CAS AMSS-PolyU Joint Laboratory of Applied Mathematics Workshop 2022

December 22-23, 2022 (Zoom)

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About

CAS AMSS-PolyU Joint Laboratory of Applied Mathematics Workshop

This workshop is organized by CAS AMSS-PolyU Joint Laboratory of Applied Mathematics¹ and supported by AMSS, PolyU, AMA and CAS-Croucher Funding Scheme for Joint Laboratories.

- * CAS: Chinese Academy of Sciences
- * AMSS: Academy of Mathematics and Systems Science
- * PolyU: The Hong Kong Polytechnic University
- * AMA: Department of Applied Mathematics, PolyU

¹ The AMSS-PolyU Joint Research Institute (JRI) for Engineering and Management Mathematics was jointly established by the AMSS and PolyU in 2005. Approved by CAS, the JRI has upgraded to one of 22 CAS joint laboratories with Hong Kong universities in 2019 and named CAS AMSS-PolyU Joint Laboratory of Applied Mathematics (JLab). JLab website: https://www.polyu.edu.hk/ama/research-and-consultancy/cas-amss-polyu-jlab/.

Thursday, 22 December

09:00-09:15	Welcome Remarks	Chair: Defeng Sun (PolyU)		
	Ya-xiang Yuan AMSS	Speech		
	Xiaojun Chen PolyU	Speech		
09:15-11:45 Session 1: Differential Equations Chair: Zhonghua Qiao (PolyU)				
09:15	Fanghua Lin New York University	TBA		
10:00	Coffee Break			
10:15	Ping Zhang AMSS	Gevrey Solutions of Quasi-linear Hyperbolic Hydrostatic Navier-Stokes System		
11:00	Tong Yang PolyU	Analysis on Tollmien-Schlichting Waves in MHD and Compressible Fluid		
14:30-17:00 Session 2: Mathematical Finance Chair: Zhan Shi (AMSS)				
4:30	Min Dai PolyU	Strategic Investment under Uncertainty with First-and Second-mover Advantages		
15:15	Yongsheng Song AMSS	The Central Limit Theorem and the Law of Large Numbers under Sublinear Expectations		
16:00	Coffee Break			
16:15	Nizar Touzi Ecole Polytechique	Mean Field Game of Mutual Holding and Systemic Risk		

Program

Friday, 23 December

09:15-11:45	Session 3: Statistics	Chair: Xingqiu Zhao (PolyU)			
09:15	Tengyuan Liang University of Chicago	Universal Prediction Band and Variance Interpolation via Semi-Definite Programming			
10:00	Coffee Break				
10:15	Jian Huang PolyU	Conditional Deep Generative Learning			
11:00	Xinyu Zhang AMSS	Optimal Parameter-transfer Learning by Semiparametric Model Averaging			
14:30-17:00	14:30-17:00 Session 4: Optimization Chair: Yu-Hong Dai (AMSS)				
14:30	Xin Liu AMSS	Optimization Models and Approaches for Strictly Correlated Electrons			
15:15	Houduo Qi PolyU	Euclidean Distance Matrix Optimization and Its Application to Portfolio Theory			
16:00	Coffee Break				
16:15	Daniel Kuhn Ecole Polytechique Federale de Lausanne	A General Framework for Optimal Data-Driven Optimization			
17:00-17:15	Closing				

TBA

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TBA

Gevrey Solutions of Quasi-linear Hyperbolic Hydrostatic Navier-Stokes System

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We study the well-posedness of a hyperbolic quasilinear version of hydrostatic Navier-Stokes system in $\mathbb{R} \times \mathbb{T}$, and prove the global well-posedness of the system with initial data which are small and analytic in both variables. We also prove the convergence of such analytic solutions to that of the classical hydrostatic Navier-Stokes system when the delay time converges to zero. Furthermore, we obtain a local well-posedness result in Gevrey class 2 when the initial datum is a small perturbation of some convex function.

