

一 四则运算文法

1.1 文法

$$G[E] : E \rightarrow E + T | E - T | T$$

$$T \rightarrow T \times F | T \div F | F$$

$$F \rightarrow (E) | n$$

拓广文法
 \Rightarrow

$$G[S'] : S' \rightarrow E$$

$$E \rightarrow E + T | E - T | T$$

$$T \rightarrow T \times F | T \div F | F$$

$$F \rightarrow (E) | n$$

1.2 非终结符 FIRST 集

$$\text{FIRST}(E) = \{ (, n \}$$

$$\text{FIRST}(T) = \{ (, n \}$$

$$\text{FIRST}(F) = \{ (, n \}$$

1.3 项目集规范族与预测分析表

$S_0 : S' \rightarrow \cdot E, \#$ $E \rightarrow \cdot E + T, \#+-$ $E \rightarrow \cdot E - T, \#+-$ $E \rightarrow \cdot T, \#+-$ $T \rightarrow \cdot T \times F, \#+-\times\div$ $T \rightarrow \cdot T \div F, \#+-\times\div$ $T \rightarrow \cdot F, \#+-\times\div$ $F \rightarrow \cdot (E), \#+-\times\div$ $F \rightarrow \cdot n, \#+-\times\div$	$S_1 : S' \rightarrow E \cdot, \#$ $E \rightarrow E \cdot + T, \#+-$ $E \rightarrow E \cdot - T, \#+-$	$S_2 : E \rightarrow T \cdot, \#+-$ $T \rightarrow T \cdot \times F, \#+-\times\div$ $T \rightarrow T \cdot \div F, \#+-\times\div$
$S_3 : T \rightarrow F \cdot, \#+-\times\div$	$S_4 : F \rightarrow (\cdot E), \#+-\times\div$ $E \rightarrow \cdot E + T,)+-$ $E \rightarrow \cdot E - T,)+-$ $E \rightarrow \cdot T,)+-$ $T \rightarrow \cdot T \times F,)+-\times\div$ $T \rightarrow \cdot T \div F,)+-\times\div$ $T \rightarrow \cdot F,)+-\times\div$ $F \rightarrow \cdot (E),)+-\times\div$ $F \rightarrow \cdot n,)+-\times\div$	$S_5 : F \rightarrow n \cdot, \#+-\times\div$
$S_6 : F \rightarrow (E \cdot), \#+-\times\div$ $E \rightarrow E \cdot + T,)+-$ $E \rightarrow E \cdot - T,)+-$	$S_7 : E \rightarrow T \cdot,)+-$ $T \rightarrow T \cdot \times F,)+-\times\div$ $T \rightarrow T \cdot \div F,)+-\times\div$	$S_8 : T \rightarrow F \cdot,)+-\times\div$

