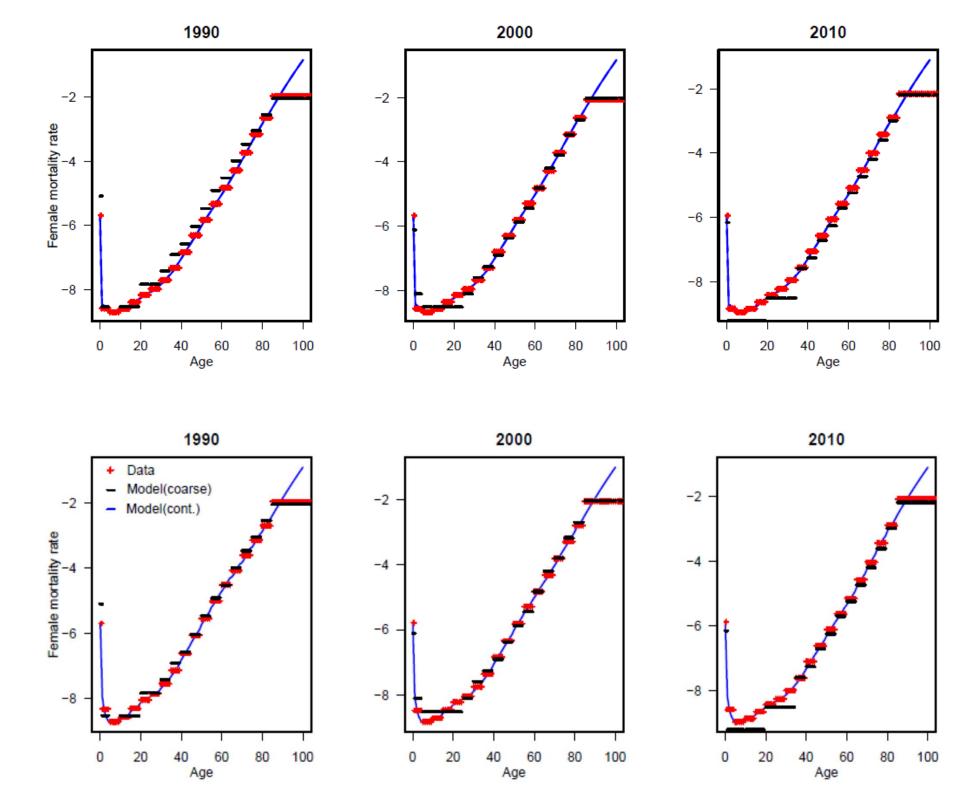
$$\kappa_{g,a+1} = \kappa_{g,a} - R_g$$

Solving for R yields:

$$R_g = \frac{36 \times \kappa_{g,84} + \tau_{g,84}(0) - \tau_{g,120}(0)}{666}$$

Replace $\kappa_{g,84}$ with moving average of $\kappa_{g,82}$ to $\kappa_{g,86}$

$$R_g = \frac{\frac{37}{5} \times (\kappa_{82} + \kappa_{83} + 3 \times \kappa_{84}) + ln\left(\frac{\mu_{g,82}(0) + \mu_{g,83}(0) + \mu_{g,84}(0)}{3}\right) - ln(\mu_{g,120}(0))}{666 + \frac{37 \times 3}{5}}$$



Race-specific mortality rate

Proportional to mortality rate of total population

$$\mu_{g,a}^{r}(t) = e^{\theta_{\mu,r}} \times \mu_{g,a}(t)$$

With $\theta_{\mu,Chi} = 0$; $\theta_{\mu,Mal} \sim N(0.33, 0.25)$;

 $\theta_{\mu,Ind} \sim N(0.87, 0.23)$ (informative prior from

literature (Ma et al. 2003))

