FormlSlicer: A Model Slicing Tool to Support Feature-oriented Requirements in Software Product Line

by

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Abstract

A model used in feature-oriented requirements in Software Product Line (SPL) usually contains a large number of non-trivial features; each feature may have unintended interactions with one another. It is difficult to comprehend or verify such a model. Model slicing is a useful approach to overcome such a challenge by reducing the model size while preserving the feature interactions with respect to the Feature of Interest (FOI). Model slicing evolves from traditional program slicing; it is a technique to extract a sub-model from the original model with respect to a slicing criterion. In this thesis we focus only on one type of models—the State-Based Model (SBM). Because of the difference in granularity between program and SBM, as well as the difficulty of maintaining well-formedness of a sliced SBM, slicing in SBM is much more challenging than program slicing. Among a diverse range of SBM slicing approaches, dependence-based analysis is the most popular.

We propose a unique slicing workflow on the Behaviour Model of Feature-oriented Requirements Modelling Language (FORML), a language which targets at modelling featureoriented requirements in SPL. The model consists of many feature modules; we treat each feature as a Feature-oriented state machine (FOSM). There are many variables in the environment of the model; a variable can be monitored or controlled by one or more FOSMs. The slicing workflow has two tasks—the preprocessing task and the slicing task. In the preprocessing task, we converts the model into many Control Flow Graphs (CFGs); each node in a CFG is either a TNode or an SNode, which represents a transition or a state respectively in the original model. Then, three types of dependences are computed on the CFG nodes: Hierarchy Dependence (HD), which represents the state hierarchy relation among SNodes; Data Dependence (DD), which captures the monitor-control relationship among TNodes with respect to a variable; and Control Dependence (CD), which captures the notion on whether one node can decide the execution of another node. In the slicing task, we conduct multiple slicing processes on the model; each slicing process considers one feature as the FOI and the rest of features as the Rest of System (ROS). Each slicing process undergoes a Multi-Stage Model Slicing Process, which is divided into three stages: (1) the Initiation Stage which selects the initial set of TNodes into the sliced model based on the set of variables monitored by the FOI, (2) the General Iterative Slicing Stage which uses the pre-computed dependences to add more SNodes and TNodes iteratively based on the initial sliced model, and (3) the Model Enrichment Stage which ensures that all the nodes in the sliced model are connected. In the end, the CFGs are converted back to a well-formed model as the slicing output.

A correctness proof is performed to show that a sliced model produced by this slicing workflow can simulate the original model, by proving that an execution step of a given execution trace in the original model can always be projected to an execution step of at least one execution trace in the sliced model.

We have implemented our proposed slicing workflow in a tool called FormlSlicer. We have conducted empirical evaluations and testing on FormlSlicer, to show that our proposed slicing workflow can significantly reduce model size after slicing.

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Glossary

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ACC Adaptive Cruise Control. xi, xii, 86, 91–94
BDS Basic Driving Service. 22
CC Cruise Control. 22
CD Control Dependence. 11, 14, 37, 41
CFG Control Flow Graph. 7, 10, 15, 17, 18, 28, 30, 31, 33, 38, 43, 53
DD Data Dependence. 11, 14, 23, 26, 30, 34, 35, 74
EFSM Extended Finite State Machine. 2, 11, 14, 17, 19
FCA Forward Collision Alert. xi, xii, 87, 91, 92
FOI Feature of Interest. 5–8, 24, 27, 28, 35, 44, 46, 47, 62, 63, 72, 74
FORML Feature-oriented Requirements Modelling Language. 7, 8, 12, 21–23, 25, 28, 30,
     32, 33, 37, 47, 55, 62, 65, 83
FOSD Feature-oriented Software Development. 4, 21
FOSM Feature-oriented state machine. x, 7, 8, 22–25, 28, 30–33, 35, 38, 46, 47, 55, 63,
     65, 67, 72
HC Headway Control. 4
HD Hierarchy Dependence. 30, 34
```

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LCA Lane Change Alert. xi, xii, 88, 91–93
```

LCC Lane Centring Control. xi, xii, 89, 91–93

NTSCD Non-Termination Sensitive Control Dependence. 16–18, 38

ROS Rest of System. 5–7, 24, 27, 28, 46, 47, 62, 63

SBM State-Based Model. 2, 3, 7, 11, 12, 14, 22, 38

SLC Speed Limit Control. xi, xii, 4, 90, 94

SNode A Node in CFG representing a state in FORML model. 32, 33, 43, 46, 53

SPL Software Product Line. 3, 4, 6–8, 21, 66

TNode A Node in CFG representing a transition in FORML model. 32, 33, 44, 46, 53

WCA World Change Action. 23, 25, 26, 32, 70

WCE World Change Event. 23–25, 32, 70

Chapter 1

Introduction

1.1 Model Slicing

1.1.1 What Is Model Slicing

In English, "slicing" usually refers to the act of cutting a portion from something larger with a sharp implement. In the software engineering research community, the word was firstly adopted to refer to the reduction of a software program to its minimal form which still produces a subset of the program's behaviour [2]. Since then, program slicing becomes a well-discussed topic; various slightly different notions of program slices have been proposed, as well as different methods to compute them [1]. In general, all of these methods try to extract parts of the original program that may influence a variable at some point of interest. After more than thirty years of development, program slicing has gradually become a mature source code analysis and manipulation technique, which can be used in software debugging, software maintenance, optimization, program analysis and information control flow.

As software production nowadays becomes more sophisticated, models that are used in specification become more unwieldy in scale. In recent years, researchers have begun to consider slicing from a program level to a model level [3]. Similar to program slicing, model slicing extracts a sub-model from the original model while preserving the behaviour with respect to a point of interest. Because of the graph-based nature and other features of models that are different from software program, model slicing needs to be considered as a distinct research area.

Among a diverse range of software modelling languages, State-Based Model (SBM) receives an abundant amount of attention from researchers. SBM is an umbrella term for a wide-range of related languages (Extended Finite State Machine (EFSM), UML state machines, etc.) [3]. These models are based on finite state machines which depict some sequences of execution. There are many variants on this notion; but in general, an SBM consists of a finite set of states, a set of transitions that moves from current state to next state based on an event. Many languages have defined additional features, such as global variables, hierarchical constructs, or parallelism constructs.

This thesis will mainly concern slicing on State-Based Models. In general, it is a procedure in reducing the original model to a smaller one, called the sliced model, so that the sliced model contains less number of transitions, states, or other model elements than that in the original model. At the same time, the sliced model preserves a subset of behaviours of the original model with respect to a slicing criteria. Usually, the slicing criteria refers to a set of relevant variables; it means that in spite of a smaller size, the sliced model can output the same values of these variables as the original model. Lastly, the sliced model must maintain its well-formedness as an independent SBM; it means that the model slicing procedure needs to "rewire" the SBMs to prevent nodes being orphaned.

1.1.2 Properties of a Useful Sliced Model

We believe that a useful sliced model should possess the following properties¹:

correctness

The sliced model can simulate the original model with respect to the slicing criteria;

precision

The sliced model is supposed to retain the information in the original model as much as possible;

reduction

The sliced model is supposed to be as smaller as possible than the original model.

The property of correctness is non-negotiable. The slicer is incorrect if it produces a sliced model which cannot simulate the original model with respect to a user-defined slicing criteria. Some may define correctness in a stronger sense such that not only the

 $^{^{1}}$ We summarize these based on information learnt from various literature on model slicing. See Section 2.2.5 for the literature survey.

sliced model can simulate the original model, but also the original model can simulate some observable actions of the sliced model² [4]. In this thesis, we will only enforce the first correctness property.

Sometimes, the properties of precision and reduction are opposite to each other. If a model slicer reduces the original model aggressively in order to make it as small as possible, it risks sacrificing precision. If a model slicer retains too much details of the original model, it risks sacrificing reduction.

For slicing on an SBM, if we maximize the degree of reduction and minimize the degree of precision, we may obtain a single "super" state in the sliced model such that all the original transitions become self-looping transitions of the "super" state [5]. If, on the other hand, we minimize the degree of reduction and maximize the degree of precision, we may obtain a sliced model which is exactly same as the original model. Either of these two sliced models are correct³, but not useful for comprehension purpose. Engineers will gain no useful information from either of these two sliced models.

Therefore, to make a sliced model useful, a good model slicer is supposed to strike a balance between precision and reduction. A sliced model must have appropriate trade-off between the properties of precision and reduction, while it maintains the correctness property.

1.2 Feature-oriented Model Slicing

The model slicing techniques can be applied in many different domains. This thesis will only focus on one specific domain—feature-oriented requirements in Software Product Line (SPL).

This section will present some backgrounds about feature-oriented requirements in SPL, as well as feature interactions that exist in most SPLs. Then it will discuss the importance and challenges of detecting unintended feature interactions and how model slicing is useful in overcoming the challenges.

²See Chapter 2 for more details on how researchers define correctness property of a model slicer.

³The sliced model with a "super" state is correct because the set of all its possible execution traces is a superset of the set of all possible execution traces in the original model.

1.2.1 Feature Interactions in SPL Requirements

Many organizations develop a family of similar software systems in the same domain, called an SPL. For example, an automotive manufacturer can design a series of new vehicle models that are close variants of one another. These software systems have different combinations of features. For example, the 2015 Buick Encore premium model is equipped with the Forward Collision Alert feature whilst the convenience model in the same SPL is not; yet both convenience and premium models have many other common features, such as the Traction Control feature.

In light of this, the Feature-oriented Software Development (FOSD) paradigm is usually adopted in SPL requirements. The paradigm itself advocates the use of system features as the primary criterion to identify separate concerns when developing a single software system or an SPL. A feature is defined as a cohesive set of system functionality, that can be represented as a grouping or modularization of individual requirements within the system specification [6]. By applying the FOSD paradigm in SPL requirements, an SPL model can be modelled as a finite set of feature modules, each representing one feature's requirements. Based on that, a system variant in the SPL can be obtained by selecting a subset of these feature modules.

One well-known challenge of applying the FOSD paradigm in SPL requirements is managing feature interactions. In software requirements, features are usually modelled in isolation by different groups of software engineers; this is especially the case when there are hundreds of non-trivial features. When these features are added onto a system, different features can influence one another in determining the overall properties and behaviours of their combinations [7]. In a single system, such feature interactions can still be predetermined during the modelling stage. But in an SPL, different system variants can be equipped with different subsets of all possible features, resulting in a possibly exponential number of feature combinations; therefore, detecting feature interactions in an SPL is a complicated task.

Certain feature interactions are *intended*. For example, the Call Waiting feature of a telephone service is designed to override the Basic Call Service feature's treatment of incoming calls when the subscriber is busy; the engineers who model the Call Waiting feature understand this intention and handle the feature interaction with care.

On the other hand, certain feature interactions are *unintended*. These unintended feature interactions can cause unexpected behaviour of the system and pose potential hazards to the system users. Consider the Headway Control (HC) feature and Speed Limit Control (SLC) feature, if the vehicle approaches an obstacle at a speed faster than speed

limit, both features will simultaneously send messages to the actuators responsible for controlling vehicle acceleration. If their messages are different, the behaviour of the vehicle is undefined and acceleration may be set to an unpredictable value [8].

1.2.2 Model Slicing used in Feature-oriented Requirements in SPLs

From Subsection 1.2.1, we have learnt that an SPL model can be modelled as a finite set of feature modules, each representing one feature's requirements. Also, we have learnt that detecting unintended feature interactions in an SPL model is a highly complicated task.

This is where model slicing comes into play as a useful technique.

Slicing can be performed on an SPL model with respect to only one feature, called the Feature of Interest (FOI), so that the huge SPL model can be reduced to a feasible size, while it still preserves the behaviour of the FOI. The slicing criteria is the variables related to the FOI. All the other features except the FOI form the Rest of System (ROS) in the SPL model; only a relevant portion of them will be kept after slicing. The (possibly) smaller ROS in a sliced SPL will form a "smaller context" for the FOI.

In Subsection 1.2.2.1 and Subsection 1.2.2.2, we will explain why this is useful in detecting unintended feature interactions in an SPL from the perspectives of model comprehension and model checking respectively.

1.2.2.1 Model Comprehension of Feature-oriented Requirements in SPLs

As described in Subsection 1.2.1, features are usually modelled in isolation by different groups of software engineers. When there are hundreds of features, which is typically the case in an SPL, it is likely that there are unintended feature interactions. In an industrial world, it is much better to detect and resolve these unintended feature interactions at a requirements stage, rather than at an implementation stage, in which the cost is substantially higher. However, engineers will be overwhelmed if they try to comprehend the whole SPL model. There is a fundamental limitation of human capacity to deal with such a highly complex model because there are far too many details for a single person to keep track at once [9].

Feature-oriented model slicing can facilitate model comprehension on one feature (i.e., the FOI) at a time. Because it removes irrelevant details of other features in the ROS and only keeps the portions that may (potentially) interact with the FOI, engineers can focus

on understanding the FOI together with a smaller ROS. It will be much easier to detect any unintended feature interactions between the FOI and other features.

Thus, with the help from model slicing, the complex task of detecting unintended feature interactions in a huge SPL model is decomposed into many smaller tasks, each task focuses on detecting unintended feature interactions between one feature and the others.

1.2.2.2 Compositional Verification of SPLs

To ensure safe operation of all system variants in an SPL, there is a need to provide effective and scalable means of understanding and managing feature interactions. Formal method techniques like model checking have been proposed to detect feature interactions in SPL. In the past, several strategies for SPL analysis have been proposed, in particular, family-based, product-based and feature-based strategies [10]. Family-based strategy exploits commonality among products in an SPL and delivers sound and complete analysis results; but it is often computationally infeasible as the whole SPL is too huge to be analysed in one go. Product-based strategy performs model checking on individual products in an SPL and thus faces severe scalability problems for larger sets of products. Feature-based strategy ignores interactions across feature boundaries; it is fast, but it yields incomplete analysis result.

The compositional verification is proposed as an improved analysis strategy from the feature-based approach. It verifies each feature with its smaller, relevant ROS. In each iteration of analysis, a feature (i.e., the FOI) and its smaller ROS are fed into a model checker to check whether a set of safety properties related to the FOI is maintained in all executions. The benefits of this compositional verification are evident: linear number of models to check, possible parallel verification. Also, feature interactions are taken into considerations and this can yield complete verification result.

Model slicing is an essential technique in achieving compositional verification. It creates the FOI's smaller, relevant ROS. Because feature interactions between FOI and ROS is included in model verification, the combined verification results from individual feature verification can be complete.

1.3 Thesis Overview

Generally, a feature-oriented requirements model should model each feature's requirements as a separate feature module [11]. There are many standard software-engineering modelling languages that might be suitable to declare a feature module. Among them, State-Based Model (SBM) is a suitable language to express the behaviour of a feature. In Feature-oriented Requirements Modelling Language (FORML), which is the SPL modelling language that we have chosen to perform slicing, the syntax of its feature modules is based on UML state machines, and therefore many existing slicing practices on SBM can be applied on it.

This thesis introduces a model slicing tool that aims to slice the feature modules in FORML, with respect to one feature module at a time. The tool is called **FormlSlicer** because it is slicing on FORML. In FormlSlicer, each feature module in the FORML is treated as a complete SBM, which is called a Feature-oriented state machine (FOSM).



Figure 1.1: A Comparison of the SPL Model before and after Slicing by FormlSlicer

Figure 1.1 shows a side-to-side comparison of the SPL model before and after slicing performed by FormlSlicer. The FOI remains unchanged in the sliced model. The portions that are irrelevant to FOI are removed; this results in some FOSMs in the ROS that are completely removed and some FOSMs partially removed.

FormISlicer undergoes multiple stages to produce the sliced model. It is divided into two tasks. In the preprocessing task, it needs to parse and process the whole original model into a set of Control Flow Graph (CFG)s so that it can compute the dependency relationship among the nodes in CFGs easily. In the slicing task, multiple slicing processes are created, each process treats one FOSM as the FOI, and slices all the other FOSMs with respect to the FOI. Since the slicing process starts from emptiness and gradually include model elements into slice, the FOSMs in the sliced model might become disconnected state-based machines; thus the slicing processes will undergo an "enrichment" stage to make these FOSMs to become well-formed state-based machines.

1.3.1 Thesis Statement

We can slice a feature-oriented requirements model, which consists of many FOSMs, with respect to one FOSM (i.e., the FOI), by performing the following two tasks:

- the preprocessing task, that parses the FOSMs and computes dependences,
- and the slicing task, that gradually adds model elements from the original model into the sliced model and enriches it in the end;

in order to produce a sliced model

- that can simulate the original model while keeping the constraints raised from feature interactions with the FOI,
- that achieves a satisfactory degree of reduction and precision,
- and that each FOSM in it remains as a well-formed finite state machine;

so that the sliced models generated by repeating the slicing task for all features can be useful in detecting unintended feature interactions in the SPL.

1.4 Chapter Summary

The thesis explains all the work devoted in creating FormlSlicer.

Chapter 2 shows the literature survey on a wide range of existing model slicing techniques.

Chapter 3 explains the semantics of FORML, as well as other important concepts used extensively throughout the thesis, e.g., how monitored variables and controlled variables are extracted from the feature modules in FORML.

Chapter 4 is the main chapter in the thesis. It elaborates the internals of FormlSlicer.

Chapter 5 is the theoretical evaluation of FormlSlicer. It takes on an abstract approach to prove the correctness of FormlSlicer, by showing how a sliced model produced by FormlSlicer can simulate its original model.

Chapter 6 is the empirical evaluation of FormlSlicer. There are two empirical evaluations performed on FormlSlicer.

Chapter 7 concludes the thesis and shows the contributions, challenges and possible extensions of this research work.

Chapter 2

Related Work

2.1 Program Slicing

To understand model slicing, it is better to understand first the notion of program slicing from which model slicing evolves.

The notion of a program slice was introduced by Weiser [2]. He defined a program slice S as a reduced, executable program obtained from a program P, such that S replicates part of the behaviour of P. Later, many slightly different notions of program slices have been proposed. The general notion of program slice has been summarized in an survey paper by Tip [1]: the program slice consists of the parts of a program that (potentially) affect the values computed at some point of interest. Such a point of interest is called a slicing criterion, and is typically specified by a pair (program point, set of variables). The sub-program that have direct or indirect influence on a slicing criterion C is called a program slice with respect to criterion C. The task of computing program slices is called program slicing.

Figure 2.1a [1] is an example program to show the effect of program slicing. It computes both the sum and the product of the first n positive numbers. Figure 2.1b shows its program slice with respect to a slicing criterion of (12,product). We can see that all computations that are irrelevant to the value of variable at Line 12 have been "sliced away".

Program slicing has been further divided into different categories. There is a distinction between static slicing and dynamic slicing. The former is computed without making assumptions regarding a program's input, whereas the latter relies on some selected variables and inputs [12]. Another distinction is made between forward slicing and backward slicing.

```
1 read(n);
                                        read(n);
   i := 1;
                                         i := 1;
   sum := 0;
   product := 1;
                                         product := 1;
                                         while i \le n do
   while i \le n do
6
   begin
                                         begin
 7
      sum := sum + i;
8
      product := product * i;
                                           product := product * i;
9
      i := i + 1
                                           i := i + 1
10
  \mathbf{end}:
                                        end:
   write (sum);
11
12 write (product);
                                         write (product);
             (a) The Original Program
                                               (b) Program Slice w.r.t. (12,product)
```

Figure 2.1: An Example Program [1]

Informally, a forward slice consists of all statements and control predicates dependent on the slicing criterion, i.e., the program subset that is influenced by the slicing criterion; a backward slice is the program subset that may affect the slicing criterion.

In this thesis, we will only concern static slicing and backward slicing.

2.1.1 Dependence-based Slicing

Slices are computed by finding consecutive sets of transitively relevant statements, according to data flow and control flow dependences. This is generally referred to as dependence-based slicing [13], because it involves the computation of dependence relations between the program statements. Using dependence relations information, slicing can be reduced to a simple reachability problem.

There are different computation approaches based on different graph representations of a program. Control Flow Graph (CFG) is one graph representation to capture the reachability of program statements in a program. A CFG contains a node for each statement and control predicate in the program; an edge from node i to node j indicates the possible flow of control from the former to the latter. Dependencies are defined in terms of the CFG of a program.

Dependencies arise as the result of two separate effects [14]:

- 1. First, a dependence exists between two statements whenever a variable appearing in one statement may have an incorrect value if the two statements are reversed. In the example program in Figure 2.1a, if Line 12 appears before Line 4, the value of product written will be incorrect at Line 12. Therefore we know that the statement at Line 12 is dependent on the statement at Line 4. This is Data Dependence (DD).
- 2. Second, a dependence exists between a statement and the predicate whose value immediately controls the execution of the statement. In the example program in Figure 2.1a, the statement at Line 8 is dependent on the predicate at Line 5 since the condition in the while loop at Line 5 determines whether the statement at Line 8 is executed. This is Control Dependence (CD).

2.2 Slicing on State-Based Models (SBMs)

As software production nowadays becomes more sophisticated, models that are used in specification become more unwieldy in scale. In recent years, researchers have begun to consider slicing from a program level to a model level [3]. Similar to program slicing, model slicing extracts a sub-model from the original model while preserving a subset of the original model's behaviour with respect to a slicing criterion.

2.2.1 What Is an SBM

Among a diverse range of software modelling languages, State-Based Model (SBM) receives an abundant amount of attention from researchers. SBM is an umbrella term for a wide-range of related languages (EFSM, UML state machines, etc.) [3]. These models are based on finite state machines which depict some sequences of execution. There are many variants on this notion; many languages have defined additional features, such as global variables, hierarchical constructs, or parallelism constructs [15].

The basic definition of an SBM comes from Mealy machine [16]. In general, an SBM consists of a finite set of states (including start states), a set of events (or "inputs") and a transition function that determines the next state based on the current state and event. Each transition has a source state, a destination state and a label. The label is of the form e[g]/a, where each part is optional: e is the event necessary to trigger a possible change of state; g is the guard (i.e. a boolean expression) that further constraints a possible change of state; and a is a sequence of actions (mostly updates to variables in the environment or generation of events) to be executed when the transition occurs.

The notion of an SBM with hierarchy and parallelism constructs has been introduced long time ago [15]. In a hierarchical state machine, a state may be further refined into another sub-state machine; this is a composite state. The hierarchy can be arbitrarily deep. If the state machine incorporates parallelism construct into its semantics, a state can consist of multiple orthogonal regions, each containing a sub-state machine; the sub-state machines are executing concurrently. Researchers have identified that the states in a sub-state machine follow an XOR relationship (i.e., it can be in exactly one state at a time) and the orthogonal regions in a state follow an AND relationship (i.e., when the system is in the state, it must be in all of its containing regions) [15]. Communication between concurrent SBMs can be synchronous (the SBM blocks until the receivers consume the event) or asynchronous (non-blocking).

More advanced constructs have been added to basic SBM languages to augment their expressive power. These include:

- global variables: a set of variables in the environment that can be read or written by the SBM;
- parameterised events: triggering events that come with parameters, like functions in a program;
- event generation: event can be generated by a transition's action to trigger another transition.

