

/\* Set the times \*/

TL0 = 0x18;

TH0 = 0x80;

TR0 = 1 // Start Timer0

while (TF == 0); // Wait for flag

TR0 = 0; // Stop timer0

}

$$\left\{ \begin{array}{l} 0190 - 1000 = 7143 \\ 11100000 \quad 011000 \\ \text{oxf0} \qquad \quad \text{0x18} \end{array} \right\}$$

TL0 = 0x18

TH0 = 0xF0;

TR0 = 0

TF0 = 0

$$65536 - 1000 = 64536$$

TH0 = 0xF0

TL0 = 0x18

Half-House control of Timer -

#include  $\overline{\text{P1.7}}$  TR0 = 1  $\overline{\text{P1.6}}$  TR0 = 1 / 0

Void main()

{

TMOD = 0x09

TR0 = 1;

while (1)

{ if (TF == 1)

TF = 0;

}

To get baud rate

$$TH_1 = TL_1 = 253$$

$$TR_1 = 1;$$

① Tx char 'A' serially through UART to Hyperterminal

#

void uart\_init(void);

void uart\_Tx(unsigned char);

void main()

{

uart\_init();

uart\_Tx('A');

while(1);

}

void uart\_init(void)

{

SCON = 0x40;

TMOD = 0x20;

TH1 = TL1 = 253;

TR1 = 1;

}

void uart\_tx(unsigned char d)

{

SBUF = d;

while(TI == 0);

TI = 0;

}

Q Rx & Rx generally

① Define the fun to transmit  
the string.  
integers, float

1  
#  
Void west-init(void);  
Void west-Tx (unsigned char);  
unique class west-Rx (void);  
Void main()  
{

void west-Rx (unsigned char\*)

{

while (\*P)

Elwest-Tx (\*P++);

}

unsigned char X;

west init();

while (1)

{

X = west-Rx();

west-Tx(X);

}

Void west\_init(void)

{

SCON = 0X50;

TMOD = 0X20;

TH1 = TL1 = 255;

TR1 = 1;

{

Void west-Tx (unsigned char)

2. ~~sent~~ SBUF = j

while (TI == 0)

TI = 0;

}

unique  
Void user west-Rx (void)

{

while (RI == 0)

RI = 0;

return SBUF; }.



Q : WAPL to demonstrate : Ex Int 0 in low level triggering  
to demo. Ex 0 & 100# in falling Edge triggering

LEDO Bit P1.0

CSB4 AT 0

LJMP MARN

// Ex-Int 0 - RX

CSF4 AT 0003H

CLR LEDO

SETB LEDO

RETI

// main line prog.

CSB4 AT 100H

MAIN : \$

SRTD RA // Global Int Enable bit

SRTB EX0 // Enable Ex-Int 0

CLR ITO // Low-level Trig.

Repeat :

INC RO

STMP: Repeat

END

LEDO Bit P1.0

WBD BRT P1.0

CSB4 AT 0

LJMP MARN

CSF4 AT 0003H

CLR LEO0

SRTD - LEDO

RETI

CSB4 AT 0013H

CLR LEO1

SRTB LEO1

RETI

// Main-line prog.

MARN :

SRTD RA

SRTD EX0

SRTD RX1

SRTD ITO

SRTD RTO

ECP to EXI-0 in(LT)

```
#include <reg51.h>
```

```
Sbit led = P1^0;
```

```
Void ext_int0_isr (void) interrupt 0
```

{

```
led = 0;
```

```
ILO = 1;
```

}

```
Void main()
```

{

```
int c = 0
```

```
EA = 0;
```

```
EX0 = 1;
```

```
IT ERO = 0;
```

```
while (1)
```

```
{  
    (c++);
```

}

(ID \* 8) + 3

EPPs to demonstrate two Ex-0s

i.e. EX0 & EX1 in falling edge

```
#include <reg51.h>
```

```
Sbit Led1 = P1^0;
```

```
Sbit Led2 = P1^0;
```

```
Void ext_int0_isr (void) interrupt 0
```

{

```
Led1 = 0
```

↑

↓

↓

```
IT0 = 1
```

```
IT0 = 1
```

Ex: Tx a char serially through UART using interrupt  
② EEP to receive & re-transmit the same char using interrupt method.

```
#include <reg51.h>
```

```
void serial_isr(void) interrupt 4
```

```
{
```

```
if (TI == 1)
```

```
TI = 0;
```

```
}
```

```
void main()
```

```
int cnt = 0;
```

```
SCON = 0x40;
```

```
TMOD = 0x20
```

```
TH1 = TL1 = 253
```

```
TR1 = 1;
```

```
(* Enable serial interrupt*)
```

```
EA = 1
```

```
ES = 1;
```

```
(* Initiate the Tx *)
```

~~EA = 1;~~~~ES = 1;~~

```
(* Initiate the transmission *)
```

```
SBUF = 'A';
```

```
while (1)
```

```
{
```

```
Cnt ++;
```

```
}
```

```
.
```

```
#include <reg51.h>
```

```
unsigned char x
```

```
void serial_isr(void)
```

```
interrupt 4
```

```
{
```

```
if (TI == 1)
```

```
TI = 0,
```

```
else
```

```
RI = 0;
```

```
x = SBUF; // read the Rx byte
```

```
SBUF = x; // Initialize the Tx
```

```
3
```

```
3
```

```
void main()
```

```
{
```

```
int cnt = 0;
```

```
(* initialize the port *)
```

```
SCON = 0x50;
```

```
TMOD = 0x20;
```

```
TM1 = TL1 = 253
```

```
TR1 = 1;
```

```
(* enable serial int. *)
```

```
EA = 1;
```

~~ES = 1;~~

```
while (1)
```

```
{ Cnt ++;
```

```
3
```

write 'A' into EEPROM (AT24C08) read back the same data & display it on alphanumeric LCD.

```
#include "testing-i2c.h"
```

```
extern void Led-init(void);
```

```
extern void lcd-cmd(unsigned char);
```

```
extern void Led-state (unsigned char);
```

```
extern void string (unsigned char*);
```

```
Void main ()
```

```
{
```

```
Led-init();
```

```
string ("I2C-test!");
```

```
delay (ms(500));
```

```
i2c-slave-write (0xA0, 0x00, 'A');
```

```
Led-state (i2c-slave-read (0xA0, 0x00));
```

```
while (1);
```

```
};
```

```

#include <reg51.h>
#include <inttypes.h>

Sbit SCL = P3^2;
Sbit SDA = P3^3;
extern void delay_ms(int);

void i2c_start(void)
{
    SCL = 1;
    SDA = 1;
    SDA = 0;
}

void i2c_stop(void)
{
    SDA = 0;
    SCL = 1;
    SDA = 1;
}

void i2c_bytewrite(uint8_t)
{
    unsigned char j;
    for (j=0; j<8; j++)
    {
        SCL = 0;
        SDA = df(0x80>>j)?1:0;
        SCL = 1;
    }
}

unsigned char i2c_bytoread(void)
{
    unsigned char j, buf=0;
    for (j=0; j<8; j++)
    {
        SCL = 0;
        -nop-();
        SCL = 1;
    }
}

if (SDA)
    buf |= (0x80 >> j);
return buf;
}
}

void i2c_ACK(void)
{
    SCL = 0;
    SDA = 1;
    SCL = 1; // write SDA=0
    SCL = 0;
}

void i2c_NOACK(void)
{
    SCL = 0;
    SDA = 1;
    SCL = 1;
    SCL = 0;
}

```

```
void i2c_slave_write (unsigned char sa,  
                      unsigned char r-add,  
                      unsigned char dat)  
{  
    i2c_start();  
    i2c_bytewrite(sa);  
    i2c_ACK();  
    i2c_bytewrite(r-add);  
    i2c_ACK();  
    i2c_bytewrite(dat);  
    i2c_ACK();  
    i2c_stop();  
    delay_1ms(10);  
}
```

Var ~~var~~

```
unsigned char i2c_slave_read (unsigned char sa,  
                             unsigned char r-add)
```

```
{  
    unsigned char buff;  
    i2c_start();  
    i2c_bytewrite(sa);  
    i2c_ACK();  
    i2c_bytewrite(r-add);  
    i2c_ACK();  
    i2c_start();  
    i2c_bytereadwrite(sa|1);  
    i2c_ACK();  
    buff = i2c_byteread();  
    i2c_noack();  
    i2c_stop();  
    return buff;  
}
```

# LED

Ques No.  
Page No.

① delay of 1 ms.

```
delay 1ms (void);  
Void main ()  
{  
    delay 1-ms();  
    while ();  
}  
Void delay -1ms (void)  
{  
    unsigned char i;  
    for (i = 250; i > 0; i--);  
    for (i = 247; i > 0; i--);  
}
```

② delay 1-ms (unsigned int);

Void main()

{

```
delay -1ms (1000);  
while (1);  
}
```

Void delay -1ms (unsigned int tly)

{

unsigned char i;

```
for (tly; tly > 0; tly--)
```

```
for (i = 250; i > 0; i--);
```

```
for (i = ; i > 0; i--);
```

}

VOCES

Term By Value

Aug.

Mixture

Relationship

?

P & LOR

- ✓ Time & work
- ✓ Pipes & Cistern
- ✓ Simple Interest
- ✓ Compound Interest
- ✓ Time & Distance
- ✓ Boats & Streams
- ✓ Problem on trains

ratio & proportion

No. 24:-

DIA-ORG

### Calculation Tricks.

① No. which end with 5

squaring

$$(25)^2 \rightarrow 625$$

$\downarrow$

3

$$(35)^2 \rightarrow 1225$$

$$\begin{array}{r} 4 \\ | \\ (95)^2 \end{array} \rightarrow (9025)$$

→ Neighbours of 100.

$$\begin{array}{r} 9 \\ | \\ (102)^2 \end{array} \rightarrow \underline{104} \underline{04}$$

$$\begin{array}{r} 4 \\ | \\ 104 \end{array} \rightarrow \underline{108} \underline{16}$$

$$\begin{array}{r} -2 \\ | \\ (98)^2 \end{array} \rightarrow \underline{96} \underline{04}$$

$$\begin{array}{r} -4 \\ | \\ (96)^2 \end{array} \rightarrow \underline{92} \underline{16}$$

→ Neighbours of 50

(Base 50)

$$\begin{array}{r} 9 \\ | \\ (52)^2 \end{array} \rightarrow \underline{27} \underline{04}$$

$$\begin{array}{r} 4 \\ | \\ 54 \end{array} \rightarrow \underline{29} \underline{16}$$

$$\begin{array}{r} -3 \\ | \\ (47)^2 \end{array} \rightarrow (2209)$$

## Multiplication

→ 2 digit No. → Base 10       $12 \times 13 \rightarrow 15 \frac{6}{2 \times 3}$

Base 100 →  $99 \times 98 \rightarrow (97 \underline{02})$   
 $\begin{array}{r} -1 \\ -2 \end{array}$

Base 100       $95 \times 96 \rightarrow 9120$   
 $\begin{array}{r} -5 \\ -4 \end{array}$

Base 100       $67 \times 98 = 65 \underline{66}$   
 $\begin{array}{r} -33 \\ -2 \end{array}$

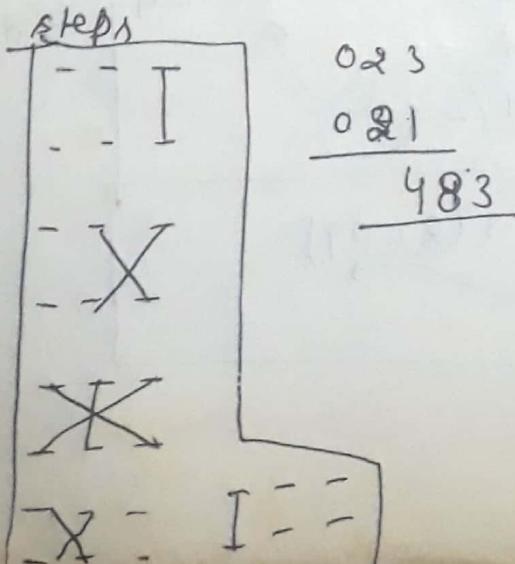
Base 50       $54 \times 49 \rightarrow 53 (-4)$   
 $(10 \times 5 = 50)$        $+4 \quad -1$   
 $\begin{array}{r} \times 5 \\ \hline 2650 \\ -4 \\ \hline 2646 \end{array}$

base 20       $23 \times 21 \rightarrow 24 (+3)$   
 $(10 \times 2 = 20)$        $+3 \quad +1$   
 $\begin{array}{r} \times 2 \\ \hline 48 (+3) \Rightarrow 483 \end{array} \approx$

→ 3 digit No.

Ex 123

$$\begin{array}{r} 321 \\ \times 123 \\ \hline 39483 \end{array}$$



...| :x | \* | x | ...

306

024

$$\begin{array}{r} \\ \hline 71344 \end{array}$$

$$0.59 \times 0.58$$

$$\begin{array}{r} 0.59 & 40 \\ 0.58 & 45 \\ \hline 3492 \end{array}$$

For multiplication of 4 No.  $\rightarrow$  7 steps.

$$\begin{array}{r} \dots | \dots :x | \cdot * | * | * : | x | \dots \\ \dots | \dots :x | \cdot * | * | * : | x | \dots \\ \hline \text{For 3 Variable} \rightarrow 5 \text{ steps} \end{array}$$

$$\begin{array}{r} \dots | \dots :x | \cdot * | x : | \dots \end{array}$$

## H.C.F & L.C.M of No.

- ①  $\frac{6}{a}$  exactly,  $a$  is factor of 6.  
 $6$  is multiple of  $a$ .
- ② Product of two No. = product of their H.C.F & L.C.M.
- ③ Co-prime  $\rightarrow$  two No. are said to be co-prime if their H.C.F is 1.
- ④  $H.C.F = \left( \frac{\text{H.C.F of Numerator}}{\text{L.C.M of Denominators}} \right)$
- $L.C.M = \left( \frac{\text{L.C.M of Numerator}}{\text{H.C.F of Denominators}} \right)$

$\rightarrow$  for  $n$ -Rational No.  $b/a$   $a \neq b$

$$a \left( \frac{n+1}{n+1} \right) : b \left( \frac{n+1}{n+1} \right)$$

Ex find 4 Rational No.  $b/a$   $3 \neq 4$ .

$$4+1 = 5$$

$$3 \times \frac{5}{5} = \frac{15}{5} \quad 4 \times \frac{5}{5} = \left( \frac{20}{5} \right)$$

(1)  $\frac{15}{5}, \frac{16}{5}, \frac{17}{5}, \frac{18}{5}, \frac{19}{5}, \frac{20}{5}$

$\rightarrow$  Rational No.  $b/a$ .  $3 \neq 4 \rightarrow \frac{3+4}{2} = \left( \frac{7}{2} \right)$

$\rightarrow$  How to convert Recurring Decimal into fraction

Ex  $0.\overline{6}$

Let  $x = 0.\overline{6} \quad \textcircled{1}$

Multiply both side by 10

$$\begin{aligned} 10x &= 6.\overline{6} \quad \textcircled{2} \\ \text{Sub. } \textcircled{1} &\text{ from } \textcircled{2} \\ 9x &= 6 \end{aligned}$$

$$x = \frac{6}{9} = \left( \frac{2}{3} \right)$$

## Ratio & proportion & mixture

$$\begin{array}{c} A \\ \backslash \\ B \\ / \\ C \end{array} \Rightarrow A : B : C$$

$a = a+b$   
 $B = B$   
 $C = B+c$

$$\begin{array}{l} A:B = 11:2 \\ B:C = 3:4 \\ C:D = 6:8 \\ D:E = 12:16 \end{array}$$

$$\begin{aligned}
a:b:c:d &\text{ is } ? \\
a = 1 \times 3 \times 6 \times 12 &= \\
E = 2 \times 4 \times 9 \times 16 & \\
B = 3 \times 6 \times 12 \times 2 & \\
D = 6 \times 12 \times 2 \times 4 & \\
D = 12 \times 2 \times 4 \times 9 &
\end{aligned}$$

Note  $\frac{A}{B} = \frac{B}{C}$  &  $A, B, C$  are in same ratio  
 $D:C$  then  $\frac{a}{b} \times \frac{B}{C} \times \frac{C}{D} \times \frac{D}{A} = 1$

## Proportion

Let  $a, b, c, d$

### Normal proportion

$$a:b :: c:d$$

Extremes  
or  
 $\frac{a}{b} = \frac{c}{d}$

### ① Continue proportion

$$\frac{a}{b} = \frac{b}{c} = \frac{c}{d}$$

$$\text{Component & Divitento Law } \frac{a}{b} = \frac{c}{d} \Rightarrow \left( \frac{a+b}{a-b} \right) = \left( \frac{c+d}{c-d} \right)$$

$$\frac{a}{b} = \frac{c}{d} \Rightarrow \frac{a+b}{b} = \frac{c+d}{d}$$

$$\frac{a}{b} = \frac{c}{d} \Rightarrow \frac{a-b}{b} = \frac{c-d}{d}$$

Q: Least No. that must be subtracted from 4, 5, 7 so that two No. must be in Continue Prop.

$$(4-x)(5-x) 17 - 29$$

$$\frac{4-x}{5-x} = \frac{5-x}{7-x}$$

$$x=3$$

Q:  $x = \frac{abc}{a+b}$  value of  $\frac{x+2a}{x-a} + \frac{x+2b}{x-b}$  is

$$\frac{x}{2a} = \frac{ab}{a+b}$$

## Variation

### Direct

$$P \propto Q$$

$$P = kQ \quad (k \text{ constant}) \quad P \propto \frac{1}{Q}$$

### Indirect

$$P \propto \frac{1}{Q}$$

$$P \propto m \Rightarrow P \propto \frac{1}{m}$$

$$P \propto Q \text{ and } P \propto \frac{1}{m} \Rightarrow P \propto \frac{Q}{m}$$

$$P \propto \frac{1}{Q} \text{ and } P \propto \frac{1}{m} \Rightarrow P \propto \frac{1}{Qm}$$

$$\text{No. of coins} = \frac{\text{Total value}}{\text{Denomination}}$$

Ex - Q of Rs 10 paise coins.

$$\Rightarrow \frac{2}{y_n} = 8 \text{ coins}$$

1 d 10,000  
100

Q A bag contain Rs 90 in coins of denomination of 50 paise, 25 paise & 10 paise. If coins of 50 paise, 25 paise & 10 paise are in the ratio of 2:3:5, then no. of 25 paise coins in bag.

$$\text{No. of coins} \times \text{denomination} = \text{total value}$$

$$\begin{aligned} 50 &= \frac{1}{2}x + 2y + z \\ 25 &= \frac{1}{4}x + 3y + z \\ 10 &= \frac{1}{4}x + 5y + z \end{aligned}$$

$$25 \text{ paise coins} = 120$$

6000

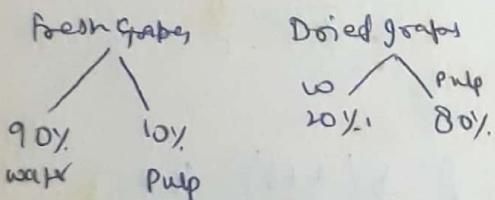
$$\frac{4000 \times 10}{100}$$

1993 →

UP	2
Bihar	2
AS	0
K	1
M	1
T.H	1
K	1

### Mixture

Fresh grapes contain 90% of water by weight while dried grapes contain 20% water by weight. What is the weight of 8 kg grapes available from 20 kg of fresh grapes.

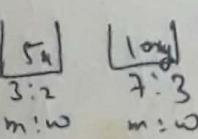


$$\frac{20 \times 16}{100} = 20 \text{ kg fresh grapes}$$

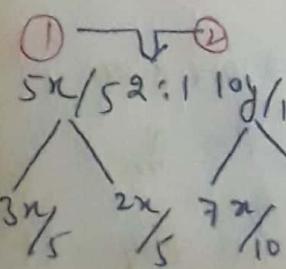
$$\downarrow$$

$$\left( x - \frac{8x}{100} \right) \text{ kg Dry grapes.}$$

$$x = 2.5 \text{ kg}$$

 find ratio in which the content of two vessels have to be mixed to get new mixture in given ratio.

m:w in 2:1

①  5x/5:2:1 10y/10

$$\frac{6x+7y}{4x+3y} = \frac{2}{1}$$

$$\frac{\text{milk}}{\text{water}} : \frac{2}{1} = \frac{3x+7y}{2x+3y} : \frac{2x+3y}{10} \quad \frac{2x+3y}{10} = \frac{1}{2} \quad \frac{2x+3y}{10} = 1 : 2$$

6

(7)

$$\frac{10}{100} \times 10,000$$

$$\frac{5 \times 80000}{100} =$$

6000

$$\frac{4000}{100} \times 100$$

$$\frac{4000 \times 10000}{100}$$

D.T

1993 → 25 Lack.

Q

287.25 L

UP	20	M:F
Bihar	21	4:3
AD	0	3:2
K	13	4:3
M	10 Y.	4:5
T.H	11 Y.	4:5
K	8 Y.	3:4
		5:6

$$\frac{\frac{4}{7}(28)}{100} + \frac{4}{9}(10) + \frac{5}{11}(8)$$

$$16 + \frac{40}{9} + \frac{40}{11}$$

$$\frac{\frac{3}{7}(9)}{100} +$$

$$\frac{4}{7}(11) 2.4$$

$$\frac{3 \times \frac{27}{95} \times \frac{25}{100}}{4 \times 11}$$

$$6 \times 5 = 30 \text{ Y.} \quad \frac{20 \text{ Y.}}{20} \rightarrow 50$$

$$45 \times 5 = 35 \times 4$$

$$(7)(38 + 3) \quad 28(7) + 21(5) \quad 50 \quad 11 \times 25 \text{ Lack}$$

$$\frac{38 \times 7}{35 \times 5}$$

$$\frac{4}{7} \times 11 \times$$

$$7. N = \underline{11 \times 25 \text{ Lack}}$$

$$\frac{9}{100} \times 8 + \frac{7}{20} \times 4$$

$$\frac{6}{51} \times 8$$

$$\frac{4}{7}(30) + 11 \times 250000$$

$$\left(\frac{9}{4} + \frac{7}{5}\right) \frac{45 + 28}{20} 4.$$

$$\frac{2}{6 \times 7 \times 8} \times$$

$$25 \times \frac{3}{7} 11 \times 250000$$

$$\left(\frac{73}{28} \times 9\right) \frac{8.1}{9} \frac{73}{121}$$

1. → fraction.

$$\frac{1}{2} \rightarrow 50\%$$

$$\frac{1}{3} \rightarrow 33\frac{1}{3}\%$$

$$\frac{1}{4} \rightarrow 25\%$$

$$\frac{1}{5} \rightarrow 20\%$$

$$\frac{1}{6} \rightarrow 16.\overline{6}\%$$

$$\frac{1}{7} \rightarrow 14.\overline{28}\%$$

$$\frac{1}{8} \rightarrow 12.\overline{5}\%$$

$$\frac{1}{9} \rightarrow 11.\overline{1}\%$$

$$\frac{1}{10} \rightarrow 10\%$$

$$\frac{1}{11} \rightarrow 9.\overline{09}\%$$

$$\frac{1}{12} \rightarrow 8.\overline{33}\%$$

$$\frac{1}{13} \rightarrow 7.\overline{69}\%$$

$$\frac{1}{14} \rightarrow 7.\overline{14}\%$$

$$\frac{1}{15} \rightarrow 6.\overline{66}\%$$

$$\frac{1}{16} \rightarrow 6.\overline{25}\%$$

$$\frac{1}{17} \rightarrow 5.\overline{88}\%$$

$$\frac{1}{18} \rightarrow 5.\overline{55}\%$$

$$\frac{1}{19} \rightarrow 5.\overline{26}\%$$

42.75% of 960

$$48\% \text{ of } 960 \\ 50\% - 6.25\%$$

$$1\% \text{ of } 960 = 9.6$$

$$\frac{1}{2} \times 960 - \frac{1}{16} \times 960$$

$$480 - 60 = 420 - 9.6$$

$$\Rightarrow 410.4$$

$$32\% \text{ of } 55 = 55\% \text{ of } 32$$

$$9\% \text{ of } 6 = 6\% \text{ of } 9$$

$$16 + 1.6 = 17.6$$

$$24\% \text{ of } 225 = 25\% \text{ of } 24$$

$$\cancel{25\% \text{ of } 225} \Rightarrow 200\% + 25\% \\ \Rightarrow 48 + 6$$

$$\Rightarrow 54$$

$$83.\overline{33}\% \text{ of } 1296$$

$$50\%, 33.\overline{33}$$

$$83.\overline{33} = \frac{5}{6}$$

or

$$10\% \cdot 8.\overline{33}$$

$$10 \times \frac{1}{12} + \frac{5}{6} \text{ of } 1296 = 1080$$

$$91.\overline{66} \text{ of } 2472$$

$$100\% - 8.\overline{33}$$

$$1 - \cancel{\frac{1}{12}} = \frac{11}{12}$$

$$\frac{11}{12} \times 2470 = 2261$$

$$\textcircled{8} \quad 87.5\% \text{ of } 2432$$

$$100 - 12.5$$

$$1 - \frac{1}{8} = \frac{7}{8}$$

$$\frac{7}{8} \times 2432 = \boxed{2128}$$

$$\textcircled{9} \quad 14.2\% \text{ of } 230$$

$$14.2\% \text{ of } 230$$

$$\frac{1}{7} \times 230 = \boxed{34}$$

$$\textcircled{10} \quad 44.44\% \text{ of } 9936$$

$$4 \times 11.11 \text{ of } 9936$$

$$4 \times \frac{1}{9} \times 9936 = \boxed{4454.4}$$

$$\textcircled{11} \quad 45\% \text{ of } 2662$$

$$50\% - 5\%$$

$$1331 \leftarrow 133.1$$

$$\Rightarrow \cancel{133.1} \cancel{+ 99} \boxed{197.9}$$

$$\textcircled{12} \quad = 45\% \text{ of } 2662$$

$$45 + 45\% \text{ of } 2662.$$

$$5 \times 9.09\%$$

$$\frac{5}{11} \times 2662 = 242 \times 5 \\ \Rightarrow \boxed{1210}$$

$$\textcircled{13} \quad 42.044\% \text{ of } 245$$

$$\cancel{245} \times \cancel{42.044}.$$

$$(20 + 5\%)$$

$$3 \times 14.28 = \frac{3}{7} \times 245 = \boxed{105}$$

19/July/18  
Test of Divisibility. (ABCD)

① 2  $\rightarrow$  ABC 0/2

② 3  $\rightarrow$   $(A+B+C+D)/3$

③ 4  $\rightarrow$  ABC (C/D)

④ 5  $\rightarrow$  ABC 0/5

⑤ 6  $\rightarrow$  ABCD is even  
 $\& (A+B+C+D)/3$

⑥ 7:

⑦ 8  $\rightarrow$  A (BCD)/8

⑧ 9  $\rightarrow$   $(A+B+C+D)/9$

⑨ 10  $\rightarrow$  ABC 0

⑩ 11  $\rightarrow$  A B C D

$$\left[ \frac{(C+B+D)-(A+C)}{11} \right] \text{ or } = 0$$

for finding unit digit  
(2, 3, 7, 8, 4, 9)  
⑥ x.

if Non zero Rem  
↓  
Process

Zero Rem.  
↓  
Procedure

baseRem=6  
" " odd = 1

Cyclicity

unit digit  
→ used for calculating  
unit digits:

① cyclicity of 1. =  $\boxed{1}$

$1^n \rightarrow$  unit digit always 1

② 2  $\rightarrow$   $\boxed{2, 4, 8, 6}$

③ 3  $\rightarrow$   $\boxed{3, 9, 7, 1}$

④ 4  $\rightarrow$   $\boxed{4, 6}$

Unit digit of  $4^n$  depends on n  
if  $n=$  odd, unit digit = 4  
 $n=$  even " " = 6

⑤ 5  $\rightarrow$  always  $\boxed{5}$

⑥ 6  $\rightarrow$   $\boxed{6}$

⑦ 7  $\rightarrow$   $\boxed{7, 9, 3, 1}$

⑧ 8  $\rightarrow$   $\boxed{8, 4, 2, 6}$

⑨ 9  $\rightarrow$   $\boxed{9, 1}$

⑩ 0  $\rightarrow$   $\boxed{0}$

Conclusion:

0, 1, 5, 6  $\rightarrow$  Same unit digit

(2, 3, 7, 8)  $\rightarrow$  freq. is 4

(4, 9)  $\rightarrow$  " is 2

Finding Zeros at last in the expression.