Analysis on Tollmien-Schlichting Waves in MHD and Compressible Fluid

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In a region closer to the boundary compared to Prandtl layer, an inviscid disturbance can be manifested by the interaction with viscous mode via the no-slip boundary condition due to resonance. In some unstable range of parameters, this leads to instability in the transition regime from laminar flow to turbulence. This instability phenomenon was observed by physicists long time ago, such as Heisenberg, Tollmien and C.C. Lin, etc. And it was justified rigorously in mathematics by Grenier-Guo-Nguyen using the incompressible Navier-Stokes equation. In this talk, we will present some results on this phenomenon in other physical situations that the governing system is either MHD or compressible Navier-Stokes equation. The talk is based on some recent joint work with Chengjie Liu and Zhu Zhang.

Strategic Investment under Uncertainty with First-and Second-mover Advantages

Min Dai

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We analyze a duopoly entry game where firms trade off the first-mover advantage (of earning monopoly rents) against the second-mover advantage (of paying a lower entry cost) in the classic real-option framework. We show that the equilibrium value function is governed by a variational inequality. The equilibrium solution features five regions. There are two waiting regions due to two distinct waiting motives: a new waiting-to-save-entry-costs and the standard option-value-of-waiting motives. For sufficiently high market demand, there is no first-mover advantage in equilibrium as Follower immediately enters after Leader. Therefore, firms use mixed strategies to enter as Leader with a rate increasing in market demand, giving rise to a probabilistic entry region. For intermediate levels of market demand, firms rush to enter in the firstmover-advantage-induced "rent-equalization" region (Fudenberg and Tirole, 1985; Grenadier, 1996). Finally, a second probabilistic entry region (where Follower waits so that Leader collects some monopoly rents) emerges to connect the rent-equalization region and the waiting-to-be-the-second-mover region. Quantitatively, the secondmover advantage can cause firms to significantly delay entry and substantially erode firm value. This work is joint with Zhaoli Jiang and Neng Wang.

The Central Limit Theorem and the Law of Large Numbers under Sublinear Expectations

Yongsheng Song

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We first introduce Stein's method under sublinear expectations, by which we give convergence rates for the central limit theorem and the (weak) law of large numbers under sublinear expectations (CLT* & LLN*). Then we give a version of strong LLN* as the sublinear expectation defined on a Polish space is regular, which shows that any constant μ in the mean interval $[\underline{\mu}, \overline{\mu}]$ can be considered as a limit of the emperical averages.

Mean Field Game of Mutual Holding and Systemic Risk

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We provide an explicit solution for the mean-field game of mutual holding with defaultable agents modeled by absorption at zero. The optimal dynamics are defined by a Mckean-Vlasov SDE with a discontinuous diffusion coefficient and nonsmooth drift coefficient. We also provide an autonomous characterization of the distribution of defaults.

Universal Prediction Band and Variance Interpolation via Semi-Definite Programming

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We propose a computationally efficient method to construct nonparametric, heteroscedastic prediction bands for uncertainty quantification, with or without any user-specified predictive model. Our approach provides an alternative to the now-standard conformal prediction for uncertainty quantification, with novel theoretical insights and computational advantages. The data-adaptive prediction band is universally applicable with minimal distributional assumptions, has strong non-asymptotic coverage properties, and is easy to implement using standard convex programs. Our approach can be viewed as a novel variance interpolation with confidence and further leverages techniques from semi-definite programming and sum-of-squares optimization. Theoretical and numerical performances for the proposed approach for uncertainty quantification are analyzed.

Conditional Deep Generative Learning

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Conditional distribution is a fundamental quantity in statistics and machine learning that provides a full description of the relationship between a response and a predictor. There is a vast literature on conditional density estimation. A common feature of the existing methods is that they seek to estimate the functional form of the conditional density. We propose a deep generative approach to learning a conditional distribution by estimating a conditional generator, so that a random sample from the target conditional distribution can be obtained by transforming a sample from a simple reference distribution. The conditional generator is estimated nonparametrically with neural networks by matching appropriate joint distributions using a discrepancy measure. There are several advantages of the proposed generative approach over the classical methods for conditional density estimation, including: (a) there is no restriction on the dimensionality of the response or predictor, (b) it can handle both continuous and discrete type predictors and responses, and (c) it is easy to obtain estimates of the summary measures of the underlying conditional distribution by Monte Carlo. We show that the proposed conditional learning approach can mitigate the curse of dimensionality under a low-dimensional data support assumption. We also conduct extensive numerical experiments to validate the proposed method and using several benchmark datasets, including the California housing, the MNIST, and the CelebA datasets, to illustrate its applications in conditional sample generation, uncertainty quantification of prediction, visualization of multivariate data, image generation and image reconstruction.

