# Stanford University, CS 106A, Homework Assignment 5 Melody Maker & Image Algorithms (PAIR ASSIGNMENT)

Thanks to Keith Schwarz and Allison Obourn for problem ideas, spec text, and code used in this assignment.

The purpose of this assignment is to practice writing algorithms that use 1-D and 2-D arrays. You will turn in:

- Melody.java and mysong.txt, your solution to Problem 1: Melody Player
- ImageAlgorithms.java, your solution to Problem 2: Image Algorithms

#### **Problem 1, Melody Player:**

This problem concerns playing music. A song consists of notes, each of which has a *length* (duration) and *pitch*. The pitch of a note is described with a letter ranging from A to G. As 7 notes would not be enough to play very interesting music, there are multiple *octaves*; after we reach note G we start over at A. Each set of 7 notes is considered an octave. Notes may also be *accidentals*, meaning that they are not in the same key in which the music is written. We normally notate this by calling them *sharp*, *flat*, or *natural*. Music also has silences that are called *rests*.



For this program we will be representing notes using scientific pitch notation. This style of notation represents each note as a letter and a number specifying the octave it belongs to. For example, middle C is represented as C4. You do not need to understand any more than this about scientific pitch notation, but you can read more about it here:

• http://en.wikipedia.org/wiki/Scientific pitch notation

You will write a Melody class that uses an array to represent a song comprised of a series of notes. It may have repeated sections; as we don't like to have any redundancy, we will only store one copy of a repeated chunk of notes. Your Melody class will read files in a format described below and represent the song's notes using an array of Note objects. The most challenging part of this assignment is handling melodies that contain repeated sections. You will also submit a file mysong.txt representing a song of your own that you have written in our specified format.

#### **Input File Format:**

Music is usually printed like the example sheet music at right. The notes are a series of dots. Their position in relation to the lines determines their pitch and their tops and color, among other things, determine their length. Since it would be difficult for us to read input in this style, we will read input from a text file in a specific format.

An example input file is at right. The first two lines contain the **title** and **artist**, respectively. The third line is the number of notes in the song; this is the number of lines that will follow in the file. You may assume that every input file is valid and follows this exact format. Each subsequent line represents a single note in the following format:

#### duration pitch octave accidental repeat

The first number on each line describes the duration of the note in seconds. The next letter describes the pitch of the note, using the standard letters A-G or R for a rest. The third token is the octave that the note is in. The fourth is the note's accidental value of sharp, flat, or natural. (For a rest, the octave and accidental are omitted.) The final token indicates whether the note is the start or stop of a repeated section: true if so, and false otherwise. In the example at right, notes 3-5 and 9-12 (lines 6-8 and 12-15) represent two repeated sections. The meaning of the data is that the song should play notes 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 9, 10, 11, 12, 13. Our format does not allow nested repetition, nor sections that repeat more than twice.

#### **Hot Crossed Buns**



#### Example input file (line numbers added): My Song Title 2 Joe Smith 3 13 4 0.2 C 4 NATURAL false 5 0.4 F 4 NATURAL false 6 0.2 F 4 NATURAL true 7 0.4 G 4 NATURAL false 8 0.2 A 4 NATURAL true 9 0.2 A 4 NATURAL false 10 0.4 R false 11 0.2 B 4 NATURAL false 12 0.2 C 4 NATURAL true 13 0.4 D 4 NATURAL false 14 0.2 C 5 NATURAL false 15 0.2 A 4 NATURAL true 16 0.4 D 4 NATURAL false

#### **Note class** (provided by instructor):

We have provided you with a class named Note that your Melody class will use. To access the Note class in your code, write the following atop your class: import stanford.cs106.audio.\*;

A **Note** object represents a single musical note that will form part of a melody. It keeps track of the length (duration) of the note in seconds as a **double**, the note's pitch (A-G, or R if the note is a rest), the octave as an **int**, and the accidental (sharp, natural or flat). Each **Note** object also uses a **boolean** field to keep track of whether it is the first or last note of a repeated section of the melody. You pass this information to the **Note**'s constructor when you create a **Note** object.

The Note uses two types of constants named Pitch and Accidental.

- A Pitch is a constant from Pitch.A through Pitch.G or Pitch.R, meaning the frequency of the note.
- An Accidental indicates whether a note is sharp, flat, or neither using the constants Accidental.SHARP, Accidental.FLAT, and Accidental.NATURAL respectively.