These should be multiple of 10 direct ( $10 \times 100 \dots$ )  
+

Detailed multiple (hidden)  $\rightarrow (5 \times 2)$

Note

The total No. of  $(2 \times 5)$  combinations in the expression  
is equal to No. of zeros at last in the expression.

$$\boxed{\text{Least No. of } (2 \times 5) = \text{No. of zeros at last.}}$$

Ex:  $25 \times 4 \times 7 \times 16 \times 10 \times 8 \times 100$ .

$$5^2 \times 2^2 \times 7 \times 2^4 \times 5 \times 2 \times 2^3 \times 2^2 \times 5^2 = (2^{12} \times 5^5)$$

$$\text{Least } = [5] = (2^5 \times 5^5)$$

Hence 5 zeros at last.

Ex How many zeros at last in

$\textcircled{1}$  L6     $\textcircled{2}$  L100

$$\rightarrow L6 = 6 \times 5 \times 4 \times 3 \times 2 \times 1 =$$

$$= 2 \times 3 \times 5 \times 2 \times 2 \times 3 \times 2 \times 1 =$$

$$(2 \times 5)^7 \Rightarrow (2^4 \times 5^1) \Rightarrow (2 \times 5)^1 \text{ least} = [1] \text{ zero.}$$

Note  $\rightarrow$  for any factorial greater than (L4), total No. of 5 in the expansion are always less than total No. of 2 in the expression.

Since Least power is always our answer.

Since Least power is always our answer.  
i.e. The exponent of 5 is nothing but total No. of zeros at last in the expansion.

$$\text{S.C. } L_{145} = \frac{145}{5}^{29} + \frac{145}{25}^5 + \frac{145}{125}^1 \Rightarrow [29+5+1] = \begin{matrix} (35 \text{ zero}) \\ \text{at last} \end{matrix}$$

$$\text{formula} \rightarrow \left[ \frac{x}{5^1} + \frac{x}{5^2} + \frac{x}{5^3} + \dots + \frac{x}{5^n} \right] \quad 5^n \leq x$$

This conceptual formula is applicable for all the prime No.

Q What is highest power of 3 in  $\text{exp}^m 110$ .

$$\frac{x}{3} + \frac{x}{3^1} + \frac{x}{3^2} + \dots = \frac{x}{3^n} \quad 3^n \leq x.$$

$$\frac{100}{3} + \frac{100}{9} + \frac{100}{27} + \dots = \boxed{48}$$

$$= \text{exp} \quad \boxed{110}^{\underline{3}}$$

$$\frac{10}{5} = \boxed{2}.$$

$2 \times \underline{13} = (12 \text{ zero atleast})$

To find No. of factors  $\rightarrow$   
Ex How many factors of 1800.

$$\rightarrow 2^3 \times 3^2 \times 5^2$$

① Prime factorize

② write all powers separately  $\rightarrow 3^2 \times 2^3 = 2^3$

③ add 1 to each power.  $\rightarrow (3+1) (2+1) (2+1)$

④ multiply.  $\rightarrow 4 \times 3 \times 3 = \boxed{36}$

find even factors

① Prime factorize

② write all powers separately

③ don't add 1 in the 2's power  
④ multiply.

$$2^3 \times 3^2 \times 5^2$$

$$\text{even factors} = 3 \times (2+1) \times (2+1)$$

$$\Rightarrow \boxed{27}$$

find odd factors

① Prime factorize

② do not consider the section of 2 at all.  ~~$2^3 \times 3^2 \times 5^2$~~

$$(2+1) \times (2+1) = \boxed{9}$$

$$\boxed{\text{Total} - \text{even} = \text{odd}}$$

✓  $\rightarrow$  vinculum ( $\overline{101}$ )

B  $\rightarrow$  [ ]

O  $\rightarrow$  { }

D  $\rightarrow$  %

M  $\rightarrow$  \*

A  $\rightarrow$  +

S  $\rightarrow$  -

$$\rightarrow \text{HCF } d(a) = \frac{\text{HCF of Numerator}}{\text{LCM of Denominators}}$$

$$\rightarrow a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$

$$\rightarrow a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

$$\rightarrow a^4 - b^4 = (a^2)^2 - (b^2)^2$$

$$= (a^2 + b^2)(a^2 - b^2)$$

$$\rightarrow (a+b)^2 - (a-b)^2 = 4ab$$

$$\rightarrow (a+b)^2 + (a-b)^2 = 2(a^2 + b^2)$$

$\rightarrow$  Remainder theorem

$$\left( \frac{ax+bc}{n} \right) \text{ i.e. (ax+bc) divided by } n = \text{Remainder of } \left( \frac{an+r}{n} \right)$$

where  $a_n$  is remainder when  $a$  is divided by  $n$

$$bn \equiv a \quad (b \equiv a \text{ mod } n)$$

$$cn \equiv b \quad (c \equiv b \text{ mod } n)$$

Ex Find Remainder of  $\frac{15 \times 17 \times 19}{7}$  when divided by 7.

$$\frac{1 \times 3 \times 5}{7} = \frac{15}{7} = 1 \Rightarrow \text{Remainder } 1$$

Polynomial theorem:

$$(x+a)^n = x^n + {}^n C_1 x^{n-1} a^1 + {}^n C_2 x^{n-2} a^2 + {}^n C_3 x^{n-3} a^3 + \dots + {}^n C_{n-1} x^1 a^{n-1} + a^n.$$

$$\frac{(x+a)^n}{x} = \frac{(x^n + {}^n C_1 x^{n-1} a^1 + \dots + {}^n C_{n-1} x^1 a^{n-1} + a^n)}{x}$$

∴ Remainder is  $\left( \frac{a^n}{x} \right)$  b/c rest of term contain  $x$  hence completely divisible by  $x$ .

$$\text{Ex } \frac{9^{99}}{8} \Rightarrow \frac{(8+1)^{99}}{8} \Rightarrow \frac{1^{99}}{8} = 1 \approx$$

$$\frac{5^{100}}{7} \Rightarrow \frac{(25)^{50}}{7} \Rightarrow \frac{(7 \times 3 + 4)^{50}}{7} = \frac{4^{50}}{7} \Rightarrow \frac{2^{100}}{7} = \frac{(2^3)^{33} \times 2}{7}$$

$$\Rightarrow \frac{9(7+1)^{33} \times 2}{7} \Rightarrow \left( \frac{1 \times 2}{7} \right) \Rightarrow 9 \approx$$

Case 1 → on dividing a number by  $a, b \& c$ ,  
 if we get  $a-k, b-k, c-k$  as remainder resp.  
 then [number will be =  $n \times \text{LCM of } [a, b, c] - k$ ]

Ex on dividing a No. by  $x$  by 4, 5, & 6 we get  
 remainder : 3, 4, 5 find the No. ( $x$ ).

$\begin{array}{ccc} 4 & 5 & 6 \\ \text{Remainder} & 3 & 4 & 5 \\ = & (4-1) (5-1) (6-1) i.e. k=1 \end{array}$	so that No. will be. $n \times \text{LCM of } [a, b, c] - k$ $n \times \text{LCM } (4, 5, 6) - 1$ $\Rightarrow [60n - 1] \text{ if } n=1 = \boxed{59}$ is the smallest such natural No. for highest No. →
--	---

Case 2 → on dividing a no. ( $x$ ) by  $a, b, \& c$ , if we get  
 $k$  as remainder always then that ~~be  $x$~~ .

No. will be  $x = (n-1) \text{LCM } (a, b, c) + k$ ,

Ex if  $5, 6, 7$ , dividing by  $x$ , we get 2 as remainder then what  $x$ .

$(n-1) \text{LCM } (a, b, c) + k \rightarrow (n-1) \text{LCM } (5, 6, 7) + 2.$

$\Rightarrow (n-1)210 + 2$

$\Rightarrow 2$  is such a smallest No.

next will be =  $210 + 2 = \boxed{212}$

Case 3 → if a no. after adding  $k$  is exactly divisible by  $a, b, c$   
 then that No. will be  $x = n \times \text{LCM } (a, b, c) - k$

Ex find a No. which after adding 7 is divisible by 10, 11, 12.

$n \text{LCM } (10, 11, 12) - 7 \Rightarrow n660 - 7 = \boxed{653} \text{ (n=1)}$

26/July/2018

## Vector

### Loss & profit

1) CP (Cost Price)

$$\text{Profit} = SP - CP = SP - CP$$

2) SP (Selling Price)

$$\text{Loss} = CP - SP = CP - SP$$

3) MP (Marked ")

discount

$$\% \text{ Profit} = \left( \frac{SP - CP}{CP} \right) \times 100$$

or  $\frac{\text{Profit}}{CP} \times 100$

$$\% \text{ Loss} = \frac{CP - SP}{CP} \times 100$$

$\frac{100}{CP} \times 100$

→ In profit & loss  $\rightarrow$  CP is always different.

→ In discount  $\rightarrow$  MP is " "

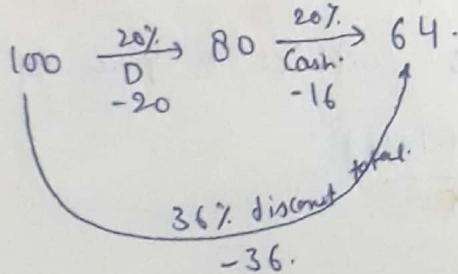
Q SP = 1499 flipkart give 20% of 20% cashback.

+ Amazon give 10% discount & 30% cashback.

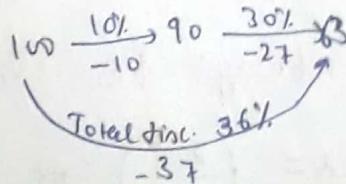
Take 100 as reference

price always

f.



A.



Q If CP = 2400 MP = 3000 SP = (on 10% discount)

$$SP = 3000 - 300 = 2700$$

$$\text{Profit} = 300$$

$$CP 100 \rightarrow ?$$
  
$$2400 \times ? = \frac{2700 \times 100}{2400}$$

$$? = 12.5\%$$

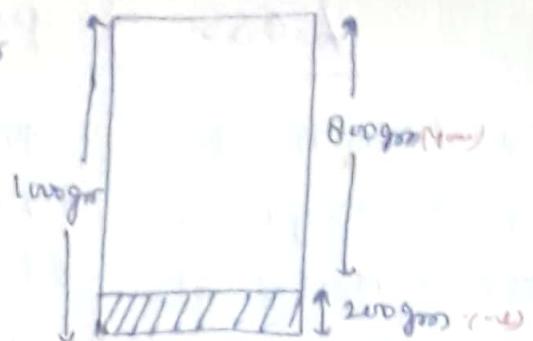
Q True weight = 1000 gm false weight = 800 gm

800 → 200 gm

100 → ?

$$? \times 800 = 200 \times 100$$

$$\boxed{? = 25\%}$$



$$\boxed{\text{Profit \%} = \frac{T.W - F.W}{F.W} \times 100}$$

Q Adyar  
SP = 49,00,000

Profit 25%

Besant Nagar  
49,00,000

Loss 25%

$$\frac{x^2}{100} = \frac{25 \times 25}{100} = \boxed{-6.25} \approx$$

Note:- Whenever there is same selling price (SP)

they have same % of profit & loss.

there always be a loss which is given by

$$\text{Loss} = \left( \frac{x^2}{100} \right) \text{ or } \frac{(\text{Profit or Loss})^2}{100}$$

$$\rightarrow (\text{Profit} +) \quad (\text{Loss} -)$$

$$\rightarrow \boxed{\text{Rate} \uparrow * \text{Consumption} \downarrow = \text{Expenditure constant}}$$

$\uparrow \frac{1}{n} \quad \underset{\text{compensated by}}{\text{by}} \quad \left( \frac{1}{n+1} \right) \downarrow$

for successive ~~successive~~ profit (+) & loss (-).

$$(P+ \text{or } L) = \left[ A + (-B) + \frac{(A)(-B)}{100} \right]$$

① If S.P is different but having same profit of loss on different SP. Hence.

CP is  $\left( \frac{SP_1 + SP_2}{2} \right)$  or  $[SP_1 - CP = CP - SP_2]$

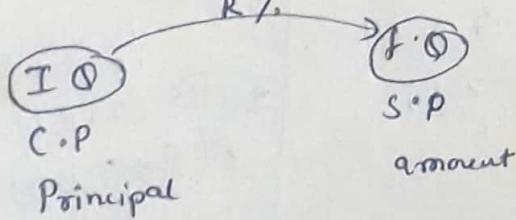
→ If an article is sold at a gain of 20% then  $SP = 120\% \text{ of } CP$  or  $[(20\% \text{ of } CP) + CP]$ .

→ If an article is sold at a loss of 20% then  $SP = 80\% \text{ of } CP$ .

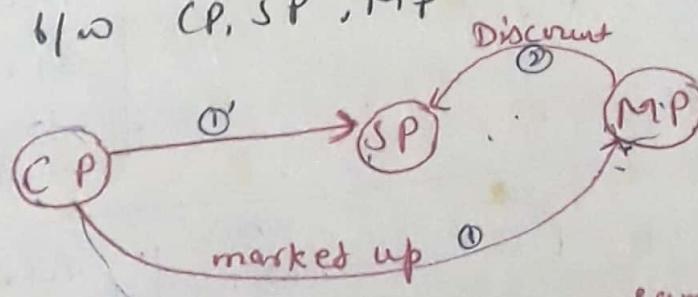
UTube

$$\text{Final Quantity} = \frac{SP}{\text{Initial C.P}} \left( 1 \pm \frac{\text{Gain/Loss}}{100} \right)^n$$

$n = \text{no. of steps}$



Relation b/w CP, SP, MP



→ always compare price with same quantity.

25<sup>th</sup> July.

Q Cost of 8 article = SP of 6 articles, find out profit/loss%.

$$SP\ of\ 6 = CP\ of\ 8.$$

$$\frac{SP}{CP} = \frac{8}{6} \rightarrow \left[ \frac{2}{3} \times 100\% P \right]$$

$$\frac{SP - CP}{CP} = \left( \frac{8-6}{6} \right) \times 100 \left[ 33\frac{1}{3}\% P \right]$$

$$\rightarrow \frac{2}{3} \times 100 \rightarrow \left[ 33\frac{1}{3}\% \right]$$

Sir.

$$CP\ of\ 8 = SP\ of\ 6.$$

$$CP\ of\ 8 = 8Rs$$

$$SP\ of\ 6 = 8Rs$$

$$CP\ of\ 6 = 6Rs.$$

$$6 \rightarrow 2$$

$$100 \rightarrow 2\left(33\frac{1}{3}\%\right)$$

$$CP(8) = SP(6)$$

$$\frac{CP}{SP} = \frac{6}{8}$$

$$CP = 6 \quad 6 \rightarrow 2$$

$$SP = 8 \quad 100 \rightarrow 33\frac{1}{3}$$

$$\begin{array}{c} \text{SC} \\ CP\ of\ 8 = SP\ of\ 6 \end{array}$$

→ whenever there is such type of Q. then CP b/w SP & SP b/w CP.

Q In 2018, population is 50k.

it will ↑ by 10%. what will be the population in 2020 & 2016.

$$50,000 = CP \left( 1 + \frac{10}{100} \right)^2$$

$$50,000 = CP \cdot \frac{11}{10} \cdot \frac{11}{10}$$

$$2016 \rightarrow CP = \frac{50,000}{11 \times 11}$$

$$\begin{array}{c} \text{SC} \\ 10\% \rightarrow \begin{cases} 100 \\ +10 \\ \hline 110 \\ \downarrow \\ 10\% \rightarrow \\ 12 \\ \hline 121 \end{cases} \end{array}$$

$$\begin{array}{ccc} 2018 & 100 \rightarrow 121 \\ \text{if} & 50,000 \rightarrow ? \end{array}$$

$$\uparrow 5\% / yr \rightarrow 9261 \rightarrow 3 \text{ years ago} \rightarrow ?$$

$$\begin{array}{c} \checkmark 50k \left( 1 + \frac{10}{100} \right)^2 \\ \frac{11}{10} \times \frac{11}{10} \times 50,000 \\ 2020 \quad 121 \times 500 \\ (60,500) \end{array}$$

$$\begin{array}{c} 50,000 \cdot \frac{9}{10} \times \frac{9}{10} \\ .81 \times 500 \\ 40,500 \end{array}$$

N.B

SP of 4,

SP / CP

10  
8  
80  
80

60  
SP (1)

Income =

97000 =

$$\begin{array}{c} Q \\ = \\ 150 \\ SP = 96 \\ 9625 \\ CP = 9 \end{array}$$

77

120%

Cubes - 1-20  
square - 1-30

②  
=

SP(1.4)

N.B

SP of 4,

Income = Saving + Expenditure

$$97000 = 70000 + 27000$$

Q SP = 9625 Loss = 23% . what price taget 20%  
= 100  
$$9625 = CP \left(1 - \frac{23}{100}\right)$$
$$CP = \frac{(9625 \times 100)}{77}$$

A10.  $77\% = 9625 \Rightarrow 77\% ? = 9625 \times 120$

$$120\% = ? \quad ? = \frac{9625 \times 120}{77}$$

$$? = \frac{120 \times 120}{77} = 15000$$

cubes = 1-20

square = 1-30

②  
=

$$SP(4) = CP(3)$$

Find P or L%.  $100 \rightarrow ?$

$$\frac{SP}{CP} = \frac{3}{4} \Rightarrow L = \frac{1}{4} \times 100 = 25\%$$

A16  
SP of 4 = CP of 3

4 → 1

100 → ?

$$? = 25\% \text{ loss}$$

③  
-

10 → Re 40. → CP

8 → 34 → SP.

$$\text{Profit} = \frac{24}{32} \times 100 = \frac{50}{8}$$

80 → 64 → CP

80 → 340 → SP

$$P = 6.25\%$$

④  
-

60 Mangoes → 100 → 10% P → 10  
SP (60M → 100 → ?)  $\frac{10 \times 100}{60} \cdot 6 = \frac{600}{6}$

$$SP \text{ of } 60 - CP \text{ of } 60 = CP \text{ of } 10$$

$$SP \text{ of } 60 = CP \text{ of } 70.$$

$$60 \rightarrow 10$$

$$100 \rightarrow ?$$

$$\boxed{? = 16\left(\frac{2}{3}\right)}$$

(5)  $28 \rightarrow SP_B \rightarrow CP$  40% profit. How many lemons sold for 10?

$$? \rightarrow 100$$

$$\left( \frac{100 \times 28}{x} \right) \quad \textcircled{6}$$

$$\begin{aligned} CP \text{ of } 10 &= \left( \frac{50}{28} \right) \\ SP \text{ of } 10 &= \frac{50}{28} \left( 1 + \frac{40}{100} \right) \Rightarrow \frac{50}{28} \times \frac{14}{10} = \frac{5}{2} \\ SP &= \frac{100}{x} \\ \frac{40}{100} &= \frac{100}{x} - 1 \Rightarrow \frac{1}{10} + 1 = \frac{100}{x} \times \frac{28}{50} \\ x &= \frac{2 \times 28 \times 10}{14} = 40. \end{aligned}$$

$$Rs. 50 \rightarrow 28 \text{ lemon.}$$

$$\text{from Rs. } 100 \xrightarrow{40\%} 40.$$

$$Rs. 40 \xrightarrow{40\%} 20.$$

hence  $Rs. 70 \rightarrow 28 \text{ lemon.} \Rightarrow \frac{100 \times 28}{70} \quad \textcircled{7} \Rightarrow \boxed{40}.$

(6) Loss = 5%. more 700 Rs. then gain of 7.5%.  
find CP.

$$\begin{array}{ccc} 100x & \xrightarrow{\text{SP}} & (95) \\ 850 & \xrightarrow{\cancel{x}} & \end{array}$$

$$\begin{aligned} 850 &= CP \left( 1 + \frac{7.5}{100} \right) \\ 850 \cdot CP &= \frac{107.5}{100} \cdot CP \\ CP &= \frac{400}{34} \left( \frac{850 + 1000}{107.5} \right) \\ &= \frac{400}{34} \cdot \frac{1850}{107.5} \\ &= \frac{400}{34} \cdot 17.5 \\ &= 6000 \end{aligned}$$

$$95\% + 750 = 107.5\%$$

$$750 = 12.5\%.$$

$$? = 100\%.$$

$$\boxed{? = 6000} \approx$$

(7)

$$\begin{array}{c}
 300 \\
 | \\
 100 + 10 = 110 \\
 | \\
 200 (-35) ? \\
 | \\
 (235) ?
 \end{array}
 \quad
 \begin{array}{c}
 (30+15) \\
 \downarrow \\
 345 \\
 | \\
 345 - 110 = 235 \\
 | \\
 200 \rightarrow 35 \\
 | \\
 100 \rightarrow (17.5) ?
 \end{array}$$

(8)

$$\begin{array}{c}
 4500 \\
 | \\
 1500 + 10\% = 1650 \\
 | \\
 3000 + 15\% = 3450 \\
 | \\
 3525
 \end{array}
 \quad
 \begin{array}{c}
 15\% \\
 \downarrow \\
 4500 - 1650 = 2850 \\
 | \\
 4500 - 3450 = 1050 \\
 | \\
 3525
 \end{array}
 \quad
 \begin{array}{c}
 3000 \rightarrow 525 \\
 100 \rightarrow ? \\
 1680 \times 525 = 3000 \\
 | \\
 f
 \end{array}$$

(9)

$$\begin{array}{c}
 \$750 \text{ gain} \rightarrow [250] \\
 100 \rightarrow ?
 \end{array}
 \quad
 ? = \frac{100 \times 250}{384} = (33\frac{1}{3}) \approx$$

(9)

$$\begin{array}{l}
 SP = 18000 \rightarrow \text{Profit} \\
 SP = 16800 \rightarrow \text{Loss} \\
 \text{Profit} = \text{Loss} \Rightarrow \frac{16800}{x} = \frac{18000 - x}{x} \\
 \Rightarrow 2x = (34800) \\
 x = 17400 \text{ Rs.}
 \end{array}$$

(10)

$$\begin{array}{c}
 \text{S.P.} = 18000 \\
 \text{C.P.} = 16800 \\
 \text{Profit} = 18000 - 16800 = 1200
 \end{array}$$

$$2x = 1200 \\ x = 600 \checkmark$$

$$\text{C.P.} = 16800 + 600 = 17400 \approx$$

$$25 \leftarrow 20 \\ 10 \rightarrow ?$$

$$\frac{20}{25}$$

(10)

$SP = 1200$  Profit  $\rightarrow$  twice.

$$2(\text{Profit}) = (\text{Loss or } SP - \text{C.P.})$$

$$2(1200 - x) = (x - 600)$$

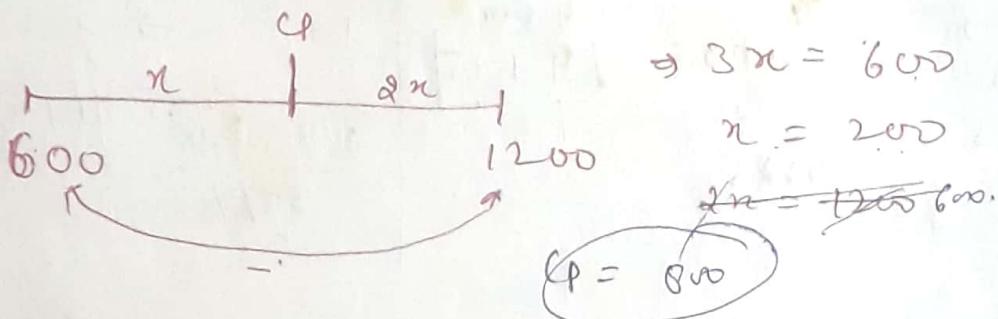
~~2400~~  $\cancel{x}$

$$8x = 3000 \quad 600$$

~~2400~~

~~300~~

$x = 1000$



26/July

(11)

$$\begin{array}{r} \text{Rs} \\ \parallel \\ \begin{array}{r} 100 \rightarrow CP \\ + 40 \\ \hline 140 \rightarrow MP \\ - 28 \\ \hline 112 - SP \end{array} \end{array}$$

(12)

Succesive discount of 10%; 20%; 15%.

