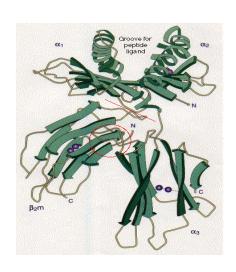
## Active Learning

Maria-Florina Balcan 04/01/2015

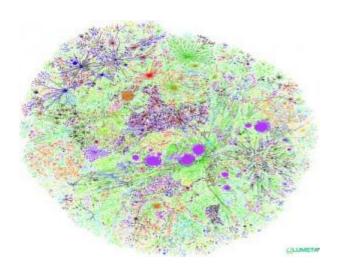
# Classic Fully Supervised Learning Paradigm Insufficient Nowadays

Modern applications: massive amounts of raw data.

Only a tiny fraction can be annotated by human experts.







Billions of webpages



Images

## Modern ML: New Learning Approaches

Modern applications: massive amounts of raw data.

Techniques that best utilize data, minimizing need for expert/human intervention.

Paradigms where there has been great progress.

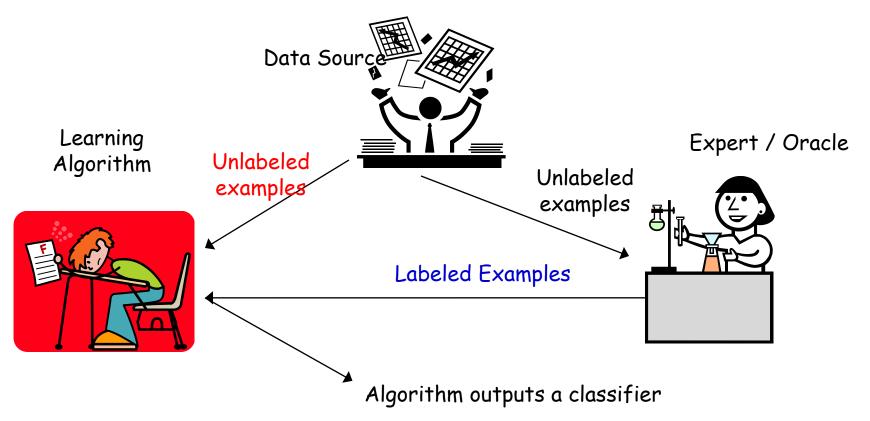
· Semi-supervised Learning, (Inter)active Learning.







## Semi-Supervised Learning



$$S_l = \{(x_1, y_1), ..., (x_{m_l}, y_{m_l})\}$$

 $x_i$  drawn i.i.d from D,  $y_i = c^*(x_i)$ 

 $S_u = \{x_1, ..., x_{m_u}\}$  drawn i.i.d from D

Goal: h has small error over D.

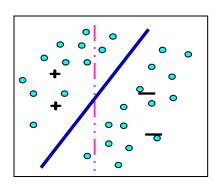
$$\operatorname{err}_{D}(h) = \Pr_{x \sim D}(h(x) \neq c^{*}(x))$$

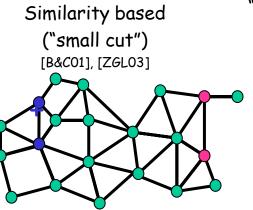
## Semi-supervised Learning

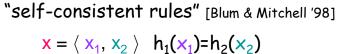
#### Key Insight/Underlying Fundamental Principle

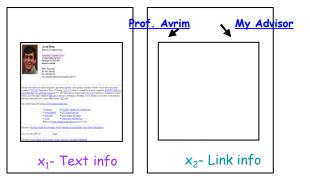
Unlabeled data useful if we have a bias/belief not only about the form of the target, but also about its relationship with the underlying data distribution.











Unlabeled data can help reduce search space or re-order the fns
in the search space according to our belief, biasing the search
towards fns satisfying the belief (which becomes concrete once
we see unlabeled data).

#### A General Discriminative Model for SSL

[BalcanBlum, COLT 2005; JACM 2010]

As in PAC/SLT, discuss algorithmic and sample complexity issues.

Analyze fundamental sample complexity aspects:

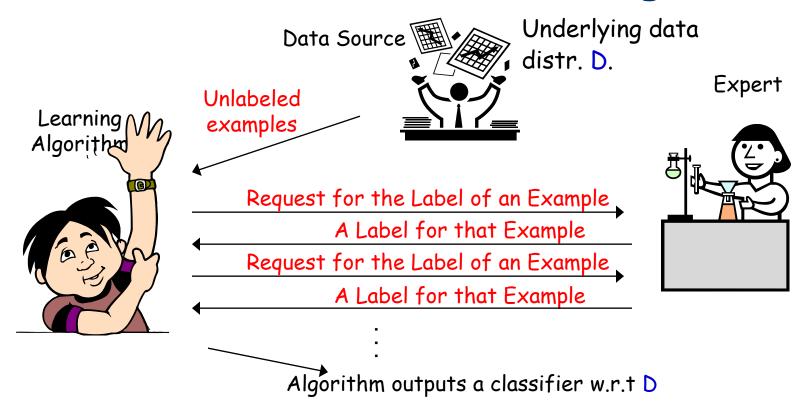
- How much unlabeled data is needed.
  - depends both on complexity of H and of compatibility notion.
- Ability of unlabeled data to reduce #of labeled examples.
  - compatibility of the target, helpfulness of the distrib.
- Survey on "Semi-Supervised Learning" (Jerry Zhu, 2010)
   explains the SSL techniques from this point of view.
- Note: the mixture method that Tom talked about on Feb 25th can be explained from this point of view too. See the Zhu survey.

