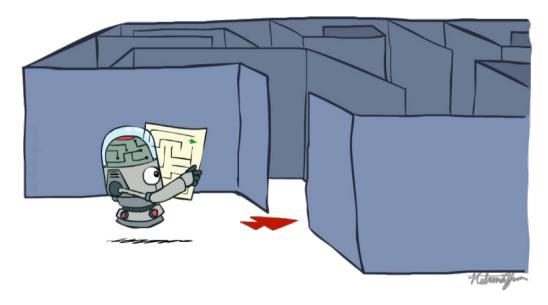
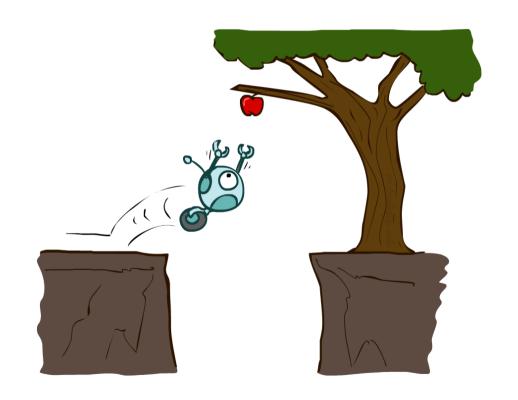
Search



AIMA Chapter 3

Reflex Agents

- Reflex agents:
 - Choose action based on current percept (and maybe memory)
 - Require a mapping from percepts to actions
 - Do not consider the future consequences of their actions
 - Consider how the world IS



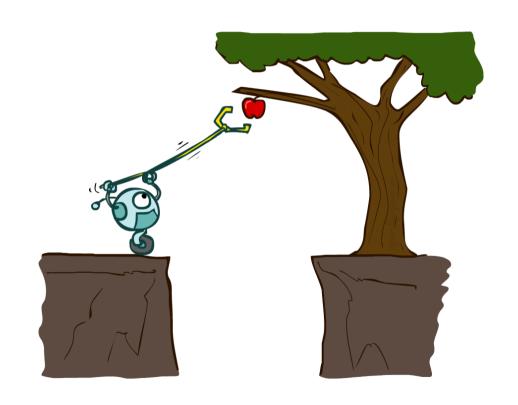
Reflex Agents



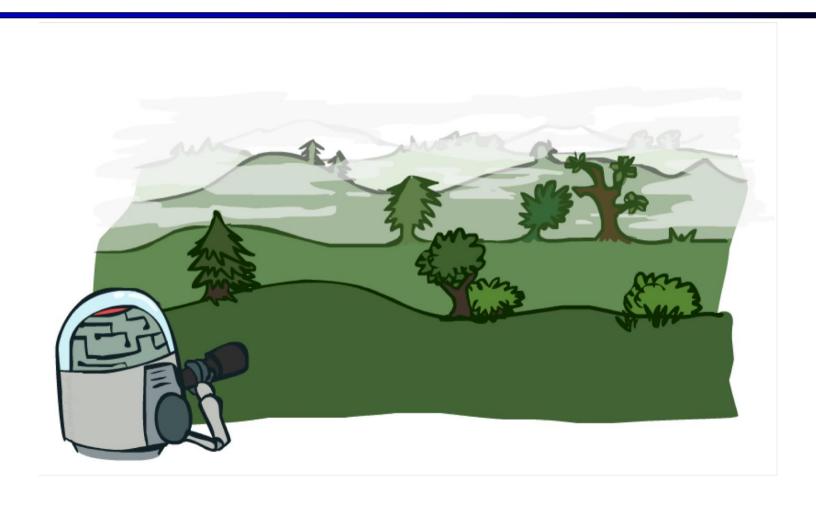
Roomba from iRobot

Planning Agents

- Planning agents:
 - Ask "what if"
 - Decisions based on (hypothesized) consequences of actions
 - Must have a model of how the world evolves in response to actions
 - Must formulate a goal
 - Consider how the world WOULD BE



Search Problems



Search Problems

- A search problem consists of:
 - A state space



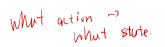




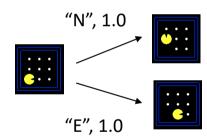








 A successor function (with actions, costs)



A start state and a goal test



 A solution is a sequence of actions (a plan) which transforms the start state to a goal state

What's in a State Space?

The world state includes every last detail of the environment



A search state keeps only the details needed for planning (abstraction)

- Problem: Pathing
 - States: (x,y) location
 - Actions: NSEW
 - Successor: update location only
 - Goal test: is (x,y)=END

- Problem: Eat-All-Dots
 - States: {(x,y), dot booleans}
 - Actions: NSEW
 - Successor: update location and possibly a dot boolean
 - Goal test: dots all false

State Space Sizes?

