

Python [solutions]

Python and R for Data Science

Data Science and Management



Exercise 1: find how many equal numbers

Define a function `count_equals` that:

- takes as arguments four numbers
- returns:
 - the maximum number of equal numbers between the four

Example:

- `count_equals(1,2,3,4)` should return `0`
- `count_equals(1,2,5,4)` should return `0`
- `count_equals(1,2,2,2)` should return `3` because there are three `2` in the sequence
- `count_equals(1,1,1,2)` should return `3` because there are three `1` in the sequence

In [6]: *# Solution goes here*

Test your code

Run this code to test your solution:

```
In [7]: try: assert count_equals(1,2,3,4) == 0 and count_equals(1,5,3,4) == 0 and count_e  
except: print('Test failed')
```

Test failed

Solution

```
In [2]: def count_equals(a, b, c, d):  
        numbers = [a, b, c, d]  
        max_count = 0  
  
        for num in numbers:  
            count = 0  
            for other in numbers:  
                if num == other:  
                    count += 1  
            if count > max_count:  
                max_count = count  
  
        return max_count if max_count > 1 else 0  
  
        # test  
        assert count_equals(1,2,3,4) == 0 and count_equals(1,5,3,4) == 0 and count_equals
```

Test passed

Exercise 2: Fibonacci's sequence

Define a function `fibonacci` that:

- takes as arguments:
 - an integer number `n`
- returns:
 - a list containing the first `n` numbers of the Fibonacci's sequence

Note: The Fibonacci sequence is a series of numbers where each number is the sum of the two previous ones, starting with 0 and 1. To calculate it, you begin with 0 and 1, then add these to get the next number. Continue this process to generate the sequence. It goes 0, 1, 1, 2, 3, 5, 8, and so on.

In [6]: *# Solution goes here*

Test your code

Run this code to test your solution:

```
In [7]: try: assert fibonacci(1) == [0] and fibonacci(3) == [0,1,1] and fibonacci(7) == [
except: print('Test failed')
```

Test failed

Solution

```
In [13]: def fibonacci(n):  
         fib_sequence = [0, 1]  
  
         if n == 1:  
             return [0]  
  
         for i in range(2, n):  
             next_fib = fib_sequence[-1] + fib_sequence[-2]  
             fib_sequence.append(next_fib)  
  
         return fib_sequence[:n]  
  
         # test  
         assert fibonacci(1) == [0] and fibonacci(3) == [0,1,1] and fibonacci(7) == [0, 1,
```

Test passed

Exercise 3: zero-sum triplets

Define a function `zero_sum_triplets` that:

- takes as arguments:
 - a list of integers `numbers`
- returns:
 - the number of triplets whose sum is zero

Example:

- `zero_sum_triplets([1,-1,0,7,12])` should return `1` because the sum of 1,-1,0 is `0`
- `zero_sum_triplets([1,9,0,7,12])` should return `0` because there are no triplets that sum up to zero
- `zero_sum_triplets([1,-9,8,6,-14])` should return `2` because the sum of 1,-1,0 is `0` and the sum of 8,6,-14 is `0`

In [8]: `# Solution goes here`

Test your code

Run this code to test your solution:

```
In [9]: try: assert zero_sum_triplets([1,-1,0,7,12]) == 1 and zero_sum_triplets([1,9,0,7,  
except: print('Test failed')
```

Test passed

Solution

```
In [10]: def zero_sum_triplets(numbers):  
          n = len(numbers)  
          count = 0  
  
          for i in range(n - 2):  
              for j in range(i + 1, n - 1):  
                  for k in range(j + 1, n):  
                      if numbers[i] + numbers[j] + numbers[k] == 0:  
                          count += 1  
  
          return count  
  
          # test  
          assert zero_sum_triplets([1,-1,0,7,12]) == 1 and zero_sum_triplets([1,9,0,7,12])
```

Test passed

Exercise 4: Collatz

Define a function `collatz` that:

- takes as argument an integer number `n`
- returns:
 - a list containing all the numbers generated by the Collatz conjecture (stopping when reaching `1`)

Note: The Collatz Conjecture is a mathematical problem that starts with any positive integer. The process involves two steps: if the number is even, divide it by 2; if it's odd, multiply it by 3 and add 1. Repeat this process with the resulting number. The conjecture suggests that, no matter what number you start with, you'll eventually reach the number 1.

In [12]: *# Solution goes here*

Test your code

Run this code to test your solution:

```
In [13]: try: assert collatz(12) == [6,3,10,5,16,8,4,2,1] and collatz(1) == [] and collatz  
except: print('Test failed')
```

Test failed

Solution

```
In [12]: def collatz(n):  
         sequence = []  
  
         while n != 1:  
             if n % 2 == 0:  
                 n = n // 2  
             else:  
                 n = 3 * n + 1  
             sequence.append(n)  
  
         return sequence  
  
         # test  
         assert collatz(12) == [6,3,10,5,16,8,4,2,1] and collatz(1) == [] and collatz(2) ==
```

Test passed

Exercise 5: Greatest Common Divisor (GCD)

Define a function `gcd` that:

- takes as argument two integer numbers `a` and `b`
- returns:
 - the gcd between `a` and `b`

