

Optimized Selection Sort Algorithm is faster than Insertion Sort Algorithm: a Comparative Study

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Abstract– Optimized Selection Sort Algorithm is a new sorting algorithm that has been developed to address the shortcomings of the current popular sorting algorithms. The goal of this research is to perform an extensive empirical analysis of Optimized Selection Sort against Selection Sort and Insertion Sort Algorithms. The results proved that Optimized Selection Sort is much more efficient than Selection Sort Algorithm; Furthermore analysis supports the fact that Optimized Selection Sort is better than Insertion Sort in worst case scenario.

Index Term-- Optimized Selection Sort, Worst Case, Efficiency, Sorting Algorithm

I. INTRODUCTION

SORTING algorithms are the basic foundations of practical Computer Science, and therefore, the analysis and design of useful sorting algorithms has remained one of the most important research area in the field. Despite the fact that, several new sorting algorithms being introduced, the large number of programmers in the field depends on one of the comparison-based sorting algorithms: Bubble, Insertion, Selection sort etc. The new algorithms are usually not being used as much because they are not as general purpose as comparison-based sorting algorithms, usually require more alteration to work with new classes and data types and in large cases, do not perform as well as expected due to poorer locality of reference caused by linear passes through the array [1] [2] [3] [4].

It is necessary for a new algorithm to be acknowledged and used in the field of Computer Science, the process must be shown to have as good as performance to the abovementioned sorting algorithms and be easy to use, implement, and debug. Better performance will get programmers interested in the algorithm, and ease-of-use will be the final determinate in changing the programmer's sorting preference. The easiest, most time efficient way to accomplish a task is usually preferred, and the comparison-based sorts tinted here offer excellent performance and adaptability to any type of record or data type to be sorted [5][6][7].

Insertion Sort and Selection Sort have been around for over half a century, and have been taught widely in the academic

Computer Science community. These algorithms are established and well documented with literally dozens of thousands of published empirical analyses comparing and contrasting performances, highlighting theoretical boundaries, and recommending preferred solutions. This paper is no different in this aspect. However, this paper does reveal new information on a newly developed comparison-based sorting algorithm based on the Selection Sort Algorithm, known as Optimized Selection Sort Algorithm [8] [9] [15].

OSSA also referred to as Optimized Selection Sort Algorithm, is a new in place comparison-based sort. Logic of OSSA based on the old selection sort algorithm. The main difference in old SS and new OSSA is that the former sorts the data from one end i.e from largest element of array to smallest element or from smallest to largest but the later starts sorting from both ends and finds the largest and smallest data elements of array in single iteration and place them at their proper locations then during second iteration it sorts the second largest and second smallest elements from the remaining array data and place them in their appropriate location in the array. Similarly it sorts rest of the data elements and put them in their proper positions. OSSA sort the data in half iterations as compared to old SS. It sorts two data elements at a time, which is why it minimizes the sorting time up to 50%. Other characteristics of this algorithm are as under [15].

- It is an in place algorithm.
- It is simple.
- Although it is $O(n^2)$ Algorithm, yet it is faster than all algorithms of this order.
- It is two times faster than old SS and Almost as
- It is a Stable algorithm.
- It performs less data exchange operation than bubble or insertion sort algorithm of this order.

II. SELECTION SORT ALGORITHM

A. Selection Sort

It is one of the easiest and most useful sorting algorithms for dealing with small amount of data set. Even though it

performs a lot of comparisons, but it performs the least amount of data moving. Thus, if your data has small keys but large data area, then selection sorting may be the quickest [15].

