# READING TEST SCORES

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# Load the training and testing sets

pisaTrain=read.csv("pisa2009train.csv")
pisaTest=read.csv("pisa2009test.csv")
summary(pisaTrain)

```
##
       grade
                         male
                                                   raceeth
##
   Min. : 8.00
                   Min.
                          :0.0000
                                     White
                                                       :2015
                   1st Ou.:0.0000
##
   1st Ou.:10.00
                                     Hispanic
                                                       : 834
   Median :10.00
                   Median :1.0000
##
                                     Black
                                                       : 444
##
          :10.09
                   Mean
                           :0.5111
                                     Asian
   Mean
                                                       : 143
##
   3rd Qu.:10.00
                    3rd Qu.:1.0000
                                     More than one race: 124
                    Max.
##
   Max.
          :12.00
                           :1.0000
                                     (Other)
                                                       : 68
##
                                     NA's
                                                       : 35
##
     preschool
                     expectBachelors
                                         motherHS
                                                     motherBachelors
##
   Min.
                                      Min. :0.00
                                                            :0.0000
          :0.0000
                    Min.
                            :0.0000
                                                   Min.
##
   1st Qu.:0.0000
                     1st Qu.:1.0000
                                      1st Qu.:1.00
                                                    1st Qu.:0.0000
   Median :1.0000
                    Median :1.0000
##
                                      Median :1.00
                                                     Median : 0.0000
##
   Mean
          :0.7228
                    Mean
                          :0.7859
                                      Mean :0.88
                                                     Mean
                                                           :0.3481
   3rd Ou.:1.0000
                     3rd Ou.:1.0000
##
                                      3rd Ou.:1.00
                                                     3rd Ou.:1.0000
   Max.
                                      Max.
                                                     Max.
##
          :1.0000
                     Max.
                           :1.0000
                                            :1.00
                                                            :1.0000
##
   NA's
          :56
                     NA's
                            :62
                                      NA's
                                           :97
                                                     NA's
                                                           :397
##
     motherWork
                                      fatherBachelors
                                                         fatherWork
                        fatherHS
                                                       Min. :0.0000
   Min. :0.0000
                          :0.0000
                                      Min. :0.0000
##
                    Min.
   1st Qu.:0.0000
                     1st Qu.:1.0000
                                      1st Qu.:0.0000
                                                       1st Qu.:1.0000
##
##
   Median :1.0000
                    Median :1.0000
                                      Median :0.0000
                                                       Median :1.0000
                                                      Mean :0.8531
          :0.7345
                    Mean :0.8593
                                      Mean :0.3319
##
   Mean
   3rd Qu.:1.0000
                     3rd Qu.:1.0000
                                      3rd Qu.:1.0000
##
                                                       3rd Qu.:1.0000
##
   Max.
          :1.0000
                     Max.
                            :1.0000
                                      Max.
                                             :1.0000
                                                       Max.
                                                               :1.0000
##
   NA's
          :93
                     NA's
                            :245
                                      NA's
                                             :569
                                                       NA's
                                                             :233
##
     selfBornUS
                     motherBornUS
                                      fatherBornUS
                                                       englishAtHome
##
   Min.
          :0.0000
                     Min.
                            :0.0000
                                      Min.
                                             :0.0000
                                                       Min.
                                                               :0.0000
   1st Qu.:1.0000
                     1st Qu.:1.0000
                                      1st Qu.:1.0000
                                                       1st Qu.:1.0000
##
   Median :1.0000
                    Median :1.0000
                                      Median :1.0000
                                                       Median :1.0000
##
   Mean
          :0.9313
                            :0.7725
