

Gebze Technical University
Computer Engineering

CSE 222
2017 Spring

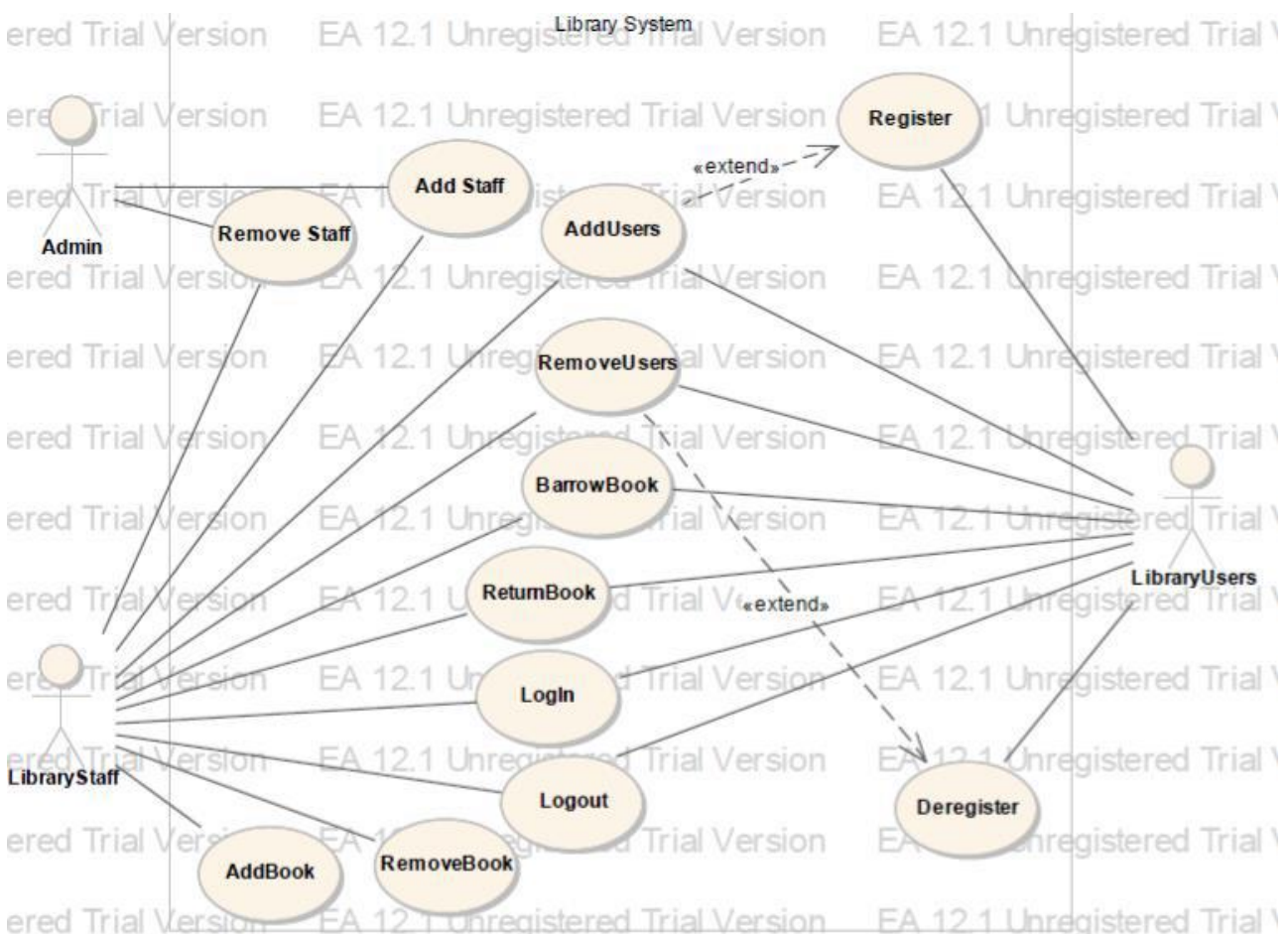
HOMEWORK 02 REPORT

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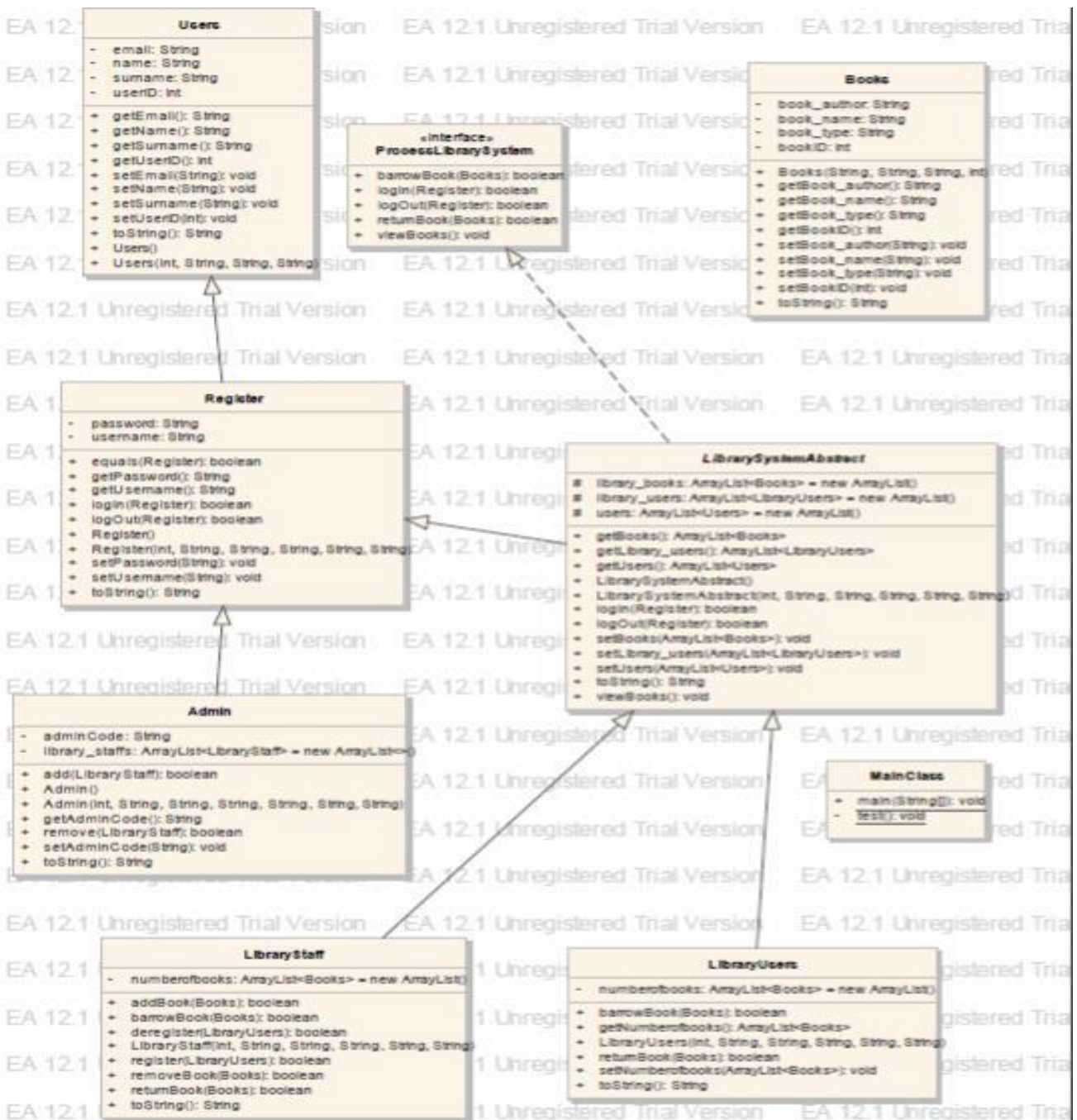
1. System Requirements

