IN3050/IN4050 Mandatory Assignment 2, 2022: Supervised Learning

Rules

Before you begin the exercise, review the rules at this website: https://www.uio.no/english/studies/examinations/compulsory-activities/mn-ifi-mandatory.html, in particular the paragraph on cooperation. This is an individual assignment. You are not allowed to deliver together or copy/share source-code/answers with others. By submitting this assignment, you confirm that you are familiar with the rules and the consequences of breaking them.

Delivery

Deadline: Friday, March 25, 2022, 23:59

Your submission should be delivered in Devilry. You may redeliver in Devilry before the deadline, but include all files in the last delivery, as only the last delivery will be read. You are recommended to upload preliminary versions hours (or days) before the final deadline.

What to deliver?

You are recommended to solve the exercise in a Jupyter notebook, but you might solve it in a Python program if you prefer.

If you choose Jupyter, you should deliver the notebook. You should answer all questions and explain what you are doing in Markdown. Still, the code should be properly commented. The notebook should contain results of your runs. In addition, you should make a pdf of your solution which shows the results of the runs. (If you can't export: notebook -> latex -> pdf on your own machine, you may do this on the IFI linux machines.)

If you prefer not to use notebooks, you should deliver the code, your run results, and a pdf-report where you answer all the questions and explain your work.

Your report/notebook should contain your name and username.

Deliver one single zipped folder (.zip, .tgz or .tar.gz) which contains your complete solution.

Important: if you weren't able to finish the assignment, use the PDF report/Markdown to elaborate on what you've tried and what problems you encountered. Students who have made an effort and attempted all parts of the assignment will get a second chance even if they fail initially.

This exercise will be graded PASS/FAIL.

Goals of the assignment

The goal of this assignment is to get a better understanding of supervised learning with gradient descent. It will, in particular, consider the similarities and differences between linear classifiers and multi-layer feed forward networks (multi-layer perceptron, MLP) and the differences and similarities between binary and multi-class classification. A main part will be dedicated to implementing and understanding the backpropagation algorithm.

Tools

The aim of the exercises is to give you a look inside the learning algorithms. You may freely use code from the weekly exercises and the published solutions. You should not use ML libraries like scikit-learn or tensorflow.

You may use tools like NumPy and Pandas, which are not specific ML-tools.

The given precode uses NumPy. You are recommended to use NumPy since it results in more compact code, but feel free to use pure python if you prefer.

Beware

There might occur typos or ambiguities. This is a revised assignment compared to earlier years, and there might be new typos. If anything is unclear, do not hesitate to ask. Also, if you think some assumptions are missing, make your own and explain them!

Initialization

```
import numpy as np
import matplotlib.pyplot as plt
import sklearn #for datasets
```

Part 1: Linear classifiers

Datasets

We start by making a synthetic dataset of 2000 datapoints and five classes, with 400 individuals in each class. (See https://scikit-learn.org/stable/modules/generated/sklearn.datasets.make_blobs.html regarding how the data are generated.) We choose to use a synthetic dataset---and not a set of natural occurring data---because we are mostly interested in properties of the various learning algorithms, in particular the differences between linear classifiers and multi-layer neural networks together with the difference between binary and multi-class data.

When we are doing experiments in supervised learning, and the data are not already split into training and test sets, we should start by splitting the data. Sometimes there are natural ways to split the data, say training on data from one year and testing on data from a later year, but if that is not the case, we should shuffle the data randomly before splitting. (OK, that is not necessary with this particular synthetic data set, since it is already shuffled by default by scikit, but that will not be the case with real-world data.) We should split the data so that we keep the alignment between X and t, which may be achieved by shuffling the indices. We split into 50% for training, 25% for validation, and 25% for final testing. The set for final testing *must not be used* till the end of the assignment in part 3.

We fix the seed both for data set generation and for shuffling, so that we work on the same datasets when we rerun the experiments. This is done by the random state argument and the rnq = np.random.RandomState(2022).

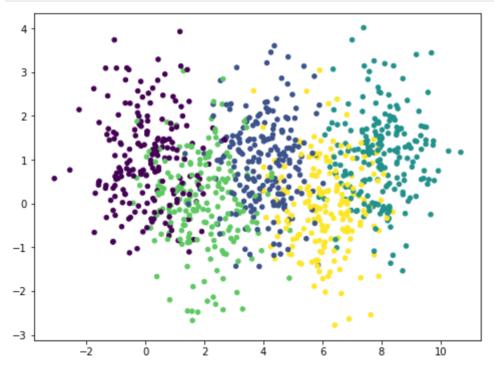
```
In [ ]:
         from sklearn.datasets import make blobs
         X, t = make blobs(n samples=[400,400,400, 400, 400], centers=[[0,1],[4,1],[8,1],[2,0],[6,0]],
                           n features=2, random state=2019, cluster std=1.0)
In [ ]:
         indices = np.arange(X.shape[0])
         rng = np.random.RandomState(2022)
         rng.shuffle(indices)
         indices[:10]
        array([1018, 1295, 643, 1842, 1669,
                                               86, 164, 1653, 1174, 747])
Out[ ]:
In [ ]:
         X train = X[indices[:1000],:]
         X val = X[indices[1000:1500],:]
         X test = X[indices[1500:],:]
         t train = t[indices[:1000]]
         t val = t[indices[1000:1500]]
         t test = t[indices[1500:]]
```

Next, we will make a second dataset by merging the two smaller classes in (X,t) and call the new set (X, t2). This will be a binary set.