The **Note** class provides the following constructors and methods that you should use in your program. The various **get** and **is** methods are accessors that return the values that you previously passed to the **Note** constructor.

Method	Description
new Note( <i>line</i> )	Constructs a new Note object with data from the given String line, such as "0.2 C 4 NATURAL false" or "0.4 R false".
<pre>getAccidental(), getDuration(), getOctave(), getPitch(), isRepeat()</pre>	Returns the state of the note as passed to the constructor.
play()	Plays the note so that it can be heard from the computer speakers.
<pre>setAccidental(accidental), setDuration(duration), setOctave(octave), setPitch(pitch), setRepeat(repeat)</pre>	Sets aspects of the state of the note based on the given value.
toString()	Returns a text representation of the note.

See the contents of the provided **Note** class documentation provided on the class web site to answer any further questions about how it works. We also provide its source code, though you don't need to paste it into your project.

### **Melody Class** (for you to implement):

You will implement the Melody class and its methods listed here and described in detail on the following pages:

• getTitle, getArtist, getTotalDuration (information about the song's state)

• plays the song on the computer's speakers)

• octaveDown, octaveUp, changeDuration, reverse (methods that manipulate the song's state)

You will need several fields to implement all of the required behavior. Your class <u>must</u> use a field that is an **array of Note objects** to store the notes in the song. You will need other fields to implement all of the behavior shown below, but you may not create any other data structures (such as arrays or lists) to help you.

Testing: Test your Melody class by running our instructor-provided class MelodyMain that allows you to select text files and play them. Each time you click Load and choose a file from the disk, a Melody object will be created for that file. Most of the other buttons essentially map to the various methods in your Melody class. When the user clicks Play, your Melody object's play method is called. When the user clicks Reverse, your Melody object's reverse method is called. And so on. Not every button directly maps to a Melody method; for example, the Stop button tells the underlying audio system to halt, but this has the effect of making it temporarily ignore any further notes that your Melody code tries to play.

Debugging: Since your Melody class is not a complete program, you can't use the println command for debugging. But there is a similar command named System.out.println that can be used from any class; it prints output to a console at the bottom of the Eclipse IDE.

#### public Melody(Scanner input)

In this constructor you should populate your melody's array of notes by reading note data from the specified **Scanner**. The file format was described previously; it begins with the song title, author, and number of notes, followed by a series of lines, each of which describes a single **Note** object. You should read each note line, use each line to construct a **Note** object, and put this **Note** into your internal array.

The constructor is the only part of your code that should read data from the input file. All other methods should refer to your internal array of notes. Re-reading the file to implement other methods is forbidden.

**Assume valid input.** You may assume that the file exists, is readable, and that its contents exactly follow the format described on the previous page. The file contains exactly the number of note lines equal to the number written on the file's third line. You may assume that each note line contains a valid note, such as "1.2 C 4 NATURAL false" for a 1.2-second natural C note in the 4th octave, or "0.4 R false" for a 0.4-second rest. No line will contain a note other than A-G or R (rest); none will contain any badly formatted tokens or lines; etc.

#### public String getTitle()

In this method you should return the title of the song, as was found in the first line of the song's input file.

#### public String getArtist()

In this method you should return the artist of the song, as was found in the second line of the song's input file.

#### public double getTotalDuration()

In this method you should return the total duration (length) of the song, in seconds. In general this is equal to the sum of the durations of the song's notes, but if some sections of the song are repeated, those parts count twice toward the total. For example, a song whose notes' durations add up to 6 seconds that has a 1.5-second repeated section and a 1-second repeated section has a total duration of (6.0 + 1.5 + 1.0) = 8.5 seconds.

Tip: If the provided GUI's slider doesn't move properly when playing, your total duration code is probably wrong.

#### public void play()

In this method you should play your melody so that it can be heard on the computer's speakers. Essentially this consists of calling the play method on each Note in your array. The notes should be played from the beginning of the list to the end, unless there are notes that are marked as being part of a repeated section. If a series of notes represents a repeated section, that sequence is played twice. For example, in the diagram below, suppose the notes at indexes 3, 5, 9, and 12 all indicate that they are start/end points of repeated sections (their isRepeat method returns true). In this case, the correct sequence of note indexes to play is 0, 1, 2, 3, 4, 5, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 9, 10, 11, 12, 13. Note that notes at indexes 3-5 and 9-12 are played twice in our example.