- Sistemim 8 classtan oluşuyor
- Classlarım:Admin, Users, LibraryStaff, LibraryUsers, Register, Books, LibrarySystemAbstract, ProcessLibrarySystem. Ve main Classtan oluşuyor.
- Admin Classım:
 - ✓ staffları add/remove yapabilir.
- Staff Classım:
 - ✓ User add/remove,
 - ✓ User register/deregister,
 - ✓ Book add/remove,
 - ✓ Barrow/return,
 - ✓ Log In/Log Out yapabilir.
- User Classım:
 - ✓ Log in/log out,
 - ✓ Barrow/return yapabilir.

2. Use Case Diagrams



3. Class Diagrams



4. Other Diagrams

..

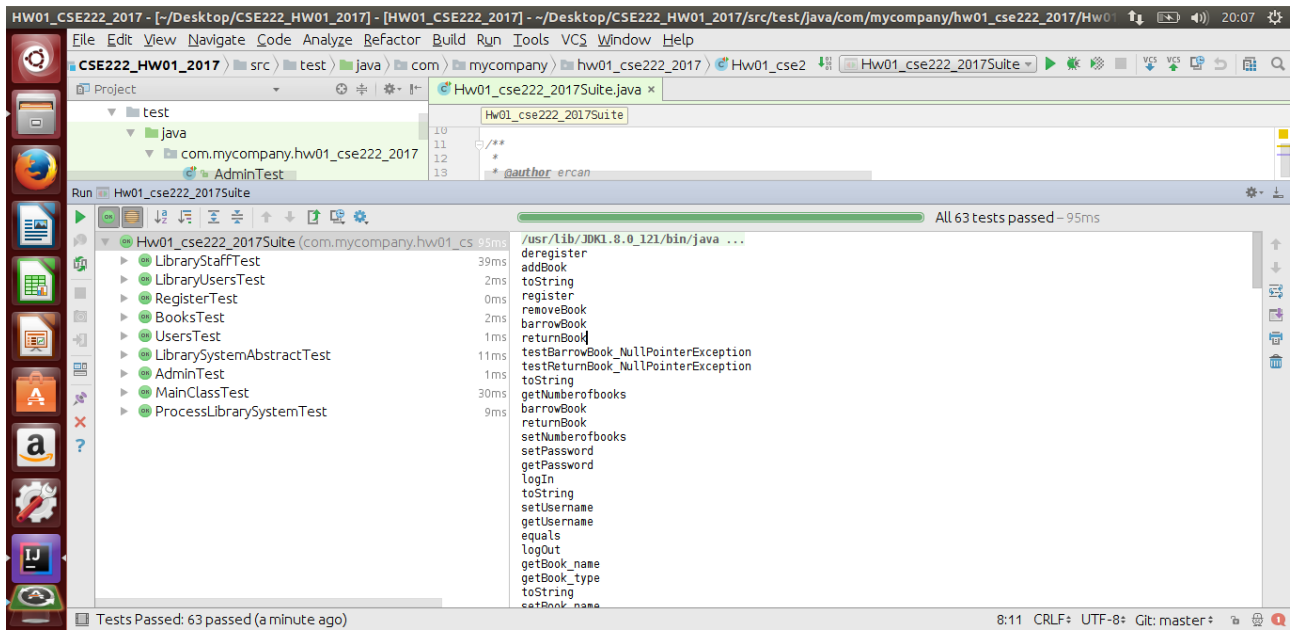
5. Problem Solutions Approach

- ✓ LibrarySystemAbstract classım ile ortak yapılan işlemler (logIn/logOut veya Barrow/return) ları bu abstract classımda tanımladım.
- ✓ Ortak olmayanlar ise bu classı extend ederek.
- ✓ Kendi yapabildiklerini kendisinde yeniden implement edebilir yapıyı sağladım.
- ✓ Bu sayede polymorphism sağlanmış oldu.
- ✓ User ve staffın ortak yaptıklarını ise yeniden implement edilebilir yapılrısa ovirrede yapılmış oldu.

(Sistemin basit omurga yapısı.)

- ✓ Admin oluşturularak işleme başlandı.
- ✓ Admin staff oluşturdu.
- ✓ Staff log In yaptı.
- ✓ Staff da, register user/add user yaptı
- ✓ Ayrı olarak kitaplar oluşturuldu.
- ✓ Staff kitapları add yaptı.
- ✓ Register olan kullanıcı log in yaptı.
- ✓ Kullanıcı barrow book yaptı.
- ✓ Kitabı return book yaptı.
- ✓ Kullanıcı log out yaptı.
- ✓ Staff log out yaptı.