World state:

Agent positions: 120

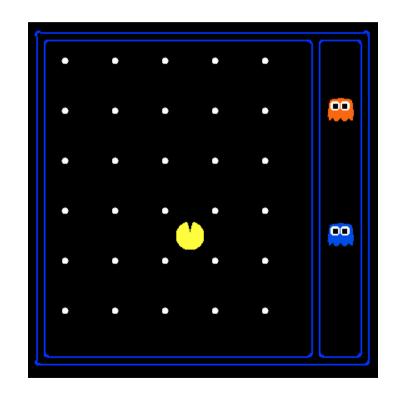
■ Food count: 30

Ghost positions: 12

Agent facing: NSEW

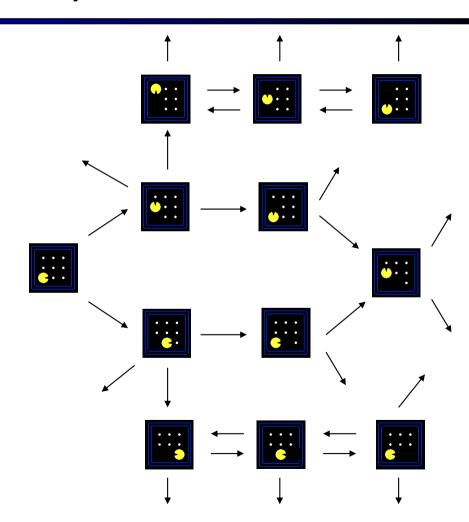
How many

- World states?
 120x(2³⁰)x(12²)x4
- States for pathing?120
- States for eat-all-dots?
 120x(2³⁰)

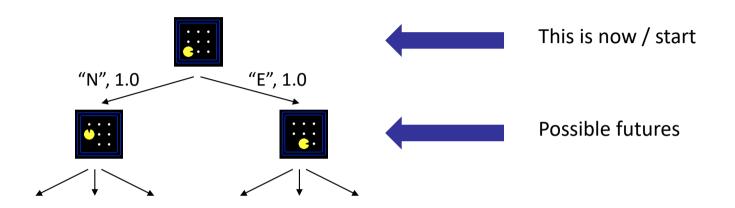


State Space Graphs

- State space graph: A mathematical representation of a search problem
 - Nodes are (abstracted) world configurations
 - Arcs represent successors (action results)
 - The goal test is a set of goal nodes (maybe only one)
- In a state space graph, each state occurs only once!
- We can rarely build this full graph in memory (it's too big), but it's a useful idea



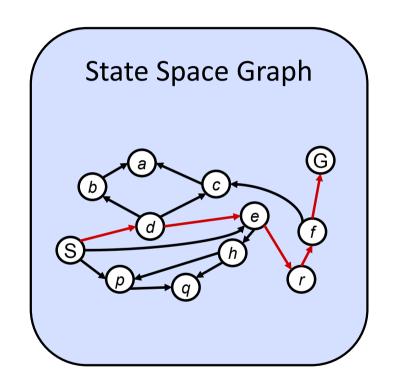
Search Trees

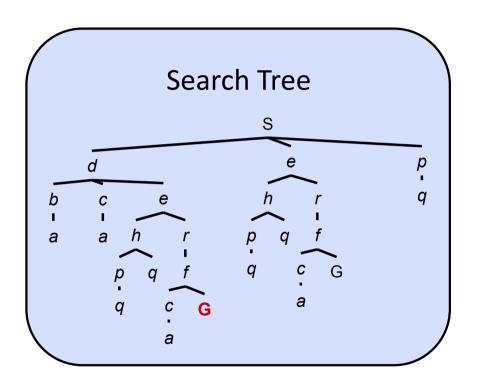


A search tree:

- A "what if" tree of plans and their outcomes
- The start state is the root node
- Children correspond to successors
- For most problems, we can never actually build the whole tree

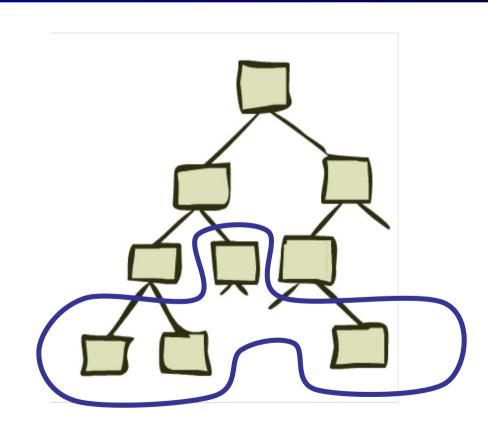
State Space Graphs vs. Search Trees





Each NODE in in the search tree is an entire PATH in the state space graph, corresponding to a PLAN that achieves the state.