B. Pseudo Code and Execution Time of Individual Statement of Old Selection Sort

Algorithm SelectionSort (X, n) ▷
X[0..n-1]

S. No	Iteration	Cost	Times
1	FOR i ← n - 1 TO 0	C_1	n
2	IndexOfLarge ← 0	C_2	$n - 1$
3	FOR j ← 1 TO n	C_3	$\sum_{i=1}^{n-1} (i + 1)$
4	if (X[j] > X[IndexOfLarge])	C_4	$\sum_{i=1}^{n-1} (i)$
5	IndexOfLarge ← j	C_5	$\sum_{j=2}^n i(t_j)$
6	Large ← X[IndexOfLarge]	C_6	$n - 1$
7	X[IndexOfLarge] ← X[i]	C_7	$n - 1$
8	X[i] ← Large	C_8	$n - 1$

C. Best-Case Time Complexity of Old Selection Sort.

For the best-case scenario when we have all $t_{ij} = 0$

$$T(n) = C_1 n + C_2(n-1) + C_3 \sum_{i=1}^{n-1} (i+1) + C_4 \sum_{i=1}^{n-1} (i) + C_5 \sum_{i=1}^{n-1} (i) + C_6(n-1) + C_7(n-1) + C_8(n-1)$$

$$C_3 \sum_{i=1}^{n-1} (i+1) = C_3 \frac{n(n-1)}{2} + C_3(n-1)$$

$$C_4 \sum_{i=1}^{n-1} (i) = C_4 \frac{n(n-1)}{2}$$

$$C_5 \sum_{i=1}^{n-1} (i+1) = C_5 \frac{n(n-1)}{2}$$

$$T(n) = C_1 n + C_2(n-1) + C_3 \frac{n(n-1)}{2} + C_3(n-1) + C_4 \frac{n(n-1)}{2} + C_5 \frac{n(n-1)}{2} + C_6(n-1) + C_7(n-1) + C_8(n-1)$$

$$T(n) = C_1 n + C_2 n - C_2 + C_3 \frac{n(n-1)}{2} + C_3(n-1) + C_4 \frac{n(n-1)}{2} + C_6 n - C_6 + C_7 n - C_7 + C_8 n - C_8$$

$$T(n) = C_1 n + C_2 n - C_2 + C_3 n^2/2 - C_3 n/2 + C_3 n - C_3 + C_4 n^2/2 - C_4 n/2 + C_6 n - C_6 + C_7 n - C_7 + C_8 n - C_8$$

$$T(n) = \left(\frac{C_3}{2} + \frac{C_4}{2} \right) n^2 + \left(C_1 + C_2 + C_3 + C_6 + C_7 + C_8 - \frac{C_3}{2} - \frac{C_4}{2} \right) n - (C_2 + C_3 + C_7 + C_8)$$

Let

$$a = \frac{C_3}{2} + \frac{C_4}{2}$$

$$b = C_1 + C_2 + C_3 + C_6 + C_7 + C_8 - \frac{C_3}{2} - \frac{C_4}{2}$$

$$c = -(C_2 + C_3 + C_7 + C_8)$$

Then replacing the values of a, b and c in $T(n)$ we have

$$T(n) = an^2 + bn + c$$

Thus here in best-case, the complexity of execution time of an algorithm shows the lower bound and is asymptotically denoted with Ω . Therefore by ignoring the constant a, b, c and the lower terms of n , and taking only the dominant term i.e. n^2 , then the asymptotic running time of selection sort will be $\Omega(n^2)$ and will lie in of set of asymptotic function i.e. $\Theta(n^2)$. Hence we can say that the asymptotic running time of old SS will be:

$$T(n) = \Omega n^2$$

D. Worst-Case Time Complexity.

Now for the worst-case scenario when we have all $t_{ij} = 1$ so we have

$$T(n) = C_1 n + C_2(n-1) + C_3 \frac{n(n-1)}{2} + C_3(n-1) + C_4 \frac{n(n-1)}{2} + C_5 \frac{n(n-1)}{2} + C_6(n-1) + C_7(n-1) + C_8(n-1)$$

$$T(n) = C_1 n + C_2 n - C_2 + \frac{C_3 n^2}{2} - \frac{C_3 n}{2} + C_3 n - C_3 + \frac{C_4 n^2}{2} - \frac{C_4 n}{2} + \frac{C_5 n^2}{2} - \frac{C_5 n}{2} + C_6 n - C_6 + C_7 n - C_7 + C_8 n - C_8$$

$$T(n) = \left(\frac{C_3}{2} + \frac{C_4}{2} + \frac{C_5}{2}\right)n^2 + \left(C_1 + C_2 + C_3 + C_6 + C_7 + C_8 - \frac{C_3}{2} - \frac{C_4}{2} - \frac{C_5}{2}\right)n - (C_2 + C_3 + C_7 + C_8) \quad (\text{Eq: 01})$$

