

An abstract graphic on the left side of the slide consists of three overlapping circles in different shades of teal. The largest circle is a light teal, the medium one is a medium teal, and the smallest is a dark teal. They overlap in a way that creates a sense of depth and movement.

Generative Models

What we will learn today

- ❑ Autoencoder
- ❑ Variational Autoencoder
- ❑ Generative Adversarial Network

Supervised vs. Unsupervised Learning

Supervised Learning

Data: (x, y)

x is data, y is label

Data Labeling is needed

Goal: Learn a function to map $x \rightarrow y$

$$y = f(x)$$

Examples: classification, regression, object detection, semantic segmentation, image segmentation etc.

Classification: Input x



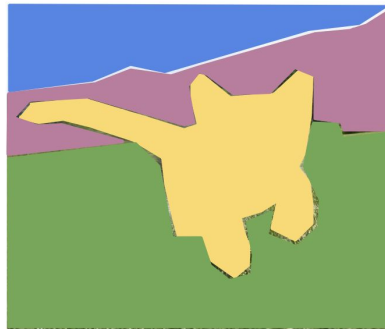
$$y = 8$$

Object Detection



DOG, DOG, CAT

Semantic Segmentation



GRASS, CAT, TREE, SKY

Supervised vs. Unsupervised Learning

Supervised Learning

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Goal: Learn a function to map $x \rightarrow y$

$$y = f(x)$$

Examples: classification, regression, object detection, semantic segmentation, image segmentation etc.

Unsupervised Learning

Data: x

Just data, No labels!

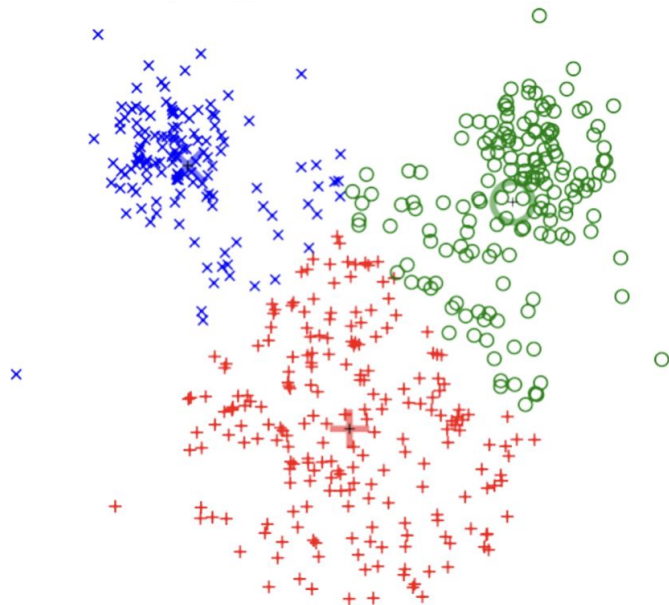
Goal: Learn some underlying hidden structure of the data

Examples: clustering, dimensionality reduction, feature learning, density estimation etc.

Supervised vs. Unsupervised Learning

Unsupervised Learning

Clustering
(e.g. k-Means)



Data: x

Just data, No labels!

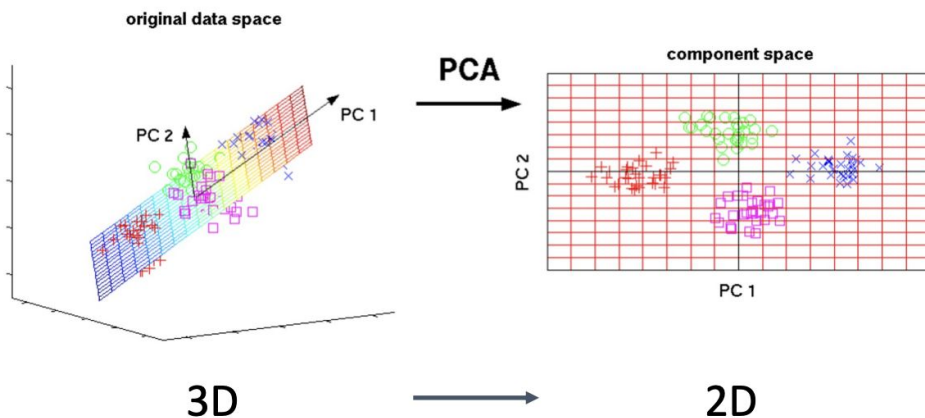
Goal: Learn some underlying hidden structure of the data

Examples: clustering, dimensionality reduction, feature learning, density estimation etc.

Supervised vs. Unsupervised Learning

Unsupervised Learning

Dimensionality Reduction
(e.g. Principal Component Analysis- PCA)



Data: x

Just data, No labels!

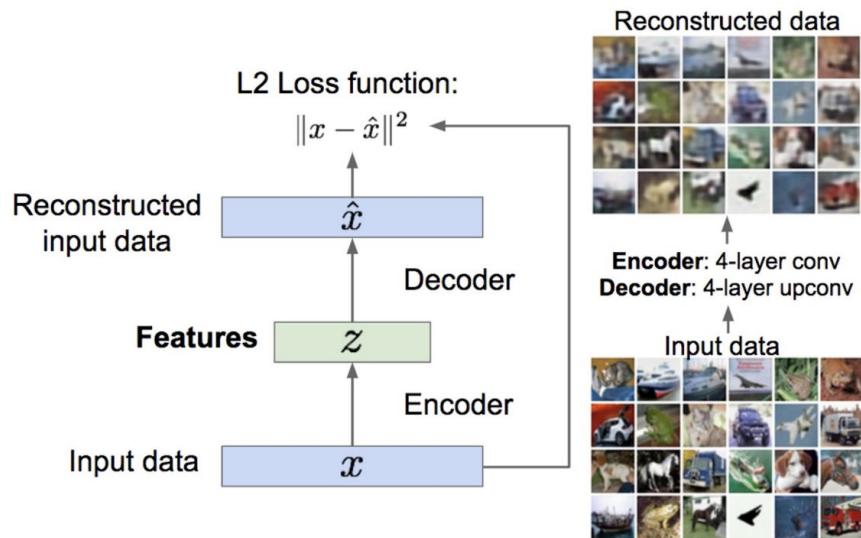
Goal: Learn some underlying hidden structure of the data

Examples: clustering, dimensionality reduction, feature learning, density estimation etc.

Supervised vs. Unsupervised Learning

Unsupervised Learning

Feature Learning
(e.g. Autoencoders)



Data: x

Just data, No labels!

Goal: Learn some underlying hidden structure of the data

Examples: clustering, dimensionality reduction, feature learning, density estimation etc.

Discriminative vs. Generative Models

Discriminative Model:

Learn a probability distribution $P(y|x)$

Generative Model:

Learn a probability distribution $P(x)$

Conditional Generative Model: Learn a probability distribution $P(x|y)$

Data: x



Label: $y = \text{Cat}$

Probability Recap:

Density Function

$P(x)$ assigns a positive number to each possible x ; higher numbers mean x is more likely

Density functions are **normalized**:

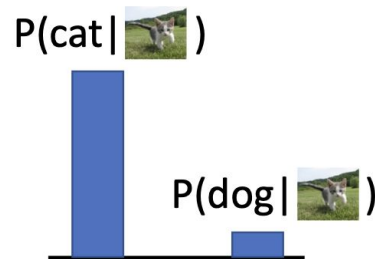
$$\int_x P(x)dx = 1$$

Different values of x **complete** for density

Discriminative vs. Generative Models

Discriminative Model:

Learn a probability distribution $P(y|x)$



Generative Model:

Learn a probability distribution $P(x)$

Density Function

$P(x)$ assigns a positive number to each possible x ; higher numbers mean x is more likely

Conditional Generative Model: Learn a probability distribution $P(x|y)$

Density functions are **normalized**:

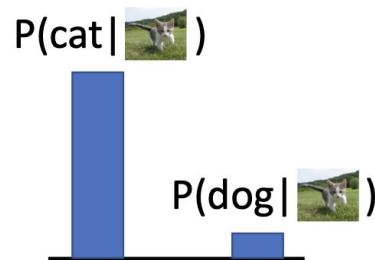
$$\int_x P(x) dx = 1$$

Different values of x **complete** for density

Discriminative vs. Generative Models

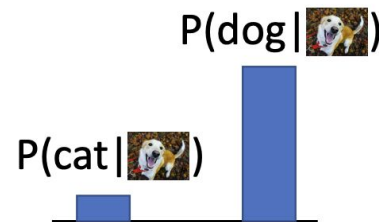
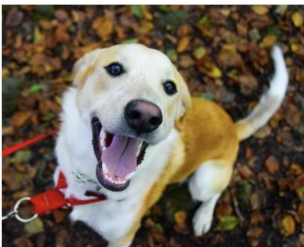
Discriminative Model:

Learn a probability distribution $P(y|x)$



Generative Model:

Learn a probability distribution $P(x)$



Conditional Generative

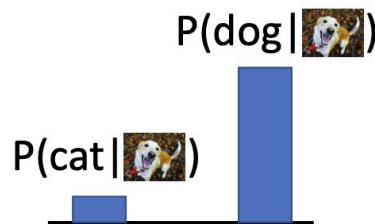
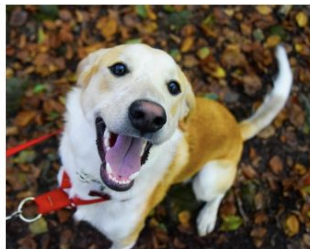
Model: Learn a probability distribution $P(x|y)$

Discriminative model: the possible labels for each input "compete" for probability mass. But no competition between **images**

Discriminative vs. Generative Models

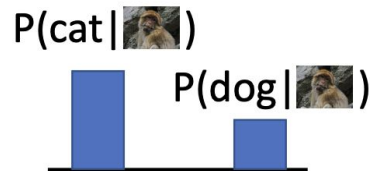
Discriminative Model:

Learn a probability distribution $P(y|x)$



Generative Model:

Learn a probability distribution $P(x)$



Conditional Generative

Model: Learn a probability distribution $P(x|y)$

Discriminative model: No way for the model to handle unreasonable inputs; it must give label distributions for all images

Discriminative vs. Generative Models

Discriminative Model:

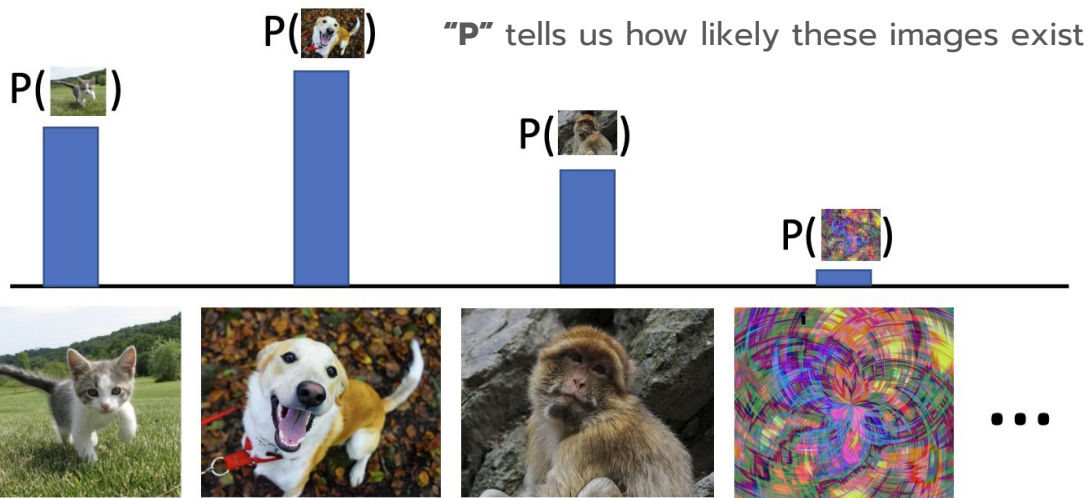
Learn a probability distribution $P(y|x)$

Generative Model:

Learn a probability distribution $P(x)$

Conditional Generative

Model: Learn a probability distribution $P(x|y)$



Generative model: All possible images compete with each other for probability mass

Requires deep image understanding! Is a dog more likely to sit or stand? How about 3-legged dog vs 3-armed monkey?

Discriminative vs. Generative Models

Discriminative Model:

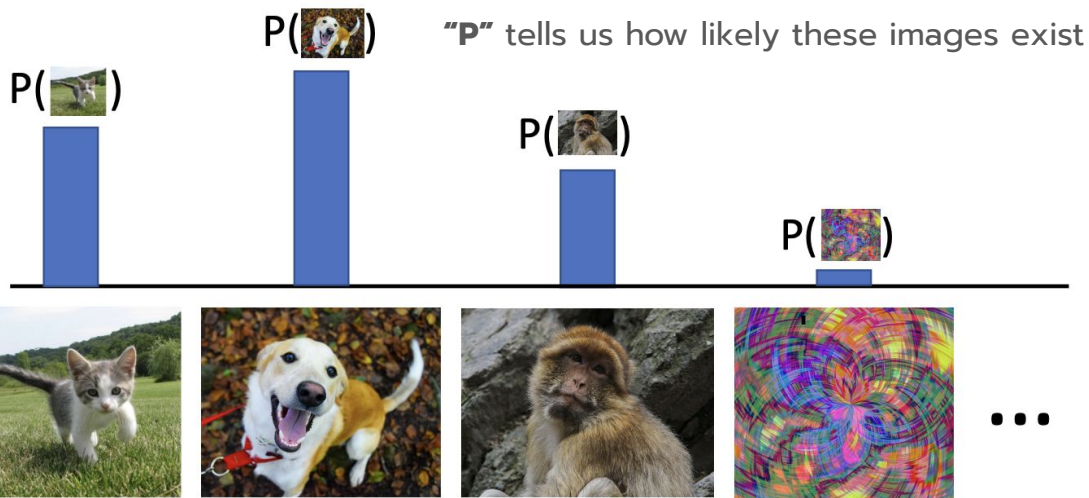
Learn a probability distribution $P(y|x)$

Generative Model:

Learn a probability distribution $P(x)$

Conditional Generative

Model: Learn a probability distribution $P(x|y)$



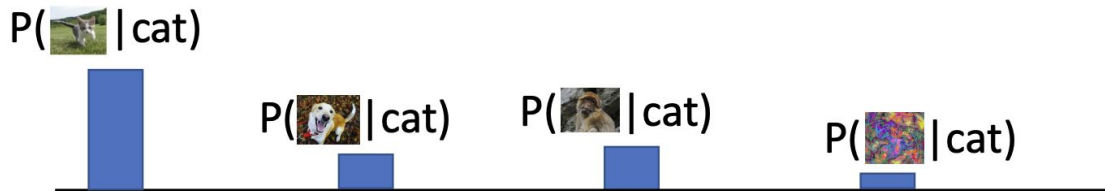
Generative model: All possible images compete with each other for probability mass

Model can "reject" unreasonable inputs by assigning them small values

Discriminative vs. Generative Models

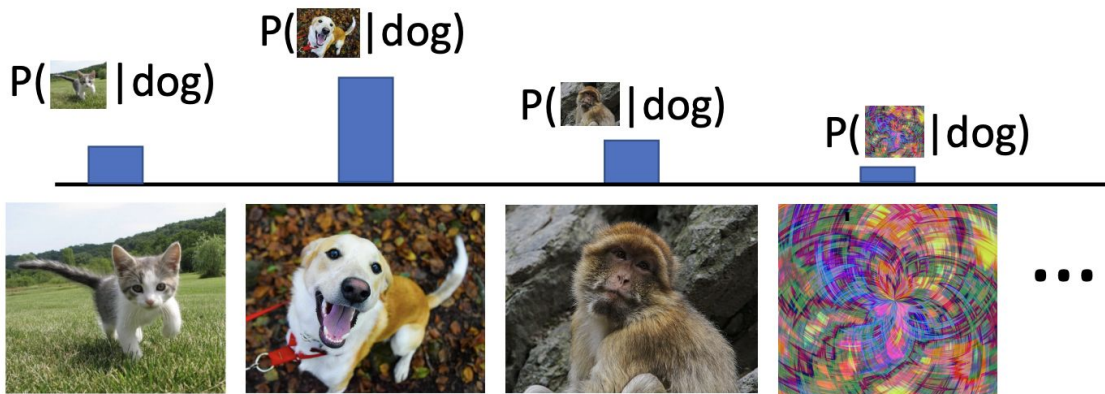
Discriminative Model:

Learn a probability distribution $P(y|x)$



Generative Model:

Learn a probability distribution $P(x)$



Conditional Generative Model: Learn a probability distribution $P(x|y)$

Conditional Generative Model: Each possible label induces a competition among all images

Discriminative vs. Generative Models

Discriminative Model:

Learn a probability distribution $P(y|x)$

Generative Model:

Learn a probability distribution $P(x)$

Conditional Generative

Model: Learn a probability distribution $P(x|y)$

These models may seem to be very distinct.
Although, they are actually **not fully** distinct.