## Active Learning

#### Additional resources:

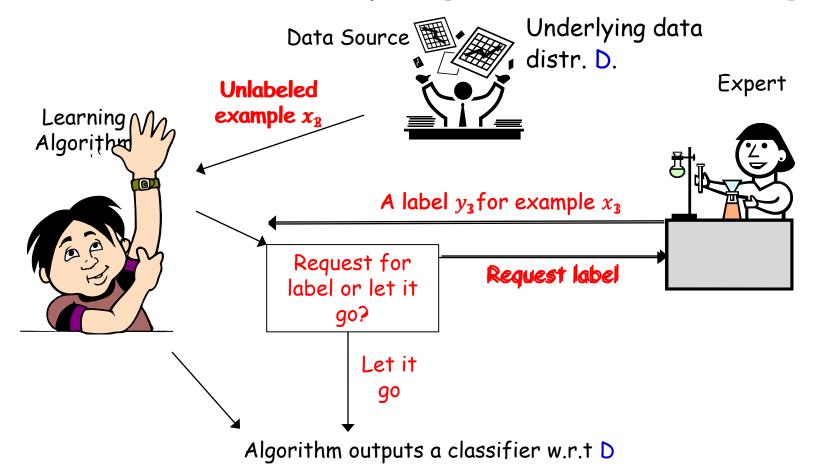
- Two faces of active learning. Sanjoy Dasgupta. 2011.
- Active Learning. Bur Settles. 2012.
- · Active Learning. Balcan-Urner. Encyclopedia of Algorithms. 2015

## Batch Active Learning



- Learner can choose specific examples to be labeled.
- Goal: use fewer labeled examples [pick informative examples to be labeled].

## Selective Sampling Active Learning



- Selective sampling AL (Online AL): stream of unlabeled examples, when each arrives make a decision to ask for label or not.
- · Goal: use fewer labeled examples [pick informative examples to be labeled].

## What Makes a Good Active Learning Algorithm?

- Guaranteed to output a relatively good classifier for most learning problems.
- · Doesn't make too many label requests.

Hopefully a lot less than passive learning and SSL.

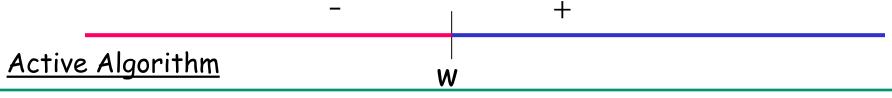
 Need to choose the label requests carefully, to get informative labels.

# Can adaptive querying really do better than passive/random sampling?

- YES! (sometimes)
- We often need far fewer labels for active learning than for passive.
- This is predicted by theory and has been observed in practice.

#### Can adaptive querying help? [CAL92, Dasgupta04]

• Threshold fns on the real line:  $h_w(x) = 1(x \ge w)$ ,  $C = \{h_w : w \in R\}$ 



- Get N unlabeled examples
- How can we recover the correct labels with  $\ll N$  queries?
- Do binary search! Just need O(log N) labels!



- Output a classifier consistent with the N inferred labels.
- $N = O(1/\epsilon)$  we are guaranteed to get a classifier of error  $\leq \epsilon$ .

<u>Passive supervised</u>:  $\Omega(1/\epsilon)$  labels to find an  $\epsilon$ -accurate threshold.

Active: only  $O(\log 1/\epsilon)$  labels. Exponential improvement.

Uncertainty sampling in SVMs common and quite useful in practice. E.g., [Tong & Koller, ICML 2000; Jain, Vijayanarasimhan & Grauman, NIPS 2010; Schohon Cohn, ICML 2000]

#### Active SVM Algorithm

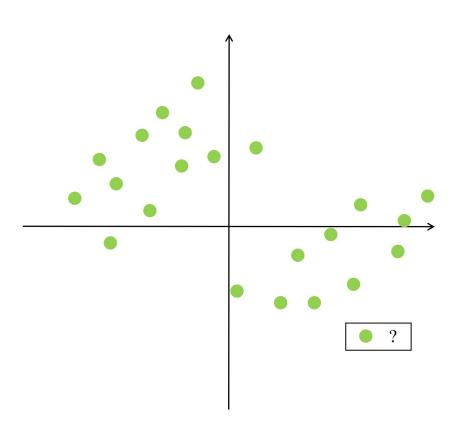
- At any time during the alg., we have a "current guess"  $\mathbf{w}_t$  of the separator: the max-margin separator of all labeled points so far.
- Request the label of the example closest to the current separator.

#### Active SVM seems to be quite useful in practice.

[Tong & Koller, ICML 2000; Jain, Vijayanarasimhan & Grauman, NIPS 2010]

#### Algorithm (batch version)

Input  $S_u = \{x_1, ..., x_{m_u}\}$  drawn i.i.d from the underlying source D



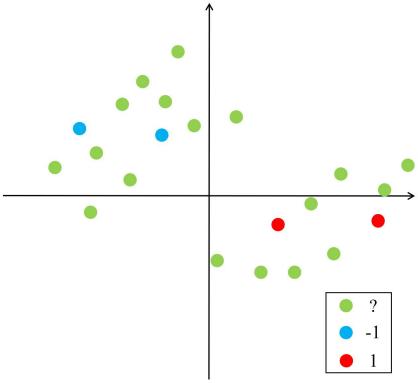
#### Active SVM seems to be quite useful in practice.