In this thesis, we have chosen a modelling language—FORML—which feature module is an advanced SBM that encompasses all the above-mentioned advanced constructs. More details will be elaborated in later chapters.

2.2.2 Challenges of SBM Slicing Compared to Program Slicing

It may seem easy to directly apply the techniques from program slicing on SBM slicing. But anyone who attempts to do so will find it a naive approach. There are several differences of SBM slicing compared to program slicing, each posing a non-trivial challenge in designing correct and useful SBM slicing techniques.

The first difference is the level of granularity between a program and an SBM [3]. Program slicing often operates at a line of code, which is a natural level of granularity. Program slices are thus typically subsets of the lines of code in the original program. However, the level of granularity in an SBM is unclear: an individual node may represent

the equivalent of several lines of code, or several nodes may represent the equivalent of a single line of code. Because of this difference of granularity, it is very hard to automate the translation of an SBM into a program.

The second difference is the well-formedness property between a program and an SBM. In program slicing, after removing some lines of code from the original model, the resultant program slice is still an executable, standalone program. We say that the program slice is a well-formed program. However, such a well-formedness property is not easy to maintain in SBM slicing. The well-formedness of an SBM is formally defined slightly differently depending on statistical constructs and related semantics of the different state machine modelling approaches [17]; but in this thesis, we will simply use an informal notion that a well-formed SBM slice is a standalone SBM itself. A well-formed SBM must not have orphaned transitions or states; in other words, all its states should be reachable from the default start state.

An SBM slice must be "rewired" to prevent nodes being orphaned [3]. Among the model slicing techniques we have surveyed, researchers adopt different approaches to maintain the well-formedness of an SBM slice. One approach is to completely avoid removing transitions in an SBM and only replace the triggers, guards and actions with some dummy values, such as a NONE value [18]; in this way, the sliced SBM retains the same structure as the original SBM and therefore does not risk becoming not well-formed. Another approach is to start with an SBM slice as same as the original SBM and delete only transitions that are self-looping or unreachable [5]; in this way, at each step of slicing, the sliced SBM is always well-formed. One more approach is to add an "enrichment" step as a post-processing step of a normal slicing step, so as to potentially further enrich the resulting slice with model elements in order to satisfy the well-formedness properties [17]. This thesis will follow the last approach.

There are many other differences of SBM slicing compared to program slicing: (1) most state-based modelling languages allow non-determinism, which does not exist in programs; (2) If the SBM is added with extra constructs on hierarchy or concurrency, the SBM can be in multiple states at a time; (3) the control flow in an SBM is arbitrary compared to that in a program. As what the survey paper [3] describes, by considering all these difficulties together, the SBM slicing task resembles the task of "slicing a non-deterministic set of concurrently executed procedures with arbitrary control flow". As a summary, SBM slicing is still in the early stages and there are still many challenges yet to be tackled.

2.2.3 Dependencies in SBM Slicing

As described in Subsection 2.1.1, program slices are computed according to data flow and control flow dependences. Similarly, most model slicing approaches use different dependences to compute slices.

DD is the most commonly mentioned dependence in the model slicing works. DD in an EFSM (one type of SBM languages) has been defined as [5]: DD captures the notion that one transition defines a value to a variable and another transition may potentially use this value. More formally, transition T_k is dependent on T_i with respect to variable v if (1) v is defined by T_i , (2) v is used by T_k , and (3) there exists a path (transition sequence) in the EFSM model from T_i to T_k along which v is not re-defined; such a path is referred to as definition-clear path [5]. This definition on DD will be used in this thesis.

CD in an SBM is a lot more complicated. It will be elaborated in a separate subsection 2.2.3.

Besides DD and CD, researchers have used a large variety of different dependences in their model slicers [17, 19]. Most of these dependences arise due to more advanced constructs added onto a basic SBM. We presents some of them here:

- Parallel Dependence: two states have parallel dependence if they are concurrent elements
- Synchronization Dependence: two transitions have synchronization dependence when one generates an event that the other consumes
- Refinement Control Dependence: this dependence exists between a state and the initial states of all its descendants
- Decisive Order Dependence: two nodes m and p are decisively order dependent on n when all maximal control flow paths from n contain m and p, one of them passing m before p and another of them passing p before m
- Interference Dependence: an dependence induced by concurrent reads and writes of shared variables

Unlike DD and CD which serve for more general purposes in model slicing, each of the above-mentioned dependences is only restricted to some advanced SBMs with special semantics. In spite of this, they are useful in showing that one of the best ways to cope with an SBM with more complex semantics is to improve the dependence-based slicing technique by including more types of dependences.

Control Dependence

In program slicing, control dependence is traditionally defined in terms of a post-dominance relation in a CFG [14, 20]. Intuitively, a node n_i is post-dominated by a node n_j in a CFG if in every execution of the program, n_j always occurs after n_i . Having calculated the post-dominance relation in a CFG, the control dependence relation can be obtained according to this: a statement n_j is said to be control dependent on a statement n_i if there exists a nontrivial path p from n_i to n_j such that every statement $n_k \neq n_i$ in p is post-dominated by n_j and n_i is not post-dominated by n_j .

Although this definition of control dependence is widely used in program slicing, there are some other slightly different definitions as well. Researchers have distinguished two different notions on control dependence—strong control dependence and weak control dependence [21]:

- 1. n_j is strongly control dependent on n_i if there is a path from n_i to n_j that does not contain the immediate post-dominator of n_i ;
- 2. n_j is weakly control dependent on n_i if n_j strongly post-dominates n_k , a successor of n_i , but does not strongly post-dominates n_l , another successor of n_i .

The notion of strong control dependence is similar to the traditional notion, except that it captures both direct and indirect control dependences. For example, if n1 is control dependent on n2 and n2 is control dependent on n3, then n3 is strongly control dependent on n1, which is not the case in the traditional definition of control dependence. Other than that, it roughly corresponds to the traditional definition in [14, 20].

Weak control dependence shows a dependence relationship between the predicate condition of a loop (i.e. the branching node in a CFG) and a statement outside the loop that may be executed after the loop is exited, while strong control dependence does not [21]. Re-consider the program in Figure 2.1a; the statement at Line 11 is weakly control dependent, but not strongly control dependent, on the predicate condition at Line 5.

As we can see, both the traditional control dependence and strong control dependence ignores the possibility of an infinite loop. They determine that a statement outside the loop (e.g. Line 11 in Figure 2.1a) must always be executed after the predicate condition (e.g. Line 5), and therefore the latter is post-dominated by the former. In other words, they are non-termination insensitive [22]. However, they are widely used in most program slicing tasks which focus on debugging and program visualization and understanding; these slicing tasks do not consider preserving non-termination properties as an important requirement.

Because the post-dominance relation assumes a single end node in the CFG, all of these definitions of control dependence assume that the single end node property in CFG is satisfied.

The traditional definition on control dependence has been applied in model slicing. Korel et al. [5] presents the definition for control dependence between transitions in terms of the concept of post-dominance: a state Z post-dominates another state Y iff Z is on every path from Y to the exit state; Z post-dominates a transition T, which is an outgoing transition of Y, iff Z is on every path from Y to the exit state through T. Based on the concept of post-dominance, control dependence is defined as:

Definition (Control Dependence [5]). Transition T_i has control dependence on transition T_k (transition T_k is control dependent on transition T_i) if (1) T_k 's source state does not post-dominate T_i 's source state, and (2) T_k 's source state post-dominates transition T_i .

This definition captures the traditional notion of control dependence. However, as the traditional notion is only applicable to program CFGs with single end node, this definition is also limited to SBMs with single end node.

Later, some researchers in program slicing community have recognized that these traditional notions on control dependence are no longer applicable to most modern programs. Ranganath et al.[22] have identified two trends in modern program structures:

- 1. Many methods in modern programs raise exceptions or include multiple returns. This means that their corresponding program CFGs have multiple end nodes.
- 2. There is an increasing number of reactive programs with control loops that are designed to run indefinitely. This means that their corresponding CFGs have no end node.

Therefore, in most modern programs, their corresponding CFGs do not satisfy the single end node property. Ranganath et al.[22] proposed a new definition on control dependence:

Definition (Non-Termination Sensitive Control Dependence (NTSCD) [22]). In a CFG, n_j is (directly) non-termination sensitive control dependent on node n_i if n_i has at least two successors, n_k and n_l ,

1. for all maximal paths from n_k , n_j always occurs and it occurs before any occurrence of n_i ;

2. there exists a maximal path from n_l on which either n_j does not occur, or n_j is strictly preceded by n_i .

The key observation on NTSCD is that reaching again a start node in a loop is analogous to reaching an end node. This intuition is similar to weak control dependence [21] which considers that an infinite loop is important in determining control dependence. This implies that NTSCD is non-termination sensitive [22], like the notion on weak control dependence. In addition, NTSCD gets rid of the concept of post-dominance and uses the concept of a maximal path. A maximal path is any path that terminates in a final transition, or is infinite [23]. The consideration of maximal paths imply that NTSCD is applicable to CFGs that do not satisfy the single end node property.

There are more "advanced" definitions that extend the definition on NTSCD. In summary, these definitions replace the "maximal paths" in NTSCD to other types of paths [23].

- By replacing "maximal paths" with "sink-bounded paths" we obtain the definition on Non-Termination Insensitive Control Dependence (NTICD). This definition does not calculate control dependences within control sinks¹ [22].
- By replacing "maximal paths" with "unfair sink-bounded paths" we obtain the definition on Unfair Non-Termination Insensitive Control Dependence (UNTICD). This definition is in essence a version of NTICD modified to EFSMs rather than CFGs [24].

As a summary, we can see that the definition of control dependence has been improved by researchers in several generations, because of a change in modern program structures and a need to apply control dependence from program slicing to model slicing. Nevertheless, they all aim to capture the dependence that one node is determining the execution of another node. Among a diverse range of definitions, this thesis will simply choose the NTSCD as a guideline in implementing the control dependence computation and follow an algorithm presented by Ranganath et al. [22] with some modifications to fit our own needs. Since the algorithm is used in CFGs, our model slicer will also want to convert the original model into its CFG representation.

¹A control sink is a set of nodes that form a strongly connected component such that for each node n in the control sink each successor of n is also in the control sink [22]

2.2.4 Relevant SBM Slicing Techniques

One of the main tasks for this thesis project is to implement a model slicer. Therefore our literature survey focuses more on implementations. In an implementation document for a slicer of UML State Machine [18], a CFG is constructed to capture all the possible executions of the UML state machines. There are different types of CFG nodes, including BRANCH, SIMPLE and SEND. We observe that the conversion of CFG from model makes it easy for the slicer to directly use the notion of NTSCD as defined in [22].

Many literature on SBM slicing present their respective slicing algorithms. In general, there are two approaches.

- 1. In the first approach, the algorithm incrementally removes model elements. The slicing algorithm presented in [5] starts with an initial slice which is as same as the original model. Initially, all transitions are marked as non-contributing transitions. Then the algorithm repeatedly marks some transitions as contributing transitions based on pre-computed dependences. At the end, only unreachable transitions or self-looping, non-contributing transitions are deleted from the slice.
- 2. In the second approach, the slicing algorithm incrementally adds model elements. The slicing algorithm presented in [17] starts with an initial slice which solely contains the model elements of the slicing criterion, and adds more model elements incrementally based on pre-computed dependences; after each addition, a model enrichment step is carried out as a post-processing step to satisfy the well-formedness properties of the slice. At the end of all iterations, one more step is performed to remove unreachable states in the slice.

In Section 2.2.3, we have also shown a wide range of dependences used in many slicing algorithms. They show that one of the best ways to cope with an SBM with more complex semantics is to improve the dependence-based slicing technique by including more types of dependences.

Altogether, these literature have given us several ideas on designing our own model slicing algorithm: (1) slicing needs to be performed in an iterative way to incrementally add or remove more model elements into slice (we will choose the former in this thesis); (2) there can be more types of dependences besides data and control dependences, if the SBM has more complex constructs such as hierarchy or concurrency; (3) dependences are precomputed and can be used repeatedly during slicing steps; (4) converting the model into the CFG representation makes the data structure lightweight for dependences computation; (5)

an enrichment step can be added as a post-processing step to maintain the well-formedness of the model.

2.2.5 Correctness of SBM Slices

As introduced in Section 1.1.2, a useful sliced model should be correct, precise and reduced. We summarize these properties based on information learnt from literature on evaluating an SBM slice.

First of all, the basic correctness property has been mentioned in various literature. The first condition for a sliced EFSM, as listed by Korel et al.[5] is as follows:

Let M be an EFSM model. Let v be a variable at transition T_I in M. An EFSM sub-model M' is a non-deterministic slice of M with respect to variable v at transition T_I if for every input x the value of v at T_I during execution of M is equal to the value of v at T_I during at least one possible execution of M' on x.

In Amtoft et al.'s research note on SBM slicing correctness [4], the same condition is phrased differently:

If the original program can do some observable action then also the sliced program can do that action; here an observable action may be defined either as one that is part of the slicing criterion, or as one that is part of the slice.

In this thesis, the same condition is expressed as that the sliced model can simulate the original model with respect to the slicing criteria. Chapter 5 will prove this basic correctness property on the model slicer we have developed.

However, many have recognized that such a correctness property is not sufficient. If a slice only satisfies the basic correctness property, it might be "over-minimized" making it useless, if not misleading, for comprehension purposes [5]. Korel et al. has illustrated an example of such an "over-minimized" slice: the SBM becomes a single state such that all relevant transitions become self-looping transitions on this state. Certainly, this sliced model can satisfy the basic correctness property, because there definitely exists an execution in the sliced model that can simulate an execution in the original model. However, this sliced model is not useful.

Because of that, researchers have imposed a second condition on the sliced model; that means the correctness property will become "stronger" if both conditions are satisfied. The second condition is to ensure that the original model can simulate the sliced model. Korel et al. refers to this second condition as a *traversability property* and proposed two state merging rules that satisfy this condition.

This raises another problem. In order to satisfy this "strong" correctness property, the sliced model needs to be as close as possible to the original model. In the worst case, slicing does not remove anything from the original model (or in the approach of incremental addition, adds the whole original model to the slice). If the sliced model is same as the original model, it will be correct but not useful. We still want to reduce the size of the slice as much as possible. This prompts us to separate the two properties of precision and reduction.

Precision property corresponds to the "strong" correctness property, with some differences: a sliced model does or does not satisfy the "strong" correctness property (a yes-or-no answer), but can be precise to a different degree. In this thesis, we will use the two state merging rules proposed by Korel et al. which satisfy the "strong" correctness property. But in all other cases, we will favour reduction over precision.

Chapter 3

Preliminaries

This chapter presents the preliminaries before the design of FormlSlicer. Section 3.1 introduces the semantics of FORML [11] and explains how FormlSlicer treats the feature modules in FORML. Then Section 3.2 discusses the scope of FormlSlicer. Lastly, Section 3.3 illustrates a big picture of the slicing task and how FormlSlicer extracts monitored and controlled variables.

3.1 What is FORML

FORML is a modelling language designed to specify feature-oriented models of SPL requirements. It is based on the paradigm of FOSD and accompanied by a taxonomy for explicitly modelling intended feature interactions [25]. A model expressed in this language consists of two major portions: a World Model, which is a description of the world in terms of a set of concepts and the relationships between them, and a Behaviour Model, which is structured in terms of many feature modules. Each feature module specifies the behaviour of one feature. If a feature is independent of existing features, then the module is expressed as a fully executable state machine. If a feature enhances (i.e., extends or modifies) existing features, the enhancements are expressed as a set of state-machine fragments that extend existing feature modules [11].

There are many reasons why we choose FORML. The most important ones are:

• FORML is a UML-like language. Its feature modules are designed based on UML state machine, which is one type of State-Based Model (SBM). This makes the design

of our slicing tool much easier, because we can utilize some existing literature on SBM slicing.

• It is a good practice in software engineering research community to adopt and extend state-of-the-art analysis tools [26]. FORML is initially designed as a precise modelling language within NECSIS Theme 3¹ and there have been a few tools developed within the research group to manipulate the language, including FORML Feature Composer and a collection of transformation tools from FORML to SMV [26]—a modelling language used in model checking by the NuSMV model checker [28]. It is beneficial to the community in further extending this line of works by creating a model slicer to support the compositional model verification.

FormlSlicer treats each feature module in FORML as a state machine. If a feature is an independent feature (e.g., the Basic Driving Service (BDS) feature which controls basic acceleration, deceleration and steering functionalities of a car), the feature module is treated as a complete state machine. If a feature is an enhancement or modification of another feature (e.g., the Cruise Control (CC) feature which is built on top of the BDS feature), the feature module is represented as a fragment in FORML. However, we will compose the fragmented feature module with its base feature modules together to create one complete state machine.

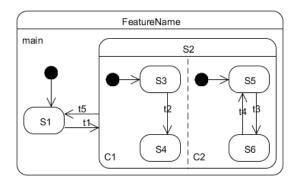


Figure 3.1: The Structure of FOSM in FormlSlicer

We call such a complete state machine as a Feature-oriented state machine (FOSM) to indicate that it is a composed feature in the format of a state machine.

An FOSM is the sub-state machine contained within the main region of a composite state carrying the name of the feature. A typical example of an FOSM is shown in Figure 3.1. This FOSM contains two states, S1 and S2. S1 is a basic state. S2 is a composite state which consist of two orthogonal regions, C1 and C2. The state and region form a

¹The Network for the Engineering of Complex Software-Intensive Systems for Automotive Systems (NECSIS) is a research network to tackle the obstacles and develop new Model Drive Engineering capabilities that lead to the development of the next generation of MDE methods and tools. This project, Feature Oriented Modelling and Analysis, groups activities within the NECSIS *Theme 3*: Uncertainty, Adaptability, and Variability [27].

containment relation in hierarchy (each composite state contains one or more regions; each region contains a sub-state machine). We can see that such a mutual relationship between state and region is recursive. The black solid circle, called *pseudo state*, is a notation to point to the default start state. For example, S1, S3 and S5 in Figure 3.1 are default start states in their respective region.

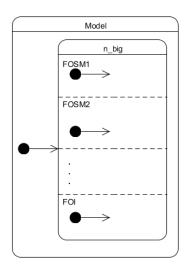


Figure 3.2: An Example Model

FormISlicer treats the whole Behaviour Model as one big state machine. This big state machine only has a composite state containing many orthogonal regions. Each orthogonal region contains one sub-state machine, which is an FOSM. Figure 3.2 shows an example of such a big state machine in FormISlicer.

Strictly speaking, this is not an SPL model, because:

- the FOSMs in different orthogonal regions are likely to have overlapping components;
- the FOSMs may be mutually exclusive features.

In some literature, this is called an 150% model [29]. The 150% model contains the behaviour of all features, no matter if those features exclude each other within a configuration of the SPL. The 150% model can be converted to an SPL model and vice versa.

Throughout the thesis, we are going to use the following definitions adapted from Pourya's PhD thesis [11] to access information about state hierarchy in a state machine:

The root of the state hierarchy represents the state machine, which is a composite state itself. The ancestors of a state x are all of the nodes along the path from the root node to x. The descendants of a node x are all of the states in the subtrees of x. The rank of a node x in the state hierarchy is the length of the path from the root to x. The least common ancestor of a state x1 and a state x2 is the maximum-rank node that has both x1 and x2 as descendants.

The transition in an FOSM has the following format:

```
id: te[gc]/al_1...al_n
```

where id is the name of the transition, te is an optional trigger expression, or called World Change Event (WCE), gc is an optional guard condition, and $al_1...al_n$ are labels that specify a set of concurrent actions, or called World Change Action (WCA). Section 3.3.1 will explain how FormlSlicer extracts information from the transition.

3.2 Scope of FormlSlicer

The task of FormlSlicer is to produce a sliced model, in which some model elements that are irrelevant to our interest are removed.

FormISlicer does not resolve conflicts which arise from unintended feature interactions. However, it keeps the conflicts in the sliced model; because the sliced model has a smaller size than the original model, the conflicts become much more obvious and easily detectable.

FormISlicer does not compose feature modules in FORML. The FOSMs must be composed first before being passed to FormISlicer as inputs.

FormISlicer does not deal with a real SPL model. As introduced in the previous section, it takes in the 150% model. However, the 150% model can be converted to an SPL model and vice versa.

FormISlicer focuses slicing on the feature modules in the Behaviour Model of FORML. It does not perform slicing on the World Model, which is the world domain designed based on UML class diagram. However, it is very easy to perform slicing on the World Model by using the set of relevant variables in FormISlicer's slicing output. We can simply identify those fields that are not in the set of relevant variables and slice them away from the World Model; if all fields in a class are sliced away, we slice away the class as well. This can be done either manually, or by writing a small program to automate it.

Form Slicer imposes certain restrictions on the input model.

The first restriction is that transitions crossing two parallel orthogonal regions (i.e., different regions that are contained by the same composite state) are not allowed. The ultimate reason of having concurrent regions in a model is to simulate multiple threads in a program. Although different threads can interact with one another by accessing a shared memory, it is illogical that a running thread suddenly reaches the middle of execution of another thread. Similarly, executions in different orthogonal regions can affect one another

by generating or receiving the same event (i.e., one transition generates the event in WCA and another transition listens to that event in WCE), but not transiting from one state to another state crossing two parallel regions.

The second restriction is that if a state is within an orthogonal region which has another parallel orthogonal region (i.e., it is part of a concurrency construct), any transitions crossing hierarchy boundary from or to this state are not allowed. This kind of transition is illustrated in Figure 3.3. Because FormlSlicer has many other more important challenges to solve, we do not want to further complicate FormlSlicer by considering this special case which occur very rarely in real-life models.

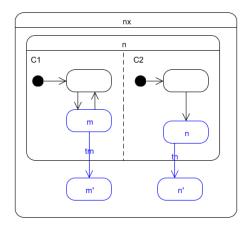


Figure 3.3: Concurrent Transitions crossing Hierarchy Border are not allowed in FormlSlicer

3.3 The Big Picture of Slicing Environment

Figure 3.4 shows the big picture of environment during one iteration of the slicing task.

In Section 3.1, we have introduced that a model consists of many FOSMs, each representing a feature in the SPL. One of them is the FOI. The FOI is the feature that we are interested in. All other features need to be sliced so that only the components that are relevant to FOI are kept in the sliced model. We say that all these other features form the ROS.

In each of all the iterations of the slicing task, a different FOSM is selected to be the FOI.

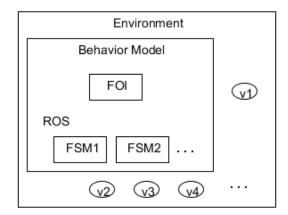


Figure 3.4: The Big Picture of Slicing Environment in FormlSlicer

There are a collection of variables that are influencing the behaviours of one or more features. They are divided into two groups:

- The first group is the set of environment-controlled variables, i.e., their values can only be changed by the external environment. We use V_{env} to refer to this set of variables. As an example, consider the actual speed of a car; its value can only be a result of a combination of external and internal factors. No equipped features of the car can directly modify the actual speed; instead, they can only monitor it.
- The second group is the set of system-controlled variables, i.e., their values can be influenced by one or more FOSMs. We use V_{sys} to represent them. For example, the acceleration of a car is a system-controlled variable.