This method should not modify the state of your array. Also, it should be possible to call play multiple times and get the same result each time.

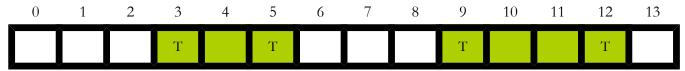


diagram of array of notes with repeated sections at indexes 3-5 and 9-12

#### public boolean octaveDown()

In this method you should modify the state of the notes in your internal array so that they are all exactly 1 octave

lower in pitch than their current state. For example, a C note in octave 4 would become a C note in octave 3. Rests are not affected by this method, and the notes' state is otherwise unchanged other than the octaves.

There is one special case to watch out for. Octave 1 is the lowest possible octave allowed by our system. If any note(s) in your song are already down at octave 1, then the entire **octaveDown** call should do nothing. In such a case, no notes (even ones above octave 1) should be changed; the call should have no effect.

You should return true if this method lowered the octave, and false if you hit the above special case.

#### public boolean octaveUp()

In this method you should modify the state of the notes in your internal array so that they are all exactly 1 octave higher in pitch than their current state. For example, a C note in octave 4 would become a C note in octave 5. Rests are not affected by this method, and the notes' state is otherwise unchanged other than the octaves.

There is one special case to watch out for. Octave 10 is the highest possible octave allowed by our system. If any note(s) in your song are already up at octave 10, then the entire **octaveUp** call should do nothing. In such a case, no notes (even ones below octave 10) should be changed; the call should have no effect.

You should return true if this method raised the octave, and false if you hit the above special case.

#### public void changeDuration(double ratio)

In this method you should scale the duration of each note in your melody by the given ratio. For example, passing a ratio of 1.0 will do nothing, while a ratio of 2.0 will make each note's duration twice as long (slow down the song), or a ratio of 0.5 will make each note half as long (speed up the song).

#### public void reverse()

In this method you should reverse the order of the notes in your melody, so that future calls to play would play the notes in the opposite of the order they were in before the call. For example, a song containing notes A, F, G, B would become B, G, F, A. This amounts to reversing the order of the elements of your internal array of notes. Do not make a complete copy of your internal array, and do not create any other data structures such as arrays, strings, or lists; just modify your array in-place. You must write the reversal code yourself; you are not allowed to call an existing Java reversal library.

#### public String toString() (optional)

You are not required to write a toString method in your Melody class, but if you do, it will be called by our MelodyMain program when any operations are performed. For example, after loading a song from a file, or reversing the song, or changing duration or octaves, the MelodyMain program prints out the toString representation of your Melody on the console. If you do write a toString, you can return any string you want. This may be useful for debugging. Recall that Arrays.toString returns a string representation of an array.

#### Creative Aspect, mysong.txt:

Along with your Melody class, turn in a file named mysong.txt that contains song data that you have made yourself. This file can have any contents you want, so long as it follows our specified song file format with the title on the first line, the song's artist or creator on the second line, the number of notes on the third line, and a valid note on each line after that. To receive full credit, your mysong.txt file should be different from the other song files we have provided with the starter ZIP, and it should contain at least 5 notes, but otherwise it can be anything you want. You can make up a song of your own, or you can make a version of an existing song that you like. If you work as a pair, you must each make a song. Turn in mysong.txt and mysong2.txt; make sure to label the author of each song.

This part is worth a small part of your grade. If you don't want to spend time on this part of the assignment, just make a very simple file that plays a scale of notes or something and turn that in; that will be fine. But we encourage you to **be creative** and submit a neat song! Some especially cool songs may be played in class later on.

#### **Problem 2: Image Algorithms**

For the second part of this assignment, you will write a series of algorithms to manipulate the pixels of images. We provide you with an overall graphical user interface **ImageMain.java** and you will write your image manipulation algorithms in a file named **ImageAlgorithms.java**.

As shown in class, we will represent images as 2-dimensional arrays, where each array element is an integer containing the red, green, and blue components of a single pixel. The red, green, and blue components of a pixel are integer values from 0 (none of that color) to 255 (maximum amount of that color).