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#### Algorithm (batch version)

Input  $S_u = \{x_1, ..., x_{m_u}\}$  drawn i.i.d from the underlying source D

Start: query for the labels of a few random  $x_i$ s.



#### Active SVM seems to be quite useful in practice.

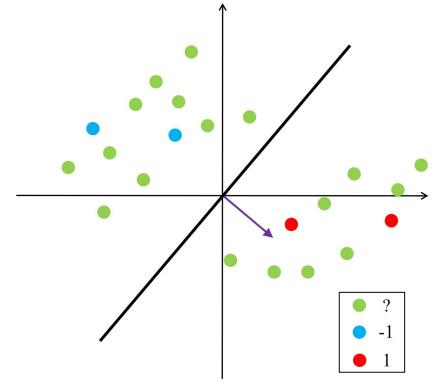
[Tong & Koller, ICML 2000; Jain, Vijayanarasimhan & Grauman, NIPS 2010]

#### Algorithm (batch version)

Input  $S_u = \{x_1, ..., x_{m_u}\}$  drawn i.i.d from the underlying source D Start: query for the labels of a few random  $x_i$ s.

For  $t = 1, \ldots,$ 

• Find  $w_t$  the max-margin separator of all labeled points so far.



#### Active SVM seems to be quite useful in practice.

[Tong & Koller, ICML 2000; Jain, Vijayanarasimhan & Grauman, NIPS 2010]

#### Algorithm (batch version)

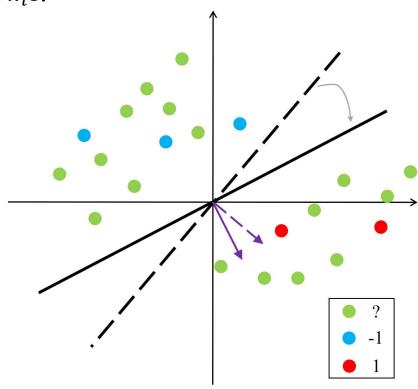
Input  $S_u = \{x_1, ..., x_{m_u}\}$  drawn i.i.d from the underlying source D

Start: query for the labels of a few random  $x_i$ s.

#### For $t = 1, \ldots,$

- Find  $w_t$  the max-margin separator of all labeled points so far.
- Request the label of the example closest to the current separator: minimizing  $|x_i \cdot w_t|$ .

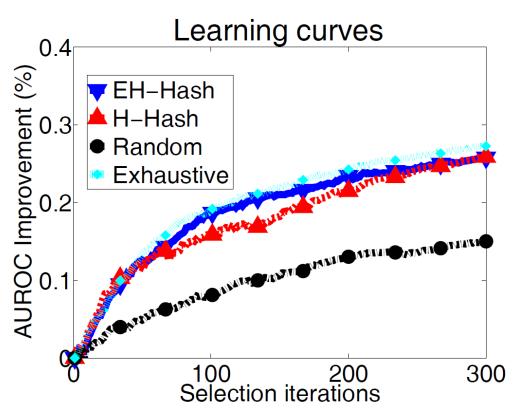
(highest uncertainty)



Active SVM seems to be quite useful in practice.

E.g., Jain, Vijayanarasimhan & Grauman, NIPS 2010

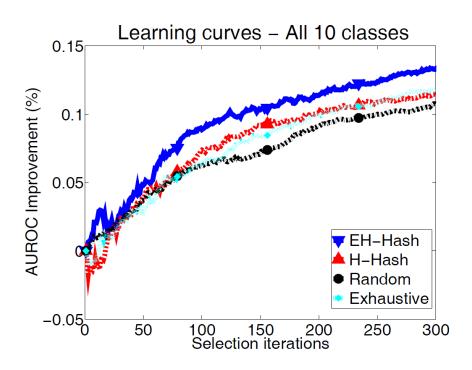
Newsgroups dataset (20.000 documents from 20 categories)



Active SVM seems to be quite useful in practice.

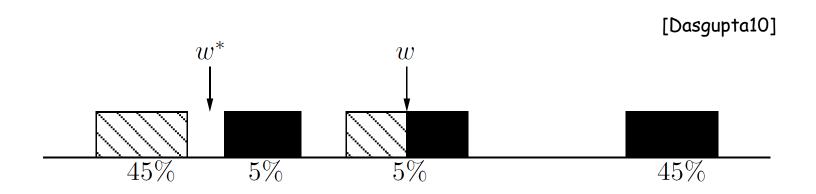
E.g., Jain, Vijayanarasimhan & Grauman, NIPS 2010

CIFAR-10 image dataset (60.000 images from 10 categories)