Let

$$a = \frac{C_3}{2} + \frac{C_4}{2} + \frac{C_5}{2}$$

$$b = C_1 + C_2 + C_3 + C_6 + C_7 + C_8 - \frac{C_3}{2} - \frac{C_4}{2}$$

$$c = -(C_2 + C_3 + C_7 + C_8)$$

If we suppose $C_1 = C_2 = C_4 = C_5 = C_6 = C_7 = C_8 = 1$ and put it in Equation 01

Then

$$T(n) = 3/2n^2 + 9/2n - 5$$

$$T(n) = an^2 + bn + c$$

Thus here in worst-case, the complexity of execution time of an algorithm shows the upper bound and is asymptotically denoted with Big-O. Therefore by ignoring the constant a, b, c and the lower terms of n, and taking only the dominant term i.e. n^2 , then the asymptotic running time of selection sort will be of the order of $O(n^2)$ and will lie in of set of asymptotic function i.e. $\Theta(n^2)$. Hence we can say that the asymptotic running time of old SS will be:

$$T(n) = On^2$$

It means that the best and worst case asymptotic running time of selection sort is same i.e. $T(n) = On^2$ however there may be little difference in actual running time, which will be very less and hence ignored.

III. INSERTION SORT ALGORITHM

A. Insertion Sort

Insertion sort algorithm is also one of oldest, easiest and most useful sorting algorithms for dealing with modicum of data set. If the first few objects are already sorted, an unsorted object can be inserted in the sorted set in proper place [10].

B. Pseudo Code & Execution Time of Individual Statement of Insertion Sort

Algorithm InsertionSort (X, n) ▷
X[0..n-1]

S.No	Iteration	Cost	Times
1	FOR j ← 2 TO length[X]	C_1	n
2	DO key ← X[j]	C_2	$n - 1$
3	▶ Put X[j] into the sorted sequence X[1 .. j - 1]	0	$n - 1$
4	$i \leftarrow j - 1$	C_4	$n - 1$
5	WHILE $i > 0$ and $X[i] > \text{key}$	C_5	$\sum_{j=2}^n t_j$
6	DO $X[i+1] \leftarrow X[i]$	C_6	$\sum_{j=2}^n (t_j - 1)$
7	$i \leftarrow i - 1$	C_7	$\sum_{j=2}^n (t_j - 1)$
8	$X[i+1] \leftarrow \text{key}$	C_8	$n - 1$

C. Best-Case Time Complexity of Insertion Sort.

$$T(n) = C_1n + C_2(n-1) + C_4(n-1) + C_5 \sum_{j=2}^n t_j + C_6 \sum_{j=2}^n (t_j - 1) + C_7 \sum_{j=2}^n (t_j - 1) + C_8(n-1) \quad \text{Equation - 01}$$

If $t_j = 1$ for $j = 2, 3, \dots, n$ and the best-case running time can be computed as follows:

$$T(n) = C_1n + C_2(n-1) + C_4(n-1) + C_5 \sum_{j=2}^n (1) + C_6 \sum_{j=2}^n (1-1) + C_7 \sum_{j=2}^n (1-1) + C_8(n-1)$$

$$T(n) = C_1n + C_2(n-1) + C_4(n-1) + C_5(1) + C_6(1-1) + C_7(1-1) + C_8(n-1)$$

$$T(n) = (C_1 + C_2 + C_4 + C_5 + C_8)n - (C_2 + C_4 + C_8) \quad \text{Suppose}$$

$$a = (C_1 + C_2 + C_4 + C_5 + C_8)$$

And

$$b = -(C_2 + C_4 + C_8)$$

Then

$$T(n) = an + b$$

The punch line here is that the while-loop in line 5 executed only once for each j . This happens if given array A is already sorted.

$$T(n) = an + b = O(n)$$

It is a linear function of n .

