

Nobody can go back and start a new beginning,  
but anybody can start today and make a new ending.

3.1

## LINK LIST

→ Unknown

### Array

#### Advantage

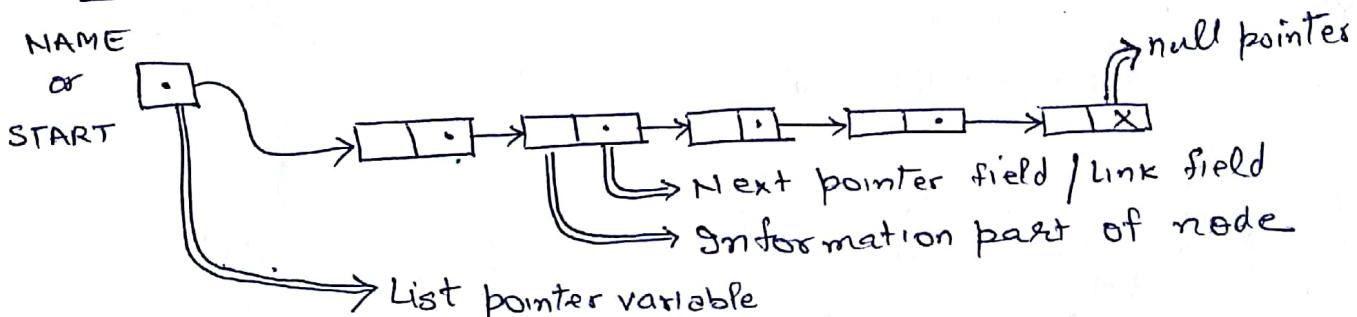
- Easy to compute the address of an element in an array

#### Disadvantage

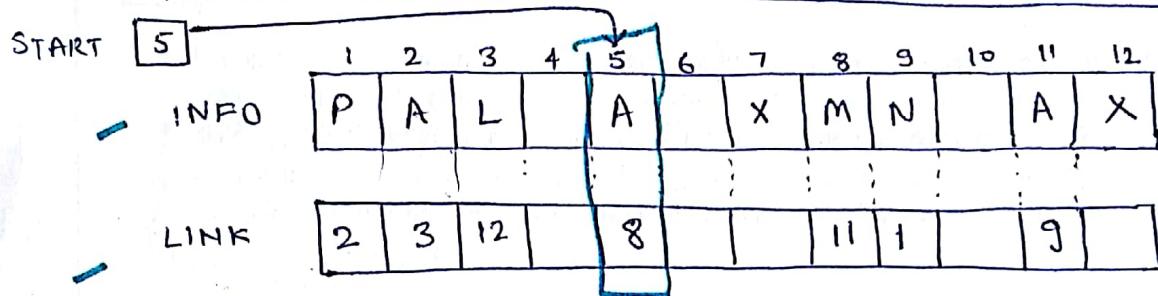
- Relatively expensive to insert and delete elements in an array
- One can not simply double or triple the size of an array when additional space is required. (that's why it's called static data structure)

In case of link list, the successive elements in the list need not occupy adjacent space in memory.  
(as in case of array)  
— This will make it easier to insert & delete elements in the list.

### LINKED LIST



## REPRESENTATION OF LL IN MEMORY



In this way, more ( glove mom )  
 ↘  
 ↗

More than one list may be maintained in the same linear arrays INFO & LINK. However, each list must have its own pointer variable giving the location of its first node.

## TRaversing A LINK LIST

Traversing algorithm uses a pointer variable PTR, which points to the node that is currently being processed.

Accordingly, LINK[PTR] points to the next node to be processed.

Thus

$$\text{PTR} := \text{LINK}[\text{PTR}]$$

moves the pointer to the next node in the list.

## Algorithm LinkList-Traversals

Let LIST be linked list. This algo traverses LIST, applying PROCESS to each element of LIST. The variable PTR points to node currently being processed.

1. Set PTR := START
2. Repeat step 3 & 4 while PTR  $\neq$  NULL
3. Apply PROCESS to INFO[PTR]
4. Set PTR := LINK[PTR]  
[END of step 2 loop]
5. EXIT

=====

## Procedure: COUNT (INFO, LINK, START, NUM)

1. Set NUM := 0
2. Set PTR := START
3. Repeat step 4 & 5 while PTR  $\neq$  NULL
4. Set NUM := NUM + 1
5. Set PTR := LINK[PTR]  
[END of step 3 loop]
6. Return

## SEARCHING A LINKED LIST

Let LIST be a linked list in memory, a specific ITEM of information is given.

There are two searching algorithm for finding the LOC location of NODE.

(a) LIST is Unsorted: Using a pointer variable PTR & comparing ITEM with the contents —

INFO[PTR] of each node, one by one, of LIST.

- We update pointer PTR by  $PTR := \text{LINK}[PTR]$
- We require two tests

(i) whether  $PTR = \text{NULL}$

If not (ii) check whether  $\text{INFO}[PTR] = \text{ITEM}$

Accordingly, we use first test to control the execution of a loop, second test place inside the loop.

Algorithm SEARCH (INFO, LINK, START, ITEM, LOC)

1. Set  $PTR := \text{START}$
2. Repeat step 3 while  $PTR \neq \text{NULL}$ :
3.   if  $\text{ITEM} = \text{INFO}[PTR]$ , then  
        set  $LOC := PTR$  and exit.