Discriminative vs. Generative Models

Discriminative Model:

Learn a probability distribution $P(y|x)$

Generative Model:

Learn a probability distribution $P(x)$

Conditional Generative

Model: Learn a probability distribution $P(x|y)$

Recall **Bayes' Rule:**

$$\underbrace{P(x | y)}_{\text{Conditional Generative Model}} = \frac{\underbrace{P(y | x)}_{\text{Discriminative Model}} \underbrace{P(x)}_{\text{(Unconditional) Generative Model}}}{\underbrace{P(y)}_{\text{Prior over labels}}}$$

We can build a conditional generative model from other components!

Discriminative vs. Generative Models

Discriminative Model:

Learn a probability distribution $P(y|x)$



Assign labels to data
Feature learning (with labels)

Generative Model:

Learn a probability distribution $P(x)$



Detect outliers
Feature learning (without labels)
Sample to **generate** new data

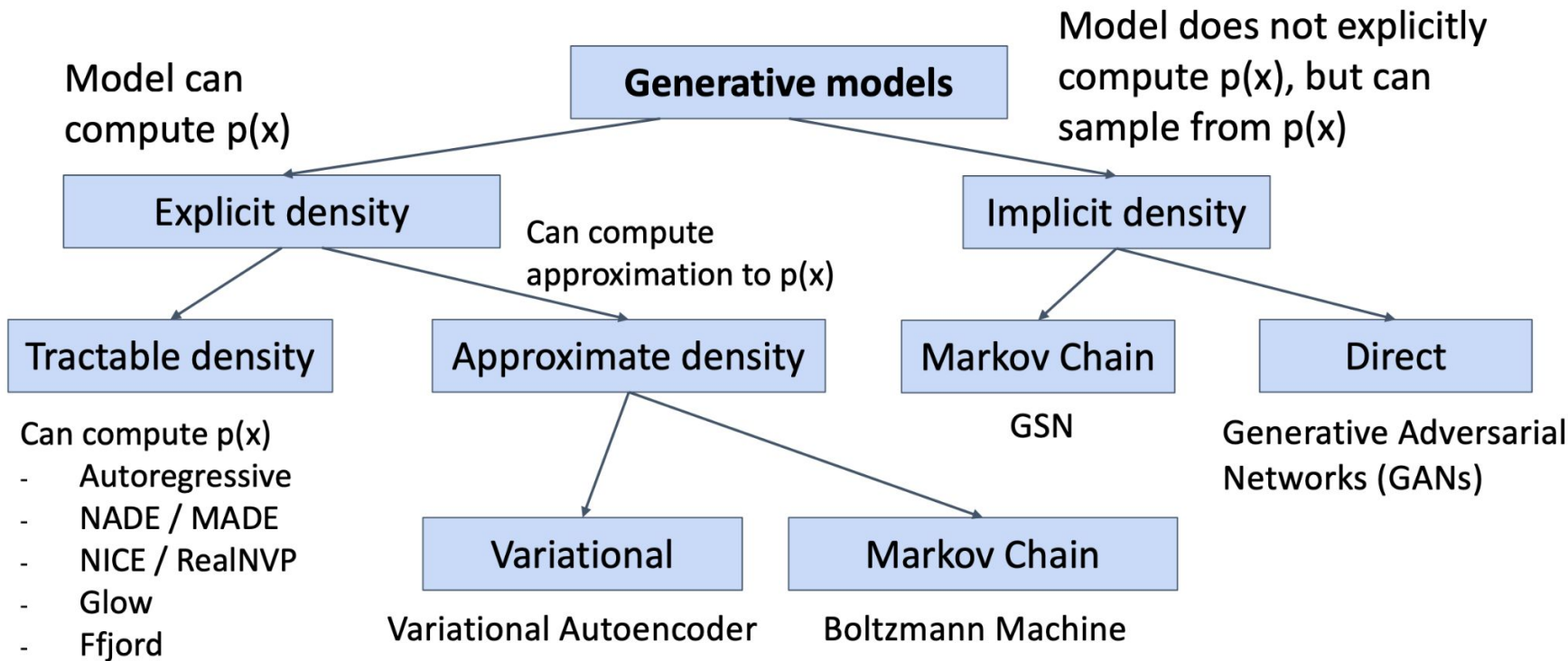
Conditional Generative

Model: Learn a probability distribution $P(x|y)$

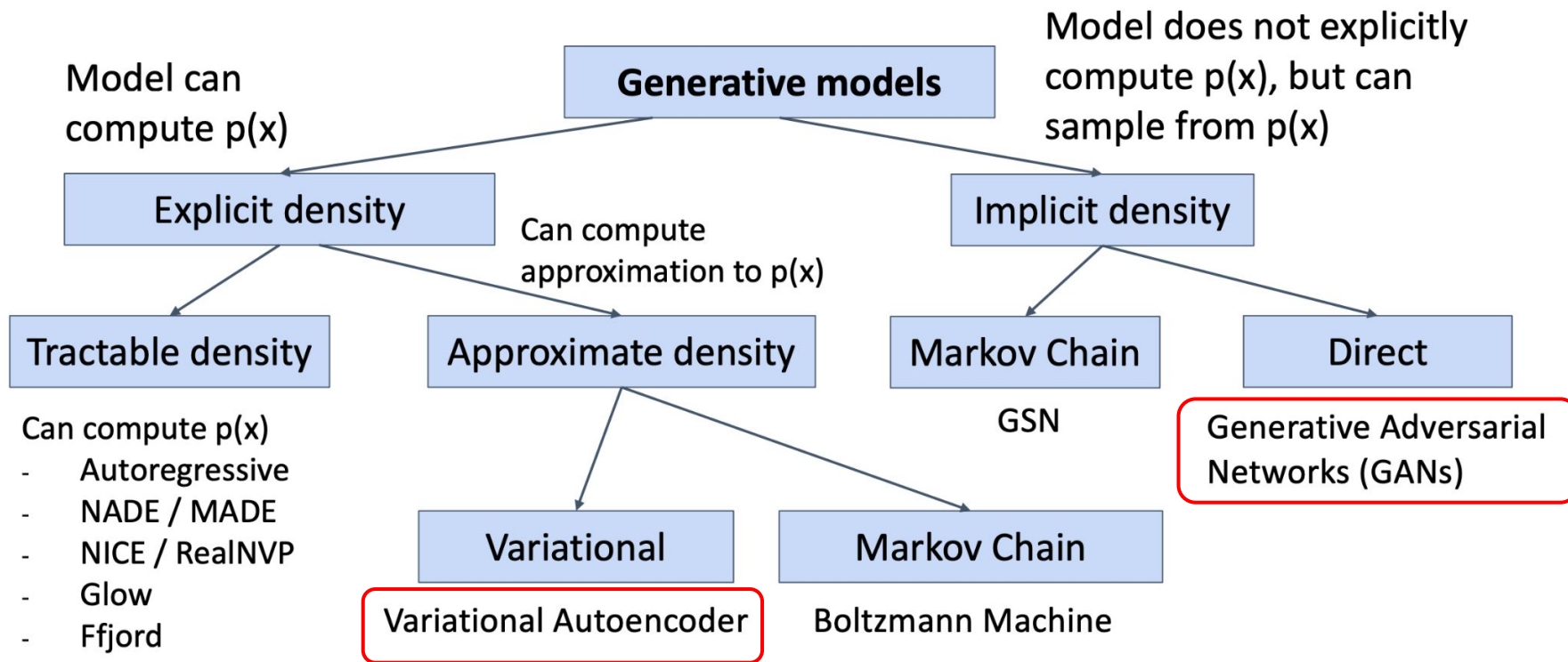


Assign labels, while rejecting outliers!
Generate new data conditioned on input labels

Taxonomy of Generative Models



Taxonomy of Generative Models

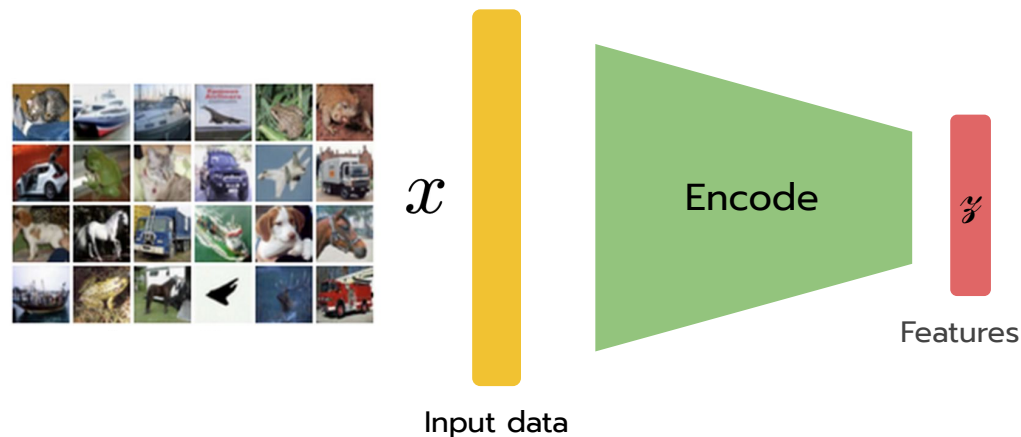


Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

Unsupervised method for learning feature vectors from raw data x , without any labels.

"Autoencoding" = encoding itself



Features should extract useful information (maybe object identities, properties, scene type, etc) that we can use for downstream tasks

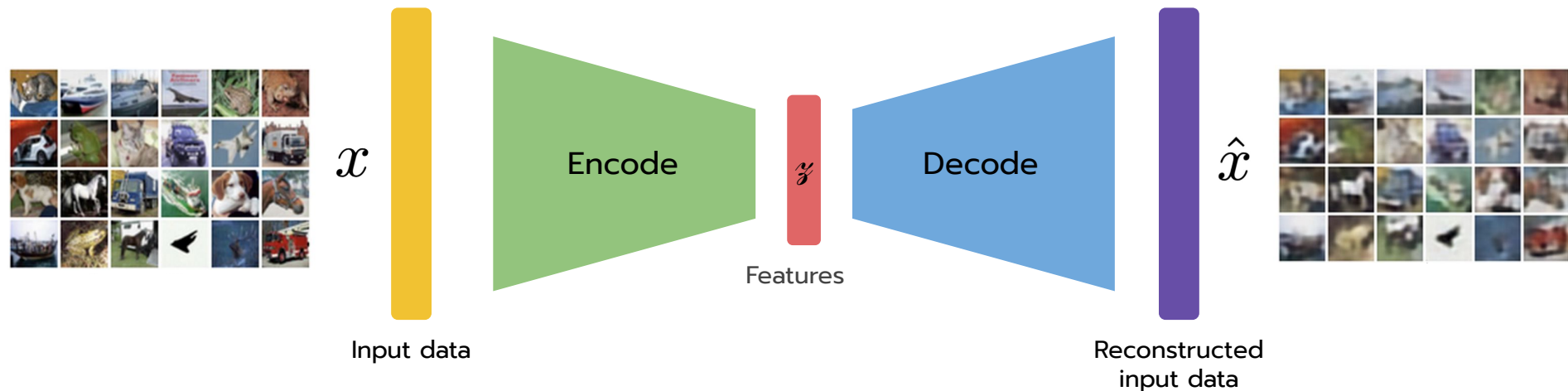
Problem: How can we learn this feature transform from raw data?

Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

Idea: Use the features to **reconstruct the input data** with a decoder

“Autoencoding” = encoding itself

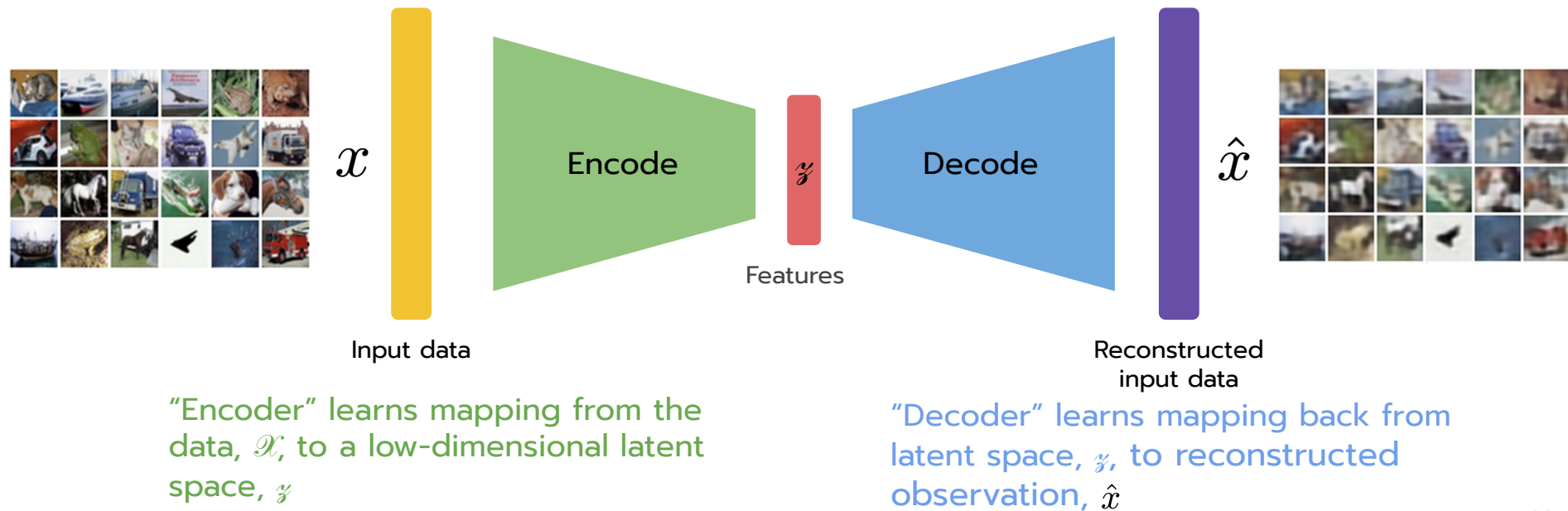


Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

Idea: Use the features to **reconstruct the input data** with a decoder

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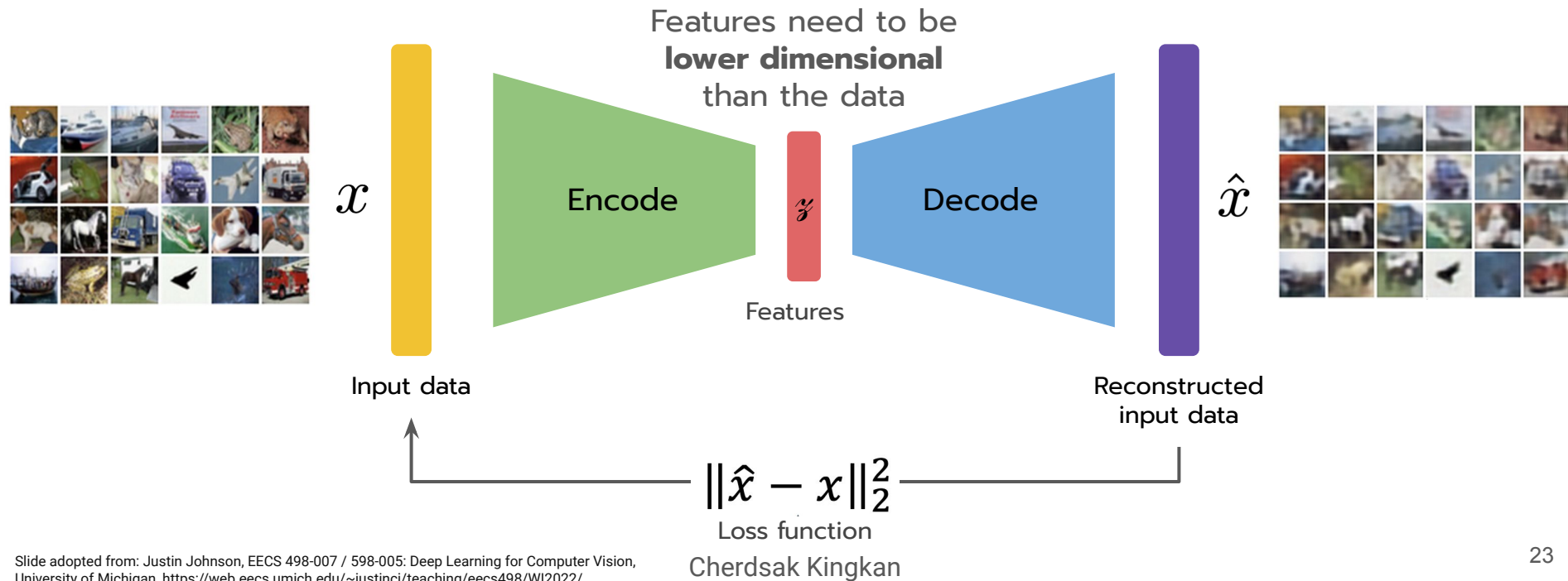


Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

Loss: L2 distance between input and reconstructed data.

Does not use any labels! Just raw data!

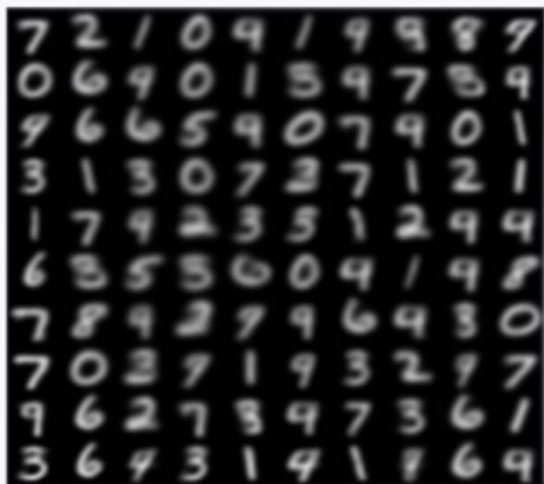


Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

Autoencoding is a form of compression! **Size of latent vector** affects the reconstructed data quality.

2D latent space



5D latent space



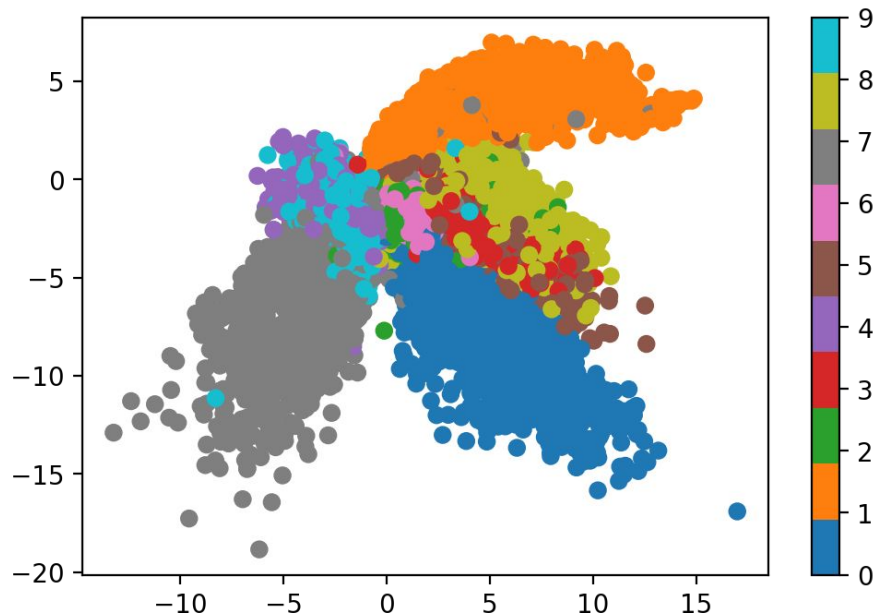
Ground truth



Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

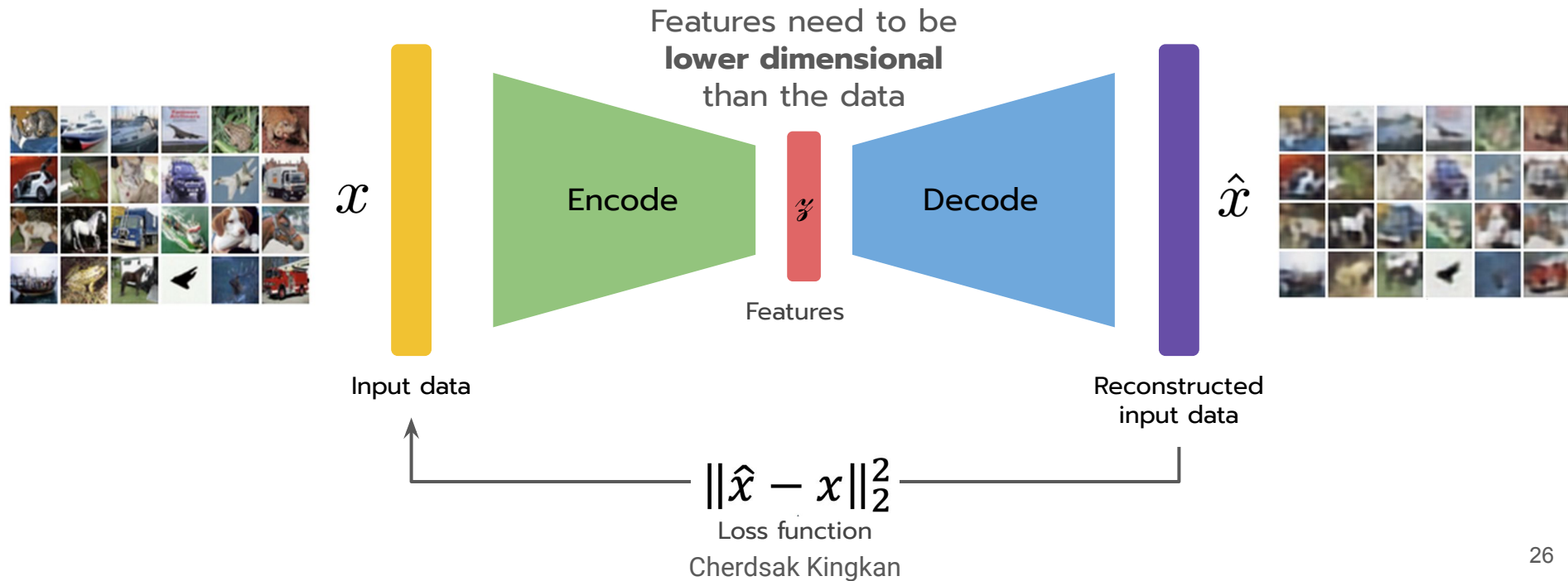
Latent Space of MNIST dataset



Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

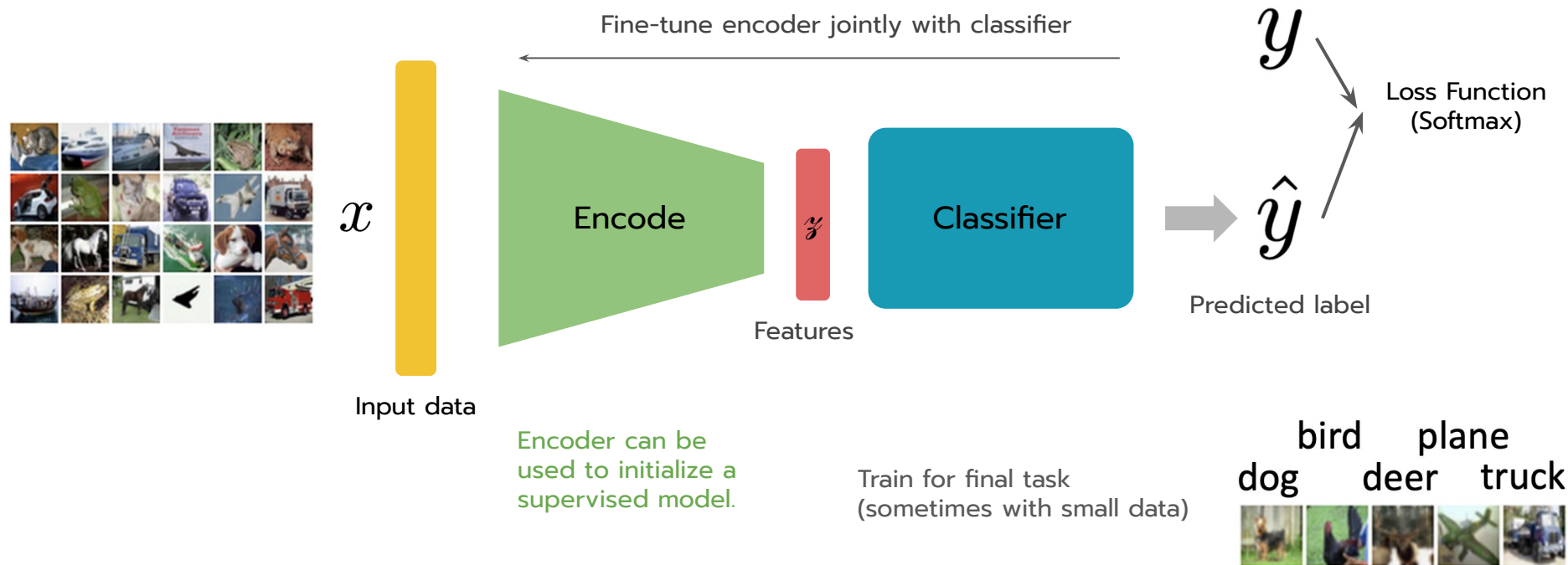
After training, **throw away decoder** and use encoder for a downstream task



Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

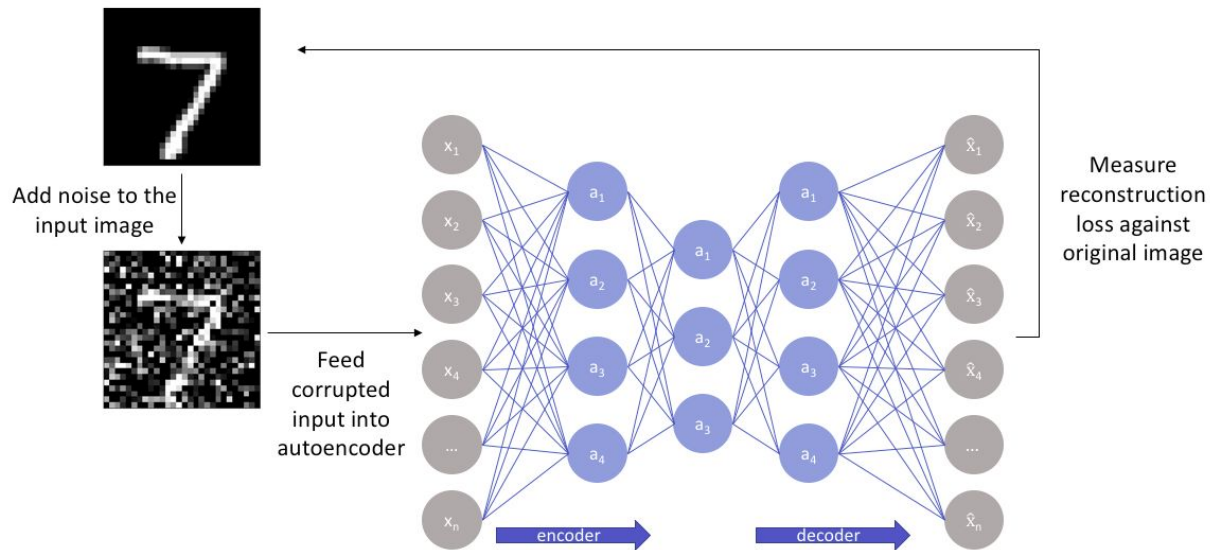
After training, **throw away decoder** and use encoder for a downstream task



Variational AUTOENCODERS

Applications

- Dimensionality Reduction and Feature Extraction
- Denoising Data
- Anomaly detections



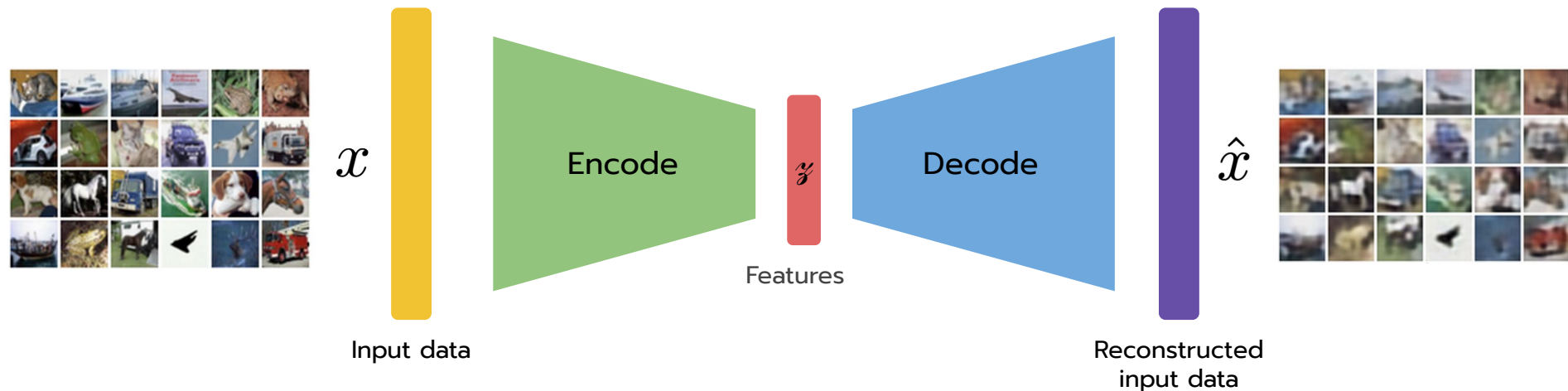
Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

Autoencoders learn **latent features** for data without any labels!