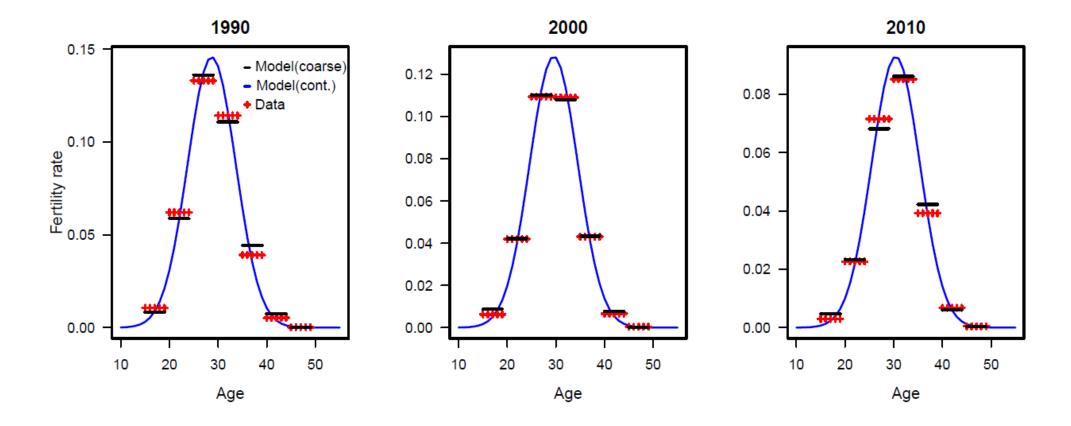
FERTILITY SUBMODEL

Gaussian function with linear trend on peak age

$$f_a(t) = \theta_2 \times \left(\sum_{i=1}^t \theta_{3,i}\right) \times \frac{1}{\sqrt{2 \times \pi \times \sigma_f^2}} \times e^{\left(\frac{-[a-\mu+\theta_1\times(t-1)]^2}{2\times\sigma_f^2}\right)}$$

Secular trend on scale $\theta_{3,t}$ is random walk with drift

FERTILITY SUBMODEL



MIGRATION SUBMODEL

<u>Alternative model</u> – simplified migration schedule

$$m(x) = a_1 \times e^{-\alpha_1 x} + a_2 \times e^{-\alpha_2 (x-\mu) - e^{-\lambda_2 (x-\mu)}} + c$$