Else

    set  $PTR := \text{LINK}[PTR]$

[End of if structure]

[End of step 2 loop]

4. Set  $LOC := \text{NULL}$  [unsuccessful]
5. EXIT

The complexity of this algorithm is same as that of the linear search algorithm.

### (b) LIST is sorted

Now, however, we can stop once ITEM exceeds INFO[PTR].

Algorithm SEARCH-SOR (INFO, LINK, START, ITEM, LOC)

1. Set PTR := START
2. Repeat Step 3 while PTR ≠ NULL
  3. If ITEM < INFO[PTR], then:  
set PTR := LINK[PTR]
  - Else if ITEM = INFO[PTR], then:  
set LOC := PTR, # Exit
  - Else  
set LOC := NULL, # Exit

[End of if structure]

[End of step 2 loop]
4. Set LOC := NULL
5. EXIT

Binary search algorithm cannot be applied to a sorted link list, since there is no way of indexing the middle element in the list.

### GARBAGE COLLECTION

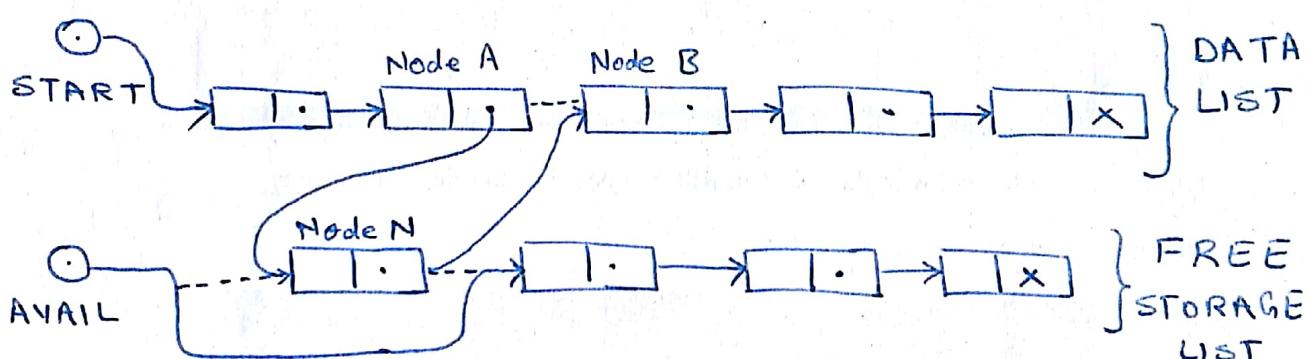
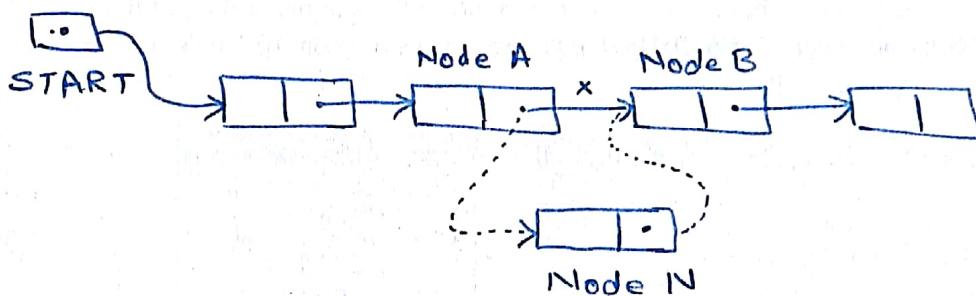
Suppose a memory space become reusable because a node is deleted, we want space to be available for future use. (one way to bring this into free-storage list <time consuming>)

The operating system of computer may periodically collect all the deleted space into the free-storage list.

## OVERFLOW & UNDERFLOW

- \* Overflow: New data are to be inserted into a data structure but there is no available space.
- \* Underflow: situation where one wants to delete data from data structure that is empty.

### INSERTION INTO LINKED LIST



The three pointer fields are going to be change

(i) Next PTR of Node A points to Node N

(ii) AVAIL now points to NEXT AVAIL

(iii) Next PTR of Node N points to Node B

Two special case

(i) If new node N is the first node, then START points to N

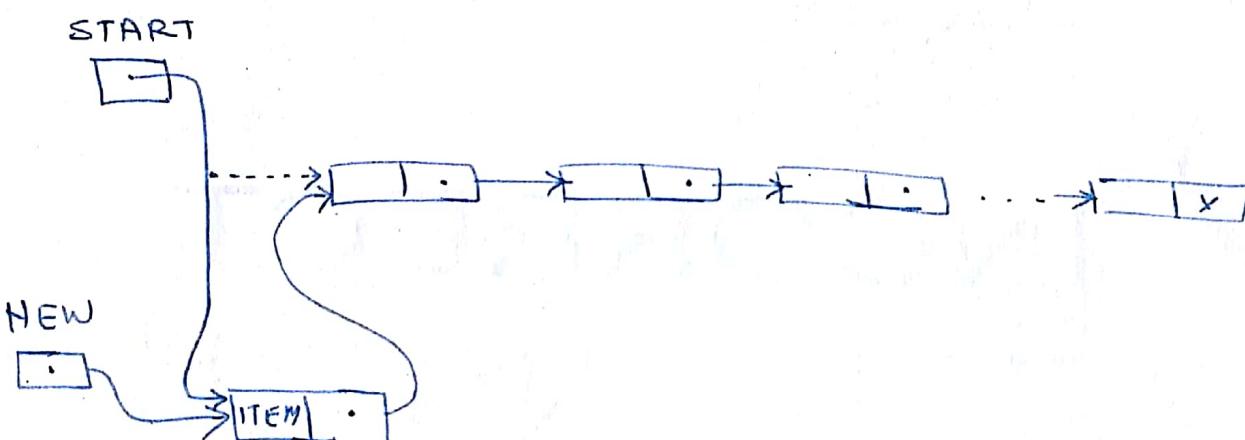
(ii) If new node N is the last node, then N will contain null pointer.