In [15]: *# Solution goes here*

Test your code

Run this code to test your solution:

```
In [16]: try: assert gcd(1,2) == 1 and gcd(7,2) == 1 and gcd(4,2) == 2 and gcd(15,25) == 5  
except: print('Test failed')
```

Test failed

Solution

```
In [18]: def gcd(x, y):
          while y != 0:
              (x, y) = (y, x % y)
          return x

          # test
          assert gcd(1,2) == 1 and gcd(7,2) == 1 and gcd(4,2) == 2 and gcd(15,25) == 5 and
```

Test passed

Exercise 6: Factorial of a number

Define a function `factorial` that:

- takes as argument two integer numbers `a`
- returns:
 - the factorial of `a` (i.e., $n! = n * (n-1) * (n-2) * \dots * 1$)

```
In [ ]: # Solution goes here
```

Test your code

Run this code to test your solution:


```
In [ ]: try: assert factorial(1) == 1 and factorial(0) == 1 and factorial(5) == 120 and n
except: print('Test failed')
```

Test failed

Solution

```
In [9]: def factorial(x):
        result = 1
        for i in range(0,x):
            result *= x-i
        return result

# test
assert factorial(1) == 1 and factorial(0) == 1 and factorial(5) == 120 and not pr
```

120

Test passed

Exercise 7: Count vowels in a string

Define a function `vowels_counter` that:

- takes as argument a string `a`
- returns:
 - a dictionary with as key each vowel and as values the occurrences of each vowel

```
In [ ]: # Solution goes here
```

Test your code

Run this code to test your solution:

```
In [ ]: try: assert vowels_counter("ciao") == {'i': 1, 'a': 1, 'o': 1} and vowels_counter
except: print('Test failed')
```

Test failed

Solution

```
In [13]: def vowels_counter(x):
          result = {}
          vowels = ["a", "e", "i", "o", "u"]
          for i in x:
              if i in vowels:
                  if i in result:
                      result[i] = result[i]+1
                  else:
                      result[i] = 1
          return result

          # test
          assert vowels_counter("ciao") == {'i': 1, 'a': 1, 'o': 1} and vowels_counter("abb
```

{'a': 2, 'e': 2, 'i': 1, 'o': 1}

Test passed

Exercise 8: Find missing number in a sequence

Define a function `find_missing` that:

- Takes a list of `n-1` integers, which represents a sequence of numbers from 1 to `n`, but one number is missing.
- Returns the missing number.

Note: Suppose that there is always only one number missing

Example:

- `find_missing([1, 2, 4, 5])` should return `3`.
- `find_missing([2, 3, 4, 6, 1])` should return `5`.

```
In [ ]: # Solution goes here
```

Test your code

Run this code to test your solution:

```
In [ ]: try: assert find_missing([1, 2, 4, 5]) == 3 and find_missing([2, 3, 4, 6, 1]) == 5
except: print('Test failed')
```

Test failed

Solution

```
In [17]: def find_missing(nums):  
          n = len(nums) + 1  
          total_sum = n * (n + 1) // 2  
          actual_sum = sum(nums)  
  
          return total_sum - actual_sum  
  
# test  
assert find_missing([1, 2, 4, 5]) == 3 and find_missing([2, 3, 4, 6, 1]) == 5 and
```

Test passed

Exercise 9: Longest Substring Without Repeating Characters

Define a function `longest_unique_substring` that:

- Takes a string as input.
- Returns the length of the longest substring that contains only unique characters.

Example:

- `longest_unique_substring("abcabcbb")` should return `3` (substring "abc").
- `longest_unique_substring("bbbbbb")` should return `1`.

```
In [ ]: # Solution goes here
```

Test your code

Run this code to test your solution:

```
In [ ]: try: assert longest_unique_substring("abcabcbb") == 3 and longest_unique_substring("bb") == 2
except: print('Test failed')
```

Test failed

Solution

```
In [16]: def longest_unique_substring(s):
max_length = 0

for i in range(len(s)):
    seen_chars = set()

    for j in range(i, len(s)):
        if s[j] in seen_chars:
            break
        seen_chars.add(s[j])

    max_length = max(max_length, j - i)

    return max_length

# test
assert longest_unique_substring("abcabcbb") == 3 and longest_unique_substring("bb") == 2
```

Test passed

Exercise 10: Find the Majority Element

Define a function `majority_element` that:

- Takes a list of integers as input.
- Returns the element that appears more than half of the time in the list (if it exists). If no such element exists, return `None`.

Example:

- `majority_element([3, 3, 4, 2, 3, 3, 5])` should return `3`.
- `majority_element([1, 2, 3, 4, 5])` should return `None`.

```
In [ ]: # Solution goes here
```

Test your code

Run this code to test your solution:

```
In [ ]: try: assert majority_element([3, 3, 4, 2, 3, 3, 5]) == 3 and majority_element([1,
except: print('Test failed')
```

Test failed

Solution

```
In [14]: def majority_element(nums):
          count = {}
          n = len(nums)

          for num in nums:
              if num in count:
```

```
        count[num] = count[num] + 1
    else:
        count[num] = 1

    if count[num] > n // 2:
        return num

    return None

# test
assert majority_element([3, 3, 4, 2, 3, 3, 5]) == 3 and majority_element([1, 2, 3
```

Test passed