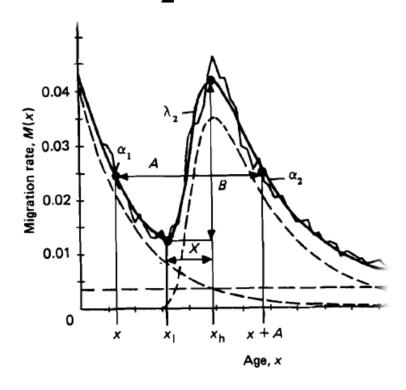
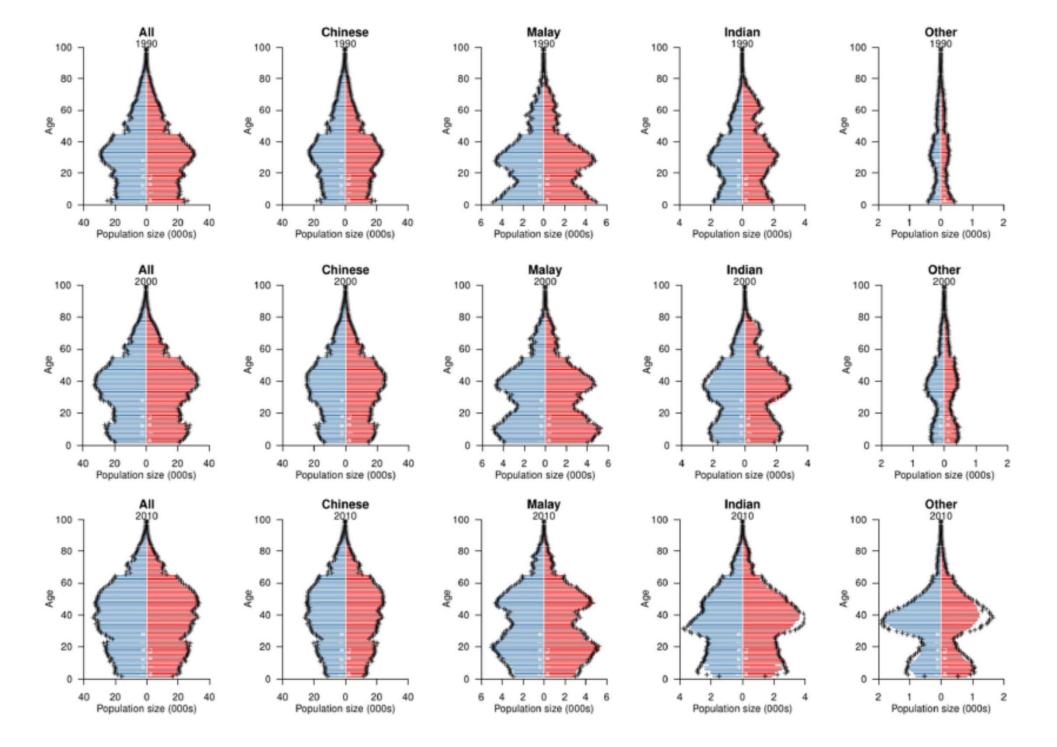
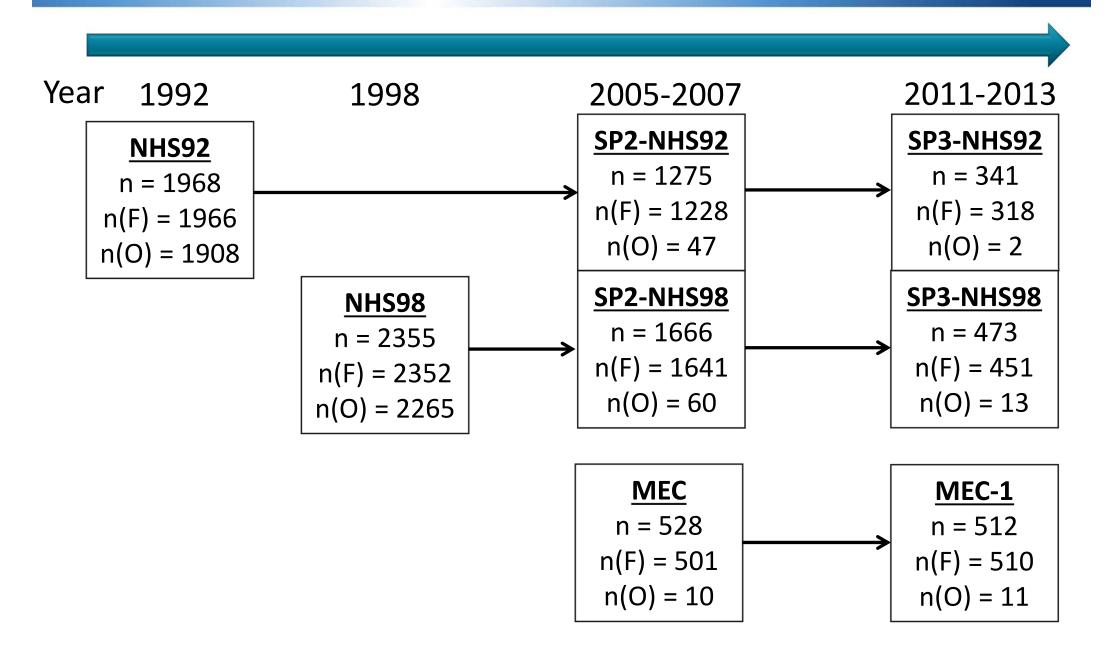


FIGURE 4 The model migration schedule.