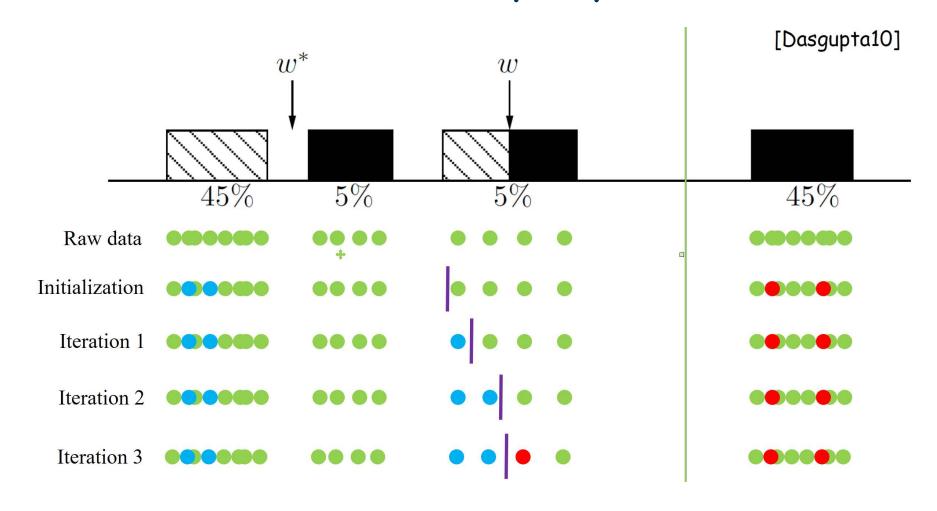
## Active SVM/Uncertainty Sampling

- Works sometimes....
- However, we need to be very very careful!!!
  - Myopic, greedy technique can suffer from sampling bias.
  - A bias created because of the querying strategy; as time goes on the sample is less and less representative of the true data source.



## Active SVM/Uncertainty Sampling

- Works sometimes....
- However, we need to be very very careful!!!

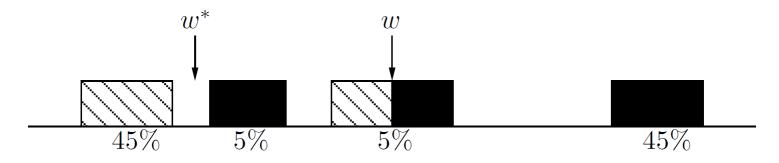


## Active SVM/Uncertainty Sampling

- Works sometimes....
- However, we need to be very very careful!!!
  - Myopic, greedy technique can suffer from sampling bias.
  - Bias created because of the querying strategy; as time goes on the sample is less and less representative of the true source.
  - Observed in practice too!!!!



 Main tension: want to choose informative points, but also want to guarantee that the classifier we output does well on true random examples from the underlying distribution.



## Safe Active Learning Schemes

# Disagreement Based Active Learning Hypothesis Space Search

[CAL92] [BBL06]

[Hanneke'07, DHM'07, Wang'09, Fridman'09, Kolt10, BHW'08, BHLZ'10, H'10, Ailon'12, ...]

## Version Spaces

- X feature/instance space; distr. D over X;  $c^*$  target fnc
- Fix hypothesis space H.

```
Definition (Mitchell'82) Assume realizable case: c^* \in H.
 Given a set of labeled examples (x_1, y_1), ..., (x_{m_l}, y_{m_l}), y_i = c^*(x_i)
 Version space of H: part of H consistent with labels so far.
 I.e., h \in VS(H) iff h(x_i) = c^*(x_i) \ \forall i \in \{1, ..., m_l\}.
```

## Version Spaces

- X feature/instance space; distr. D over X;  $c^*$  target fnc
- Fix hypothesis space H.

**Definition (Mitchell'82)** Assume realizable case:  $c^* \in H$ .

Given a set of labeled examples  $(x_1, y_1)$ , ...,  $(x_{m_1}, y_{m_1})$ ,  $y_i = c^*(x_i)$ 

Version space of H: part of H consistent with labels so far.

E.g.,: data lies on circle in R<sup>2</sup>, H = homogeneous linear seps.

+ region of disagreement in data space

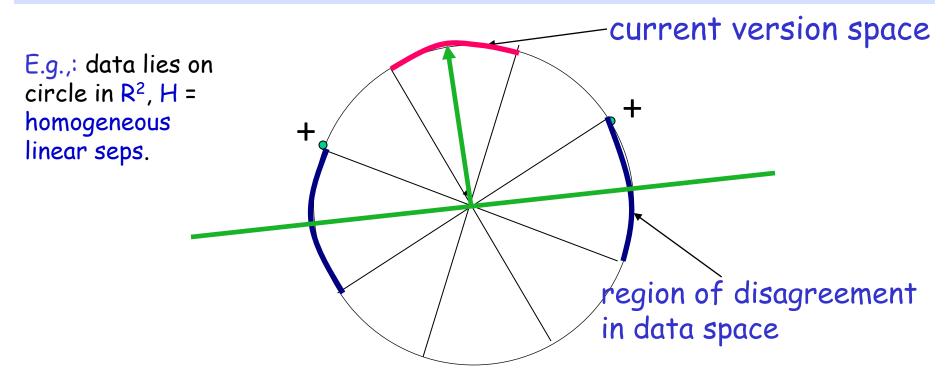
#### Version Spaces. Region of Disagreement

#### Definition (CAL'92)

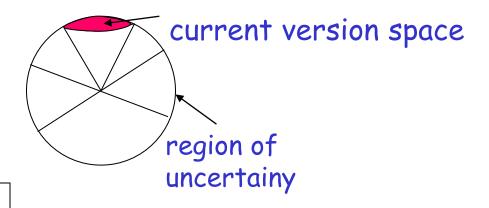
Version space: part of H consistent with labels so far.

Region of disagreement = part of data space about which there is still some uncertainty (i.e. disagreement within version space)

 $x \in X, x \in DIS(VS(H))$  iff  $\exists h_1, h_2 \in VS(H), h_1(x) \neq h_2(x)$ 



#### Disagreement Based Active Learning [CAL92]



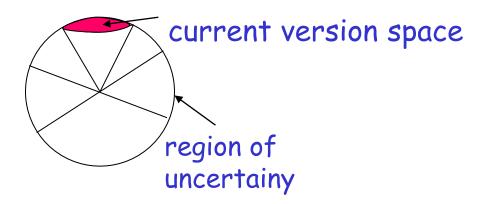
#### Algorithm:

Pick a few points at random from the current region of uncertainty and query their labels.