$\rightarrow$  total discount of 10% 120% 15%.

Let  $100$

$$\begin{array}{r} 10\% \\ - 10 \\ \hline 90 \\ 20\% \\ - 18 \\ \hline 72 \\ 15\% \\ - 10.8 \\ \hline 61.2 \end{array} \quad \begin{array}{l} \frac{7}{2} : 2 + 3 \cdot 6 \\ 10.8 \end{array}$$

38.8%

No need to follow order.

$$\begin{array}{r} 100 \\ 25\% \\ - 25 \\ \hline 75 \\ x \\ \hline x \end{array} \quad \begin{array}{r} 100 \\ 40\% \\ - 40 \\ \hline 60 \\ 600 \end{array}$$

$$75 - x = 60 \Rightarrow 15 = x$$

$$\begin{array}{l} 10\% \text{ of } 75 \rightarrow 7.5 \\ 20\% \text{ of } 7.5 \rightarrow 1.5 \\ \hline 15.0 \end{array}$$

(14)

$$\begin{array}{c} CP \\ 344.25\% \\ SP \\ 344.25\% \\ MP \\ 150 \\ 100 \end{array}$$

$$344.25 = 400 \left( \frac{90}{100} \right) \left( \frac{100-x}{100} \right)$$

$$100-x = \frac{344.25 \times 100 \times 100}{400 \times 90}$$

$$x = 18\%$$

$$\begin{array}{r} \text{815} \\ - 45 \\ \hline 405 \\ ? 60.75 \\ \hline 344.25 \end{array}$$

$$\begin{array}{r} 54 = 20.75 \\ 10y. = 40.5 \\ 100 \quad ? \\ 60.75 \end{array}$$

$15 = 60.75$

$$15\% = 15.0$$

$$\begin{array}{r} \text{15} \\ \text{50} \rightarrow 60 \\ 100 \quad 12.5 \\ \hline 50 \quad 72.5 \end{array}$$

$$\begin{array}{r} 50 \rightarrow 60 + 12.5 = 72.5 \\ ? \rightarrow (30) \Rightarrow \text{20} \end{array}$$

~~$$\begin{array}{r} 60 \quad 10 \\ 200 \times 50 \\ \hline 72.5 \\ 20 \quad 145.29 \end{array}$$~~

$$\begin{array}{r} \text{815} \\ \text{Rs. } 60 \rightarrow 50 \text{ pence} \\ 25\% \rightarrow 75 \rightarrow 50 \text{ pence} \\ 30 \text{ Rs.} \rightarrow ? \\ ? = \frac{200 \times 10}{75} = 20 \end{array}$$

$$\begin{array}{r} \text{16} \\ \text{200}(50) \rightarrow 100(100) \\ 75x = 200 \\ x = \end{array}$$

$$\begin{array}{r} \text{15} \\ 1 \rightarrow 200 \text{ Rs.} \Rightarrow 125\% \rightarrow 200 \\ 100 y. = ? \end{array}$$

$$\begin{array}{r} \text{CP} = 6 \times 160 = (960). \\ \text{SP} \qquad \qquad \qquad = 1056. \end{array}$$

$$\begin{array}{r} ? = \frac{40}{200 \times 100} \times 200 \\ \qquad \qquad \qquad \Rightarrow 160 \end{array}$$

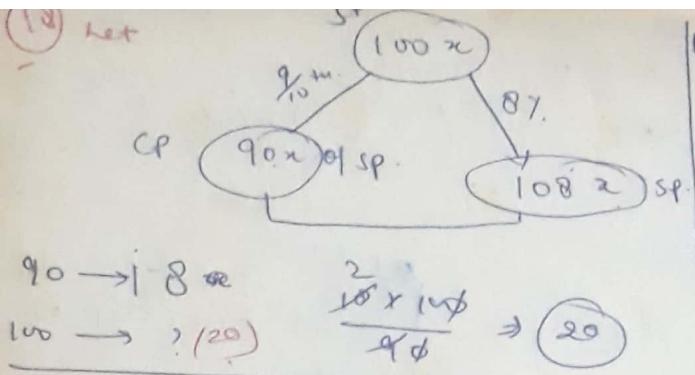
$$\begin{array}{r} 96 \\ 960 \rightarrow 96 \\ 100 \rightarrow ? \quad (10) \end{array}$$

$$\begin{array}{r} \text{17} \\ 125 \rightarrow \text{Rs. } 120 \text{ per stool. Transport exp @ Rs. } 14 \text{ per stool.} \\ \text{Tax} = 6y. \quad \text{Coolie charge} = 250. \end{array}$$

$$\begin{array}{r} 1 \rightarrow 120 \\ 1 \rightarrow 14 \dots = 2.8 \text{ Rs.} \end{array}$$

$$\begin{array}{r} 19 \\ 25 \\ 95 \\ 38 \\ 775 \end{array}$$

$$\begin{array}{r} 3800.0 \rightarrow \text{CP} \\ 25 \\ \text{SP} = \frac{3800 \times 125}{380 + 125} \Rightarrow 25 \times 19 \\ 19 \quad 2.8 \rightarrow 22.5 \\ 132 \times 22.5 \rightarrow 475 \end{array}$$



Q.  $108 = 90 \left( \frac{100+x}{100} \right)$

$$12 \frac{108 \times 100}{90} = 100+x$$

$$120 = 100+x$$

$$x = 20\%$$

(A)  $7\% \text{ of SP} = 8\% \text{ of CP} \quad \left\{ \begin{array}{l} \text{CP}=? \\ 9\% \text{ of SP} + 1 = 10\% \text{ of CP} \end{array} \right.$

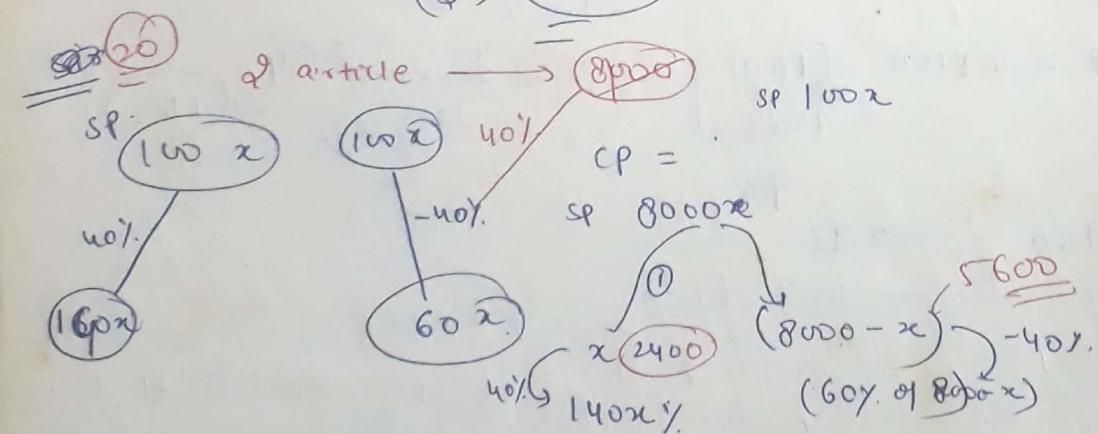
Let

$$7\% \text{ of SP} = 8\% \text{ of CP} \quad 9\% \text{ of SP} + 1 = 10\% \text{ of SP}$$

$$\frac{\text{SP}}{\text{CP}} = \left( \frac{8}{7} \right) \quad \text{SP} = 1.$$

$$\frac{100x}{8\%} \rightarrow \frac{\text{SP} - \text{CP}}{\text{CP}} = \left( \frac{1}{7} \right) \quad 9\% \left( \frac{8}{7} \text{ CP} \right) - 10\% \text{ CP} = 1$$

$$\text{CP} = \left( \frac{7}{2} \right) y \quad \left( 72 - 70 \right) \text{ CP} = 1$$



$$200\% \text{ of } x = 4800$$

$$100x = ? \quad ? = 2400$$

① Percent  $\leftrightarrow$

②  $4\% \text{ of } x = 12$

$$x = \frac{1200}{4\%}$$

③  $x\% \text{ of } 44 = 10$

$$x = \frac{10}{44\%}$$

$44 \rightarrow 33$

$100 \rightarrow ? \quad ? = 75$

29 75

30  $\frac{300}{100} = 0.3P$

$0.7P$

$P =$

~~816~~ 70 %

~~100~~  $\frac{?}{160}$

$\frac{816}{100} = 120x$

$120x = 11$

## Percentage

① Percent  $\rightarrow$  fraction

$$② 4\% \text{ of } x = 12$$

$$x = \frac{12}{4\%} = 300$$

$$③ x\% \text{ of } 44 = 20\% \text{ of } 165$$

$$x = \frac{20 \times 165}{44} = \frac{150}{2} = 75$$

$$\boxed{x = 75}$$

$$④ \frac{100x}{100} = \frac{150}{39}$$

$$P = \frac{150}{39} = 3\frac{21}{39}$$

$$P = 0.3P + 91 = 91$$

$$0.7P = 91$$

$$P = \frac{91}{0.7} = 130$$

$$\frac{70}{100} = 91$$

$$100\% = ?$$

$$\boxed{? = 130}$$

$$⑤ \frac{560}{P} = \frac{80}{120} P = 1$$

$$P = 80$$

$$120 \times 80 = \boxed{96}$$

$$⑥ 140\% = 112$$

$$120 = (?) \quad \boxed{96}$$

$$⑦ 110\% = 198$$

$$100\% = ?$$

$$? = \frac{198 \times 100}{110} = \boxed{180}$$

$$110 \rightarrow 300$$

$$-150$$

$$150\% \rightarrow \boxed{300}$$

$$180\% \rightarrow 360$$

$$120 \rightarrow ?$$

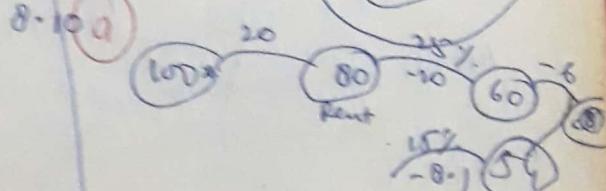
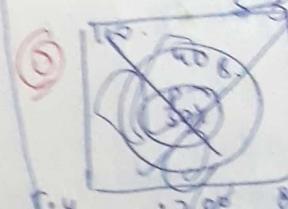
$$? = 240$$

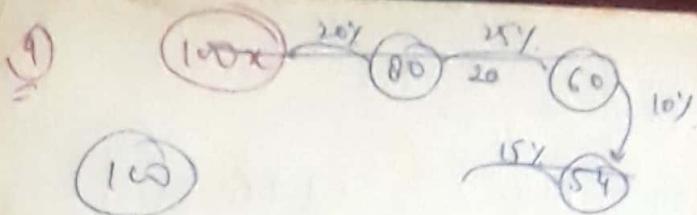
$$⑧ \frac{2100}{26} = \boxed{106}$$

$$100 \leftrightarrow 106$$

$$? \leftrightarrow 156$$

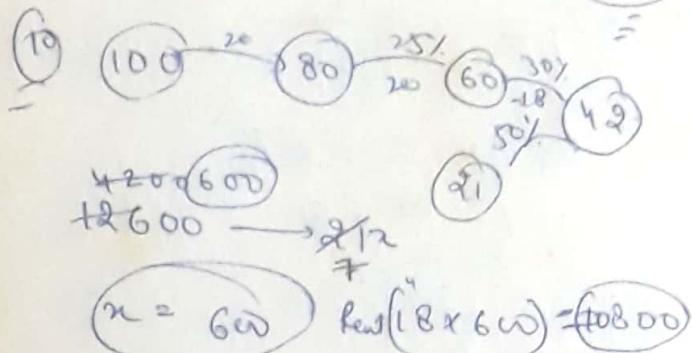
$$? = \frac{156 \times 100}{106} = \boxed{150}$$





100  
 $20 \rightarrow R$   
 $25 \rightarrow F$   
 $10 \rightarrow T$   
 $15 \rightarrow E$   
 $18 \rightarrow H.E.$   
 $\frac{100}{88}$

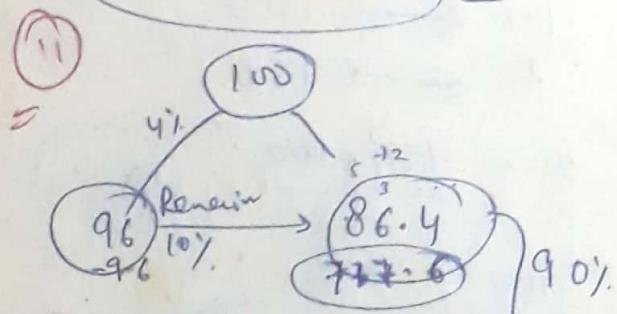
100 → 12  
? → 4800  
?  
 $= \frac{48000 \times 100}{18}$   
 $\Rightarrow 40,000 = 40k$



21 → 12600

18 → ?

? = 10,800

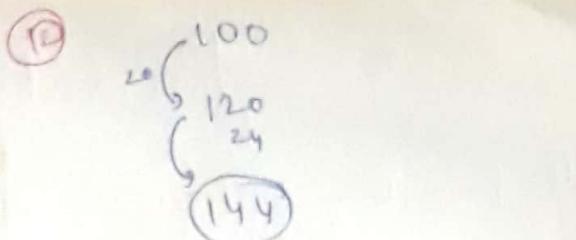


$86.40$   
 $77.76$

$8.64x = 108$

$x = \frac{10800}{864}$   
 $= 12.5$

Applies  $\Rightarrow 1250.0$

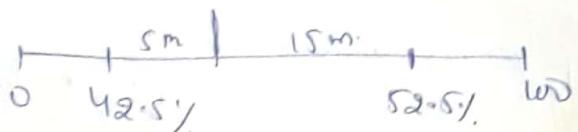


100 ← 144  
? ← 540  
 $\frac{125+15}{540 \times 10} = \frac{144}{4}$

13.

100  
 $42.5x + 5 = 52.8x - 15$   
 $20 = 10.0x$   
 $x = 2$   
~~marks~~  
~~200~~

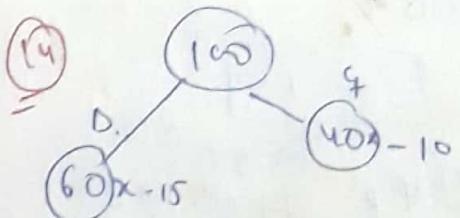
Pants Marks



10% → 20

42.5% → ? = 85

85 = 85 + 5 = 90



~~60x - 15 + 40x - 10 = 50x~~

$50x = 25$   
 $x = \frac{1}{2}$

~~75%~~ → 50%

~~50% = 25~~

~~40% = ? (20)~~

(15)

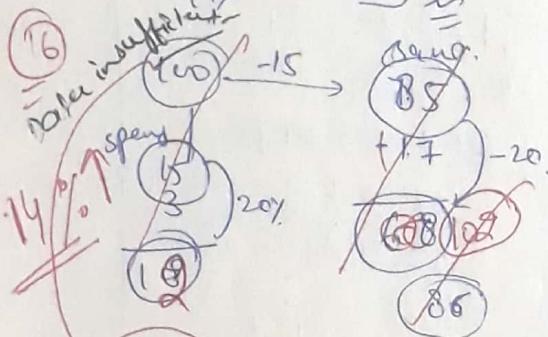
(100) → 80 Apple  
or  
80 mango.

20 → Auto.

Rs 80 → mango → 25 mango.

Rs 100 → 30 mango  
Rs 30 → ?

$$? = \frac{30}{100} \times 30 \rightarrow 9$$



(114)

$$\frac{100}{120} \times \frac{x}{x} \times \frac{6}{6} = \frac{10000}{12000} = \frac{500}{600} = \frac{25}{30}$$

$$x = \frac{10000}{120}$$

$$\frac{100}{120} \times \frac{80}{80} = \frac{100}{120} = \frac{5}{6}$$

$$\frac{100}{80} \times \frac{80}{80} = \frac{100}{80} = \frac{5}{4}$$

$$16 \div 7 = 16\frac{2}{7}$$

$$\frac{10}{30} \times \frac{30}{30} = \frac{10}{30} = \frac{1}{3}$$

(18)

$$R = 20\% H = \frac{(100)}{5} \times 1\%$$

$$V = \pi R^2 h$$

$$\frac{120}{100} \times \frac{120}{100} \times \frac{100}{100} \times \frac{100}{300} = \frac{144}{100} \times \frac{2}{3} = \frac{288}{300} = \frac{8}{10} = \frac{4}{5}$$

$$x = 15000$$

$$x = 15000 - 15K$$

(18)

$$V = \pi R^2 H$$

 $R \uparrow \rightarrow 20\%$  $H \uparrow \text{ by } 33\left(\frac{1}{3}\right)\%$ 

Let

$$R = 5 \quad \frac{20}{20} \times 5 = 6$$

$$H = 3 \quad \frac{33}{3} \times 3 = 2$$

$$V = \pi s^2 h = 75\pi \rightarrow \pi 6^2 2 = 72\pi$$

$$75 \rightarrow 3$$

$$100 \rightarrow ?$$

$$? = 4\% \quad \underline{\underline{R}}$$

(19)

$$P \downarrow 100 \times 100 = 10000$$

$$125 \times x = \frac{400}{80} = \frac{10000}{125} = 80$$

Change in Consumption  
 $100 \rightarrow 80, i.e. 20\%$

Rate  $\times$  Consumption = Exp.

$$P \downarrow 100 \times 100 = 10000 - 550 \quad 15.5\%$$

$$70 \times x = 9450$$

$$\therefore x = \frac{9450}{70} = 135$$

$$100 \rightarrow 135 \rightarrow 35\% \text{ inc}$$

(21)

100

10% invalid

90 valid

70% win

63

27% loss

36% draw

30% tie

$$63x - 27x = 5400$$

$$36x + 30x = 5400 \rightarrow 66x = 5400 \rightarrow x = 81.81$$

$$\begin{aligned}
 & \text{Q1} = 1500 \quad \text{Q2} = 625 \quad \text{Q3} = 390 \\
 & \text{Q4} = 9 \quad \text{Total} = 261 + 46.75 \\
 & \text{Avg} = \frac{261}{4} = 65.25 \\
 & \text{P1} = 11 \quad \text{P2} = 9 \quad \text{P3} = 7 \\
 & \text{P4} = 3 \quad \text{Total P} = 34 \\
 & \text{4} \rightarrow \text{kick} \\
 & \text{Q1} = 1000 \quad \text{Q2} = 500 \\
 & \text{Q3} = 300 \quad \text{Q4} = 100 \\
 & \text{Time} = 0
 \end{aligned}$$

$$\begin{aligned}
 & \text{Q1} = 1000 \rightarrow 100 \quad \text{Q2} = 800 \rightarrow 100 \\
 & \text{Q3} = 600 \rightarrow 100 \quad \text{Q4} = 400 \rightarrow 100 \\
 & \text{100} \rightarrow 250 \quad \text{250} \\
 & \text{Q1} = 100 \quad \text{Q2} = 80 \\
 & \text{Q3} = 60 \quad \text{Q4} = 40 \\
 & \frac{100}{R} = 80 \quad \frac{100}{0.8R} = 60 \\
 & (100 - 80) = 8R \quad 20 = 8R \\
 & 100 - 60 = 40 \quad R = 2.5
 \end{aligned}$$

$$\begin{aligned}
 & \text{Q1} = 20 \rightarrow 10 \text{m} \\
 & \text{Q2} = 1 \text{ mango} \\
 & \text{Q3} = 2 \\
 & \text{Q4} = ? \quad (25)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Q1} = 300 \quad \text{Q2} = 250 \\
 & \text{Q3} = 200 \quad \text{Q4} = 150 \\
 & 150 \rightarrow ? \quad 100 \rightarrow ? \\
 & \text{Q1} = 100 \quad \text{Q2} = 80 \\
 & \text{Q3} = 60 \quad \text{Q4} = 40 \\
 & \text{100} \rightarrow ? \quad (90) \\
 & 90 \rightarrow ? \quad (75)
 \end{aligned}$$

Simple Interest

$I = P \times R \times T$   
 $R = \frac{I}{P \times T}$   
 $P = \frac{I}{R \times T}$   
 $T = \frac{I}{P \times R}$

$\rightarrow$  Principle  
 $\rightarrow$  Rate %  
 $\rightarrow$  Time

$S.I. = P \times R \times T$   
 $A = P + S.I.$   
 $C.I. = P(1 + R)^T - P$

Half Yearly

$C.I. = P(1 + \frac{R}{2})^T - P$

Quarterly

$(1 + \frac{R}{4})^{4T} - 1$

$\approx$

## 31/10/18 Simple Interest & C.I.

Staya

Bank: Indian

Branch: Coimbatore

Amount = 2.75 L

R.I = 14% p.a.

$$\begin{array}{l} 17.5 \text{ L} \\ 3.6\% \text{ pa (3y, Pm)} \\ 60,000 \end{array} \left| \begin{array}{l} 17.5 \text{ L} \\ 11.5\% \text{ pa} \\ 2y \\ 60,240 \end{array} \right.$$

- > Principle amount
- > Rate of Interest
- > Time

- > Simple Interest
- > Compound II
- > Amount

$$SI = \frac{P \cdot T \cdot R}{100} \quad \text{or} \quad \frac{P \cdot N \cdot R}{100}$$

month.  
Principle amount = Principle + Interest.  
 $\frac{\text{Principle}}{12 \text{ months}}$

SI  
CI  
Remains constant every year.

Annually

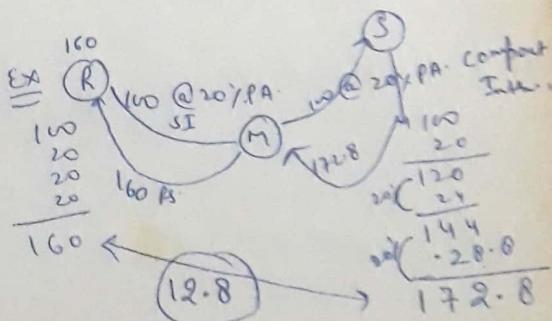
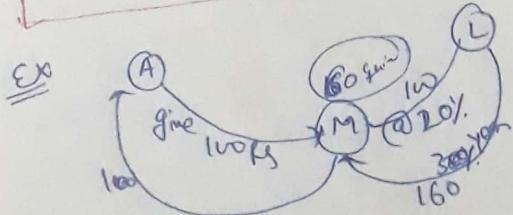
$$CI = P \left( 1 + \frac{R}{100} \right)^N - P$$

half yearly

$$CI = P \left( 1 + \frac{R/2}{100} \right)^{2N} - P$$

Quarterly

$$CI = P \left( 1 + \frac{R/4}{100} \right)^{4N} - P$$



(2) 20% P.A.

SI

100

20

20

20

20% P.A.

CI

100

20

40

20

+ 4

20

+ 8.8

44  
20%

$$\text{Q1} \quad 100 \\ = R.Y. = 4\% \\ T = 2 \text{ yrs}$$

$$100 \\ 4 \\ 4 \\ 108$$

$$100 \\ ? \\ ? =$$

$$\text{Q2} \quad 100 \\ - \\ 100 \\ 100 \\ ?$$

$$\text{CI} \\ T \\ SI \\ I \\ II$$

$$\text{I} \\ \text{II}$$

\* SI is same for all time periods.

\* 1<sup>st</sup> yr of CI is same as SI.

CI < SI  $\Rightarrow$  Relation b/w SI & CI.