## Insertion Algorithms: The main three situations

- (i) Inserting a node at the beginning of the list,
- (ii) inserting after the node with given location
- (iii) inserting a node into a sorted list.

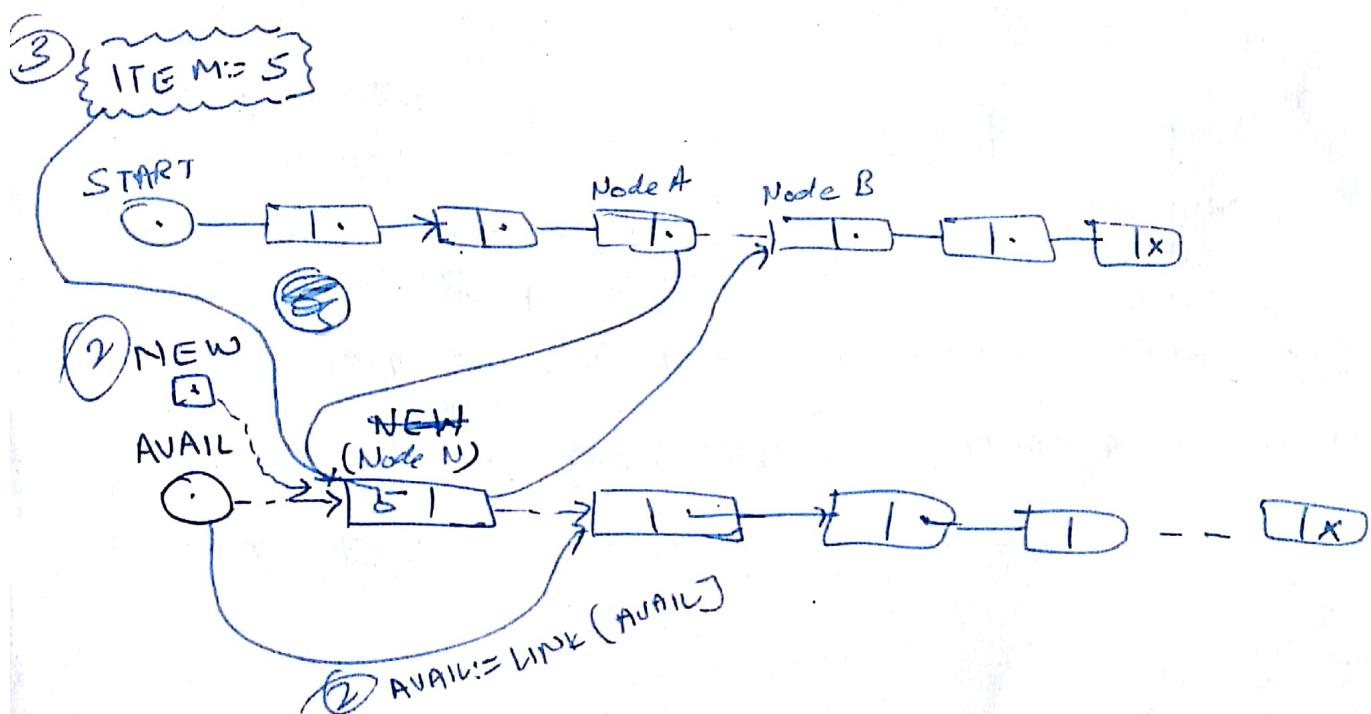
### (i) Algorithm: Insert-first(INFO, LINK, START, AVAIL, ITEM)

<p>overflow?</p> <p>Remove first node from AVAIL list</p> <p>copy new data into node</p> <p>New node points to original 1st node</p> <p>START points to first node</p>	1. If $AVAIL = \text{NULL}$ , then: Write : OVERFLOW and EXIT	
	2. Set $NEW := AVAIL$ & $AVAIL := \text{LINK}[AVAIL]$	
	3. Set $\text{INFO}[NEW] := ITEM$	
	4. Set $\text{LINK}[NEW] := START$	
	5. Set $START := NEW$	
	6. EXIT	



(ii) Algorithm: Ins\_Poc (INFO, LINK, START, AVAIL, LOC, ITEM)

- [1] If  $AVAIL = \text{NULL}$ , then:  
    WRITE : OVERFLOW, and EXIT
- [2] Set  $NEW := AVAIL$   
     $\& AVAIL := \text{LINK}[AVAIL]$
- [3] Set  $\text{INFO}[NEW] := ITEM$
- [4] If  $LOC = \text{NULL}$ , then:  
    Set  $\text{LINK}[NEW] := \text{START}$   
     $\& \text{START} := NEW$   
~~Else~~  
    Set  $\text{LINK}[NEW] := \text{LINK}[LOC]$   
     $\& \text{LINK}[LOC] := NEW$   
[End of if structure of step 4]
- [5] EXIT



## Inserting into a Sorted Linked List



Procedure: FIND (INFO, LINK, START, ITEM, LOC)