$S_9 : F \rightarrow (\cdot E) \quad ,) + - \times \div$ $E \rightarrow \cdot E + T \quad ,) + -$ $E \rightarrow \cdot E - T \quad ,) + -$ $E \rightarrow \cdot T \quad ,) + -$ $T \rightarrow \cdot T \times F \quad ,) + - \times \div$ $T \rightarrow \cdot T \div F \quad ,) + - \times \div$ $T \rightarrow \cdot F \quad ,) + - \times \div$ $F \rightarrow \cdot (E) \quad ,) + - \times \div$ $F \rightarrow \cdot n \quad ,) + - \times \div$	$S_{10} : F \rightarrow n \cdot \quad ,) + - \times \div$	$S_{11} : F \rightarrow (E \cdot) \quad ,) + - \times \div$ $E \rightarrow E \cdot + T \quad ,) + -$ $E \rightarrow E \cdot - T \quad ,) + -$
$S_{12} : F \rightarrow (E) \cdot \quad ,) + - \times \div$	$S_{13} : E \rightarrow E + \cdot T \quad ,) + -$ $T \rightarrow \cdot T \times F \quad ,) + - \times \div$ $T \rightarrow \cdot T \div F \quad ,) + - \times \div$ $T \rightarrow \cdot F \quad ,) + - \times \div$ $F \rightarrow \cdot (E) \quad ,) + - \times \div$ $F \rightarrow \cdot n \quad ,) + - \times \div$	$S_{14} : E \rightarrow E - \cdot T \quad ,) + -$ $T \rightarrow \cdot T \times F \quad ,) + - \times \div$ $T \rightarrow \cdot T \div F \quad ,) + - \times \div$ $T \rightarrow \cdot F \quad ,) + - \times \div$ $F \rightarrow \cdot (E) \quad ,) + - \times \div$ $F \rightarrow \cdot n \quad ,) + - \times \div$
$S_{15} : E \rightarrow E - T \cdot \quad ,) + -$ $T \rightarrow T \cdot \times F \quad ,) + - \times \div$ $T \rightarrow T \cdot \div F \quad ,) + - \times \div$	$S_{16} : T \rightarrow T \times \cdot F \quad ,) + - \times \div$ $F \rightarrow \cdot (E) \quad ,) + - \times \div$ $F \rightarrow \cdot n \quad ,) + - \times \div$	$S_{17} : T \rightarrow T \div \cdot F \quad ,) + - \times \div$ $F \rightarrow \cdot (E) \quad ,) + - \times \div$ $F \rightarrow \cdot n \quad ,) + - \times \div$
$S_{18} : T \rightarrow T \div F \cdot \quad ,) + - \times \div$	$S_{19} : T \rightarrow T \times F \cdot \quad ,) + - \times \div$	$S_{20} : E \rightarrow E + T \cdot \quad ,) + -$ $T \rightarrow T \cdot \times F \quad ,) + - \times \div$ $T \rightarrow T \cdot \div F \quad ,) + - \times \div$
$S_{21} : F \rightarrow (E) \cdot \quad , \# + - \times \div$	$S_{22} : T \rightarrow T \times \cdot F \quad , \# + - \times \div$ $F \rightarrow \cdot (E) \quad , \# + - \times \div$ $F \rightarrow \cdot n \quad , \# + - \times \div$	$S_{23} : T \rightarrow T \div \cdot F \quad , \# + - \times \div$ $F \rightarrow \cdot (E) \quad , \# + - \times \div$ $F \rightarrow \cdot n \quad , \# + - \times \div$
$S_{24} : T \rightarrow T \div F \cdot \quad , \# + - \times \div$	$S_{25} : T \rightarrow T \times F \cdot \quad , \# + - \times \div$	$S_{26} : E \rightarrow E + \cdot T \quad , \# + -$ $T \rightarrow \cdot T \times F \quad , \# + - \times \div$ $T \rightarrow \cdot T \div F \quad , \# + - \times \div$ $T \rightarrow \cdot F \quad , \# + - \times \div$ $F \rightarrow \cdot (E) \quad , \# + - \times \div$ $F \rightarrow \cdot n \quad , \# + - \times \div$
$S_{27} : E \rightarrow E - \cdot T \quad , \# + -$ $T \rightarrow \cdot T \times F \quad , \# + - \times \div$ $T \rightarrow \cdot T \div F \quad , \# + - \times \div$ $T \rightarrow \cdot F \quad , \# + - \times \div$ $F \rightarrow \cdot (E) \quad , \# + - \times \div$ $F \rightarrow \cdot n \quad , \# + - \times \div$	$S_{28} : E \rightarrow E - T \cdot \quad , \# + -$ $T \rightarrow T \cdot \times F \quad , \# + - \times \div$ $T \rightarrow T \cdot \div F \quad , \# + - \times \div$	$S_{29} : E \rightarrow E + T \cdot \quad , \# + -$ $T \rightarrow T \cdot \times F \quad , \# + - \times \div$ $T \rightarrow T \cdot \div F \quad , \# + - \times \div$