Monitored Variables represent phenomena that are sensed by or inputs to the system; controlled Variables represent phenomena that are controlled or affected by system outputs [30]. Based on the definitions, we know that any $v \in V_{env}$ can only be monitored variables.

3.3.1 How FormlSlicer Extracts Monitored and Controlled Variables

In the previous section, we introduce the definitions on monitored variables and controlled variables of an FOSM. The same definitions apply to a transition as well.

We can extract the monitored variables of a transition from its WCE, as shown in Table 3.1. We can also extract the monitored and controlled variables of a transition from its WCA, as shown in Table 3.2.

In FORML, some message objects that are generated by a transition t_1 can be received by another transition t_2^2 ; in this case, the message object C appears in the WCE of t_2 (i.e., C+(o)) and in the WCA of t_1 (i.e., +C(list(param=e))). In order to match t_1 and t_2 , FormlSlicer use the same String "+C" as a monitored variable of t_2 and a controlled variable of t_1 .

WCE Type	WCE Format	Monitored Variable
Message Object C Appear	C+(o)	+C
Message Object C Disappear	C-(o)	-C
Attribute in Message Object C Change Value	C.a~(o)	C.a

Table 3.1: How FormlSlicer extracts Monitored Variables from WCE

In Table 3.1, the first two columns show the types and formats of WCE in a FORML transition. The types include: creation of a message object, deletion of a message object, and changing value of an attribute of a message object. The third column shows how FormISlicer converts each of them into a monitored variable.

WCA Type	WCA Format	Monitored Variable	Controlled Variable
Generate Message Object C	+C(list(param = e))		+C
Destroy Message Object C	C-(O)		- <i>C</i>
Assignment Action	$v := \text{function}(v1, v2, \dots)$	v1,v2,	v

Table 3.2: How FormlSlicer extracts Monitored/Controlled Variables from WCA

Table 3.2 shows how FormlSlicer deals with different types of WCA. The first two columns show the three types and formats of WCA in FORML, including generation of a message object, deletion of a message object³, and assignment. The fourth column specifies how FormlSlicer converts each of them into a controlled variable. In the type of assignment action, there are also monitored variables in the arguments of the function, as shown in the third column.

²This is the construct of event generation. See Section 2.2.1 that many SBMs have this advanced construct.

³In FORML, when an action destroys a message object, it needs to specify exactly what set of objects are destroyed; but in FormlSlicer we are going to over-approximate the influence of this action by saying that all the objects belonging to that category of message are destroyed.

The guard expression can be one of the three different types, as shown in the first two columns in Table 3.3. In particular, the guard condition of inState(DummyState) is an interesting construct. It means that this guard condition is only true when the model's current state configuration contains the state DummyState. The third column shows how FormISlicer converts each of the different types of guard expression into monitored variables.

Guard Type	Guard Format	Monitored Variable
Comparison	var1 >var2	var1, var2
InState	inState(DummyState)	DummyState
Function	function1(var1) == 5	var1

Table 3.3: How FormlSlicer extracts Monitored Variables from Guard

All the monitored variables in a transition t form a set mv(t). All the controlled variables in a transition t form a set $cv(t)^4$.

The "o" notation in a Transition One may have observed that there is sometimes an "o" written inside the brackets of a WCE or function parameters. In FORML, it refers to the current message object. FormlSlicer will simply replace this "o" with its corresponding WCE. For example, if a transition is expressed as "t1: SetHeadway+(o)/a1: HC.headway:=o.dist", then SetHeadway.dist is considered as the monitored variable for the WCA a1.

Only the monitored variables of the FOI will be used as a slicing criterion to select the initial set of transitions in other FOSMs in ROS. But the controlled variables of the FOI are not. The key principle of slicing in FormlSlicer is that it only concerns with how the other FOSMs influence the FOI, but not with how the FOI influence the other FOSMs.

⁴See Chapter 5 for more usage on mv(t) and cv(t).

Chapter 4

A Full Picture of FormlSlicer's Internals

This chapter explains the design of FormlSlicer in the order of its workflow.

4.1 Overview of FormlSlicer's Workflow

Figure 4.1 shows the big picture of FormlSlicer's workflow. It consists of two major tasks: the preprocessing task and the slicing task.

The original model, which consists of multiple FOSMs, is input to the preprocessing task. The task converts this model into a group of CFGs. Based on these CFGs, the task computes three types of dependences and stores the generated results in different tables.

Next, FormlSlicer forks off multiple slicing processes to perform the slicing task. All the slicing processes are sharing the same resources on dependences and CFGs generated from the preprocessing task. Each slicing process considers a different FOSM as its FOI and treats the rest of FOSMs as the ROS. Then it goes through a multi-stage model slicing process to slice the FOSMs in ROS with respect to the selected FOI. Eventually, it outputs a sliced model.

The different slicing processes are doing their slicing jobs independently, although they are reading the same inputs. The use of concurrent threads in FormlSlicer greatly saves the time that will otherwise be spent on slicing the big model linearly.

The next three sections will explore further into the internals of the preprocessing task and the slicing task.

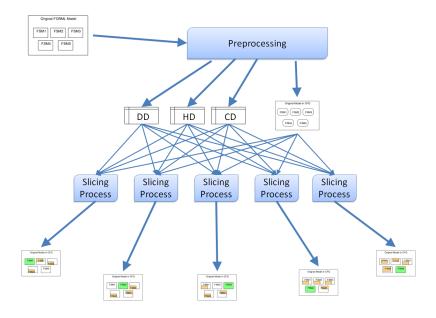


Figure 4.1: Overview of FormlSlicer's Workflow: the Preprocessing Task and the Slicing Task

Section 4.2 and Section 4.3 presents the preprocessing task. It starts with a parser and a converter from the input model to CFG, then presents three types of dependences, including Hierarchy Dependence (HD), Data Dependence (DD) and Hierarchy Dependence (HD).

Section 4.4 presents the workflow for one slicing process. The slicing is performed only on the FOSMs in the ROS. This section presents the multiple stages of the slicing process, including the Initiation Stage that utilizes a Variable Extractor, the General Iterative Slicing Stage that utilizes the dependences, and the Model Enrichment Stage that defragments all resulting FOSMs to make them well-formed state machines.

This is a list of the sub-tasks performed in FormlSlicer:

1. Preprocessing Task

- (a) Parse and Convert the input model to CFGs
- (b) Compute Hierarchy Dependence
- (c) Compute Data Dependence

- (d) Compute Control Dependence
- 2. Slicing Task
 - (a) Initiation Stage
 - i. Variable Extraction Step
 - ii. Initial Transition Selection Step
 - (b) General Iterative Slicing Stage
 - i. DD Step
 - ii. Replacing Cross-Hierarchy Transitions
 - iii. Transition-to-State Step
 - iv. CD-HD Step
 - (c) Model Enrichment Stage
 - i. Step I: State Merging Step
 - ii. Step II: True Transitions Creation

4.2 Preprocessing: Model Parsing and Conversion from FORML to CFG

FormISlicer is equipped with a simple parser to read an input model. Each FOSM in the input model must be written in the format as shown in Table 4.1 and placed in the same folder. We need to declare all the components inside an FOSM, including the states, the regions, the transitions and the macros.

Item to be Declared	Declaration Format
Feature	$\text{feature } \langle \text{feature name} \rangle$
Macro	macro $\langle \text{input sequence} \rangle \langle \text{replacement output sequence} \rangle$
State	state $\langle \text{state name} \rangle \langle \text{parent region} \rangle \langle \text{first state in region?} \rangle \langle \text{composite state?} \rangle$
Transition	transition $\langle \text{transition name} \rangle \langle \text{expression} \rangle \langle \text{source state} \rangle \langle \text{destination state} \rangle$

Table 4.1: Format of an Input/Output File to Specify one FOSM

A simple input example is shown below to declare an FOSM from Figure 3.1.

```
Feature.txt
```

```
feature FeatureName
region main FeatureName.main true false
state S1 FeatureName.main true false
state S2 FeatureName.main false true
transition t1 t1:E1+(o)/a1:x:=1; FeatureName.main.S1 FeatureName.main.S2
transition t5 t5:E1-(o)/a1:x:=0; FeatureName.main.S2 FeatureName.main.S1
region C1 FeatureName.main.S2
region C2 FeatureName.main.S2
state S3 FeatureName.main.S2.C1 true false
state S4 FeatureName.main.S2.C1 false false
transition t2 t2:[inState(FeatureName.main.S2.C2.S6)]/ FeatureName.main.S2.C1.S3 FeatureName.main.S2.C1.S4
state S5 FeatureName.main.S2.C2 true false
state S6 FeatureName.main.S2.C2 false false
transition t3 t3:E2+(o)/ FeatureName.main.S2.C2.S5 FeatureName.main.S2.C2.S6
transition t4 t4:[a=='val']/ FeatureName.main.S2.C2.S6 FeatureName.main.S2.C2.S5
```

4.2.1 Control Flow Graph

Control Flow Graph is a directed graph, usually seen in compiler analysis to represent all execution paths through a program during its execution [31]. This concept is also useful in model slicing. As introduced in Chapter 2, some model slicers [19] convert a model into CFGs before slicing. FormISlicer will do the same conversion.

The main benefit of converting an input model into CFGs is to simplify the representation of the model so that it becomes easy for further processing, particularly for the dependences computations.

A CFG only consists of nodes and edges. As shown in Figure 4.2, there are two types of nodes, TNode and SNode, which all belong to the generic type Node. Each Node has an ID, a set of outgoing nodes, and a set of incoming nodes.

TNode

FormISlicer will convert each transition into a TNode. A TN-ode contains the set of monitored variables and controlled variables of its corresponding transition.

The set of outgoing nodes and the set of incoming nodes of a transition are both singleton. They are IDs of the source and destination state of that transition respectively.

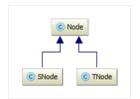


Figure 4.2: The Class Hierarchy of Node, TNode and SNode in CFG

SNode

FormISlicer will convert each state into an SNode. SNode is simpler than TNode. It does not contain more information other than the generic information (its own ID and sets of outgoing and incoming nodes' IDs) inherited from the generic type Node.

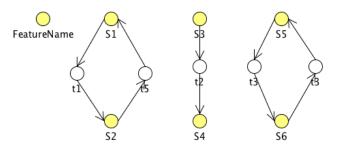


Figure 4.3: Several CFGs that are Converted from the FORML FOSM. Yellow Nodes are SNodes.

After Conversion After the conversion, each FOSM in the input model will become one or more CFGs. The FOSM example in Figure 3.1 becomes the CFGs in Figure 4.3. We can see that there is one distinctly connected CFG for each sub-state machine in this example. But if there is a transition that crosses the hierarchy border, it will be converted into a TNode that connects two distinct CFGs together.

When the CFGs for the input model are ready, it is time to move on to the next preprocessing step—dependences computation.

4.3 Preprocessing: Dependence Computation

FormlSlicer starts from an empty slice set and gradually adds model components into it. In this slicing strategy, the dependences among nodes (including SNodes and TNodes) are very important information for FormlSlicer to determine which nodes should be selected into the slice set.

In the previous section, we have discussed that the FOSMs in the input model have been converted into CFGs. CFG is a lightweight graph structure suitable for the dependence

computation, because dependence computation concerns only the connectivity relationship among nodes.

This section introduces three types of dependences that are computed by FormlSlicer.

4.3.1 Hierarchy Dependence

The states in a FORML model are organized in a hierarchy. A state may be a composite state which contains one or multiple regions; each region contains a sub-state machine which consists of more states, called the *child states* of the composite state. On the other hand, the composite state is called the *parent state* of the *child states*. As an example, Figure 4.4 shows such a state hierarchy; state n1 resides within region1 of state n2 and thus n1 is n2's child state and n2 is n1's parent state. The first state immediately after the pseudo state in the region is called the $default \ start \ child \ state^1$ of its parent state.

Hierarchy Dependence (HD) is a dependence to reflect such a state hierarchy relationship among nodes. We say that n1 is **hierarchy dependent** on n2, denoted as $n1 \xrightarrow{hd} n2$.

FormISlicer computes the HD while performing the CFG conversion. It keeps two tables to record the results:

HDtable1 a 1D-table mapping each SNode to its parent SNode

HDtable2 a 2D-table mapping each SNode to its default start child states²

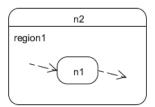


Figure 4.4: Hierarchy Dependence

4.3.2 Data Dependence

As introduced in Chapter 2, Data Dependence (DD) usually depicts the "define-use" relationship among different instructions in a program. The notion is also applicable in model slicing.

¹The arrow from a pseudo state to its default start child state (i.e., the state pointed by the arrow from the pseudo state) cannot be labelled. If users need a transition from the pseudo state to its default start state, users can make the original pseudo state as a new default start state and create a new pseudo state to point to it.

²A composite state can contain multiple regions and therefore can have multiple default start child states.

TNode A can be data dependent on TNode B with respect to a certain variable, if TNode A is monitoring that variable and TNode B is controlling that variable, and there are no other TNodes between TNode A and TNode B which interfere the controlling effect of TNode B.

To put it formally, we say t_k is **data dependent** on t_1 with respect to v, denoted as $t_k \xrightarrow{dd}_v t_1$, iff there exists a variable $v \in mv(t_k) \cap cv(t_1)$ and there exists a path $[t_1 \cdots t_k](k \ge 1)$ such that $v \notin cv(t_j)$ for all 1 < j < k. Here, t represents a TNode in a CFG produced by FormlSlicer, v represents a system-controlled variable, mv(t) and cv(t) are monitored and controlled variables contained in t respectively³.

The path of $[t_1 \cdots t_k](k \geq 1)$ such that $v \notin cv(t_j)$ for all 1 < j < k is called a **definition-clear path**.

Figure 4.5 has illustrated this concept.

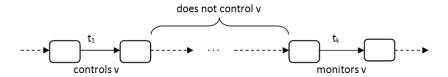


Figure 4.5: Data Dependence between t_k and t_1 w.r.t. v

DD is the most important dependence among the three. The concepts of monitored and controlled variables are specially used by it. At the end of Chapter 3, we say that FormlSlicer only concerns with how the other FOSMs influence the FOI, but not with how the FOI influence the other FOSMs. In general, FormlSlicer is looking for relevant parts in the other FOSMs which the FOI is (directly or indirectly) data dependent on.

InState Dependence FORML has a special type of guard condition called "InState". In the example shown in Figure 4.6, transition T2 contains the guard condition of "InState(DummyState)", then T2 will be triggered when the current state configuration of the model contains the state of *DummyState*. For consistency, FormlSlicer treats InState Dependence as a sub-type of Data Dependence. In this example, FormlSlicer considers T2 as data dependent on all the incoming transitions to *DummyState*, e.g., T1, with respect to the variable "DummyState". FormlSlicer will stores this information as a data dependence entry in the computation results of DD.

³See Section 3.3 on definitions on system-controlled variables, monitored and controlled variables.

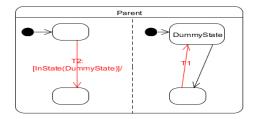


Figure 4.6: InState Dependence as a Variation of Data Dependence

Algorithm 4.1 shows how FormlSlicer computes data dependence. Compared to existing algorithms, ours is dealing with a more complex model with state hierarchy structure. The computation results are stored in a table:

DDtable a 1D-table mapping each variable to a pair of TNodes such that the left one is dependent on the right one

Algorithm 4.1 traces from a TNode with a controlled variable v to another reachable TNode which monitors v, and thereby establishes data dependence between the two TNodes. In each loop of the *foreach* statement at Line 1, the algorithm checks whether a node has controlled variables. If there are some controlled variables, it loops for each variable at Line 4 to search for nodes that are data dependent with respect to this particular variable. The algorithm uses a queue v to perform the searching. At each iteration of the v while loop at Line 8, it polls one node from v and checks whether that node is monitoring the variable. If so, data dependence is established between the starting node and the polled node, as shown at Line 21.

The *foreach* statement at Line 24 is checking whether *currNode* is controlling the variable v. If so, it means that the definition-clear path between *node1* and any other nodes reachable from *node1* beyond *currNode* is cut off, and so there is no need to continue the search beyond *currNode*.

Algorithm 4.1: Algorithm of Data Dependence Computation used in FormlSlicer

```
Input: allNodes, HDtable2
    Output: DDtable
 1 foreach node1 in allNodes do
         if node1 instanceof SNode OR node1.controlledVar = null then continue;
         set controlleds := node1.controlledVars // node1's controlled variables
 3
 4
         foreach v in controlleds do
              set \ visitedSNodes := \{\} \ // \ Empty \ visitedSNodes
 5
              \mathbf{set}\ qt := [\mathit{the\ outgoing\ node\ of\ node1}]\ \ //\ \ \mathtt{Initialize\ qt}
 6
              set dependentOn := an empty pair consisting of two Nodes
              while qt is not empty do
 8
                   set currNode := qt.poll();
 9
10
                   if currNode == node1 then continue;
                   if currNode instanceof SNode then
11
12
                         {\bf if}\ {\it visited SNodes}\ {\it contains}\ {\it currNode}\ {\bf then}\ {\bf continue};
                         if HDtable2 contains currNode then
13
                             ADD the all the default start child SNodes of currNode to qt
14
                        end
15
                         ADD all the outgoing nodes of currNode to qt
16
17
                         ADD currNode to visitedSNodes
                   else
18
                         if dd contains v \rightarrow (currNode, node1) then continue;
19
                         \mathbf{if} \ \mathit{currNode.monitoredVars} \ \mathit{contains} \ v \ \mathbf{then}
20
                          ADD (currNode,node1) to dependentOn;
21
22
                         end
                         \mathbf{set}\ isContVRset:=false
23
                         foreach c in currNode.monitoredVars do
24
25
                              if c == v then
                                   set isContVReset := true;
26
                                   break;
27
28
29
                         {f if}\ is ContVRset:=false\ {f then}\ \ {f ADD}\ {f the}\ {f outgoing}\ {f node}\ {f of}\ {f currNode}\ {f to}\ {f qt}
30
31
                   end
32
              end
              if DDtable contains Key v then MERGE dependentOn to DDtable[v]
33
34
              else DDtable[v] := dependentOn;
35
         end
36 end
```

4.3.3 Control Dependence

4.3.3.1 Non-termination Sensitive Control Dependence

As introduced in Chapter 2, Control Dependence (CD) captures the notion on whether one node can decide the execution of another node. Generally, a branching node⁴ is a decision point on whether the nodes along one of its branch can be passed through, and thus the branching node decides the execution of those nodes along one of its branch.

Without using control dependence, the sliced model will lose the useful information on how a path branches to reach an important node, and therefore become more imprecise. By using control dependence, if a node is included in the sliced model, the other node which acts as its decision point will be included in the sliced model too. In this way, the decision point serves like an "anchor" for the path flowing through it. The control flow structure is therefore preserved in the sliced model, and model comprehension is facilitated in the resultant slice.

In the scenario when the default start state is a branching state, using control dependence to add the default start state into the sliced model is crucial. In FORML, the pseudo state points to exactly one default start state; it is incorrect to have multiple default start states within one sub-state machine. If a default start state branches and it is not selected into the sliced model, we will run into trouble in determining the new default start state in the sliced model. This issue will become more evident when FormlSlicer reaches the last step of model slicing process, which will be elaborated in Section 4.4.3.2.

Therefore, control dependence is an important dependence in FormlSlicer's slicing task.

As elaborated in Section 2.2.3, researchers have proposed many different definitions on control dependence in both program slicing and model slicing. At present, there is no standard, 100% correct algorithm to compute control dependence for slicing on SBMs.

FormISlicer simply adopts one of these definitions—the NTSCD as defined by Ranganath et al. [22]. A precise definition of control dependence is presented as below:

Definition. In a CFG, n_j is (directly) non-termination sensitive control dependent on node n_i if n_i has at least two successors, n_k and n_l ,

1. for all maximal paths from n_k , n_j always occurs and it occurs before any occurrence of n_i ;

⁴A branching node in CFG has more than one outgoing paths, i.e., its outdegree is greater than 1. It is always an SNode, which is equivalent to a state in FORML with multiple outgoing transitions.

2. there exists a maximal path from n_l on which either n_j does not occur, or n_j is strictly preceded by n_i .

In other words, when there are at least two branches of paths from n_i , we can definitely pass through n_j by taking one of the branch, and can possibly avoid n_j by taking another branch. When this is the situation, n_j is control dependent on n_i . This is illustrated in Figure 4.7, the key idea behind this definition is that reaching again a start node is analogous to reaching the end of path.

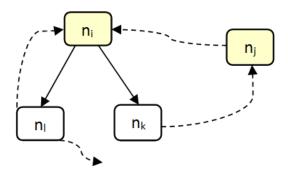


Figure 4.7: An Illustration of Non-termination Sensitive Control Dependence: n_i is control dependent on n_i

4.3.3.2 CD Algorithm: Paths Representation for a Node

Ranganath et al.[22] has presented a dynamic algorithm of computing NTSCD. Its main idea is to start from each branching node and search for any other nodes along the path that can be control dependent on that branching node. The algorithm represents sets of CFG paths symbolically and propagates these symbolic values to collect the effects of particular control flow choices at program points in the CFG. Based on the main idea, we adapted the algorithm to our CFGs and designed a dynamic algorithm to fit our own needs⁵.

We use an array p, which is an array to record the paths for each node along the traversal. The paths for node i, as stored in p[i], represent the different paths that can be traversed from a specific branching node to node i.

⁵There are a few reasons why we do not directly use the algorithm in [22]: (1) The paper only shows the skeleton of the algorithm and does not explain certain details, such as why cardinality of sets of paths and branching node's outdegree can be used in determining control dependence; (2) the CFG used in their algorithm is slightly different from ours. However, the main idea remains the same.

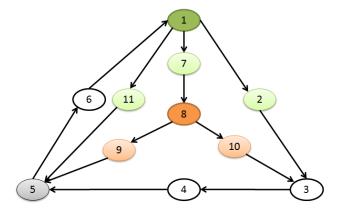


Figure 4.8: A CFG Example to Illustrate the Paths Representation of Node 5 from Node 1; Node 8 has Two Outgoing Nodes (9 and 10), Highlighted in Orange Colour; Node 1 has Three Outgoing Nodes (2, 7 and 10), Highlighted in Green Colour

The paths representation of a node can be explained in Figure 4.8. In this CFG, we want to represent the different paths from Node 1 to Node 5; Node 1 is the branching node. We observe that there are four different possible paths to reach Node 5 from Node 1:

- 1. the Path of " $1 \rightarrow 11 \rightarrow 5$ ";
- 2. the Path of " $1 \rightarrow 7 \rightarrow 8 \rightarrow 9 \rightarrow 5$ ";
- 3. the Path of " $1 \rightarrow 7 \rightarrow 8 \rightarrow 10 \rightarrow 3 \rightarrow 4 \rightarrow 5$ ";
- 4. the Path of " $1\rightarrow2\rightarrow3\rightarrow4\rightarrow5$ ";

The paths representation of Node 5 from Node 1 is shown in Figure 4.9. The paths are separated by semicolon. Each path consists of one or more sub-paths. Each subpath consists of one source index and one target index.