Each of the algorithms you will write is a method that accepts a GImage parameter representing the source image, the current state of the image on the screen. Each image algorithm method should modify the GImage passed in by setting its pixel array to contain the new state of the image after that algorithm has been applied to the source image. To interact with GImage objects and to get/set pixel integer values, you'll need to use



the methods shown in class and in section 11.7 of the  $A \mathcal{CS}$  textbook, such as getPixelArray, setPixelArray, getRed, getGreen, getBlue, createRGBPixel, and so on.

You will implement the following image manipulation algorithms:

• **grayscale**: Converts an image to a black-and-white version of itself

• **negative**: Inverts the colors of an image

• rotateLeft: Reorders the pixels to an orientation 90-degrees counterclockwise from their current state

• rotateRight: Reorders the pixels to an orientation 90-degrees clockwise from their current state

• **translate**: Moves the positions of the pixels by a given dx, dy offset

• **blur**: Averages pixel values with those of neighboring pixels to produce a "softening" effect

• mystery: Any other image manipulation algorithm of your choice (creative aspect)

Each algorithm is described in detail on the following pages. Your **ImageAlgorithms** class should not use any fields; each algorithm can be solved on its own without any fields (instance variables) in your code. Each algorithm should work on an image of any size, including very large images or very small images such as 1x1 pixels, etc. When describing the algorithms we may refer to pixels in the format (r, g, b), such as (24, 191, 65) to indicate a pixel with a red component of 24, green of 191, and blue of 65.

### public void grayscale(GImage source)

In this method you should create a grayscale (black-and-white) version of the source image. To convert an image to black-and-white, for each pixel, set all three of its red, green, and blue values to be the average of those three values, rounded <u>down</u> to the nearest integer. For example, the pixel (10, 52, 36) has an average color value of (10+52+36)/3 = 32.667, so the grayscale version of that pixel is (32, 32, 32).



#### public void negative(GImage source)

In this method you should create a new image whose pixels are the inverse of those in the source image. To convert an image to its inverse, for each pixel, set all three of its red, green, and blue values to be the inverse of their current color value. The inverse of a color value k is defined as 255 - k. For example, the pixel (110, 52, 236) has an inverse of (145, 203, 19).



#### public void rotateLeft(GImage source)

In this method you should create a new image whose pixel positions are rotated 90-degrees **counter-clockwise** relative to those in the source image. For example, the diagram below shows a source image of size 6x4 rotated left to create a result image of size 4x6; the pixels are indicated by letters for illustration. Note that the source image's width may be different from its height, and that the dimensions of the result image reflect the rotation you have performed; the result image is as wide as the source was tall, and as tall as the source was wide.



b	efo	re	rot	ate	Lef	t			а	fte	r	
	0	1	2	3	4	5			0	1	2	3
0	Α	В	C	D	Ε	F		0	F	L	R	Χ
1	G	Н	Ι	J	Κ	L	>	1	Ε	Κ	Q	W
2	Μ	Ν	0	Ρ	Q	R		2	D	J	P	٧
3	S	Т	U	V	W	Χ		3	C	Ι	0	U
								4	В	Н	N	Т
								5	Δ	G	М	S

#### public void rotateRight(GImage source)

In this method you should create a new image whose pixel positions are rotated 90-degrees **clockwise** relative to those in the source image. For example, the diagram below shows a source image of size 6x4 rotated right to create a result image of size 4x6; the pixels are indicated by letters just for illustration. Note that the source image's width may be different from its height, and that the dimensions of the result image reflect the rotation you have performed; the result image is as wide as the source was tall, and as tall as the source was wide.



before rotateRight						ht			а	fte	r	
	0	1	2	3	4	5			0	1	2	3
0	Α	В	C	D	Ε	F	0	)	S	Μ	G	Α
1	G	Н	I	J	Κ	L	> 1		Т	N	Н	В
2	Μ	Ν	0	Ρ	Q	R	2	<u>.</u>	U	0	I	C
3	S	Т	U	V	W	Χ	3		٧	Ρ	J	D
							4	+	W	Q	Κ	Ε
							5		Χ	Ř	1	F

#### public void translate(GImage source, int dx, int dy)

In this method you should create a new image whose pixel coordinates have been shifted in the x-dimension by an offset of dx pixels, and shifted in the y dimension by an offset of dy pixels, relative to those in the source image. For example, if dx is 2 and dy is -1, the pixels of the source are moved by 2 px to the right (positive x) and 1 px upward (negative y). The resulting image is the same size as the source image. For example, if the 6x4 image shown below were moved by dx of 2 and dy of 1, the pixel at (x=2, y=3) labeled as "U" would move to (x=4, y=2).