D. Worst-Case Time Complexity of Insertion Sort.

When $t_j = j$ for $j = 2, 3, \dots, n$ then the worst-case running time can be computed from equation (1) as follows:

$$T(n) = C_1n + C_2(n-1) + C_4(n-1) + C_5 \sum_{j=2}^n (j) \\ + C_6 \sum_{j=2}^n (j-1) + C_7 \sum_{j=2}^n (j-1) \\ + C_8(n-1)$$

$$T(n) = C_1n + C_2(n-1) + C_4(n-1) + C_5 \left[\frac{n(n-1)}{2} + 1 \right] \\ + C_6 \left[\frac{n(n-1)}{2} \right] + C_7 \left[\frac{n(n-1)}{2} \right] \\ + C_8(n-1)$$

$$T(n) = [C_5/2 + C_6/2 + C_7/2]n^2 + [C_1 + C_2 + C_4 + C_5/2 - C_6/2 - C_7/2 + C_8]n - [(C_2 + C_4 + C_5 + C_8)] \quad (\text{Eq: 02})$$

If we suppose $C_1 = C_2 = C_4 = C_5 = C_6 = C_7 = C_8 = 1$ and put it in Equation 02
Then

$$T(n) = [1/2 + 1/2 + 1/2]n^2 + [1 + 1 + 1 + 1/2 - 1/2 - 1/2 + 1]n - [1 + 1 + 1 + 1] \\ T(n) = 3/2n^2 + 7/2n - 4 \quad \text{Eq: 03}$$

Suppose

$$a = [C_5/2 + C_6/2 + C_7/2] \\ b = [C_1 + C_2 + C_4 + C_5/2 - C_6/2 - C_7/2 + C_8] \\ c = -[(C_2 + C_4 + C_5 + C_8)]$$

Then

$$T(n) = an^2 + bn + c$$

This running time can be expressed as $an^2 + bn + c$ for constants a , b , and c that again depends on the statement costs c_i . Therefore, $T(n)$ is a quadratic function of n .

We usually concentrate on finding the worst-case running time: the longest running time for any input size n .

IV. OPTIMIZED SELECTION SORT ALGORITHM (OSSA)

A. Optimized Selection Sort Algorithm

The three main characteristics of this algorithms is that, it is in-place, stable and easy to understand as compared to other algorithms of order $O(n^2)$ [15].

The working mechanism of OSSA is that it starts sorting the array from both ends. In a single iteration, first the smallest and largest element in the array are searched, and then both at the same time are placed at the specific location. This process is continued until the whole array is sorted [15].

Even though the order of OSSA is still $O(n^2)$, but its performance level has been very much improved as compared to other sorting algorithm of the said order i.e selection sort, insertion sort etc [15].

B. Pseudo Code & Execution Time of Individual Statement of Optimized Selection Sort Algorithm

Algorithm OSSA (X, n) ▷ X[0..n-1]

S#	Iteration	Cost	Times
1	$k \leftarrow 0$	C_1	1
2	for $i \leftarrow n-1$ to k	C_2	$\frac{n}{2} + 1$
3	IndexOfLarge \leftarrow IndexOfSmall $\leftarrow k$	C_3	$\frac{n}{2}$
4	for $j \leftarrow k+1$ to i	C_4	$\sum_{i=1}^{n/2} i + 1$
5	if $(X[j] > X[\text{IndexOfLarge}])$	C_5	$\sum_{i=1}^{n/2} i$
6	IndexOfLarge $\leftarrow j$	C_6	$\sum_{i=1}^{n/2} t_{i_j}$
7	if $(X[j] < X[\text{IndexOfSmall}])$	C_7	$\sum_{i=1}^{n/2} i$
8	IndexOfSmall $\leftarrow j$	C_8	$\sum_{i=1}^{n/2} t_{i_j}$
9	Large $\leftarrow X[\text{IndexOfLarge}]$	C_9	$\frac{n}{2}$
10	Small $\leftarrow X[\text{IndexOfSmall}]$	C_{10}	$\frac{n}{2}$
11	$X[\text{IndexOfLarge}] \leftarrow X[i]$	C_{11}	$\frac{n}{2}$
12	$X[\text{IndexOfSmall}] \leftarrow X[k]$	C_{12}	$\frac{n}{2}$
13	if $(\text{IndexOfLarge} == k)$ Temp $\leftarrow X[i]$ $X[i] \leftarrow$ Large $X[\text{IndexOfSmall}] \leftarrow$ Temp	C_{13}	$\frac{n}{2}$
14	Else $X[i] \leftarrow$ Large Temp $\leftarrow X[k]$ $X[k] \leftarrow$ Small $X[\text{IndexOfLarge}] \leftarrow$ Temp	C_{14}	$\frac{n}{2}$
15	Else $X[k] \leftarrow$ Small $k \leftarrow k+1$	C_{15}	$\frac{n}{2}$