This procedure find the location LOC of the node in a sorted list such that

INFO[LOC]<ITEM or set LOC=NULL

- 1> If  $\text{START} = \text{NULL}$ , then: Set  $\text{LOC} := \text{NULL}$ , & Return
  - 2> If  $\text{ITEM} < \text{INFO}[\text{START}]$ , then Set  $\text{LOC} := \text{NULL}$  & Return
  - 3> Set  $\text{SAVE} := \text{START}$  &  $\text{PTR} := \text{LINK}[\text{START}]$
  - 4> Repeat Step 5 & 6 while  $\text{PTR} \neq \text{NULL}$ 
    - 5> If  $\text{ITEM} < \text{INFO}[\text{PTR}]$ , then
      - Set  $\text{LOC} := \text{SAVE}$  & Return

[End of If structure]
    - 6> Set  $\text{SAVE} := \text{PTR}$  &  $\text{PTR} := \text{LINK}[\text{PTR}]$ .

[End of Step 4 loop]
  - 7> Set  $\text{LOC} := \text{SAVE}$
  - 8> Return

Algorithm: ginsert\_sort\_ll (INFO, LINK, START, AVAIL, ITEM)  
This also inserts ITEM into a sorted linked list.

  - 1> Call FIND (INFO, LINK, START, ITEM, LOC)
  - 2> Call gns\_loc (INFO, LINK, START, AVAIL, LOC, ITEM)
  - 3> EXIT

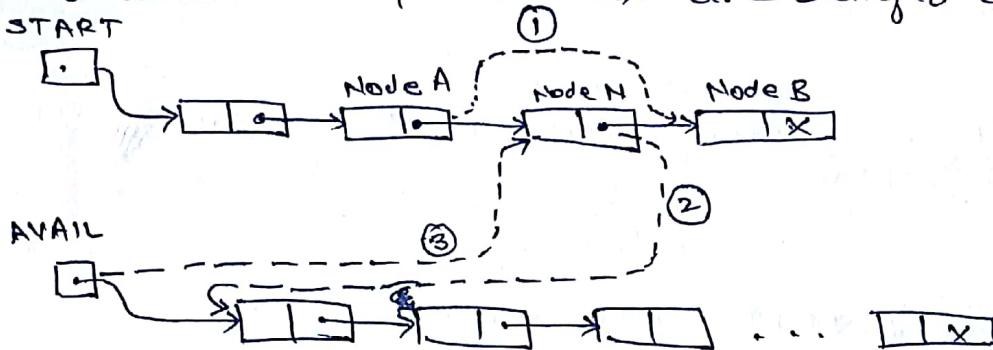
Algorithm: Insert\_Sort\_LL (INFO, LINK, START, AVAIL, ITEM)  
This algo inserts ITEM into a sorted linked list.

- 1> Call FIND (INFO, LINK, START, ITEM, LOC)
  - 2> Call gns\_loc (INFO, LINK, START, AVAIL, LOC, ITEM)
  - 3> EXIT

## DELETION FROM A LINK LIST

3.10  
 (a) Deleting node following  
a given Node  
 (b) Deleting with given ITEM  
of info.

Observe three pointer fields are changed as follows:



- (1) The next pointer field of node A now points to node B, where node N previously pointed.
- (2) The next pointer field of N now points to the original first node in the free pool, where AVAIL previously pointed.
- (3) AVAIL now points to the deleted node N.

### (2) DELETING: FOLLOWING A GIVEN NODE

Algorithm : DEL\_LL (INFO, LINK, START, AVAIL, LOC, LOCP)  
 // LOCP is the location of the node which precedes N  
 (when N is first node: LOCP = NULL)

<1> If LOCP = NULL, then:

Set START := LINK[START] //Delete first node.

Else

Set LINK[LOCP] := LINK[LOC] //Delete node N

{End of If structure}

<2> Set LINK[LOC] := AVAIL & AVAIL := LOC

//Return deleted node to the AVAIL list]

<3> EXIT

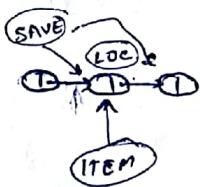
) DELETING THE NODE WITH A GIVEN ITEM of information.

Procedure : FIND\_N (INFO, LINK, START, ITEM, LOC, LOC\_P)

If list  
empty

Node is  
1st node

1. If  $START = \text{NULL}$ , then : Set  $LOC := \text{NULL}$ , &  $LOC_P := \text{NULL}$   
[End of if]
2. If  $INFO[START] = \text{ITEM}$ , then:  
Set  $LOC := \text{NULL}$  &  $LOC_P := \text{NULL}$ , & Return  
[End of if structure of step 2]
3. Set  $SAVE := START$  &  $PTR := \text{LINK}[START]$
4. Repeat step 5 & 6 while  $PTR \neq \text{NULL}$
5. If  $INFO[PTR] = \text{ITEM}$ , then:  
Set  $LOC := PTR$  &  $LOC_P := SAVE$  & Return  
[End of if structure]
6. Set  $SAVE := PTR$  &  $PTR := \text{LINK}[PTR]$   
[End of loop 4]
7. Set  $LOC := \text{NULL}$
8. Return



Algorithm : DELETE (INFO, LINK, START, AVAIL, ITEM)