Can use features to initialize a supervised model

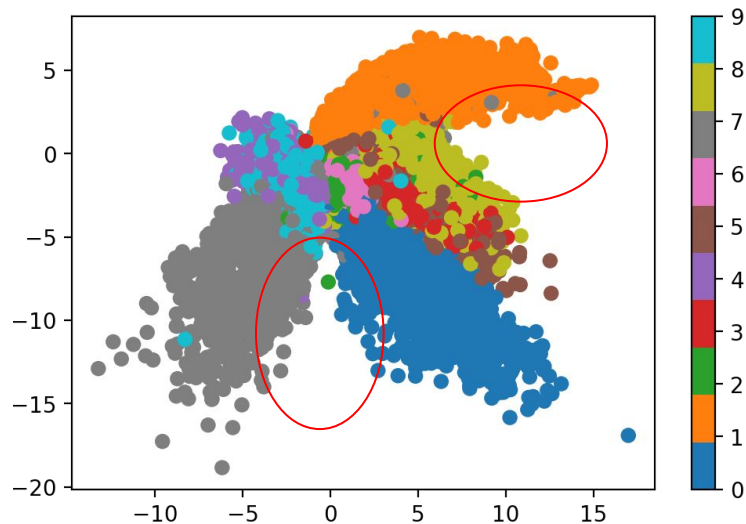
Not probabilistic: No way to sample new data from learned model



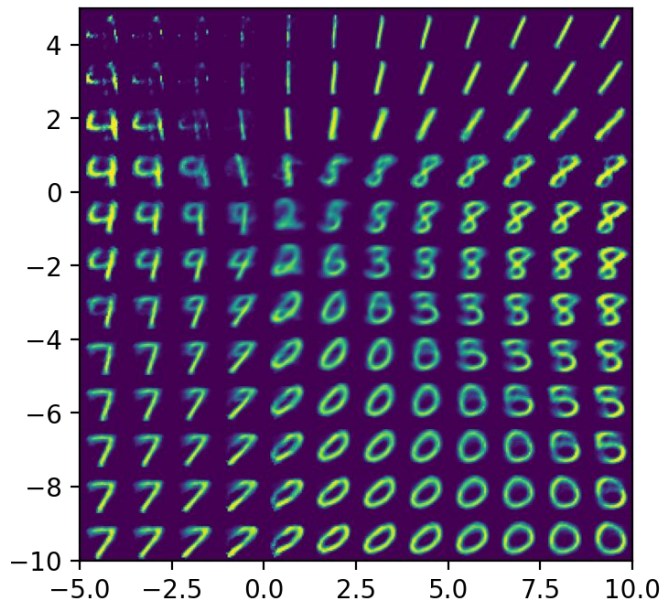
Variational AUTOENCODERS

Autoencoders (Regular, non-variational)

There are “gaps” in the latent space, where data is never mapped to.



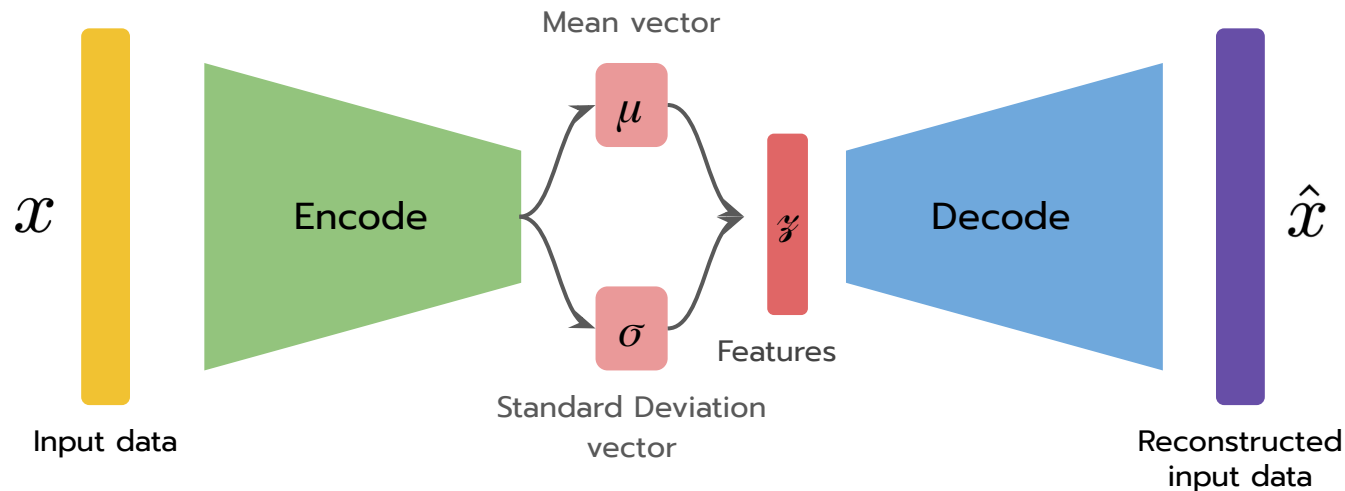
If we sample a latent vector from a **region** in the **latent space that was never seen** by the decoder during training, the output might not make any sense at all.



the latent space, \mathcal{Z} , can become **disjoint** and **non-continuous**.

Variational Autoencoder

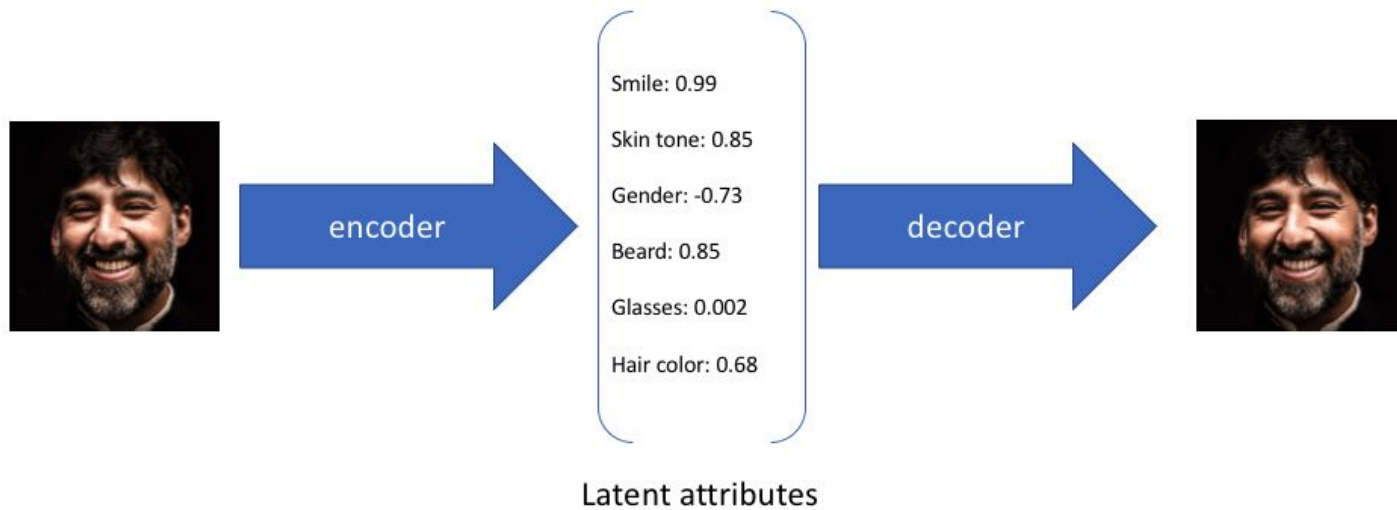
Variational autoencoders are a probabilistic twist on autoencoders!
Sample from the mean and standard deviation to compute latent sample



Overview of VAE : Instead of learning an arbitrary function, the network learns the parameters of **probability distribution** modeling the data

Variational Autoencoder

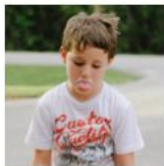
Intuition



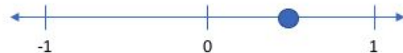
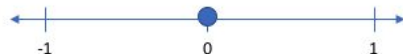
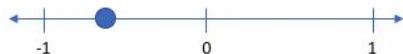
Variational Autoencoder

Intuition

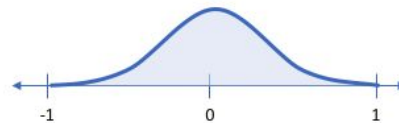
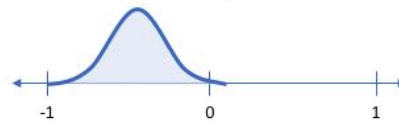
Using a variational autoencoder, we can describe latent attributes in probabilistic terms.



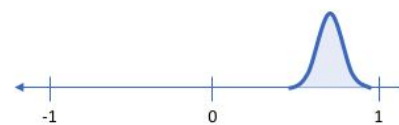
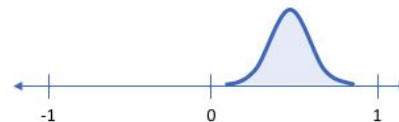
Smile (discrete value)



Smile (probability distribution)

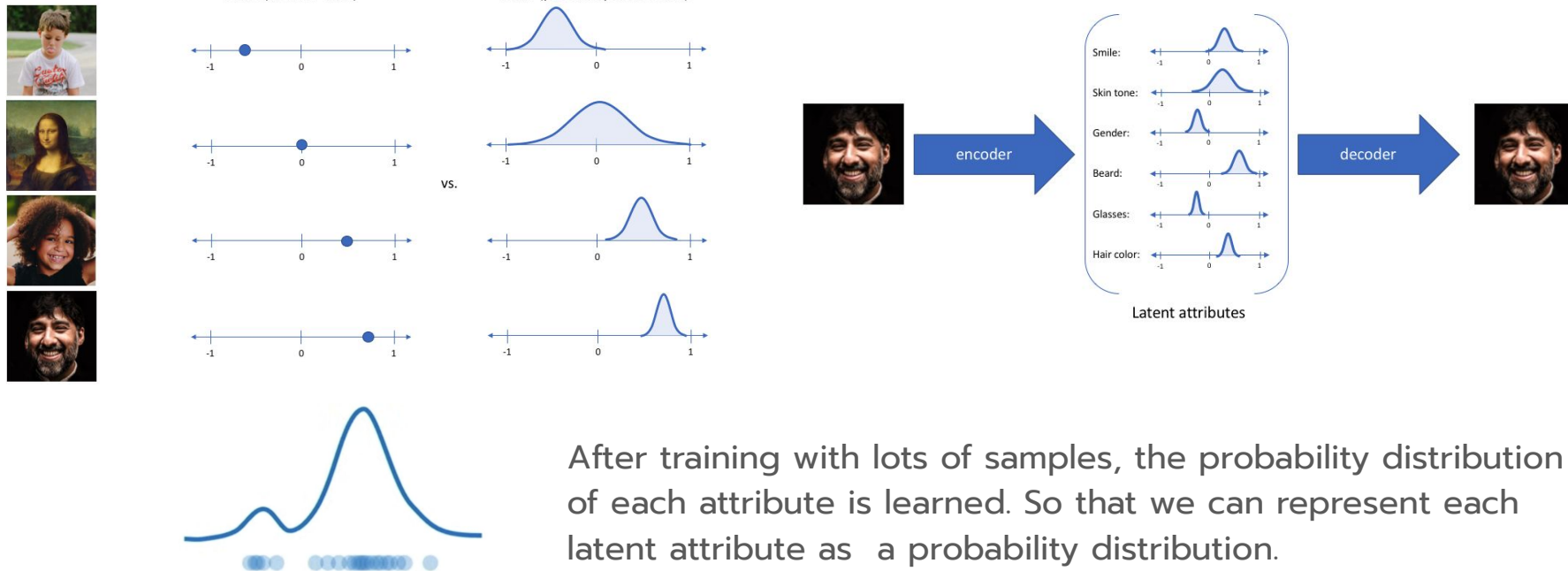


vs.



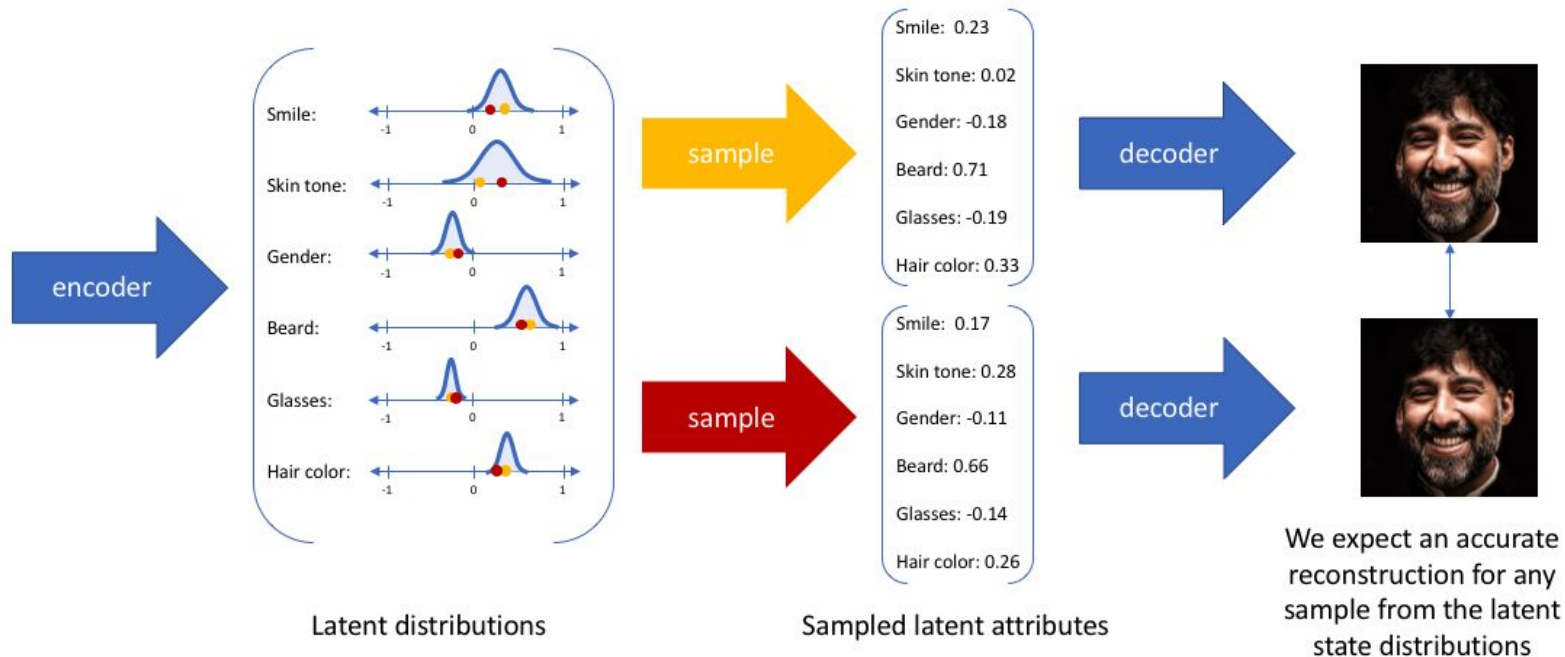
Variational Autoencoder

Intuition



Variational Autoencoder

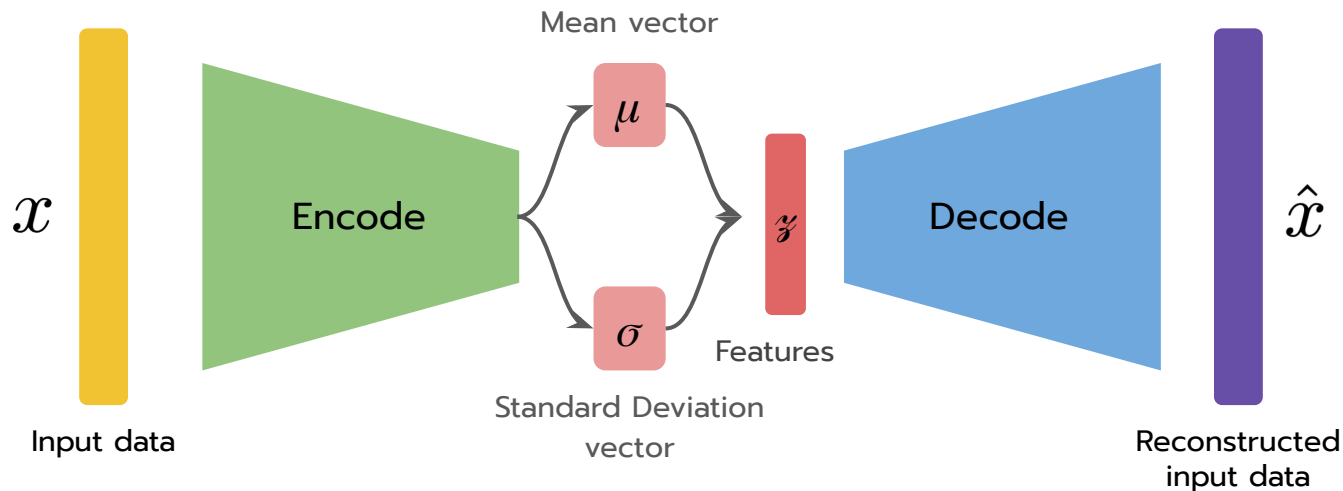
Intuition



Variational Autoencoder

Probabilistic spin on autoencoders: we want to do

1. **Learn latent features** z from raw data
2. Sample from the model to **generate new data**