For 2 yrs

$$\text{Ratio relation} = \frac{CI}{SI} = \left(1 + \frac{R}{100}\right)^2$$

Difference relation

$$CI - SI = P \left( \frac{R}{100} \right)^2 \left( \frac{R}{100} + 3 \right)$$

$$\text{Difference relation} = CI - SI = P \left( \frac{R}{100} \right)^2$$

$$\textcircled{Q} \quad \begin{array}{r} 100 \\ - R.y. = 4y. \\ \hline 100 \end{array}$$

$$T = 2y.$$

$$\begin{array}{r} 100 \\ - 4 \\ \hline 108 \end{array}$$

$$\begin{array}{r} 100 \\ - R = 5y. \\ \hline 100 \end{array}$$

$$T = 3y.$$

$$\begin{array}{r} 100 \\ - 5 \\ \hline 115 \end{array}$$

Rs.

$$\begin{array}{r} 100 \longrightarrow ? \\ ? \longrightarrow 245 \end{array}$$

$$\boxed{? = 3500}$$

$$\textcircled{Q} \quad \begin{array}{r} 100 \\ - 15 \\ \hline 100 \end{array} \quad \begin{array}{r} 100 \longrightarrow 16\phi. \\ ? \longrightarrow 880\phi \\ + 55 \end{array}$$

$$\hline 160$$

$$\boxed{? = 5500}$$

$$\textcircled{Q} \quad \begin{array}{l} S.I. = ? \\ P = 5000 \quad T = 2 \\ R = 12\% \end{array}$$

MI

$$\begin{array}{c} 5000 \\ | \quad | \\ CI \\ | \quad | \\ 600 \\ | \quad | \\ 600 + 72 \\ | \quad | \\ 6972 \\ | \quad | \\ 1272 \end{array}$$

$$\boxed{1272}$$

$$\begin{array}{r} 100 \\ | \quad | \\ 105 \\ | \quad | \\ 110.25 \\ | \quad | \\ 115.3125 \\ | \quad | \\ 115.7625 \end{array}$$

$$11.025$$

$$5.5125$$

$$115.7625$$

$$100 \leftarrow$$

$$9262 \leftarrow$$

$$? \leftarrow$$

$$\textcircled{B} \quad \begin{array}{l} CI = 40\% R.S. \\ T = 2 \\ SI = \end{array} \quad \begin{array}{r} SI \\ | \quad | \\ 100 \\ | \quad | \\ 100 \\ | \quad | \\ 150 \\ | \quad | \\ 150 \\ | \quad | \\ 400 \\ | \quad | \\ 475 \end{array} \quad \begin{array}{r} CI \\ | \quad | \\ 100 \\ | \quad | \\ 100 \\ | \quad | \\ 150 \\ | \quad | \\ 150 \\ | \quad | \\ 225 \\ | \quad | \\ 225 \end{array}$$

$$\text{I} \quad \begin{array}{r} SI \\ 200 \\ | \quad | \\ 200 \end{array}$$

$$\begin{array}{r} CI \\ 200 \\ | \quad | \\ 200 \end{array}$$

$$\text{II} \quad \begin{array}{r} 200 \\ | \quad | \\ 400 \end{array} \quad \begin{array}{r} 200 + 8 \\ | \quad | \\ 408 \end{array}$$

$$\begin{array}{r} 200 \longrightarrow 8 \\ 100 \longrightarrow ? \\ | \quad | \end{array} \quad \textcircled{4} \quad \text{Ans}$$

$$\begin{array}{r} ? \longrightarrow 200. \\ | \quad | \end{array}$$

$$\boxed{? = 5000}$$

$$\textcircled{A} \quad P \left(1 + \frac{R}{100}\right)^N.$$

$$9261 = P \left(1 + \frac{S}{100}\right)^3.$$

$$9261 = P \left(\frac{105}{100}\right) \left(\frac{105}{100}\right) \left(\frac{105}{100}\right)$$



given SI

→ ?  
2

SI  
0% 350000

2200  
500

SI → 5000

$\gamma = 1000 + 50$   
 $= 2000 + 310$

860

→ 5%

+ 5

⑨  $100 \xrightarrow{R} 300$   
 $200 \xrightarrow{R} 600$   
 $300 \xrightarrow{R} 900$   
 $SI = 200$

$100 \xrightarrow{R} 600$   
 $200 \xrightarrow{R} 1600$   
 $400 \xrightarrow{R} 3200$   
 $600 \xrightarrow{R} 4800$

⑩  $100 \xrightarrow{R} 200$   
 $100 \xrightarrow{R} 300$   
 $100 + ? \rightarrow ?$

Growth rate.

SI → AP → Difference

CI → GP → Ratio (Exponential)

CI  
 $100 \xrightarrow{R} 200$   
 $200 \xrightarrow{R} 400$   
 $400 \xrightarrow{R} 800$   
 $800 \xrightarrow{R} 1600$   
 $1600 \xrightarrow{R} 3200$   
 $3200 \xrightarrow{R} 6400$   
 $6400 \xrightarrow{R} 12800$   
 $12800 \xrightarrow{R} 25600$   
 $25600 \xrightarrow{R} 51200$   
 $51200 \xrightarrow{R} 102400$   
 $102400 \xrightarrow{R} 204800$   
 $204800 \xrightarrow{R} 409600$   
 $409600 \xrightarrow{R} 819200$   
 $819200 \xrightarrow{R} 1638400$   
 $1638400 \xrightarrow{R} 3276800$   
 $3276800 \xrightarrow{R} 6553600$   
 $6553600 \xrightarrow{R} 13107200$   
 $13107200 \xrightarrow{R} 26214400$   
 $26214400 \xrightarrow{R} 52428800$   
 $52428800 \xrightarrow{R} 104857600$   
 $104857600 \xrightarrow{R} 209715200$   
 $209715200 \xrightarrow{R} 419430400$   
 $419430400 \xrightarrow{R} 838860800$   
 $838860800 \xrightarrow{R} 1677721600$   
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 $3355443200 \xrightarrow{R} 6710886400$   
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 $913438380875404452333184002571137024007531520014745600 \xrightarrow{R} 18268767617508089046663680051422740480015063040029491200$   
 $18268767617508089046663680051422740480015063$

$$\begin{array}{r} 4000 \\ 4000 + 400 \\ \hline 4400 \end{array}$$

$$4400 + 840$$

$$\underline{13240}$$

$$(15) P = 10,000$$

$$T = 27 \text{ m. } (24+3)$$

$$3\left(2 + \frac{1}{4}\right) T.$$

$$R = \frac{20}{4} \times 3$$

$$\begin{array}{r} 101000 \\ - 9000 \\ \hline 20000 + 400 \end{array} \quad (\text{CI } R = 27)$$

$$\begin{array}{r} 14400 \\ - 720 \\ \hline 15120 \end{array} \quad 20\% = 5\%$$

$$(16) \text{ SI} \rightarrow (23\%) \text{ A. CI. } 24 \rightarrow 20\%$$

$$\begin{array}{r} 20,000 \\ - 4600 \\ \hline 4600 \\ - 4600 \\ \hline 9200 - 8800 \end{array} \quad \begin{array}{r} 20,000 \\ - 4000 \\ \hline 4000 + 800 \end{array}$$

0400

$$A = 50000 \quad 34. \quad \text{CI \& SI.} \quad 20\% \text{ pa.}$$

SI	CI	
1000	1000	200
1000	1000	+ 200
1000	1000	+ 440
2000		

Diff 640

$$(18) R = 10\%, \quad T = 34$$

$$\text{CI} + \text{SI} = 15.50$$

$$\begin{array}{r} 100 \\ - 10 \\ 10 \\ 10 \\ 10 + 1 \\ 10 \\ \hline 10 + 2.1 \end{array} \quad \begin{array}{r} 61 \\ 10 \\ 10 \\ 10 + 1 \\ 10 + 2.1 \end{array}$$

$$61 \cdot 100 \longrightarrow 3.1$$

$$? \longrightarrow 15.50$$

$$? = \frac{15.50}{3.1} \boxed{5.00}$$

$$(19) P = 1500 \quad \text{pa.}$$

$$R = 12\%, 14\%, 16\%$$

$$\text{SI} = 186. \quad \text{(29\%)}$$

$$R = 10.8\%$$

$$\begin{array}{r} 100x \\ - 9.3 \\ 18.6 \\ \hline 18.6 \end{array} \quad \begin{array}{r} 15.5 \\ - 14.5 \\ \hline 1.0 \end{array}$$

$$24x = 186.$$

$$x = \frac{186}{24} = 7.75$$

R = 7.75

$$\begin{array}{l} A \\ x \\ \hline B \\ (1500-x) \end{array}$$

$$12\% x + 14\%(1500-x) = 186$$

$$12\% x + 210 - 14\% x$$

$$2\% x = 24$$

2x = 24

$$2\% x \longrightarrow 24$$

$$100\% x \longrightarrow ? \quad \boxed{1200}$$

$$S = 1400$$

$$@ 5\% \text{ pa.}$$

S + (more)

If Samir

Sumil ka ki

100

3 years

A su

equal

be 20.

each in

[66]

$$S = 1400 \quad A$$

@ 5% p.a. for 3y.

$$S + \text{more}$$

Sunil.

for 3y.

@ 7% p.a. at  
SI.

$$\text{If Samir} = 210.$$

Sunil ko kitna diya.

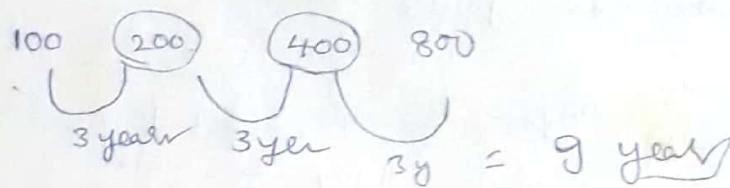
for 3 yr.

$$21\% [1400 + x] - 15\% [1400] = 210$$

$$x = 600$$

$$\begin{aligned} 21\% &= 126 \\ 100\% &=? \end{aligned}$$

$$1400 + x = 1400 + 600 \\ \underline{\underline{x = 200}}$$



Q. A sum of Rs 550 is to be repaid in two equal installments. If the rate of interest be 20% compounded annually, then the value of each installment is :

$$P. \quad 550 + 110 = 660.$$

$$[660 - x] + 20\% \overset{\uparrow}{[660 - x]} = x$$

'x'

Rate \* Consumption = Expended.

$$100 * 10. = 1000.$$

$$132 * ? = 1100$$

Q If

2\*

## Work, Time & Day

Shiva  
6

Shankar  
9

① if they work together how many days are required to complete the work.

② work alternatively (Shiva  
Shankar)

③ Shiva & shankar worked per 2<sup>nd</sup> days  
after 2<sup>nd</sup> days shiva left.

④ shiva started work after 2 days,  
Shankar joined him.

Solu<sup>n</sup>

$$\begin{array}{r} 6 \\ 9 \end{array} \rightarrow \begin{array}{l} 3 \text{ unit} \\ 2 \text{ "} \\ \hline 5 \end{array}$$

$$\text{Days} = \frac{10}{5} \Rightarrow 3\left(\frac{3}{5}\right) \text{ days.}$$

$$1 \text{ day} \rightarrow 5 \text{ unit}$$

$$? \rightarrow 18 \text{ unit}$$

$$\begin{array}{ccccccc} 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ 2 & 3 & 2 & 3 & 2 & 3 & 2 \end{array} \rightarrow \begin{array}{c} 1 \\ 2 \\ 3 \\ 4 \\ 5 \\ 6 \\ 7 \end{array}$$

8<sup>th</sup> day shiva → 3 unit

but 1 remains

$$80 \rightarrow \frac{1}{3} \text{ day.}$$

$$\text{Total } \left(7 + \frac{1}{3}\right) \text{ day.}$$

② If shiva starts work Int.

$$\begin{array}{r} 6 \\ 9 \end{array} \rightarrow 15$$

6	9
1	2
0	3
0	2
5	5
4	3
7	7

remaining 8 unit completed

③  $(5 + 5) \rightarrow 2 \text{ days} - 10 \text{ unit.}$

by shankar.  $\frac{8}{2} \Rightarrow 4 \text{ day}$  Total days = 6 days.

Extra days taken by shankar = 4 day

④ 6 unit → 2 day

$$\begin{array}{r} 1 \\ ? \end{array} \rightarrow \begin{array}{l} 5 \text{ unit} \\ 12 \text{ unit} \end{array}$$

12 unit remaining  $\rightarrow \frac{12}{5} \Rightarrow 2\left(\frac{1}{5}\right) \Rightarrow 4\left(\frac{1}{5}\right) \text{ days}$

If shankar starts -

$$6 \text{ day} \rightarrow 15 \text{ unit}$$

$$1 \text{ day} \rightarrow 2$$

$$\frac{1}{3} \rightarrow 1$$

$$\frac{7}{3} \rightarrow \frac{18}{2} =$$

s.c.

⑤ 2 day → 5 day unit  
? → 15 day (multiple of 5)

6 day → 15 unit

1 day → 3 unit

7 day → 18 unit

1 lt →

Q3 If Shiva do remaining work ~

$$2+5 = \frac{10}{8}$$

1 day?  $\rightarrow 3 \text{ unit}$   
 $\rightarrow 8 \text{ unit}$

 $T = \frac{8}{3} = 2\frac{2}{3}$   
 $\text{Total} = 2 + \frac{2}{3} = 4\frac{2}{3}$

OR

$$\begin{array}{r} 6 \\ 3 \\ \hline \text{set } x \\ \text{work } 3x \end{array} \quad \begin{array}{r} 9 \\ 2 \\ \hline 4 \\ = 18. \end{array}$$

$$x = 4\frac{2}{3} \text{ Total days.}$$

$$\text{remaining days} - 4\frac{2}{3} - 2 = 2\frac{2}{3}$$

If Shambu do work & Shiva left after 2 days.  
 Shiva start.

$$\begin{array}{r} 3 \\ 2 \\ \hline 6 \\ + 2x = 18. \end{array}$$

$$\begin{array}{r} 2x = 12 \\ x = 6 \end{array} \text{ total days}$$

$$\text{Remaining days required by Shambu } 6 - 2 = 4 \text{ days}$$

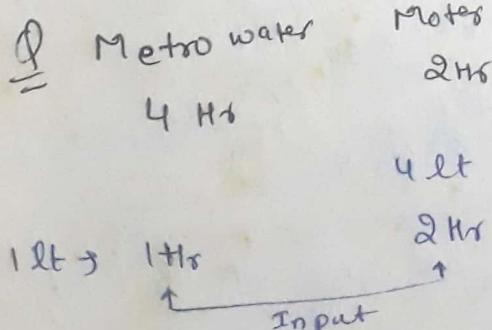
Q4  $\begin{array}{r} a \\ 3 \\ x \\ \hline \end{array}$   $\begin{array}{r} 8 \\ 2 \\ (x-2) \\ \hline \end{array}$  unit.

$$3x + 2(x-2) = 18$$

$$\begin{array}{r} 5x = 14 \\ x = 2\left(\frac{4}{5}\right) \end{array} \text{ total days.}$$

1st  $2 \times 3 = \frac{18}{12}$   
 1 day  $\rightarrow 5 \text{ unit}$   
 ?  $\rightarrow 12 \text{ units.}$

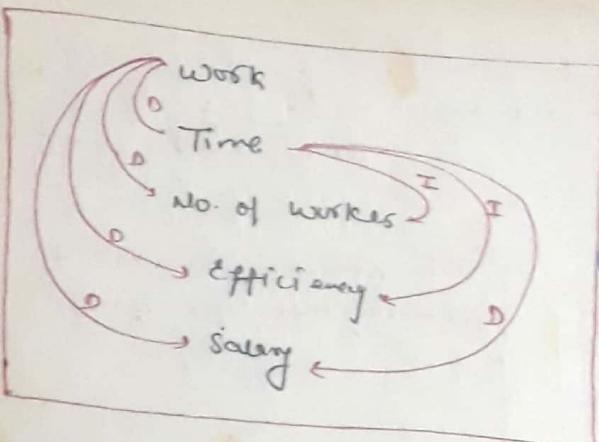
$$\frac{12}{5} = 2\left(\frac{2}{5}\right) \text{ Ans.}$$



Leakage  
 1 Hrs.

$-4 \text{ Hrs}$   
 0 Hrs.

$1 \rightarrow 4 \rightarrow 2$   
 $2 \rightarrow 4 \rightarrow 1$   
 $3 \rightarrow 4 \rightarrow -1$   
 Cut off taken in 4 Hrs



Always check the relations

$$\textcircled{5} \quad A = 40 \text{ d.} \quad B = 30 \text{ d.}$$

$$3(10) + 4(10) + C(10) = 120.$$

$$30 + 40 + C(10) = 120.$$

$$C(10) = 50$$

Result

$$10 \text{ day } C = 10$$

$$\text{Cap} = 15$$

$$( \Rightarrow 24 )$$

$$24 \text{ day } \rightarrow 120 \text{ unit}$$

$$1 \text{ day } \rightarrow 5 \text{ unit}$$

$$? = 24$$

$$\textcircled{6} \quad A + B = 40 \text{ d.} \quad \left\{ \begin{array}{l} B = 2C \\ A + C = 60 \text{ d.} \end{array} \right.$$

$$B/C = 2 \Rightarrow 2C - C = 20$$

$$\boxed{C = 20}$$

$$40 > 120 \quad \frac{3}{2}$$

$$A + B = 3 \quad B = 2C$$

$$A + B = 2$$

$$\boxed{C = 1}$$

$$1 \text{ unit } \rightarrow 1 \text{ day}$$

$$120 \text{ unit } \rightarrow ?$$

$$\boxed{120} \approx$$

$$\textcircled{7} \quad A = 3B$$

$$B = 2C$$

$$A + B + C = 12$$

$$6C + 2C + C = 12$$

$$9C \rightarrow 12$$

$$4C = 12$$

$$C = 3$$

$$1C = 12 \times 3 = 36 \quad \boxed{36} \quad \text{Q. 17 Q. 18}$$

$$A = 2 \quad B = 3x \quad C = 2x$$

$$C \rightarrow 3 \text{ unit in 1 day.} \quad 6 \text{ unit in 2 day.}$$

$$\textcircled{8} \quad A = 3B \quad A = (B - 60)$$

$$AC = (B - 60) \quad 3B = B$$

$$0(A - 60) = B$$

$$2B = 60 \quad B = 30$$

$$A = 60 \quad \frac{60}{2} = 30$$

$$\frac{80}{4} = 20$$

$$\textcircled{9} \quad A = 3B, \quad A = B - 60$$

$$A \quad B \quad 2n = 60$$

$$x \quad 3x \quad n = 30$$

$$30 \quad 90 \quad 3n = 90$$

$$3 \quad 1 \quad 1 \rightarrow 4$$

$$? \rightarrow 90$$

$$? = 22$$

$$\textcircled{10} \quad A + B = 80$$

$$B + C = 60$$

$$A + C = 120$$

$$A + B + C = ?$$

$$2(A + B + C) =$$

$$(A + B + C) =$$

$$\textcircled{11} \quad A = 8$$

$$B = 10$$

$$C = 12$$

$$3 \text{ day } \rightarrow ?$$

$$\text{Ansatz } ?$$

$$9 \text{ days.} +$$

$$9 \left(\frac{3}{5}\right) =$$

$$P =$$

$$Q =$$

$$7x$$

$$3 \text{ unit}$$

$$24 \text{ unit}$$

$$13 \times$$

$$\times 3$$

$$399$$

$$\textcircled{12} \quad A = ?$$

$$B = ?$$

check the

$$\begin{aligned} & \rightarrow 12x^3 \\ & 4 \\ & 10) + C(10) \approx 120 \\ & = 80 \end{aligned}$$

$$\begin{aligned} 10 \text{ day } c &= 10 \\ \text{Cap} &= 4 \text{ t} \end{aligned}$$

$$10 \text{ days} \rightarrow 50 \text{ kmt}$$

$$\begin{aligned} ? &\rightarrow 120 \text{ kmt} \\ ? &= 24 \text{ t} \end{aligned}$$

$$A = (B - 60)$$

$$B = 3x$$

$$\begin{aligned} A &= 3x \\ B &= 8 \\ \therefore B &= 20 \end{aligned}$$

$$\begin{aligned} 1 \\ \frac{3}{4} \end{aligned}$$

$$A = B - 60$$

$$2n = 60$$

$$x = 30$$

$$3n = 90$$

$$\begin{aligned} \rightarrow 4 \\ \rightarrow 90 \end{aligned}$$

h

$$\begin{aligned} \textcircled{3} \quad A+B &= 8 \text{ d} \\ B+C &= 6 \text{ day} \\ A+C &= 12 \text{ d} \\ A+B+C &=? \end{aligned}$$

$$\begin{aligned} 2(A+B+C) &= 26 \\ (A+B+C) &= 13 \text{ d} \\ ? &= 9 \frac{1}{3} \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad A &= 8 \\ B &= 10 \\ C &= 12 \end{aligned}$$

$$\begin{array}{r} 30 \\ 240 \\ 20 \\ \hline 74 \end{array}$$

$$\begin{array}{r} 15 \\ 120 \\ 12 \\ \hline 10 \end{array}$$

$$3 \text{ day} \rightarrow 74 \times 3$$

$$A \text{ did} \rightarrow 9 \text{ day} \rightarrow 229$$

$$9 \text{ days} + \frac{1863}{30 \times 7} = 18 \text{ remain.}$$

$$9 \left( \frac{3}{5} \right) =$$

$$\textcircled{7} \quad P = 8 \text{ d.}$$

$$Q = 6 \text{ d.}$$

$$7 \times 3 \rightarrow 21$$

$$3 \text{ unit} \rightarrow R \cdot \text{did.}$$

$$24 \text{ unit} \rightarrow \frac{1600}{24} = 66 \frac{2}{3}$$

$$(133 \cdot 3) \times 3 = 399.99$$

$$\frac{133 \cdot 3}{24} = 133.33$$

$$\frac{133.33}{24} = 5.55$$

$$\frac{133.33}{24} = 5.55$$

$$\begin{aligned} \textcircled{8} \quad A+B &= 12 \\ B+C &= 16 \\ A+C &= 13 \text{ d.} \end{aligned}$$

$$A = 5 \text{ d.} \quad C = 7 \text{ d.} \quad A+2B+C = 7 \text{ unit.}$$

$$4 \times 5 + 2 \times 3 \times 7 + 13 = 7$$

$$20 + 42 + 13 = 7 \times 48$$

$$62 + 13 =$$

$$\textcircled{8} \quad A+B = 12$$

$$4 \quad 3$$

$$8+C = 16$$

$$4 \quad 3$$

$$5 \times 4 = 20$$

$$2 \times 3 = -6$$

$$28$$

$$A = 5 \quad \{ 5$$

$$B = 7 \quad \{ 2$$

$$C = 13 \quad \{ 11$$

$$11 \text{ d} \rightarrow 22 \text{ unit.}$$

$$? \rightarrow 48 \text{ unit}$$

$$\boxed{? = 24 \text{ d.}}$$

$$\textcircled{9} \quad 12 \text{ M, 9 D.}$$

$$\text{Chain Rule } 6 \text{ d, } (6+12)$$

$$\boxed{\frac{M_1 D_1 T_1}{w_1} = \frac{M_2 D_2 T_2}{w_2}}$$

$$12 \times 9 = 108$$

$$12 \times 6 = -72$$

$$36.$$

$$10 \rightarrow 18 \text{ unit.}$$

$$? \rightarrow 36 \text{ unit}$$

$$\boxed{? = 2}$$

100118

$$\begin{aligned} m &= 12 \quad T = 0H \quad D = 10 \\ 16m & \quad D = 9 \quad T = ? \end{aligned}$$

$$12 \times 8 \times 10 = 16 \times 9 \times T$$

$$T = 12H$$

$$\begin{aligned} (13) \quad 5M + 6B &= 100H \\ 4M + 3B &= 60. \\ 3M + 6B &=? \end{aligned}$$

lameo

$$20M + 24B = 24M + 18B.$$

$$(11) \quad M = 5 \quad 60kg \quad D = 3 \\ kg = ? \quad m = 8 \quad D = 5$$

$$\frac{8 \times 3}{60 \times 20} = \frac{8 \times 5}{?}$$

$$? = 160 \text{ kg.}$$

$$\begin{aligned} (12) \quad 24 = M & \quad D = 16 \\ 8 = m & \quad D = 72. \\ 24 = CM & \quad D = 32 \end{aligned}$$

$$\frac{36}{7} \Rightarrow 5\left(\frac{1}{7}\right)$$

$$\begin{aligned} Q &= \cancel{\frac{7 \times 4}{4}} \Rightarrow \cancel{\frac{Q}{4}} \rightarrow \cancel{\frac{Q}{4}} \\ &= \cancel{\frac{P+Q}{4}} \Rightarrow \cancel{\frac{Q}{4}} \rightarrow \cancel{\frac{Q}{4}} \end{aligned}$$

$$\begin{aligned} 3M + 4M &= 7M. \rightarrow ? \\ 9M &\rightarrow 4D. \end{aligned}$$

$$(14) \quad P = (Q + R)$$

$$\begin{aligned} \cancel{\frac{P+Q}{15}} & \Rightarrow \cancel{\frac{Q}{60}} \quad Q \\ 15 & \quad 60 \quad ? \end{aligned}$$

$$15P + 15Q = 60R - 15Q.$$

$$15P = 60R - 15Q.$$

$$10M = \frac{16 \times 24}{15} + \frac{24 \times 9}{15} + \frac{32 \times 25}{15} = 15Q + 15R = 60R - 15Q.$$

$$80Q = \frac{75R}{25}.$$

$$\Rightarrow \frac{192}{5} + \frac{192}{5} + 32 = 100 = 2R.$$

$$\frac{192 \times 2}{5} + \frac{192 \times 5}{5} = \frac{384 + 160}{5}$$

$$\Rightarrow \cancel{\frac{544}{5}} \Rightarrow \boxed{108\left(\frac{4}{5}\right)}$$

$$\begin{aligned} \frac{1}{P} &= \frac{1}{Q} + \frac{1}{R} \quad \frac{1}{15} - \frac{1}{Q} = \frac{1}{60} \\ \frac{1}{R} &= \frac{1}{60} \quad \frac{1}{15} - \frac{1}{R} = \frac{2}{60} \\ \frac{1}{Q} &= \frac{2}{60} \quad \frac{1}{15} - \frac{1}{Q} = \frac{2}{60} \end{aligned}$$

$$24M \times 16 = 24C \times 32 \Rightarrow \boxed{1M = 2C}$$

$$\begin{aligned} 20C + 20C + 24C &=? \quad \begin{cases} 64 \times 32 \times 4 \\ 24C \rightarrow ? \end{cases} \quad ? = \frac{64 \times 32 \times 4}{24C} \Rightarrow \frac{256}{3} \approx 85\left(\frac{1}{3}\right) \\ 80C + 72C &= 24C + 32 \end{aligned}$$

$$\boxed{Q = 40}$$

$$\begin{array}{ccc} 23 & A & B & C \\ & 6 & 9 & 12 \\ & \swarrow & | & \searrow \\ 6 & & 36 & \\ & \swarrow & | & \searrow \\ 6 & 4 & 3 & = 13 \\ \text{Hrs} & \text{Hrs} & \text{Hrs} & \end{array}$$