Tree Search



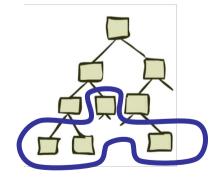
General Tree Search

```
function TREE-SEARCH( problem, strategy) returns a solution, or failure initialize the search tree using the initial state of problem loop do

if there are no candidates for expansion then return failure choose a leaf node for expansion according to strategy

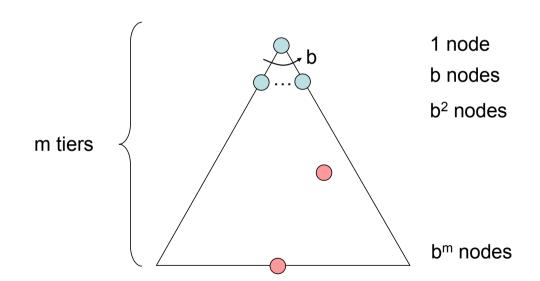
if the node contains a goal state then return the corresponding solution else expand the node and add the resulting nodes to the search tree end
```

- Important concepts:
 - Fringe (frontier) 无子结点
 - Expansion
 - Exploration strategy ← determines the search algorithm

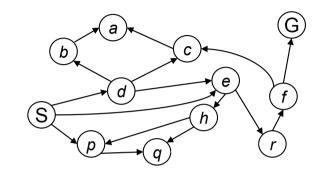


Search Algorithm Properties

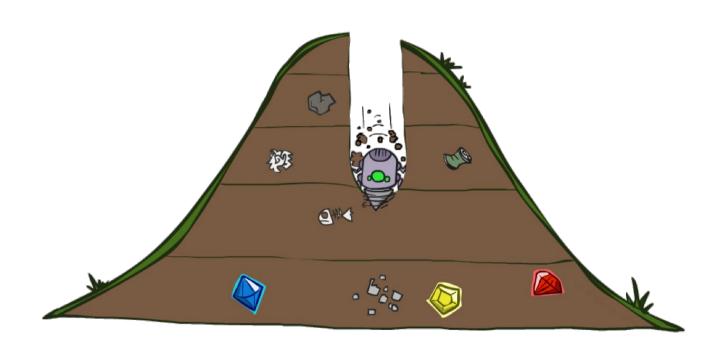
- Complete: Guaranteed to find a solution if one exists?
- Optimal: Guaranteed to find the least cost path?
- Time complexity?
- Space complexity?
- Cartoon of search tree:
 - b is the branching factor
 - m is the maximum depth
 - solutions at various depths
- Number of nodes in entire tree?
 - $1 + b + b^2 + b^m = O(b^m)$



Example: Tree Search



Depth-First Search

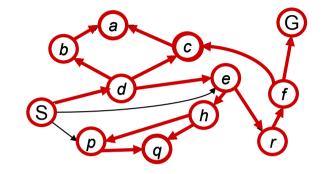


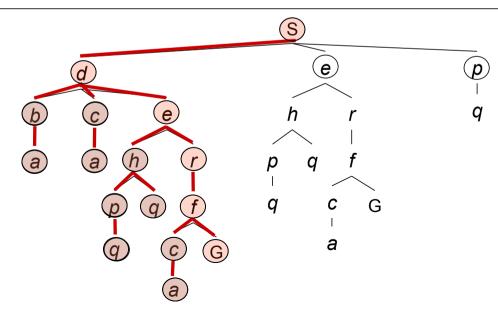
Depth-First Search

Strategy: expand a deepest node first

Implementation:

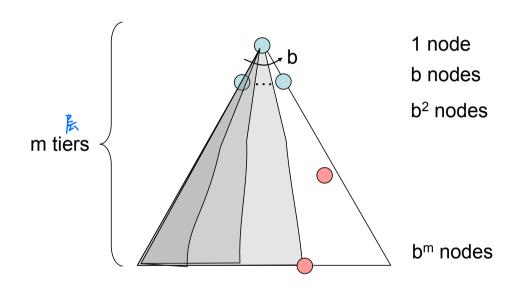
Fringe is a LIFO stack



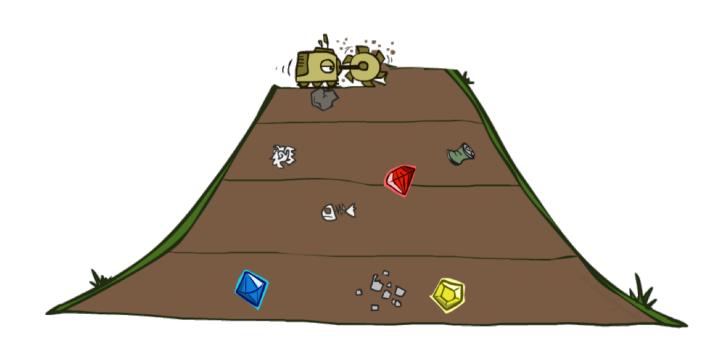


Depth-First Search (DFS) Properties

- What nodes DFS expand?
 - Left to right
 - Could process the whole tree!
 - If m is finite, takes time O(b^m)
- How much space does the fringe take?
 - Only has siblings on path to root, so O(bm)
- Is it complete?
 - m could be infinite, so only if we prevent cycles (more later)
- Is it optimal?
 - No, it finds the "leftmost" solution, regardless of depth or cost



Breadth-First Search

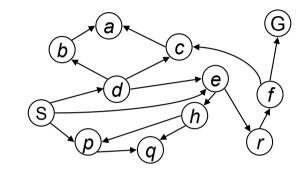


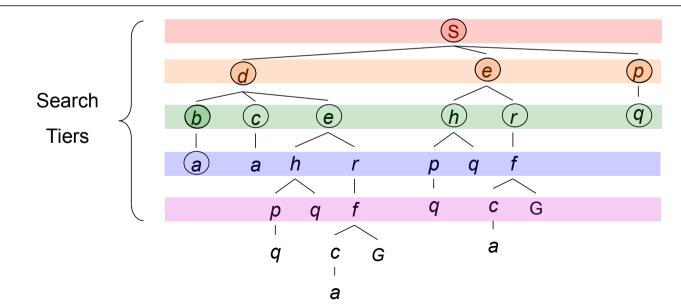
Breadth-First Search

Strategy: expand a shallowest node first

Implementation: Fringe

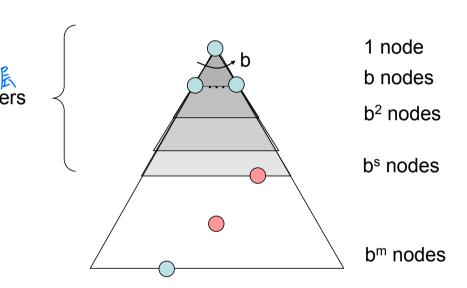
is a FIFO queue





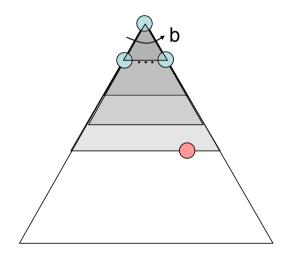
Breadth-First Search (BFS) Properties

- What nodes does BFS expand?
 - Processes all nodes above shallowest solution
 - Let depth of shallowest solution be s
 - Search takes time O(b^s)
- How much space does the fringe take?
 - Has roughly the last tier, so O(b^s)
- Is it complete?
 - s must be finite if a solution exists, so yes!
- Is it optimal?
 - Only if costs are all 1 (more on costs later)

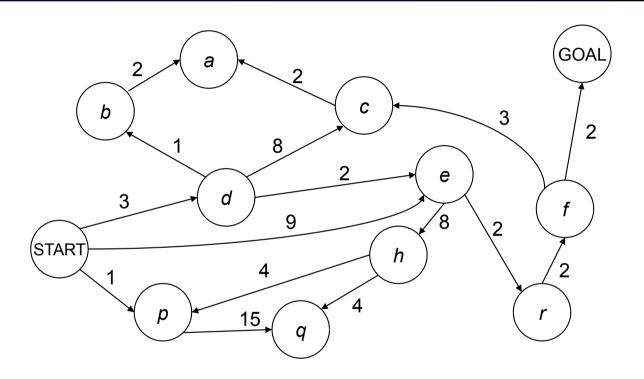


Iterative Deepening

- Idea: get DFS's space advantage with BFS's time / shallow-solution advantages
 - Run a DFS with depth limit 1. If no solution...
 - Run a DFS with depth limit 2. If no solution...
 - Run a DFS with depth limit 3.
- Isn't that wastefully redundant?
 - Generally most work happens in the lowest level searched, so not so bad!



Cost-Sensitive Search



BFS finds the shortest path in terms of number of actions. It does not find the least-cost path. We will now cover a similar algorithm which does find the least-cost path.