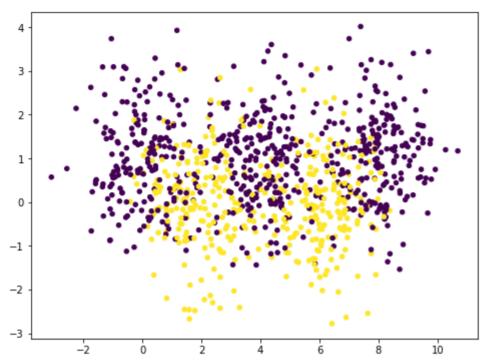
```
In []:
    t2_train = t_train >= 3
    t2_train = t2_train.astype('int')
    t2_val = (t_val >= 3).astype('int')
    t2_test = (t_test >= 3).astype('int')
```

We can plot the two traing sets.

```
plt.figure(figsize=(8,6)) # You may adjust the size
plt.scatter(X_train[:, 0], X_train[:, 1], c=t_train, s=20.0)
plt.show()
```



```
plt.figure(figsize=(8,6))
    plt.scatter(X_train[:, 0], X_train[:, 1], c=t2_train, s=20.0)
    plt.show()
```



Binary classifiers

Linear regression

We see that that set (X, t2) is far from linearly separable, and we will explore how various classifiers are able to handle this. We start with linear regression. You may make your own implementation from scratch or start with the solution to the weekly exercise set 7, which we include here.

```
def mse(t, y):
                 sum errors = 0.
                 for i in range(0,len(t)):
                     sum errors += (t[i] - y[i])**2
                 mean squared error = sum errors/len(t)
                 return mean squared error
In [ ]:
         class NumpyClassifier():
             """Common methods to all numpy classifiers --- if any"""
             epochs used = 0
             def accuracy(self, X test, y test, **kwargs):
                 pred = self.predict(X test, **kwargs)
                 if len(pred.shape) > 1:
                     pred = pred[:,0]
                 return np.sum(pred==y test)/len(pred)
In []:
         class NumpyLinRegClass(NumpyClassifier):
             def fit(self, X train, t train, loss diff, X val = X val, t val = None, eta = 0.01, epochs=1000):
                 """X train is a Nxm matrix, N data points, m features
                 t train are the targets values for training data"""
                 #cheking for optional args
                 optional args = True
                 try:
                     if X val == None and t val == None:
                         optional args = False
                 except:
                     optional args = True
                 if optional args:
                     check acc = X train
                     check acc val= X val
                     X val.shape
                     X val = add bias(X val)
                 (k, m) = X train.shape
                 X train = add bias(X train)
```

```
self.weights = weights = np.zeros(m+1)
training loss = []
validation loss = []
training accuracy = []
validation accuracy = []
#the following for loop could have been coded with less code, but I had another assignment to do.
#basically: train, track loss if we do not have optional args, if we do have optional args then we do the same
for e in range(epochs):
    #making sure we do not try loss diff unless we have something to compare current result to
    if not training loss:
       weights -= eta / k * X train.T @ (X train @ weights - t train)
        error = mse(t train, X train @ weights)
        training loss.append(error)
       if optional args:
            v error = mse(t val, X val @ weights)
            validation loss.append(v error)
            training accuracy.append(self.accuracy(check acc, t train))
            validation accuracy.append(self.accuracy(check acc val, t val))
    #making sure we do not try loss diff unless we have something to compare current result to
    elif len(training loss)==1:
        weights -= eta / k * X train.T @ (X train @ weights - t2 train)
        error = mse(t train, X train @ self.weights)
        training loss.append(error)
       if optional args:
            v error = mse(t val, X val @ weights)
            validation loss.append(v error)
            training accuracy.append(self.accuracy(check acc, t train))
            validation accuracy.append(self.accuracy(check acc val, t val))
    #here we have enough values to start using loss diff
    elif (training loss[len(training loss)-2]-training loss[len(training loss)-1])>loss diff:
        weights -= eta / k * X train.T @ (X train @ weights - t train)
        error = mse(t train, X train @ self.weights)
       training loss.append(error)
        if optional args:
            v error = mse(t val, X val @ weights)
            validation loss.append(v error)
            training accuracy.append(self.accuracy(check acc, t train))
            validation accuracy.append(self.accuracy(check acc val, t val))
    else:
        #print("eta:", eta)
        #print("loss diff:", loss diff)
```

```
return training_loss, validation_loss, training_accuracy, validation_accuracy

#print("eta:", eta)
#print("loss_diff:", loss_diff)
return training_loss, validation_loss, training_accuracy, validation_accuracy

def predict(self, x, threshold=0.5):
    z = add_bias(x)
    score = z @ self.weights
    return score>threshold
```

We can train and test a first classifier.

