# Coulomb's law

$$F_{1,2} = \frac{1}{4\pi\epsilon_0} * \frac{q_1 * q_2}{r^2}$$

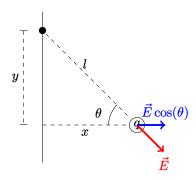
#### Electric field

Electric field is the amount of force caused by a particle on another particle with arbitrary charge.

$$\begin{split} \vec{F} &= \vec{E}*q_2 \\ \frac{\vec{F}}{q_2} &= \vec{E} \\ \frac{F_{q,\text{test charge}}}{q} &= \vec{E} = \frac{1}{4\pi\varepsilon_0}*\frac{q}{r^2} \end{split}$$

To measure electric field, one needs a test charge, which is some arbitrary small charge.

#### Electric field of a charged line



integrate the field force applied by every point on the line, integrate over  $y=+\infty$  to  $y=-\infty$ 

notice that since the integral is symmetric in the y-direction, only force in the x-direction remains.

$$E = \int_{y=+\infty}^{-\infty} E_x$$

$$= \int_{y=+\infty}^{-\infty} E \cos(\theta)$$

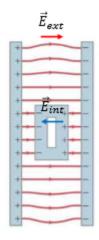
$$= \int_{y=+\infty}^{-\infty} \frac{\lambda}{4\pi\varepsilon_0 * l^2} dy * \cos(\theta)$$

 $\lambda$  is the charge per length of the charged wire.

$$l = \sqrt{x^2 + y^2}$$

TODO finish this shit

## **Induced charges**

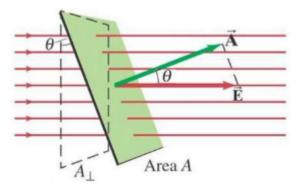


Free charges in a conductor respond to external field such that total field inside the conductor is zero.

$$E_{\text{total}} = E_{\text{external}} + E_{\text{internals}}$$

Faraday cage operates on this principle.

electric flux  $\phi$  is the amount of electric field lines that pass through a surface.



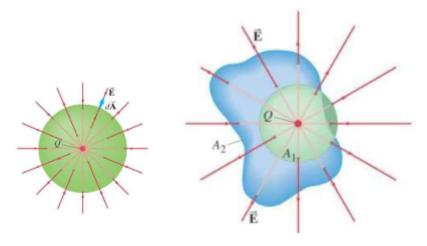
surface integral 
$$\phi = \iint \vec{E} \cdot d\vec{A}$$
$$= \iint \vec{E} * d\vec{A} * \cos(\theta)$$

 $\vec{A}$  is the normal vector of the surface, and whose magnitude is the area of the surface.

## Gauss's law

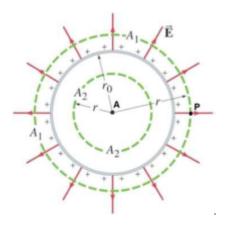
Gauss's law: The electric flux through a closed surface is equal to the net charge enclosed in it divided by  $\varepsilon_0$ 

Notice that electric flux is the number of field lines that go through a surface, therefore the following two gauss surfaces have the same flux.



$$\phi_{\rm surface} = \oiint_{\rm surface} \vec{E} \bullet d\vec{A} = \frac{q_{\rm enclosed}}{\varepsilon_0}$$

# Field of a uniformly charged sphere



since all of the field lines are perpendicular to the gauss surface  $A_1$ , and that  $\vec{E}$  has the same magnitude everywhere, this is analogous to a point charge. Thusly, uniform homogenous charged spheres can be approximated to point charges.

#### Field of a non-conducting charge sphere

spoilers, exact same thing as above.

### Field of a charged plate