Think of the image as an infinite canvas that "wraps around" on itself in all directions. If shifting a pixel causes it to pass the edge of the image, "wrap" that pixel around to the opposite side of the image. For example, if dx is 2 and dy is -1, the pixel at (x=5, y=2) labeled as "R" below would normally have shifted to (x=7, y=1), but x=7 is off the edge, so we wrap it around to (x=1, y=1) in the result. Similarly, "D" at (3, 0) moves to (5, 3).

The dx and/or dy might be **negative** or larger than the overall size of the image. In the example below, translating by a dx of 8, or 14, or 320, or -4, or -6004, etc., would yield the same result as translating by a dx of 2.

Be careful not to confuse the order and meaning of the two indexes in your 2-D array. The first of the two indexes is the row (y), and the second index is the column (x). pixels[i][j] refers to a pixel with (x=j, y=i).

before translate by					(dx	=2,	dy=-1)				aft	er		
	0	1	2	3	4	5			0	1	2	3	4	5
0	Α	В	C	D	Ε	F		0	Κ	L	G	Н	Ι	J
1	G	Н	Ι	J	Κ	L	>	1	Q	R	Μ	N	0	Ρ
2	Μ	N	0	Ρ	Q	R		2	W	Χ	S	Τ	U	V
3	S	Т	U	V	W	Χ		3	F	F	Α	В	C	D

#### public void blur(GImage source)

In this method you should create a new image whose pixel values are averaged with the values of their immediate neighbors from the source image. The general idea is that for a given pixel (r, i) located at row r and column i in the source image, you will change its red, green, and blue components to be the average of the nine red, green, and blue components in the pixels at locations (r-1, i-1) through (r+1, i+1), rounded down to the nearest integer.



For example, in the diagram below, the pixel (row 1, column 2) should be modified to store the average of the nine pixels (0, 1), (0, 2), (0, 3), (1, 1), (1, 2), (1, 3), (2, 0), (2, 1), and (2, 2). These are the eight neighbors of (1, 2) as well as (1, 2) itself. So the red part of (1, 2) would be changed from 32 to (84+74+16+66+32+95+28+47+31)/9 = 52. The green component would be changed from 67 to (22+38+17+53+67+65+49+21+41)/9 = 41. The blue component would be changed from 12 to (99+69+18+88+12+35+31+94+51)/9 = 55. Therefore the overall pixel value at (1, 2) in the result image would be (52, 41, 55).

A special case is the set of pixels along the **edges** of the image. When blurring those pixels, they do not have eight neighbors like other pixels do, so the average includes fewer data points. For example, in the diagram below, the pixel at (row 0, column 0) has no neighbors above or left of it, so it should become the average of the four pixels (0, 0), (0, 1), (1, 0), and (1, 1). So the red component of (0, 0) would become (14+84+21+66)/4 = 46, and so on. The pixel at (3, 3) has no neighbors below it, so it should become the average of the six pixels (2, 2), (2, 3), (2, 4), (3, 2), (3, 3), and (3, 4). The red component of (3, 3) would become (47+31+246+15+60+188)/6 = 97, and so on. Take care that your algorithm does not crash by trying to access outside the bounds of the array.

A common bug in this algorithm is to try to modify the pixel array <u>in-place</u>. You should not do this; you should create a new **second pixel array** to store the result image's pixels. The reason is because you don't want modifications made to one pixel to impact another pixel in the same pass over the array. In our previous example, we already stated that pixel (1, 2) should be changed from (32, 67, 12) to (52, 41, 55). But if you store (52, 41, 55) into this pixel and then use that value for further calculations on pixels in the same pass over the array, their averages will be incorrect. For example, when computing the average for pixel (1, 3), the pixel (1, 2) is one of its neighbors. But you should use that pixel's original value of (32, 67, 12) when computing that average.