Path 1 is represented as "1:11". Along the traversal from Node 1 to Node 5, there is only one decision point at Node 1 and the path has chosen the branch of Node 11 from Node 1.

Path 2 is represented as "1:7,8:9". There are two sub-paths here: "1:7" and "8:9". This means that along the traversal from Node 1 to Node 5, there are two branching nodes. The first branching node is Node 1 and the path takes the branch of Node 7. The second branching node is Node 8 and the path takes the branch of Node 9 from Node 8.

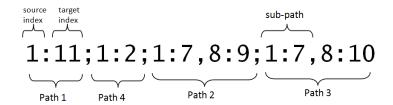


Figure 4.9: The Representation of Paths of Node 5 from Branching Node 1 in the CFG in Figure 4.8

Path 3 is represented as "1:7,8:10". The only difference between Path 3 and Path 2 is that at the second branching node (Node 8), Path 3 takes the branch of Node 10 from Node 8. Although Node 3 and 4 are along this path, they are neither branching nodes nor the next nodes of any branching nodes; at either of these two nodes, the path has only one possible way to go. Therefore, Node 3 and 4 do not carry useful information in distinguishing the current path from other paths, and we do not record them in the path.

Path 4 is represented as "1:2". At Node 1, the path takes the branch of Node 2.

After collecting all the paths from Node 1 to Node 5. We observe that no matter which path Node 1 takes, it always reaches Node 5. In other words, **Node 1 cannot avoid passing through Node 5**. This does not satisfy the definition of CD. Therefore, Node 5 is not control dependent on Node 1.

4.3.3.3 CD Algorithm: Reduction of the Paths Representation to Detect CD

FormISlicer can automatically detect the fact that Node 5 is not control dependent on Node 1 by reducing the paths representation. Based on the fact that Node 8 has only two outgoing neighbours (Node 9 and Node 10), the two paths "1:7,8:9" and "1:7,8:10" can be reduced to "1:7". This implies that at Node 8, no matter we choose the branch of "8:9" or the branch of "8:10", we always reaches Node 5.

Now the representation of paths becomes "1:11;1:2;1:7". Because Node 1 has three outgoing nodes (2, 7 and 11), a second round of reduction takes place and "1:11;1:2;1:7" is reduced to "".

As a result, the paths representation of Node 5 from Node 1 is empty.

After walking through the example, we can generalize the rule for paths reduction. Given that Node i has some outgoing nodes, $1, 2, \ldots, k$, and the sorted paths representation

of Node j from Node i contains the substring Xi:1;Xi:2;...;Xi:k (X is the common prefix for paths), we can reduce the paths by replacing the substring to be X.

The paths representations of other nodes from Node 1 cannot be reduced to empty. For example, the paths representation of Node 3 from Node 1 is "1:2;1:7,8:10". Node 3 is said to be control dependent on Node 1, because its paths representation implies that there are some possible ways from Node 1 that can pass through Node 3 and some other possible ways from Node 1 that can avoid Node 3; in other words, Node 1 controls the execution of Node 3.

4.3.3.4 CD Algorithm: Pseudo-code and Explanations

This section presents FormlSlicer's algorithm in computing the control dependence. The main algorithm is shown in Algorithm 4.2. The computation results are stored in a table:

CDset a set consisting of many pairs of nodes (n1, n2) where n2 is control dependent on n1

In Algorithm 4.2, p is an array of String, with each element storing the paths representation of each node in CFG from a specific branching node.

The algorithm examines all the nodes in the *foreach* statement at Line 3 and checks whether the node is a branching node at Line 4. Only branching nodes can possibly control other nodes' execution.

Next, from Line 5 to Line 10, the algorithm initializes the paths representation of the neighbours of the branching node *node1*. These neighbour nodes are added into *workset*.

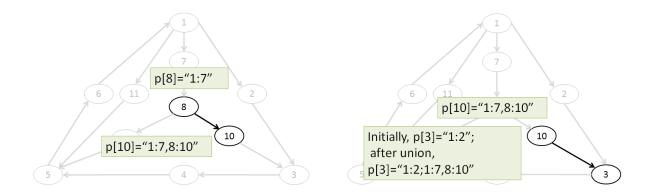
In each iteration of the *while* loop at Line 11, *currNode* is polled from the *workset* and analysed in three cases. We reuse the same CFG from Figure 4.8 to explain.

- 1. If *currNode* is a branching node, as detected at Line 13, then the paths representation of each outgoing node of *currNode* needs to be extended.
 - An example is shown in Figure 4.10a. The paths representation of Node 10 copies the paths representation of Node 8 and appends a subpath "8:10", to show that the path has branched at Node 8. We say that the paths representation of Node 10 is extended from that of Node 8.
 - The function *Extend*, as listed in Algorithm C.5, extends the paths representation of each outgoing node of a branching node.

Algorithm 4.2: Main Algorithm of Control Dependence Computation

```
Input: allNodes
   Output: CDset
 1 set CDset := \emptyset
 \mathbf{2} \ \mathbf{set} \ p := \mathit{array}[\mathit{String}]
 3 foreach node1 in allNodes do
         if node1 has 1 outgoing node then continue;
         \mathbf{set} workset := unique queue
         reset all fields in p to be null
 6
         foreach node2 (with ID n2idx) in node1.outgoingNodes do
              p[n2idx] := "n1idx:n2idx"
 8
 9
              ADD node2 into workset
10
         while workset is not empty do
11
              set currNode := workset.poll(); currIndex := currNode.ID;
12
              {\bf if} \ \ currNode.outgoingNodes.size > 1 \ {\bf then}
13
                  foreach n3 (with ID n3idx) in the currNode.outgoingNodes do
14
15
                       if n\beta == node1 then continue;
                       p[n3idx] = ExtendPath(currIndex, "currIndex:n3idx");
16
                       if NOT HasReductionOccursBefore (n3idx) AND IsReachableFromPartialPaths (n3idx) then
17
18
                            ADD n3 to workset
19
                       end
20
                  end
\bf 21
              else if currNode.outgoingNodes.size == 1 then
                  \mathbf{set} \ n3 \ (with \ ID \ n3index) := currNode.outgoingNodes[0]
22
                  if n3 == node1 then continue;
23
                  if NOT HasReductionOccursBefore (n3index) AND UnionPathHappens(n3index, n2index) then
24
                       ADD n3 to workset
25
                  end
26
27
             end
         end
28
29
         for j from 0 to last index in p do
              if IsReachableFromPartialPaths (j) then ADD the pair of (j, n1idx) into CDset
30
31
32 end
```

- 2. If *currNode* is not a branching node, as detected at Line 21, then the paths representation of *currNodes*'s only outgoing node is *union-ed* with that of *currNode*.
 - An example is shown in Figure 4.10b. The paths representation of Node 3 was initially "1:2" because of Path 4 as shown in Section 4.3.3.2. After union-ing with the paths representation of Node 10, it now becomes "1:2;1:7,8:10".
 - The function *UnionPathHappens*, as listed in Algorithm C.4, unions the paths representation of the outgoing node of a non-branching node.
- 3. If *currNode* does not have any outgoing nodes, nothing is performed because *currNode* is a terminating node.



(a) Extend the Path Representation when *currNode* is a (b) Union the Path Representation when *currNode* is a Non-Branching Node

Branching Node

Figure 4.10: Two Cases in Propagating the Paths Representation from currNode to its Neighbour in Algorithm 4.2

As mentioned in Section 4.3.3.3, when the paths representation of a node n is not empty, it implies that from the branching node, it is possible to take a path to pass through n and take another path to avoid passing through n. In this case, the branching node controls the execution of n. Function IsReachableFromPartialPaths is monitoring this scenario to determine the control dependence relationship between a given node and the branching node.

The algorithm is long and thus it is modularized into several functions. There are in total six supporting functions for the main algorithm in Algorithm 4.2. Table 4.2 lists all the supporting functions' signatures and their goals⁶. In the table, p[i] refers to the paths representation of the node with an ID of i.

Function Signature	Goal of Function	Algorithm
HasReductionOccursBefore (targetIndex)	It determines whether $p[targetIndex]$ has been reduced to empty.	C.1
$Is Reachable From Partial Paths \ (target Index)$	It determines whether p[targetIndex] contains some non-reducible paths, i.e., whether the node with an ID of targetIndex is control dependent on the branching node.	C.2
ReducePaths (originalPath)	It performs reduction on the input paths representation.	C.3

⁶In order not to break the flow of this chapter, the supporting functions' algorithms are all listed in Appendix C.

SortPaths (paths)	It performs an insertion sort on paths, firstly	Omitted
	based on units of paths, secondly based on	
	units of sub-paths. Insertion Sort is more	
	efficient because the paths are likely to be in	
	ascending order.	
UnionPathHappens (targetN-	It adds $p[prevNodeIndex]$ to	C.4
$odeIndex, \ prevNodeIndex)$	p[targetNodeIndex]. If nothing is changed,	
	the function returns false. Otherwise, it	
	returns true.	
ExtendPath (srcIndex, new-	It adds the new subpath to each path in	C.5
SubPath)	p[srcIndex] and returns the new $p[srcIndex]$.	

Table 4.2: List of Supporting Functions for Main Algorithm in Algorithm 4.2

4.3.4 Summary

In summary, we have computed all three dependences from the CFGs and obtained the following results:

HDtable1 a 1D-table mapping each SNode to its parent SNode

HDtable2 a 2D-table mapping each SNode to its start child state⁷

DDtable a 1D-table mapping each variable to a pair of TNodes such that the left one is dependent on the right one

CDset a set consisting of many pairs of nodes (n1, n2) where n2 is control dependent on n1

These results serve as dictionaries for the slicing processes to look up. They will not be modified after the preprocessing task.

We are now ready to move on to the slicing task. FormlSlicer will fork off n processes for n features, each considers one feature as the FOI. In the next section, we will present the workflow of each slicing process.

 $^{^7\}mathrm{A}$ composite state can contain multiple regions and therefore have multiple start child states

4.4 Multi-Stage Model Slicing Process

This section presents the workflow of each slicing process in the slicing task. Because the workflow is divided into several stages, we name it as **Multi-Stage Model Slicing Process**.

FormISlicer's slicing strategy is to start with an empty sliced model in the ROS. At each step in the Multi-Stage Model Slicing Process, certain model elements (either an SNode or a TNode) in the ROS are put into the sliced model. Along the process, the sliced model grows gradually.

The FOI will remain unchanged throughout the process.

Figure 4.11 shows a side-by-side comparison between the original model and the sliced model. Some FOSMs in ROS are entirely absent in the sliced model; some are partially absent.



Figure 4.11: A Comparison between Original Model and Sliced Model

Table 4.3 lists the three stages in Multi-Stage Model Slicing Process and explains their distinct purposes.

Stage Name	Purpose of Stage
Initiation Stage	This stage selects the initial set of TNodes into the sliced model.
General Iterative Slicing Stage	This stage uses the dependences computed from the preprocessing task to add more SNodes and TNodes based on the initial sliced model.
Model Enrichment Stage	This stage ensures that all the nodes in the sliced model form a well-formed state machine.

Table 4.3: Distinct Purpose of Each Stage in Multi-Stage Model Slicing Process

We will use a slicing example to illustrate each step of the Multi-Stage Model Slicing Process. The example model consists of only two FOSMs; one of which is the FOI and the other one is an FOSM in ROS.

The Multi-Stage Model Slicing Process is performed on the CFG structure. Recall from Section 4.2.1 that a state in the input model is converted into an SNode and a transition is converted into a TNode in a CFG, it is easy to match the CFGs and the equivalent FOSM. In the following sections, we will present both the CFGs and the equivalent FOSM side-by-side to show the effects of slicing at each step. Elements that are newly added into the sliced model are highlighted in red colour; existing elements in the sliced model are highlighted in black colour; elements that are not in the sliced model are coloured in grey.

For brevity, if an element is in the sliced model, we say that it is *part-of-slice*; on the other hand, an element is *out-of-slice* if it is not in the sliced model.

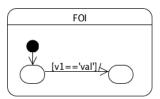
4.4.1 Initiation Stage

This stage selects the initial set of TNodes into the sliced model in ROS, based on what FOI monitors.

4.4.1.1 Variable Extraction Step

In Section 3.3, we have discussed that the monitored variables of FOI will be used as a slicing criterion to select the initial set of transitions in other FOSMs in the ROS. This is because FormlSlicer only concerns with how the other FOSMs influence the FOI, but not with how the FOI influence the other FOSMs.





- (a) The Control Flow Graph of Feature of Interest
- (b) The FOSM of Feature of Interest

Figure 4.12: A Simple Example of Feature of Interest

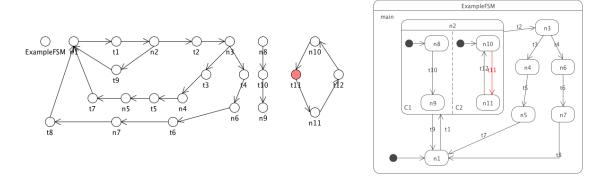
Based on this idea, *Variable Extractor* is a module in FormlSlicer to extract a collection of monitored variables from the FOI.

Figure 4.12 shows a simple example of the FOI. It monitors one variable, v1. Variable Extractor takes in the CFGs of this FOI (shown in Figure 4.12a) and extracts all the TNodes' monitored variables. In the end, it outputs a set of variables that are relevant to the FOI. We denote this set of variables as V_{Rv} and call them **relevant variables**. In this example, $V_{Rv} = [v1]$.

4.4.1.2 Initial Transition Selection Step

Initially, we have an empty sliced model in the ROS. During the Initial Transition Selection Step, FormlSlicer selects all the TNodes in the ROS that control any relevant variable, and add them into the sliced model.

A simple example of the FOSM in the ROS is shown in Figure 4.13.



(a) The Control Flow Graph of the Example FOSM in the ROS

(b) The Example FOSM in the ROS

Figure 4.13: The Example FOSM in the ROS after Initial Transition Selection Step

In our example, the transition t11 in Figure 4.13b has the label of "t11:[v2=='val2'] /a1:v1:='val';". According to how FormlSlicer extracts the monitored and controlled variables from a transition label as discussed in Section 3.3.1, the TNode of t11 has one monitored variable v2 and one controlled variable v1.

Because v1 is a relevant variable (collected by *Variable Extractor* in the previous step), t11 is added into the sliced model. The monitored variables of t11, e.g., v2, need to be added to the set of relevant variables. Now, $V_{Rv} = [v1, v2]$.

4.4.2 General Iterative Slicing Stage

As elaborated in Section 4.3, we have obtained the dependences from the preprocessing task. The results are stored at *HDtable1*, *HDtable2*, *DDtable* and *CDset*. These are useful information for the General Iterative Slicing Stage in adding more SNodes and TNodes based on the initial sliced model.

The General Iterative Slicing Stage consists of four steps (Figure 4.14):

DD Step

Add more TNodes that are transitively data dependent on the part-of-slice TNodes w.r.t. any relevant variable;

Transition-to-State Step

Add more SNodes based on the part-of-slice TNodes;

Replacing Cross-Hierarchy Transition

Replace all out-of-slice cross-hierarchy transitions with "true" transitions and add them into the sliced model;

CD-HD Step

Add more SNodes that are transitively control dependent or hierarchy dependent on the part-of-slice SNodes.

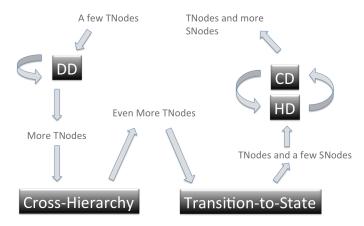


Figure 4.14: Four Steps in General Iterative Slicing Stage

Both the DD Step and CD-HD Step perform the node adding operation **iteratively**, in order to add nodes that are **transitively** dependent on any part-of-slice nodes. This is why the word "iterative" is in the name of this stage.

4.4.2.1 DD Step

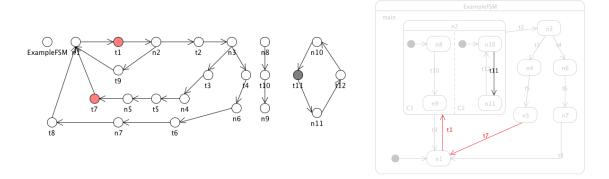
DD Step uses *DDtable* to add more TNodes that are transitively data dependent on the part-of-slice TNodes.

DD Step is a vital step in almost all SBM slicers that use dependence-based analysis. After all, slicing is a static analysis technique based on define-use relationships among elements. An SBM slicer needs to iteratively find more transitions based on define-use relationships of variables. This define-use relationship is the data dependence among nodes.

DD Step starts with V_{Rv} and the partial sliced model with a few TNodes, from the previous step. Then it iterates repeatedly to (potentially) add more TNodes into the sliced model, and (potentially) enlarges the size of V_{Rv} . It terminates when no more change to the V_{Rv} is possible.

Algorithm 4.3 shows how DD Step works. Its inputs include relevant Variables and sliceSet, which represent V_{Rv} and the partial sliced model respectively. It iterates repeatedly, as shown at Line 2. At Line 5, it looks up DDtable and checks if any TNode in the sliced model is data dependent on another TNode not in sliced model (anotherTNode) with respect to a relevant variable. If so, anotherTNode will be added into the sliced model, as shown at Line 6. At Line 7, the monitored variables of anotherTNode are added into relevant Variables.

At the end of each iteration, the algorithm checks whether there have been any new variables added to the relevant variables at Line 11. If there are any changes, the algorithm has to continue searching for more TNodes.



- (a) The Control Flow Graph of the Example FOSM in the ROS
- (b) The Example FOSM in the ROS

Figure 4.15: The Example FOSM in the ROS after DD Step

Algorithm 4.3: DD Step in General Iterative Slicing Stage

```
Input: sliceSet, relevantVariables, DDtable
   Output: SliceSet, relevantVariables
 1 set listOfRelevantVariables := {};
 2 repeat
       \mathbf{set} \ prevSizeRelVar := relevantVariables.size();
 3
       foreach v in relevant Variables do
 4
           if DDtable contains v \Rightarrow (tnode, another TNode) AND sliceSet contains tnode then
 5
               ADD another TNode to slice Set;
 6
               ADD another TNode.monitored Variables to relevant Variables;
           end
 8
       end
 9
       set currSizeRelVar := relevantVariables.size();
11 until currSizeRelVar == prevSizeRelVar
```

We need to repeatedly add more TNodes in order to add more TNodes on which the FOI is transitively data dependent. Re-consider the example in Figure 4.13. We know that $V_{Rv} = [v1, v2]$ and t11 is in the sliced model, from the previous step. Now, consider the transition t1 with a controlled variable v2 and a monitored variable v3. Then, t11 is data dependent on t1 with respect to v2; and thus t1 is added to the sliced model as well. However, the DD Step cannot simply terminate here. Because v3 is monitored by t1, this variable is important to the sliced model. If there is another transition (e.g., t7) which controls v3, that transition affects t1, and indirectly affects t11, which again indirectly affects the FOI. Therefore, we must include v3 into V_{Rv} and perform the node adding operation in another iteration.

The sliced model now contains TNodes t1 and t7, as shown in Figure 4.15.

4.4.2.2 Replacing Cross-Hierarchy Transition

A cross-hierarchy transition is a transition which crosses the hierarchy boundary, so that its source state and destination state do not have a common parent state. We determine that due to the complexities brought by any cross-hierarchy transitions in the FOSM, these transitions need to be preserved in order for the sliced model to correctly simulate the original model.

A cross-hierarchy transition may transit from the outside of a hierarchy boundary to its inside; in this case, the destination state's rank is higher than the source state's rank

(Figure 4.16a). A cross-hierarchy transition may transit from the inside of a hierarchy boundary to its outside; in this case, the destination state's rank is lower than the source state's rank (Figure 4.16b). A cross-hierarchy transition may even transit from the inside of a hierarchy boundary, to the inside of another hierarchy boundary; in this case, the destination state's rank may be higher than, lower than or same as the source state's rank (Figure 4.16c).

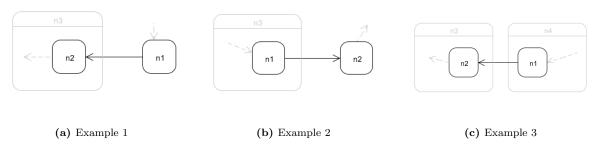


Figure 4.16: Examples of Cross-Hierarchy Transitions

The complexity comes from the composite states which hierarchy boundaries are involved in a cross-hierarchy transition t_{ch} (e.g., $n\beta$ or n4 in Figure 4.16). Consider this composite state n_{cps} ; note that n_{cps} is neither the source state nor the destination state of t_{ch} , but it is an ancestor state of either of them. If n_{cps} is selected into the slice due to some other reasons (e.g., some other nodes are control dependent on it), and FormlSlicer does not select t_{ch} into the slice, the state configuration in the sliced model cannot correctly simulate the state configuration in the original model, because n_{cps} will not be entered in the sliced model while it is entered in the original model, and will not be exited in the sliced model while it is exited in the original model.

This causes many potential problems. Assume that this composite state n_{cps} is a source state of another important transition t_x , then any appropriate events can trigger t_x to leave n_{cps} . The correct triggering of t_x is therefore affected by a cross-hierarchy transition t_{ch} which either enters or exits n_{cps} . If we do not select t_{ch} into the slice, n_{cps} will not be entered or exited in a correct manner in the sliced model, that will cause the execution of t_x incorrect, and consequently any important actions brought by t_x will be incorrect. This causes the sliced model to be incorrect.

Some may ask why we cannot simply detect that important composite state n_{cps} and create a path from a starting part-of-slice state to n_{cps} . The caveat of doing so is that it cannot accommodate many corner cases. For example, in the example of Figure 4.16a, if there is another transition t_y from n2 to another descendant state of n3, then t_y cannot be

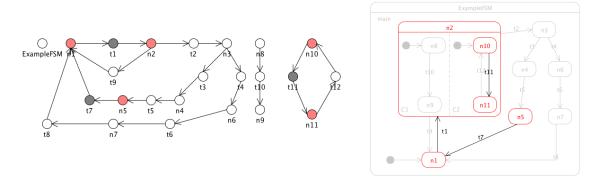
simulated in the sliced model because there is no way to transit from n3 to its descendant state using a transition. The example can be made more complex. We will then need a way to fix all possible corner cases; this will make the algorithm long and inelegant and yet it is still hard to guarantee that the sliced model is 100% correct.

Based on the above analysis, FormlSlicer has this step—"Replacing Cross-Hierarchy Transition"—after the DD Step in the Multi-Stage Model Slicing Process. The step looks for any out-of-slice cross-hierarchy transitions, and for each of them, replaces the cross-hierarchy transition with a transition carrying only "true" in its guard condition, called a "true" transition. The "true" transition is added into the sliced model.

The reason of using a "true" transition is that this transition is guaranteed not to control any relevant variables. The previous step—DD Step—has already identified all the transitions which transitively control the relevant variables. Thus, any out-of-slice transitions at this step do not affect the relevant variables. We can therefore safely ignore their monitored or controlled values.