Find  
node

node not  
in list

node is  
1st node

Return del  
node to  
avail list

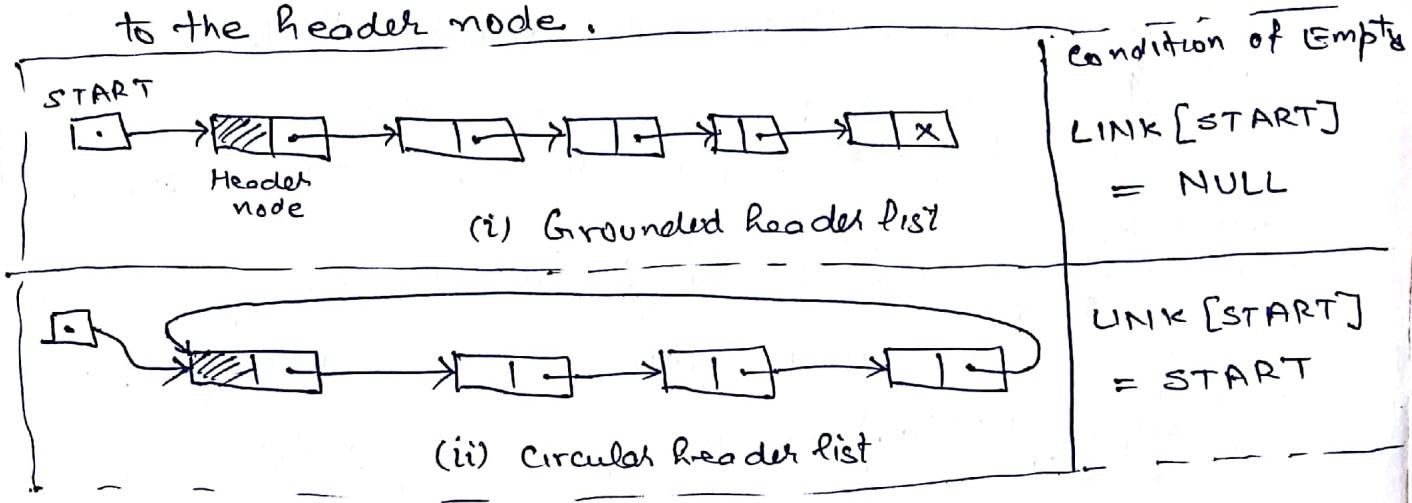
1. Call FIND\_N (INFO, LINK, START, ITEM, LOC, LOC\_P)
2. If  $LOC = \text{NULL}$ , then: Write: ITEM not in list, & Exit
3. If  $LOC_P = \text{NULL}$ , then: Set  $START := \text{LINK}[START]$   
Else Set  $\text{LINK}[LOC_P] := \text{LINK}[LOC]$   
[End of if structure]
4. Set  $\text{LINK}[LOC] := \text{AVAIL}$  &  $\text{AVAIL} := LOC$
5. EXIT

## HEADER LINK LIST

A header linked list is a linked list which always contains a special node, called header node, at the beginning of the list. Two kind of header link list:

(i) A grounded header list: is the header link list where the last node contains the null pointer

(ii) A circular header list: where last node points back to the header node.



Although our data may be maintained by Header list in memory, the AVAIL list will always be maintained as ordinary linked list.

The first node in a Header list is the node following the header node, and the location of the first node is **LINK[START]** not **START**.

→ circular Header list are frequently used instead of or property

- (i) The null pointer is not used, and hence all pointers contain valid pointer addresses
- (ii) Every (ordinary) node has a predecessor, so first node may not require a special case.

## HEADER LINKED LISTS

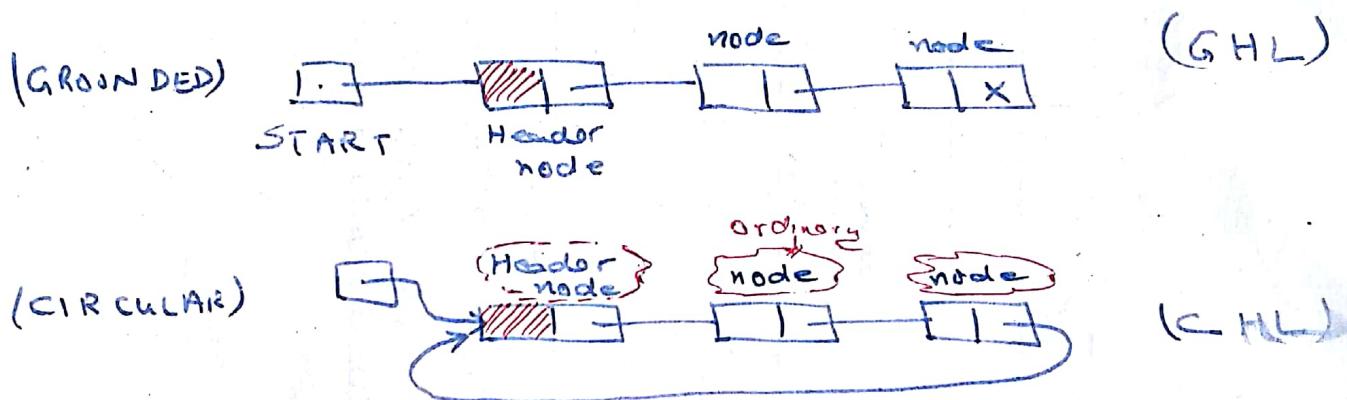
3.13

It is the link list which always contains a special node, called the Header node, at the beginning of the list.

Two type of header link lists are:

(1) Grounded Header List: where last node contains the null pointer

(2) Circular Header list: where last node points back to the Header node.