Variational Autoencoder

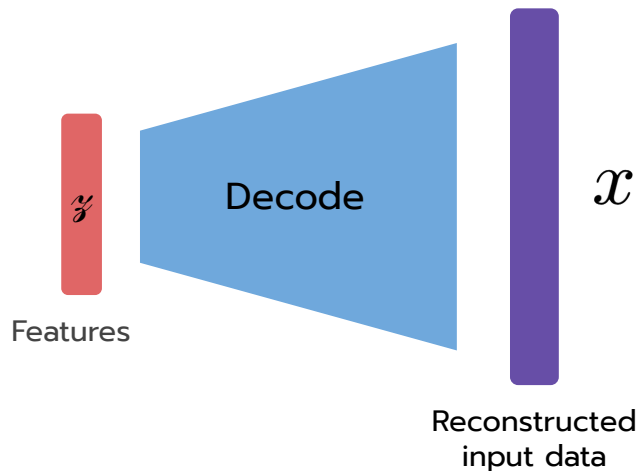
Probabilistic spin on autoencoders: we want to do

1. **Learn latent features** z from raw data
2. Sample from the model to **generate new data**

We can only see x , but we want to infer the attributes of z , i.e., we want to compute

$$p(z|x) = \frac{p(x|z)p(z)}{p(x)}$$

After training, we want to **sample** a hidden variable z which **generate** an observation x



Variational Autoencoder

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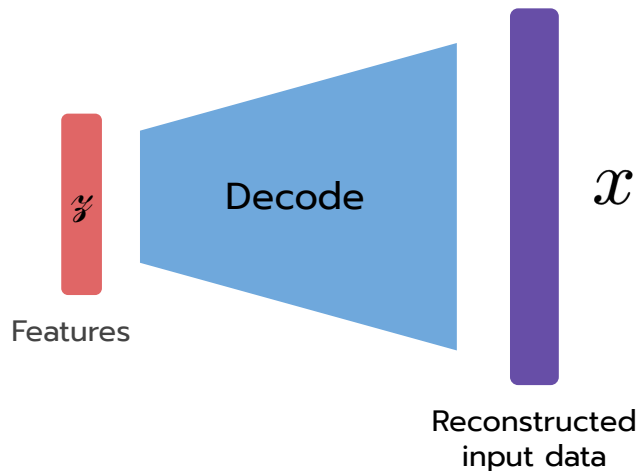
compute with
Decoder network

we assumed
Gaussian prior

$$p(z|x) = \frac{p(x|z)p(z)}{p(x)}$$

Very difficult to compute (technically possible,
but practical impossible)

After training, we want to **sample** a hidden variable z which **generate** an observation x



Variational Autoencoder

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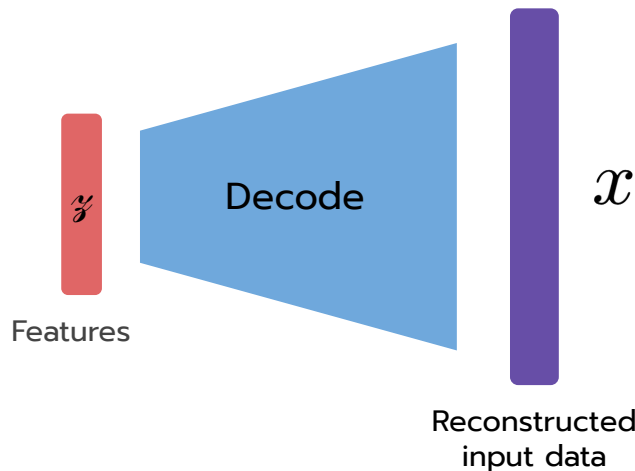
we assumed
Gaussian prior

$$p(z|x) = \frac{p(x|z)p(z)}{p(x)}$$

$$p(x) = \int p(x|z)p(z)dz$$

Impossible to integrate over all z (intractable)

After training, we want to **sample** a hidden variable z which **generate** an observation x



Variational Autoencoder

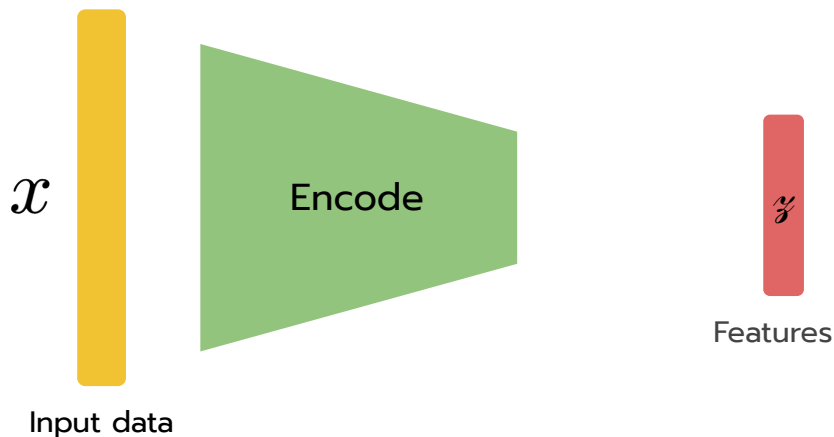
Probabilistic spin on autoencoders: we want to do

1. **Learn latent features** z from raw data
2. Sample from the model to **generate new data**

We can approximate $p(z|x)$ by another distribution $q(z|x)$, i.e.

Compute with
Encoder Network

$$q(z|x) \approx p(z|x)$$



the KL divergence is a measure of difference between two probability distributions. Thus, if we wanted to ensure that $q(z|x)$ was similar to $p(z|x)$, we could minimize the KL divergence between the two distributions.

$$\min D_{KL}(q(z|x) || p(z|x))$$

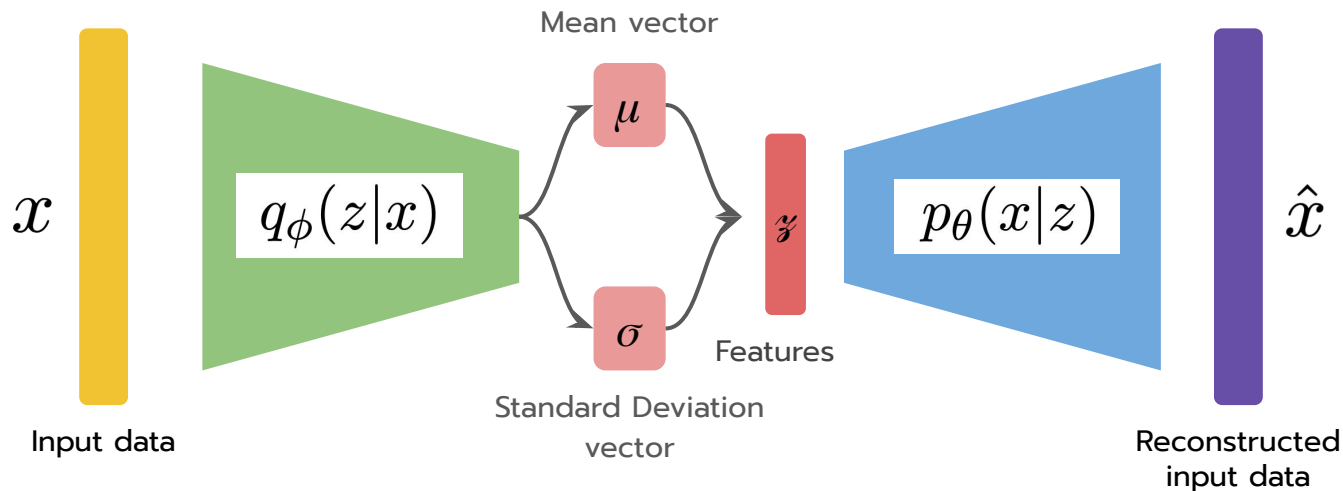
Variational Autoencoder

Common choice of prior - Gaussian Distribution

Probabilistic spin on autoencoders: we want to do

1. **Learn latent features** z from raw data
2. Sample from the model to **generate new data**

$$p(z) = \mathcal{N}(\mu, \sigma)$$



The reconstruction likelihood

$$E_{q(z|x)} \log p(x|z) - D_{KL}(q(z|x) || p(z))$$

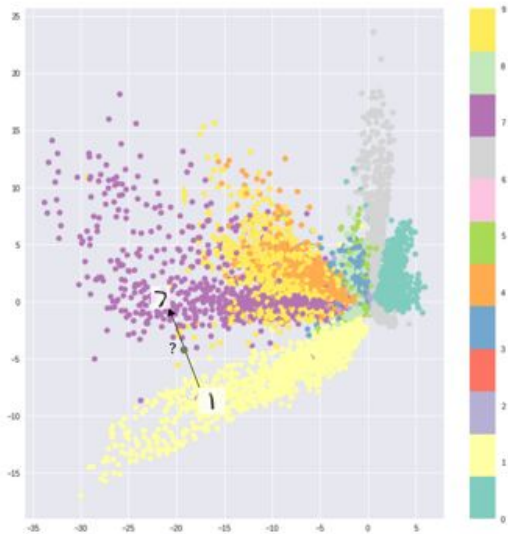
Cherdsak Kingkan

Regularization Loss: ensures that our **learned distribution** is similar to the true **prior distribution**

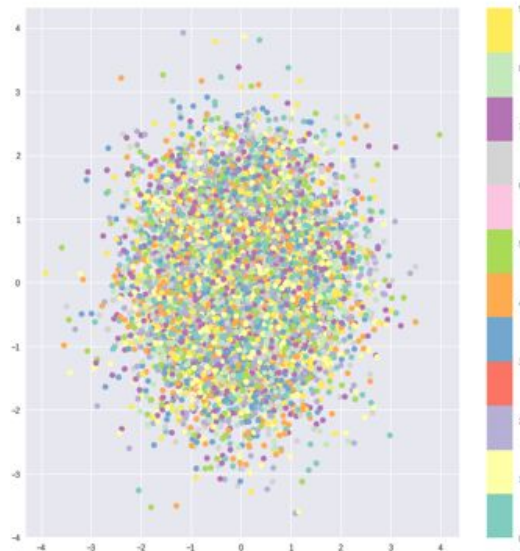
Variational Autoencoder

Why regularization term is needed

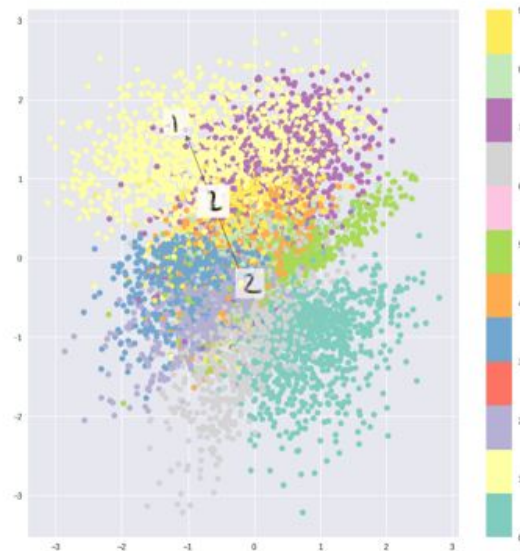
Only reconstruction loss



Only KL divergence



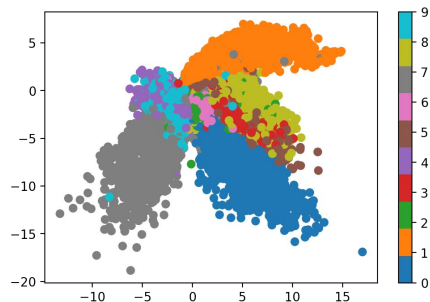
Combination



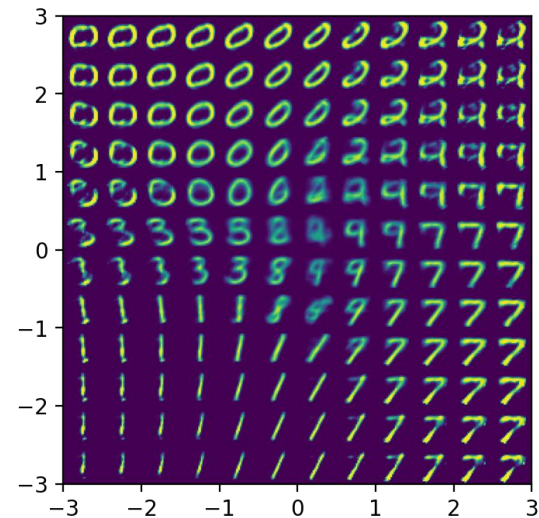
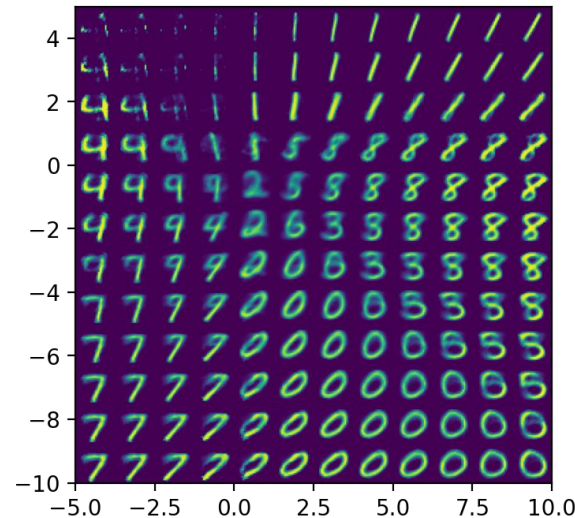
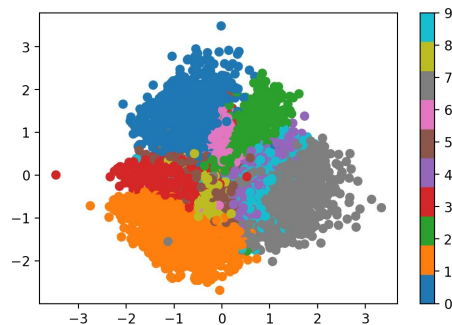
Variational Autoencoder