6. Test Cases



HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/test/java/com/mycompany/hw01_cse222_2017/LibraryUsersTest

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 | src | test | java | com | mycompany | hw01_cse222_2017 | LibraryUsersTest | LibraryUsersTest

Project | java | com.mycompany.hw01_cse222_2017 | AdminTest | BooksTest | Hw01_cse222_2017Suite | LibraryStaffTest | LibrarySystemAbstractTest | LibraryUsersTest | MainClassTest | ProcessLibrarySystemTest | RegisterTest

LibraryUsersTest.java

```
15 16 17 18 19 20 21 22 23 24 25 26 27 28
import ...
/**
 * @author ercan
 */
public class LibraryUsersTest {
    public LibraryUsersTest() {
    }

    @BeforeClass
    public static void setUpClass() {
    }
}
```

Run | LibraryUsersTest | All tests passed - 68ms

LibraryUsersTest (com.mycompany.hw01_cse222_2017) 68ms

- testToString 65ms
- testGetNumberOfbooks 0ms
- testBarrowBook 3ms
- testReturnBook 0ms
- testSetNumberOfbooks 0ms

Process finished with exit code 0

Tests Passed: 5 passed (moments ago) 9:1 CRLF UTF-8 Git: master

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/test/java/com/mycompany/hw01_cse222_2017/ProcessLibrarySystemTest

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 | src | test | java | com | mycompany | hw01_cse222_2017 | ProcessLibrarySystemTest | ProcessLibrarySystemTest

Project | java | com.mycompany.hw01_cse222_2017 | AdminTest | BooksTest | Hw01_cse222_2017Suite | LibraryStaffTest | LibrarySystemAbstractTest | LibraryUsersTest | MainClassTest | ProcessLibrarySystemTest | RegisterTest

ProcessLibrarySystemTest.java

```
17 18 19 20 21 22 23 24 25 26 27 28 29 30
import ...
/**
 * @author ercan
 */
public class ProcessLibrarySystemTest {
    public ProcessLibrarySystemTest() {
    }

    @BeforeClass
    public static void setUpClass() {
    }

    @AfterClass
    public static void tearDownClass() {
    }
}
```

Run | ProcessLibrarySystemTest | All tests passed - 51ms

ProcessLibrarySystemTest (com.mycompany.hw01_cse222_2017) 51ms

- testLogin 43ms
- testViewBooks 0ms
- testBarrowBook 1ms
- testReturnBook 7ms
- testLogout 0ms

Process finished with exit code 0

Tests Passed: 5 passed (moments ago) 9:1 CRLF UTF-8 Git: master

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/test/java/com/mycompany/hw01_cse222_2017/RegisterTest

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 | src | test | java | com | mycompany | hw01_cse222_2017 | RegisterTest | RegisterTest

Project | java | com.mycompany.hw01_cse222_2017 | BooksTest | Hw01_cse222_2017Suite | LibraryStaffTest | LibrarySystemAbstractTest | LibraryUsersTest | MainClassTest | ProcessLibrarySystemTest | RegisterTest | UsersTest

RegisterTest.java

```
14 15 16 17 18 19 20 21 22 23 24 25 26 27
import ...
/**
 * @author ercan
 */
public class RegisterTest {
    public RegisterTest() {
    }

    @BeforeClass
    public static void setUpClass() {
    }
}
```

Run | RegisterTest | All tests passed - 19ms

RegisterTest (com.mycompany.hw01_cse222_2017) 19ms

- testSetPassword 18ms
- testGetPassword 0ms
- testLogin 0ms
- testToString 1ms
- testSetUsername 0ms
- testGetUsername 0ms
- testEquals 0ms
- testLogout 0ms

Process finished with exit code 0

Tests Passed: 8 passed (moments ago) 12:1 CRLF UTF-8 Git: master

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/test/java/com/mycompany/hw01_cse222_2017/Main

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 > src > test > java > com > mycompany > hw01_cse222_2017 > MainClassTest > MainClassTest.testMain

Project

- java
 - com.mycompany.hw01_cse222_2017
 - AdminTest
 - BooksTest
 - Hw01_cse222_2017Suite
 - LibraryStaffTest
 - LibrarySystemAbstractTest
 - LibraryUsersTest
 - MainClassTest
 - ProcessLibrarySystemTest
 - RegisterTest

MainClassTest.java

```
41 // Test of main method, of class MainClass.
42 //
43 // org.junit.Test
44 public void testMain() {
45     System.out.println("main");
46     String[] args = null;
47     MainClass.main(args);
48     // TODO review the generated test code and remove the default call to fail.
49     //fail("The test case is a prototype.");
50 }
51
52 }
53
```

Run MainClassTest.testMain

1 test passed - 72ms

MainClassTest (com.mycompany.hw01_cse222_2017) 72ms

```
testMain
72ms
Books(book_name=C++, book_author=Author2, book_type=C++, bookID=1234)

-----Library user return book one by User3!-----
View Library User 3 After return a book
LibraryUsers(Register(Users{
  userID=2, name=Bekir, surname=Kurt, email=bekirkurt@hotmail.com
  username=bekirkurt, password=bekir11} numberOfbooks=1
  Books(book_name=C++, book_author=Author2, book_type=C++, bookID=1234)
})
-----Log Out Library User3 Successfull!-----
-----END OF SYSTEM-----

Process finished with exit code 0
```

Tests Passed: 1 passed (moments ago) 11:31 CRLF UTF-8 Git: master

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/test/java/com/mycompany/hw01_cse222_2017/UsersTest

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 > src > test > java > com > mycompany > hw01_cse222_2017 > UsersTest

Project

- target
 - classes

UsersTest.java

```
14 //
15 //
16 //
17 // @author ercan
18 //
19 public class UsersTest {
20
21     public UsersTest() {
22     }
23
24     @BeforeClass
25     public static void setUpClass() {
26     }
27
28 }

```

Run UsersTest

All 9 tests passed - 32ms

UsersTest (com.mycompany.hw01_cse222_2017) 32ms

```
testGetEmail 30ms /usr/lib/jdk1.8.0_121/bin/java ...
testGetSurname 0ms getEmail
testToString 0ms getSurname
testGetName 0ms toString
testSetName 1ms getName
testSetSurname 0ms setSurname
testSetUserID 0ms setUserID
testGetUserID 0ms getUserID
testSetName 1ms setName
testSetEmail 0ms setEmail
testSetEmail 0ms setEmail

Process finished with exit code 0
```

Tests Passed: 9 passed (moments ago) 13:1 CRLF UTF-8 Git: master

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/main/java/com/mycompany/hw01_cse222_2017/Admin

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 > src > test > java > com > mycompany > hw01_cse222_2017 > AdminTest

Project

- target
 - classes

AdminTest.java

```
76 //
77 //
78 //
79 //
80 //
81 //
82 //
83 //
84 //
85 //
86 //
87 //
88 //
89 //
90 //
91 //
92 //
93 //