Ques 23

$$13 \text{ Hrs} \rightarrow 36$$

$$2 \text{ Hrs} \rightarrow 26$$

$$\left\{ \begin{array}{l} ? = 6 \text{ Hrs} \\ 6 \text{ Hrs} \\ 1 \text{ Hr} \rightarrow 6 \text{ Hrs} \\ 1 \text{ Hr} \rightarrow 4 \\ 8 \rightarrow 36. \end{array} \right.$$

$$\begin{array}{ccc} 22 & A & B & C \\ & 20 & 30 & -60 \\ & \swarrow & | & \searrow \\ 3 & & 60 \text{ lt} & \\ & \swarrow & | & \searrow \\ 1 & 2 & f_1 \Rightarrow 4 & \end{array}$$

$$3 \text{ min} \rightarrow 4 \text{ lt}$$

$$4 \text{ lts} \rightarrow 18 \text{ min} + 1 \text{ lt}$$

$$? \rightarrow 60 \text{ min.}$$

$$\begin{array}{l} 16 \text{ mint. } 3 \text{ mint} \rightarrow 4 \text{ lt. } \\ 14 \text{ cycle} * 3 = (42 \text{ mint}) \\ 14'' * 4 = 56 \text{ lt} \end{array}$$

$$\begin{array}{l} 42 \text{ m} \rightarrow 56 \text{ lt} \\ 1 \text{ m.} \rightarrow 3 \\ 2 \rightarrow 1 \\ 13 \frac{1}{2} = 58 \frac{1}{2} - 1 \\ 53 - 2 \end{array}$$

$$23 \quad F_1 \quad f_2 \quad f_3 \quad \text{or}$$

$$\begin{array}{cccc} 12 & 15 & 20 & 54 \\ & | & & | \\ & 60 \text{ lt.} & & 53 \\ & | & & | \\ 5 & 1 & 3 & 53 \\ & | & & | \\ & 4 & & 53 \\ & & & | \\ & & & 54 \end{array}$$

$$2 \text{ Hrs} \rightarrow 17 \text{ lt.}$$

$$6 \text{ Hrs} \rightarrow 51 \text{ lt.}$$

$$14 \text{ Hrs} \rightarrow ?$$

$$\frac{74}{60}$$

$$24 \quad A + B + C$$

$$8 \text{ Hrs}$$

$$(A + B + C) \rightarrow + 206 \text{ Hrs} \quad ?(A + B)$$

$$25 \rightarrow 2 \text{ Hrs}$$

$$100 \rightarrow 0 \text{ Hrs.}$$

$$3 \cdot 75 \rightarrow 9$$

$$4 \cdot 100 \rightarrow ?$$

$$? = 12$$

$$24 \text{ lt}$$

$$(A + B + C)$$

$$C = 14$$

$$f_1 = 4 f_2$$

$$f_1 = f_2$$

$$1 : 4$$

$$36 \text{ Hrs.}$$

$$f_1 + f_2$$

$$5 \rightarrow 36.$$

$$1 \text{ pip} \rightarrow ?$$

$$1 \text{ pipe} = 180.$$

Ques 24

1 Monkey can eat 1 coco. In 10 mint. How much time is require for 10 Monkey to eat 10 coco. Ans 10 mint.

Ques 25

A rat travels 4 mt in 1 mint. in the next mint it sleeps 3 mint. How much time require for a rat to climb a tree of 20 mt. 1 mint  $\rightarrow$  4 unit. 1 unit  $\rightarrow$  3 m. 2 m  $\rightarrow$  1 m. 1 m  $\rightarrow$  3 m.  $\frac{20}{4} \rightarrow \frac{5}{1} \rightarrow 15$

$$\begin{array}{c} 1 \text{ min} \rightarrow 1 \text{ min} \\ | \\ 16 \text{ min} \\ | \\ 2 \text{ min} \rightarrow 1 \text{ min} \\ ? \rightarrow 16 \text{ min} \\ ? = 32 \text{ min} \end{array}$$

$$33 \text{ min}$$

9/08/18

## Time & Distance

$$\text{speed} = \frac{D}{t} \quad \text{unit} - \text{m/sec. km/hr} \quad \text{Mph}$$

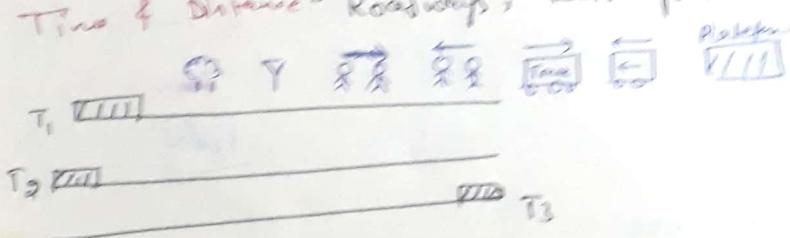
$$1 \text{ km/hr} = \frac{5}{18} \text{ m/sec.} \quad \frac{m}{sec} = \frac{18}{5} \text{ km/hr.}$$

$$\text{Avg speed} = \frac{\text{Total distance}}{\text{Total time taken.}}$$

$$\text{Relative speed for the same direction} = |S_1 - S_2|$$

$$\text{Relative speed for opp direction} = |S_1 + S_2|$$

Time & Distance - Roadways, Railways, waterways.



$$\Rightarrow S = \frac{D}{t}, \quad t_c = \text{crossing time}$$

$$\textcircled{1} = \frac{L_t}{S_t} = t_c$$

$$\text{(i) } \frac{L_t + L_p}{S_t} = t_c$$

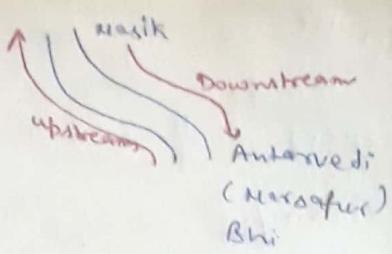
$$\textcircled{2} \quad \left[ \frac{L_t}{(S_t - S_{pn})} \right]_{\text{min}} = t_c$$

$$\text{(ii) } \frac{L_{t1} + L_{t2}}{|S_{t1} - S_{t2}|} = t_c$$

$$\textcircled{3} \quad \frac{L_t}{S_t + S_{pn}} = t_c$$

$$\text{(iii) } \left( \frac{L_{t1} + L_{t2}}{S_{t1} + S_{t2}} \right) = t_c$$

- Speed of Man or Boat =  $M$
- Speed of stream or current =  $S$
- Downstream speed =  $M + S$
- Upstream speed =  $M - S$



Q1 Q2  
1 hr 2 hrs  
when they meet

Q3

Q3

IT

1 hr  
10 km  
10 km  
20 km

Q4

H.

f2st

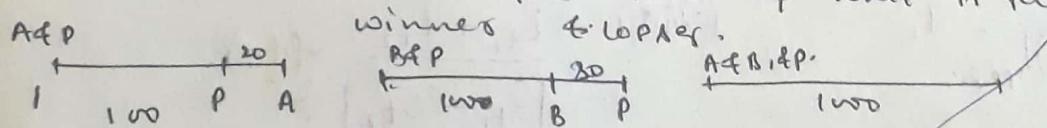
Q In 100 mt race b/w N & M, M won the race by 10 mt or 5 sec, how much time is required for N to cover 1 km.

$$\begin{aligned} \cancel{10 \text{ mt} \rightarrow 5 \text{ sec.}} \quad & \Rightarrow 500 \text{ feet.} = \frac{100}{M} \text{ m.} \\ \cancel{\text{100 mt} \rightarrow ?} \quad & \cancel{? = \frac{6.11}{55 \times 100} \Rightarrow 61/8 \text{ sec.}} \\ \cancel{90 \text{ mt} = 55 \text{ sec.}} \quad & ? = \cancel{61/8 \text{ sec.}} \\ \cancel{\text{100 mt} = ?} \quad & \end{aligned}$$

M

10 mt	$\rightarrow$	5 sec.	N
100 mt	$\rightarrow$	! (50 sec.)	45 sec. $\rightarrow$ 100 mt
			? $\rightarrow$ 100 mt
$\boxed{? = 450 \text{ sec.}}$			

Q In 100 mt race b/w A & P, A won the race by 20 mt, 100 mt race b/w P & B, P won the competition by 20 mt, In IT's competitions b/w A, P & B who will win the race of what is the distance b/w



$$\begin{aligned} P &= 20 \\ A : P &= (100 : 80) + 10 \\ A : B &= (100 : 80) \times 8 \\ A : P : B &= 100 : 800 : 640 \Rightarrow 360. \end{aligned}$$

A will  $\frac{100}{360} = \frac{5}{18}$  km

Q8

Q1 A  $\rightarrow$  36 kmph. B  $\rightarrow$  42 kmph. 1 Hr  $\rightarrow$  6 km  
 $? \rightarrow 48 \text{ km.}$   
 $? = 8 \text{ Hrs.}$

$$\frac{36}{8} + \frac{48}{8} = \boxed{6.24}$$

Ques. (Ques. 2)

1 km per 5 min

$$\text{walking speed} = \frac{1 \text{ km}}{5 \text{ min}} = 0.2 \text{ km/min}$$

Ques. 3



$$R_1 = 20 \text{ m}$$

$$R_2 = 30 \text{ m}$$

$$R_3 = 40 \text{ m}$$

$$\begin{aligned} \text{Time} &= \frac{\text{Distance}}{\text{Speed}} \\ T_1 &= \frac{2\pi R_1}{0.2} = \frac{2\pi \times 20}{0.2} = 628 \text{ min} \\ T_2 &= \frac{2\pi R_2}{0.2} = \frac{2\pi \times 30}{0.2} = 942 \text{ min} \\ T_3 &= \frac{2\pi R_3}{0.2} = \frac{2\pi \times 40}{0.2} = 1257 \text{ min} \end{aligned}$$

$$\begin{array}{r} (a) 1 \text{ min} \\ (b) 2.5 \text{ min} \\ (c) 10 \text{ min} \end{array}$$

6000... min

Ques. 4

$$\text{Inj. speed} = 10 \text{ km/hr.}$$

$$\text{Inj. speed} = 14 \text{ km/hr.}$$

$$14 \times 5 = 70.$$

- 20

$$\boxed{50}$$

km

Walking distance  $\approx 10 - 4 \text{ km} \leftarrow 1 \text{ hr.}$

Actual distance  $20 \text{ km} \leftarrow ?$

5 hr

Ques. 5

$$\frac{2x+10}{10} \text{ hr.}$$

$$\frac{5}{2x+10} \text{ hr.}$$

$$F = 3x +$$

$$5 \text{ km} \rightarrow 5 \text{ hr.}$$

$$\begin{aligned} H &= 15 \text{ km} \\ D &= 10 \text{ km} \end{aligned}$$

$$\text{DR} * \frac{S_1 : S_2}{T_1 : T_2} = 3 : 2$$

$$T_1 : T_2 = 2 : 3$$

SAT

$$\begin{array}{l} 5 \text{ hr} \\ x(3x+10) \end{array}$$

$$2x(5-x)$$

$$\begin{array}{l} 3x = 10 - 2x \\ 5x = 10 \\ x = 2 \end{array}$$

$$2 \times 3 = 6.$$

$$\begin{array}{l} 10 \text{ km} \\ 10 \text{ hr.} \end{array}$$

8 km/hr.  $\rightarrow$  foot, 16 km/hr.  $\rightarrow$  bicycle.

$$S \times t = D$$

$$\begin{array}{l} 8 \times 8t = 64t \\ 16 \times (8-t) = 128 - 16t \end{array}$$

$$\begin{array}{l} 64t \\ - 16t \\ \hline 48t \end{array}$$

$$8t + 16(8-t) = 48 \Rightarrow 8t = 48 \Rightarrow t = 6$$

$$8t = 8 \times 6 = \boxed{48 \text{ km}}$$

Q 10/08/18

Speed of bus without stoppage = 60 kmph.  $\{ 15 \text{ kmph/w}$   
" " with " = 45 kmph

What is the stoppage time of bus.

60 min  $\rightarrow$  60 km.

?  $\rightarrow$  15 km

$$\boxed{\text{?} = 15 \text{ min.}}$$

Let without with

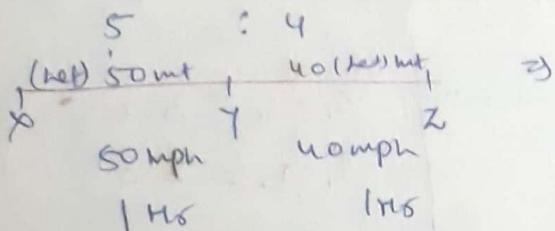
45  $\rightarrow$  36.

60 min  $\rightarrow$  45 km.

?  $\rightarrow$  9 km

Q 6

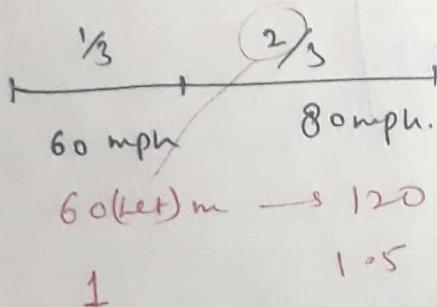
$$A.S = \frac{\text{Total Distance}}{\text{Total time.}}$$



$$\frac{\text{Total Dist}}{\text{Total time}} = \frac{40 + 50}{1 + 1} = \frac{90}{2}$$

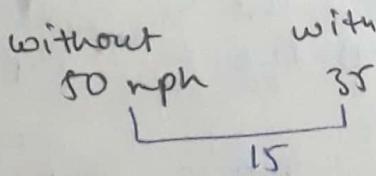
$$\Rightarrow \boxed{45 \text{ mph.}}$$

Q 7



$$\Rightarrow \frac{120}{2.5} = \boxed{72} \text{ min.}$$

Q 8



$$60 \text{ min} \rightarrow 80 \\ ? \rightarrow 18 \\ \boxed{\text{?} = 18 \text{ min.}}$$

Q 9

25 km/hr.  
15 min break.

30 km/hr  $\{$  D. is constant  
5 min early  $\rightarrow$  ~~20-1~~  
 $11:40 - 11:45 = 12:00$

$$\boxed{\frac{20}{60} \text{ hr} = \frac{1}{25} - \frac{1}{30}}$$

$$\boxed{\frac{1}{3} = \frac{1}{25} - \frac{1}{30}}$$

$$\frac{1}{3} = \frac{1}{25} - \frac{1}{30}$$

15 kmph  
 36.  
 45 kmph.  
 9 km  
 $\frac{750}{41} = \frac{90}{2}$

10 min  $\rightarrow$  12 min  
 5 km/hour  
 7 min late  
 6 km/hr  
 5 min early.  
 $\frac{1}{2} \rightarrow \frac{1}{3} \Rightarrow 12 \text{ min}$

11  
 10  
 When police will catch the thief  
 what is distance b/w them after 6 min.

$\frac{12}{60} = \frac{d}{5} - \frac{d}{6} \Rightarrow \frac{d}{30} = \boxed{6}$   
 $\frac{1}{2} \rightarrow \frac{1}{3} \Rightarrow 12 \text{ min}$

8  
 11  
 $\frac{6}{60} \text{ hr} \rightarrow ?$   
 $? = \frac{60}{60} = 1 \text{ km.}$   
 $0.1 \text{ km} = 100 \text{ m}$   
 $1.3 \rightarrow 1.1 \rightarrow \boxed{200}$

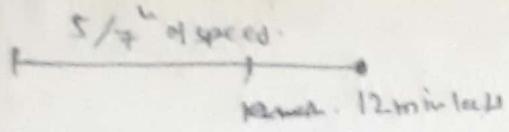
60 min  $\rightarrow$  100 mts  
 6 min  $\rightarrow$  ? (100)  $\rightarrow$   
 $? \rightarrow 300$   
 $\boxed{? = 10} \approx$

300  
 -100  
 200 m

12  
 $\frac{60 \text{ min}}{10 \text{ kmph}} = \frac{1 \text{ pm}}{2 \text{ pm}}$   
 $15 \text{ kmph} \rightarrow \frac{1}{12 \text{ pm}}$   
 $2 \text{ hrs} \rightarrow 5 \text{ kmphs.}$   
 $\frac{2}{10} \text{ hrs} \rightarrow ?$   
 $2 \text{ hrs} = \frac{d}{10} - \frac{d}{15} \Rightarrow \frac{8d}{30} = 2 \text{ hrs} \Rightarrow d = 60 \text{ km}$

$15 \text{ km} \rightarrow 12 \text{ PM}$   
 $5 \text{ hrs} \left\{ \begin{array}{l} 8 \text{ AM} \\ 1 \text{ PM} \end{array} \right\} \rightarrow \frac{60 \text{ (distance)}}{5 \text{ (time)}} = 12 \text{ kmph}$

Q 13



$$D = xt = \frac{5}{7}x(t + \frac{12}{60})$$

$$t = \frac{5}{7}t + \frac{12}{60}$$

$$\frac{2}{7}t = \frac{12}{60} \Rightarrow t = \frac{42}{7} = 6 \text{ min} \rightarrow 42 \text{ min}$$

$$t = 42$$

$$\frac{5}{7} \rightarrow 12 \text{ min late}$$

$$2 \rightarrow 12$$

$$5 \rightarrow ?30 \rightarrow \text{usual}$$

$$7 \rightarrow ?42 \rightarrow \text{today.}$$

$$\frac{7}{5} \rightarrow 12 \text{ min early}$$

$$2 \rightarrow 12$$

$$7 \rightarrow 42 \rightarrow \text{usual}$$

$$5 \rightarrow 30 \rightarrow \text{today.}$$

$$\frac{N}{D} = \begin{cases} \text{usual} \\ \text{Today.} \end{cases}$$

If speed =  $x$ ,  $D = xt$

$$x \rightarrow D$$

$$\frac{5}{7}x(t + \frac{12}{60}) = D$$

Q 16

Ric

Q 14

$$\frac{D}{6 \text{ hrs}}$$

$$W + R = 6$$

$$R + R = 4$$

$$W + W = 8$$

Q 15

$$S = d/t$$

$$t = d/S$$

Time to cross each other  
in opp. dirn

$$= \frac{(L_{t_1} + L_{t_2})}{S_{t_1} + S_{t_2}}$$

$$L_{t_1} = 180 \quad \frac{180 + 120}{20}$$

$$L_{t_2} = 150 \quad \frac{120 + 150}{20} = 15$$

$$S_{t_1} = 15 \text{ m/s}$$

$$S_{t_2} = 15 \text{ m/s}$$

$$\frac{330}{30} = 11$$

(16)  $L_1 = 130 \text{ mt} \quad P_t = 200. \quad t_1 = 7 \text{ sec.} \quad S_{t_1} = \frac{350}{7} = 50$   
 $\text{Bridge} = \text{bridge} = 150 \text{ mt} \rightarrow \text{Time?}$

$$\frac{350 + 150}{50} = \frac{14}{\frac{700}{50}} = \frac{50}{50}$$

Ric  $350 \text{ mt} \rightarrow ? \text{ sec}$

14 sec

$700 \text{ mt} \rightarrow ? \text{ (14) } \underline{\underline{m}}$

(17)  $L_1 = 130 \quad S_{t_1} = 450 \text{ km/hr.}$   $\frac{130 + \text{Bridge}}{450} = 30$   
 $\text{bridge} = ? \quad T = 30 \text{ sec.}$

$S = d/t$

$t = d/S$

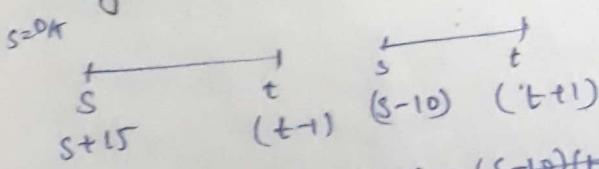
$27 = \left(\frac{L_t}{40}\right) \times \frac{18}{5}$

$t + t = 300$

$130 + \text{Bridge} = \frac{1350}{450}$

$\text{Bri} = \frac{1350}{130}$

Q If a person goes with usual speed by 15 km/hr, he reaches his destination one hr earlier than usual time. If he goes with speed by 10 km/hr, he will be late by one hr. The distance travel by him —?



~~$S(t) = (S+15)(t-1) = (S-10)(t+1)$~~

$S(S+15) = \frac{D(15)}{1} \quad \text{①} \quad S(S-10) = \frac{D(10)}{1} \quad \text{②}$

$S(S+15) = \frac{D(15)}{1} \quad \text{①} \quad S(S-10) = \frac{D(10)}{1} \quad \text{②}$

①/②  $\frac{S+15}{S-10} = \frac{15}{10} \Rightarrow 25 + 30 = 35 - 30$   
 $D = 300 \text{ km}$

Q A man when goes with speed from 24 km/hr to 30 km/hr. He takes 5 hr less than the usual time to cover a certain dist. What is distance usually covered by a man.

M1

$$C = D/T$$

$$S = 24 \text{ km/hr}$$

$$T_1 = D/24 \text{ (usual time)}$$

$$S = 30 \text{ km/hr}$$

$$T_2 = D/30 \text{ (speed up)}$$

$$T_1 = T_2 + 1$$

$$\Rightarrow D = 120$$

M2

$$S = 24 \frac{D}{t}$$

$$S = 30 \frac{D}{t-1}$$

$$D = S \times t \quad D = St$$

$$D = 24t \quad D = 30(t-1) \quad t = 5 \text{ hr}$$

$$D = 24 \times 5 = 120 \text{ km}$$

M3

If two different speeds.

$$S_1 \times S_2 = \frac{D}{|T_1 - T_2|}$$

If two different times.

$$t_1 \times t_2 = \frac{D}{(S_1 - S_2)}$$

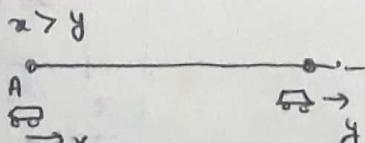
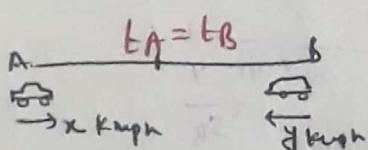
Q You arrive at your school 5 min late if you walk with speed of 4 km/hr but you arrive 10 mint before the scheduled time if you walk with of 5 km/hr. Distance b/w house & school.

$$t-10 \quad t \quad t+5 \quad t=15$$

$$4x + 5x = \frac{D}{15} \Rightarrow 5 \text{ km.}$$

### Meeting Point

time take by both body at meeting point always equal. if initial time is same.

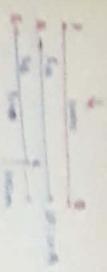


Meet  
 $t_A = t_B$

If initial time is not same, make same.



In case of train



In case of train moving  
at speed v  
Time taken by person to walk from front to back of train

Time taken by person to walk from front to back of train

Time taken by person to walk from front to back of train

- Q. A train running at 80 kmph takes 10 sec to cross a platform of 100 m. At what speed must the train run at a speed of 60 kmph to cross the same platform?

- Q. A person on train moves 10 m for journey of 100 m. If his speed is 10 m/s, what is his speed in platform? Given  $L = 100 \text{ m}$ ,  $v = 10 \text{ m/s}$

### Circular track race (4 types)

- Q. A man running will make more loops than the train. The time at time

Starting pt.  
Running pt.

Running will make more loops than the train

$$\frac{S_p}{S_t} = \frac{D_p}{D_t}$$

(S.K.D.)

$$\frac{S_p}{S_t} = \frac{T_p}{T_t}$$

(S.K.D.)

