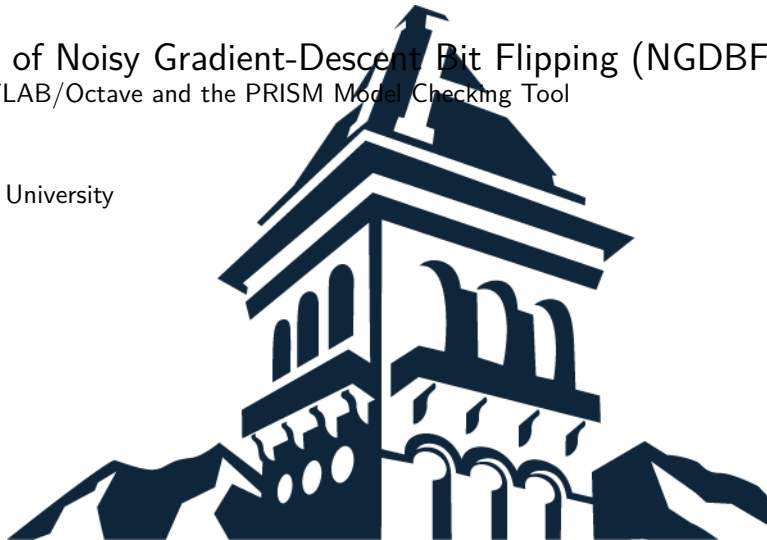


# Analysis of Noisy Gradient-Descent Bit Flipping (NGDBF)

Using MATLAB/Octave and the PRISM Model Checking Tool

Eric Reiss  
Utah State University



# Overview

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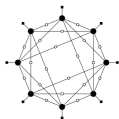


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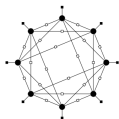


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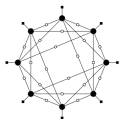


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- ▶ Absorbing sets are a special case of a trapping sets that are stable in a bit flipping decoder [1]

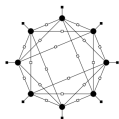


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- ▶ Samples are pulled from Gaussian distribution with a mean of 1 and a standard deviation of  $\sigma = \sqrt{\frac{1}{R \cdot 10^{SNR/10}}}$ , where  $R$  is the code rate

```
loop_check = get_error_sample_size(sym_size);
valid_samples = zeros(1,loop_check); % initialize valid samples
valid_idx = 1;
error_samples = zeros(1,loop_check); % initialize error samples
error_idx = 1;
while valid_idx <= loop_check || error_idx <= loop_check
    temp = normrnd(1,sigma); % generate samples
    if temp > 0 % sort valid samples
        valid_samples(valid_idx) = temp;
        valid_idx = valid_idx + 1;
    else % sort error samples
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end
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- ▶ Currently the tool generates a list of samples and sorts into valid and error sample bins
- ▶ An error sample is one that comes from the negative tail of the Gaussian distribution
- ▶ There is probably a better way to do this, and finding that is on the to-do list

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    end
end
```

# Energy Calculation

- To create the model, all possible energy values must be calculated

```
%initialize Energy and check node matrices
E = zeros(2^sym_size,sym_size);
chk_nodes = ones(1, check_size);
chk_sum = zeros(1,sym_size);
% Calculate all possible energy values for each state
for row = 1:2^sym_size
    % Calculate all check nodes
    for adj_row = 1:check_size
        for adj_col = 1:sym_size
            if adj_mat(adj_row,adj_col) == 1
                chk_nodes(adj_row) = chk_nodes(adj_row)*x(row,adj_col);
                chk_sum(adj_col) = chk_sum(adj_col)+chk_nodes(adj_row);
            end
        end
    end
end
% Calculate energy values
for E_idx = 1:sym_size
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# Energy Calculation

- ▶ To create the model, all possible energy values must be calculated
- ▶ The syndrome, called `chk_nodes` here, is also calculated

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E = zeros(2^sym_size,sym_size);
chk_nodes = ones(1, check_size);
chk_sum = zeros(1,sym_size);
% Calculate all possible energy values for each state
for row = 1:2^sym_size
    % Calculate all check nodes
    for adj_row = 1:check_size
        for adj_col = 1:sym_size
            if adj_mat(adj_row,adj_col) == 1
                chk_nodes(adj_row) = chk_nodes(adj_row)*x(row,adj_col);
                chk_sum(adj_col) = chk_sum(adj_col)+chk_nodes(adj_row);
            end
        end
    end
end
% Calculate energy values
for E_idx = 1:sym_size
```