Why regularization term is needed

Autoencoder

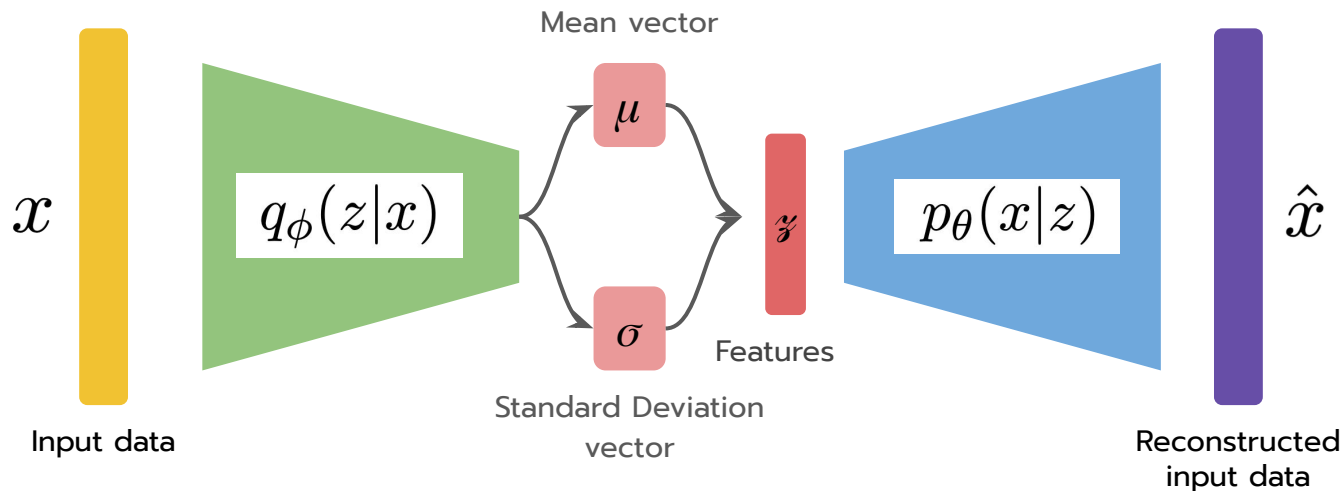


Variational Autoencoder



Variational Autoencoder

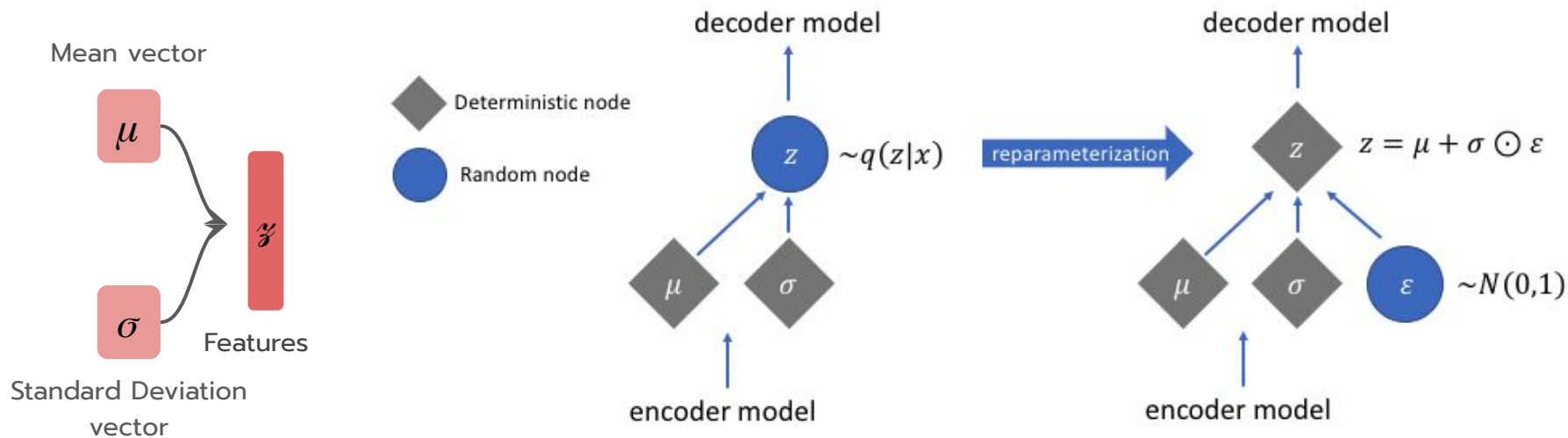
How to perform backpropagation when training the model



$$E_{q(z|x)} \log p(x|z) - D_{KL}(q(z|x)||p(z))$$

Variational Autoencoder

Reparameterization trick



Variational Autoencoder

Latent perturbation

Slowly increase or decrease a **single latent variable**. Keep all other variables fixed.

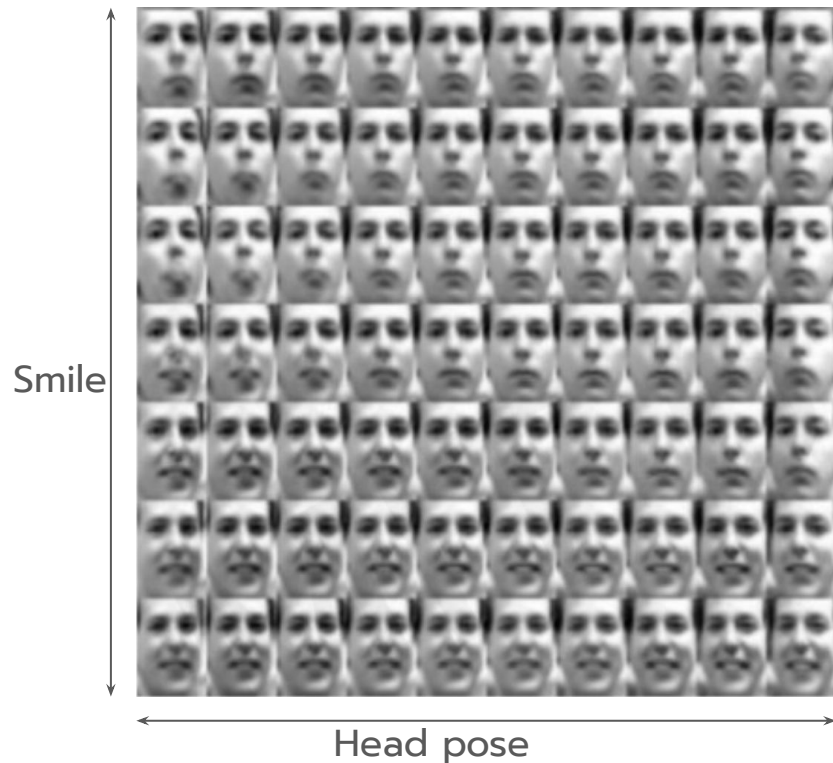


Head pose

Different dimension of z encodes **different interpretable latent features**

Variational Autoencoder

Latent perturbation



Ideally, we want latent variables that are uncorrelated with each other.

Enforce diagonal prior on the latent variables to encourage independence

Disentanglement

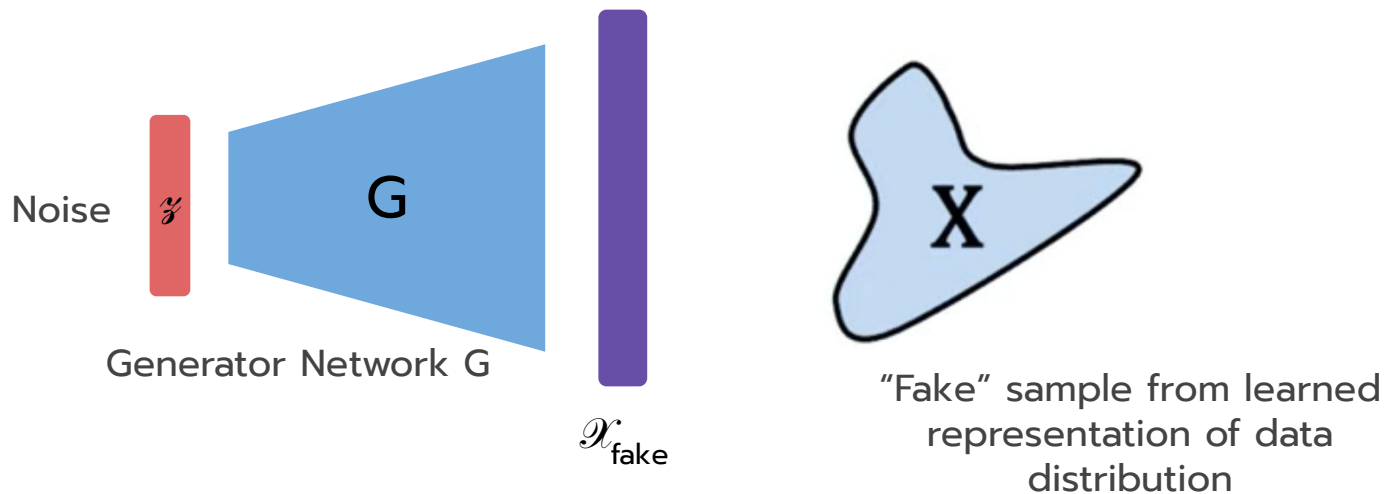
Generative Adversarial Network (GAN)

What if we just want to sample

Idea: do not explicitly model density, and instead just sample to generate new instances.

Problem: want to sample from complex distribution - cannot do this directly

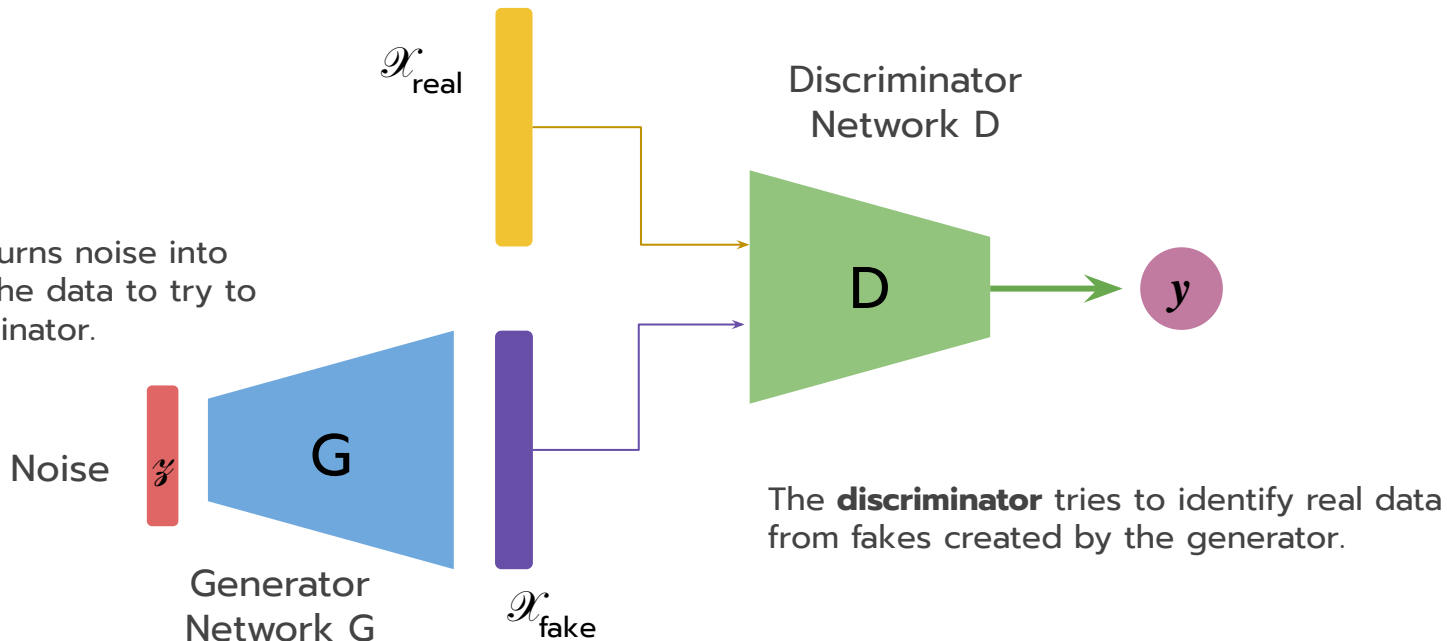
Solution: sample from something simple (e.g., noise), learn a transformation to the data distribution.



Generative Adversarial Networks (GANs)

GANs are a way to make a generative model by having two neural networks compete with each other

The **generator** turns noise into an imitation of the data to try to trick the discriminator.