```

Run AdminTest

All 7 tests passed - 78ms

AdminTest (com.mycompany.hw01_cse222_2017) 78ms

```
testAdd_NullPointerException 51ms /usr/lib/jdk1.8.0_121/bin/java ...
testSetAdminCode 0ms testAdd_NullPointerException
testAdd 17ms setAdminCode
testToString 0ms add
testRemove_NullPointerException 0ms toString
testGetAdminCode 0ms testRemove_NullPointerException
testRemove 10ms getAdminCode
testRemove 0ms remove

Process finished with exit code 0
```

Tests Passed: 7 passed (moments ago) 11:1 CRLF UTF-8 Git: master

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/main/java/com/mycompany/hw01_cse222_2017/Admin

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 | src | test | java | com | mycompany | hw01_cse222_2017 | BooksTest

Project | java | com.mycompany.hw01_cse222_2017 | AdminTest | BooksTest | Hw01_cse222_2017Suite | LibraryStaffTest | LibrarySystemAbstractTest | LibraryUsersTest | MainClassTest | ProcessLibrarySystemTest | RegisterTest | UsersTest | target

Run | AdminTest | All tests passed - 59ms

Test results for AdminTest (com.mycompany.hw01_cse222_2017):

- testAdd_NullPointerException: 59ms
- testSetAdminCode: 41ms
- testAdd: 0ms
- testToString: 13ms
- testRemove_NullPointerException: 4ms
- testGetAdminCode: 0ms
- testRemove: 1ms

Process finished with exit code 0

Tests Passed: 7 passed (moments ago)

```
Admin.java
76 public boolean remove(LibraryStaff staff) throws NullPointerException, Error {
77     if (staff == null)
78         throw new NullPointerException("Can't remove null object.");
79     else if (library_staffs.isEmpty())
80         throw new Error("No library staff");
81     return library_staffs.remove(staff);
82 }
83 /**
84  * View information about administrator
85  * @return information of administrator
86  */
87 @Override
88 public String toString() {
89     return "Admin{" + super.toString() + ", adminCode=" + adminCode + ",\n\tlibrary_staffs=" + library_staffs + "}";
90 }
91 }
92
93
```

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/main/java/com/mycompany/hw01_cse222_2017/Admin

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 | src | test | java | com | mycompany | hw01_cse222_2017 | LibraryStaffTest

Project | java | com.mycompany.hw01_cse222_2017 | AdminTest | BooksTest | Hw01_cse222_2017Suite | LibraryStaffTest | LibrarySystemAbstractTest | LibraryUsersTest | MainClassTest | ProcessLibrarySystemTest | RegisterTest | UsersTest | target

Run | LibraryStaffTest | All 9 tests passed - 48ms

Test results for LibraryStaffTest (com.mycompany.hw01_cse222_2017):

- deregister: 48ms
- addBook: 33ms
- toString: 1ms
- removeBook: 0ms
- barrowBook: 0ms
- returnBook: 13ms
- testBarrowBook_NullPointerException: 0ms
- testReturnBook_NullPointerException: 0ms
- testBarrowBook_NullPointerException: 1ms
- testReturnBook_NullPointerException: 0ms

Process finished with exit code 0

Tests Passed: 9 passed (moments ago)

```
Admin.java
76 public boolean remove(LibraryStaff staff) throws NullPointerException, Error {
77     if (staff == null)
78         throw new NullPointerException("Can't remove null object.");
79     else if (library_staffs.isEmpty())
80         throw new Error("No library staff");
81     return library_staffs.remove(staff);
82 }
83 /**
84  * View information about administrator
85  * @return information of administrator
86  */
87 @Override
88 public String toString() {
89     return "Admin{" + super.toString() + ", adminCode=" + adminCode + ",\n\tlibrary_staffs=" + library_staffs + "}";
90 }
91 }
92
93
```

HW01_CSE222_2017 - [~/Desktop/CSE222_HW01_2017] - [HW01_CSE222_2017] - ~/Desktop/CSE222_HW01_2017/src/test/java/com/mycompany/hw01_cse222_2017/LibrarySystemAbstractTest

File Edit View Navigate Code Analyze Refactor Build Run Tools VCS Window Help

CSE222_HW01_2017 | src | test | java | com | mycompany | hw01_cse222_2017 | LibrarySystemAbstractTest

Project | java | com.mycompany.hw01_cse222_2017 | AdminTest | BooksTest | Hw01_cse222_2017Suite | LibraryStaffTest | LibrarySystemAbstractTest | LibraryUsersTest | MainClassTest | ProcessLibrarySystemTest | RegisterTest | UsersTest | target

Run | LibrarySystemAbstractTest | All 10 tests passed - 46ms

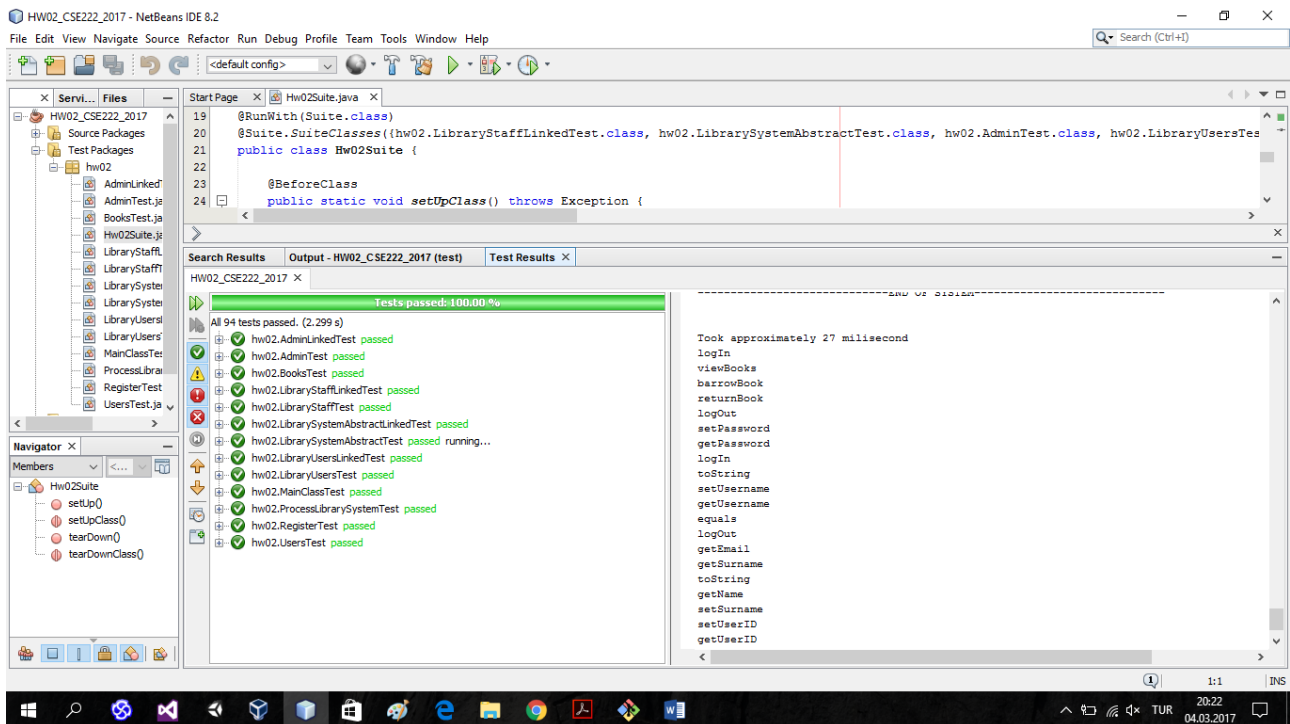
Test results for LibrarySystemAbstractTest (com.mycompany.hw01_cse222_2017):