Stop when region of uncertainty is small.

**Note**: it is active since we do not waste labels by querying in regions of space we are certain about the labels.

#### Disagreement Based Active Learning [CAL92]



#### Algorithm:

Query for the labels of a few random  $x_i$ s.

Let  $H_1$  be the current version space.

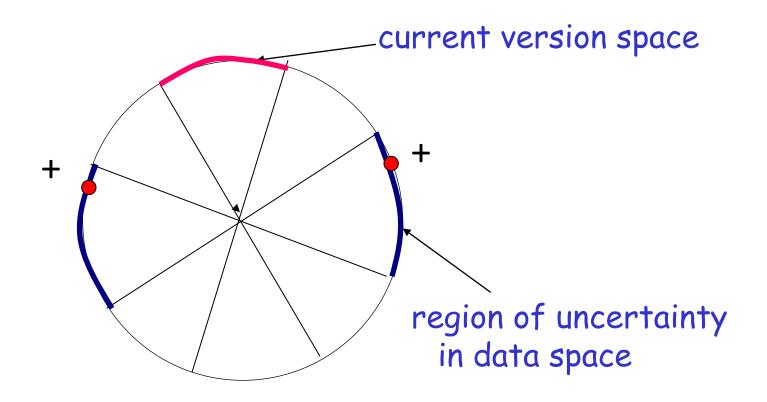
For  $t = 1, \ldots,$ 

Pick a few points at random from the current region of disagreement  $DIS(H_t)$  and query their labels.

Let  $H_{t+1}$  be the new version space.

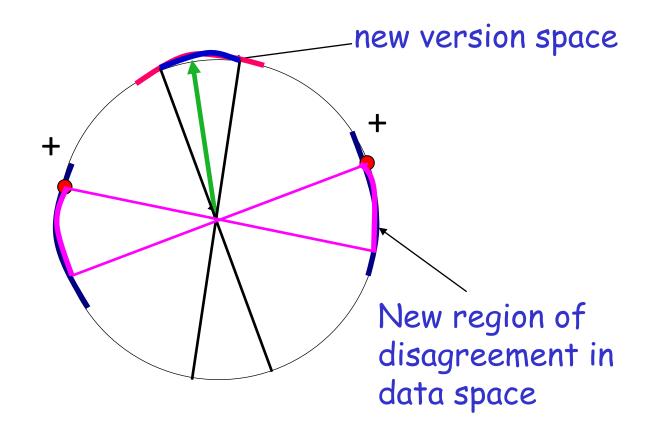
#### Region of uncertainty [CAL92]

- Current version space: part of C consistent with labels so far.
- "Region of uncertainty" = part of data space about which there is still some uncertainty (i.e. disagreement within version space)



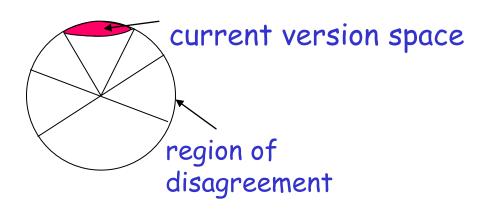
#### Region of uncertainty [CAL92]

- Current version space: part of C consistent with labels so far.
- "Region of uncertainty" = part of data space about which there is still some uncertainty (i.e. disagreement within version space)



How about the agnostic case where the target might not belong the H?

## A<sup>2</sup> Agnostic Active Learner [BBL'06]



#### Algorithm:

Let  $H_1 = H$ .

Careful use of generalization bounds; Avoid the sampling bias!!!!

For  $t = 1, \ldots,$ 

- Pick a few points at random from the current region of disagreement  $DIS(H_t)$  and query their labels.
- Throw out hypothesis if you are statistically confident they are suboptimal.

## The DHN Agnostic Active Learner [DHN'07]

```
S=\emptyset (points with inferred labels) T=\emptyset (points with queried labels) For t=1,2,\ldots:
Receive x_t
If (h_{+1}=\operatorname{learn}(S\cup\{(x_t,+1)\},T)) fails: Add (x_t,-1) to S and break If (h_{-1}=\operatorname{learn}(S\cup\{(x_t,-1)\},T)) fails: Add (x_t,+1) to S and break If \operatorname{err}(h_{-1},S\cup T)-\operatorname{err}(h_{+1},S\cup T)>\Delta_t: Add (x_t,+1) to S and break If \operatorname{err}(h_{+1},S\cup T)-\operatorname{err}(h_{-1},S\cup T)>\Delta_t: Add (x_t,+1) to S and break Request y_t and add (x_t,y_t) to T
```

Figure 16: The DHM selective sampling algorithm. Here,  $\operatorname{err}(h, A) = (1/|A|) \sum_{(x,y) \in A} 1(h(x) \neq y)$ . A possible setting for  $\Delta_t$  is shown in Equation 1. At any time, the current hypothesis is  $\operatorname{learn}(S, T)$ .

learn(A, B) returns a hypothesis  $h \in \mathcal{H}$  consistent with A, and with minimum error on B. If there is no hypothesis consistent with A, a failure flag is returned.

$$\Delta_t = \beta_t^2 + \beta_t \left( \sqrt{\operatorname{err}(h_{+1}, S \cup T)} + \sqrt{\operatorname{err}(h_{-1}, S \cup T)} \right), \quad \beta_t = C \sqrt{\frac{d \log t + \log(1/\delta)}{t}}$$

#### When Active Learning Helps. Agnostic case

 $A^2$  the first algorithm which is robust to noise.