表 1 LR(1) 项目集表

状态	ACTION								GOTO		
	+	-	\times	\div	()	n	#	E	T	F
0					S_4		S_5		1	2	3
1	S_{26}	S_{27}						ACC			
2	R_{E-2}	R_{E-2}	S_{22}	S_{23}				R_{E-2}			
3	R_{T-2}	R_{T-2}	R_{T-2}	R_{T-2}				R_{T-2}			
4					S_9		S_{10}		6	7	8
5	R_{F-1}	R_{F-1}	R_{F-1}	R_{F-1}				R_{F-1}			
6	S_{13}	S_{14}				S_{21}					
7	R_{E-2}	R_{E-2}	S_{16}	S_{17}		R_{E-2}					
8	R_{T-2}	R_{T-2}	R_{T-2}	R_{T-2}		R_{T-2}					
9					S_9		S_{10}		11	7	8
10	R_{F-1}	R_{F-1}	R_{F-1}	R_{F-1}		R_{F-1}					
11	S_{13}	S_{14}				S_{12}					
12	R_{F-0}	R_{F-0}	R_{F-0}	R_{F-0}		R_{F-0}					
13					S_9		S_{10}			20	8
14					S_9		S_{10}			15	8
15	R_{E-1}	R_{E-1}	S_{16}	S_{17}		R_{E-1}					
16					S_9		S_{10}				19
17					S_9		S_{10}				18
18	R_{T-1}	R_{T-1}	R_{T-1}	R_{T-1}		R_{T-1}					
19	R_{T-0}	R_{T-0}	R_{T-0}	R_{T-0}		R_{T-0}					
20	R_{E-0}	R_{E-0}	S_{16}	S_{17}		R_{E-0}					
21	R_{F-0}	R_{F-0}	R_{F-0}	R_{F-0}				R_{F-0}			
22					S_4		S_5				25
23					S_4		S_5				24
24	R_{T-1}	R_{T-1}	R_{T-1}	R_{T-1}				R_{T-1}			
25	R_{T-0}	R_{T-0}	R_{T-0}	R_{T-0}				R_{T-0}			
26					S_4		S_5			29	3
27					S_4		S_5			28	3
28	R_{E-1}	R_{E-1}	S_{22}	S_{23}				R_{E-1}			
29	R_{E-0}	R_{E-0}	S_{22}	S_{23}				R_{E-0}			

表 2 LR(1) 预测分析表

1.4 分析过程

步骤	状态栈	符号栈	输入串	ACTION	GOTO
1	0	#	$(n+n)\times n-n\div n\#$	S_4	
2	0,4	#($n+n)\times n-n\div n\#$	S_{10}	
3	0,4,10	#(n	$+n)\times n-n\div n\#$	R_{F-1}	8

4	0,4,8	$\#(F$	$+n)\times n-n\div n\#$	R_{T-2}	7
5	0,4,7	$\#(T$	$+n)\times n-n\div n\#$	R_{E-2}	6
6	0,4,6	$\#(E$	$+n)\times n-n\div n\#$	S_{13}	
7	0,4,6,13	$\#(E+$	$n)\times n-n\div n\#$	S_{10}	
8	0,4,6,13,10	$\#(E+n$	$)\times n-n\div n\#$	R_{F-1}	8
9	0,4,6,13,8	$\#(E+F$	$)\times n-n\div n\#$	R_{T-2}	20
10	0,4,6,13,20	$\#(E+T$	$)\times n-n\div n\#$	R_{E-0}	6
11	0,4,6	$\#(E$	$)\times n-n\div n\#$	S_{21}	
12	0,4,6,21	$\#(E)$	$\times n-n\div n\#$	R_{F-0}	3
13	0,3	$\#F$	$\times n-n\div n\#$	R_{T-2}	2
14	0,2	$\#T$	$\times n-n\div n\#$	S_{22}	
15	0,2,22	$\#T\times$	$n-n\div n\#$	S_5	
16	0,2,22,5	$\#T\times n$	$-n\div n\#$	R_{F-1}	25
17	0,2,22,25	$\#T\times F$	$-n\div n\#$	R_{T-0}	2
18	0,2	$\#T$	$-n\div n\#$	R_{E-2}	1
19	0,1	$\#E$	$-n\div n\#$	S_{27}	
20	0,1,27	$\#E-$	$n\div n\#$	S_5	
21	0,1,27,5	$\#E-n$	$\div n\#$	R_{F-1}	3
22	0,1,27,3	$\#E-F$	$\div n\#$	R_{T-2}	28
23	0,1,27,28	$\#E-T$	$\div n\#$	S_{23}	
24	0,1,27,28,23	$\#E-T\div$	$n\#$	S_5	
25	0,1,27,28,23,5	$\#E-T\div n$	$\#$	R_{F-1}	24
26	0,1,27,28,23,24	$\#E-T\div F$	$\#$	R_{T-1}	28
27	0,1,27,28	$\#E-T$	$\#$	R_{E-1}	1
28	0,1	$\#E$	$\#$	ACC	