C. Best-Case Time Complexity of Optimized Selection Sort.

$$\begin{aligned}
 T(n) &= C_1 + C_1 \frac{n}{2} + C_2 \frac{n}{2} + C_2 + C_3 \frac{n}{2} + C_4 \sum_{i=1}^{\frac{n}{2}} (i+1) \\
 &\quad + C_5 \sum_{i=1}^{\frac{n}{2}} (i) + C_6 \sum_{i=1}^{\frac{n}{2}} (i) \\
 &\quad + C_7 \sum_{i=1}^{\frac{n}{2}} (i) + C_8 \sum_{i=1}^{\frac{n}{2}} (i) + C_9 \frac{n}{2} \\
 &\quad + C_{10} \frac{n}{2} + C_{11} \frac{n}{2} + C_{12} \frac{n}{2} + C_{13} \frac{n}{2} + C_{14} \frac{n}{2} \\
 &\quad + C_{15} \frac{n}{2} \\
 C_4 \sum_{i=1}^{n/2} (i+1) &= C_4 \sum_{i=1}^{n/2} (i) + C_4 \sum_{i=1}^{n/2} (1) \\
 &= C_4 \frac{\left(\frac{n}{2} + 1\right)}{2} + C_4 \frac{n}{2} \\
 C_5 \sum_{i=1}^{n/2} (i) &= C_5 \frac{\left(\frac{n}{2} + 1\right)}{2} = C_5 \frac{n^2}{8} + C_5 \frac{n}{4} \\
 C_6 \sum_{i=1}^{n/2} (i) &= C_6 \frac{\left(\frac{n}{2} + 1\right)}{2} = C_6 \frac{n^2}{8} + C_6 \frac{n}{4} \\
 C_7 \sum_{i=1}^{n/2} (i) &= C_7 \frac{\left(\frac{n}{2} + 1\right)}{2} = C_7 \frac{n^2}{8} + C_7 \frac{n}{4} \\
 C_8 \sum_{i=1}^{n/2} (i) &= C_8 \frac{\left(\frac{n}{2} + 1\right)}{2} = C_8 \frac{n^2}{8} + C_8 \frac{n}{4} \\
 T(n) &= C_1 + C_1 \frac{n}{2} + C_2 \frac{n}{2} + C_2 + C_3 \frac{n}{2} + C_4 \frac{\left(\frac{n}{2} + 1\right)}{2} + C_4 \frac{n}{2} \\
 &\quad + C_5 \frac{n^2}{8} + C_5 \frac{n}{4} + C_7 \frac{n^2}{8} + C_7 \frac{n}{4} + C_9 \frac{n}{2} \\
 &\quad + C_{10} \frac{n}{2} + C_{11} \frac{n}{2} + C_{12} \frac{n}{2} + C_{13} \frac{n}{2} + C_{14} \frac{n}{2} \\
 &\quad + C_{15} \frac{n}{2} \\
 T(n) &= C_1 + C_1 \frac{n}{2} + C_2 \frac{n}{2} + C_2 + C_3 \frac{n}{2} + C_4 \frac{n^2}{8} + C_4 \frac{n}{4} + C_4 \frac{n}{2} \\
 &\quad + C_5 \frac{n^2}{8} + C_5 \frac{n}{4} + C_7 \frac{n^2}{8} + C_7 \frac{n}{4} + C_9 \frac{n}{2} \\
 &\quad + C_{10} \frac{n}{2} + C_{11} \frac{n}{2} + C_{12} \frac{n}{2} + C_{13} \frac{n}{2} + C_{14} \frac{n}{2} \\
 &\quad + C_{15} \frac{n}{2} \\
 T(n) &= \left(\frac{C_5}{8} + \frac{C_4}{8} + \frac{C_7}{8}\right) n^2 \\
 &\quad + \left(\frac{C_1}{2} + \frac{C_2}{2} + \frac{C_3}{2} + \frac{C_4}{2} + \frac{C_4}{4} + \frac{C_5}{4} + \frac{C_6}{4} + \frac{C_7}{4} + \frac{C_8}{4} + \frac{C_9}{2} + \frac{C_{10}}{2} + \frac{C_{11}}{2} + \frac{C_{12}}{2} + \frac{C_{13}}{2} + \frac{C_{14}}{2} + \frac{C_{15}}{2}\right) n \\
 &\quad + (C_1 + C_2)
 \end{aligned}$$