4.4.2.3 Transition-to-State Step

So far, all the model elements that have been added to the sliced model are TNodes (equivalent to transitions). The Transition-to-State Step is a turning point to bring in the SNodes (equivalent to states).



(a) The Control Flow Graph of the Example FOSM in the

(b) The Example FOSM in the ROS

Figure 4.17: The Example FOSM in the ROS after Transition-to-State Step

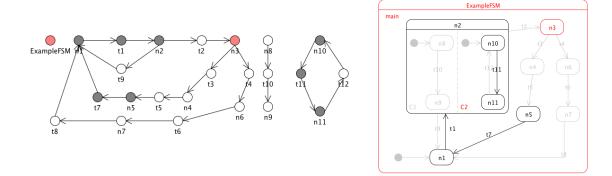
For each part-of-slice transition, this step makes its source state and destination state become part-of-slice. In other words, the SNodes that correspond to these source and destination states are added into the sliced model. Figure 4.17 shows the effect of this step.

Although this step is simple, it is very important. Firstly, it enriches the fragmented sliced model so that it becomes one step closer to well-formedness, as it is not logical to have a transition without either source or destination state. Secondly, it introduces the initial set of SNodes into the sliced model, which becomes the starting point for the iterative CD-HD Step.

4.4.2.4 CD-HD Step

We have explained the importance of control dependence and hierarchy dependence in Section 4.3.3.1 and Section 4.3.1 respectively. The computation results, *HDtable1* and *CDset*, are used in the CD-HD Step to add more SNodes that are transitively control or hierarchy dependent on the part-of-slice TNodes.

Algorithm 4.4 shows how CD-HD Step works. Similar to the algorithm for DD Step, it has a loop that will terminate only when no more changes occur, as shown at Line 12. In each iteration, there are two lookups. At Line 4, it looks up the hierarchy dependence and adds an SNode into the slice if its child SNodes are part-of-slice. At Line 8, the algorithm looks up the control dependence and adds an SNode which controls the execution of other part-of-slice nodes.



(a) The Control Flow Graph of the Example FOSM in the ROS

(b) The Example FOSM in the ROS

Figure 4.18: The Example FOSM in the ROS after CD-HD Step

The reason for such a repetition is that an SNode can be transitively control dependent or hierarchy dependent on another SNode. For example, a composite state can contain many descendants in different ranks of state hierarchy. Once a descendant state is selected into the slice, the repetition in CD-HD Step will ensure that all the states from the descendant state to the root state along the state hierarchy are all added into the slice.

Algorithm 4.4: CD-HD Step in General Iterative Slicing Stage

```
Input: sliceSet, HDtable1, CDset
   Output: SliceSet
 1 set changesOccur
 2 repeat
      reset \ changesOccur := false;
 3
      if HDtable1 contains node⇒parentSNode AND sliceSet contains node then
 4
          ADD parentSNode to sliceSet;
 5
          {f reset}\ changesOccur:=true
 6
      end
      if CDset contains node⇒controllingSNode AND sliceSet contains node then
 8
 9
          ADD controllingSNode to sliceSet;
          reset changesOccur := true
10
      end
12 until changesOccur == false
```

Such a repetition of lookups needs to include both control dependence and hierarchy dependence together, because both dependence are based on SNodes.

Figure 4.18 shows the same slicing example after the CD-HD Step. The state n3 has been added into the sliced model because n5 is control dependent on it. The state ExampleFSM has been added into the slice because many part-of-slice nodes, such as n1, are hierarchy dependent on it.

4.4.3 Model Enrichment Stage

Model Enrichment Stage aims to make the FOSMs in the sliced model become well-formed state machines, and as a consequence, the sliced model also becomes a well-formed big state machine. Informally, an FOSM is a well-formed FOSM when all the states are reachable from the pseudo state⁸ and all transitions can be triggered when appropriate.

The basic idea in this stage is to try to bring the states far away from one another to come "closer", so that they do not remain disconnected. There are two steps in this stage:

⁸A pseudo state is denoted as a black solid circle with an outgoing, non-labelling transition pointing to the default start state of a state machine, as introduced in Section 3.1.

Step I: State Merging Step

picks any two suitable states and merges them together;

Step II: True Transitions Creation

makes all part-of-slice states reachable from the pseudo state.

4.4.3.1 Step I: State Merging

The State Merging step brings two states "closer" to each other by merging them. This does not only make the FOSM one step closer to becoming a well-formed FOSM, but also increases the degree of reduction in slicing.

FormISlicer uses Korel et al.'s two state merging rules that satisfy the traversability property⁹ [5]:

Rule 1 If there exist out-of-slice transitions from state n to n' and also from state n' to n, these two states are merged into one state "n,n'".

Rule 2 States n and n' can be merged into one state "n,n'" if:

- 1. There exists a out-of-slice transition from n to n',
- 2. There does not exist a part-of-slice transition from n to n', and
- 3. There is no outgoing transition from n to n'' where $n'' \neq n'$.

Figure 4.19 illustrates these two rules.

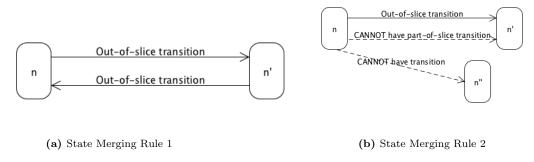


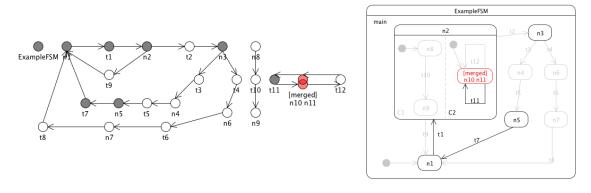
Figure 4.19: Illustration of State Merging Rules in Step I of Model Enrichment Stage

⁹See Section 2.2.5 about traversability property on a slice.

Intuitively, these two rules can be easily justified. In Rule 1, since the transitions between the two states are out-of-slice, they are not important; otherwise, they have already become part-of-slice during DD Step. In Rule 2, from n the machine does not have anywhere else to move except n'. Therefore, it is safe to merge n and n'.

FormlSlicer adjusts the two rules for its own use.

- 1. It will perform state merging only when at least one of the two states is part-of-slice. Otherwise, it will be a waste of effort to merge two out-of-slice states because in the end they will not appear in the sliced model.
- 2. It will perform state merging only when these two states have the same parent state. Otherwise, the sliced model will become incorrect.



- (a) The Control Flow Graph of the Example FOSM in the
- (b) The Example FOSM in the ROS

Figure 4.20: The Example FOSM in the ROS after Stage Merging Step

Figure 4.20 shows the same slicing example after the State Merging Step. State n11 has only one out-of-slice transition to n10 and therefore these two states satisfy Rule 2. They are merged together to become a new state "[merged] n10 n11".

4.4.3.2 Step II: True Transitions Creation

The True Transitions Creation step makes all part-of-slice states reachable from the pseudo state. It starts from the beginning of the FOSM and "probes" to connect the part-of-slice states together. This is the last step for the entire Multi-Stage Model Slicing Process.

There are two sub-steps in Step II:

Sub-step 1: Search for New Default Start States We know that each sub-state machine has one default start state. It is the state pointed by a transition without label from the pseudo state. If the default start state is out-of-slice, this sub-step 1 searches for the new default start state for the sub-state machine.

This sub-step benefits greatly from the use of control dependence. Section 4.3.3.1 has explained this scenario. When a default start state is a branching state, it will be added into the sliced model because of control dependence. This prevents FormlSlicer to run into the trouble of creating multiple default start states in the sliced model when the original default start state is out-of-slice.

As a result of this sub-step, for each sub-state machine in the original model, its default start state in the sliced model is:

- 1. the same one in the original model;
- 2. the next-part-of-slice state of the original default start state;
- 3. absent, because the whole sub-state machine is out-of-slice.

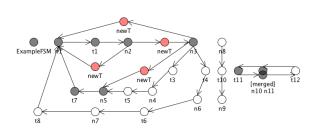
Sub-step 2: Search for Next Part-of-slice State Consider a path starting from a part-of-slice state n to another part-of-slice state n', and all the other states and transitions along this path are out-of-slice because they are not selected during all the previous steps in Multi-Stage Model Slicing Process. The original model can take this path to move from n to n'. But in the sliced model, n and n' are disconnected.

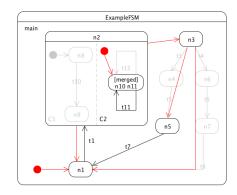
We need to connect n and n' together in the sliced model. This connection will be a "true" transition¹⁰.

All the part-of-slice states that are reachable from a part-of-slice state n via an out-of-slice path are called the "**next part-of-slice states**" of n. Informally, a part-of-slice state n' is the **next part-of-slice state** of state n' if there is a path that starts from n' and reaches n' and that all the states and transitions along this path are out-of-slice and all the states are at the same rank of state hierarchy. A state n' may have more than one part-of-slice states because a path from n' may branch. We call all of them as the **next part-of-slice state set** of n.

Sub-step 2 performs a depth-first-search from any part-of-slice state and finds all its next-part-of-slice states. It creates a "true" transition between the part-of-slice state and each of its next-part-of-slice states.

 $^{^{10}}$ Recall from Section 4.4.2.2 that a transition carrying only "true" in its guard condition is called a "true" transition.





(a) The Control Flow Graph of the Example FOSM in the ROS

(b) The Example FOSM in the ROS

Figure 4.21: The Example FOSM in the ROS after True Transitions Creation Step

Figure 4.21 shows the slicing example after this step. We can see that n3 is now connected to its next part-of-slice state n1. In fact, the path between a part-of-slice state and its next part-of-slice state can be as short as one transition. For example, n2 has an out-of-slice path to n3 and it consists of only one transition, t2; it is replaced by a "true" transition.

4.4.4 Summary and Postprocessing

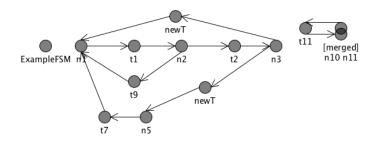
We have presented all the steps for the Multi-Stage Model Slicing Process. Figure 4.22a shows the resultant CFGs for the example feature. It looks much smaller than the original CFGs in Figure 4.13a.

As a postprocessing step, FormlSlicer converts the resultant CFGs into an FOSM, as shown in Figure 4.22.

The resultant FOSM and the FOI (which remains unchanged before and after slicing) form the sliced model. The *ModelWriter* module in FormlSlicer writes the sliced model to a text file, in the format as specified in Table 4.1.

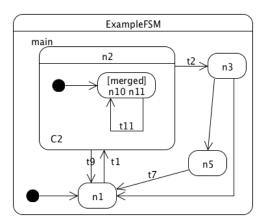
As mentioned in Section 4.1, FormlSlicer will perform the Multi-Stage Model Slicing Process for multiple times, each time with a different feature as the FOI.

In the next chapter, we will present a correctness proof on the Multi-Stage Model Slicing Process to show that the resultant sliced model can simulate the original model.



(a) The Control Flow Graph of the Example FOSM in the ROS

//



(b) The Example FOSM in the ROS

 $\textbf{Figure 4.22:} \ \ \textbf{The Example FOSM in the ROS after All Steps in Multi-Stage Model Slicing }$

Chapter 5

Correctness of FormlSlicer

This chapter presents a correctness proof to show that the sliced model produced by the Multi-Stage Model Slicing Process (described in Chapter 4) can simulate the original model.

5.1 Overview

5.1.1 Purpose of the Proof

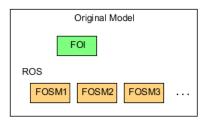
As the sliced model is used to replace the original model for safety property checking, the non-negotiable requirement for the sliced model is to guarantee that

$$M_{ROS_{\mathcal{L}}+FOI} \models \varphi \quad \Rightarrow \quad M_{ROS+FOI} \models \varphi$$

whereby FOI is the Feature of Interest (FOI), ROS is the Rest of System (ROS) executing with the FOI (i.e., all the feature-oriented state machines except the FOI state machine), $ROS_{\mathcal{L}}$ is the ROS after slicing, $M_{ROS+FOI}$ is the original model, $M_{ROS_{\mathcal{L}}+FOI}$ is the sliced model and φ is the safety property for FOI.

This is equivalent to saying that the execution traces in FOI in the original model is a subset of the execution traces in FOI in the sliced model. In such case, if a safety property is maintained in all execution traces in the sliced model, we can confidently claim that the safety property is maintained in all execution traces in the original model. It is acceptable if there are some execution traces in the sliced model that are impossible to occur in the original model¹.

¹This is the basic correctness property of a sliced model. See Section 2.2.5 on discussions in literature about correctness of SBM slicing.



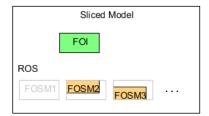


Figure 5.1: The Slicing Environment with Original Model and Sliced Model

Figure 5.1 shows a side-by-side comparison between the original model and sliced model. Some FOSMs in ROS are entirely absent in the sliced model; some are partially absent.

5.1.2 Intuition of the Proof

We can visualize an execution trace in the original model as a long sequence of execution steps:

$$e_0, e_1, e_2, \ldots, e_k$$

Due to feature interactions between FOI and other FOSMs in the ROS, there are certain execution steps that occur in other FOSMs to support the execution within FOI. For example, the initial execution step in FOI may be triggered only when a particular system-controlled variable v is equal to a certain value 'val', as illustrated in Figure 5.2; in this case, the execution step in FOSM1 that assigns v to be 'val' must be executed before the initial execution step in FOI, so as to trigger the latter.

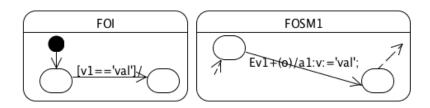


Figure 5.2: A Simple FOI Executing with Another FOSM in the Rest of System

In order to show that the set of execution traces in FOI in the original model is a subset of the execution traces in FOI in the sliced model, we want to prove that any given

execution trace in original model can be *simulated* by an execution trace in the sliced model.

This means that for each execution trace in the original there exists a simulating trace in the sliced model, such that one step in the original model's execution trace can be projected to one execution step in the sliced model's execution trace.

The intuition of our proof is to show that the snapshot between two execution steps in original model can be projected to a corresponding snapshot in sliced model, and that such a projection is maintained before and after each step in original model's execution trace.

5.1.3 Proof Outline

The proof is using induction to show that the execution trace in the original model can be simulated by at least one execution trace in the sliced model.

Section 5.2 defines terminology that is useful for the proof. This section introduces some concepts, such as state configuration and interpretation.

Section 5.3 describes the state transition rule that is standard to a hierarchical concurrent state machine.

Section 5.4 writes the Multi-Stage Model Slicing Process using the semantics defined in Section 5.2.

Section 5.5 shows the proof. It starts with the concept of relevant variables, and describes the projection of snapshot, transition and execution step from the original model to the sliced model.

5.2 Semantics

5.2.1 Variables, States, Regions, Transitions and Model

In the previous chapters, we have informally introduced and used the concepts of variable, state, region, transition and model. This section will define their respective notations in the proof.

Variables

A single variable is denoted as v; a set of variables is usually denoted as V with appropriate subscripts. The set of environment-controlled variables is denoted as V_{env} , whilst the set of system-controlled variables is denoted as V_{sus}^2 .

States

A state is denoted as either n or m; sometimes p is used to denote a parent state. A set of states is denoted as N when it refers a state configuration; otherwise, it is denoted as S. Among them, S^{pseudo} is the set of all pseudo states and n^{pseudo} denotes one of them. A pseudo state is represented as a black solid circle \bullet in an FOSM; it is a notation to point to the default start state.

A state can be either a basic state (i.e., state without child regions and states), or a composite state (i.e., state that contains child regions and states). A composite state p can have many child states n_1, \ldots, n_k , denoted as a set $ChildStates(p) = [n_1, \ldots, n_k]$; also, a state's parent state is denoted as $ParentState(n_1) = p$.

Regions

We use r to denote an orthogonal region inside a composite state³. The composite state n that contains this region is denoted as ParentStateOfRegion(r); and $ChildRegions(n) = [r]^4$. On the other hand, if a state n is in the sub-state machine enclosed by an orthogonal region r (i.e., n's rank in state hierarchy is one level higher than the rank of ParentStateOfRegion(r)), we use ParentRegion(n) = r to denote this relationship. Section 3.1 has shown a FORML example to illustrate this relationship.

We also need a notation to indicate that two orthogonal regions are parallel with each other when these two regions are both contained within the same composite state n and they are at the same rank of state hierarchy:

Definition 1. Two orthogonal regions r and r' are said to be parallel regions, denoted as $r \parallel r'$, when ParentStateOfRegion(r) = ParentStateOfRegion(r') and $r \neq r'$.

²Environment-controlled variables' values can only be changed by the external environment. System-controlled variables' values can be influenced by one or more FOSMs. Section 3.3 has defined these two sets of variables more clearly.

 $^{^3}$ See Chapter 3 for explanations on concepts like "orthogonal regions" and "composite state" in FORML

⁴There may be more than one orthogonal regions in a composite state; so here we use a set of regions, [r].

Transitions

A transition is a progression in a model's execution from one state (called the transition's source state) to another state (called the transition's destination state).

Definition 2. We write $n \xrightarrow{t} n'$ to denote a **transition** t from state n to state n'.

Moreover, ss(t) and ds(t) refer to the source state and destination state of t, respectively. In Definition 2, ss(t) = n and ds(t) = n'. The source state and destination state of t do **not** need to be at the same rank of state hierarchy, but there is a restriction: if a state is a child state of a composite state that has multiple orthogonal regions, we do not allow any transitions crossing hierarchy boundary from or to this state⁵.

Model

As introduced in Section 3.1, FormlSlicer treats the Behaviour Model in FORML as a big state machine. This big state machine only has a composite state containing many orthogonal regions. Each orthogonal region contains one sub-state machine, which is an FOSM. In some literature, this is called an 150% model [29].

In this proof, We use M to denote a model. As M contains k FOSMs, $[F_1, \ldots, F_k]$, we write it as:

$$M = \vdots$$

$$F_k$$

5.2.2 State Configuration and Interpretation

An FOSM F is a well-formed state machine. It consists of a finite set of states, S_F , including composite states and basic states. It contains a finite set of orthogonal regions, R_F . The state and region form a containment relation in hierarchy (each composite state $n \in S_F$ contains one or more regions; each region contains a sub-state machine). S_F^I is the set of all default start states in F and $S_F^I \subseteq S_F$. F also consists of a finite set of transitions, T_F , each starting from a source state $ss(t) \in S_F$ and ending at a destination state $ds(t) \in S_F$. There is a set of variables, V_F , which is controlled or monitored by F.

⁵See Section 3.2 for more details on this restriction.

We know that a basic state machine without hierarchy and concurrency constructs can be in only one state at a time; the state it is in at any given time is called the *current state*. However, because of hierarchy and concurrency, an FOSM can be in multiple states at a time. Therefore, we use N to refer to the **state configuration** of the FOSM.

This is not saying that the machine can be in any arbitrary combination of states at a time. Rather, N is the set of current states $N \subseteq S_F$ such that if any state n is in N, then so are all of n's ancestors, and if any composite state n is in N, then for each r in ChildRegions(n), there must be one state contained in r that are in N too. (A state machine's current state configuration is the set of current states in a hierarchy tree where a current composite state contains one current substate per orthogonal region. [32])

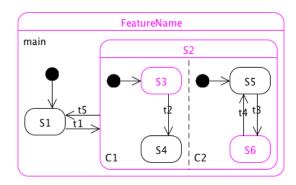


Figure 5.3: The FORML Example from Figure 3.1 with its Current States Highlighted in Magenta

Figure 5.3 shows an example of an FOSM with current states in FeatureName, S2, S3, S6 simultaneously. The state configuration is N = [FeatureName, S2, S3, S6]. Note that the root state is always in the state configuration.

Since a model M is a big state machine, the definition of state configuration also applies to M. Similarly, it consists of a finite set of states (S_M) , a finite set of regions (R_M) , a finite set of transitions (T_M) and a finite set of variables (V_M) . Its set of default start states is $S_M^I \subseteq S_F$. For any FOSM F contained within one orthogonal region of M, $S_F \subset S_M \wedge R_F \subset R_M \wedge T_F \subset T_M \wedge V_F \subset V_M$.

We use σ to denote an **interpretation** which maps variables to their values; thus, $\sigma(v)$ represent the interpretation of the variable v in the environment. The domain of σ is the set of all variables $V_{sys} \cup V_{env}$ in the slicing environment.

5.2.3 Execution Step

Informally, a **snapshot** is an observable point in an model's execution [33]; it refers to the status of an model between execution steps.

Definition 3. We define the snapshot of a model as a combination of the model's state configuration, N, and the interpretation of variables, σ , at that particular point in time; we denote the snapshot as (N, σ) .

An execution step changes the snapshot of the model. Through an execution step, the model effectively exits the set of current states and enters the set of destination states of the transitions in the execution step⁶; meanwhile, the values of some variables may be changed.

Here we define an execution step formally.

Definition 4. We write $M \vdash e : (N, \sigma) \Rightarrow (N', \sigma')$ when we refer to an execution step, e, that occurs in a model, M, such that its snapshot (N, σ) evolves to (N', σ') due to actions through the execution or environmental changes.

Each execution step involves a set of transitions which occur concurrently, denoted as:

$$e = \vdots$$

$$t_k$$

For any t_i for all $1 \leq i \leq k$, we write $t_i \subset e$ to denote that t_i is one of the many concurrent transitions in the execution step e.

When the execution step e involves only one transition t (i.e., k = 1), we write e = t. This is a **non-concurrent execution step**.

In general, we want to precisely describe what combination of transitions can occur concurrently in a single execution step. Recall Definition 1 on parallel regions and the various accessor functions in Section 5.2.1.

Definition 5. The set of concurrent transitions that are triggered simultaneously in an execution step e in $M \vdash e : (N, \sigma) \Rightarrow (N', \sigma')$ must satisfy:

⁶An model starts executing from an initial snapshot, (N^I, σ^I) .

- there are k transitions $[t_1, ..., t_k] \subseteq T$ that are triggered simultaneously, such that $ss(t_j) \xrightarrow{t_j} ds(t_j)$ where $ss(t_j) \in N$ and $ds(t_j) \in N'$ for all $1 \le j \le k$;
- $ParentRegion(ss(t_i)) = ParentRegion(ds(t_i))$ for all $1 \le j \le k$;
- $ParentRegion(ss(t_i)) \parallel ParentRegion(ss(t_j))$, or there exists another state p such that $ss(t_i) \xrightarrow{hd} p$ and $ParentRegion(ss(t_j)) \parallel ParentRegion(p)$, for any $1 \le i \le k \land 1 \le j \le k \land i \ne j$;

Figure 5.4 illustrates an example of an execution step which consists of two concurrent transitions t_m , t_n . One may observe that the two transitions t_m , t_n are "contained" within their respective orthogonal region only. This is consistent as FormlSlicer's restriction on transitions crossing hierarchy boundary on parallel regions, as discussed in Section 3.2.