- getBooks: 46ms
- getUsers: 38ms
- login: 0ms
- setLibrary_users: 0ms
- toString: 1ms
- viewBooks: 0ms
- getLibrary_users: 0ms
- logout: 0ms
- setBooks: 0ms
- setUsers: 7ms

Process finished with exit code 0

Tests Passed: 10 passed (moments ago)

```
LibrarySystemAbstractTest.java
15 /**
16  *
17  * @author ercan
18  */
19 public class LibrarySystemAbstractTest {
20     public LibrarySystemAbstractTest() {
21     }
22     @BeforeClass
23     public static void setUpClass() {
24     }
25 }
26
27
28
```



7. Running and Results

-----Created admin!-----

View Admin

```
Admin{
    Register{Users{
        userID=11, name=Ercan, surname=UCA, email=ercanuca@gmail.com}
        username=ercanuca, password=1234}, adminCode=1111,
        library_staffs=[]}
```

-----Created staff!-----

View Staff

```
LibraryStaff{
    Register{Users{
        userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
        username=kenankurt, password=1234}
    []
    library_books=[]
}
```

-----Add staff by admin-----

After added Staff View Admin

```
Admin{
    Register{Users{
        userID=11, name=Ercan, surname=UCA, email=ercanuca@gmail.com}
        username=ercanuca, password=1234}, adminCode=1111,
        library_staffs=[
            LibraryStaff{
                Register{Users{
                    userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
```



```

        username=kenankurt, password=1234}
        []
        library_books=[]
    }}}

```

-----Created 2 Books!-----

-----Add Books by staff-----

After added 2 books View books by staff

```

LibraryStaff{
    Register{ Users{
        userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
        username=kenankurt, password=1234}
        []
        library_books=[
            Books{book_name=System Programlama, book_author=Author1, book_type=C and
C++, bookID=4583}
        ,
            Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
        ]
    }
}

```

-----Created Library User!-----

-----Registered Library User by Staff!-----

```

LibraryStaff{
    Register{ Users{
        userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
        username=kenankurt, password=1234}
        [LibraryUsers{ Register{ Users{
            userID=0, name=Elif, surname=Serap, email=elifserap.1@gmail.com}
            username=elif, password=222} numberOfbooks=[]}]
        library_books=[
            Books{book_name=System Programlama, book_author=Author1, book_type=C and
C++, bookID=4583}
        ,
            Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
        ]
    }
}

```

-----Created Library User2!-----

View Library User 2

```

LibraryUsers{ Register{ Users{
    userID=1, name=Yagmur, surname=Can, email=yagmurcan2@gmail.com}
    username=yagmurcan, password=321} numberOfbooks=[]}
}

```

-----Registered Library User2!-----

-----Created Library User3!-----

View Library User 3

```

LibraryUsers{ Register{ Users{

```

```
userID=2, name=Bekir, surname=Kurt, email=bekirkurt@hotmail.com}
username=bekirkurt, password=bekir11 } numberOfbooks=[]}
```

-----Register User3!-----

-----Registered Successfull!-----

-----Log In Library User3 Successfull!-----

-----Library user barrow 2 book User3!-----

```
[
    Books{book_name=System Programlama, book_author=Author1, book_type=C and
C++, bookID=4583}
,
    Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
]*****
```

View Library User 3 After barrow 2 books

```
LibraryUsers{Register{ Users{
    userID=2, name=Bekir, surname=Kurt, email=bekirkurt@hotmail.com}
    username=bekirkurt, password=bekir11 } numberOfbooks=[
        Books{book_name=System Programlama, book_author=Author1, book_type=C and
C++, bookID=4583}
,
        Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
    ]}
```

-----Library user return book one by User3!-----

View Library User 3 After return a book

```
LibraryUsers{Register{ Users{
    userID=2, name=Bekir, surname=Kurt, email=bekirkurt@hotmail.com}
    username=bekirkurt, password=bekir11 } numberOfbooks=[
        Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
    ]}
```

-----Log Out Library User3 Successfull!-----

-----END OF SYSTEM-----

Took approximately 43 milisecond

-----Created admin!-----

View Admin

```
Admin{
    Register{ Users{
        userID=11, name=Ercan, surname=UCA, email=ercanuca@gmail.com}
        username=ercanuca, password=1234 }, adminCode=1111,
        library_staffs=[]}
```

-----Created staff!-----

View Staff

```
LibraryStaff{
  Register{ Users{
    userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
    username=kenankurt, password=1234}
  []
  library_books=[]
}
```

-----Add staff by admin-----

After added Staff View Admin

```
Admin{
  Register{ Users{
    userID=11, name=Ercan, surname=UCA, email=ercanuca@gmail.com}
    username=ercanuca, password=1234}, adminCode=1111,
    library_staffs=[
      LibraryStaff{
        Register{ Users{
          userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
          username=kenankurt, password=1234}
        []
        library_books=[]
      }
    ]
  }
}
```

-----Created 2 Books!-----

-----Add Books by staff-----

After added 2 books View books by staff

```
LibraryStaff{
  Register{ Users{
    userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
    username=kenankurt, password=1234}
  []
  library_books=[
    Books{book_name=System Programlama, book_author=Author1, book_type=C and
    C++, bookID=4583}
    ,
    Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
  ]
}
```

-----Created Library User!-----

-----Registered Library User by Staff!-----

```
LibraryStaff{
  Register{ Users{
    userID=0, name=Kenan, surname=Kurt, email=kenankara12@hotmail.com}
    username=kenankurt, password=1234}
  [LibraryUsers{ Register{ Users{
    userID=0, name=Elif, surname=Serap, email=elifserap.1@gmail.com}
  }}
]
```

```

        username=eliff, password=222} numberofbooks=[]}]
        library_books=[
            Books{book_name=System Programlama, book_author=Author1, book_type=C and
C++, bookID=4583}
        ,
            Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
        ]
    }
}