# Transition Probabilities

- Using the energy calculations, the transition matrix is generated

```
p = ones(2^sym_size,2^sym_size);  
% Flip probabilities calculated according to Eq 3.13 in T. Tithi  
% dissertation (pg. 26)  
for row = 1:2^sym_size  
    px = zeros(1,sym_size);  
    for p_idx = 1:sym_size  
        px(p_idx) = normcdf(theta,E(row,p_idx),sigma);  
    end  
    rowbin = dec2bin(row-1,sym_size);  
    for col = 1:2^sym_size  
        colbin = dec2bin(col-1,sym_size);  
        for p_idx = 1:sym_size  
            if rowbin(p_idx) == colbin(p_idx)  
                p(row,col) = p(row,col)*(1-px(p_idx));  
            else  
                p(row,col) = p(row,col)*px(p_idx);  
            end  
        end  
    end  
end
```

# Write Files and Process Outputs

- The model is written using the helper functions `write_model.m` and `write_explicit_model.m`

```
% Process Output for transient and steady state
if (tag(3) == 't' && tag(4) == 'r') || (tag(3) == 's' && tag(4)
    str_idx = regexp(output,regexptranslate('wildcard','0:\'\\(\\*\\
    output = substr(output,str_idx);
    split_output = strsplit(output,\'\\n\');
    for out_idx = 1:2^sym_size
        str_to_parse = char(split_output(out_idx));
        if (str_to_parse(1) >= "0") && (str_to_parse(1) <= "9")
            temp = textscan(str_to_parse,"%d:(%d)=%f");
```

# Write Files and Process Outputs

- ▶ The model is written using the helper functions `write_model.m` and `write_explicit_model.m`
- ▶ A system call to PRISM runs either a transient analysis, steady-state analysis, or a user-defined property analysis

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% Process Output for transient and steady state
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- ▶ The model is written using the helper functions `write_model.m` and `write_explicit_model.m`
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- ▶ The result is saved for transient and steady-state analysis

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- ▶ A system call to PRISM runs either a transient analysis, steady-state analysis, or a user-defined property analysis
- ▶ The result is saved for transient and steady-state analysis

▶ It works with some properties, but this needs to be expanded

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% Process Output for transient and steady state
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    split_output = strsplit(output,'\n');
    for out_idx = 1:length(split_output)
        str_to_parse = char(split_output(out_idx));
        if (str_to_parse(1) >= "0" && (str_to_parse(1) <= "9"))
            temp = textscan(str_to_parse,"%d:(%d)=%f");
```

# What's Next

## ► Issues and Possible Solutions



# What's Next

- ▶ Issues and Possible Solutions

- ▶ Runtime

# What's Next

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- ▶ Runtime

- ▶ Large trapping sets take a long time to run

# What's Next

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- Large trapping sets take a long time to run
- Maybe rewrite in C?

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## ► Issues and Possible Solutions

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  - Large trapping sets take a long time to run
  - Maybe rewrite in C?
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- Sample generation



# What's Next

## ► Issues and Possible Solutions

- Runtime
  - Large trapping sets take a long time to run
  - Maybe rewrite in C?
  - Need to determine if PRISM is slow or just file I/O
- Sample generation
  - Also takes a long time for large trapping sets

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## ► Issues and Possible Solutions

- Runtime
  - Large trapping sets take a long time to run
  - Maybe rewrite in C?
  - Need to determine if PRISM is slow or just file I/O
- Sample generation
  - Also takes a long time for large trapping sets
  - Maybe use some kind IS?

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## ► To do



# What's Next

## ► Issues and Possible Solutions

- Runtime
  - Large trapping sets take a long time to run
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## ► To do

- Use PRISM output to generate FER graphs

# What's Next

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  - Large trapping sets take a long time to run
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## ► To do

- Use PRISM output to generate FER graphs
  - May need to run more simulations for each initial state and take average?

# What's Next

## ► Issues and Possible Solutions

- Runtime
  - Large trapping sets take a long time to run
  - Maybe rewrite in C?
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  - Also takes a long time for large trapping sets
  - Maybe use some kind IS?

## ► To do

- Use PRISM output to generate FER graphs
  - May need to run more simulations for each initial state and take average?
- Validate tool against Tasnuva's dissertation results

# Sources

- ▶ [1] T. Tithi, “Error-Floors of the 802.3an LDPC Code for Noise Assisted Decoding”, *All Graduate Theses and Dissertations*, pp. 7465, 2019.

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- ▶ [3] T. Wadayama, K. Nakamura, M. Yagita, Y. Funahashi, S. Usami, and I. Takumi, “Gradient descent bit flipping algorithms for decoding LDPC codes”, *Communications, IEEE Transactions on*, vol. 58, no. 6, pp. 1610-1614, 2010.

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- ▶ [4] C. Winstead and E. Boutillon, “Hardware Demonstration of Noisy Gradient Descent Bit Flipping (NGDBF) for IEEE 802.3 Standard Code”.

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- ▶ [4] C. Winstead and E. Boutillon, “Hardware Demonstration of Noisy Gradient Descent Bit Flipping (NGDBF) for IEEE 802.3 Standard Code”.
- ▶ [5] “Trapping Set Ontology”,  
<https://uweb.engr.arizona.edu/~vasiclab/Projects/CodingTheory/TrappingS>  
(accessed Aug 4, 2023).