# START always points to the header node.

#  $\text{LINK}[\text{START}] = \text{NULL}$ ; GHL is empty

#  $\text{LINK}[\text{START}] = \text{START}$ ; CHL is empty

# Data may be maintained in memory by Header list but the AVAIL list will always be maintained as ordinary linked list.

# Location of first node is  $\text{LINK}[\text{START}]$  not START.

Algorithm : TCHL (Traversed circular header LL)

- conditions (i) begins with  $\text{PTR} = \text{LINK}[\text{START}]$  not  $\text{START}$   
 (ii) end  $\text{PTR} = \text{START}$  not  $\text{PTR} = \text{NULL}$

Let LIST be circular header link list in memory

The algorithm traverses LIST, applying an operation  
 PROCESS to each node in LIST

1. Set  $\text{PTR} := \text{LINK}[\text{START}]$
  2. Repeat step 3 & 4 while  $\text{PTR} \neq \text{START}$
  3. Apply process to  $\text{INFO}[\text{PTR}]$
  4. Set  $\text{PTR} := \text{LINK}[\text{PTR}]$
- [End of step 2 loop]
5. EXIT

### PROPERTIES

- # The NULL pointer is not used, hence all pointers contain valid addresses
- # Every (ordinary) node has a predecessor, so the first node may not require a special case

Procedure : Find\_Loc\_CHL (INFO, LINK, START, ITEM, LOC, LOC\_P)

1. Set SAVE := START & PTR := LINK[START]
2. Repeat while INFO[PTR] ≠ ITEM & PTR ≠ START  
 Set SAVE := PTR & PTR := LINK[PTR]  
 [END of loop 2]
3. If INFO[PTR] = ITEM, then:  
 Set LOC := PTR & LOC\_P := SAVE  
 Else  
 Set LOC := NULL & LOC\_P := SAVE  
 [END of IF structure]

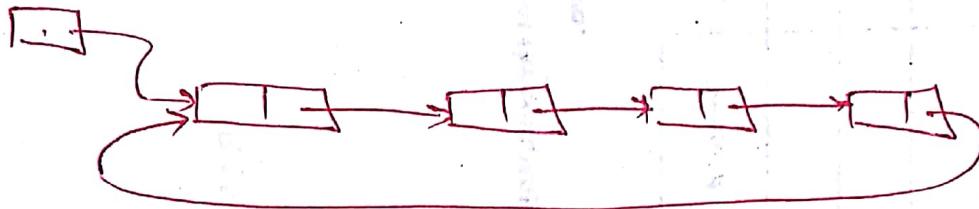
4. EXIT

Algorithm: Del\_Loc\_CHL (INFO, UNK, START, AVAIL, ITEM)

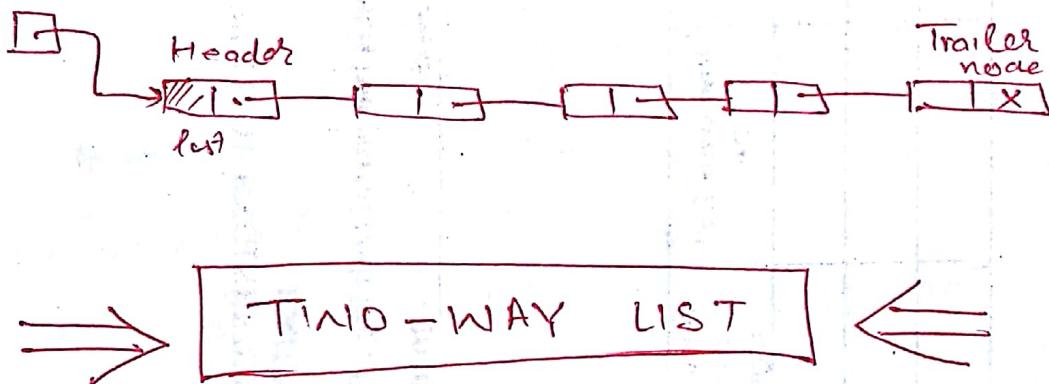
1. [Use above procedure to find the location of N & its preceding node] Call Find\_Loc\_CHL(...)
2. If LOC = NULL, then: Write: ITEM not in list, & EXIT
3. Set LINK[LOC\_P] := LINK[LOC] // Delete node
4. Set LINK[LOC] := AVAIL & AVAIL := LOC
5. EXIT

Two other variant of link lists:

- (1) Simple link list, whose last node points to first node



- (2) list contain both header & trailer node



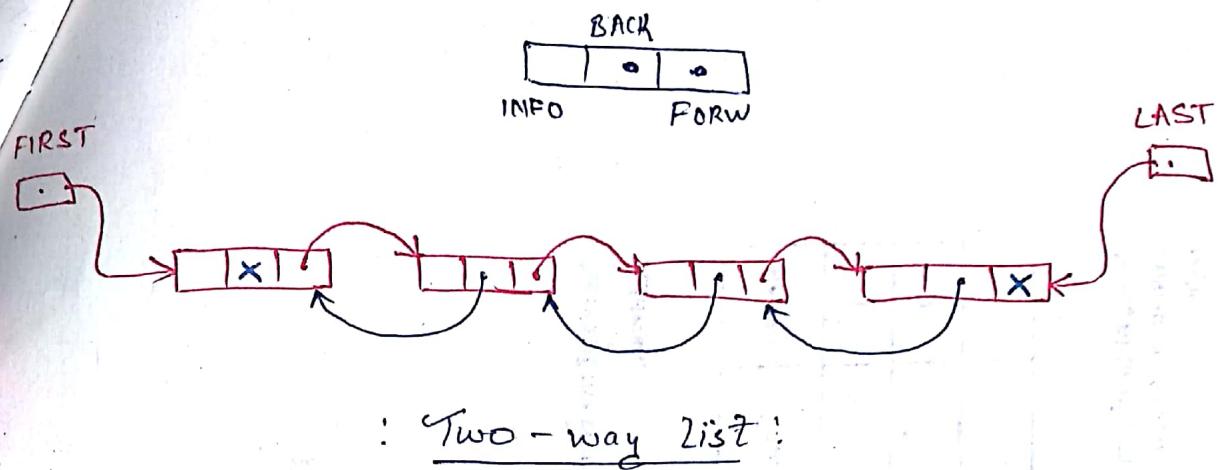
Two-way list can be traversed into two direction.