```

-----Created Library User2!-----

View Library User 2

```

LibraryUsers{Register{Users{
    userID=1, name=Yagmur, surname=Can, email=yagmurcan2@gmail.com}
    username=yagmurcan, password=321} numberofbooks=[]}
}

```

-----Registered Library User2!-----

-----Created Library User3!-----

View Library User 3

```

LibraryUsers{Register{Users{
    userID=2, name=Bekir, surname=Kurt, email=bekirkurt@hotmail.com}
    username=bekirkurt, password=bekir11} numberofbooks=[]}
}

```

-----Register User3!-----

-----Registered Successfull!-----

-----Log In Library User3 Successfull!-----

-----Library user barrow 2 book User3!-----

```

[
    Books{book_name=System Programlama, book_author=Author1, book_type=C and
C++, bookID=4583}
    ,
    Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
]*****

```

View Library User 3 After barrow 2 books

```

LibraryUsers{Register{Users{
    userID=2, name=Bekir, surname=Kurt, email=bekirkurt@hotmail.com}
    username=bekirkurt, password=bekir11} numberofbooks=[
        Books{book_name=System Programlama, book_author=Author1, book_type=C and
C++, bookID=4583}
    ,
        Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
    ]}
}

```

-----Library user return book one by User3!-----

View Library User 3 After return a book

```
LibraryUsers{Register{Users{
    userID=2, name=Bekir, surname=Kurt, email=bekirkurt@hotmail.com}
    username=bekirkurt, password=bekir11} numberofbooks=[
        Books{book_name=C++, book_author=Author2, book_type=C++, bookID=1234}
    ]}
-----Log Out Library User3 Successfull!-----
-----END OF SYSTEM-----
```

Took approximately 29 milisecond

9)(1-2-3-4-5 questions answers)

①

HW02

091044011
Ercan UCA

Q1)

1) for(int i=0; i<n-1; i++) \rightarrow n-1 times
for(int j=i+1; j<n; j++) \rightarrow n-i times
3 statement \rightarrow 3 times

$T(1) = ?$ $T(1) = 0$ times
 $T(2) = 3$ times

$$T(n) = (n-1) \cdot (n-1) \cdot 3 = 3n^2 - 6n + 3$$

$$T(n) = \Theta(n^2)$$

$$c_1 n^2 \leq 3n^2 - 6n + 3 \leq c_2 n^2$$

$$c_1 n^2 \leq 3n^2 - 6n + 3$$

$$\begin{array}{l} n=1 \quad 3 \cdot 1 \leq 3 \cdot 1^2 - 6 \cdot 1 + 3 \quad \text{false} \\ n=2 \quad 3 \cdot 2^2 \leq 3 \cdot 2^2 - 6 \cdot 2 + 3 \end{array}$$

false $T(n) \neq \Omega(n^2)$

$$3n^2 - 6n + 3 \leq c_2 n^2 \quad c_2 \geq 3$$

$$\begin{array}{l} n=1 \Rightarrow 3 \cdot 1^2 - 6 \cdot 1 + 3 \leq c_2 \cdot 1^2 \\ n=2 \Rightarrow 3 \cdot 2^2 - 6 \cdot 2 + 3 \leq c_2 \cdot 2^2 \end{array} \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{it is true}$$

Assume it is true $n=k \Rightarrow 3k^2 - 6k + 3 \leq c_2 k^2$
 $n=k+1 \Rightarrow 3(k+1)^2 - 6(k+1) + 3 \leq c_2 (k+1)^2$

$$n=k \Rightarrow 3k^2 - 6k + 3 \leq c_2 k^2 \Rightarrow c_2 k^2 \gg 3k^2 - 6k + 3 \quad \text{true} \checkmark$$

$$n=k+1 \Rightarrow (3k^2 + 6k + 3 - 6k - 6 + 3) \leq c_2 k^2 + 2c_2 k + c_2$$

$$6k + 3 - 6 \leq 2c_2 k + c_2$$

$$6k - 3 \leq 2c_2 k + c_2$$

$$c_2 > 3 \quad \checkmark$$

$$T(n) = \Theta(n^2) \quad \checkmark$$

2

Q1)

```

2) public static int length(String str) {
    if (str == null || str.equals(""))
        return 0;
    return 1 + length(str.substring(1));
}

```

$$T(0) = ? \quad T(0) = 0, \quad T(1) = 1$$

$$T(n) = 1 + T(n-1) \Rightarrow \begin{aligned} T(1) &= 1 + T(0) \\ T(2) &= 1 + T(1) \\ &\vdots \\ T(k) &= k + T(k-1) \end{aligned}$$

$$\begin{aligned} T(k) &= \frac{k(k+1)}{2} \\ &= \frac{k^2 + k}{2} \end{aligned}$$

$$T(n) = \frac{n^2 + n}{2}$$

$$T(n) = \Theta(n^2)$$

$$T(n) = O(n^2)$$

$$c_1 n^2 \leq \frac{n^2 + n}{2} \leq c_2 n^2$$

$$c_1 n^2 \leq \frac{n^2 + n}{2} \quad c_1 \leq 2$$

$$n=1 \quad c_1 \cdot 1 \leq \frac{1^2 + 1}{2} \quad \checkmark$$

$$n=2 \quad c_1 \cdot 4 \leq \frac{2^2 + 2}{2} \quad \checkmark$$

$$n=k \Rightarrow c_1 k^2 \leq \frac{k^2 + k}{2} \quad \text{assume true} \quad \checkmark$$

$$n=k+1 \Rightarrow c_1 (k+1)^2 \leq \frac{(k+1)^2 + (k+1)}{2}$$

$$c_1 k^2 + 2c_1 k + c_1 \leq \frac{k^2 + k}{2} + \frac{k+1}{2}$$

$$2c_1 k + c_1 \leq k+1 \quad \checkmark$$

$c_1 \leq 2$ $\log n$ $\log n$

$$\frac{n^2 + n}{2} \leq c_2 n^2 \quad c_2 > 2$$

$$n=1 \quad \frac{1^2 + 1}{2} \leq c_2 \cdot 1^2 \quad \checkmark$$

$$n=2 \quad \frac{2^2 + 2}{2} \leq c_2 \cdot 2^2 \quad \checkmark$$

$$n=k \quad \frac{k^2 + k}{2} \leq c_2 k^2 \quad \text{assume true}$$

$$n=k+1 \Rightarrow \frac{(k+1)^2 + (k+1)}{2} \leq c_2 (k+1)^2$$

$$\frac{k^2 + k}{2} + \frac{k+1}{2} \leq c_2 k^2 + 2c_2 k + c_2$$

$$k+1 \leq 2c_2 k + c_2 \quad c_2 > 2$$

$\log n$

3

P2)

```

n ← length(A)
for i ← 1 to n-1
  do select ← i
  for j ← i+1 to n
    do if A[j] < A[select]
      then select ← j
  exchange A[i] ↔ A[select]