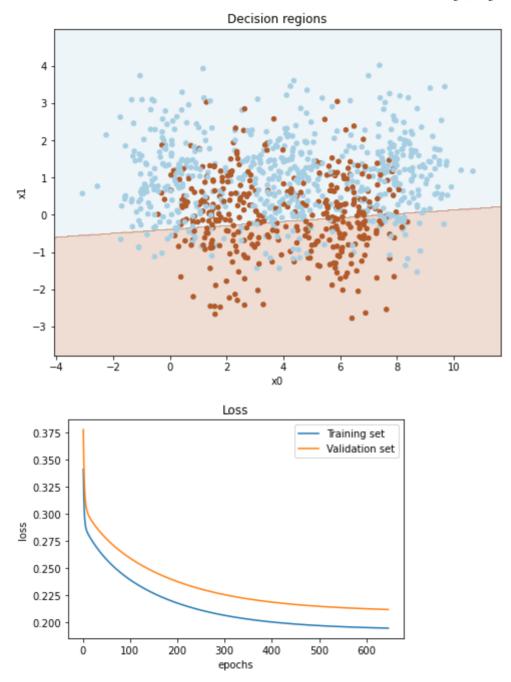
```
In [ ]:
         cl = NumpyLinRegClass()
         training loss, validation loss, training accuracy, validation accuracy = cl.fit(X train, t2 train, 0.00001, X val, t2 val)
         cl.epochs used = len(training loss)
         print("Epochs:", len(training loss))
         print("Accuracy:", cl.accuracy(X val, t2 val))
         #plotting method
         def plot(train stats, title, xlab, ylab, val stats = None):
             y line = train stats
             x line = []
             for i in range(1, len(y line)+1):
                 x line.append(i)
             plt.figure()
             plt.title(title)
             plt.xlabel(xlab)
             plt.ylabel(ylab)
             plt.plot(x line, y line)
             if val stats:
                 y line = val stats
                 plt.plot(x line, y line)
                 plt.legend(["Training set", "Validation set"])
             else:
                 plt.legend(["Training set"])
```

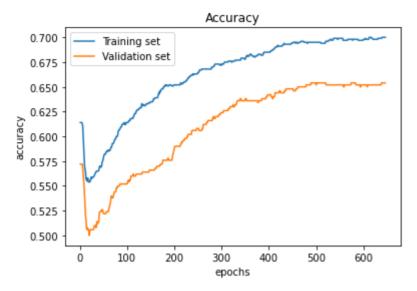
eta: 0.01 loss_diff: 1e-05 Epochs: 646 Accuracy: 0.654 The result is far from impressive. Experiment with various settings for the hyper-parameters, eta and epochs. Report how the accuracy vary with the hyper-parameter settings. When you are satisfied with the result, you may plot the decision boundaries, as below.

Feel free to improve the colors and the rest av of the graphics. We have chosen a simple set-up which can be applied to more than two classes without substanial modifications.

```
In [ ]:
         def plot decision regions(X, t, clf=[], size=(8,6)):
              # Plot the decision boundary. For that, we will assign a color to each
              # point in the mesh [x min, x max]x[y min, y max].
              x \min_{x \in X} x \max_{x \in X} = X[:, 0].\min() - 1, X[:, 0].\max() + 1
              y \min_{x \in X} y \max_{x \in X} = X[:, 1] \cdot \min_{x \in X} (1 - 1, X[:, 1] \cdot \max_{x \in X} (1 + 1)
              h = 0.02 # step size in the mesh
              xx, yy = np.meshgrid(np.arange(x min, x max, h), np.arange(y min, y max, h))
              Z = clf.predict(np.c [xx.ravel(), yy.ravel()])
              plt.figure(figsize=size) # You may adjust this
              # Put the result into a color plot
              Z = Z.reshape(xx.shape)
              plt.contourf(xx, yy, Z, alpha=0.2, cmap = 'Paired')
              plt.scatter(X[:,0], X[:,1], c=t, s=20.0, cmap='Paired')
              plt.xlim(xx.min(), xx.max())
              plt.ylim(yy.min(), yy.max())
              plt.title("Decision regions")
              plt.xlabel("x0")
              plt.ylabel("x1")
              plt.show()
In [ ]:
         plot decision regions(X train, t2 train, cl)
         plot(training loss, "Loss", "epochs", "loss", validation loss)
         plot(training accuracy, "Accuracy", "epochs", "accuracy", validation accuracy)
          #Choosing high ETA of 0.1, or low ETA of 0.00001 gives poor accuracy and high loss. A ETA of 0.01 gives a good balance.
```

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Loss

The linear regression classifier is trained with mean squared error loss. So far, we have not calculated the loss explicitly in the code. Extend the code to calculate the loss on the training set for each epoch and to store the losses such that the losses can be inspected after training.

Train a classifier with your best settings from last point. After training, plot the loss as a function of the number of epochs.

Control training

The training runs for a number of epochs. We cannot know beforehand for how many epochs it is reasonable to run the training. One possibility is to run the training until the learning does not improve much. Extend the fit-method with a keyword argument, <code>loss_diff</code>, and stop training when the loss has not improved with more than loss_diff. Also add an attribute to the classifier which tells us after fitting how many epochs were ran.

In addition, extend the fit-method with optional arguments for a validation set (X_val, t_val). If a validation set is included in the call to fit, calculate the loss for the validation set, and the accuracy for both the training set and the validation set for each epoch.

Train classifiers with the best value for learning rate so far, and with varying values for loss_diff . For each run report, loss_diff , accuracy and number of epochs ran.