Generative Adversarial Network (GAN)

Intuition behind GANs

Discriminator looks at both real and fake data created by the generator

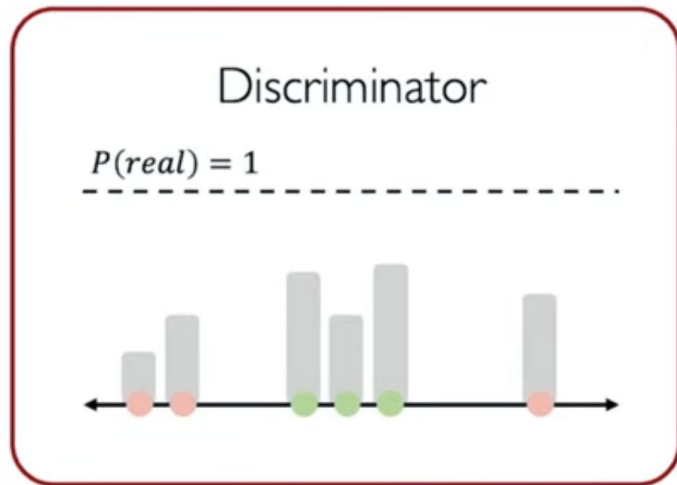
Generator starts from noise to try to create an imitation of the data



Generative Adversarial Network (GAN)

Intuition behind GANs

Discriminator tries to predict what's real and what's fake



Generator starts from noise to try to create an imitation of the data

Generator



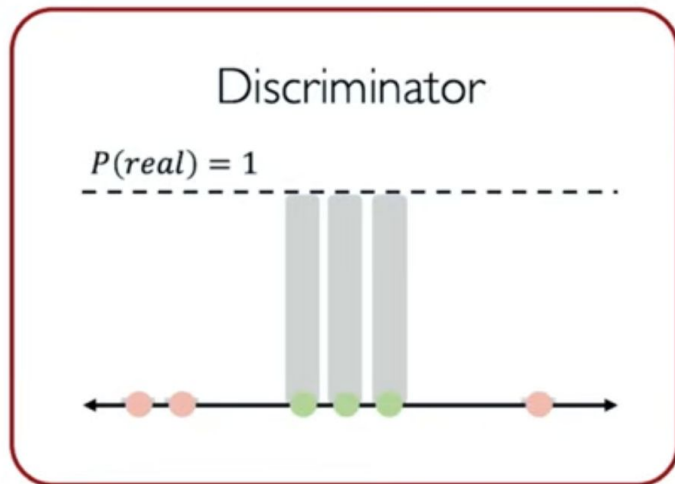
● Real data

● Fake data

Generative Adversarial Network (GAN)

Intuition behind GANs

Discriminator tries to predict what's real and what's fake



Generator starts from noise to try to create an imitation of the data

Generator



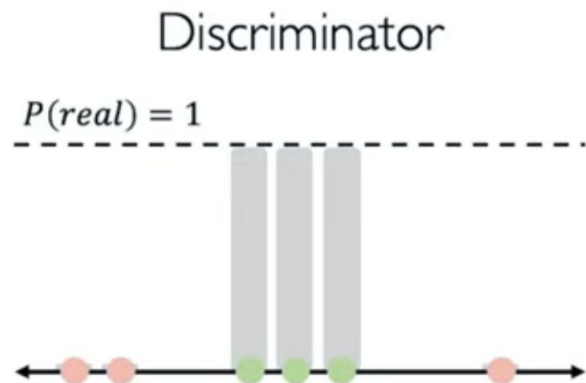
● Real data

● Fake data

Generative Adversarial Network (GAN)

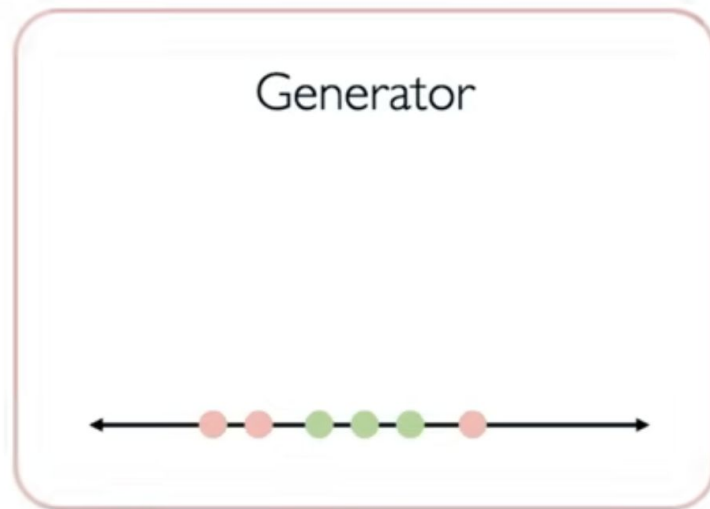
Intuition behind GANs

Discriminator tries to predict what's real and what's fake



● Real data

Generator tries to improve its imitation of the data



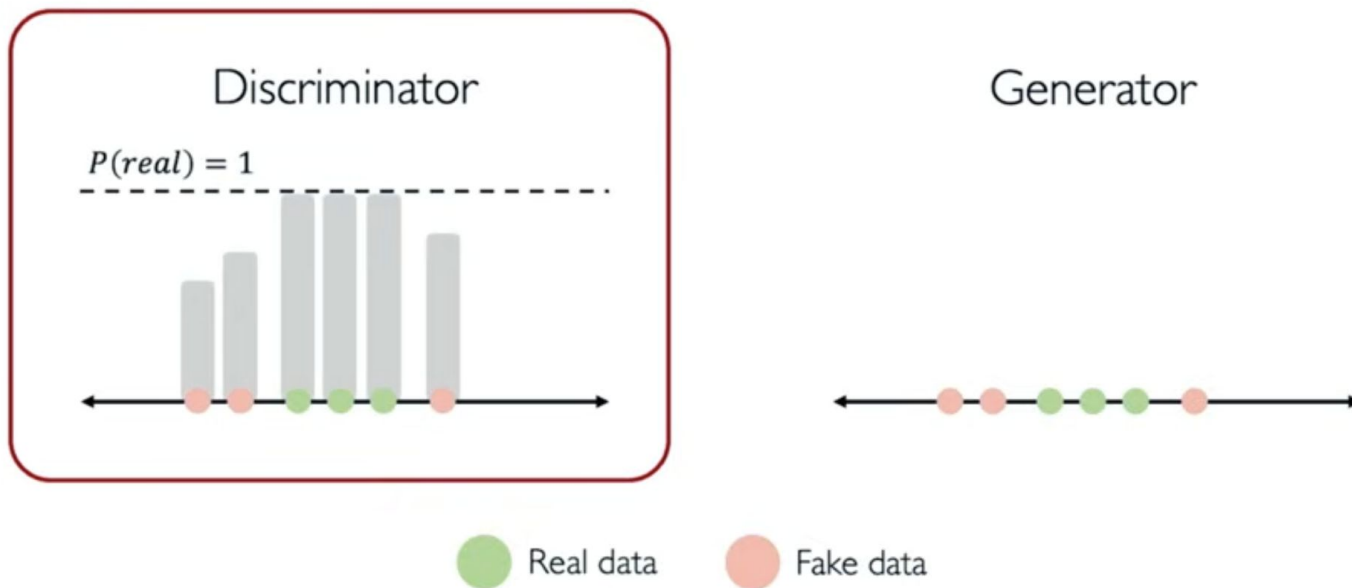
● Fake data

Generative Adversarial Network (GAN)

Intuition behind GANs

Discriminator tries to predict what's real and what's fake

Generator tries to improve its imitation of the data



Generative Adversarial Network (GAN)

Intuition behind GANs

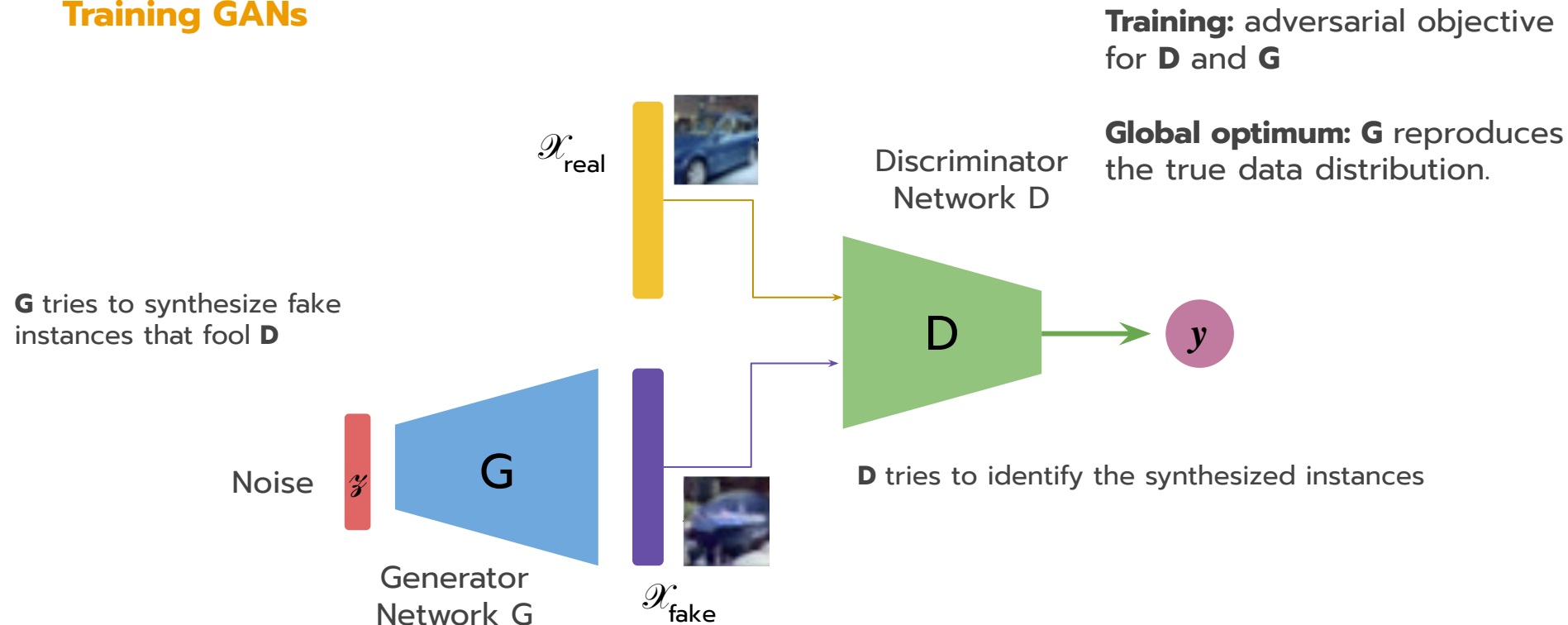
Discriminator tries to identify real data from fakes created by the generator.

Generator tries to create imitations of data to trick the discriminator.



Generative Adversarial Networks (GANs)

Training GANs



Generative Adversarial Networks (GANs)

Training GANs

Jointly train generator G and discriminator D with a **minimax game**

Discriminator wants
 $D(x) = 1$ for real data

Discriminator wants $D(x)$
 $= 0$ for fake data

$$\min_G \max_D \left(\overbrace{E_{x \sim p_{data}} [\log D(x)]}^{\text{Discriminator wants } D(x)=1 \text{ for real data}} + E_{z \sim p(z)} \left[\overbrace{\log (1 - D(G(z)))}^{\text{Discriminator wants } D(x)=0 \text{ for fake data}} \right] \right)$$

Generator wants $D(x) = 1$
for fake data

Generative Adversarial Networks (GANs)

Training GANs

Jointly train generator G and discriminator D with a **minimax game**

Training G and D using alternating gradient updates

$$\min_G \max_D \left(E_{x \sim p_{data}} [\log D(x)] + E_{z \sim p(z)} [\log (1 - D(G(z)))] \right)$$

$$= \min_G \max_D V(G, D)$$

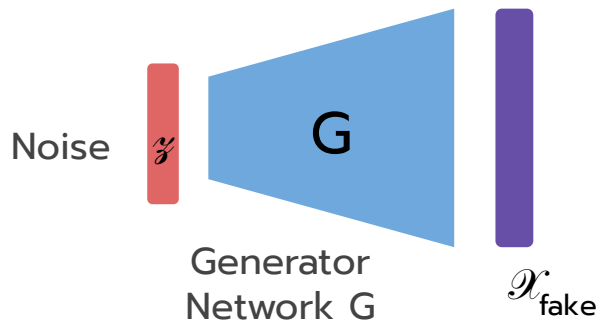
For t in $1, \dots, T$:

1. (Update D) $D = D + \alpha_D \frac{\partial V}{\partial D}$
2. (Update G) $G = G - \alpha_G \frac{\partial V}{\partial G}$

Generative Adversarial Network (GAN)

Generating new data with GANs

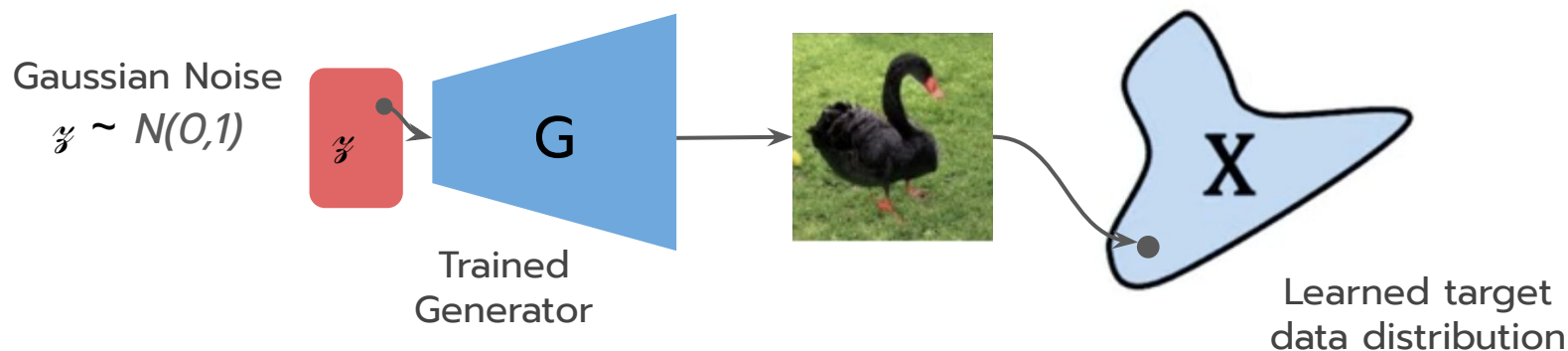
After training, use generator network to create **new data** that's never been seen before.



Generative Adversarial Network (GAN)

GANs are distribution transformers

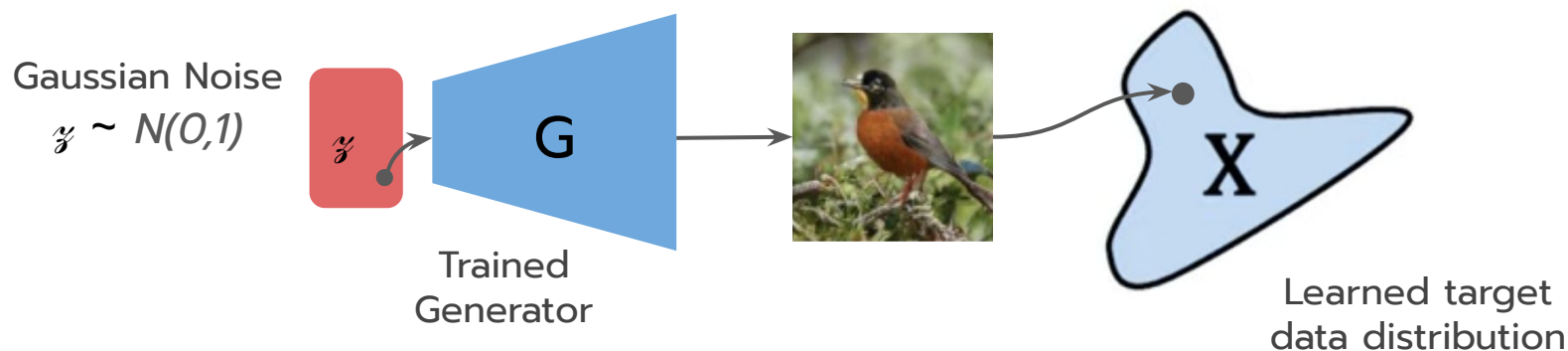
After training, use generator network to create **new data** that's never been seen before.



Generative Adversarial Network (GAN)

GANs are distribution transformers

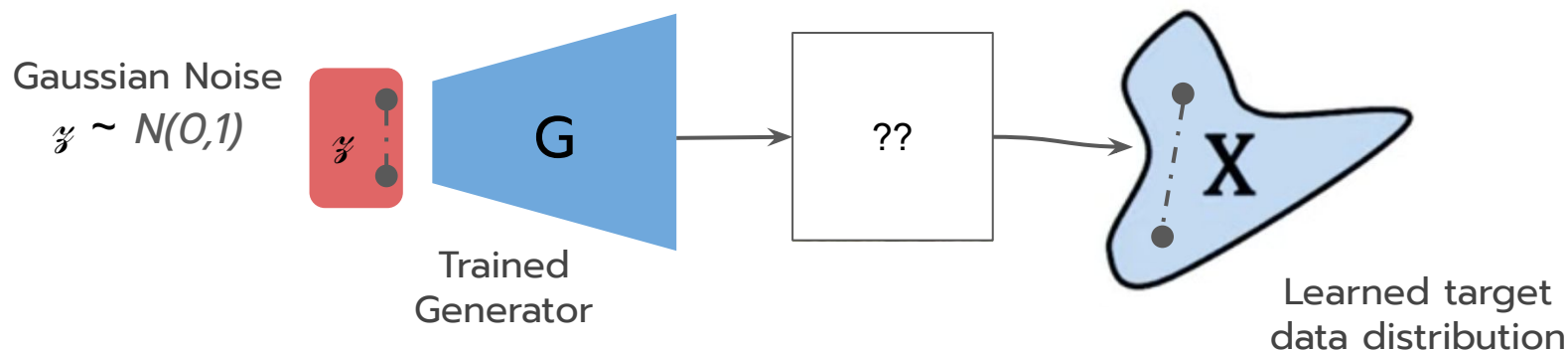
After training, use generator network to create **new data** that's never been seen before.