                                             :0.7668
                                                       Mean :0.8717
                    Mean
                                      Mean
##
   3rd Qu.:1.0000
                     3rd Qu.:1.0000
                                      3rd Qu.:1.0000
                                                       3rd Qu.:1.0000
##
   Max.
          :1.0000
                     Max.
                            :1.0000
                                      Max.
                                             :1.0000
                                                       Max.
                                                               :1,0000
                     NA's
                            :71
                                             :113
                                                       NA's
                                                              :71
##
   NA's
          :69
                                      NA's
                                           minutesPerWeekEnglish
   computerForSchoolwork read30MinsADay
##
##
   Min.
          :0.0000
                          Min.
                                 :0.0000
                                           Min.
                                                 :
                                                      0.0
##
   1st Ou.:1.0000
                          1st Ou.:0.0000
                                           1st Ou.: 225.0
                          Median :0.0000
##
   Median :1.0000
                                           Median : 250.0
##
   Mean
          :0.8994
                          Mean
                                 :0.2899
                                           Mean
                                                  : 266.2
##
   3rd Ou.:1.0000
                          3rd Qu.:1.0000
                                           3rd Ou.: 300.0
          :1.0000
                                                  :2400.0
##
   Max.
                          Max.
                                 :1.0000
                                           Max.
##
   NA's
           :65
                          NA's
                                 :34
                                           NA's
                                                  :186
##
   studentsInEnglish schoolHasLibrary publicSchool
                                                            urban
                             :0.0000
##
   Min.
          : 1.0
                     Min.
                                       Min.
                                              :0.0000
                                                        Min.
                                                               :0.0000
##
   1st Qu.:20.0
                      1st Qu.:1.0000
                                      1st Qu.:1.0000
                                                        1st Qu.:0.0000
   Median :25.0
                      Median :1.0000
                                     Median :1.0000 Median :0.0000
##
   Mean
          :24.5
                     Mean
                             :0.9676
                                              :0.9339
                                                       Mean
                                                                :0.3849
##
                                       Mean
##
   3rd Qu.:30.0
                      3rd Qu.:1.0000
                                     3rd Qu.:1.0000
                                                        3rd Qu.:1.0000
##
          :75.0
                             :1.0000
                                       Max. :1.0000
                                                               :1.0000
   Max.
                     Max.
                                                        Max.
##
   NA's
          :249
                      NA's
                             :143
```

```
## schoolSize readingScore
## Min. : 100 Min. :168.6
## 1st Qu.: 712 1st Qu.:431.7
## Median :1212 Median :499.7
## Mean :1369 Mean :497.9
## 3rd Qu.:1900 3rd Qu.:566.2
## Max. :6694 Max. :746.0
## NA's :162
```

```
str(pisaTrain)
```

```
## 'data.frame': 3663 obs. of 24 variables:
## $ grade
                        : int 11 11 9 10 10 10 10 10 9 10 ...
                        : int 1 1 1 0 1 1 0 0 0 1 ...
## $ male
## $ raceeth
                        : Factor w/ 7 levels "American Indian/Alaska Nativ
e",..: NA 7 7 3 4 3 2 7 7 5 ...
   $ preschool
                       : int NA 0 1 1 1 1 0 1 1 1 ...
  $ expectBachelors
                       : int 0 0 1 1 0 1 1 1 0 1 ...
  $ motherHS
                        : int NA 1 1 0 1 NA 1 1 1 1 ...
  $ motherBachelors : int NA 1 1 0 0 NA 0 0 NA 1 ...
                       : int 1 1 1 1 1 1 1 0 1 1 ...
  $ motherWork
  $ fatherHS
                       : int NA 1 1 1 1 1 NA 1 0 0 ...
  $ fatherBachelors : int NA 0 NA 0 0 0 NA 0 NA 0 ...
  $ fatherWork
                       : int 1 1 1 1 0 1 NA 1 1 1 ...
## $ selfBornUS
                       : int 1 1 1 1 1 1 0 1 1 1 ...
  $ motherBornUS
                       : int 0 1 1 1 1 1 1 1 1 1 ...
  $ fatherBornUS
                       : int 0 1 1 1 0 1 NA 1 1 1 ...
## $ englishAtHome
                    : int 0 1 1 1 1 1 1 1 1 ...
  $ computerForSchoolwork: int 1 1 1 1 1 1 1 1 1 1 ...
                    : int 0 1 0 1 1 0 0 1 0 0 ...
## $ read30MinsADay
## $ minutesPerWeekEnglish: int 225 450 250 200 250 300 250 300 378 294 ...
  $ studentsInEnglish : int NA 25 28 23 35 20 28 30 20 24 ...
  $ schoolHasLibrary
                       : int 1 1 1 1 1 1 1 1 0 1 ...
  $ publicSchool
                       : int 1 1 1 1 1 1 1 1 1 ...
## $ urban
                        : int 1 0 0 1 1 0 1 0 1 0 ...
## $ schoolSize
                       : int 673 1173 1233 2640 1095 227 2080 1913 502 89
## $ readingScore : num 476 575 555 458 614 ...
```