After a successful training, plot both training loss snd vslidation loss as functions of the number of epochs in one figure, and both accuracies as functions of the number of epochs in another figure. Comment on what you see.

Logistic regression

You should now do similarly for a logistic regression classifier. Calculate loss and accuracy for training set and, when provided, also for validation set.

Remember that logistic regression is trained with cross-entropy loss. Hence the loss function is calculated differently than for linear regression.

After a successful training, plot both losses as functions of the number of epochs in one figure, and both accuracies as functions of the number of epochs in another figure.

Comment on what you see. Do you see any differences between the linear regression classifier and the logistic regression classifier on this dataset?

Starting point: Code from weekly 7

```
In []:
    def logistic(x):
        return 1/(1+np.exp(-x))

#algorithm for measuring loss, modelled from lectures.
    def log_loss(t, y):
        loss = -np.mean(t*(np.log(abs(y))) - (1-t)*np.log(1-abs(y)))
        return loss
```

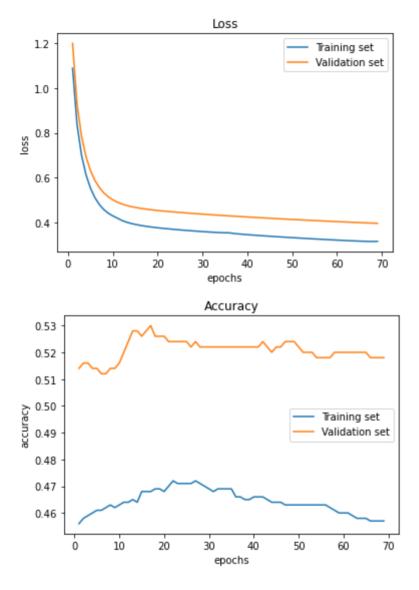
```
if optional args:
    check acc = X train
    check acc val= X val
    X val.shape
    X val = add bias(X val)
(k, m) = X train.shape
X train = add bias(X train)
self.weights = weights = np.zeros(m+1)
training log loss = []
validation log loss = []
training log accuracy = []
validation log accuracy = []
for e in range(epochs):
    #making sure we do not try loss diff unless we have something to compare current result to
    if not training log loss:
            weights -= eta / k * X train.T @ (X train @ weights - t train)
            error = log loss(t train, X train @ weights)
            training log loss.append(error)
            if optional args:
                v error = log loss(t val, X val @ weights)
                validation log loss.append(v error)
                training log accuracy.append(self.accuracy(check acc, t train))
                validation log accuracy.append(self.accuracy(check acc val, t val))
    #making sure we do not try loss diff unless we have something to compare current result to
    elif len(training log loss)==1:
            weights -= eta / k * X train.T @ (X train @ weights - t train)
            error = log loss(t train, X train @ weights)
            training log loss.append(error)
            if optional args:
                v error = log loss(t val, X val @ weights)
                validation log loss.append(v error)
                training log accuracy.append(self.accuracy(check acc, t train))
                validation log accuracy.append(self.accuracy(check acc val, t val))
    #here we have enough values to start using loss diff
    elif (training log loss[e-2]-training log loss[e-1])>loss diff:
            weights -= eta / k * X train.T @ (X train @ weights - t train)
            error = log loss(t train, X train @ weights)
            training log loss.append(error)
            if optional args:
                v error = log loss(t val, X val @ weights)
                validation log loss.append(v error)
```

```
training log accuracy.append(self.accuracy(check acc, t train))
                    validation log accuracy.append(self.accuracy(check acc val, t val))
        else:
            #print("eta:", eta)
            #print("loss diff:", loss diff)
            return training log loss, validation log loss, training log accuracy, validation log accuracy
    return training log loss, validation log loss, training log accuracy, validation log accuracy
def forward(self, X):
    return logistic(X @ self.weights)
def score(self, x):
    z = add bias(x)
    score = self.forward(z)
    return score
def predict(self, x, threshold=0.5):
    z = add bias(x)
    score = self.forward(z)
    return (score>threshold).astype('int')
```

```
In []:
    log_cl = NumpyLogReg()
    training_log_loss, validation_log_loss, training_log_accuracy, validation_log_accuracy = log_cl.fit(X_train, t2_train, print("Epochs:", len(training_log_loss))
    print("Accuracy:", log_cl.accuracy(X_val, t2_val))
    plot(training_log_loss, "Loss", "epochs", "loss", validation_log_loss)
    plot(training_log_accuracy, "Accuracy", "epochs", "accuracy", validation_log_accuracy)

#Accuracy for the logistic classifier varies more, but also appears to have a higher loss. Logistic classif. also finds
```

Epochs: 69
Accuracy: 0.518



Multi-class classifiers

We turn to the task of classifying when there are more than two classes, and the task is to ascribe one class to each input. We will now use the set (X, t).

"One-vs-rest" with logistic regression

We saw in the lecture how a logistic regression classifier can be turned into a multi-class classifier using the one-vs-rest approach. We train one logistic regression classifier for each class. To predict the class of an item, we run all the binary classifiers and collect the probability score from each of them. We assign the class which ascribes the highest probability.

Build such a classifier. Train the resulting classifier on (X_train, t_train), test it on (X_val, t_val), tune the hyper-parameters and report the accuracy.