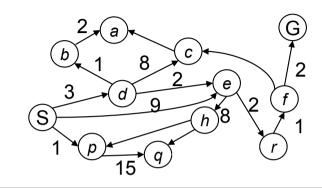
Uniform Cost Search

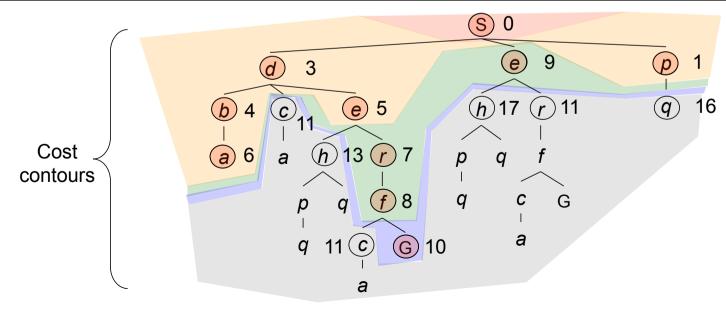


Uniform Cost Search

Strategy: expand a cheapest node first:

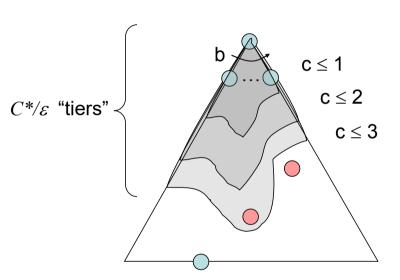
Fringe is a priority queue (priority: cumulative cost)





Uniform Cost Search (UCS) Properties

- What nodes does UCS expand?
 - Processes all nodes with cost less than cheapest solution!
 - If that solution costs C^* and arcs cost at least ε , then the "effective depth" is roughly C^*/ε
 - Takes time $O(b^{C*/\varepsilon})$ (exponential in effective depth)
- How much space does the fringe take?
 - Has roughly the last tier, so $O(b^{C^*/\varepsilon})$
- Is it complete?
 - Assuming best solution has a finite cost and minimum arc cost is positive, yes!
- Is it optimal?
 - Yes!

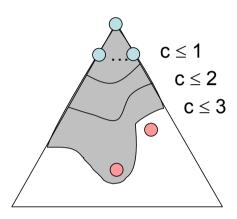


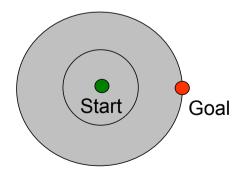
Uniform Cost Issues

The good: UCS is complete and optimal!

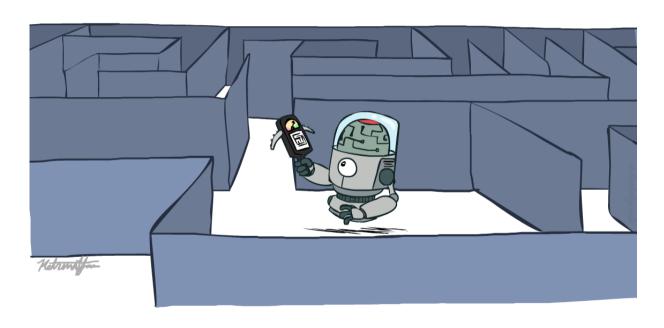
- The bad:
 - Explores options in every "direction"
 - No information about goal location

We'll fix that soon!





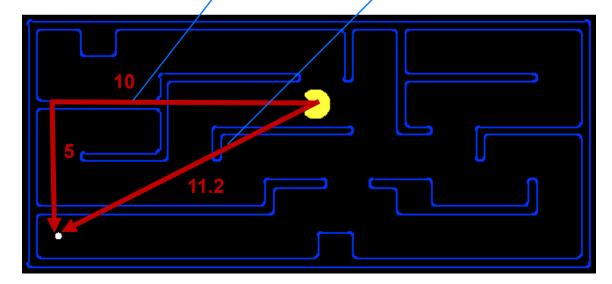
Informed Search

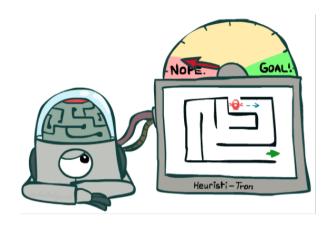


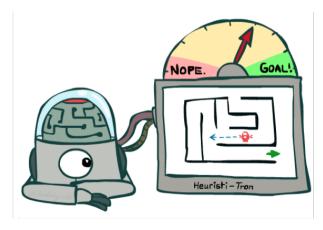
曼哈顿距离:在几何度量中,曼哈顿距离是指两点之间在各个坐标轴上的距离之和,通常用于计算网格状空间中的距离。网格中两点之间的曼哈顿距离是它们坐标的绝对差值之和。