	0	1	2	3	4
0	(14, 97, 63)	(84, 22, 99)	(74, 38, 69)	(16, 17, 18)	(85, 75, 75)
1	(21, 18, 45)	(66, 53, 88)	(32, 67, 12)	(95, 65, 35)	(6, 0, 2)
2	(37, 29, 61)	(28, 49, 31)	(47, 21, 94)	(31, 41, 51)	(246, 84, 13)
3	(82, 33, 90)	(42, 43, 44)	(15, 80, 50)	(60, 40, 12)	(188, 45, 1)

## public void mystery(GImage source) (creative aspect)

After implementing the other image algorithms, you should come up with one more algorithm of your choice named mystery that does anything you want. This algorithm can do anything to the source image as long as it is not essentially the same as one of the existing image algorithms in this assignment or shown in lecture/section. Your algorithm should make some kind of visible change to the source image on the screen, but beyond that it can do anything you want. For example, you



could zoom the image, or make funny changes to its colors, or sharpen it, or any number of interesting manipulations. You might want to search the web for ideas of interesting algorithms that can be performed on pixels of images. In your comments, explain what your mystery method is doing so that it is clear to the grader.

This method is worth a very small part of your grade and is meant to give you an outlet to **be creative**, but if you don't want to spend much time on it, just make a simple change to the image and that will be fine.

If you want to add more than one mystery method, our provided code will notice any methods you write with names like mystery1, mystery2, etc. and provide buttons for all of them in the main GUI. You must still have a method whose name is exactly "mystery", but any others whose names start with "mystery" will be used.

**Extra Features:** (Extra features are optional and will earn you a small amount of extra credit if you complete them.)

There are many possibilities for extra features that you can add if you like. If you are going to do extra features, submit two versions of the assignment: the basic Java file that meets all the normal assignment requirements, and an "extra" file such as MelodyExtra.java or ImageAlgorithmsExtra.java containing your extended version. (If your extra features don't break or change the base functionality in any way, you can just put the extra features in the existing Melody.java or ImageAlgorithms.java file.) At the top of your .java file in its comment header, you must comment what extra features you completed. Here are a few ideas for extra features:

- Change key: Can you change a melody from one key to another? This is harder than it sounds because of complexities in music and keying. Read online about different keys and how to convert between them.
- Start playing from a given time offset: Write a variation of the play method that accepts a start time offset as a parameter and plays the melody's notes starting from that time offset.
- *Merge two melodies:* Write a method that accepts another Melody as a parameter and appends its notes to the end of the current Melody.
- Additional melody manipulation: Write more methods that modify your melody's song.
- Lyrics: How would you represent a song that had lyrics that display when certain notes are played?
- Ability to visually compose a song: Provide a user interface where the user can click piano keys to input a song.
- Multiple image mystery methods: Write several neat image mystery manipulations that do interesting things.
- Paint program: Modify our provided ImageMain to have drawing tools like paint brush, line drawing, fill, etc.
- Other: Use your imagination. What other features could you imagine in a program like this?

#### Grading

Functionality: Your code should compile without any errors or warnings. For Problem 1, you can listen to the song to verify it, and you can also check Eclipse's console to see text output of each note as it is played. For Problem 2, we use an Image Comparison Tool to see that your image exactly matches the one expected. You can use the same Image Comparison Tool with expected output images from the class web site to verify your program's behavior.

Style: Follow style guidelines taught in class and listed in the course **Style Guide**. For example, use descriptive **names** for variables and methods. **Format** your code using indentation and whitespace. Avoid **redundancy** using methods, loops, and factoring. Use descriptive **comments**, including the top of each java file, atop each method, inline on complex sections of code, next to each field, and a **citation of all sources** you used to help write your program. If you complete any **extra features**, list them in your comments to make sure the grader knows what you completed. In general, limit yourself to using Java syntax taught in lecture and textbook parts we have read so far.

Fields: As mentioned earlier, in Problem 2 you should not use any **fields** (a.k.a. private instance variables). In Problem 1, fields are allowed and necessary, but you should still minimize the number of fields and generally not make a value a field unless it is necessary to do so. Write a brief **comment** on each field in your code explaining its purpose and why you it is necessary to make that into a field. All fields must be private. If there are important fixed values used in your code, declare them as final **constants**.

Procedural decomposition: Most of the methods you'll need to write on this assignment are already specified for you. But you should still work to avoid redundancy. For example, if two or more specified methods have similar behavior, make one call the other, or create a private method that captures the redundancy and is called by both.

Honor Code: Follow the **Honor Code** when working on this assignment. Submit your own (pair's) work and do not look at others' solutions nor give out your solution. Do not place a solution to this assignment on a public web site or forum. Solutions from this quarter, past quarters, and any solutions found online, will be electronically compared.