Also plot the decision boundaries for your best classifier similarly to the plots for the binary case.

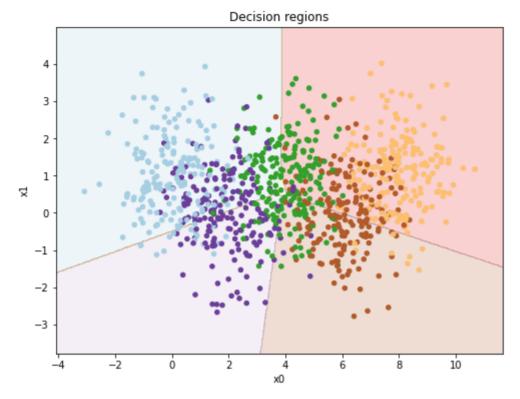
```
In [ ]:
         class NumpyLogRegMultiClass(NumpyClassifier):
             def fit(self, X train, t train, eta = 0.01, epochs=800):
                 (k, m) = X train.shape
                 X train = add bias(X train)
                 (c, r) = t train.shape
                 self.weights = weights = np.zeros((m+1, r))
                 for e in range(epochs):
                     weights -= eta / k * X train.T @ (X train @ weights - t train)
             def forward(self, X):
                 return X @ logistic(self.weights)
             def score(self, x):
                 z = add bias(x)
                 score = self.forward(z)
                 return score
             #could have used argmax further down, but did not have time to implement this
             def predict(self, x):
                 z = add bias(x)
                 score = self.forward(z)
                 (c, r) = x.shape
                 output = np.zeros((c,), dtype=int)
                 index = 0
                 for s in score:
                     best p = -100
                     for p in s:
                         if p > best p:
                             best p = p
                     label = s.tolist().index(best p)
```

```
output[index] = label
            index +=1
        return (output).astype('int')
def make binary(label, classes):
    array = np.zeros((classes,), dtype=int)
    array[label] = 1
    return np.array(array)
def hot encoding(data):
    vectors = []
    classes = np.unique(data)
    for c in data:
        array = []
        for 1 in range(0, len(classes)):
            array.append(0)
        array[c] = 1
        vector = np.array(array)
        vectors.append(vector)
    return np.array(vectors)
multi cl = NumpyLogRegMultiClass()
multi cl.fit(X train, hot encoding(t train))
acc = multi cl.accuracy(X val, t val)
print("Accuracy:", acc)
plot decision regions(X train, t train, multi cl)
```

Accuracy: 0.564

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For in4050-students: Multi-nominal logistic regression

The following part is only mandatory for in4050-students. In3050-students are also welcome to make it a try. Everybody has to return for the part 2 on multi-layer neural networks.

In the lecture, we contrasted the one-vs-rest approach with the multinomial logistic regression, also called softmax classifier. Implement also this classifier, tune the parameters, and compare the results to the one-vs-rest classifier. (Don't expect a large difference on a simple task like this.)

Remember that this classifier uses exponetiation followed by softmax in the forward phase. For loss, it uses cross-entropy loss. The loss has a somewhat simpler form than in the binary case. To calculate the gradient is a little more complicated. The actual gradient and update rule is simple, however, as long as you have calculated the forward values correctly.

Part II

Multi-layer neural networks

We will implement the Multi-layer feed forward network (MLP, Marsland sec. 4.2.1), where we use mean squared loss together with logistic activation in both the hidden and the last layer.

Since this part is more complex, we will do it in two rounds. In the first round, we will go stepwise through the algorithm with the dataset (X, t). We will initialize the network and run a first round of training, i.e. one pass through the algorithm at p. 78 in Marsland.

In the second round, we will turn this code into a more general classifier. We can train and test this on (X, t) and (X, t2), but also on other datasets.

Round 1: One epoch of training

Scaling

First we have to scale our data. Make a standard scaler (normalizer) and scale the data. Remember, not to follow Marsland on this point. The scaler should be constructed from the training data only, but be applied both to training data and later on to validation and test data.

Initialization

We will only use one hidden layer. The number of nodes in the hidden layer will be a hyper-parameter provided by the user; let's call it dim_hidden. (dim_hidden is called M by Marsland.) Initially, we will set it to 3. This is a hyper-parameter where other values may give better results, and the hyper-parameter could be tuned.

Another hyper-parameter set by the user, is the learning rate. We set the initial value to 0.01, but also this may need tuning.

```
eta = 0.01 #Learning rate
dim_hidden = 3
```

We assume that the input *X_train* (after scaling) is a matrix of dimension *P x dim_in*, where *P* is the number of training instances, and *dim_in* is the number of features in the training instances (*L* in Marsland). Hence we can read *dim_in* off from *X_train*.

The target values have to be converted from simple numbers, 0, 2,.. to "one-hot-encoded" vectors similarly to the multi-class task. After the conversion, we can read dim_{out} off from t_{train} .

We need two sets of weights: weights1 between the input and the hidden layer, and weights2, between the hidden layer and the output. Make sure that you take the bias terms into consideration and get the correct dimensions. The weight matrices should be initialized to small random numbers, not to zeros. It is important that they are initialized randomly, both to ensure that different neurons start with different initial values and to generate different results when you rerun the classifier. In this introductory part, we have chosen to fix the random state to make it easier for you to control your calculations. But this should not be part of your final classifier.