This mean, one is able to delete N from the list without traversing any part of list.

# Provide immediate access to the next & preceding node.

Each node is divided into three parts:

- (i) An information field INFO which contains the data.
- (ii) A pointer field PFORW, contain location of next node.
- & (iii) A pointer field BACK, contains location of preceding node.



It also requires two list pointer variables:

FIRST → points to the first node in the list.

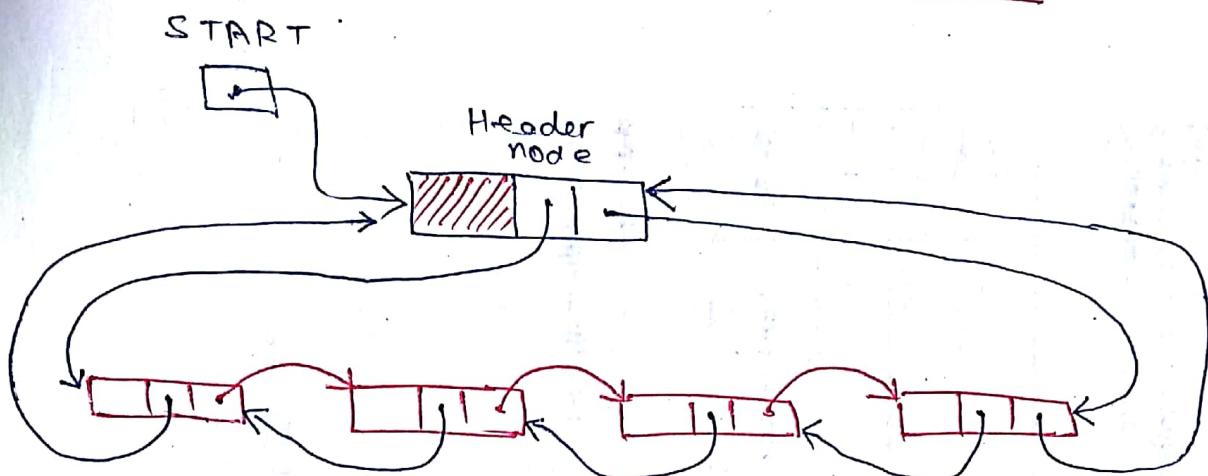
LAST → .. . . . last node " " " .

Observe that null pointer appears in FORW field of the last node in the list \$

Also in BACK field of the first node in the list.

Beside so many changes, the AVAIL list of available space in the arrays will still be maintained as one-way list - using FORW as pointer field - since we delete and insert nodes only at the beginning of the AVAIL list.

## TWO-WAY HEADER LISTS



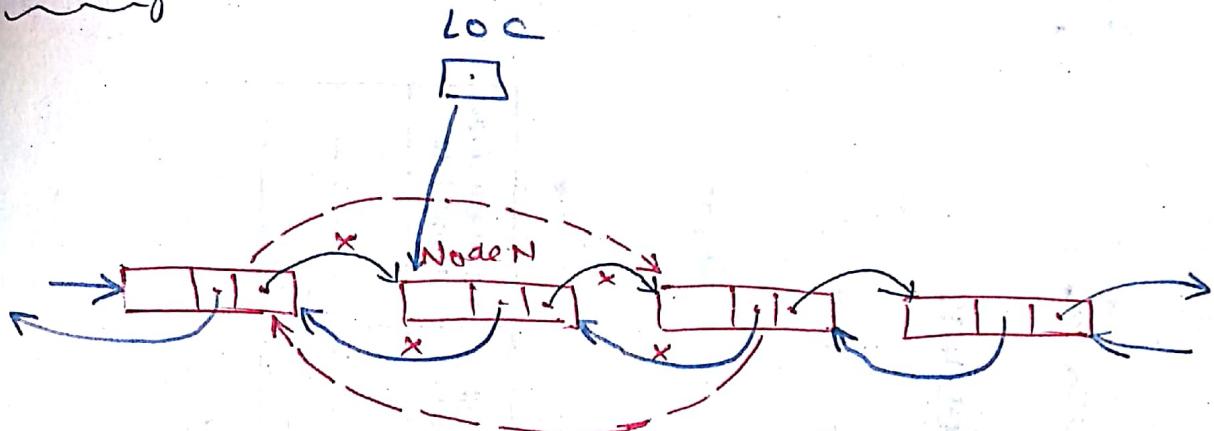
Two way Circular Header List

This list is circular because the two end nodes point back to the header node.