- Distance covered by train in time  $T$  is  $D_p = S_p T$

Distance covered by person in time  $T$  is  $D_t = S_t T$

Distance covered by person in time  $T$  is  $D_t = S_t T$

Distance covered by person in time  $T$  is  $D_t = S_t T$

Distance covered by person in time  $T$  is  $D_t = S_t T$

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Distance covered by person in time  $T$  is  $D_t = S_t T$

Distance covered by person in time  $T$  is  $D_t = S_t T$

Distance covered by person in time  $T$  is  $D_t = S_t T$

- Q. A man can walk up moving up

escalator in 10 sec. Time

man can walk down

moving up escalator in 10 sec.

Time man

walks

down escalator

time

walks

down

- Q. A man can walk up moving up

escalator in 10 sec. Time

man can walk down

moving up escalator in 10 sec.

Time man

walks

down escalator

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escalator in 10 sec. Time

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moving up escalator in 10 sec.

Time man

walks

down escalator

time

walks

down

- Q. A man can walk up moving up

escalator in 10 sec. Time

man can walk down

moving up escalator in 10 sec.

Time man

walks

down escalator

time

walks

down

- Q. A person in train moves 10 m

for journey of 100 m. His

speed is 10 m/s. What is his

speed in platform

Given  $L = 100 \text{ m}$ ,  $v = 10 \text{ m/s}$



$$\frac{D}{26} = \frac{24}{60}$$

$$D = \frac{4}{24} \times \frac{24}{60}$$

$$\Rightarrow 10.4 \text{ km}$$

or 60 min  $\rightarrow$  26 km  
24 min  $\rightarrow$  ? (10.4)  $\approx$

$$\frac{7.5 \text{ km}}{15 \text{ kmph}} = \frac{7.5 \text{ hr}}{?}$$

$$\frac{m+s}{2m} = \frac{5}{2m}$$

$$? = 3 \text{ hrs}$$

$$60 \text{ min} \rightarrow 15 \text{ km.}$$

$$60 \text{ min} \rightarrow ?(18)$$

$$\frac{m-s}{s+P_t} = \frac{9.5 - s}{1.5 + s} =$$

$$m-s = 18$$

$$m = 18 + 3 = 21$$

$$1 \text{ hr} \rightarrow 1.5 \text{ kmph.}$$

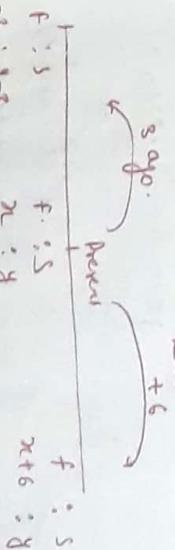
$$3 \text{ hrs} \rightarrow ?$$

$$? = 7.5$$

$$m+s = 6 \quad (6) \text{ km.}$$

$$m-s = 3$$

$$\frac{\text{Total distance}}{s+P_t} = \frac{6+6}{1+2} = \frac{12}{3} \quad (4)$$



$$(S+m) = 5 = 3 \text{ kmph. Total distance}$$

$$(S-m) = 1 \text{ hr} \rightarrow 1.5 \text{ kmph.}$$

$$\frac{45 \text{ km}}{S+m} = \frac{15 \text{ km}}{S-m}$$

$$3m - 9 = 2m + 6$$

$$m = 15 \text{ kmph}$$

$$m-s = 12-3 = 9$$

$$\frac{45}{15} = \frac{1.5}{1.5} \rightarrow 1 \text{ hr} \rightarrow 1.5 \text{ kmph.}$$

$$(m+s) = \frac{45}{3} = 15 \quad (S=5)$$

$$9 \text{ } 60 + 80 \boxed{140} \approx (m-s) = .$$

$$\frac{44x+20}{26} \rightarrow$$

M

P

"Age difference is always constant."

$$26 : ? \left[ \frac{2x+15}{3} \right] \quad (24) \text{ (+) future (after or hence) } = m+s$$

Present

= m

(-) Past (before or Ago) = m-s

Partnership  $\rightarrow$  profit rate = ratio of investment.

As per the ratio of "total Investment" divide profit  
of each partner to the investors in the business.

6 yrs hence a father age will be three times his son's age, & three  
yrs ago father was nine times as old as his son. What is the  
present age of father.

$$\begin{aligned} f : s & \quad f : s & \quad f : s \\ x-s : s-s & \quad x : y & \quad x+6 : y+6 \\ (x-s) = 9(y-s) & \quad \text{for Q. Q.} & \quad x+6 = 3(y+6) \\ x-s = 9y-s & \quad \frac{f}{s} = \frac{3y+6}{y+6} & \quad x = 3y+18-6 \\ x = 9y & \quad f = \frac{3y+6}{y+6} & \quad x = 3y+12 \quad (1) \\ 9y = 9 & \quad f = 3 \times 5 & \\ y = 1 & \quad f = 15 & \\ x = 9 & \quad \text{Ans.} & \end{aligned}$$

$$10 \times 10 = 100 \text{ m}^2$$

→ 30%  $\left\{ \begin{array}{l} \text{ad what value} \\ \text{will trip me} \end{array} \right.$   
 → 5%  $\left\{ \begin{array}{l} \text{what trip me} \\ \text{get truth.} \end{array} \right.$

$$\begin{array}{r}
 A = 5 \\
 C : 3 \\
 B \rightarrow ? \\
 ? = 150,000
 \end{array}
 \quad
 \begin{array}{l}
 4\% \text{ of profit} \\
 \frac{54000}{150000} \\
 \times 100 = ?
 \end{array}$$

(13)

$\begin{array}{r} 5 : 6 : 10 \\ \hline 20 \end{array}$	$\begin{array}{r} A : B \\ = 1 : 2 \\ + 1 : 3 \\ \hline 12 \end{array}$	$\begin{array}{r} 8 \times 0 \\ 4 : 3 : 5 \\ \hline 14 \end{array}$
--	---	---

$\frac{3}{33} + \frac{4}{43} = \frac{76}{760} = \frac{9}{33} = 330$

Q. If  $A = 1000$ ,  $B = 1500$ ,  $C = 2000$   
 $\frac{A}{B} = \frac{1000}{1500} = \frac{2}{3}$   
 $\frac{B}{C} = \frac{1500}{2000} = \frac{3}{4}$   
 $\frac{A}{C} = ?$

Ans:  $\frac{A}{C} = \frac{2}{3} \times \frac{3}{4} = \frac{1}{2}$   
 $\therefore A : C = 1 : 2$

Q. A invested  $\frac{1}{3}$  of the total money.  
 B invested  $\frac{1}{4}$  of the total money.  
 C invested  $\frac{1}{2}$  of the total money.  
 Total profit was  $\$400$ .  
 Find their individual shares.

Ans:  $\frac{1}{3} + \frac{1}{4} + \frac{1}{2} = \frac{10}{12} = \frac{5}{6}$   
 $\therefore \text{Total profit} = \$400$   
 $\therefore \text{Share of } A = \frac{1}{6} \times 400 = \$66\frac{2}{3}$   
 $\therefore \text{Share of } B = \frac{2}{6} \times 400 = \$133\frac{1}{3}$   
 $\therefore \text{Share of } C = \frac{3}{6} \times 400 = \$200$

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 $\therefore \text{Share of } C = \frac{3}{6} \times 400 = \$200$

$$\begin{array}{r}
 & 5 \\
 & \times 4 \\
 \hline
 & 20 \\
 \end{array}$$

x 8

$$\begin{array}{r}
 A : B \\
 4 : 5 \\
 \times 3 \\
 \hline
 12 \\
 \end{array}$$
  

$$\begin{array}{r}
 3 \\
 \times 7 \\
 \hline
 21 \\
 \end{array}$$
  

$$\begin{array}{r}
 15 \\
 \times 3 \\
 \hline
 45 \\
 \end{array}$$
  

$$\begin{array}{r}
 4 \\
 \times 7 \\
 \hline
 28 \\
 \end{array}$$
  

$$\begin{array}{r}
 1 \\
 \hline
 28 \\
 \end{array}$$
  

$$\begin{array}{r}
 33 + 43 = 76 \\
 76 - 33 = 43 \\
 43 - 33 = 10 \\
 10 - 10 = 0 \\
 \hline
 0 = 330
 \end{array}$$

$$1.6 \times 10^3 \text{ m}^3 \times 5 \times 10^3 \text{ N/m}^2 = 8 \times 10^6 \text{ N}$$

$$\text{Ans. } 8 \times 10^6 \text{ N}$$

$$\text{Ans. } 50$$

$$\text{Ans. } 10$$

$$\text{Ans. } 5$$

$$\text{Ans. } 25$$

$$\text{Ans. } 150$$

$$\text{Ans. } 14$$

$$\text{Ans. } 25$$

$$\text{Ans. } 10:11$$

$$\text{Ans. } 12$$

$$\text{Ans. } 10$$

$$\text{Ans. } 11:11$$

$$\text{Ans. } 12$$





Relatively → 60 min → 55 ms  
hour coincide at → 45 ms

$$\text{at } 0^\circ \text{ angle} - ? = \frac{60 \times 55}{55} = 540 = 41\left(\frac{1}{11}\right) \text{ ms}$$

$$\begin{array}{r} 120 \\ 21' \\ \hline 117' \end{array}$$

$$180$$

$$\begin{array}{r} 120 \\ 21' \\ \hline 99' \end{array}$$

$$\begin{array}{r} 120 \\ 21' \\ \hline 99' \end{array}$$

$$6$$

$$300 \text{ means } 5 \text{ ms gap}$$

$$60m \rightarrow 55ms$$

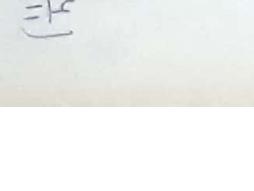
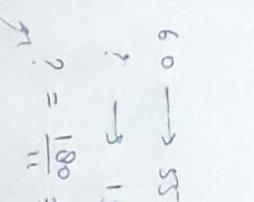
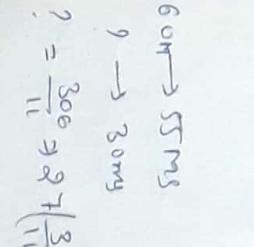
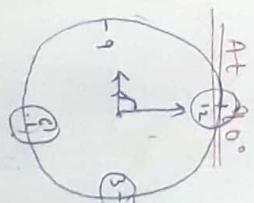
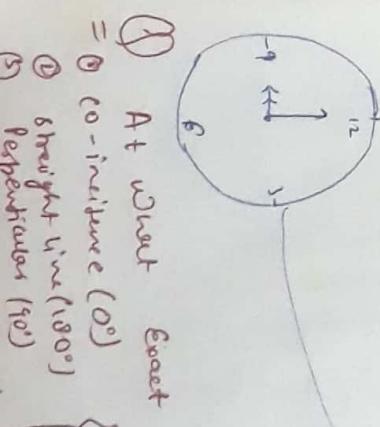
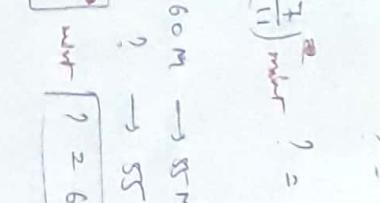
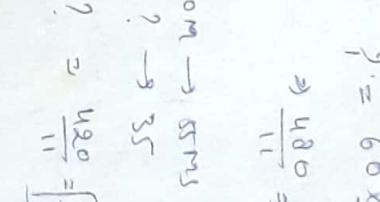
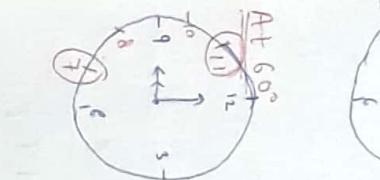
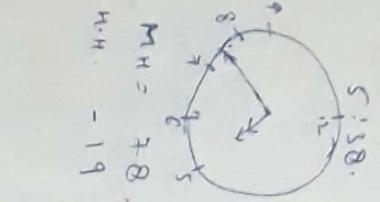
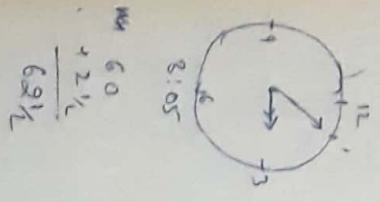
$$? \rightarrow 35$$

$$? \rightarrow 15$$

$$? = \frac{300}{11} = 27\left(\frac{3}{11}\right)$$

$$? = \frac{180}{11} = 16\left(\frac{4}{11}\right)$$

$$\boxed{\text{for reflex angle } = 360^\circ - (\text{angle})}$$



**Q** At what exact time do the  $mh$  &  $hh$  of clock  
co-incide ( $0^\circ$ ) { each other by  $7 + 8$   
straight line ( $180^\circ$ )  
perpendicular ( $90^\circ$ )}

$$\Rightarrow \frac{480}{11} = 43\left(\frac{7}{11}\right) \text{ min} \quad ? = 54\left(\frac{6}{11}\right) \text{ min.}$$

$$60m \rightarrow 55ms$$

$$60m \rightarrow 55ms$$

$$60 \rightarrow 55ms$$

$$? \rightarrow 35$$

$$? \rightarrow 55$$

$$? \rightarrow 15$$

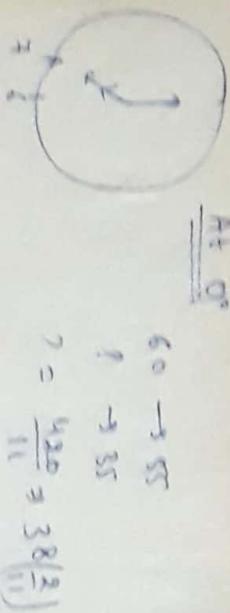
$$? = \frac{420}{11} = 38\frac{2}{11} \text{ min}$$

$$? = \frac{120}{11} = 10\frac{10}{11} \text{ min}$$

$$? = \frac{180}{11} = 16\left(\frac{4}{11}\right)$$

Q. At 6:00 am & 8:00 pm, hands may meet at  $0^\circ$ ,  $30^\circ$ ,  $60^\circ$  &  $90^\circ$ .

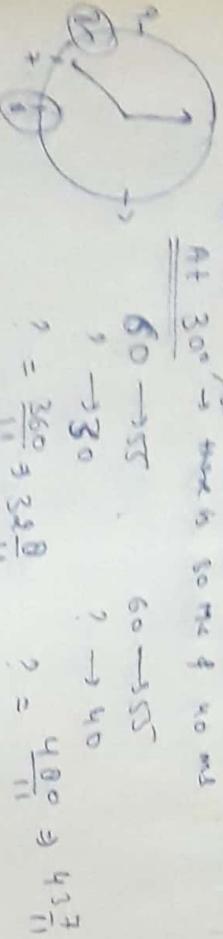
At  $0^\circ$



$$60 \rightarrow 55 \\ ? \rightarrow 35 \\ ? = \frac{420}{11} = 38\frac{2}{11}$$

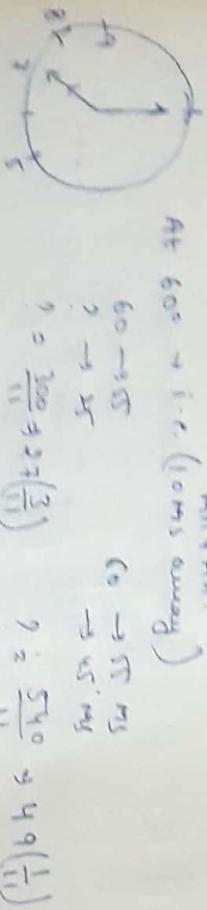
to min.  $\left[ \text{5 minutes away} \right]$

At  $30^\circ$  → there is 30 ms & no ms



$$60 \rightarrow 55 \\ ? \rightarrow 30 \\ ? = 60 - 35 \\ ? = \frac{360}{11} = 32\frac{8}{11} \\ ? = \frac{480}{11} = 43\frac{7}{11}$$

At 6:00 → i.e. (10 ms away)



$$60 \rightarrow 55 \\ ? \rightarrow 40 \\ ? = \frac{360}{11} = 32\frac{8}{11}$$

At  $90^\circ$ .

$$60 \rightarrow 55 \\ ? \rightarrow 20 \\ ? = \frac{240}{11} = 21\frac{9}{11}$$

At  $105^\circ$

$$60 \rightarrow 55 \\ ? \rightarrow 5 \\ ? = \frac{60}{11} = 5\left(\frac{5}{11}\right)$$

Q. How many time HH & MM will coincide at 6:00 am? [6:00 am only]

in 1 hr → 1 time

12 hr → 11 times

24 hrs → 22 times

2 days → 44 times

11

Minor image	$=$	five times
-		11:60

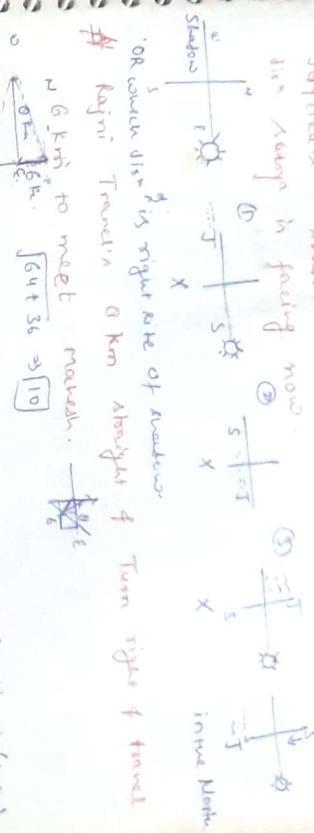
$$\frac{11:60 \text{ (start)}}{-7:20 \text{ (end)}} = \frac{11:60}{-7:15} = \frac{11:60}{-7:00} = \frac{11:60}{-6:30}$$

$$\frac{11}{4} : \frac{40}{45} = \frac{11}{4} : \frac{16}{30}$$

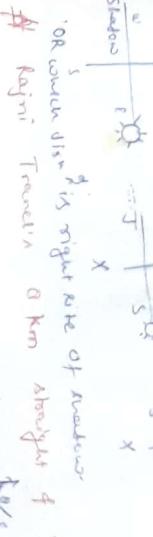
for Elevation  
60 m → it will cover  $65 \frac{5}{11}$  min

(1)  $60 \text{ m} \rightarrow 60 \text{ m}$   
 $\Rightarrow 0.45 \left(\frac{5}{11}\right) \text{ min.}$

Ans  $64 \text{ min} \rightarrow 1\frac{5}{11} \text{ (min)}$  |  $66 \text{ min} \rightarrow \frac{6}{11}$   
 $64 \rightarrow \frac{16}{11}$  |  $24 * 60 \rightarrow ?$   
 $24 * 60 \rightarrow ?$   
 $\rightarrow \frac{16}{11} \times 60 = \frac{960}{11} \text{ min.}$



(2) To take & always come at position to start loc.  
try & facing opposite to east start.  
Jay hiker shadow's in right side of sunset. In which  
dir. Raja is facing now.



OR when JSA is right side of sunset  
Rajni Travelling 8 km straight & turn right & travel

$\approx 6 \text{ km.}$  to meet manish.

$\sqrt{64+36} \approx \boxed{10}$

(3) what is the shortest dist b/w starting pt & ending pt (10m)

(4) what is the total distance covered by Rajni (14km)

(5) In which dir. Rajni is travelling finally (11)

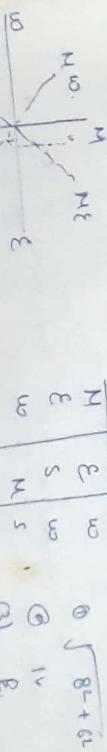
(6) Dist. Starting pt. where will be the ending pt. (S.W)

w.r.t. ending pt. where is starting pt. (S.W)

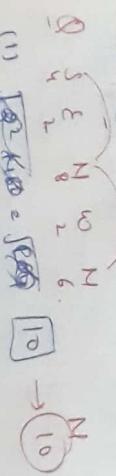
→ Default dirn should be North.

→ Angle " "  $90^\circ$

$\frac{\pi}{2}$



$\Rightarrow \boxed{10} \rightarrow N$

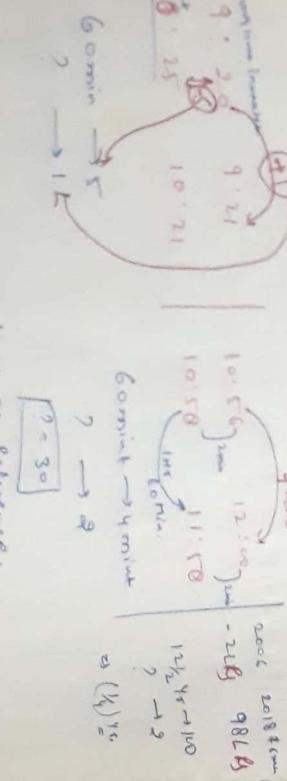


$\Rightarrow \boxed{10} \rightarrow N$

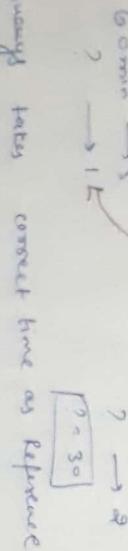
$\Rightarrow \boxed{2}$

$\Rightarrow \boxed{5}$

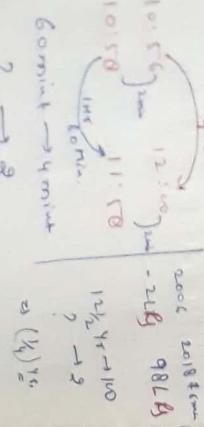
> Always takes correct time as reference.