Generative Adversarial Network (GAN)

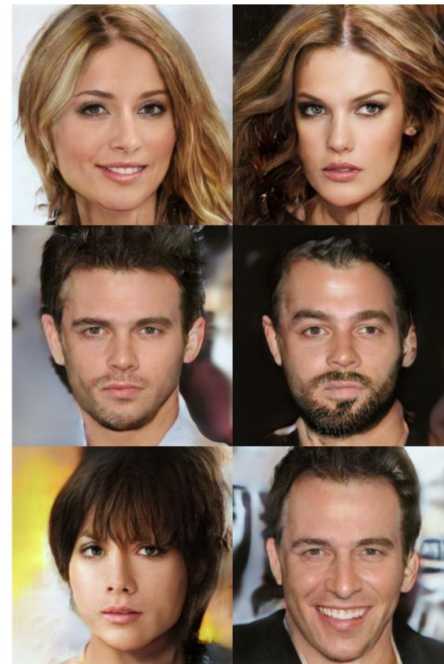
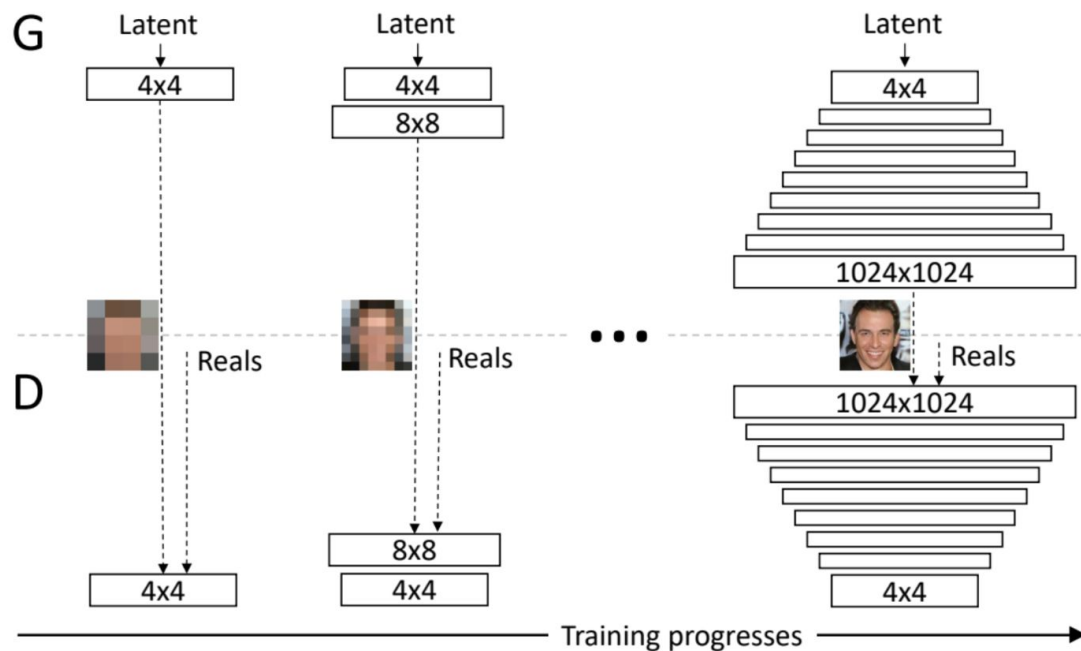
GANs are distribution transformers

After training, use generator network to create **new data** that's never been seen before.



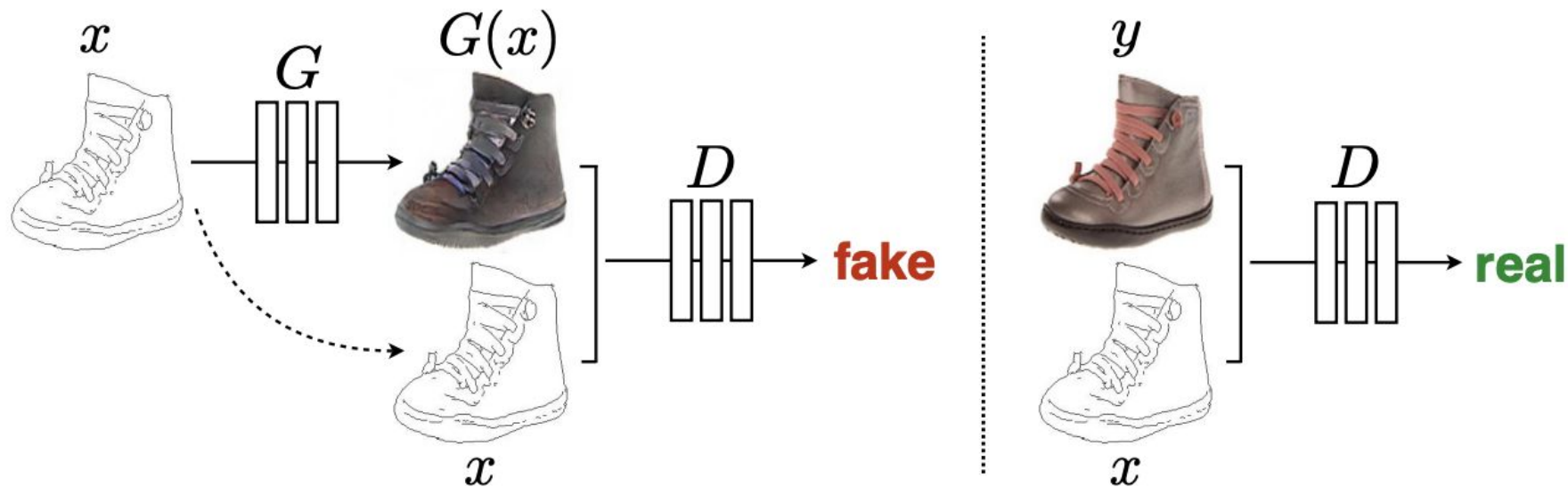
Generative Adversarial Network (GAN)

Applications - Progressively Growing GAN



Generative Adversarial Network (GAN)

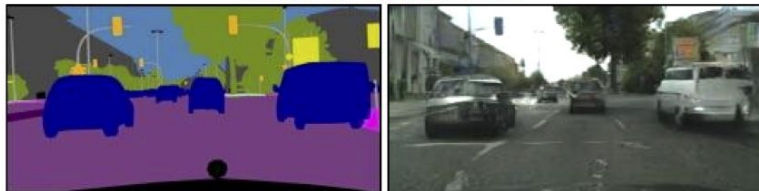
Applications - Conditional GAN



Generative Adversarial Network (GAN)

Applications - Conditional GAN

Labels to Street Scene



input

output

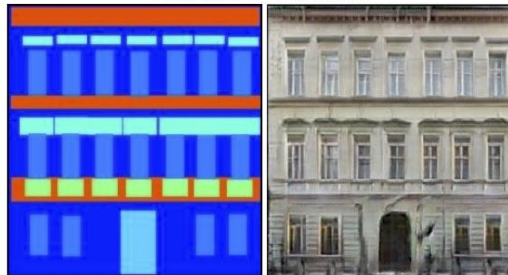
Aerial to Map



input

output

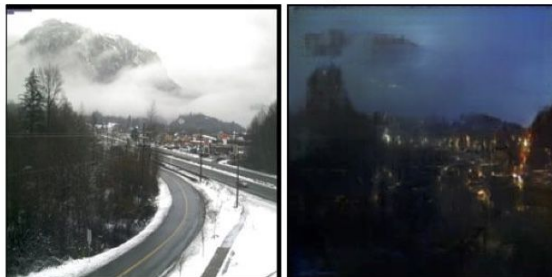
Labels to Facade



input

output

Day to Night



input

output

BW to Color



input

output

Edges to Photo



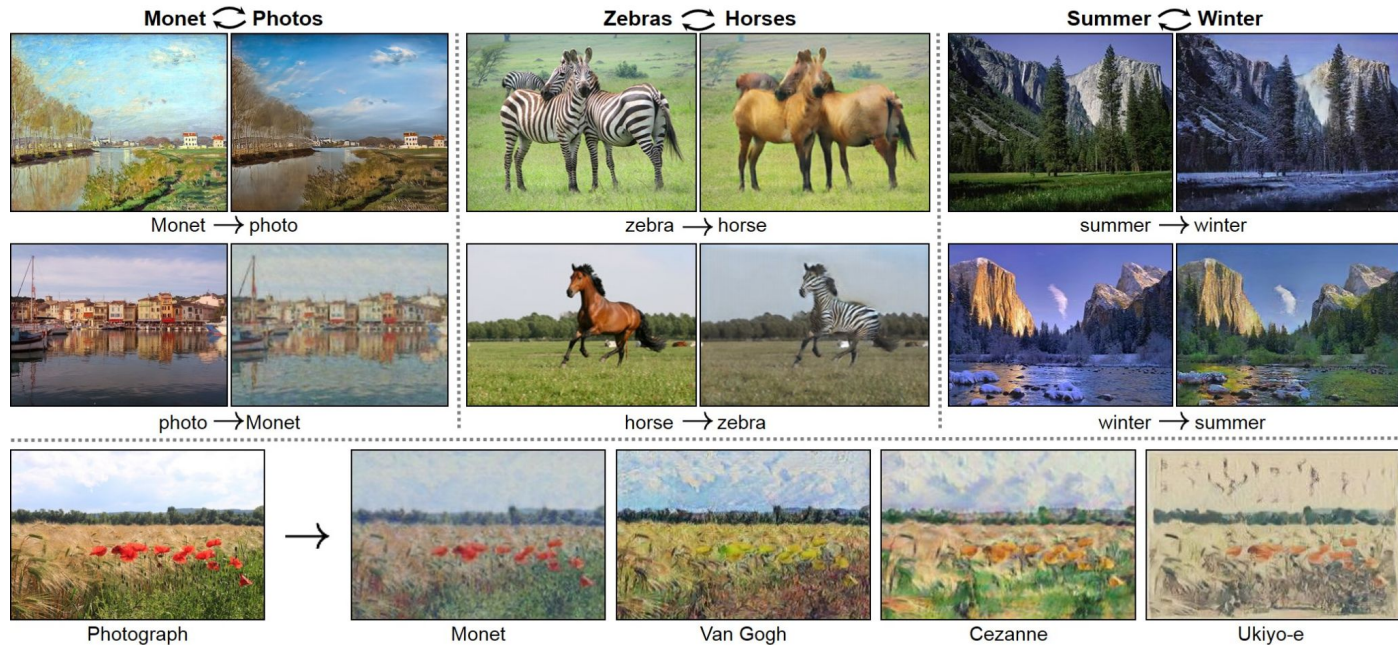
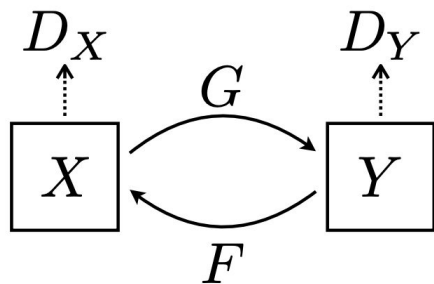
input

output

Generative Adversarial Network (GAN)

Applications - Cycle GAN

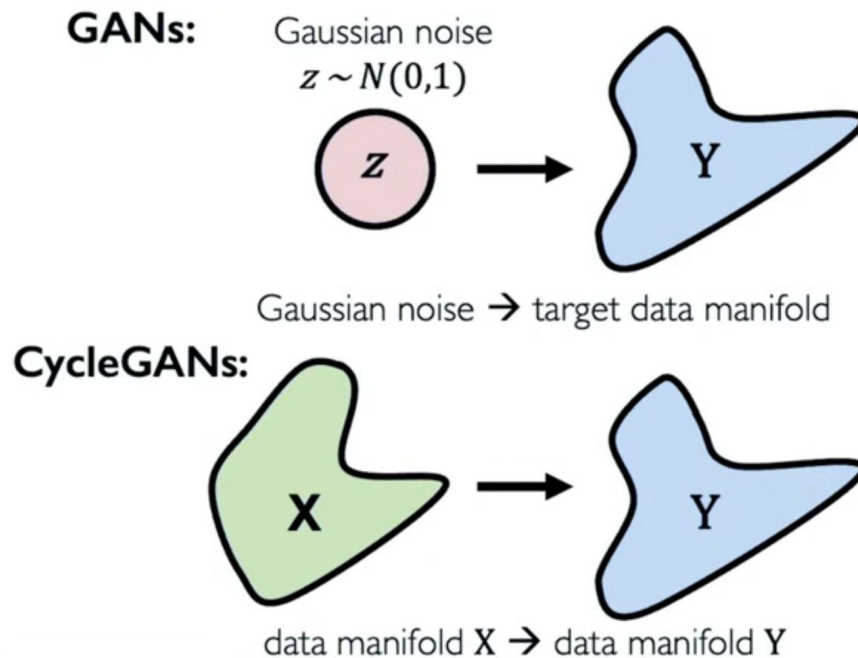
Domain transformation: CycleGAN learns transformations across domains with unpaired data.



Generative Adversarial Network (GAN)

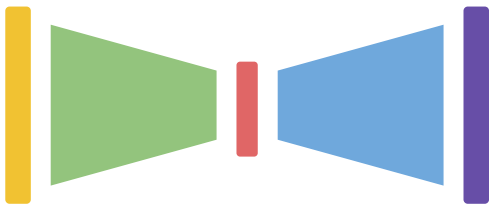
Applications - Cycle GAN

Distribution transformations.

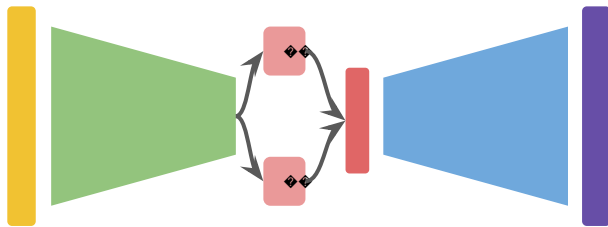


Summarize

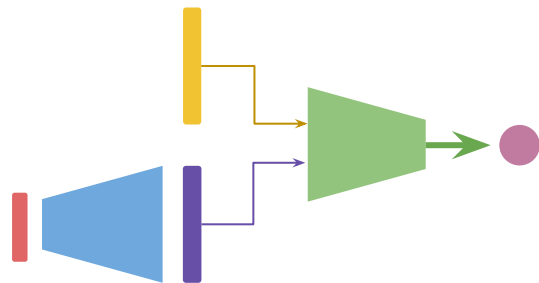
Autoencoder (AE)



Variational Autoencoder (VAE)



Generative Adversarial Network (GAN)



Announcement

November 2, 2024

- No lecture

BUT

- **There is a Lab session**
 - **k-Means**
 - **Mean Shift**
 - **UNet**
 - **AE/VAE**
 - **GAN**