### OPERATIONS ON TWO-WAY LIST

- (i) Traversing: Same procedure as in ordinary / Read link list. (not any specific advantage of two way)
- (ii) Searching: Same as previous algorithms.  
Advantage: We can search for ITEM in the backward direction if we have reason to suspect that ITEM appears near the end of the list.

i) Deleting:



Pointer changes as:

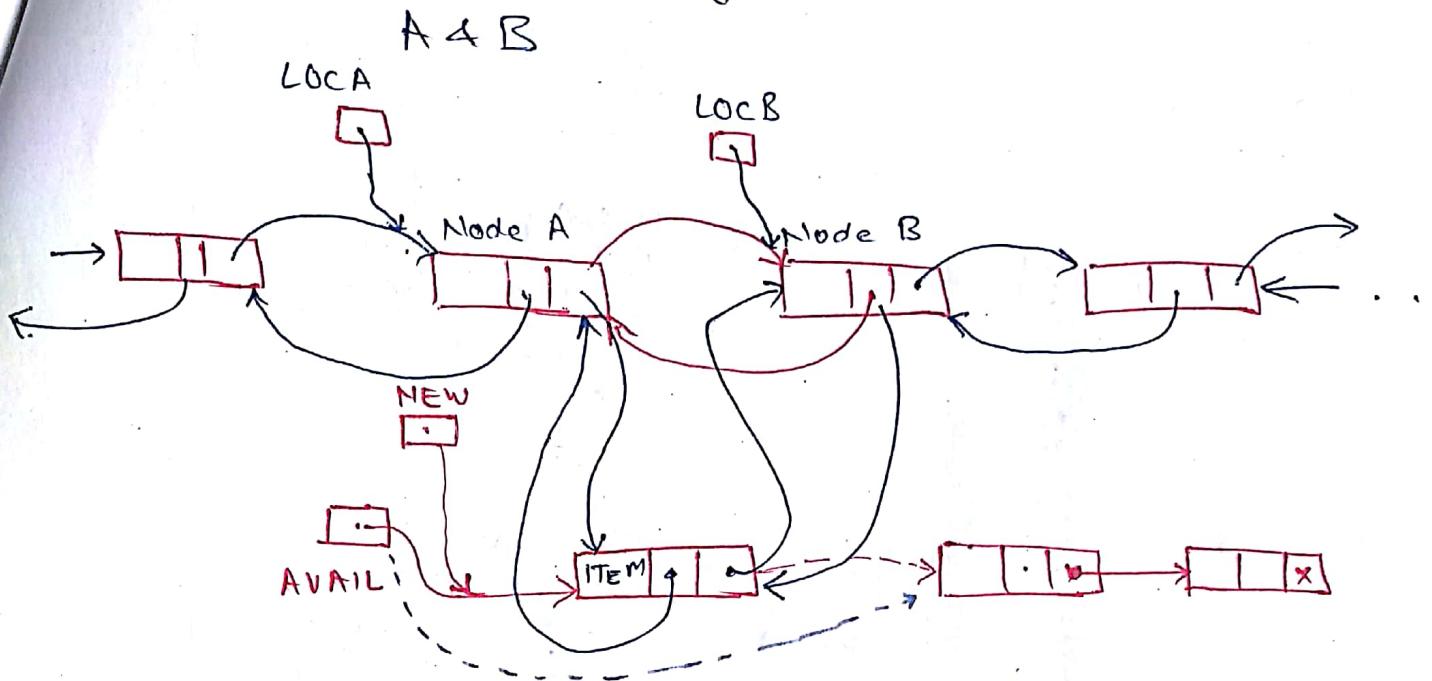
$$\text{FORW}[\text{BACK}[\text{Loc}]] := \text{FORW}[\text{Loc}] \quad \notin$$

$$\text{BACK}[\text{FORW}[\text{Loc}]] := \text{BACK}[\text{Loc}]$$

Algorithm: Del\_TWL (INFO, FORW, BACK, START, AVAIL, LOC)

1. Set  $\text{FORW}[\text{BACK}[\text{Loc}]] := \text{FORW}[\text{Loc}] \quad \& \quad \left. \begin{array}{l} \text{Deleting node} \\ \text{in TWL} \end{array} \right\}$   
 $\text{BACK}[\text{FORW}[\text{Loc}]] := \text{BACK}[\text{Loc}]$
2. Set  $\text{FORW}[\text{Loc}] := \text{AVAIL} \quad \& \quad \left. \begin{array}{l} \text{ReTurn node} \\ \text{to AVAIL list} \end{array} \right\}$   
 $\text{AVAIL} := \text{LOC}$
3. EXIT

iv) Inserting : Inserting node N between node A & B



Suppose we are given the locations LOC A & LOC B of adjacent nodes A & B in LIST.

# We set: (for removing first node from AVAIL)

$NEW := AVAIL$  ,  $AVAIL := FORW[AVAIL]$

$INFO[NEW] := ITEM$

# Insert into LIST by changing following four pointers:-

$FORW[LOC A] := NEW$  ;  $FORW[NEW] := LOC B$

$BACK[LOC B] := NEW$  ;  $BACK[NEW] := LOC A$

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Algorithm : INS-TWL (INFO, FORW, BACK, START, AVAIL, LOC<sub>A</sub>, LOC<sub>B</sub>, ITEM)

1. If AVAIL = NULL then: write : OVERFLOW, & EXIT
2. Set NEW := AVAIL  
AVAIL := FORW[AVAIL]  
INFO[NEW] := ITEM
3. Set FORW[LOC<sub>A</sub>] := NEW  
FORW[NEW] := LOC<sub>B</sub>  
BACK[LOC<sub>B</sub>] := NEW  
BACK[NEW] := LOC<sub>A</sub>
4. EXIT