```

- 1) ilk elemanın indexi tutulurak en küçük eleman seçilir. Sonra arrayin sonuna kadar girilip en küçük indexli seçilir ve en başa atılır. Sonra arrayin $n/2$ 1 sayı azaltılarak sonrakı en küçük seçilip en başa atılır. Selection sort algoritmasıdır yani.

```

2) int i, j, n;
for (i = 0; i < n-1; i++)
{
  int min = i;
  for (j = i+1; j < n; j++)
  {
    if (A[j] < A[min])
      min = j;
  }
  if (min != i)
    swap(A[i], A[min]);
}

```

2n
4

En küçük indexi bulmak için tüm statementların geçmesi gerekir.

$$T(n) = n(2n+5) \Rightarrow 2n^2 + 5n$$

$$c_1 n^2 \leq 2n^2 + 5n \leq c_2 n^2$$

$$\sqrt{c_1} \leq 2$$

$$5 \leq \sqrt{c_2}$$

$$T(n) = \Theta(n^2) \quad \checkmark$$

4

2)

2) devoni

$$\underbrace{c_1 n^2 \leq 2n^2 + 5n}_{\Omega(n^2)} \leq \underbrace{c_2 n^2}_{O(n^2)}$$

$$c_1 \leq 2$$

$$c > 2$$

$$n=1 \Rightarrow c_1 \cdot 1^2 \leq 2 \cdot 1^2 + 5 \cdot 1 \quad \checkmark$$

$$n=2 \Rightarrow c_1 \cdot 2^2 \leq 2 \cdot 2^2 + 5 \cdot 2 \quad \checkmark$$

$$n=k \Rightarrow c_1 k^2 \leq 2k^2 + 5k \quad \text{Assume it's true.}$$

$$n=k+1 \Rightarrow c_1 k^2 + 2ck + c_1 \leq 2k^2 + 2k + 1 + 5k + 5$$

$$(c_1 k^2 + 2ck + c_1) \leq (2k^2 + 4k + 7 + 5k)$$

$$c_1 \leq 2 \quad 2ck + c_1 \leq 4k + 7$$

$$1.2k + 2 \leq 4k + 7$$

$$T(n) = \Omega(n^2) \quad 1.2 \leq 7 \quad \checkmark$$

$$T(n) = \Theta(n^2)$$

$$2n^2 + 5n \leq c_2 n^2$$

$$n=1 \Rightarrow 2 \cdot 1^2 + 5 \cdot 1 \leq c_2 \cdot 1^2$$

$$n=2 \Rightarrow 2 \cdot 2^2 + 5 \cdot 2 \leq c_2 \cdot 2^2$$

$$n=k \Rightarrow 2k^2 + 5k \leq c_1 k^2$$

$$n=k+1 \Rightarrow (2k^2 + 4k + 7 + 5k) \leq c_1 k^2 + 2ck + c_1$$

$$4k + 7 \leq 2ck + c_1$$

$$c_1 > 2 \quad 1.4n$$

$$4k + 7 \leq 6k + 3$$

$$7 \leq 2k + 3 \quad \checkmark$$

$$T(n) = O(n^2) \quad \text{true}$$

5

Q3) $\Theta(g(n))$ has $\Theta(g(n))$ and $\Omega(g(n))$ checker.

$$g(n) = 3n^2 + 2n + 5 \quad \text{given}$$

$$g(n) = \Theta(n^2) ?$$

$$c_1 n^2 \leq 3n^2 + 2n + 5 \leq c_2 n^2$$

$\Omega(n^2)$
best case

$O(n^2)$

worst-case

$$3n^2 + 2n + 5 \leq c_2 n^2$$

$$c_1 n^2 \leq 3n^2 + 2n + 5$$

$$n=1 \Rightarrow c_1 \cdot 1^2 \leq 3 \cdot 1^2 + 2 \cdot 1 + 5, c_1 \leq 3 \text{ true}$$

$$n=2 \Rightarrow c_1 \cdot 2^2 \leq 3 \cdot 2^2 + 2 \cdot 2 + 5, c_1 \leq 3, \text{ true}$$

assume not it's true

$$n=k \Rightarrow c_1 \cdot k^2 \leq 3 \cdot k^2 + 2 \cdot k + 5, c_1 \leq 3 \quad \checkmark$$

$$n=k+1 \Rightarrow c_1 \cdot (k+1)^2 \leq 3(k+1)^2 + 2(k+1) + 5$$

$$\Rightarrow 2c_1 k + c_1 \leq 6k + 5, c_1 \leq 3$$

$$2 \cdot 3 \cdot k + 3 \leq 6k + 5$$

$$3 \leq 5 \quad \checkmark$$

$$\Omega(g(n)) \quad \checkmark$$

$$n=1 \Rightarrow 3 \cdot 1^2 + 2 \cdot 1 + 5 \leq c_2 \cdot 1^2, c_2 \geq 11 \quad \checkmark$$

$$n=2 \Rightarrow 3 \cdot 2^2 + 2 \cdot 2 + 5 \leq c_2 \cdot 2^2, c_2 \geq 3 \quad \checkmark$$

assume it's true

$$n=k \Rightarrow 3 \cdot k^2 + 2 \cdot k + 5 \leq c_2 \cdot k^2, c_2 \geq 3$$

$$n=k+1 \Rightarrow 3(k+1)^2 + 2(k+1) + 5 \leq c_2(k+1)^2$$

$$6k + 5 \leq 2c_2 k + c_2$$

$$6k + 5 \leq 8k + 4$$

$$1 \leq k \quad \checkmark$$

$$O(g(n)) \quad \checkmark$$

$\Theta(g(n))$ proved it.

