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1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %% Problem 1
3  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
4  function P1
5  %% In EMOS Units
6      r1 = 1; % Mars Semi-Major Axis [AU]
7      r2 = 1.5237; % Mars Semi-Major Axis [AU]
8      mu = 1; % Standard Gravitation of Sun [AU^3/TU^2]
9
10     disp('Normalized Units')
11     [a_H,t_H,dv_1, dv_2, dv_tot] = HohmannTransfer(r1,r2,mu);
12
13
14     mfmo = exp(-dv_tot/0.1);
15     mpmo = 1-mfmo;
16
17     eps = 1/7;
18     mo=100;
19     mp = 84.71;
20
21     ms = (eps*mp)/(1-eps);
22     ml = 100-(mp+ms);
23
24 %% In Standard Units
25     r1 = 149600000; % Earth Semi-Major Axis [km]
26     r2 = 227940000; % Mars Semi-Major Axis [km]
27     mu = 1.327e11; % Standard Gravitation of Sun [km^3/s^2]
28
29     disp('Standard Units')
30     [a_H,t_H,dv_1, dv_2, dv_tot] = HohmannTransfer(r1,r2,mu);
31
32 end
33
34 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
35 % Hohmann Transfer
36 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
37
38 function [a_H,t_H,dv_1, dv_2, dv_tot] = HohmannTransfer(r1,r2,mu)
39     a_H = (r1+r2)/2;
40     t_H = pi*sqrt((a_H^3)/mu);
41
42     dv_1 = sqrt(mu*((2/r1)-(1/a_H))) - sqrt(mu/r1);
43     dv_2 = sqrt(mu/r2) - sqrt(mu*((2/r2)-(1/a_H)));
44     dv_tot = abs(dv_1) + abs(dv_2);
45 end

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1  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2  %% Problem 2
3  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
4
5
6  function P2
7      r1 = 400+6378;
8      r2 = 382900;
9      mu = 3.985e5;
10
11  %% Quasi-Hohmann
12      [a_H,t_H,dv_1, dv_2, dv_totH] = HohmannTransfer(r1,r2,mu);
13
14  %% Quasi-Bi-Elliptic
15      ri = 3*0.3844e6;
16      [a_1,a_2,dv_1,dv_i,dv_2,dv_totB,R,t1,t2,ttot] = BiEllipticTransfer(r1,r2,ri,mu);
17      (1-(dv_totB/dv_totH))*100
18  end
19
20  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
21  % Bi-Elliptic Transfer
22  %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
23
24  function [a_1,a_2,dv_1,dv_i,dv_2,dv_tot,R,t1,t2,ttot] = BiEllipticTransfer(r1,r2,ri,mu)
25      a_1 = (r1+ri)/2;
26      a_2 = (ri+r2)/2;
27
28      dv_1 = sqrt(mu*((2/r1)-(1/a_1))) - sqrt(mu/r1);
29      dv_i = sqrt(mu*((2/ri)-(1/a_2))) - sqrt(mu*((2/ri)-(1/a_1)));
30      dv_2 = sqrt(mu/r2) - sqrt(mu*((2/r2)-(1/a_2)));
31      dv_tot = abs(dv_1) + abs(dv_2) + abs(dv_i);
32
33      R = r2/r1;
34
35      t1 = pi*sqrt((a_1^3)/mu);
36      t2 = pi*sqrt((a_2^3)/mu);
37      ttot = t1+t2;
38  end

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1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 %% Problem 3A
3 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
4
5 function P3A
6     % Program to optimize two-stage rocket mass
7     x0=[20000,5000,3000];
8     %options=optimset('LargeScale','off','display','iter');
9     options=optimset('LargeScale','off');
10    x=fmincon(@objfun3,x0,[],[],[],[],[],[],@confuneq3,options);
11    x(1)
12    x(2)
13    x(3)
14    f=objfun3(x)
15    [c,ceq]=confuneq3(x);
16 end
17
18 % objfun3.m
19 % Objective function (total mass) for optimal rocket problem
20 function f=objfun3(x)
21     mp=1000;
22     f=x(1)+x(2)+x(3)+mp;
23 end
24
25 % confuneq3.m
26 % constraint equation for optimal rocket problem
27 function [c,ceq]=confuneq3(x)
28     c1 = 3500;
29     c2 = 3800;
30     c3 = 4100;
31     e1 = 0.10;
32     e2 = 0.12;
33     e3 = 0.09;
34     mp = 1000;
35     vfinal = 8500;
36
37     ceq = c1*log((x(1)+x(2)+x(3)+mp)/(e1*x(1)+x(2)+x(3)+mp))+...
38           c2*log((x(2)+x(3)+mp)/(e2*x(2)+x(3)+mp))+...
39           c3*log((x(3)+mp)/(e3*x(3)+mp))-vfinal;
40     c=[];
41 end

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1 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
2 %% Problem 3B
3 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
4
5 function P3B
6 % Program to optimize two-stage rocket mass
7     x0=[20000,5000,3000];
8     %options=optimset('LargeScale','off','display','iter');
9     options=optimset('LargeScale','off');
10    x=fmincon(@oobjfun3,x0,[],[],[],[],[],[],@cconfuneq3,options);
11    x(1)
12    x(2)
13    x(3)
14    f=oobjfun3(x)
15    [c,ceq]=cconfuneq3(x);
16 end
17
18 % objfun3.m
19 % Objective function (total mass) for optimal rocket problem
20 function f=oobjfun3(x)
21     mp=1000;
22     f=x(1)+x(2)+x(3)+mp;
23 end
24
25 % confuneq3.m
26 % constraint equation for optimal rocket problem
27 function [c,ceq]=cconfuneq3(x)
28     c1 = 3500;
29     c2 = 3800;
30     c3 = 4100;
31     e1 = 0.10;
32     e2 = 0.12;
33     e3 = 0.09;
34     mp = 1000;
35     vfinal = 8500;
36     g = 9.81;
37     t = 90;
38
39     ceq = c1*log((x(1)+x(2)+x(3)+mp)/(e1*x(1)+x(2)+x(3)+mp))-g*t+...
40           c2*log((x(2)+x(3)+mp)/(e2*x(2)+x(3)+mp))+...
41           c3*log((x(3)+mp)/(e3*x(3)+mp))-vfinal;
42
43     c=[];
44 end

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