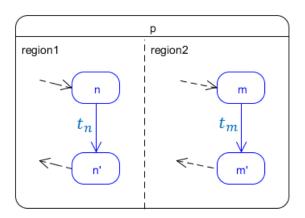


Figure 5.4: Concurrency in Orthogonal Regions as an Execution Step (Only Blue Coloured Components are Relevant in the Execution)

Slice Set This symbol \mathcal{L} is used as a subscript to annotate a model component in the sliced model. A state n in the sliced model is denoted as $s \in S_{\mathcal{L}}$. A transition t in the sliced model is denoted as $t \in T_{\mathcal{L}}$. Thus, an original FOSM F would become $F_{\mathcal{L}}$ after slicing. A sliced model is denoted as $M_{\mathcal{L}}$. A state configuration in the sliced model is denoted as $N_{\mathcal{L}}$. An interpretation of variables in the sliced model is denoted as $\sigma_{\mathcal{L}}$.

Monitored and Controlled Variables The set of monitored variables and controlled variables of an execution e are denoted as mv(e) and cv(e) respectively.

5.2.4 Dependences

As introduced in Section 4.3, there are three types of dependences used by FormlSlicer: Hierarchy Dependence (HD), Data Dependence (DD), and Control Dependence (CD).

Definition 6. We say $n \in S_M$ is **hierarchy dependent** on $n' \in S_M$, denoted as $n \xrightarrow{hd} n'$, iff n is a child state of n''s containing region.

Definition 7. We say $t \in T_M$ is **data dependent** on $t' \in T_M$ with respect to v, denoted as $t \xrightarrow{dd}_v t'$, iff there exists a variable $v \in mv(t) \cap cv(t')$ and there exists a path $[t_1 \cdots t_k](k \ge 1)$ such that $t_1 = t'$, $t_k = t$ and $t_j \in T_M \land v \notin cv(t_j)$ for all 1 < j < k.

Definition 8. We say $n \in S_M$ (or $t \in T_M$) is **control dependent** on $n' \in S_M$, denoted as or $n \xrightarrow{cd} n'$ (or $t \xrightarrow{cd} n'$), iff n' has at least two outgoing edges, t_k and t_l ,

- 1. for all maximal paths from t_k , n (or t) always occurs and it occurs before any occurrence of n';
- 2. there exists a maximal path from t_l on which either n (or t) does not occur, or n (or t) is strictly preceded by n'.

Transitivity on dependences is also considered. If $n_1 \xrightarrow{hd} n_2$ and $n_2 \xrightarrow{hd} n_3$, then $n_1 \xrightarrow{hd} n_3$; this means that the state n_3 is the grandparent state of n_1 . Similarly, if $n_1 \xrightarrow{dd} n_2$ and $n_2 \xrightarrow{dd} n_3$, then $n_1 \xrightarrow{dd} n_3$. The transitivity applies to control dependence too.

5.3 State Transition Rule

The state transition rule defines how the current state configuration N evolves to the next state configuration N' in the original and the sliced model.

Intuitively, we know that through an execution step t, the current state configuration exits the source state of t and enters the destination state. This forms the base rationale of our state transition rule⁷.

First of all, we use two accessor functions for a transition t:

⁷In hierarchical systems without concurrency, the state transition rule for one transition t is non-trivial: the set of entered states includes not only ds(t), but also all of the ds(t)s ancestor states plus the default states of ds(t) and of its entered descendants [33]. By adding in concurrency, it becomes more complicated. Due to the complexity of such a state machine, we will not formalize the state transition rule strictly.

exited(t)

states exited when ss(t) is exited, including ss(t)'s ancestors and descendants;

entered(t)

states entered when ds(t) is entered, including ds(t)'s ancestors and relevant descendants' default start states.

The least common ancestor between two states is the state of highest rank that is an ancestor state of both states[34, 11].

Now, we can define a state transition rule for one transition t as:

$$N' = (N - exited(t)) \cup entered(t)$$

 S_M refers to the set of all states in model M.

- $N \subseteq S_M$ and $N' \subseteq S_M$ are the current and next state configuration of the model;
- exited(t) is the set of all states including:
 - the source state itself (ss(t)),
 - the ancestor states of ss(t) up along the tree of state hierarchy before reaching the least common ancestor with ds(t) (AncestorTillLCA(ss(t), ds(t))),
 - the descendant states of ss(t) (Descendants(ss(t))).
- entered(t) is the set of all states including:
 - the destination state itself (ds(t)),
 - the ancestor states of ds(t) up along the tree of state hierarchy before reaching the least common ancestor with ss(t) (AncestorTillLCA(ds(t), ss(t))),
 - the recursively identified default start states of ds(t) and its entered descendant states (InitDesc(ds(t))).

A more detailed version of the state transition rule will be:

$$N' = (N - ss(t) - AncestorTillLCA(ss(t), ds(t)) - Descendants(ss(t)))$$
$$\cup ds(t) \cup AncestorTillLCA(ds(t), ss(t)) \cup InitDesc(ds(t))$$

⁸If ds(t) is a composite state, then the default start state within ds(t) is entered; if the default start state is also a composite state, then the default start child state within the default start state is also entered. This is defined recursively.

5.4 FormlSlicer's Multi-Stage Model Slicing

Section 4.4 has elaborated on how the FormlSlicer performs a Multi-Stage Model Slicing Process on an FOSM with respect to the FOI. This section writes the process using the terminologies defined in Section 5.2.

5.4.1 Definitions

Firstly, we need to formalize some definitions.

The concept of the next part-of-slice state set has been informally introduced in Section 4.4.3.2. Here we define it formally.

Definition 9. The next part-of-slice state set of state n, denoted as $\widetilde{npos}(n)$, is the set of states such that for each $n' \in \widetilde{npos}(n)$:

- $n' \in S_{\mathcal{L}}$;
- \exists sequence of transitions $[t_1 \cdots t_k]$ such that $ss(t_1) = n \wedge ds(t_k) = n' \wedge (\forall i.1 \leq i \leq k.t_i \notin T_{\mathcal{L}} \wedge ParentState(ss(t_i)) = ParentState(ds(t_i))) \wedge (\forall j.1 \leq j < k.ds(t_j) \notin S_{\mathcal{L}}).$

Note that k can be 1 in Definition 9. In this case, there is exactly one out-of-slice transition between the state n and its next-part-of-slice state n'.

The concept of relevant variables has been informally introduced in Section 4.4.1 and Section 4.4.2.1 where it is used to initiate the initial selection of nodes into the sliced model. We need to formally define this concept.

Definition 10. We define v to be a **relevant variable**, written $v \in Rv$, iff there exists $t \in T_{FOI}$ such that either $v \in mv(t)$ or there exists t' such that $t' \stackrel{dd}{\Longrightarrow} t$ and $v \in mv(t')$.

Note that T_{FOI} represent $\bigcup_{\forall t \in T_{FOI}} t$ in Definition 10.

In other words, a variable is a relevant variable if it directly or indirectly controls the FOI. It appears in at least one data dependence entry in the DD table and there is at least one transition in the sliced model which uses it.

5.4.2 Multi-Stage Model Slicing Process

We denote T_{ROS} to represent $\bigcup_{\forall f \in ROS, \forall t \in T_f} t$ and S_{ROS} to represent $\bigcup_{\forall f \in ROS, \forall n \in S_f} n$.

At each step, certain model elements from the original model are added into the sliced model.

- 1. Initiation Stage
 - (a) Variable Extraction Step Let

$$Rv = \bigcup_{\forall t \in T_{FOI}} mv(t)$$

- (b) Initial Transition Selection Step $\forall v \in Rv. (\exists t \in T_{ROS}. v \in cv(t)) \Rightarrow (t \in T_{\mathcal{L}} \land mv(t) \subset Rv).$
- 2. General Iterative Slicing Stage
 - (a) DD Step $\forall t, t' \in T_{ROS}.(t \xrightarrow{dd} t' \land t \in T_{\mathcal{L}}) \Rightarrow (t' \in T_{\mathcal{L}} \land mv(t') \subset Rv).$
 - (b) Replacing Cross-Hierarchy Transition $\forall t \in T_{ROS}. (t \notin T_{\mathcal{L}} \land ParentState(ss(t)) \neq ParentState(ds(t))),$ create true transition $ss(t) \xrightarrow{t_{true}} ds(t)$ and add t_{true} to $T_{\mathcal{L}}$.
 - (c) Transition-to-State Step $\forall t \in T_{ROS}.t \in T_{\mathcal{L}} \Rightarrow (ss(t) \in S_{\mathcal{L}} \land ds(t) \in S_{\mathcal{L}}).$
 - (d) CD-HD Step $\forall n, n' \in S_{ROS}. (n \xrightarrow{cd} \xrightarrow{hd} n' \land n \in S_{\mathcal{L}}) \Rightarrow n' \in S_{\mathcal{L}}.$
- 3. Model Enrichment Stage
 - (a) Step I: State Merging Step
 - i. Rule 1 Consider two states $n, n' \in N_{ROS}.n \in S_{\mathcal{L}}$. Let $T_{n,n'}$ to be the set of all transitions $t \in T_{ROS}$ such that ss(t) = n and ds(t) = n', and $T_{n',n}$ to be the set of all transitions $t \in T_{ROS}$ such that ss(t) = n' and ds(t) = n. If $T_{n,n'} \neq \emptyset \land T_{n',n} \neq \emptyset \land (\forall t \in T_{n,n'} \cup T_{n',n} \Rightarrow t \notin T_{\mathcal{L}})$, then n and n' can be merged together.

ii. Rule 2

Consider two states $n, n' \in N_{ROS}.n \in S_{\mathcal{L}}$. Let $T_{n,n'}$ to be the set of all transitions $t \in T_{ROS}$ such that ss(t) = n and ds(t) = n'. Let T_n be the set of all transitions $t \in T_{ROS}$ such that ss(t) = n. If $T_{n,n'} \cap T_{\mathcal{L}} = \emptyset \wedge T_{n,n'} = T_n$, then n and n' can be merged together.

(b) Step II: True Transitions Creation $\forall n \in S_{\mathcal{L}}. (\forall n' \in \widetilde{npos}(n), \text{ create true transition } n \xrightarrow{t_{true}} n' \text{ and add } t_{true} \text{ to } T_{\mathcal{L}}.$

5.5 Proof

5.5.1 Projection of Snapshot in the Original Model to Snapshot in the Sliced Model

In Subsection 5.1.2, we present that the intuition is to show that the snapshot in original model can be projected to a corresponding snapshot in sliced model, and that such a projection is maintained before and after each step in original model's execution trace.

Recall from Definition 3 that a snapshot consists of two components: the state configuration and the interpretation of variables. Similarly, the projection of snapshot from the original model to the sliced model also include two notions:

- 1. the value of any relevant variable is the same in both the original model and the sliced model;
- 2. The state configuration of the original model has certain relation with that of the sliced model.

For the first notion, we only consider the system-controlled variables. Because the environment-controlled variables are influenced by the external environment, we cannot and need not to prove their values if any of them are monitored in a transition. For example, it is meaningless to prove that a variable like "actual temperature" has a value of "larger than 37°C".

For the second notion, based on the fact that true transitions are added into $T_{\mathcal{L}}$ connect two part-of-slice states⁹, we can imagine that sometimes the set of current states in sliced

⁹See "Step II: True Transitions Creation" in Section 4.4.3.2

model is larger than the set of current states in original model. This is acceptable because we allow extra execution traces in the sliced model. However, the state configuration in sliced model is not strictly a superset of that in original model, because those states that are not added into the sliced model cannot possibly appear in the state configuration of the sliced model. Based on these two observations, we write that the state configuration N in original model has the following relation with the state configuration $N_{\mathcal{L}}$ in sliced model, if that sliced model simulates the original model:

$$N \cap \mathcal{L} = N_{\mathcal{L}}$$

Definition 11. We define that a snapshot in the original model (N, σ) is **is projected to** another snapshot in the sliced model, $(N_{\mathcal{L}}, \sigma_{\mathcal{L}})$, when

- $N \cap \mathcal{L} \subseteq N_{\mathcal{L}}$;
- $\forall v \in Rv, \ \sigma(v) = \sigma_{\mathcal{L}}(v).$

We write it as $P((N, \sigma)) = ((N_{\mathcal{L}}, \sigma_{\mathcal{L}}))$.

5.5.2 Projection of One Transition in the Original Model to Epsilon or One Transition in the Sliced Model

We want to prove that one transition t in the original model can be projected to one transition $t_{\mathcal{L}}$ or epsilon in the sliced model (Figure 5.5c), such that if the snapshot in the original model is projected to the snapshot in the sliced model before the transition (Figure 5.5a), then the snapshot in the original model is still projected to the snapshot in the sliced model after the transition in the original model (Figure 5.5b).

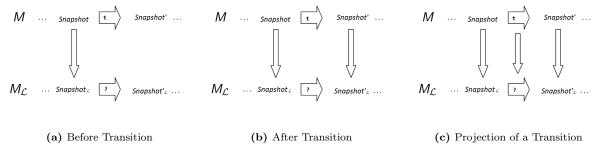
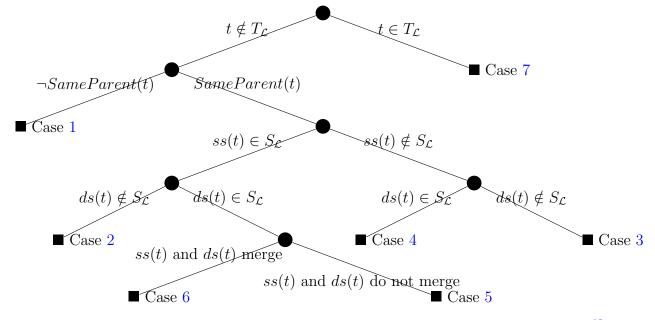


Figure 5.5: Projection of a Transition from the Original Model to the Sliced Model

This can be proved by case-based analysis. For brevity, we denote SameParent(t) to represent the condition of (ParentState(ss(t)) = ParentState(ds(t))).

We divide the situation into 7 different cases as shown in the decision tree below:



Lemma 1. Consider a transition t in the original model M, $M \vdash t : (N, \sigma) \Rightarrow (N', \sigma')^{10}$ The projection function of t to its counterpart $(t_{\mathcal{L}} \lor \epsilon)$ (consider $t_{\mathcal{L}}$ to be $M_{\mathcal{L}} \vdash t_{\mathcal{L}} : (N_{\mathcal{L}}, \sigma_{\mathcal{L}}) \Rightarrow (N'_{\mathcal{L}}, \sigma'_{\mathcal{L}})$) in the sliced model is:

$$P(t) = \begin{cases} t_{true} & \text{if } t \notin T_{\mathcal{L}} \land \neg SameParent(t) \\ \epsilon & \text{if } ss(t) \in S_{\mathcal{L}} \land ds(t) \notin S_{\mathcal{L}} \land t \notin T_{\mathcal{L}} \land SameParent(t) \\ \epsilon & \text{if } ss(t) \notin S_{\mathcal{L}} \land ds(t) \notin S_{\mathcal{L}} \land t \notin T_{\mathcal{L}} \land SameParent(t) \end{cases}$$
(2)
$$t_{true} & \text{if } ss(t) \notin S_{\mathcal{L}} \land ds(t) \notin S_{\mathcal{L}} \land t \notin T_{\mathcal{L}} \land SameParent(t) \\ t_{true} & \text{if } ss(t) \notin S_{\mathcal{L}} \land ds(t) \in S_{\mathcal{L}} \land t \notin T_{\mathcal{L}} \land SameParent(t) \\ \epsilon & \text{if } n_{merged} = (ss(t) \lor ds(t)) \in S_{\mathcal{L}} \land t \notin T_{\mathcal{L}} \land SameParent(t) \\ t & \text{if } t \in T_{\mathcal{L}} \end{cases}$$
(6)

such that given $P((N, \sigma)) = ((N_{\mathcal{L}}, \sigma_{\mathcal{L}}))$, then:

$$P((N', \sigma')) = \begin{cases} (N_{\mathcal{L}}, \sigma_{\mathcal{L}}) & \text{for the cases of 2, 3 and 6} \\ (N'_{\mathcal{L}}, \sigma'_{\mathcal{L}}) & \text{for the cases of 1, 4, 5 and 7} \end{cases}$$

 $^{^{10}}$ Recall from Section 3.1 that a model M is a big state machine consisting of k FOSMs, each as a sub-state machine in one of its k orthogonal regions. Also, recall from Section 5.2.3 that we write e=t when the execution step consists of only one transition t.

Proof.

Given Conditions Because $P((N, \sigma)) = ((N_{\mathcal{L}}, \sigma_{\mathcal{L}}))$, we know that:

$$N \cap \mathcal{L} \subseteq N_{\mathcal{L}} \tag{8}$$

$$\sigma_{\mathcal{L}}(v) = \sigma(v) \forall v \in Rv \tag{9}$$

Also, the state transition rule is:

$$N' = (N - ss(t) - AncestorTillLCA(ss(t), ds(t)) - Descendants(ss(t)))$$

$$\cup ds(t) \cup AncestorTillLCA(ds(t), ss(t)) \cup InitDesc(ds(t))$$
(10)

The Case of Cross-Hierarchy Transition This proves for Case (1).

When $(t \notin T_{\mathcal{L}}) \wedge (\neg SameParent(t))$, the step of Replacing Cross-Hierarchy Transition in General Iterative Slicing Stage will replace t with a "true" transition $t_{true} \in T_{\mathcal{L}}$, which preserves the original ss(t) and ds(t). Then because of the Transition-to-State Step,

$$ss(t), ds(t) \in \mathcal{L}$$
 (11)

Because of (11) and the CD-HD Step in General Iterative Slicing Stage, we get:

$$AncestorTillLCA(ss(t), ds(t)) \subset S_{\mathcal{L}}, \quad AncestorTillLCA(ds(t), ss(t)) \subset S_{\mathcal{L}}.$$
 (12)

We can also observe that:

$$Descendants(ss(t)) \cap S_{\mathcal{L}} = Descendants_{\mathcal{L}}(ss(t))$$
 (13)

$$InitDesc(ss(t)) \cap S_{\mathcal{L}} = InitDesc_{\mathcal{L}}(ss(t))$$
 (14)

Given the condition (8), (10), (11), (12), (13) and (14), we can deduce that:

$$N' \cap S_{\mathcal{L}} \subseteq N'_{\mathcal{L}}. \tag{15}$$

Next, we want to prove that $\sigma'(v) = \sigma'_{\mathcal{L}}(v) \forall v \in Rv$. In order to do so, we can firstly prove $\sigma(v) = \sigma'(v) \forall v \in Rv$ by assuming in contradiction that there is a variable $v \in Rv$ that has its value changed through t, making $\sigma(v) \neq \sigma'(v)$. Then $v \in cv(t)$. Based on Definition 10, there must be another transition $t_x \in T_{\mathcal{L}}$ such that $v \in mv(t_x)$ and a sequence of execution steps exist between t_x and t. According to the DD Step in General

Iterative Slicing Stage, as $t_x \xrightarrow{dd}_v t, t_x \in T_{\mathcal{L}}$, so $t \in T_{\mathcal{L}}$ which contradicts with the given condition $t \notin T_{\mathcal{L}}$. Therefore:

$$\sigma(v) = \sigma'(v) \forall v \in Rv \tag{16}$$

In addition, because t_{true} does not change values of any variables in the sliced model,

$$\sigma_{\mathcal{L}} = \sigma_{\mathcal{L}}' \tag{17}$$

Given condition (9), (16) and (17), we get

$$\sigma_{\mathcal{L}}'(v) = \sigma_{\mathcal{L}}(v) = \sigma(v) = \sigma'(v) \forall v \in Rv.$$
(18)

Given both (15) and (18), we can deduce that $P((N', \sigma')) = (N'_{\mathcal{L}}, \sigma'_{\mathcal{L}})$ by projecting the transition t in the original model to t_{true} in the sliced model.

The Case of Having Only Source State in Slice This proves for Case (2).

When $ss(t) \in S_{\mathcal{L}} \wedge ds(t) \notin S_{\mathcal{L}} \wedge t \notin T_{\mathcal{L}} \wedge SameParent(t)$, the state configuration in the sliced model does not change when the state configuration in original model changes from N to N' through the transition t. We observe that:

$$SameParent(t) \Rightarrow (AncestorTillLCA(ss(t), ds(t)) = AncestorTillLCA(ds(t), ss(t)) = \emptyset)$$

(19)

$$ds(t) \notin S_{\mathcal{L}} \Rightarrow InitDesc(ds(t)) = \emptyset$$
 (20)

Because of (19) and (20), we get:

$$entered(t) \cap \mathcal{L} = \emptyset$$
 (21)

Because of (21), (8) and the state transition rule (10), and the fact that exited(t) will not affect the subset relation between state configuration in the original model and $N_{\mathcal{L}}$, we have

$$N' \cap S_{\mathcal{L}} \subseteq N_{\mathcal{L}}. \tag{22}$$

Next, we want to prove that $\sigma'(v) = \sigma_{\mathcal{L}}(v) \forall v \in Rv$. In order to do so, we can firstly prove $\sigma(v) = \sigma'(v) \forall v \in Rv$; this proof will be exactly same as that in the Case 1 because of the DD Step. Given condition (9), we can therefore deduce that

$$\sigma_{\mathcal{L}}(v) = \sigma'(v) \forall v \in Rv.$$
 (23)

Given both (22) and (23), we can deduce that $P((N', \sigma')) = (N_{\mathcal{L}}, \sigma_{\mathcal{L}})$ by projecting the transition t in the original model to epsilon ϵ in the sliced model.

The Case of Having Nothing in Slice This proves for Case (3).

When $ss(t) \notin S_{\mathcal{L}} \wedge ds(t) \notin S_{\mathcal{L}} \wedge t \notin T_{\mathcal{L}} \wedge SameParent(t)$, the state configuration in the sliced model does not change when the state configuration in original model changes from N to N' through the transition t. This case is same as Case (2) except that ss(t) is not in the slice. Because of the fact that exited(t) in state transition rule (10) will not affect the subset relation between state configuration in the original model and $N_{\mathcal{L}}$, this difference does not matter. Therefore, the proof about state configuration will be exactly the same as in the Case (2). Therefore:

$$N' \cap \mathcal{L} \subseteq N_{\mathcal{L}}.$$
 (24)

Next, we want to prove that $\sigma'(v) = \sigma_{\mathcal{L}}(v) \forall v \in Rv$. In order to do so, we can firstly prove $\sigma(v) = \sigma'(v) \forall v \in Rv$; this proof will be exactly same as that in the Case 1 because of the DD Step. Given condition (9), we can therefore deduce that

$$\sigma_{\mathcal{L}}(v) = \sigma'(v) \forall v \in Rv. \tag{25}$$

Given both (24) and (25), we can deduce that $P((N', \sigma')) = (N_{\mathcal{L}}, \sigma_{\mathcal{L}})$ by projecting the transition t in the original model to epsilon ϵ in the sliced model.

The Case of Having Only Destination State in Slice This proves for Case (4).