Let

$$a = \frac{C_5}{8} + \frac{C_4}{8} + \frac{C_7}{8}$$

$$\begin{aligned}
 b &= \frac{C_1}{2} + \frac{C_2}{2} + \frac{C_3}{2} + \frac{C_4}{2} + \frac{C_4}{4} + \frac{C_5}{4} + \frac{C_6}{4} + \frac{C_7}{4} + \frac{C_8}{4} + \frac{C_9}{2} + \frac{C_{10}}{2} + \frac{C_{11}}{2} \\
 &\quad + \frac{C_{12}}{2} + \frac{C_{13}}{2} + \frac{C_{14}}{2} + \frac{C_{15}}{2} \\
 c &= (C_1 + C_2) \\
 T(n) &= an^2 + bn + c
 \end{aligned}$$

A. Worst-Case Time Complexity of Optimized Selection Sort.

$$\begin{aligned}
 T(n) &= C_1 + C_1 \frac{n}{2} + C_2 \frac{n}{2} + C_2 + C_3 \frac{n}{2} + C_4 \sum_{i=1}^{\frac{n}{2}} (i+1) \\
 &\quad + C_5 \sum_{i=1}^{\frac{n}{2}} (i) + C_6 \sum_{i=1}^{\frac{n}{2}} (i) \\
 &\quad + C_7 \sum_{i=1}^{\frac{n}{2}} (i) + C_8 \sum_{i=1}^{\frac{n}{2}} (i) + C_9 \frac{n}{2} \\
 &\quad + C_{10} \frac{n}{2} + C_{11} \frac{n}{2} + C_{12} \frac{n}{2} + C_{13} \frac{n}{2} + C_{14} \frac{n}{2} \\
 &\quad + C_{15} \frac{n}{2} \\
 T(n) &= C_1 + C_1 \frac{n}{2} + C_2 \frac{n}{2} + C_2 + C_3 \frac{n}{2} + C_4 \frac{n^2}{8} + C_4 \frac{n}{4} + C_4 \frac{n}{2} \\
 &\quad + C_5 \frac{n^2}{8} + C_5 \frac{n}{4} + C_6 \frac{n^2}{8} + C_6 \frac{n}{4} + C_7 \frac{n^2}{8} \\
 &\quad + C_7 \frac{n}{4} + C_8 \frac{n^2}{8} + C_8 \frac{n}{4} + C_9 \frac{n}{2} + C_{10} \frac{n}{2} \\
 &\quad + C_{11} \frac{n}{2} + C_{12} \frac{n}{2} + C_{13} \frac{n}{2} + C_{14} \frac{n}{2} + C_{15} \frac{n}{2} \\
 T(n) &= \left(\frac{C_4}{8} + \frac{C_5}{8} + \frac{C_6}{8} + \frac{C_7}{8} + \frac{C_8}{8}\right) n^2 \\
 &\quad + \left(\frac{C_1}{2} + \frac{C_2}{2} + \frac{C_3}{2} + \frac{C_4}{2} + \frac{C_4}{4} + \frac{C_5}{4} + \frac{C_6}{4} + \frac{C_7}{4} + \frac{C_8}{4} + \frac{C_9}{2} + \frac{C_{10}}{2} + \frac{C_{11}}{2} + \frac{C_{12}}{2} + \frac{C_{13}}{2} + \frac{C_{14}}{2} + \frac{C_{15}}{2}\right) n \\
 &\quad + (C_1 + C_2)
 \end{aligned}$$