## Average reading test score of males and females

Male - 1 Female - 0

```
tapply(pisaTrain$readingScore,pisaTrain$male,mean,na.rm=TRUE)
```

```
## 0 1
## 512.9406 483.5325
```

### Variables that are missing data in at least one observation in the training set

```
colnames(pisaTrain)[colSums(is.na(pisaTrain))>0]
```

```
## [1] "raceeth"
                                "preschool"
## [3] "expectBachelors"
                                "motherHS"
                                "motherWork"
## [5] "motherBachelors"
## [7] "fatherHS"
                                "fatherBachelors"
## [9] "fatherWork"
                                "selfBornUS"
## [11] "motherBornUS"
                                "fatherBornUS"
## [13] "englishAtHome"
                                "computerForSchoolwork"
## [15] "read30MinsADay"
                                "minutesPerWeekEnglish"
## [17] "studentsInEnglish"
                                "schoolHasLibrary"
## [19] "schoolSize"
```

# Linear regression discards observations with missing data, so we will remove all such observations from the training and testing sets.

```
pisaTrain=na.omit(pisaTrain)
pisaTest=na.omit(pisaTest)
colnames(pisaTrain)[colSums(is.na(pisaTrain))>0]
```

```
## character(0)
```

```
colnames(pisaTest)[colSums(is.na(pisaTest))>0]
```

```
## character(0)
```

For variable raceeth, by default, R selects first level alphabetically as shown by code.

```
str(pisaTrain$raceeth)

## Factor w/ 7 levels "American Indian/Alaska Native",..: 7 3 4 7 5 4 7 4 7
7 ...
```

We can reset the reference level using following code.

```
pisaTrain$raceeth = relevel(pisaTrain$raceeth, "White")
pisaTest$raceeth = relevel(pisaTest$raceeth, "White")
str(pisaTrain$raceeth)
```

```
## Factor w/ 7 levels "White", "American Indian/Alaska Native",..: 1 4 5 1 6 5 1 5 1 1 ...
```