Source from Roger & Castro (1981)

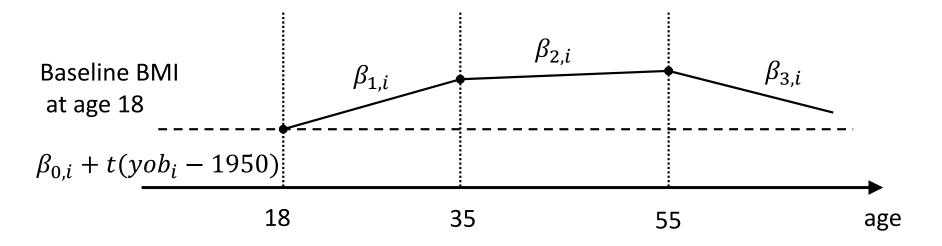


DATA



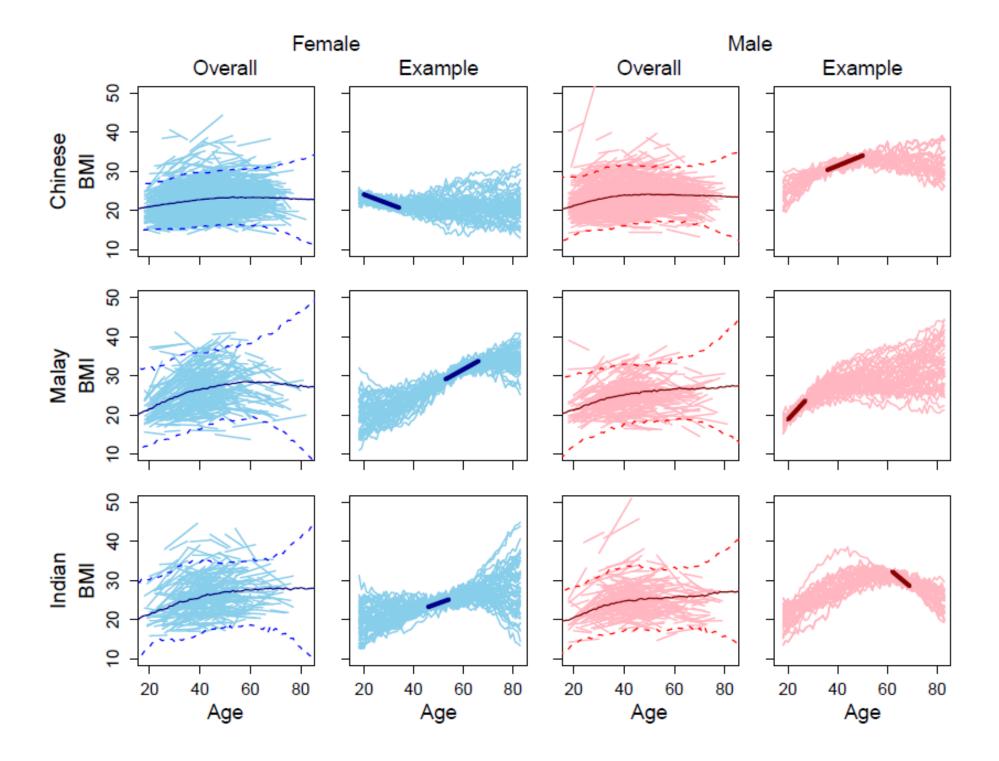
BMI trajectory

BMI model For each race and gender combination, we have:



Individual parameters $(\beta_{0,i}, \beta_{1,i}, \beta_{2,i}, \beta_{3,i})$ are derived from multivariate normal distribution:

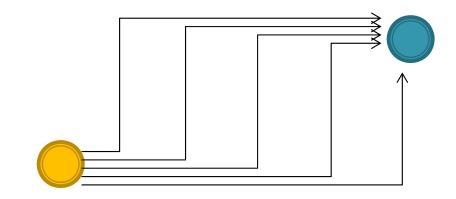
$$\begin{pmatrix} \beta_{0,i} \\ \beta_{1,i} \\ \beta_{2,i} \\ \beta_{3,i} \end{pmatrix} \sim \text{MVN} \begin{pmatrix} \varphi_0 \\ \varphi_1 \\ \varphi_2 \\ \varphi_3 \end{pmatrix}$$



The diabetes model

Annual risk of developing (cryptic) DM, depends on:

- age
- race, sex
- genetic risk
- BMI that year



Estimated from longitudinal data

Corrected DM status accounts for differing tests