[Balcan, Beygelzimer, Langford, ICML'06] [Balcan, Beygelzimer, Langford, JCSS'08]

"Region of disagreement" style: Pick a few points at random from the current region of disagreement, query their labels, throw out hypothesis if you are statistically confident they are suboptimal.

#### Guarantees for A<sup>2</sup> [BBL'06,'08]:

- It is safe (never worse than passive learning) & exponential improvements.
  - C thresholds, low noise, exponential improvement,
  - C homogeneous linear separators in R<sup>d</sup>,
  - D uniform, low noise, only  $d^2 \log (1/\epsilon)$  labels.

A lot of subsequent work.

[Hanneke'07, DHM'07, Wang'09, Fridman'09, Kolt10, BHW'08, BHLZ'10, H'10, Ailon'12, ...]

#### General guarantees for A<sup>2</sup> Agnostic Active Learner

"Disagreement based": Pick a few points at random from the current region of uncertainty, query their labels, throw out hypothesis if you are statistically confident they are suboptimal. [BBL'06]
How quickly the region of disagreement

collapses as we get closer and closer to optimal classifier

Guarantees for A<sup>2</sup> [Hanneke'07]:

Disagreement coefficient 
$$\theta_{c^*} = \sup_{r \geq \eta + \epsilon} \frac{\Pr(DIS(B(c^*, r)))}{r}$$

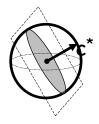
Theorem

$$m = \left(1 + \frac{\eta^2}{\epsilon^2}\right) VCdim(C)\theta_{c^*}^2 \log(\frac{1}{\epsilon})$$

labels are sufficient s.t. with prob.  $\geq 1-\delta$  output h with  $err(h) \leq \eta + \epsilon$ .

Realizable case:  $m = VCdim(C)\theta_{c^*}\log(\frac{1}{\epsilon})$ 

Linear Separators, uniform distr.:  $\theta_{c^*} = \sqrt{d}$ 



#### Disagreement Based Active Learning

"Disagreement based" algos: query points from current region of disagreement, throw out hypotheses when statistically confident they are suboptimal.

- Generic (any class), adversarial label noise.
- Computationally efficient for classes of small VC-dimension

Still, could be suboptimal in label complex & computationally inefficient in general.

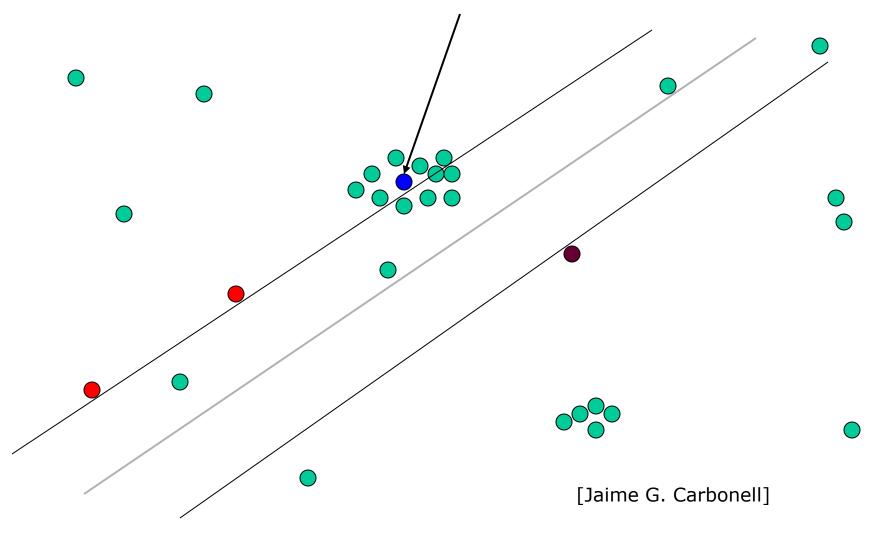
Lots of subsequent work trying to make is more efficient computationally and more aggressive too: [HannekeO7, DasguptaHsuMontleoni'07, Wang'09, Fridman'09, Koltchinskii10, BHW'08, BeygelzimerHsuLangfordZhang'10, Hsu'10, Ailon'12, ...]

# Other Interesting ALTechniques used in Practice

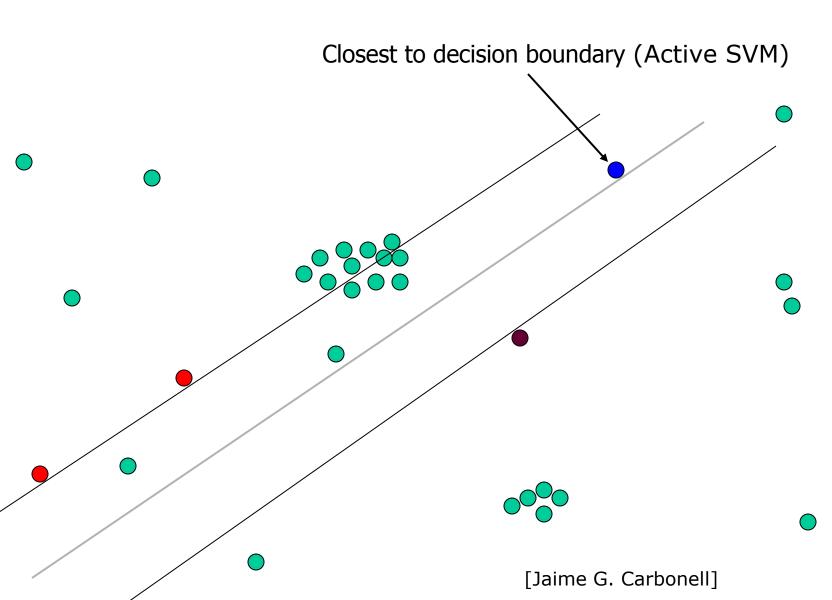
Interesting open question to analyze under what conditions they are successful.