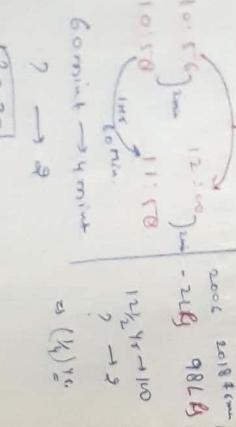
$\boxed{P=30}$



$\boxed{P=30}$



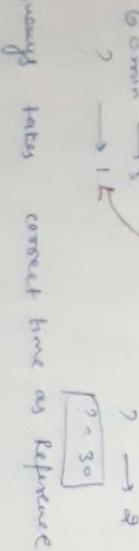
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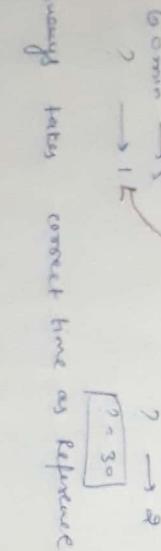
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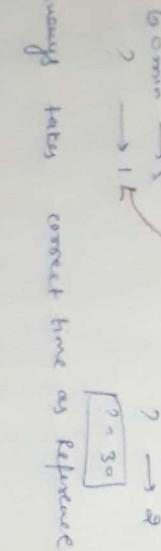
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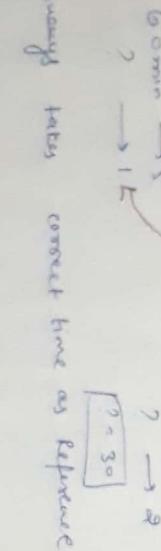
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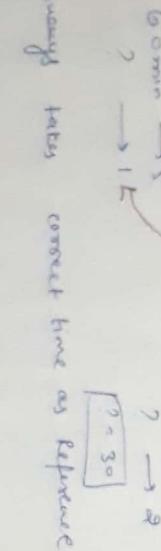
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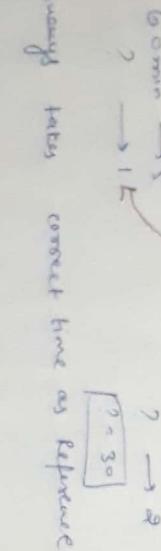
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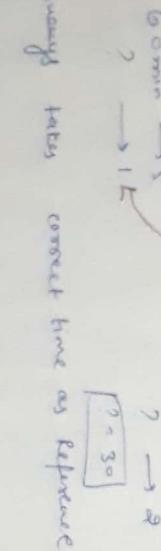
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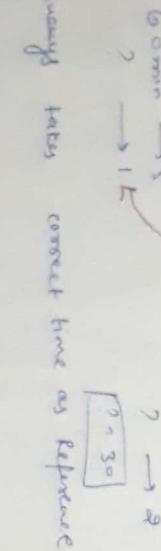
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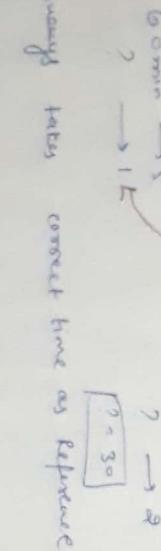
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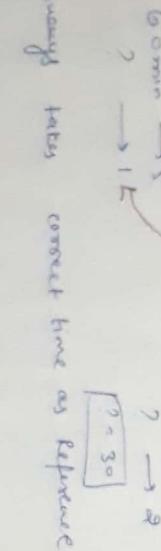
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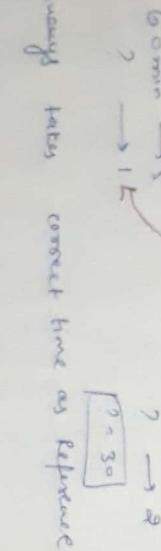
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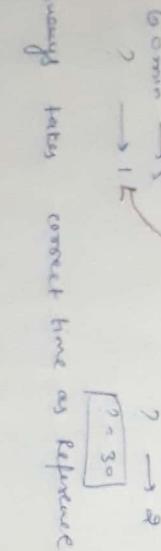
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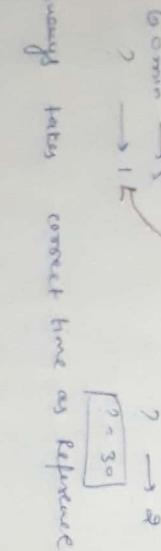
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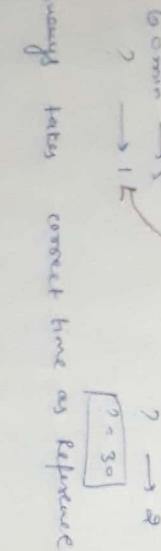
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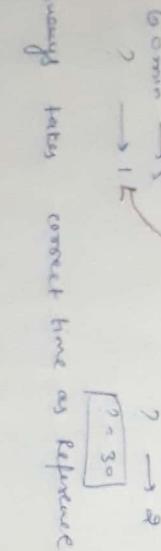
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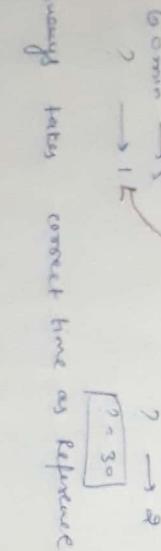
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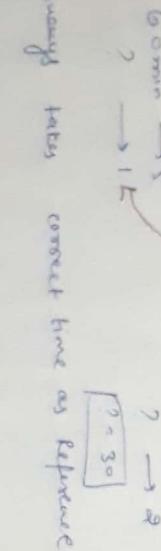
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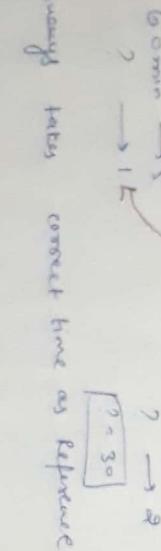
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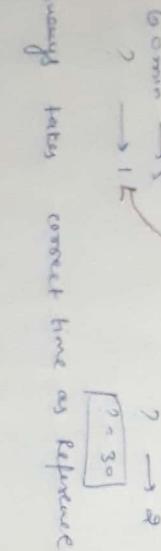
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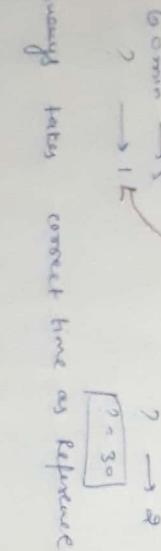
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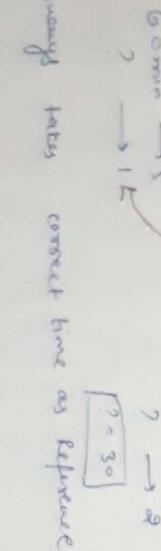
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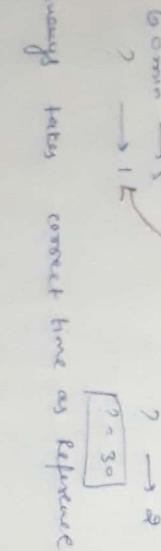
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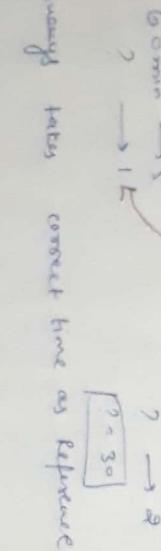
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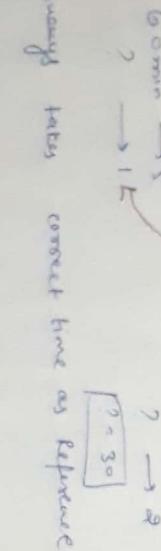
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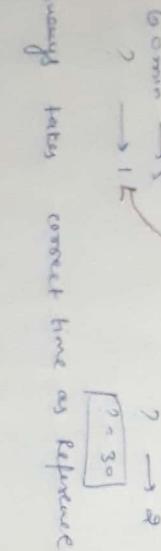
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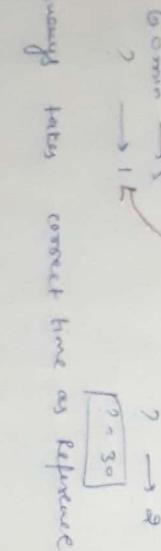
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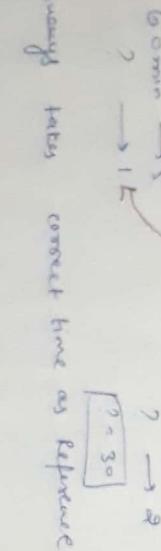
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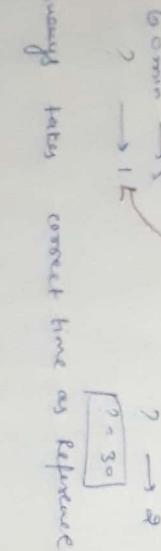
$\boxed{P=30}$



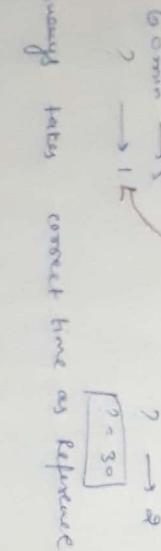
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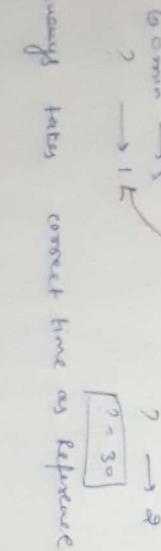
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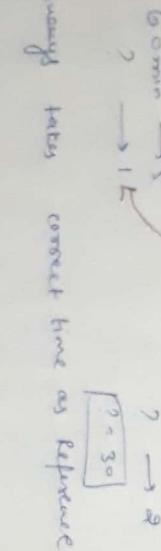
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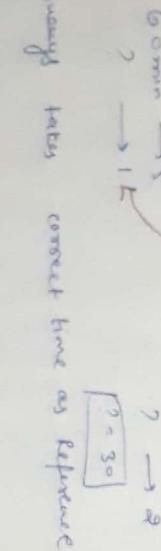
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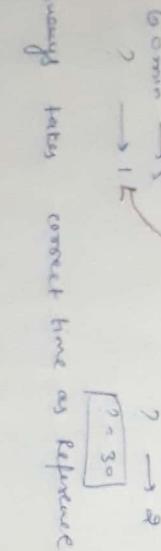
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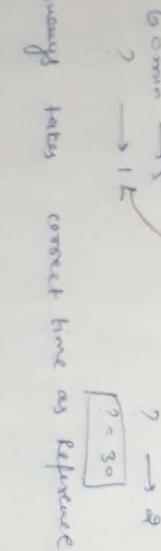
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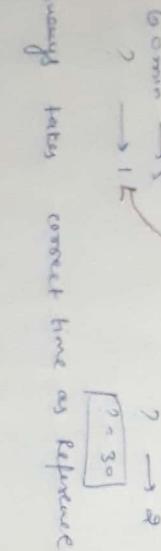
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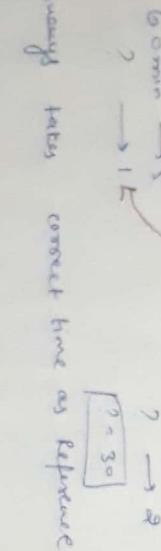
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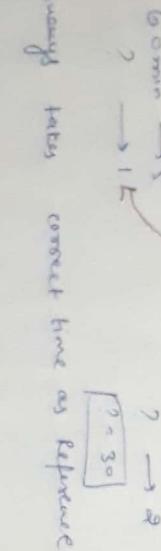
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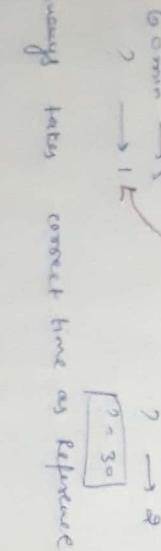
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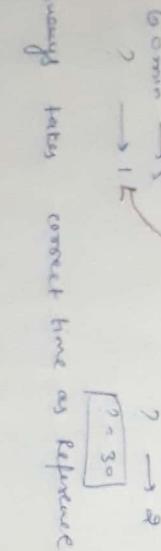
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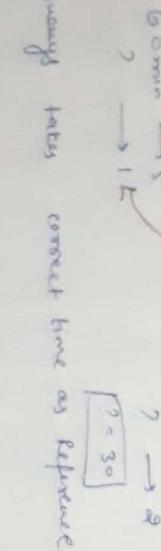
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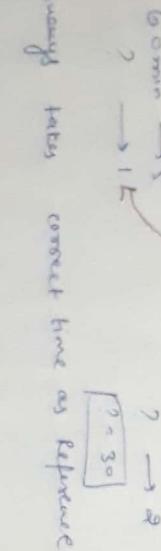
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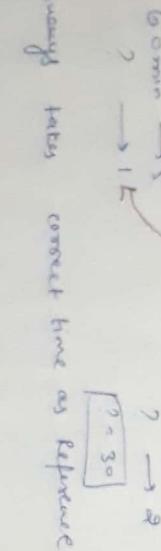
$\boxed{P=30}$



$\boxed{P=30}$



$\boxed{P=30}$



16 pag 11

$$= \begin{matrix} N & E & W & S \\ 8 & 6 & 4 & 2 \\ 6 & 4 & 2 & 8 \\ 4 & 2 & 8 & 6 \\ 2 & 8 & 6 & 4 \\ \hline 4 & 2 & 8 & 6 \end{matrix}$$

$$\begin{matrix} N & E & W & S \\ 4 & 2 & 8 & 6 \\ 6 & 4 & 2 & 8 \\ 8 & 6 & 4 & 2 \\ 2 & 8 & 6 & 4 \\ \hline 4 & 2 & 8 & 6 \end{matrix}$$

- (1)  $\sqrt{16+4} = \sqrt{20}$   
 (2) 2c  
 (3)  $\theta_N \rightarrow$  without magnification  
 (4) NE  
 (5) SW.

### Mirror Image / Water Image

\* ANAMIK A MAHE SHWARI

> MOMOS > ~~DEPARTMENT~~

> NORWAY

> VICEZAS > ~~DEPARTMENT~~

$$\begin{matrix} \text{Mirror Image} \rightarrow \text{symmetric abt} & \text{vertical axis.} \\ \hline \text{A} & \text{B} & \text{C} & \text{D} & \text{E} & \text{F} & \text{G} & \text{H} & \text{I} & \text{J} & \text{K} & \text{L} & \text{M} & \text{N} & \text{O} & \text{P} & \text{Q} \\ \text{A} & \text{g} & \text{c} & \text{o} & \text{d} & \text{e} & \text{f} & \text{r} & \text{h} & \text{i} & \text{t} & \text{x} & \text{j} & \text{m} & \text{n} & \text{o} & \text{q} & \text{p} \end{matrix}$$

$$\begin{matrix} \text{R} & \text{S} & \text{T} & \text{U} & \text{V} & \text{W} & \text{X} & \text{Y} & \text{Z} \\ \text{g} & \text{2} & \text{T} & \text{U} & \text{V} & \text{W} & \text{X} & \text{Y} & \Sigma \end{matrix}$$

water image  $\rightarrow$  symmetric abt horizontal axis.

A B C D E F G H I J K L M N O P Q R S T U V W X Y Z

# 1 Normal year  $\div 365$  day  $\rightarrow$  52 week + 1 odd day.  
 1 leap year  $\div 366$  day - 52 weeks + 2 odd day.

Month	Jan	Feb	Mar	Apr	May	Jun	Jul	Aug	Sep	Oct	Nov	Dec
Days	31	28/29 (01)	31 (3)	30 (2)	31 (3)	30 (2)	31 (3)	31 (3)	30 (2)	31 (2)	30 (2)	31 (3)
1 → Sun												
2 → Mon												
3 → Tue												
4 → Wed												
5 → Thu												
6 → Fri												
7 → Sat												

1) Find day? 13.03.1996, 30.09.1996  $\rightarrow$  52 weeks + 2 days  
 16.08.2018, 14.02.2019  $\rightarrow$  52 weeks + 1 day  
 16/08/2010 is Thursday  $\rightarrow$  52 weeks + 1 day  
 13.09.2018  
 x. 12. 2018  
 14.02.2019  
 1) which year start (or same day) when we know calendar or timing  
 2017, 2018, 2019, 2020.  
 2) last day of century, first day of century  
 3) March 1st which month starts with same day.



Paternal, maternal, etc.

Sun, Oct 1995  
Sat 10-1995  
1995, 09  
 $y = 19$   
 $m = 22$   
 $d = 01$

$$\frac{142}{4} \rightarrow \boxed{[4]} \text{ today.}$$

Tue, Nov 2018  
Oct 2017  
1997  
1600 300 97  
(b) 11 47 47  
24 73  
 $\frac{47}{2} = \boxed{[5]} \text{ framing}$

Wednesday, Nov 1996  
01 - Tuesday  
2  
3  
4  
5  
6  
7  
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31  
M  
T  
W  
Th  
F  
S  
Su

I - Grand father, grand mother,  
II - Father, mother, Aunt, uncle, brother in law, mother in law.  
III - Uncle, Sis, Bro, Cousin, brother in law, son in law, daughter in law  
IV - Sun daughter, nephews, nieces, son in law, daughter in law  
Grand son, Grand D.

what is the max gap b/w two successive L.Y.  
 $\max(h, g) \rightarrow \boxed{8}$

$$y = 1995 + 27 \\ (1995 + 27) = 2022 \\ 2022 - 1995 = 27$$

$\frac{g}{2.0}$  Area, A.m | 30°. vol.  
T.S.A., L.S.A.

1 → 1  
2 → 2, 4, 8, 16  
3 → 3, 9, 7, 1  
4 → 4, 6  
5 → 5, 1  
6 → 6, 4  
7 →

Q Table

Square -  $g - 30$

Cube -  $1 \rightarrow 2.0$ .

Find out unit digit of -

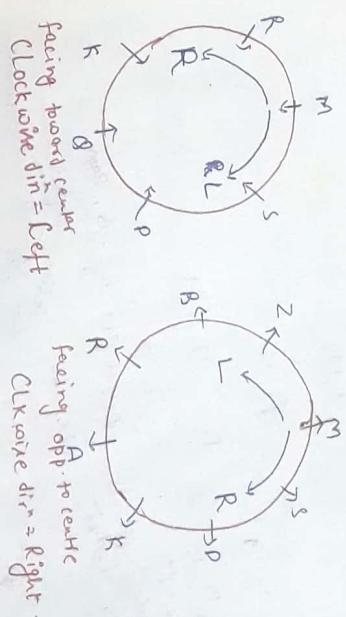
$$(1318)^{20} \rightarrow 6 \quad (105212)^{14} \quad 2 \quad (2031)^5 \quad 1 \quad (111015)^{13} \quad 5$$

In posn  
↓ M S P K R  
↑ SH V T VASW

Extreme Right corner = m, sw  
" Left " = R, sw  
Diagonal opp. = SH, R, m, sw.

### Seating Arrangement

Default dir: N. ↑ Intermediate Right, Right, Extreme left, Left, Left, " Right, " Left, " Left, " Right.



2D	3D	L.S.A
Circle	cube	$a^3$
Area	vol.	$\frac{4}{3}\pi r^3$
$\pi r^2$	cube	$6a^2$
$4\pi r^2$	(cuboid)	$2a(b+h)$
$\pi r^2$	sphere	$4\pi r^2$
$\pi(r+y)$	hemisphere	$\frac{4}{3}\pi r^3$
$\pi r^2$	elliptic	$\frac{2}{3}\pi r^3$
$\frac{1}{3}\pi r^2 h$	cone	$\pi r^2 h$
		$\pi r^2 h$

80 R S K R S K R S > K > K > R S

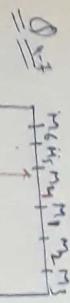
height → R → S → K → K → R → S

weight → K → K

height → Rāmāl Kāmāl Pānāl Kāmāl Pānāl Kāmāl Pānāl

weight → Rāmāl Kāmāl Kāmāl Pānāl Kāmāl Pānāl Kāmāl Pānāl

(1) feeta (2) pāna (3) Rāmāl.



f<sub>1</sub>, f<sub>2</sub>, f<sub>3</sub>

⑤ f<sub>6</sub> ⑦ f<sub>3</sub> m<sub>1</sub>, ③ f<sub>3</sub>

⑥ ⑨ orange green fed mind

⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

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① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

① ② ③ ④ ⑤ ⑥ ⑦ ⑧ ⑨ ⑩ ⑪ ⑫ ⑬ ⑭ ⑮

name	previous job	sequence	P.J.
① Han	Vale executive	M-Singh	Doctor
②	NS	Edins	
③	Deeper	A. Edits	
④			Delection
⑤	Harmont	Patentee	Patraise

Table

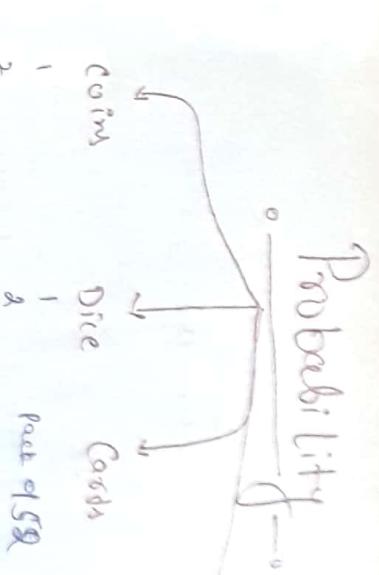
Sl No	Name	Surname	Position	Description
1	Deepak	Singh	SP	Police
2	Ajay	Sharma	RTM	Officer
3	Sanjay	Kumar	AC	Photo.
4	Munnu	Verma	CE	Detective
5	Himanshu	Adhikari	Adviser	Adviser
6	Ram	Thakur	SE	Balies.

Deputy  
Ajay

~ Advisor  
~ PA

Speaker ~ ce

Date		Sun	Mon	Tue	Wed	Thu	Fri	Sat.
-	Sanjay	(A)						
-	Komal	(A)						
-	Sneha	(A)						
-	Gautam	(A)						
-	Parvaneh	(A)						



coin 1 of H, T } = 2 { 0, 1 }

$2^1 \rightarrow$  (Outcomes)  
no. of coins

coin 2 of H, T } = 4 { 00, 01, 10, 11 }

$2^2$

$2^3$

$2^4$

$2^5$

$2^n$

Dice :-

1 → 6 outcomes →  $6^1 \rightarrow$  no. of Dice → { 1, 2, 3, 4, 5, 6 }

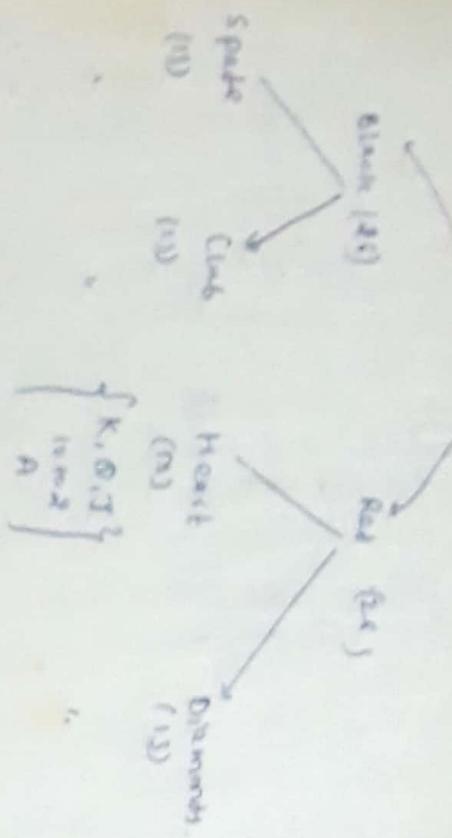
2 → 36 →  $6^2 \rightarrow$  outcomes

3 → 216 →  $6^3 \rightarrow$  outcomes

n →  $6^n \rightarrow$  outcomes

$\left\{ \begin{array}{l} 11 \\ 12 \\ 13 \\ 14 \\ 15 \\ 16 \\ 21 \\ 22 \\ 23 \\ 24 \\ 25 \\ 26 \\ 31 \\ 32 \\ 33 \\ 34 \\ 35 \\ 36 \\ 41 \\ 42 \\ 43 \\ 44 \\ 45 \\ 46 \\ 51 \\ 52 \\ 53 \\ 54 \\ 55 \\ 56 \\ 61 \\ 62 \\ 63 \\ 64 \\ 65 \\ 66 \end{array} \right\}$

## Cards (52)



- Q When a coin is tossed find the prob. of
- Getting a head (i) getting a tail.
  - When 2 coins r tossed find the prob. of
  - Getting exactly 1 head or 1 tail.  $\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right) = \frac{1}{2}$
  - Getting at least 2 head.
  - Getting at least 2 head.  $\left(\frac{1}{4}\right)$ .

Q 3 fair coins r tossed simultaneously

- Getting 1 head  $\frac{3}{8}$
- Getting 2 tail  $\frac{3}{8}$
- Getting at least 2 head  $\frac{7}{8}$
- " " " "  $\frac{5}{8}$

$$\text{Prob.} = \frac{5}{8} = \frac{1}{2}$$

toss One die 3 time = 3 dice tossed

- Q Find the prob. of - when 1 die is rolled -
- Getting a No. less than 7 but greater than 0  $\left(\frac{6}{6}\right)$
  - Getting a multiple of 2  $\left(\frac{3}{6}\right)$
  - Getting a prime No.  $\left(\frac{3}{6}\right)$
  - Getting even No.  $\left(\frac{3}{6}\right)$
- Outcome. (1, 2, 3, 4, 5, 6)
- (1) (2) (3) (4)

- Q At least 2 head  $\frac{5}{8}$
- Q Getting more heads than tails  $\left(\frac{1}{2}\right)$
- Q Two faces have  $> 0.51$
- Q At least 2 head  $\frac{5}{8}$
- Q Getting 1 head & 1 tail  $\frac{3}{8}$
- Q 100 0.11
- Q 101 1.10

(7) getting sum no. divisible by 3 or 4  
 " " as prime no.  $\frac{15}{36}$  ( $\frac{29}{36}$ )

(8) " atleast single 5  $\left(\frac{1}{3}\right)$

" " as prime no.  $\frac{15}{36}$  ( $\frac{29}{36}$ )

1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36

(6)  $\left[ \begin{matrix} 23, 26 \\ 32, 34, 36 \\ 43, 46 \\ 62, 63, 64, 66 \end{matrix} \right]$

one card is drawn from a pack of 52 cards

28/52

1. last drawn in black  $\frac{4}{52}$

2. last drawn is Queen  $\frac{4}{52}$

3. last drawn is black & Queen  $\frac{2}{52}$

4. either black or Queen  $\frac{28}{52} = \frac{28}{52} = \frac{14}{26}$

5. either black or Queen  $\frac{8}{52} = \frac{8}{52} = \frac{1}{52}$

6. " " " " King or Queen  $\frac{8}{52} = \frac{8}{52} = \frac{1}{52}$

7. " " " " neither black nor King or Queen  $\frac{39}{52} - \frac{3+3}{52} = \frac{36}{52} = \frac{9}{13}$

8. " " " " is Ace or King  $\frac{1}{52}$

9. " " " " is Ace or King  $\frac{1}{52}$

solve (13)

spade (26) Club (15) Diamond (13) Heart (13)

10. 10 10 10

$$\text{P}(A \cup B) = \text{P}(A) + \text{P}(B) - \text{P}(A \cap B)$$

$$\text{P}(A \cup B \cup C) = \text{P}(A) + \text{P}(B) + \text{P}(C) - \text{P}(A \cap B) - \text{P}(B \cap C) - \text{P}(A \cap C) + \text{P}(A \cap B \cap C)$$

(i) mutually exclusive.

$$\text{P}(A \cup B \cup C) = \text{P}(A) + \text{P}(B) + \text{P}(C)$$

(ii) independent.

$\text{P}(A) = \text{Prob. of occurrence of } A$

$\text{P}(AB) = \text{Prob. of occurrence of } A \text{ and } B$

$\text{P}(AB) = \text{Prob. of occurrence of } A \text{ and } B \text{ or both } A \text{ and } B$

$\text{P}(AB \cup C) = \text{Prob. of occurrence of } A \text{ or } B \text{ or both } A \text{ and } B \text{ or } C$

$\text{P}(A \cup B \cup C) = \text{Prob. of occurrence of } A \text{ or } B \text{ or } C$

Ques. A bag contains 4 white & 3 black balls.

$$P(A) = \frac{4}{7}, P(B) = \frac{3}{7}, P(A \cap B) = \frac{1}{7}$$

Find the probability of getting a white ball.

White	Black	Total
1	2	3
2	3	5
3	4	7
4	5	9

$$P(A) = \frac{4}{7}, P(B) = \frac{3}{7}, P(A \cap B) = \frac{1}{7}$$

A die is rolled. Find the prob. that the outcome is an odd no. subject to the prob. that it is a prime no.

i.e.

Ques. A die is thrown. Find the prob. that the sum of the faces shown is 8, if 4 appears on the first die.

Ques. A class has 45% student read Tamil, 30% read Telugu

4 20% read both Tamil & Telugu. One (1) student is selected at random. Find the prob. that he reads Tamil, if it is known that he reads Telugu.

$P(\text{Read Tamil}) = \frac{P(\text{Read Tamil} \cap \text{Read Telugu})}{P(\text{Read Tamil})}$  if cond. prob. of A given B.