Q4)

① function InsertionSortRec (array A, int n)

```

1 ← if (n > 1)
  T(n-1) ← InsertionSortRec(A, n-1)
  x ← A[n]
  j ← n-1
  while (j > 0 and A[j] > x)
    2n-2 { A[j+1] ← A[j]
          j ← j-1
          }
  1 ← A[j+1] = x
end if

```

end function

②

$$T(n) = T(n-1) + 2n$$

$$T(1) = T(0) + 2 \cdot 1$$

$$T(2) = T(1) + 2 \cdot 2$$

$$T(3) = T(2) + 2 \cdot 3$$

$$+ T(k) = T(k-1) + 2 \cdot k$$

$$T(k) = T(0) + 2 \cdot \frac{k \cdot (k+1)}{2}$$

$$T(k) = \frac{k^2 + k}{2}$$

$$T(n) = n^2 + n$$

$T(n) = O(n^2)$ worst case

$$n^2 + n \leq c \cdot n^2 \quad c > 1$$

$$n=1 \Rightarrow 1+1 \leq c \cdot 1^2 \quad \checkmark$$

$$n=2 \Rightarrow 2^2+2 \leq c \cdot 2^2 \quad \checkmark$$

$$n=k \Rightarrow k^2+k \leq c \cdot k^2 \quad \text{assume } c > 1$$

$$n=k+1 \Rightarrow (k+1)^2 + (k+1) \leq c \cdot (k+1)^2$$

$$\Rightarrow 2k+1 \leq 2ck+c$$

$$c=2$$

$$2k+1 \leq 4k+2$$

$$-1 \leq 2k \quad \text{true}$$

$$T(n) = O(n^2)$$

$n=k$ then

less steps
again

worst case

$O(n^2)$ or. hypothesis is true.

③

3, 4, 1, 2 \Rightarrow 3, 4

3, 4, 1, 2 \Rightarrow 4, 1

3, 1, 4, 2 \Rightarrow 4, 2

3, 1, 2, 4 \Rightarrow 3, 1

1, 3, 2, 4 \Rightarrow 3, 2

1, 2, 3, 4 \Rightarrow 1, 2

1, 1, 2, 3, 4 \Rightarrow 1

1, 2, 3, 4

7

Q2)

$f(n) = O(g(n))$, $f(n) = \Omega(g(n))$ or $f(n) = \Theta(g(n))$

① $f(n) = n^{0.1}$, $g(n) = (\log n)^{10}$
 Θ notation

$$c_1 (\log n)^{10} \leq n^{0.1} \leq c_2 (\log n)^{10}$$

$$\log (c_1 (\log n)^{10}) \leq \log (n^{0.1})$$

$$\log (n^{0.1}) \leq \log (c_2 (\log n)^{10})$$

$$\log c_1 + 10 \log (\log n) \leq \frac{\log n}{10}$$

$$\frac{\log n}{10} \leq \log c_2 + 10 \log (\log n)$$

$$n=2 \Rightarrow \log c_1 \leq 0.1, c_1 \leq 2 \quad \times$$

$$\frac{\log n}{10} \leq \log c_2 + 10 \log (\log n) \quad c_2 \geq 2$$

$$n=4 \Rightarrow \log c_1 + 10 \leq 0.2, c_1 \leq 2 \quad \times$$

$$n=2 \Rightarrow 0.1 \leq \log c_2 \quad \checkmark$$

$$n=4 \Rightarrow 0.2 \leq \log c_2 + 10 \quad \checkmark$$

$$f(n) \neq \Omega(g(n))$$

$$\text{true} \Rightarrow n=k \Rightarrow \frac{\log k}{10} \leq \log c_2 + 10 \log (\log k)$$

$$n=k+1 \Rightarrow \frac{\log (k+1)}{10} \leq \log c_2 + 10 \log (\log (k+1))$$

$$\frac{\log k}{10} + \frac{\log 1}{10} \leq \log c_2 + 10 \log (\log k + \frac{\log 1}{10})$$

$$0 \leq \log c_2 \quad \text{its true} \quad \underline{f(n) = O(g(n))} \quad \checkmark$$

$$c_2 \geq 2 \quad \checkmark$$

② $f(n) = n!$, $g(n) = 2^n$

$$c_1 2^n \leq n! \leq c_2 2^n$$

$$c_1 \leq 1$$

$$n=1 \quad c_1 \cdot 2^1 \leq 1! \quad \text{false}$$

$$n=2 \quad c_1 \cdot 2^2 \leq 2! \quad \text{false}$$

$$f(n) \neq \Omega(g(n))$$

$$n! \leq c_2 2^n$$

$$n=1 \quad 1! \leq c_2 \cdot 2^1, \quad c_2 \geq 1 \quad \checkmark$$

$$n=2 \quad 2! \leq c_2 \cdot 2^2, \quad c_2 \geq 1 \quad \checkmark$$

$$n=k \Rightarrow k! \leq c_2 \cdot 2^k \quad \text{assume true}$$

$$n=k+1 \Rightarrow (k+1)k! \leq c_1 \cdot 2 \cdot 2^k$$

$$k+1 \leq 2 c_2$$

$$c_2 \geq 1, \quad n \geq 10 \quad \checkmark$$

$$\underline{f(n) = O(g(n))} \quad \checkmark$$

[8]

Q5)

[3]

$$f(n) = (\log n)^{\log n}, g(n) = 2^{(\log_2 n)^2}$$

$$g(n) = 2^{\log_2 n \cdot \log_2 n} = \underbrace{2^{\log_2 n}}_n \cdot \underbrace{2^{\log_2 n}}_n$$

$$g(n) = n^2$$

$$\Rightarrow c_1 n^2 \leq (\log n)^{\log n} \leq c_2 n^2$$

$$\log c_1 + 2 \log n \leq \log n (\log(\log n)) \quad c_1 \neq 2$$

$$n=2 \Rightarrow \log c_1 + 2 \leq 0 \quad \times$$

$$n=4 \Rightarrow \log c_1 + 4 \leq 0 \quad \times$$

$$f(n) \neq \Omega(g(n))$$

$$\log(\log(\log n)) \leq \log c_2 + 2 \log n \quad c_2 \geq 2$$

$$n=2 \Rightarrow 0 \leq \log c_2 + 2$$

$$n=4 \Rightarrow 0 \leq \log c_2 + 4$$

Assume true

$$n=k \Rightarrow \log k (\log(\log k)) \leq \log c_2 + 2 \log k$$

$$n=k+1 \Rightarrow \log k (\log(\log k)) \leq \log c_2 + 2 \log k$$

$$\log 1 = 0 \quad \checkmark$$

$$0 \leq \log c_2 \quad \text{true}$$

$$f(n) = O(g(n))$$

8) Github Link

Hw02 link: https://github.com/erccanuca/cse222_hw02_2017