Assignment Discrete Mathematics

MANAS KHANNA

April 10, 2025



SUBMITTED TO Dr. SANJAY KUMAR ASET, AMITY UNIVERSITY MOHALI SUBMITTED BY MANAS KHANNA B.TECH.-4th SEM A25305223002

1 Problem 1

The college catering service must decide if the mix of food that is supplied for receptions is appropriate. Of the 100 people questioned, 37 say they eat fruits, 33 say they eat vegetables, 9 say they eat cheese and fruits, 12 eat cheese and vegetables, 10 eat fruits and vegetables, 12 eat only cheese, and 3 report they eat all three offerings. How many people surveyed eat cheese? How many do not eat any of the offerings?

2 Problem 2

Solve the recurrence relation:

$$a_n = 7a_{n-2} + 6a_{n-3}, a_1 = 3, a_2 = 6, a_3 = 10$$

3 Problem 3

3.1 Determine values of the constants A and B such that $a_n = An + B$ is a solution of recurrence relation

$$a_n = 2a_{n-1} + n + 5$$

- 3.2 Find all solutions of this recurrence relations
- 3.3 Find the solution of this recurrence relation if $a_0 = 4$

4 Problem 4

By mathematical induction, show that $7^n - 2^n$ is divisible by 5 for all $n \in \mathbb{N}$