When $ss(t) \notin S_{\mathcal{L}} \land ds(t) \in S_{\mathcal{L}} \land t \notin T_{\mathcal{L}} \land SameParent(t)$, the step of Step II: True Transitions Creation in Model Enrichment Stage has searched from another state $n \in \mathcal{L}$ to reach $ds(t) \in \widetilde{npos}(n)$ and creates a "true" transition $n \xrightarrow{t_{true}} ds(t)$. The step has ensure that all the states along the path $[n_1, \ldots, n_k]$ $(n_1 = n, n_k = ds(t))$ are at the same rank of state hierarchy, and therefore in the state transition rule (10) we know that:

$$AncestorTillLCA(n, ds(t)) = AncestorTillLCA(n_i, n_j) = \emptyset. \forall (i, j \in [1 \cdots k]) \land (i \neq j)$$

$$(26)$$

$$(ds(t) \in \mathcal{L}) \Rightarrow (InitDesc(ds(t)) \cap \mathcal{L} = InitDesc_{\mathcal{L}}(ds(t)))$$
 (27)

In the sliced model, the "true" transition has changed the state configuration such that ds(t), $InitDesc_{\mathcal{L}}(ds(t))$ will be entered and n and Descendants(n) will be exited (because of (26), we will ignore their ancestor states in state transition rule (10)).

From the analysis result of Case (2) and Case (3), we know that the subset relation of state configurations between sliced model and original model is maintained when the state configuration in the original model changes through a sequence of transitions while

the state configuration in the sliced model remains unchanged. Therefore, condition (8) holds in this case.

Because of (26), (27), and (8), we can get that

$$N' \cap \mathcal{L} \subseteq N'_{\mathcal{L}}. \tag{28}$$

Next, we want to prove that $\sigma'(v) = \sigma'_{\mathcal{L}}(v) \forall v \in Rv$. In order to do so, we can firstly prove $\sigma(v) = \sigma'(v) \forall v \in Rv$; this proof will be exactly same as that in the Case 1 because of the DD Step. Together with condition (9), we get

$$\sigma_{\mathcal{L}}'(v) = \sigma'(v) \forall v \in Rv. \tag{29}$$

Given both (28) and (29), we can deduce that $P((N', \sigma')) = (N'_{\mathcal{L}}, \sigma'_{\mathcal{L}})$ by projecting the transition t in the original model to t_{true} in the sliced model.

The Case of Having Source and Destination States in Slice This proves for Case (5).

When $ss(t) \in S_{\mathcal{L}} \wedge ds(t) \in S_{\mathcal{L}} \wedge t \notin T_{\mathcal{L}} \wedge SameParent(t)$, the Step II: True Transitions Creation in Model Enrichment Stage will add in a "true" transition t_{true} to the slice connecting ss(t) and ds(t). Thus we know that the state configuration in the sliced model will change through t_{true} in the same fashion as that in the original model through t. Given condition (8), we thus know that:

$$N' \cap \mathcal{L} \subseteq N'_{\mathcal{L}}. \tag{30}$$

Next, we want to prove $\sigma'(v) = \sigma'_{\mathcal{L}}(v) \forall v \in Rv$. Like the proof for all above cases, the fact that $t \notin T_{\mathcal{L}}$ is that it does not control any relevant variables and thus is not selected into the slice during the DD Step. Similarly, we get:

$$\sigma_{\mathcal{L}}'(v) = \sigma'(v) \forall v \in Rv. \tag{31}$$

Given both (30) and (31), we can deduce that $P((N', \sigma')) = (N'_{\mathcal{L}}, \sigma'_{\mathcal{L}})$ by projecting the transition t in the original model to t_{true} in the sliced model.

The Case of Having a Merged State in Slice This proves for Case (6).

When $n_{merged} = (ss(t) \vee ds(t)) \in S_{\mathcal{L}} \wedge t \notin T_{\mathcal{L}} \wedge SameParent(t)$, which satisfy one of the two state merging rules, are merged together to become a merged state n_{merged} because of the State Merging Step in Model Enrichment Stage. We know that:

$$n_{merged} = (ss(t) \lor ds(t)) \tag{32}$$

$$n_{merged} \in N_{\mathcal{L}}$$
 (33)

Because (32) and (33),
$$ds(t) = n_{merged} \in N_{\mathcal{L}}$$
 (34)

The state configuration in sliced model remains unchanged as $N_{\mathcal{L}}$.

Because of the CD-HD Step in General Iterative Slicing Stage, the parent node of $ss(t), ds(t), n_{merged}^{11}$, p must have been added to the slice set. Because of (33) and the CD-HD Step,

$$p \in N_{\mathcal{L}}, \forall p. (n_{merged} \xrightarrow{hd} p)$$
 (35)

Because (35),
$$AncestorTillLCA(ds(t), ss(t)) \subseteq N_{\mathcal{L}}$$
 (36)

Because during the <u>State Merging Step</u> in Model Enrichment Stage, the merged state will contain all child regions of the original states if they are composite states. Therefore:

$$InitDesc(ds(t)) \subseteq N_{\mathcal{L}}$$
 (37)

We apply the state transition rule in original model from Equation (10) and finds that all components of entered(t) are all subsets of $N_{\mathcal{L}}$ as explained in (34), (37) and (36). Given that (8), we can deduce that $N' \cap \mathcal{L}$ remains the same subset relation with $N_{\mathcal{L}}$, as

$$N' \cap \mathcal{L} \subseteq N_{\mathcal{L}} \tag{38}$$

Next, we want to prove that $\sigma'(v) = \sigma'_{\mathcal{L}}(v) \forall v \in Rv$. When $t \notin T_{\mathcal{L}}$, the proof will be same as the cases in (2), (3), (4), (5) because of the DD Step. Therefore:

$$\sigma'(v) = \sigma_{\mathcal{L}}'(v) \forall v \in Rv \tag{39}$$

Given both (38) and (39), we can deduce that $P((N', \sigma')) = (N'_{\mathcal{L}}, \sigma'_{\mathcal{L}})$ by projecting the transition t in the original model to ϵ in the sliced model.

¹¹The two SNodes, ss(t) and ds(t), are merged only when they are at the same rank of state hierarchy; their merged node is therefore at the same rank of hierarchy. See Section 4.4.3.1 for further details.

The Case when the Transition is Part-of-Slice This proves for Case (7).

When $t \in T_{\mathcal{L}}$, according to the <u>Transition-to-State Step</u> in General Iterative Slicing Stage, $ss(t) \in S_{\mathcal{L}}$, $ds(t) \in S_{\mathcal{L}}$. The state configuration in original model changes in the same fashion as that in the sliced model. Because $t \in T_{\mathcal{L}}$, the value of any relevant variable in the sliced model will change in the same way as that in the original model. Therefore, $P((N', \sigma')) = (N'_{\mathcal{L}}, \sigma'_{\mathcal{L}})$ by projecting the transition t in the original model to t in the sliced model.

5.5.3 Projection of One Execution Step in the Original Model to One Execution Step in the Sliced Model

As mentioned in Section 5.2.3, each execution step involves a set of transitions which occur concurrently, denoted as:

$$e = \vdots$$

$$t_k$$

In addition, we have proved that $P(t) = (\epsilon \vee t_{\mathcal{L}})$ in Lemma 1.

Moreover, according to Definition 5, each concurrent transition of an execution step e occurs in a distinct orthogonal region; they do not interfere each other.

Based all the above evidences, We can compose the projections of the transitions in e together to form $e_{\mathcal{L}}$:

$$P(e) = P\begin{pmatrix} t_1 \\ \vdots \\ t_k \end{pmatrix} = \begin{pmatrix} P(t_1) \\ \vdots \\ P(t_k) \end{pmatrix} = e_{\mathcal{L}}$$

$$\tag{40}$$

such that $P(t_j) = (\epsilon \vee t_{\mathcal{L}})$ for all $j.1 \leq j \leq k$.

In other words, an execution step e in the original model is projected to an executions step $e_{\mathcal{L}}$ in the sliced model. This means that if the snapshot in the original model is projected to the snapshot in the sliced model before e, then the snapshot in the original model is projected to the snapshot in the sliced model after e.

5.5.4 Simulation

The initial snapshot of the original model will be (N^I, σ^I) . N^I will be the set of root state and all the default start states of relevant descendant states of the root state, identified recursively. $\sigma^I(v)$ for all $v \in Rv$ will be at default or uninitialized value of each variable.

Intuitively, we know that the initial state configuration in the sliced model $N_{\mathcal{L}}^{I}$ will be:

$$N_{\mathcal{L}}^{I} = (N^{I} \cap S_{\mathcal{L}}) \cup N^{newI}$$

where N^{newI} is the new default start states in the sliced model¹². Therefore, $N^I \cap \mathcal{L} \subseteq N^I_{\mathcal{L}}$.

In addition, we also know that the values of all relevant variables in the sliced model are at their default or uninitialized values, because no transitions have occurred yet when the model is in its initial state configuration. Therefore, $\sigma^I(v) = \sigma_L^I(v) \forall v \in Rv$.

Because $N^I \cap \mathcal{L} \subseteq N^I_{\mathcal{L}}$ and $\sigma^I(v) = \sigma^I_{\mathcal{L}}(v) \forall v \in Rv$, we can conclude that the initial snapshot in the original model can be projected to the initial snapshot in the sliced model. This forms the **base case** of the simulation.

The **inductive case** is that if the snapshot in the original model is projected to the snapshot in the sliced model before e, then the snapshot in the original model is projected to the snapshot in the sliced model after e. This is already proved in Section 5.5.3.

Together with the base case and the inductive case, we know that the original model's snapshot is always projected to the sliced model's snapshot for the whole execution trace in the original model. We can therefore conclude that:

Theorem 1. By simulating an original model inside a sliced model produced by FormlSlicer, an execution step in original model can always be projected into one execution step in sliced model.

This completes our correctness proof for FormlSlicer.

As a summary, this chapter proves that the sliced model produced by FormlSlicer is correct. However, correctness is not a sufficient criterion for a good model slicer. In the next chapter, we will present the empirical evaluation on FormlSlicer to show that the sliced model is not only correct, but also useful.

 $^{^{12}}$ Recall from the sub-step 1 of "True Transitions Creation" in Section 4.4.3.2 that sometimes when the original default start state is missing in the sliced model, FormlSlicer will search for the next part-of-slice state to be a new default start state.

Chapter 6

Empirical Evaluations of FormlSlicer

This chapter will show that FormlSlicer successfully implements our proposed workflow in Chapter 4 and that it significantly reduces the size of the original model.

FormISlicer is a tool implemented using Java. At the time of writing, it has 2743 lines of code and is available as an open-source project in GitHub¹.

We use two models for slicing targets. As the pictures of the models are big, they are shown in Appendix A and Appendix B respectively.

6.1 Reduction of Model Size

The first model is an automotive case study. The FOSMs are primarily derived from the FORML model from Shaker's automotive case study [11]. Some functions used in the model are derived from Dietrich's mode-based state machines that model the behavioural requirements of production-grade automotive features [35].

Figure A.1 shows the original model. It consists of five FOSMs:

- Adaptive Cruise Control (ACC) (Figure A.2)
- Forward Collision Alert (FCA) (Figure A.3)
- Lane Change Alert (LCA) (Figure A.4)

¹FormISlicer is available at https://github.com/erencie/FORMLSlicer, as of 21 March 2015.

- Lane Centring Control (LCC) (Figure A.5)
- Speed Limit Control (SLC) (Figure A.6)

Each FOSM is in one orthogonal region of the composite state within the model. As explained in Section 3.1, this is a 150% model.

In Section 1.1.2, we mentioned that a useful sliced model must be smaller than the original model. Our FormlSlicer is able to achieve what we want. Table 6.1 shows the empirical results on the automotive case study. Because there are four types of model elements in FORML—state, region, transition and variable, we use them to measure a model's size. The original model consists of 66 states, 46 variables, 46 regions and 79 transitions. As FormlSlicer has multiple slicing processes², each considering a different feature as the FOI, we therefore have five different sliced models for the automotive case study.

Model	# States	# Variables	# Regions	# Transitions
Original Model	66	46	46	79
Sliced Model w.r.t. ACC	40	19	31	41
Sliced Model w.r.t. LCA	21	5	18	13
Sliced Model w.r.t. FCA	45	22	34	45
Sliced Model w.r.t. LCC	48	24	37	50
Sliced Model w.r.t. SLC	41	21	31	43
Average Percentage of Sliced/Original	59.1%	40.9%	65.7%	48.6%

Table 6.1: Empirical Results of FormlSlicer on the Automotive Case Study

From Table 6.1, we can see that each of the five sliced models has a reduced size as compared to the original model. In average, a sliced model has 59.1% of states, 40.9% of variables, 65.7% of regions and 48.6% transitions of the original model. This is a significant reduction on the model size.

The first observation from Table 6.1 is that the number of regions is not as significantly reduced as other model elements in the sliced model. The reason is that FormlSlicer does not change the state hierarchy structure; sometimes, in order to keep a transition within an innermost region, FormlSlicer keeps many layers of state hierarchy. Figure A.10 is a good example on this problem. In order to keep a transition LCCt5 within the region

²See Section 4.1 on the different slicing processes in the slicing task.

centerCar, all the parent states and regions (e.g., region LCC) are kept in the sliced model as well. In an ideal sliced model, these parent states and regions should be "sliced away" so that the transition LCCt5 can be directly placed under the region CCmain. The same problem affects the reduction of states in the sliced model as well; but because of our State Merging Step, the reduction in the number of states is still better than that in the number of regions. We will make some recommendations on improving this situation in Chapter 7.

The second observation from Table 6.1 is that not every sliced model has same degree of reduction. Some sliced models (e.g., the sliced model w.r.t. LCA) are much smaller than the others. This is because the FOI in the sliced model has fewer feature interactions with the other features. For example, the feature of LCA is only monitoring those system-controlled variables related to the vehicle's steering direction (e.g., car.steerDirection), whilst the majority of features in the model (ACC, FCA and SLC) are affecting the variables related to vehicle's acceleration. In this case, the sliced model consists only the FOI and a very small portion of the ROS.

6.2 Testing the Multi-Stage Model Slicing Process

The second model is created by our own in order to test some steps in the Multi-Stage Model Slicing Process that are not used in the first model. We call it a "stress test". Figure B.1 shows the original model. It consists of four FOSMs—E1 (Figure B.2), E2 (Figure B.3), E3 (Figure B.4) and E4 (Figure B.5). The sliced model with respect to E1 is shown in Figure B.6.

In Section 4.4, we have explained the majority of steps in the Multi-Stage Model Slicing Process using a slicing example. The slicing example we use is E2. The resultant sliced FOSM is shown in Figure B.7. However, there are a few corner cases that are not covered in the examples; so we create E3 and E4.

Here are the steps in the Multi-Stage Model Slicing Process that are not covered in E2:

Replacing Cross-Hierarchy Transition

This is a step in the General Iterative Stage. As explained in Section 4.4.2.2, any cross-hierarchy transitions will be retained in the sliced model. There are two cross-hierarchy transitions in the FOSM E4 (Figure B.5): cross1 transits from the state nx within the state inactive to the state active; cross2 transits from the state ny within inactive to the state nk within active. Both cross1 and cross2 are preserved in the sliced FOSM (Figure B.9).

State Transition Rule 1

Section 4.4.3.1 presents two state merging rules. In Rule 1, if there exist out-of-slice transitions from state n to n' and also from state n' to n, these two states are merged into one state "n,n'". This is shown in the FOSM E3 (Figure B.4). The transitions t3 and t4 are both out-of-slice and transiting between states n2 and n3; therefore n2 and n3 are merged (Figure B.8).

Sub-step 1: Search for New Default Start States

Section 4.4.3.2 presents the "True Transitions Creation" step in the Model Enrichment Stage. There are two sub-steps. The first sub-step is to search for the new default start state for the sub-state machine. In the FOSM E4, the state nz and the transition t4 is not added into the sliced model, making the state nk to be the next part-of-slice state for the pseudo state in the region of withinactive. In the sliced model, nk becomes the new start state in the sub-state machine within the region withinactive.

As a summary, FormlSlicer has implemented correctly on all the steps specified in the Multi-Stage Model Slicing Process.

Chapter 7

Conclusion

This chapter presents a summary of this thesis and its contributions, as well as possible directions for future work.

7.1 Summary of Thesis and Contributions

This thesis mainly consists of four parts:

Literature Survey on **SBM** Slicing

Chapter 2 presents the history, the challenges, the various proposed slicing techniques, the various dependences' definitions and discussions on slicing correctness that are related to SBM slicing.

A Detailed Slicing Workflow

Chapter 3 and Chapter 4 propose a workflow of slicing on the Behaviour Model in FORML. The workflow includes two tasks: the preprocessing task and the slicing task. The preprocessing task converts the original FORML semantics to a simpler data structure—CFG and computes three types of dependences within CFG. The slicing task is to fork off multiple processes, each working on a different feature as the FOI; this is the Multi-Stage Model Slicing Process.

Correctness

Chapter 5 presents the proof to show the correctness of the proposed slicing workflow. It proves that an execution trace in the original model can be simulated by at least

one execution trace in the sliced model, which is produced by the proposed slicing workflow.

The Tool

An open-source model slicing tool—FormlSlicer—implements the proposed slicing workflow. Chapter 6 presents the testing and empirical evaluations on this tool to show that the proposed slicing workflow can generate useful sliced models for the Behaviour Model in FORML.

As a nutshell, this thesis proposes a unique slicing workflow on a hierarchical and concurrent state-based model for feature-oriented SPL requirements, by coalescing various slicing techniques from the literature, and then evaluates the workflow theoretically and empirically.

7.1.1 Contributions

This thesis has the following contributions.

- 1. Compared to other existing SBM slicing approaches, the target model of this slicing workflow is much more complex. We devise different ways to tackle the different challenges of the model.
 - The challenge of having hierarchical construct is solved by using Hierarchy Dependence (HD). In HD, each state is mapped to its parent state. Therefore, the difficult task of slicing a hierarchical state machine is decomposed into many simple tasks of slicing on flat state machines.
 - The challenge of having concurrent construct is also solved by using HD. Each parent state is mapped to multiple start states, each in one of its containing regions.
 - The challenge of having "inState" expression in guard condition is solved by making it as a subtype of Data Dependence (DD).
 - The challenge of having cross-hierarchy transitions is solved by preserving these transitions. Because the Multi-Stage Model Slicing Process is designed not to change the state hierarchy, these transitions can be correctly preserved in the sliced model.

- The complexity of having feature fragments in the model is solved by composing the feature fragments with their corresponding base features. Therefore, each feature can be represented as an FOSM and be sliced in the same way as one another.
- 2. We design a unique workflow by coalescing different slicing techniques from multiple literature studies, including:
 - Korel et al.'s state merging rules [5],
 - Various existing algorithms in data dependence [5, 20],
 - Ranganath et al.'s definition and algorithm in control dependence [22],
 - Ojala's use of CFG to perform slicing on an SBM [19],
 - and Kamischke et al.'s use of a model enrichment step in the slicing algorithm which incrementally adds the model elements [17].
- 3. We simplify the descriptive and complex semantics of FORML so that it becomes possible to automate the slicing on the behaviour model of FORML.
 - We converts the model into CFGs, so as to simplify the complex structures of state, region and transitions in FORML into a simple graph representation consisting of only nodes.
 - We converts the transition label in FORML, which contains complex information on events, guard and actions, into two groups of variables—monitored variables and controlled variables.
- 4. We conduct a proof to show that the workflow we have proposed can produce correct sliced models.
- 5. Lastly, we implement a tool to show that this slicing workflow is feasible.

7.2 Future Work

The following are possible directions for extending the work presented in this thesis.

7.2.1 Customization of Slicing in FormlSlicer

The FormlSlicer tool can be extended by adding more customization options for the users.

Keeping Some Environment-Controlled Variables in the Sliced Models By observing the automotive case study in Appendix A, we find that it is a bit confusing that certain states are merged. For example, the on and off states are merged together (e.g., the sliced ACC feature w.r.t. LCA in Figure A.8). The reason is that the triggering events for transitions between on and off are IgniteOn+ and IgniteOff+ (e.g., Figure A.2)—they are both environment-controlled variables. The mutual transitions between On and Off are thus not added into the sliced model during the DD Step in the General Iterative Slicing Stage. This makes On and Off satisfy the State Merging Rule 1 and therefore they are merged together.

Some engineers may want to keep the triggering events IgniteOn+ and IgniteOff+ in the sliced model. FormISlicer can be extended to allow such a customization. This can be done by reading a list of user-defined variables and add them into the set of relevant variables, before the DD Step. By allowing so, the transitions between on and off are preserved in the sliced model and these two states will not be merged.

Only Interested in a Few Features but not All Although the use of concurrent slicing processes is efficient in producing multiple sliced models with respect to different features, this is an overkill to someone who just want to focus on one feature. FormlSlicer can be extended to allow users to specify which features they want to focus and then only forks off a few slicing processes.

Adjusting Degree of Reduction and Precision A more advanced FormlSlicer can allow users to customize the degree of reduction and precision in the sliced models, depending on the users' needs. More aggressive state merging rules can be implemented in FormlSlicer; they all aim to reduce the size of the sliced model further. Users can be allowed to select which state merging rules to use during the Multi-Stage Model Slicing Process. The more state merging rules they choose to use, the smaller and (potentially) more imprecise the sliced models will become. In this way, we can leave the decision over trade-off between degree of reduction and precision to users.

7.2.2 Improving the Multi-Stage Model Slicing Process

Currently, the Multi-Stage Model Slicing Process we propose is still conservative.

As mentioned in Section 6.1, the number of regions is not as significantly reduced as other model elements in the sliced model, because our model slicing process does not

distort the state hierarchy of the original model at all. However, in some special cases (e.g., Figure A.10), it is preferable to merge several layers of state hierarchy together so that the sliced model looks more neat. In future work, we can study on how to merge different layers of state hierarchy of a model without making the sliced model incorrect.

Another issue is that currently we preserve all cross-hierarchy transitions in the sliced model. Taking away any cross-hierarchy transitions while maintaining the correctness of the sliced model will be a non-trivial task. We can conduct another independent project to specifically study on slicing a hierarchical state machine with cross-hierarchy transitions.

7.2.3 Making the Correctness Proof More Rigorous

Currently, many definitions in the correctness proof are not formalized strictly because of their complexities. Some examples are shown below.

- The state transition rule (Section 5.3) is not formalized because of its complexity. In this thesis, we use six components to represent the state transition rule, including ss(t), AncestorTillLCA(ss(t), ds(t)), Descendants(ss(t)), ds(t), AncestorTillLCA(ds(t), ss(t)) and InitDesc(ds(t)). Only ss(t) and ds(t) are clearly defined as the source state and destination state of the transition t. The other four components are described using plain English.
- The state machine used in FOSM is not formalized. In Section 5.2.2, we introduce this state machine in a paragraph. But it is not trivial to formalize it as a tuple, because this state machine contains many model components and each component is in a relationship with one another (e.g., state and region forming a containment relation).

A possible future work can make the correctness proof more rigorous by defining the concepts formally. This requires a non-trivial amount of efforts.

7.2.4 Using FormlSlicer

As mentioned in Section 1.2.2, the sliced models can be used for two purposes: model comprehension of feature-oriented requirements in SPLs, compositional verification of SPLs. For the first purpose, more case studies (from the automotive and telephony domains, as well as other domains such as banking, email, and smart homes) can be performed. User

studies can be conducted to evaluate the usefulness of sliced models produced by Forml-Slicer. For the second purpose, a conversion between an FORML SPL model and our 150% model needs to be performed.