Search Heuristics

- A heuristic h is:
 - A function that estimates how close a state is to a goal
 - h(goal)=0
 - Designed for a particular search problem
 - Examples: Manhattan distance, Euclidean distance for pathing







Greedy Search

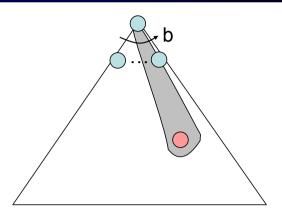


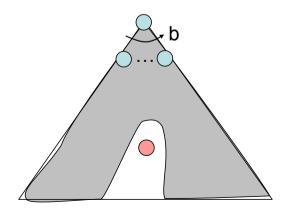
Greedy Search

 Strategy: expand a node that you think is closest to a goal state

- The ideal scenario:
 - Best-first takes you straight to the goal

Worst-case: like a badly-guided DFS

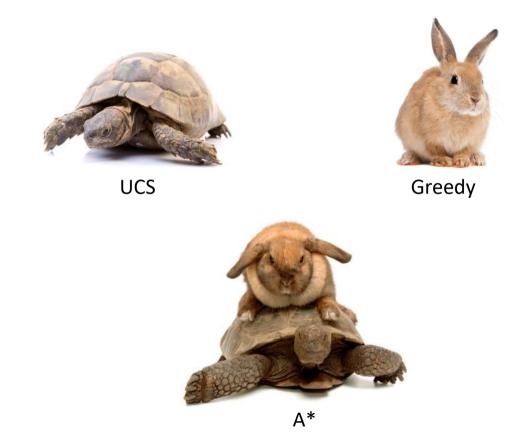




A* Search

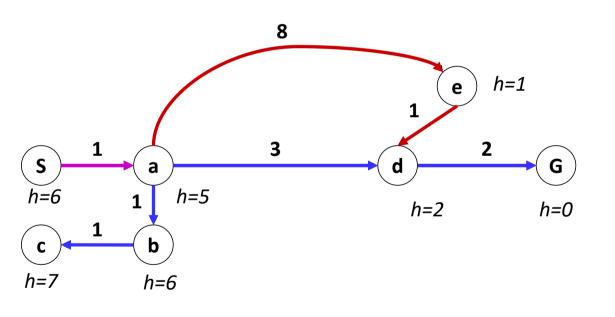


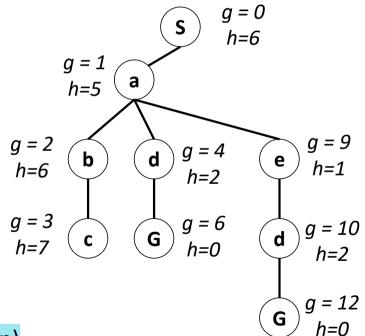
A* Search



Combining UCS and Greedy

- Uniform-cost orders by path cost, or backward cost g(n)
- Greedy orders by goal proximity, or forward cost h(n)

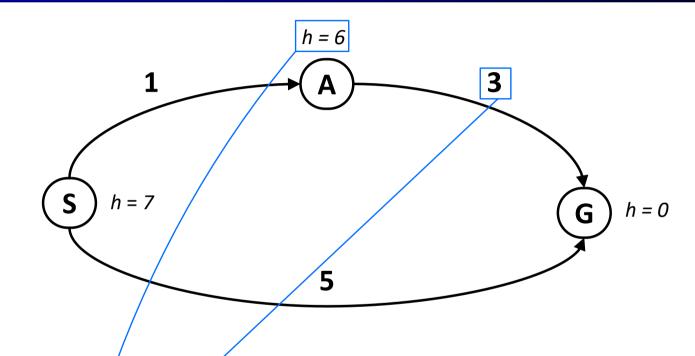




A* Search orders by the sum: f(n) = g(n) + h(n)

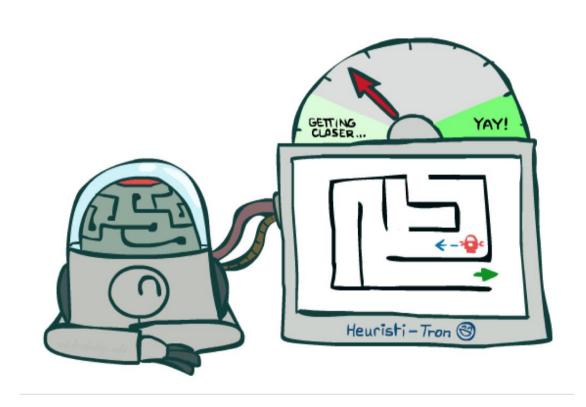
Example: Teg Grenager

Is A* Optimal?