表3 $(n+n)\times n-n\div n$ 的 LR(1) 分析过程

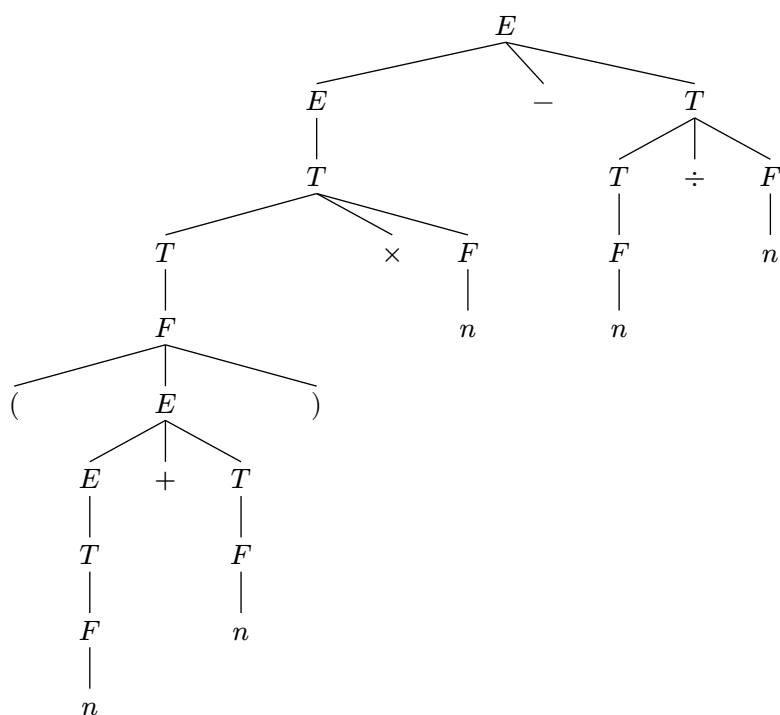


图 1 $(n+n) \times n - n \div n$ 的 LR(1) 语法树

二 非 LR1 文法

2.1 文法

$$G[S] : S \rightarrow Aa|Bb$$

$$A \rightarrow Ab|\varepsilon|b$$

$$B \rightarrow Ba|\varepsilon$$

拓广文法
 \Rightarrow

$$G[S'] : S' \rightarrow S$$

$$S \rightarrow Aa|Bb$$

$$A \rightarrow Ab|\varepsilon|b$$

$$B \rightarrow Ba|\varepsilon$$

2.2 非终结符 FIRST 集

$$\text{FIRST}(S) = \{b, a\}$$

$$\text{FIRST}(A) = \{\varepsilon, b\}$$

$$\text{FIRST}(B) = \{\varepsilon, a\}$$

2.3 项目集规范族与预测分析表

$S_0 : S' \rightarrow \cdot S , \#$ $S \rightarrow \cdot Aa , \#$ $S \rightarrow \cdot Bb , \#$ $A \rightarrow \cdot Ab , ab$ $A \rightarrow \cdot , ab$ $A \rightarrow \cdot b , ab$ $B \rightarrow \cdot Ba , ba$ $B \rightarrow \cdot , ba$	$S_1 : S' \rightarrow S \cdot , \#$	$S_2 : S \rightarrow A \cdot a , \#$ $A \rightarrow A \cdot b , ab$
$S_3 : S \rightarrow B \cdot b , \#$ $B \rightarrow B \cdot a , ba$	$S_4 : A \rightarrow b \cdot , ab$	$S_5 : S \rightarrow Bb \cdot , \#$
$S_6 : B \rightarrow Ba \cdot , ba$	$S_7 : S \rightarrow Aa \cdot , \#$	$S_8 : A \rightarrow Ab \cdot , ab$

表 4 LR(1) 项目集表

状态	ACTION			GOTO		
	<i>a</i>	<i>b</i>	#	<i>S</i>	<i>A</i>	<i>B</i>
0	R_{A-1}, R_{B-1}	S_4, R_{A-1}, R_{B-1}		1	2	3
1			ACC			
2	S_7	S_8				
3	S_6	S_5				
4	R_{A-2}	R_{A-2}				
5			R_{S-1}			
6	R_{B-0}	R_{B-0}				
7			R_{S-0}			
8	R_{A-0}	R_{A-0}				

表 5 LR(1) 预测分析表

!!! 该文法非 LR1 文法