# Density-Based Sampling

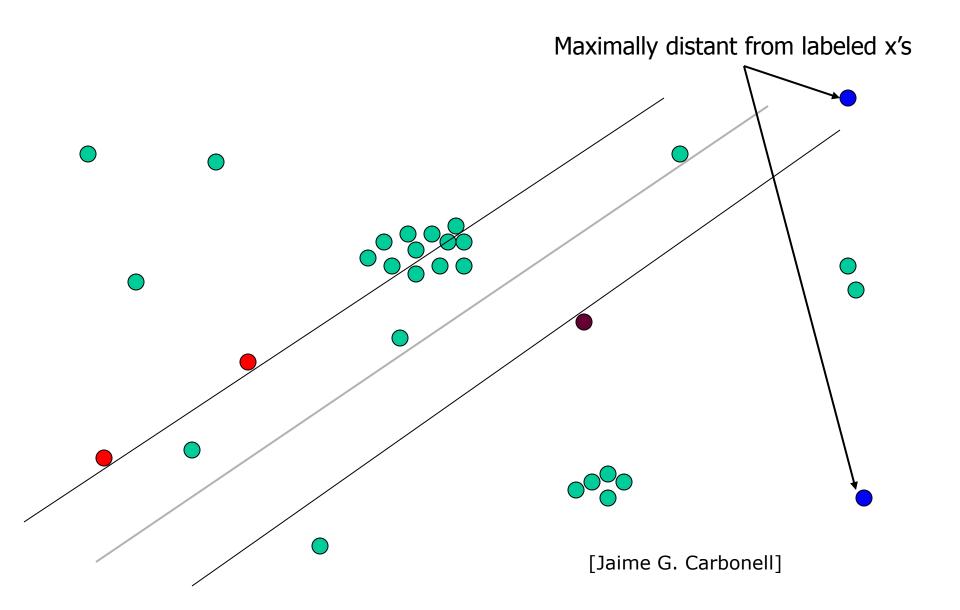




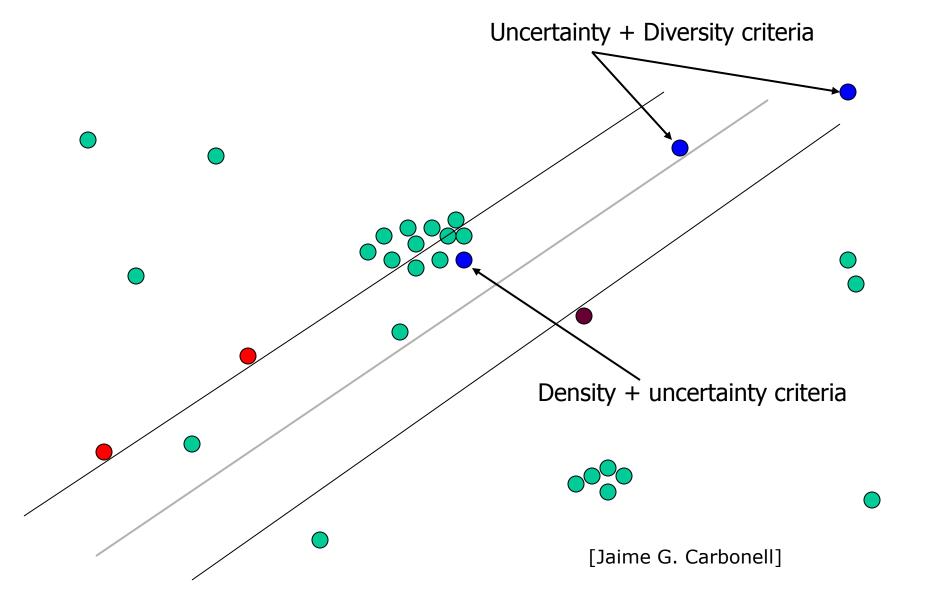
# Uncertainty Sampling



# Maximal Diversity Sampling



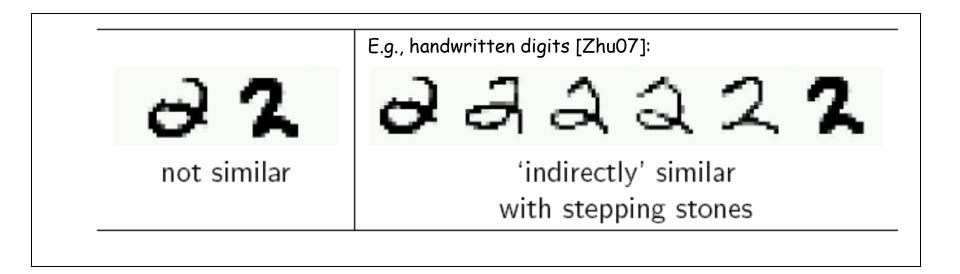
#### Ensemble-Based Possibilities



# Graph-based Active and Semi-Supervised Methods

## Graph-based Methods

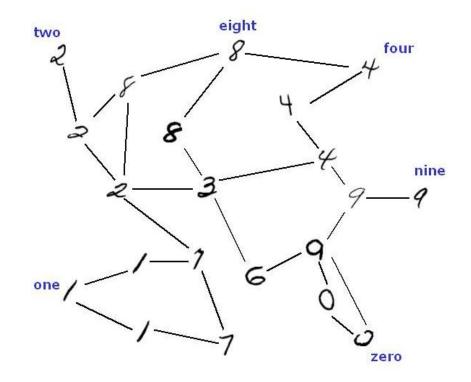
- Assume we are given a pairwise similarity fnc and that very similar examples probably have the same label.
- If we have a lot of labeled data, this suggests a Nearest-Neighbor type of algorithm.
- If you have a lot of unlabeled data, perhaps can use them as "stepping stones".