- What went wrong?
- Over-estimated goal cost

Admissible Heuristics



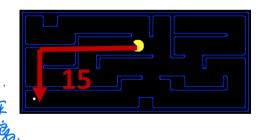
Admissible Heuristics

A heuristic h is admissible (optimistic) if:

$$0 \le h(n) \le h^*(n)$$

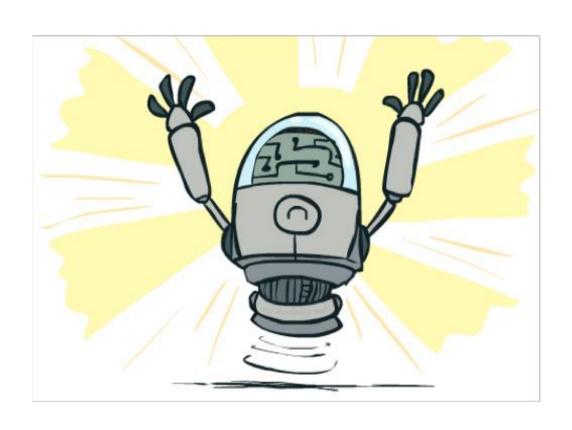
where $h^*(n)$ is the true cost to a nearest goal

• Examples:



 Coming up with admissible heuristics is most of what's involved in using A* in practice.

Optimality of A* Tree Search



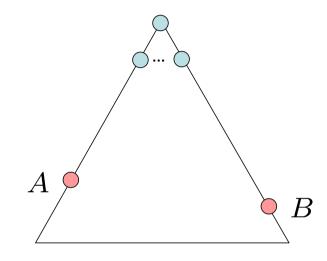
Optimality of A* Tree Search

Assume:

- A is an optimal goal node
- B is a suboptimal goal node
- h is admissible

Claim:

A will exit the fringe before B

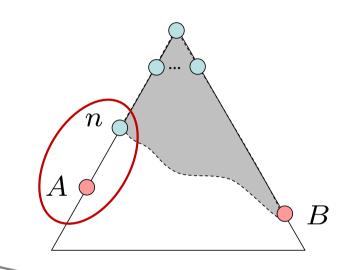


Optimality of A* Tree Search: Blocking

Proof:

- Imagine B is on the fringe
- Some ancestor n of A is on the fringe, too (maybe A!)
- Claim: n will be expanded before B
 - 1. f(n) is less or equal to f(A)

$$h(n)$$
 是被例/估价的 ω st
 $f(n) \in g(n) + h^*(n) = g(A)$



$$f(n) = g(n) + h(n)$$

$$f(n) \le g(A)$$

$$g(A) = f(A)$$

Definition of f-cost

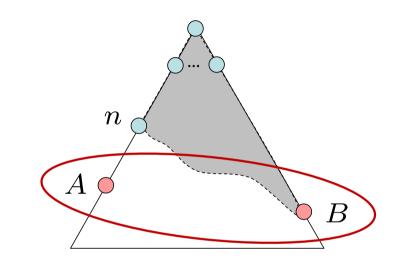
Admissibility of h

h = 0 at a goal

Optimality of A* Tree Search: Blocking

Proof:

- Imagine B is on the fringe
- Some ancestor n of A is on the fringe, too (maybe A!)
- Claim: n will be expanded before B
 - 1. f(n) is less or equal to f(A)
 - 2. f(A) is less than f(B)



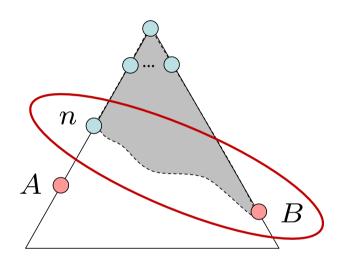
B is suboptimal

$$h = 0$$
 at a goal

Optimality of A* Tree Search: Blocking

Proof:

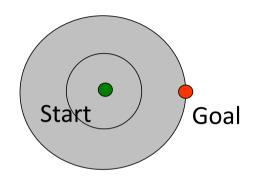
- Imagine B is on the fringe
- Some ancestor n of A is on the fringe, too (maybe A!)
- Claim: n will be expanded before B
 - 1. f(n) is less or equal to f(A)
 - 2. f(A) is less than f(B)
 - 3. *n* expands before B
- All ancestors of A expand before B
- A expands before B
- A* search is optimal



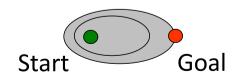
$$f(n) \le f(A) < f(B)$$

UCS vs A* Contours 轮廓

Uniform-cost expands equally in all "directions"