Forwards phase

We will run the first step in the training, and start with the forward phase. Calculate the activations after the hidden layer and after the output layer. We will follow Marsland and use the logistic (sigmoid) activation function in both layers. Inspect whether the results seem reasonable with respect to format and values.

```
In [ ]:
         def add negative bias(X):
             # Put bias in position 0
             sh = X.shape
             if len(sh) == 1:
                 #X is a vector
                 return np.concatenate([np.array([1]), X])
             else:
                 # X is a matrix
                 m = sh[0]
                 bias = np.ones((m,1)) # Makes a m*1 matrix of 1-s
                 return np.concatenate([np.negative(bias), X], axis = 1)
         def activation(w, x t):
             #w = weight
             \#x = input
             bias = add negative bias(x t)
             weighted input = bias @ w
             sigmoid = logistic(weighted input)
             return sigmoid
         hidden activations = activation(weights1, scaled data)
```

```
In []: output_activations = activation(weights2, hidden_activations)
    print(output_activations[0, :])
```

```
 [\, 0.26999006 \,\, 0.4474561 \,\, 0.4150512 \,\, 0.37452743 \,\, 0.44141406 \, ]
```

To control that you are on the right track, you may compare your first output value with our result. We have put the bias term -1 in position 0 in both layers. If you have done anything differently from us, you will not get the same numbers. But you may still be on the right track!

```
In [ ]: outputs[0, :]
```

Backwards phase

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Calculate the delta terms at the output. We assume, like Marsland, that we use sum of squared errors. (This amounts to the same as using the mean square error).

Update the weights in both layers.. See whether the weights have changed.

```
In []:
    updatew1 = eta*(np.dot(np.transpose(add_negative_bias(scaled_data)),deltah[:,1:]))
    updatew2 = eta*(np.dot(np.transpose(add_negative_bias(hidden_activations)),deltao))
    weights1 += updatew1
    weights2 += updatew2
```

As an aid, you may compare your new weights with our results. But again, you may have done everything correctly even though you get a different result. For example, there are several ways to introduce the mean squared error. They may give different results after one epoch. But if you run sufficiently many epochs, you will get about the same classifier.

```
In []:
    print("New weights:")
    print(weights1)
```

Step 2: A Multi-layer neural network classifier

Make the classifier

You want to train and test a classifier on (X, t). You could have put some parts of the code in the last step into a loop and run it through some iterations. But instead of copying code for every network we want to train, we will build a general Multi-layer neural network classfier as a class. This class will have some of the same structure as the classifiers we made for linear and logistic regression. The task consists mainly in copying in parts from what you did in step 1 into the template below. Remember to add the *self*- prefix where needed, and be careful in your use of variable names. And don't fix the random numbers within the classifier.

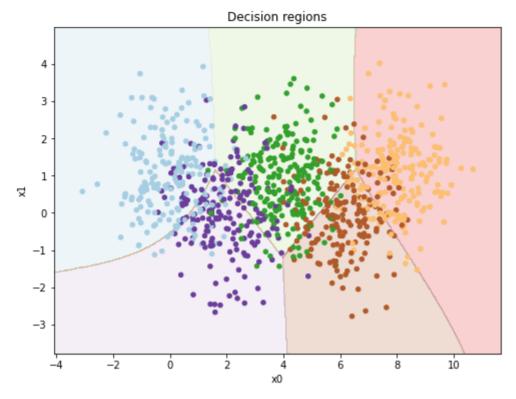
```
In [ ]:
         class MNNClassifier():
             """A multi-layer neural network with one hidden layer"""
             def init (self,eta = 0.1, dim hidden = 6):
                 """Initialize the hyperparameters"""
                 self.eta = eta
                 self.dim hidden = dim hidden
                 self.scaler = MMScaler()
             def fit(self, X train, t train, epochs = 1000):
                 """Initialize the weights. Train *epochs* many epochs."""
                 self.scaler.fit(X train)
                 scaled input = self.scaler.transform(X train)
                 # convert t train
                 (p, d) = scaled input.shape
                 #as explained in the task, dim in must be d from line above
                 dim in = d
                 vectors = hot encoding(t train)
                 (c, r) = vectors.shape
                 dim out = r
                 self.weights1 = weights1 = (np.random.rand(dim in + 1, dim hidden) * 2 - 1)/np.sqrt(dim in)
                 self.weights2 = weights2 = (np.random.rand(dim hidden+1, dim out) * 2 - 1)/np.sqrt(dim hidden)
```

```
for e in range(epochs):
        # Run one epoch of forward-backward
        hidden activations = activation(weights1, scaled input)
        output activations = activation(weights2, hidden activations)
        deltao = (vectors-output activations)*output activations*(1.0-output activations)
        deltah = add negative bias(hidden activations)*(1.0-add negative bias(hidden activations))*(np.dot(deltao,n)
        updatew1 = eta*(np.dot(np.transpose(add negative bias(scaled input)),deltah[:,1:]))
        updatew2 = eta*(np.dot(np.transpose(add negative bias(hidden activations)),deltao))
        weights1 += updatew1
        weights2 += updatew2
def forward(self, X):
    """Perform one forward step.
    Return a pair consisting of the outputs of the hidden layer
    and the outputs on the final layer"""
    self.scaler.fit(X)
    scaled input = self.scaler.transform(X)
    hidden activations = activation(self.weights1, scaled input)
    output activations = activation(self.weights2, hidden activations)
    return hidden activations, output activations
#predict function so that we can plot, could have used argmax
def predict(self, x):
    hidden output, final output = self.forward(x)
    (c, r) = final output.shape
    output = np.zeros((c,), dtype=int)
    index = 0
    for s in final output:
        best p = -100
        for p in s:
            if p > best p:
                best p = p
        label = s.tolist().index(best p)
        output[index] = label
        index +=1
    return (output).astype('int')
#custom accuracy func, could have used argmax
def accuracy(self, X test, t test):
    """Calculate the accuracy of the classifier for the pair (X test, t test)
    Return the accuracy"""
```

```
hidden output, final output = self.forward(X test)
        (c, r) = final output.shape
        output = np.zeros((c,), dtype=int)
        index = 0
        for s in final output:
            best_p = -100
            for p in s:
                if p > best p:
                    best p = p
            label = s.tolist().index(best_p)
            output[index] = label
            index +=1
        pred = (output).astype('int')
        if len(pred.shape) > 1:
            pred = pred[:,0]
        return output, np.sum(pred==t test)/len(pred)
mnn = MNNClassifier()
mnn.fit(X train, t train)
output, acc = mnn.accuracy(X val, t val)
print("Accuracy:", acc)
plot decision regions(X train, t train, mnn)
```