## Graph-based Methods

Idea: construct a graph with edges between very similar examples.

Unlabeled data can help "glue" the objects of the same class together.



# Graph-based Methods

Often, transductive approach. (Given L + U, output predictions on U). Are alllowed to output any labeling of  $L \cup U$ .

#### Main Idea:

 Construct graph G with edges between very similar examples.

 Might have also glued together in G examples of different classes.

 Run a graph partitioning algorithm to separate the graph into pieces.

# eight four prine prine prince prince

#### Several methods:

- Minimum/Multiway cut [Blum&Chawla01]
- Minimum "Soft-cut" [ZhuGhahramaniLafferty'03]
- Spectral partitioning

- ...

# SSL using soft cuts

[ZhuGhahramaniLafferty'03]

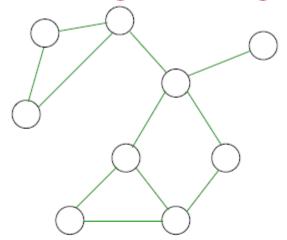
Solve for label function  $f(x) \in [0,1]$  to minimize:

$$J(f) = \sum_{edges(i,j)} w_{ij} (f(x_i) - f(x_j))^2 + \sum_{x_i \in L} \lambda (f(x_i) - y_i)^2$$

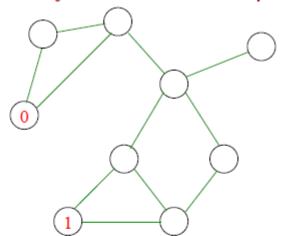
Similar nodes get similar labels (weighted similarity) Agreement with labels (agreement not strictly enforces)

#### Active learning with label propagation

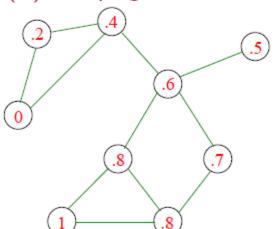
(1) Build neighborhood graph



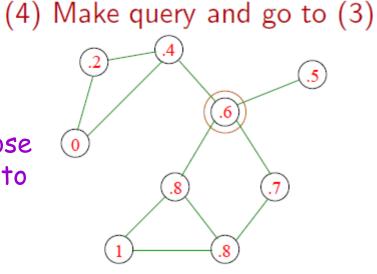
(2) Query some random points



(3) Propagate labels (using soft-cuts)



How to choose which node to query?



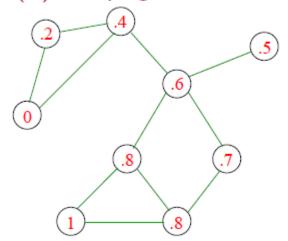
#### Active learning with label propagation

One natural idea: query the most uncertain point.

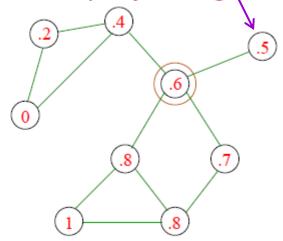
But this has only one edge. Query won't have much impact!

(even worse: a completely isolated node)

(3) Propagate labels (using soft-cuts)



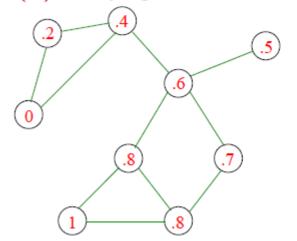
(4) Make query and go to (3)



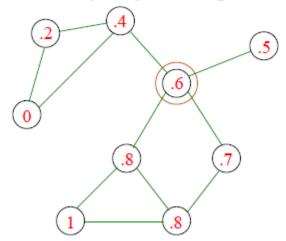
#### Active learning with label propagation

Instead, use a 1-step-lookahead heuristic:

- For a node with label p, assume that querying will have prob p of returning answer 1, 1-p of returning answer 0.
- Compute "average confidence" after running soft-cut in each case:  $p\frac{1}{n}\sum_{x_i}\max(f_1(x_i),1-f_1(x_i))+(1-p)\frac{1}{n}\sum_{x_i}\max(f_0(x_i),1-f_0(x_i))$
- Query node s.t. this quantity is highest (you want to be more confident on average).
  - (3) Propagate labels (using soft-cuts)



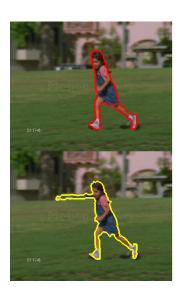
(4) Make query and go to (3)



# Active Learning with Label Propagation in Practice

Does well for Video Segmentation (Fathi-Balcan-Ren-Regh, BMVC 11).





#### What You Should Know

- Active learning could be really helpful, could provide exponential improvements in label complexity (both theoretically and practically)!
- Common heuristics (e.g., those based on uncertainty sampling). Need to be very careful due to sampling bias.
- Safe Disagreement Based Active Learning Schemes.
  - Understand how they operate precisely in noise free scenarios.