If we put values of all C's equal to one then we get

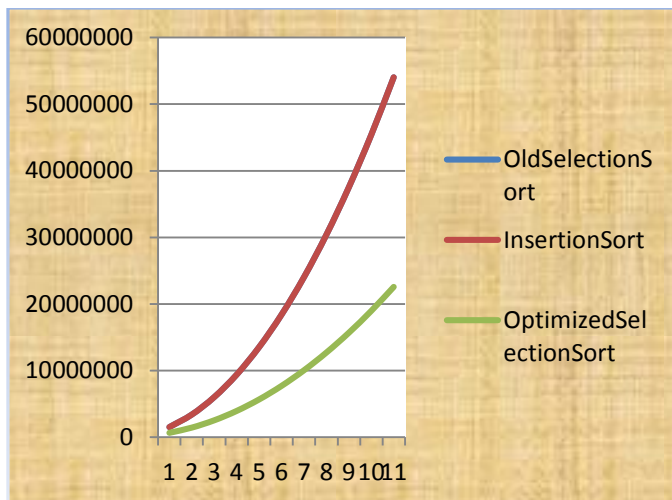
$$\begin{aligned}
 T(n) &= \frac{5}{8} n^2 + \frac{25}{4} n + 2 \\
 a &= \frac{C_5}{8} + \frac{C_4}{8} + \frac{C_7}{8} + \frac{C_8}{8} \\
 b &= \frac{C_1}{2} + \frac{C_2}{2} + \frac{C_3}{2} + \frac{C_4}{2} + \frac{C_4}{4} + \frac{C_5}{4} + \frac{C_6}{4} + \frac{C_7}{4} + \frac{C_8}{4} + \frac{C_9}{2} + \frac{C_{10}}{2} \\
 &\quad + \frac{C_{11}}{2} + \frac{C_{12}}{2} + \frac{C_{13}}{2} + \frac{C_{14}}{2} + \frac{C_{15}}{2} \\
 c &= (C_1 + C_2) \\
 T(n) &= an^2 + bn + c
 \end{aligned}$$

V. COMPARISON OF SELECTION SORT, INSERTION SORT AND OPTIMIZED SELECTION SORT ALGORITHM

Below is the table representing the calculated time, when multiple values of n are used.

n	Calculated Time of SSA	Calculated Time of Optimized SSA	Calculated Time of Insertion Sort
n	T(n) Old SS	T(n) OSSA	T(n) InsetT
1000	1504495	631254	1503496
1500	3381745	1415629	3380246
2000	6008995	2512504	6006996
2500	9386245	3921879	9383746
3000	13513495	5643754	13510496
3500	18390745	7678129	18387246
4000	24017995	10025004	24013996
4500	30395245	12684379	30390746
5000	37522495	15656254	37517496
5500	45399745	18940629	45394246

Below is the line graph plotted in response of data given in above table.



The graph shows that optimized selection is far better than its competitor algorithms of the same order of $O(n^2)$.

CONCLUSION

OSSA is basically based on the logic of old Selection Sort, but it performs less amount of iteration that's why it saves almost fifty percent of the execution time. OSSA is a new comparison-based sorting algorithm, with an $O(n^2)$ order complexity, yet it is the fastest of its kinds, like selection and insertion sort in

the worst case. The results proved the claim.

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