Accuracy: 0.726

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Multi-class

Train the network on (X_train, t_train) (after scaling), and test on (X_val, t_val). Tune the hyperparameters to get the best result:

- number of epochs
- learning rate
- number of hidden nodes.

When you are content with the hyperparameters, you should run the same experiment 10 times, collect the accuracies and report the mean value and standard deviation of the accuracies across the experiments. This is common practise when you apply neural networks as the result may vary slightly between the runs. You may plot the decision boundaries for one of the runs.

Discuss shortly how the results and decsion boundaries compare to the "one-vs-rest" classifier.

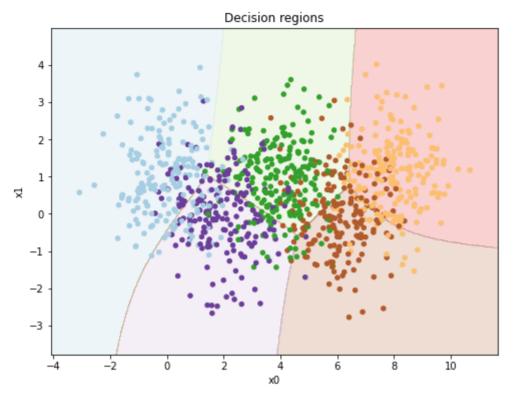
In []: import statistics

```
all_acc = []
for e in range(10):
    mnn = MNNClassifier()
    mnn.fit(X_train, t_train)
    output, acc = mnn.accuracy(X_val, t_val)
    all_acc.append(acc)
    print("Accuracy:", acc)
print("Mean value:", statistics.mean(all_acc))
print("Standard deviation:", statistics.stdev(all_acc))
plot_decision_regions(X_train, t_train, mnn)

#We see in that the accuracy is better for MNN than OVR, and we can see why in the decision boundaries. MNN is able to
```

```
Accuracy: 0.74
Accuracy: 0.738
Accuracy: 0.736
Accuracy: 0.732
Accuracy: 0.738
Accuracy: 0.736
Accuracy: 0.718
Accuracy: 0.718
Accuracy: 0.742
Accuracy: 0.718
Mean value: 0.7316
Standard deviation: 0.009743373816770734
```

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Binary class

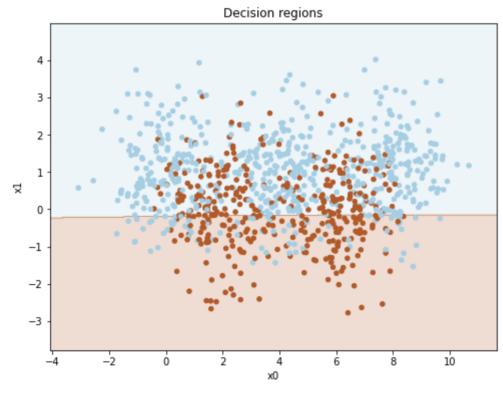
Let us see whether a multilayer neural network can learn a non-linear classifier. Train a classifier on (X_train, t2_train) and test it on (X_val, t2_val). Tune the hyper-parameters for the best result. Run ten times with the best setting and report mean and standard deviation. Plot the decision boundaries.

```
import statistics

all_acc = []
for e in range(10):
    mnn = MNNClassifier()
    mnn.fit(X_train, t2_train)
    output, acc = mnn.accuracy(X_val, t2_val)
    all_acc.append(acc)
    print("Accuracy:", acc)
print("Mean value:", statistics.mean(all_acc))
```

```
print("Standard deviation:", statistics.stdev(all acc))
plot decision regions(X train, t2 train, mnn)
```

Accuracy: 0.67 Accuracy: 0.672 Accuracy: 0.67 Accuracy: 0.674 Accuracy: 0.674 Accuracy: 0.67 Accuracy: 0.674 Accuracy: 0.662 Accuracy: 0.672 Accuracy: 0.674 Mean value: 0.6712 Standard deviation: 0.003675746333890729



For in4050-students: Early stopping

The following part is only mandatory for in4050-students. In3050-students are also welcome to make it a try. Everybody has to return for the part 2 on multi-layer neural networks.