Optimal Parameter-transfer Learning by Semiparametric Model Averaging

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In this article, we focus on prediction of a target model by transferring the information of source models. To be flexible, we use semiparametric additive frameworks for the target and source models. Inheriting the spirit of parameter-transfer learning, we assume that different models possibly share common knowledge across parametric components that is helpful for the target predictive task. Unlike existing parameter-transfer approaches, which need to construct auxiliary source models by parameter similarity with the target model and then adopt a regularization procedure, we propose a frequentist model averaging strategy with a J-fold cross-validation criterion so that auxiliary parameter information from different models can be adaptively utilized through data-driven weight assignments. The asymptotic optimality and weight convergence of our proposed method are built under some regularity conditions. Extensive numerical results demonstrate the superiority of the proposed method over competitive methods.

Optimization Models and Approaches for Strictly Correlated Electrons

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In electronic structure calculations, Kohn-Sham equations rank among the most widely adopted mathematical models. However, due to the deficiency of available approximations for exchange-correlation energy, Kohn-Sham equations cannot well describe strictly correlated electrons at present. To this end, some models based on the strong-interaction limit of density functional theory have been developed in recent decades. The associated energy minimizations can be formulated as multimarginal optimal transport problems with Coulomb cost (MMOT). Since the curse of dimensionality resides in MMOT, its low-dimensional reformulations are indispensable. In this talk, we consider the reformulation based on a Monge-like ansatz. We discuss the difficulties in the corresponding optimization problems, and also propose a global optimization approach for numerical resolution.

Euclidean Distance Matrix Optimization and Its Application to Portfolio Theory

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Euclidean distance matrix (EDM) optimization has proven very useful in data embedding in Euclidean space. This talk reviews some fundamental geometric embedding theory and illustrates its application to portfolio construction. In particular, we study the implication of EDM optimization to the maximum diversification return portfolio, proposed by Booth and Fama in 1990s. We are able to develop diversification return and risk relationship for the efficient frontier and derive the efficient portfolio that has the largest diversification return. Essential to this new development is the concept of portfolio centrality, that is closely related to the principal coordinate system defined by EDM. We will use DAX Index 30 stocks to demonstrates the reported results.

A General Framework for Optimal Data-Driven Optimization

Daniel Kuhn

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We propose a statistically optimal approach to construct data-driven decisions for stochastic optimization problems. Fundamentally, a data-driven decision is simply a function that maps the available training data to a feasible action. It can always be expressed as the minimizer of a surrogate optimization model constructed from the data. The quality of a data-driven decision is measured by its out-of-sample risk. An additional quality measure is its out-of-sample disappointment, which we define as the probability that the out-of-sample risk exceeds the optimal value of the surrogate optimization model. The crux of data-driven optimization is that the data-generating probability measure is unknown. An ideal data-driven decision should therefore minimize the out-of-sample risk simultaneously with respect to every conceivable probability measure (and thus in particular with respect to the unknown true measure). Unfortunately, such ideal data-driven decisions are generally unavailable. This prompts us to seek data-driven decisions that minimize the outof-sample risk subject to an upper bound on the out-of-sample disappointment again simultaneously with respect to every conceivable probability measure. We prove that such Pareto-dominant data-driven decisions exist under conditions that allow for interesting applications: the unknown data-generating probability measure must belong to a parametric ambiguity set, and the corresponding parameters must admit a sufficient statistic that satisfies a large deviation principle. If these conditions hold, we can further prove that the surrogate optimization model generating the optimal data-driven decision must be a distributionally robust optimization problem constructed from the sufficient statistic and the rate function of its large deviation principle. This shows that the optimal method for mapping data to decisions is, in a rigorous statistical sense, to solve a distributionally robust optimization model. Maybe surprisingly, this result holds irrespective of whether the original stochastic optimization problem is convex or not and holds even when the training data is non-i.i.d. As a byproduct, our analysis reveals how the structural properties of the data-generating stochastic process impact the shape of the ambiguity set underlying the optimal distributionally robust optimization model.