$P(\text{Read Tamil} \cap \text{Read Telugu}) = P(\text{Read Tamil}) \times P(\text{Read Telugu})$ .

$$\frac{1}{4} \times \frac{1}{3} = \frac{1}{12}$$

$P(\text{Read Tamil}) = \frac{P(\text{Read Tamil} \cap \text{Read Telugu})}{P(\text{Read Tamil})}$

$$\approx P(\text{Read Tamil}) = P(\text{Read Tamil}) = \frac{1}{12}$$

Ques. A bag contains 4 white & 3 black balls.

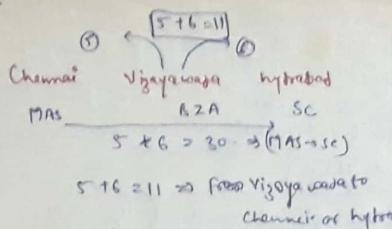
$$P(A) = \frac{4}{7}, P(B) = \frac{3}{7}, P(A \cap B) = \frac{1}{7}$$

A die is rolled. Find the prob. that the outcome is an odd no. subject to the prob. that it is a prime no.

$$P(A) = \frac{4}{7}, P(B) = \frac{3}{7}, P(A \cap B) = \frac{1}{7}$$

$$P(A) = \frac{4}{7}, P(B) = \frac{3}{7}, P(A \cap B) = \frac{1}{7}$$

21/08/19



Principle of Multiplication -  $m \times n =$  Dependent (AND)

" " Addition -  $m + n =$  Independent (OR)

$$\text{Letters} = 26 \quad \text{If select 1 vowel and 1 consonant}$$

$$\text{Vowel} = 5 \quad 5 \times 21$$

$$\text{Consonent} = 21 \quad \text{If select either Vowel or consonant } (5+21)$$

P	C
> Arrangement	> Cm selection
> $n_{Pr} = \frac{n!}{(n-r)!}$	> $n_{Cr} = \frac{n!}{r!(n-r)!}, \frac{P!}{r!}$
, order will consider	Order will not be consider.
> Drinking of sambar	> Sambar
> Eating of combornice	> combornice.

Q There are 20 buses running b/w Chennai to Trivandrum. In how many ways a student can go to Trivandrum & return Chennai in different bus. (Journey depend on both)

$$\rightarrow 20 \times 19 = 380$$

$$\begin{array}{c} \text{MAS} \xrightarrow{\hspace{1cm}} \text{TPTY} \\ \downarrow \uparrow \\ 3 \times 2 \\ 1 \times 2 \\ \downarrow \uparrow \\ 3 \times 2 = 6 \end{array}$$

Q In how many ways can a chairman & vice chairman be elected from 11 members -

$$11 \times 10 = 110$$

Q In a placement drive, there are 3 sections, Reasoning aptitude, electrical, containing 10 Q, 5 Q, 20 Q. In how many ways a student select 1 Q from each section each of these see

$$10 \times 5 \times 20 = 1000$$

Q A Test paper have 10 Q of each Q have 4 options. If each Q is necessarily attempted. Find the No. of ways of answering.

$$(4)^{10} \quad \begin{array}{c} 1 \times 4 = 4 \\ \downarrow 1 \times 4 \\ 1 \times 4 \end{array} \approx$$

$$4 \times 4 = 4^{10} = 1024$$

Q A set of 6 Q contain True or false Q's. In how many ways a student can take the test if all the students answer differently from others & must attempt all Q. \*

$$(2^6) = (2^6)$$

Q In the 1st section contain 5 Q with 4 option. Second section have 4 Q with 2 option. In how many ways can the paper be attempted  $(4)^5 * (2)^4$

Q. How many 3 letter words can be formed using only consonants yet each word  $\rightarrow$   $24 \times 20 \times 19$   
 $\rightarrow 17280$

Q. How many 3 digit no. can be formed using unit digit is 0-4 repetition not allowed.  
 $\rightarrow 8 \times 9 \times 4 = 288$

Q. How many 4 digits no. can be formed with 2, 4, 6, 8  
 $4 \times 4 \times 4 \times 4 = 4^4$

Q. How many nos. can be form 2, 4, 6, 8 without repetition.  
 $4 \times 3 \times 2 \times 1 = 24$

$$\begin{array}{r} 4 \times 3 \times 2 \times 1 \\ = 24 \\ 4 \times 2 \\ = 8 \\ 4 \times 1 \\ = 4 \\ \hline 24 \end{array}$$

Q. How many ways 3 different rings can be fixed for 3 fingers with atmost 1 in each finger  
 $\rightarrow \frac{3!}{2!} = 3$

Q. In how many ways 5 letters be posted in 3 boxes.

$$2^5 = 32 \quad \text{ways.} \quad \begin{array}{l} n - \text{No. of} \\ x - \text{No. of outcomes.} \end{array}$$

22/08/18  
 In how many ways SINDHU & GANGA can be arrange -

$$\begin{array}{l} \text{SINDHU} \rightarrow 6! \\ \text{GANGA} \rightarrow 5! \\ \hline 6! \end{array}$$

$$\text{MALAYALAM} = \frac{9!}{2!4!2!}$$

Q. On the occasion of New Year, 1000 friends conducted running race, singing, dancing, cycling, programming. In how many 5 prize distributed to 10 participant.

$$10 \times 9 \times 8 \times 7 \times 6 = 120$$

$$\begin{array}{l} 10 \times 9 \times 8 \times 7 \times 6 \\ \cancel{5} \quad \cancel{4} \quad \cancel{3} \quad \cancel{2} \quad \cancel{1} \\ \hline 120 \end{array} \Rightarrow 50 + 36 + 24 + 16 + 10 = 120$$

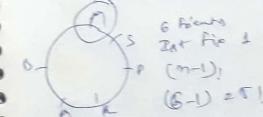
$$10 \times 10 \times 10 \times 10 \times 10 = 100000 \rightarrow 10^5 \text{ participants}$$

Q. In how many ways 12 friends can stand in a row.  
 Q. In how many ways 12 friends can stand in a circular form.

$$\begin{array}{l} 12! \\ \cancel{12} \end{array}$$

$$\textcircled{Q} \quad (6! 6!) = 12! \times 6! \times 2$$

$$\textcircled{Q} \quad 12! / (n-1)! = (12-1)! = 11!$$



Q. In how many ways 9 diamonds can string as necklace.

$$\begin{array}{l} 8! \\ \cancel{8} \end{array}$$

Whenever class of and anticlass is same then  $\frac{(n-1)!}{2}$

Q In how many ways 12 lines can form a girdle.  
 $(12-1)!$  =  $\boxed{11!}$

Q By using 7 point if no one is collinear  
 then how many straight line is possible  
 to make.

Ans To make straight line 2 points required

$${}^7C_2 = \boxed{21}$$

Q How many triangle can be form by using 5 dots.  
 ${}^5C_3 = \frac{5 \times 4 \times 3}{3} = \boxed{10}$

Q 29 girls have to shakehand with each other,  
 In how many ways they can do this?

$$\boxed{{}^{29}C_2}$$

Ans: find the rank of word "DOG", "LION", "TIGER",  
 "CHEETA" & "PANDA" in dictionary order.

	Rank
DOG	1
GOD	2
GOD	3
OGD	4
OGD	5
ODG	6
ODG	7

$$\begin{array}{r} 34351 \\ PRAYA \\ 22110 \\ + 41321101 \\ \hline 48+12+2+1+0 = 63 \end{array}$$

$$63+1 = \boxed{64}$$

$$\begin{array}{r} 132 \\ DOG \\ 010 \\ 21101 \\ 0+1+0=1 \\ 1+1=2 \end{array}$$

Step ① In R.L.A write the position according to dictionary  
 $213 \rightarrow$  vowel letter will come first  
 C-A-T

Q See how many No. is less than that NO.

$$\begin{array}{r} 213 \\ 100 \\ \hline \text{No. less} \end{array}$$

Q write factorial from right hand side starting from 0

$$213$$

$$\begin{array}{r} 100 \\ \hline \text{Ans} \end{array}$$

Repetitions

$$\begin{array}{r} 413253 \\ MAHESHA \\ 401010 \\ 2121 \\ 5141321101 \\ \hline \end{array}$$

$$413253$$

$$\overline{\text{MAHESHA}}$$

$$\overline{5}$$

$$40+0+5+0+1+0=244$$

$$\boxed{245}$$

~~2x10^12~~

### Arithmetic Progression (A.P.)

When the difference b/w two successive terms is constant, then the progression is called A.P.  
 $\Rightarrow$  (i)  $a, a+d, a+2d, a+3d, \dots$   
(ii) Simple Interest.

$$n^{th} term = a + (n-1)d$$

$$\text{Sum} = S_n = \frac{n}{2} (2a + (n-1)d)$$

$$\Rightarrow \frac{n(a+2d)}{2}$$

G.P. → When the ratio b/w two successive terms is constant,

$$\text{nth term} = ar^{n-1} \text{ or } a r^{1-n}$$

$$\text{Sum} = \left( \frac{a(1-r^n)}{1-r} \right) \text{ or } \left( \frac{a(r^n-1)}{r-1} \right)$$

H.P. → When the reciprocals of the terms form an arithmetic progression.

$$\frac{1}{a}, \frac{1}{a+d}, \frac{1}{a+2d}, \frac{1}{a+3d}, \dots$$

$$\frac{n}{m} = \left[ \frac{1}{a} - \frac{1}{a+(n-1)d} \right]$$

$$\text{Sum} = \frac{d}{n(m+l)}$$

Q. Q. 72, 70, 68, 66, ... 40.

Find the sum of the series.

$$a = 72, d = -2, l = 40$$

$$\text{Sum} = \frac{17}{2} (72 + 40) \Rightarrow \frac{56}{2} \times 17$$

$$72 + (n-1)(-2) = 40$$

$$(n-1)(-2) = -32 \Rightarrow 16 \Rightarrow \frac{(72 \times 17)}{2} = \frac{119}{2}$$

$$(n-1) = 16 \Rightarrow n = 17$$

$$\Rightarrow \frac{(16 \times 72)}{2} = \frac{1920}{2} = 960$$

$$\frac{960}{16} = \frac{60}{1} = 60$$

Find the sum of the series

$$2 + 2^2 + 2^3 + \dots + 2^{10}, \text{ Q. Q.}$$

$$r = 2, a = 2$$

$$\text{Sum} = 2 \times \frac{2^{10} - 1}{2-1} = 2^{11} - 2 = 2046 \quad (n=10)$$

$$\frac{2(2^{10}-1)}{1} \Rightarrow 2(1024) \Rightarrow 2(1023) \Rightarrow 2046$$

II

① Sum of Natural No. =

$$1+2+3+4+\dots+n = \boxed{\frac{n(n+1)}{2}}$$

② Sum of square of 'n' natural No. =

$$1^2+2^2+3^2+4^2+\dots+n^2 = \boxed{\frac{n(n+1)(2n+1)}{6}}$$

③ Sum of Cubes of 'n' natural No.

$$1^3+2^3+3^3+4^3+\dots = \boxed{\left[\frac{n(n+1)}{2}\right]^2}$$

④ Sum of first 'n' odd no.

$$1+3+5+7+\dots = \boxed{n^2}$$

⑤ Sum of 1st 'n' even no.

$$2+4+6+8+\dots = \boxed{n(n+1)}$$

⑥ Sum of square of 'n' odd No.

$$1^2+3^2+5^2+7^2+\dots = \boxed{\frac{n}{3}(4n^2-1)}$$

⑦ Sum of square of 'n' even No.

$$2^2+4^2+6^2+8^2+\dots = \boxed{\frac{2n(n+1)(6n+1)}{3}}$$

The sum of the 'n' terms of the following series

(8)  $1+(1+2)+(1+2+3)+\dots+(1+2+3+\dots+n)$

$$\Rightarrow \boxed{\frac{1}{6}n(n+1)(n+2)}$$

⑧  $1 \cdot 2 + 2 \cdot 3 + 3 \cdot 4 + \dots = \boxed{\frac{n(n+1)(n+2)}{3}}$

⑨  $1 \cdot 2 \cdot 3 + 2 \cdot 3 \cdot 4 + 3 \cdot 4 \cdot 5 = \boxed{\frac{n(n+1)(n+2)(n+3)}{4}}$

## Logarithms

were developed

difficult & complicated calculation easy.

If 3. No's , a, n, m & such that

$$a^x = n$$

then  $x$  = logarithm of the No. n to the base 'a'

$$x = \log_a n$$

①  $\log_a(MN) = \log_a(m) + \log_a(n)$

②  $\log_a(M/N) = \log_a(m) - \log_a(n)$

③  $\log_a(a) = 1$

④  $\log_a m^n = n \log_a m$

⑤  $\log_a(1) = 0$

⑥  $\log_a(m) = \frac{1}{\log_a(a)} = \log_a(m) + \log_m(a) = 1$

- (1)  $\log_b^{(n)} = \frac{\log_a(n)}{\log_a(b)}$
- (2)  $\log_a(b) * \log_c(b) * \log_d(a) = 1$
- (3)  $\log_a(b^m) = \frac{m}{b} \log_a(m)$
- (4)  $\log_a(b^n) = \log_a(n) + \log_a(b)$
- (5)  $\log_a(16) = \log_a(2)^4 = [4]$
- (6)  $\log_7\left(\frac{1}{343}\right) \rightarrow \log_7\left(\frac{1}{7^3}\right) = [-3]$
- (7)  $\log_{10}(0.001) = \log_{10}\left(\frac{1}{1000}\right) = [-3]$
- (8)  $\log_{3\sqrt{2}} 5832 \rightarrow [6]$
- (9)  $\log_{x/4} \frac{1}{4} = -1 \rightarrow [x=4]$
- (10)  $\log_{10}(x) = -2 \rightarrow x = 10^{-2} \rightarrow \boxed{\frac{1}{100}}$
- (11)  $\log_x \sqrt{2} = \left(\frac{1}{2}\right) \rightarrow x^{1/2} = 2^{1/2}$   
 $(x^{1/2})^{1/2} = (2^{1/2})^{1/2}$
- (12)  $\log_{\frac{x}{8}} x = \frac{3}{3} \rightarrow$
- (13)  $\log_8(128) = \log_8(8 \times 8 \times 2) = x$
- (14)  $\log_{5.55}(125)$
- (15)  $\log_{15}$

Rough

$$\begin{array}{r} 6 \\ 49 \text{ is } 7^2 \\ 343 \text{ is } (7^3) \\ 3 | 5832 \quad (7^6) \\ \hline 3 | 1944 \\ 3 | 648 \quad \text{as } 6 \end{array}$$

$$\begin{array}{r} 3 | 216 \\ 3 | 72 \quad (3^2 \cdot 2^2) \\ 3 | 24 \\ 2 | 8 \quad (3^2)(2^3) \\ 2 | 4 \\ \hline 2 | 2 \end{array}$$

$$x^{-1} = \frac{1}{4}$$

$$x^{-1} = 4^{-1}$$

$$(x^{-1})^3 = x$$

$$(\frac{1}{4})^3 = \frac{1}{64}$$

(16)  $\log_5 \log_3(3125) =$

- (17) The value of  $\log_b$  is equal to
- (a)  $\log_1 + \log_2 + \log_3 + \dots$
- (b)  $\log(1+2+3)$
- (c)  $\log(1+2+3)$
- (d) All of the above.

A B C D E F G H I J K L M N  
 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17

- (1) MAHESH  $\rightarrow$  N B I P T I  
 INDIA =
- (2) MAHESH  $\rightarrow$  HAMHSE  
 INDIA  $\rightarrow$
- (3) MAHESH = 36 ( $6^2$ )  
 INDIA =  $(5)^2 = 25$
- (4) MAHESH = 123453  
 SAM = 521

INDIA IS GOOD BOY (Ri) boy  
 Good boy = Ri  
 boy is kind = boy Tu Ni  
 Good = Ri  
 Boy = Baat  
 Is = 42  
 Kind = Tu.

Q If sky is blue  
 blue is green  
 green is red  
 red is rose  
 Rose is "dangerous"  
 Danger is safe  
 Safe is sky

what is the code for flower -  
 "Danger"

①  $P(E) = \frac{\text{favourable outcome}}{\text{Total possible outcome}}$

OR = addition  
 AND = multiplication

②  $P(\bar{E}) = 1 - P(E)$

Q 4G, 5Blue, 2Red, 3Y - ?

③ If marbles r drawn at random, What is p of both  
red or at least one is red. arrange (RR)

$$\left( \frac{2}{14} \right) \left( \frac{1}{13} \right) \left( \frac{2!}{2} \right) \underbrace{\frac{1}{P(RR)}}_{\text{arrangement}} + \frac{2}{14} \cdot \left( \frac{12}{13} \right)^{2!} \Rightarrow \frac{1}{91} + \frac{24}{91} = \frac{25}{91}$$

for at least 2 balls (at least Red) -  
take -ve approach

$$1 - P(\text{Not Red}) \Rightarrow 1 - P(XX)$$

④ If 3 marbles r drawn, what is p (at least one is yellow)

$$1 - P(\text{No. any one yellow}) = 1 - P(XXX)$$

$$\Rightarrow 1 - \frac{11}{14} \cdot \frac{10}{13} \cdot \frac{9}{12} = \frac{31}{36}$$

$$\Rightarrow 1 - \frac{165}{364} = \frac{199}{364}$$

⑤ If 8 balls r drawn, what is p that there r equal no.  
of marbles of each colour.

$$4G, 5B, 2R, 3Y = 14 \text{ ball}$$

$$\frac{8}{14} = 2 \quad P(GGBBRYY) = \left( \frac{4}{14} \cdot \frac{3}{13} \cdot \frac{5}{12} \cdot \frac{4}{11} \cdot \frac{3}{10} \cdot \frac{1}{9} \cdot \frac{3}{8} \cdot \frac{2}{7} \right) \times \frac{8!}{2! 2! 2!}$$

$$= \left( \frac{60}{1001} \right)$$

(Q) If 3 balls are drawn at random, P( None is green).

$$P(X \neq X) = \frac{10}{14} \cdot \frac{9}{13} \cdot \frac{8}{12} = \left( \frac{5}{7} \right)^3 = \frac{125}{343} \approx \left( \frac{3}{7} \right)^3$$

### Approximation (Trick)

Time

Speed = Distance

Time

→ Concept :-

Q

Answer

when a car has speed from 24 km/hr to 30 km/hr taken 1 hr less than the usual time. What is time.

D.

$$S = 24 \text{ km}$$

$$T_1 = \left(\frac{D}{24}\right)$$

$$T_1 - T_2 = 1$$

$$S = 30 \text{ km}$$

$$T_2 = \frac{D}{30}$$

$$\frac{D}{24} - \frac{D}{30} = 1 \Rightarrow D = 120 \text{ km}$$

Basic

D.

$$S = 24 \text{ km} \quad D$$

$$S = 30 \text{ km} \rightarrow t-1$$

Here Distance is constant

$$24t = 30(t-1)$$

$$6t = 30 \Rightarrow t = 5$$

$$D = 120 \text{ km}$$

$$18 = 0$$

$$0n = 52 + 00$$

$$\frac{18}{D} = \frac{52}{52+0}$$

$$0_1 = 0_2$$

$$0_1 = 0_2$$

$$\overleftarrow{\rightarrow 01}$$

$$\overleftarrow{\rightarrow 02}$$

$$\overleftarrow{\rightarrow 01}$$

$$\overleftarrow{\rightarrow 02}$$

$$Z = 20 \text{ mm}$$

On the right side of the diagram there is a note:  
"This is the same as the previous one, but with  
a different angle and distance from the center of  
rotation to the center of the wheel. This is a 10° angle".

$$0_1 = 0_2 \text{ and } r_1 = r_2$$



$$0_1 = 0_2 \text{ and } r_1 = r_2$$

From the notes:



$$r_1 = 10$$

From the notes:



A note to the right of the diagram: "The angle is 10°".

Another note to the right of the diagram: "The angle is 10°".



Another note to the right of the diagram: "The angle is 10°".

$$km/hr = \frac{5}{18} \times m/s$$

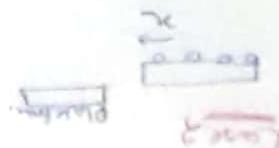
$$m/s = \frac{18}{5} \times km/hr$$

$$m/s \longleftrightarrow km/hr$$

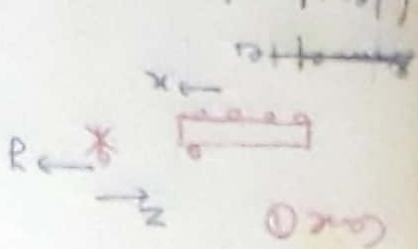
K. Speed  
(Relative speed of two bodies)



(Speed of two bodies)  
Relative speed of two bodies



(Relative speed of two bodies + 0)



Relative speed.

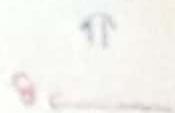
$$\text{Relative speed} = \frac{s}{t} = \text{Sum of speeds of two bodies}$$

Relative speed =  $|A+B|$



$A > B \rightarrow$  separation  $\theta$   
 $B > A \rightarrow$  meeting  $\theta$

Relative speed =  $|A-B|$



Relative speed =  $|A+B|$

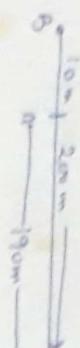
Car A moves more in time  
Car B moves less in time

Time of meeting

Concept of Relative

In a race of 200 m, B can give A start of 10 m to A. The start that C gives to A in race in

metre



S & D

$$\frac{s_A}{s_B} = \frac{200}{190} \quad \textcircled{1}$$

$$\frac{s_C}{s_B} = \frac{200}{180} \quad \textcircled{2}$$

$$\frac{s_C}{s_A} = \frac{200 \times \frac{200}{190}}{170} \quad \textcircled{3}$$

$$(S_A \propto 17)$$

In a 2 km race, A beats B by 30 sec. B beats C by 15 sec. If A beats C by 180 m in the time taken by A to run 1 km in —

$$\boxed{S_A \propto \frac{1}{t}}$$

$$\frac{s_A}{s_B} \propto \frac{t+30}{t} = \frac{t+30}{t}$$

$$\frac{s_B}{s_C} = \frac{t+30+15}{t+30} = \frac{t+45}{t+30}$$

$$\frac{s_A}{s_C} = \frac{180}{820} \frac{s_B}{s_1}$$

$$\frac{s_A}{s_B} \times \frac{s_B}{s_C} = \frac{t+30}{t} \times \frac{t+45}{t+30} = \frac{50}{41}$$

$$41t + 41 \times 45 = 50t$$

$$\boxed{t = 205 \text{ sec}}$$

To & time taken by  
C to win race

Cane 1 km (T<sub>A</sub>)  
When they will

meet at time

Starting pt.

$$\begin{array}{c} A \rightarrow 20 \text{ sec} \\ B \rightarrow 30 \text{ sec} \\ C \rightarrow 40 \text{ sec} \end{array}$$

$$\begin{array}{c} T_A = 300, 600, 900 \\ T_B = 200, 400, 600 \\ T_C = 175, 350 \end{array}$$

$$\boxed{\frac{\text{Km} (T_A)}{\text{Km} (T_B)}}$$

hence

$$\begin{array}{l} D_A = 20 \\ D_B = 30 \end{array}$$

fixed &  
her fire  
km

→ Race (Circular)







- Rule 18 → water out of ~~the~~ superficial words.
- Rule 19 / is superlative than that, Rule 20 + to
- Rule 10 - when comparing, adjective ending in -er, -est, -more, -most follows by
- Rule 11 Transitive Verb of the verb are a preparation when
- Rule 12 ~~they decided~~ ~~arrange~~ a general party in the end
- Rule 13 ~~of his~~ ~~difference~~ ~~(as)~~ ~~especially~~ as she had been working for the first ~~since~~ ~~almost~~ ~~every year~~.
- Rule 14 ~~she~~ ~~had~~ ~~built~~, I ~~have~~ ~~placed~~ the book
- Rule 15 ~~farm~~ ~~out~~, ~~"If~~ ~~condition~~.
- Rule 16 ~~I~~ ~~would have~~ ~~paid~~ the ~~expenses~~.
- Rule 17 ~~If~~ ~~and~~ ~~then~~ ~~I~~ ~~had~~ ~~built~~, ~~I~~ ~~would have~~ ~~paid~~ the ~~expenses~~.
- Rule 18 ~~she~~ ~~had~~ ~~built~~, ~~I~~ ~~would have~~ ~~paid~~ the ~~expenses~~.
- Rule 19 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 20 ~~they~~ ~~decided~~ ~~arrange~~ a general party in the end
- Rule 21 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 22 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 23 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 24 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 25 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 26 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
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- Rule 92 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 93 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 94 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 95 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 96 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 97 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 98 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 99 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.
- Rule 100 ~~she~~ ~~had~~ ~~placed~~ the ~~book~~.

(1) will force you / even as ordinary mouse  
In these days of inflation / as less supplies now

(2) but I was really anxious about it.  
part of my friends (had the experience)

(3) feel  

$$S + V + MV + MV$$

(4) part perfect + could have + M.V.

(5) You asked him.  
Fav: course / have told you / the truth.

(6) very hard job / the fastest moving month.  
The captain along with us learns (especially)

(7) enjoy + seemed (M.V-ing)

(8) Do you / enjoy (if not) the comedy show / for boy!  
Do you / enjoy (if not) the cartooning.

(9) Prevented + seem + M.V.(ing)

(10) He's father / will be in the same  
of (not) / been prevented / among them

(11) He's father / will be in the same  
as V + H + H + going to meet very

(12) you / buy / buy it for me