Appendix A

Automotive: A Slicing Example

The original model, as shown in Figure A.1, consists of five FOSMs—ACC (Figure A.2), FCA (Figure A.3), LCA (Figure A.4), LCC (Figure A.5) and SLC (Figure A.6).

Figure A.7 shows the sliced automotive model with respect to the feature of LCA. It consists of the original LCA (because it is the FOI) and a sliced ROS. The sliced FOSMs in the ROS are shown in Figure A.8, Figure A.9, Figure A.10 and Figure A.11.

Figure A.12 shows the sliced automotive model with respect to the feature of ACC. It consists of the original ACC (because it is the FOI) and a sliced ROS. The sliced FOSMs in the ROS are shown in Figure A.13, Figure A.14, Figure A.15 and Figure A.16.

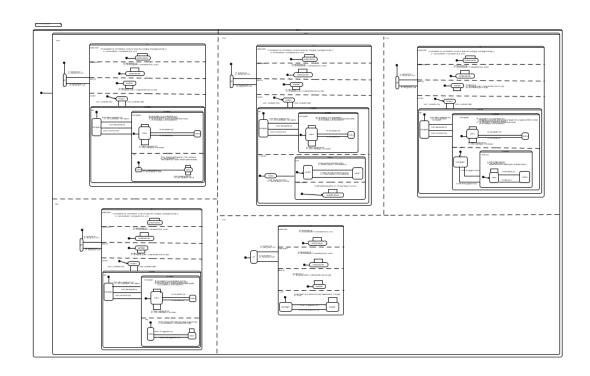


Figure A.1: The Original Automotive Model

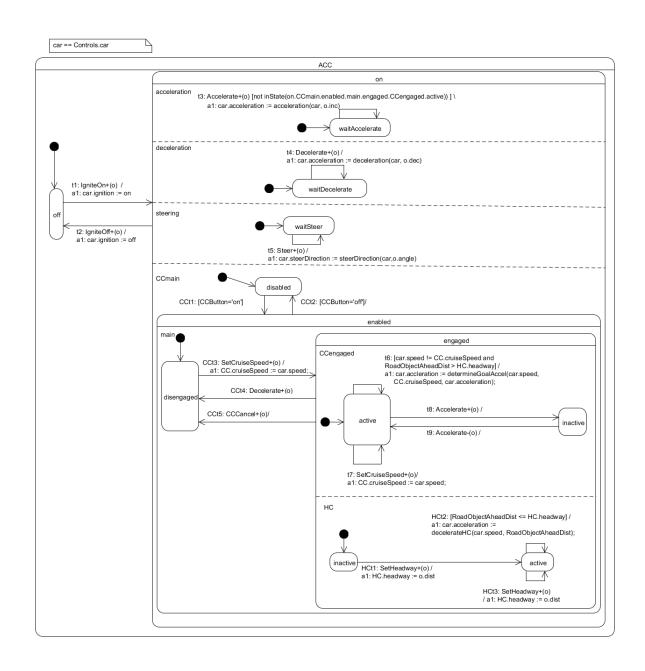


Figure A.2: Original ACC feature of the Automotive Model

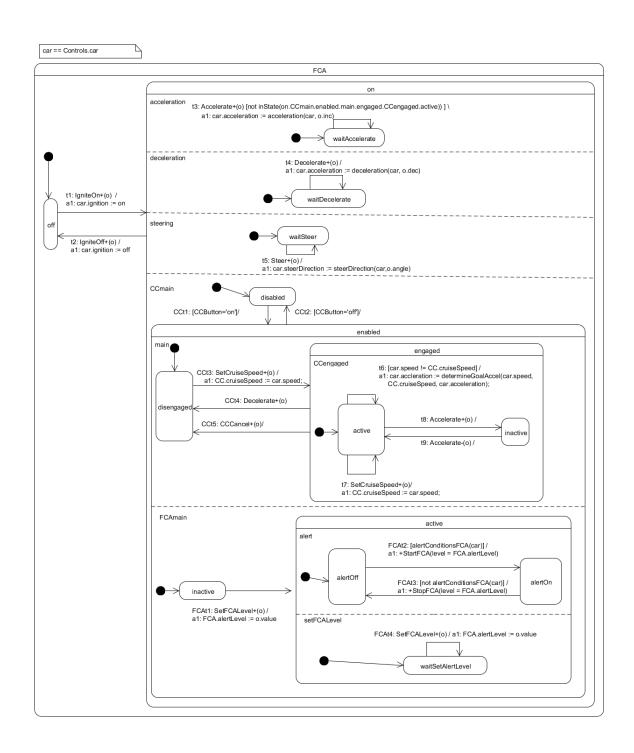


Figure A.3: Original FCA feature of the Automotive Model

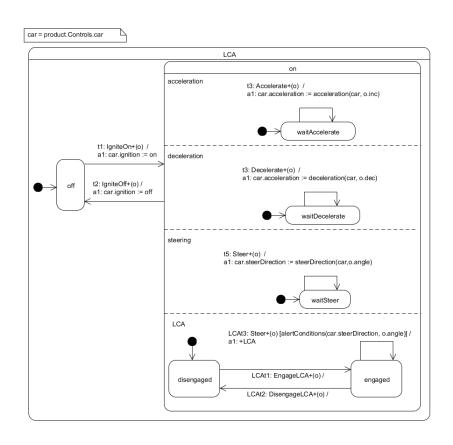


Figure A.4: Original LCA feature of the Automotive Model

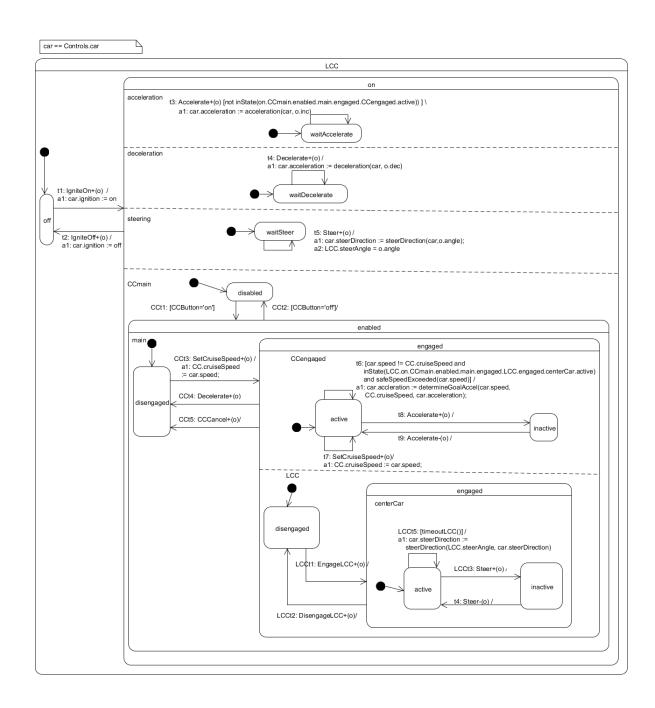


Figure A.5: Original LCC feature of the Automotive Model

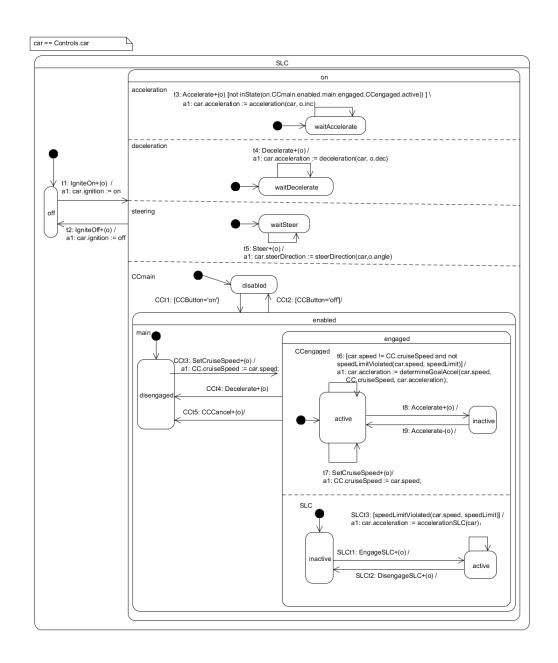


Figure A.6: Original SLC feature of the Automotive Model

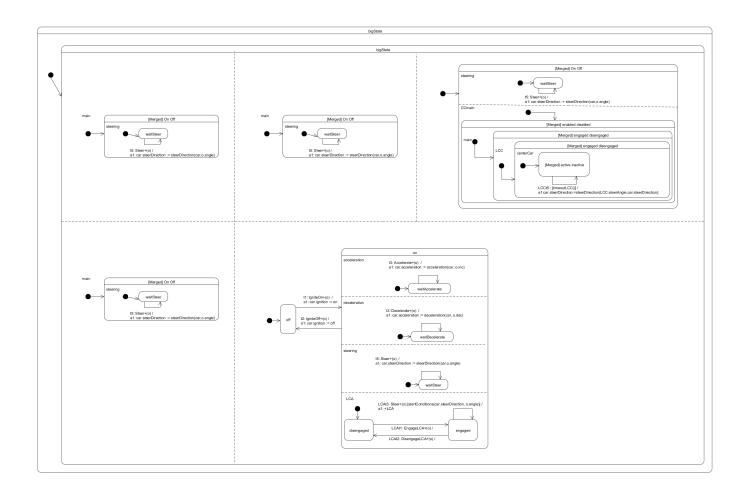


Figure A.7: The Sliced Model w.r.t. LCA

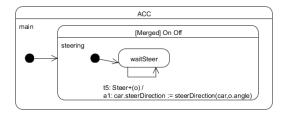


Figure A.8: Sliced ACC feature w.r.t. LCA

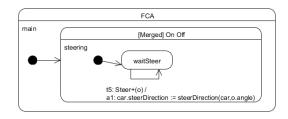


Figure A.9: Sliced FCA feature w.r.t. LCA

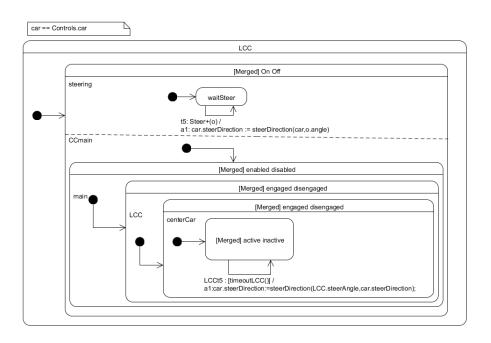


Figure A.10: Sliced LCC feature w.r.t. LCA

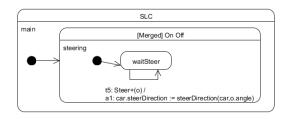


Figure A.11: Sliced LCC feature w.r.t. LCA

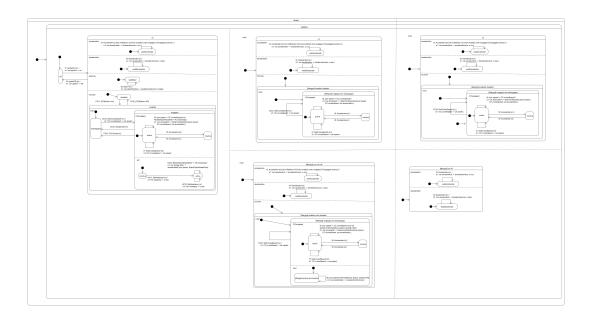


Figure A.12: The Sliced Model w.r.t. ACC

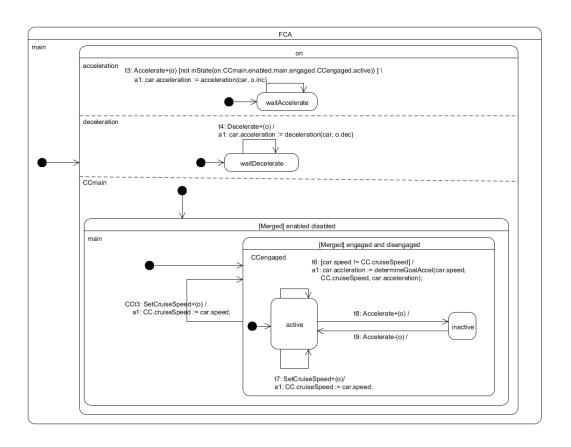


Figure A.13: Sliced FCA feature w.r.t. ACC

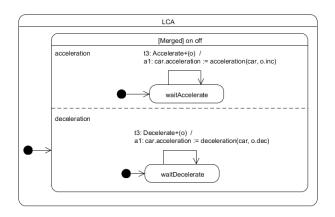


Figure A.14: Sliced LCA feature w.r.t. ACC

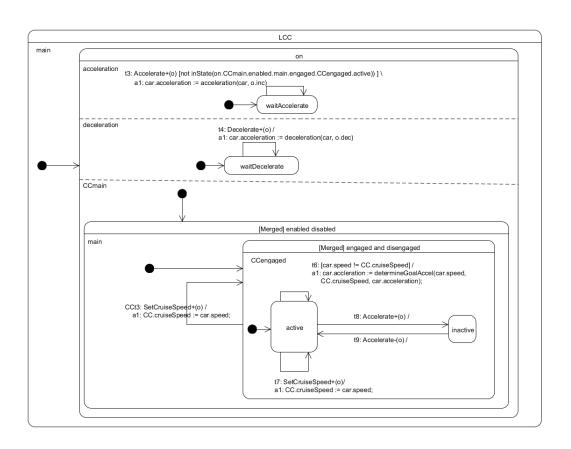


Figure A.15: Sliced LCC feature w.r.t. ACC

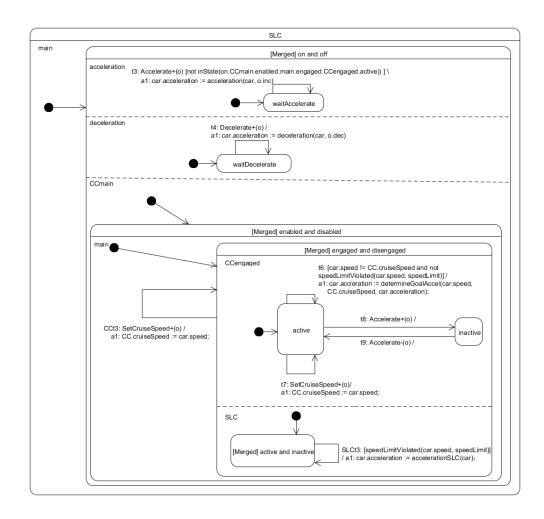
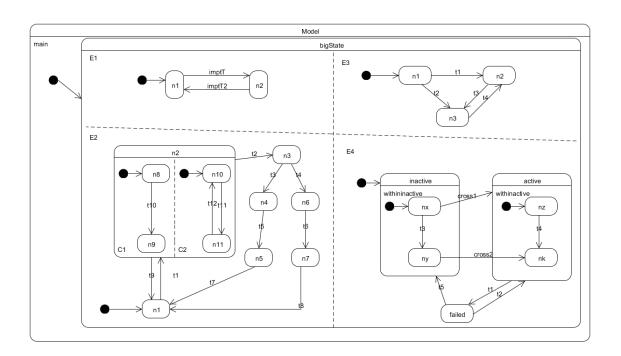


Figure A.16: Sliced SLC feature w.r.t. ACC

Appendix B

Stress Test



 $\textbf{Figure B.1:} \ \, \textbf{The Original Model} \\$

The original model, as shown in Figure B.1, consists of four FOSMs—E1 (Figure B.2), E2 (Figure B.3), E3 (Figure B.4) and E4 (Figure B.5).

Figure B.6 shows the sliced model with respect to E1.

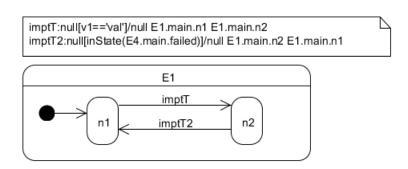


Figure B.2: Original E1

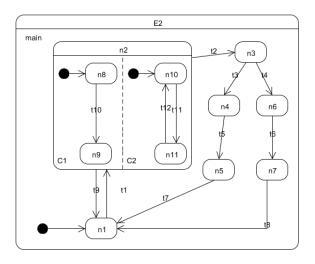


Figure B.3: Original E2

The sliced model consists of three FOSMs in the ROS, as shown in Figure B.7, Figure B.8 and Figure B.9.

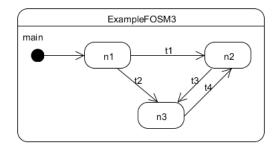


Figure B.4: Original E3

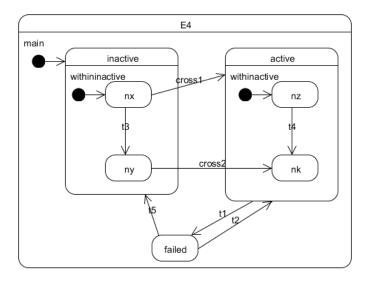


Figure B.5: Original E4

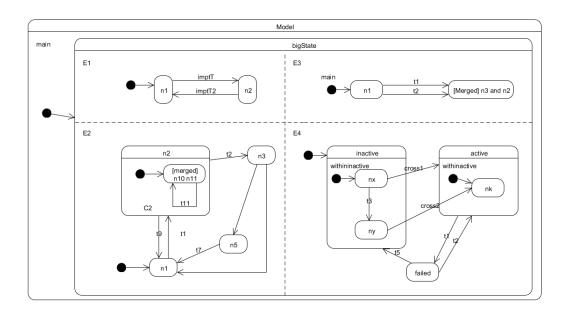


Figure B.6: The Sliced Model w.r.t E1

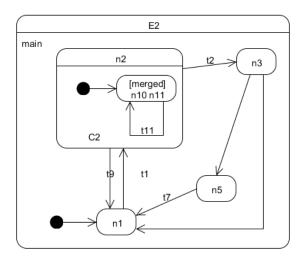


Figure B.7: Sliced E2 w.r.t. E1

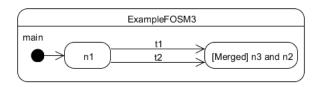


Figure B.8: Sliced E3 w.r.t. E1

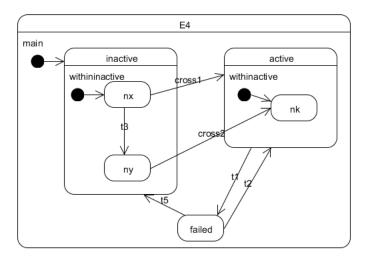


Figure B.9: Sliced E4 w.r.t. E1

Appendix C

Supporting Functions for Control Dependency Algorithm

This chapter lists all the supporting functions for Algorithm 4.2. Their respective function goals have been listed in Table 4.2.

```
Algorithm C.1: Supporting Function for CD Algorithm: HasReductionOccursBefore
```

```
Function HasReductionOccursBefore\ (targetIndex):

if p[targetIndex] == "!" then return true
else return false
end
```

Algorithm C.2: Supporting Function for CD Algorithm: IsReachableFromPartial-Paths

```
Function IsReachableFromPartialPaths (targetIndex):

if p[targetIndex] == null OR p[targetIndex] == "!" then return false;

set originalPath := p[targetIndex];

set paths := ReducePaths (originalPath);

set resultString := paths.join(";");

if originalPath != null AND resultString == null then

set p[targetIndex] := "!";

return false

end

set p[targetIndex] := resultString

return true

end
```

Algorithm C.3: Supporting Function for CD Algorithm: ReducePaths

```
Function ReducePaths (originalPath):
     set paths := array.split(originalPath, ";");
     if paths.length \leq 1 then return paths;
     SortPaths (paths);
     \mathbf{set}\ \mathit{start} := \mathit{paths.lastIndex};
     set i := start - 1;
     set targetIndices := \emptyset;
     ADD the target index of the last subpath of paths[start] into targetIndices
           if paths[i] and paths[start] are the same except the last target index then
            ADD the last target index of paths[i] to targetIndices Decrement i;
           else
                 if targetIndices.size > 1 then
                       set srcIndex := source \ index \ of \ last \ subpath \ of \ paths[start];
                       set n := allNodes[srcIndex];
                       \mathbf{if} \ \mathit{n.outgoingNodes.size} == \mathit{targetIndices.size} \ \mathbf{then}
                             // reduction occurs
                             for j from i+1 to start do
                              | set paths[j] := null;
                             \mathbf{end}
                             Delete the last subpath in paths[i+1]
                       end
                 end
                 if i == -1 then break;
                 \mathbf{reset}\ \mathit{targetIndices} := \emptyset;
                 \mathbf{reset}\ \mathit{start} := \mathit{index}\ \mathit{of}\ \mathit{the}\ \mathit{last}\ \mathit{unprocessed}\ \mathit{path}\ \mathit{in}\ \mathit{paths}
                 ADD the target index of the last subpath of paths[start] to targetIndices;
                 reset i := start-1;
           end
     end
     return paths
end
```

Algorithm C.4: Supporting Function for CD Algorithm: UnionPathHappens

```
Function UnionPathHappens (targetNodeIndex, prevNodeIndex):
      \mathbf{set} \ oldTargetNodeIndex := \mathsf{p}[targetNodeIndex];
      \mathbf{if}\ \mathit{hasReductionOccursBefore}\ (\mathit{prevNodeIndex}) == \mathit{true}\ \mathbf{then}
            set p[targetNodeIndex] := "!";
           {\bf return}\ true
      end
      \mathbf{if}\ \mathsf{p}[\mathit{prevNodeIndex}] \mathrel{!=} \mathit{null}\ \mathbf{then}
            if p[targetNodeIndex] != null then
                  set prevNodeIndexSet := array.split(p[prevNodeIndex], ";");
                  set targetNodeIndexSet := array.split(p[targetNodeIndex], ";");
                  {\bf foreach}\ prevP\ in\ prevNodeIndexSet\ {\bf do}
                        set duplicate := false;
                        {\bf foreach} \ \textit{targetP} \ \textit{in} \ \textit{targetNodeIndexSet} \ {\bf do}
                             if prevP starts with targetP then
                                   reset duplicate := true;
                                    break
                             end
                        end
                        if duplicate == false then APPEND prevP to p[targetNodeIndex];;
                 end
            else
                 set ptargetNodeIndex := p[prevNodeIndex];
            end
      else
           \mathbf{set} \ \mathsf{p}[\mathit{targetNodeIndex}] := \mathit{null};
           return true
      \mathbf{end}
      if p[targetNodeIndex] == oldTargetNodeIndex then
           return false
      else
           return true
      end
\quad \mathbf{end} \quad
```

Algorithm C.5: Supporting Function for CD Algorithm: ExtendPath

```
Function ExtendPath (srcIndex, newSubPath):

if p[srcIndex] == null then return newSubPath;

if hasReductionOccursBefore (srcIndex) == true then return "!";

set srcIndexArr := array.split(p[srcIndex], ";")

foreach i from 1 to srcIndexArr.size do

| APPEND newSubPath to srcIndexArr[i];

end

return srcIndexList.join(";")

end
```

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