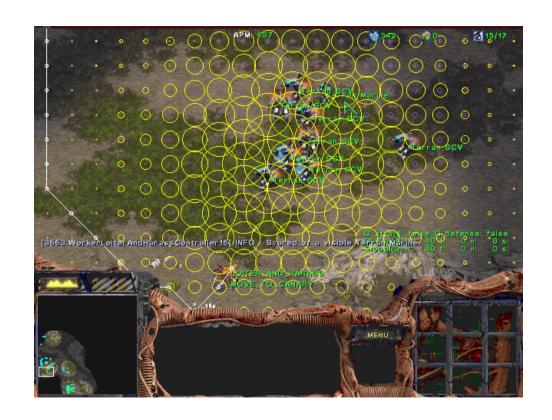
 A* expands mainly toward the goal, but does hedge its bets to ensure optimality



A* Applications

- Video games
- Pathing / routing problems
- Resource planning problems
- Robot motion planning
- Language analysis
- Machine translation
- Speech recognition



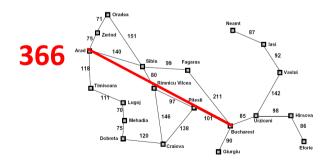


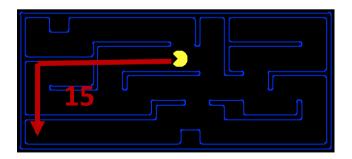
Creating Heuristics



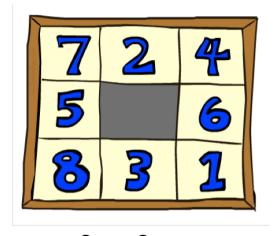
Creating Admissible Heuristics

- Most of the work in solving hard search problems optimally is in coming up with admissible heuristics
 - Inadmissible heuristics are often useful too
- Often, admissible heuristics are solutions to relaxed problems, where new actions are available

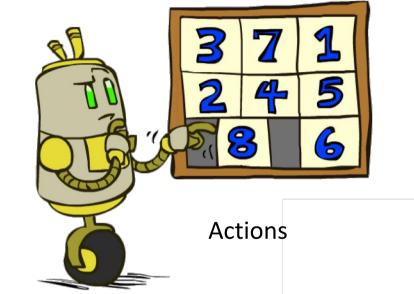




Example: 8 Puzzle



Start State

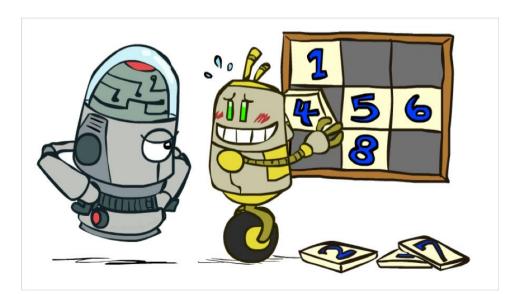


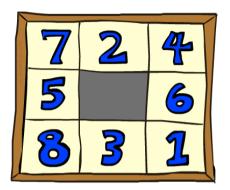
1 2 3 4 5 6 7 8 Goal State

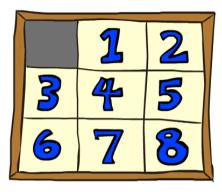
- What are the states?
- How many states?
- What are the actions?
- How many successors from the start state? 4
- What should the costs be?

8 Puzzle I

- Heuristic: Number of tiles misplaced
- h(start) = 8
- Is it admissible? YES
- This is a relaxed-problem heuristic







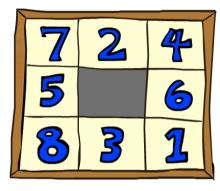
Start State

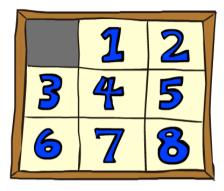
Goal State

	Average nodes expanded when the optimal path has				
	4 steps	8 steps	12 steps		
UCS	112	6,300	3.6×10^6		
TILES	13	39	227		

8 Puzzle II

- Heuristic: total Manhattan distance
- h(start) = 3 + 1 + 2 + ... = 18
- Is it admissible?
- Relaxed-problem: any tile could slide in any direction at any time, ignoring other tiles





Start	State
Juli	Juli

Goal State

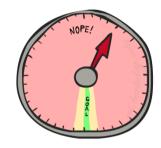
	Average nodes expanded when the optimal path has			
	4 steps	8 steps	12 steps	
TILES	13	39	227	
MANHATTAN	12	25	73	

8 Puzzle III

- How about using the actual cost as a heuristic?
 - Would it be admissible? YES
 - Would we save on nodes expanded?
 - What's wrong with it?







- With A*: a trade-off between quality of estimate and work per node
 - As heuristics get closer to the true cost, you will expand fewer nodes but usually do more work per node to compute the heuristic itself