There is a danger of overfitting if we run too many epochs of training. One way to control that is to use early stopping. We can use (X_val, t_val) as valuation set when training on (X_train, t_train).

Let e=50 or e=10 (You may try both or choose some other number) After e number of epochs, calculate the loss for both the training set (X_train, t_train) and the validation set (X_val, t_val), and store them.

Train a classifier for many epochs. Plot the losses for both the training set and the validation set in the same figure and see whether you get the same effect as in figure 4.11 in Marsland.

Modify the code so that the training stops if the loss on the validation set is not reduced by more than *t* after *e* many epochs, where *t* is a threshold you provide as a parameter.

Run the classifier with various values for *t* and report the accuracy and the number of epochs ran.

Part III: Final testing

We can now perform a final testing on the held-out test set.

Binary task (X, t2)

Consider the linear regression classifier, the logistic regression classifier and the multi-layer network with the best settings you found. Train each of them on the training set and evaluate on the held-out test set, but also on the validation set and the training set. Report in a 3 by 3 table.

Comment on what you see. How do the three different algorithms compare? Also, compare the result between the different data sets. In cases like these, one might expect slightly inferior results on the held-out test data compared to the validation data. Is so the case?

Also report precision and recall for class 1.

Multi-class task (X, t)

For IN3050 students compare the one-vs-rest classifier to the multi-layer preceptron. Evaluate on test, validation and training set as above. In4050-students should also include results from the multi-nomial logistic regression.

Comment on the results.

```
In [ ]:
         #BTNARY
         #Linear
         cl = NumpyLinRegClass()
         training loss, validation loss, training accuracy, validation accuracy = cl.fit(X train, t2 train, 0.00001, X val, t2 val)
         lin train acc = cl.accuracy(X train, t2 train)
         lin t2 acc = cl.accuracy(X val, t2 val)
         lin test acc = cl.accuracy(X test, t2 test)
         #Logistic
         log cl = NumpyLogReg()
         training log loss, validation log loss, training log accuracy, validation log accuracy = log cl.fit(X train, t2 train,
         log train acc = log cl.accuracy(X train, t2 train)
         log t2 acc = log cl.accuracy(X val, t2 val)
         log test acc = log cl.accuracy(X test, t2 test)
         #MNN
         mnn = MNNClassifier()
         mnn.fit(X train, t2 train)
         output, mnn train acc = mnn.accuracy(X train, t2 train)
         output, mnn t2 acc = mnn.accuracy(X val, t2 val)
         output, mnn test acc = mnn.accuracy(X test, t2 test)
         #MULTI-CLASS
         #Logistic
         multi cl = NumpyLogRegMultiClass()
         multi cl.fit(X train, hot encoding(t train))
         multi train acc = multi cl.accuracy(X train, t train)
         multi t acc = multi cl.accuracy(X val, t val)
         multi test acc = multi cl.accuracy(X test, t test)
         #MNN
         mnn = MNNClassifier()
         mnn.fit(X train, t train)
         output, mnn train acc = mnn.accuracy(X_train, t_train)
         output, mnn t acc = mnn.accuracy(X val, t val)
         output, mnn test acc = mnn.accuracy(X test, t test)
```

```
names = ["linear", "logistic", "mnn"]
binary train acc = [lin train acc, log train acc, mnn train acc]
binary t2 acc = [lin t2 acc, log t2 acc, mnn t2 acc]
binary test acc = [lin test acc, log test acc, mnn test acc]
multi train acc = ["x", multi train acc, mnn train acc]
multi t acc = ["x", multi t acc, mnn t acc]
multi test acc = ["x", multi test acc, mnn test acc]
titles = ["classifier", "binary train", "binary validation", "binary test", "multiclass train", "multiclass validation"
data = [titles] + list(zip(names, binary train acc, binary t2 acc, binary test acc, multi train acc, multi t acc, multi
for i, d in enumerate(data):
   line = '|'.join(str(x).ljust(12) for x in d)
   print(line)
   if i == 0:
        print('-' * len(line))
#Linear: better results for test set than training set, usually we do not expect this.
#Usually test set will have accuracy closer to that which we see in the validation set.
#The training set must therefore be closer to trainin set than validation set.
#Logistic: the binary version gets worse accuracy for test set as expected.
#The OVR classifier gets better results than binary, and I am not sure as to why.
#The OVR gets similiar accuracy for sets.
#MNN: clearly the best and most versatile classifier. We get about equal accuracies for training and testing.
#This classifier works well for both binary and multiclass.
```

classifier	binary tra	n binary va	lidation binary	test multi	class train m	ulticlass	validation multiclass test
linear	0.7	0.654	0.716	x	x	x	
logistic	0.464	0.528	0.482	0.567	0.564	0.566	
mnn	0.78	0.674	0.788	0.78	0.738	0.788	

```
In []:
```