## Creating Linear Model.

We can use dot(.) if we want to use all the independent variables in our model.

```
lmScore=lm(readingScore ~ . , data=pisaTrain)
summary(lmScore)
```

```
##
## Call:
## lm(formula = readingScore ~ ., data = pisaTrain)
##
## Residuals:
     Min 1Q Median 3Q Max
## -247.44 -48.86 1.86 49.77 217.18
##
## Coefficients:
                                                 Estimate Std. Error
##
                                               143.766333 33.841226
## (Intercept)
                                                29.542707 2.937399
## grade
## male
                                               -14.521653 3.155926
## raceethAmerican Indian/Alaska Native
                                               -67.277327 16.786935
## raceethAsian
                                                -4.110325 9.220071
## raceethBlack
                                               -67.012347 5.460883
## raceethHispanic
                                               -38.975486 5.177743
## raceethMore than one race
                                               -16.922522 8.496268
## raceethNative Hawaiian/Other Pacific Islander -5.101601 17.005696
## preschool

  -4.463670
  3.486055

## expectBachelors
                                                55.267080 4.293893
## motherHS
                                                 6.058774 6.091423
                                                12.638068 3.861457
## motherBachelors
## motherWork
                                                -2.809101 3.521827
## fatherHS
                                                 4.018214 5.579269
                                                16.929755 3.995253
## fatherBachelors
## fatherWork
                                                5.842798 4.395978
## selfBornUS
                                                -3.806278 7.323718
                                                -8.798153 6.587621
## motherBornUS
## fatherBornUS
                                                 4.306994 6.263875
## englishAtHome
                                                 8.035685 6.859492
                                                22.500232 5.702562
## computerForSchoolwork
## read30MinsADay
                                                34.871924 3.408447
                                                 0.012788 0.010712
## minutesPerWeekEnglish
## studentsInEnglish
                                                -0.286631 0.227819
## schoolHasLibrary
                                                12.215085 9.264884
## publicSchool
                                               -16.857475 6.725614
## urban
                                                -0.110132 3.962724
## schoolSize
                                                 0.006540 0.002197
##
                                               t value Pr(>|t|)
## (Intercept)
                                                 4.248 2.24e-05 ***
## grade
                                                10.057 < 2e-16 ***
## male
                                                -4.601 4.42e-06 ***
## raceethAmerican Indian/Alaska Native
                                                -4.008 6.32e-05 ***
## raceethAsian
                                                -0.446 0.65578
## raceethBlack
                                               -12.271 < 2e-16 ***
                                                -7.528 7.29e-14 ***
## raceethHispanic
## raceethMore than one race
                                                -1.992 0.04651 *
```

```
## raceethNative Hawaiian/Other Pacific Islander -0.300 0.76421
## preschool
                                                 -1.280 0.20052
                                                 12.871 < 2e-16 ***
## expectBachelors
## motherHS
                                                  0.995 0.32001
## motherBachelors
                                                   3.273 0.00108 **
## motherWork
                                                 -0.798 0.42517
## fatherHS
                                                   0.720 0.47147
                                                   4.237 2.35e-05 ***
## fatherBachelors
## fatherWork
                                                  1.329 0.18393
## selfBornUS
                                                 -0.520 0.60331
                                                  -1.336 0.18182
## motherBornUS
## fatherBornUS
                                                  0.688 0.49178
                                                  1.171 0.24153
## englishAtHome
                                                  3.946 8.19e-05 ***
## computerForSchoolwork
                                                 10.231 < 2e-16 ***
## read30MinsADay
## minutesPerWeekEnglish
                                                  1.194 0.23264
## studentsInEnglish
                                                 -1.258 0.20846
## schoolHasLibrary
                                                  1.318 0.18749
                                                  -2.506 0.01226 *
## publicSchool
## urban
                                                 -0.028 0.97783
## schoolSize
                                                  2.977 0.00294 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 73.81 on 2385 degrees of freedom
## Multiple R-squared: 0.3251, Adjusted R-squared: 0.3172
## F-statistic: 41.04 on 28 and 2385 DF, p-value: < 2.2e-16
```

Note that the R-squared is lower than the usuals. This does not necessarily imply that the model is of poor quality. More often than not, it simply means that the prediction problem at hand (predicting a student's test score based on demographic and school-related variables) is more difficult than other prediction problems (like predicting a team's number of wins from their runs scored and allowed, or predicting the quality of wine from weather conditions).

## Calculating Root Mean Square Error.

```
SSE = sum(lmScore$residuals^2)
RMSE = sqrt(SSE/nrow(pisaTrain))
RMSE
```

```
## [1] 73.36555
```

A alternative way of getting this answer would be with the following command:

```
sqrt(mean(lmScore$residuals^2))
```

```
## [1] 73.36555
```

Question: Consider two students A and B. They have all variable values the same, except that student A is in grade 11 and student B is in grade 9. What is the predicted reading score of student A minus the predicted reading score of student B?

```
2*lmScore$coefficients["grade"]

## grade
## 59.08541
```

Question: What is the meaning of the coefficient associated with variable raceethAsian?

```
lmScore$coefficients["raceethAsian"]

## raceethAsian
## -4.110325
```

The only difference between an Asian student and white student(set as reference level) with otherwise identical variables is that the former has raceethAsian=1 and the latter has raceethAsian=0. The predicted reading score for these two students will differ by the coefficient on the variable raceethAsian.

#### Predicting on Test data

```
predTest=predict(lmScore,newdata = pisaTest)
summary(predTest)
```

```
## Min. 1st Qu. Median Mean 3rd Qu. Max.
## 353.2 482.0 524.0 516.7 555.7 637.7
```

```
SSE_test = sum((predTest - pisaTest$readingScore)^2)
RMSE_test = sqrt(SSE_test/nrow(pisaTest))
SSE_test
```

```
## [1] 5762082
```

```
RMSE_test
```

```
## [1] 76.29079
```

```
baseline = mean(pisaTrain$readingScore)
SST_Test = sum((baseline - pisaTest$readingScore)^2)
SST_Test
```

## [1] 7802354

```
R2_Test = 1 - SSE_test/SST_Test
R2_Test
```

## [1] 0.2614944