

Section 4: Kinetic Theory

AE435
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2 Mean Free Path

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Assume a particle with diameter, d .

Collisions occur when the center of a another particle falls within a volume of diameter, $2d$, swept out by the initial particle.

Figure 2

For an average speed:

$$\bar{c} = \frac{\sum c_i}{N} \quad (13)$$

The volume swept out per unit time is: $\pi d^2 \bar{c}$

Given a number density, n , $\frac{\#}{m^3}$

The number of collisions will be:

$$\theta = n \pi d^2 \bar{c} \quad (14)$$

If only one particle is moving, we can derive...

Mean Free Path

$$\lambda_1 = \frac{\bar{c}}{\theta} = \frac{1}{n \pi d^2} \quad (15)$$

The average distance between collisions for a particle

If all the particles are moving at the same speed, the relative velocity becomes $\frac{\bar{c}}{\sqrt{2}}$ such that the mean free path becomes:

$$\lambda = \frac{\bar{c}}{\sqrt{2} \theta} = \frac{1}{\sqrt{2} n \pi d^2} \quad (16)$$

Example

Consider air at STP with number density $n_o = 2.69 \times 10^{25} \text{ m}^{-3}$ which is the number of particles per cubic meter.

The average space between particles:

$$\begin{aligned}\delta &= n_o^{-\frac{1}{3}} = 3.34 \times 10^{-9} \text{ [m]} \\ &= 3.34 \text{ [nm]}\end{aligned}$$

While the molecular diameter is:

$$\begin{aligned}d &\approx 0.37 \text{ [nm]} \\ &= 3.7 \text{ [\AA]}\end{aligned}$$

As a result, the Mean Free Path is:

$$\lambda = \frac{1}{\sqrt{2} n \pi d^2} = 61.1 \text{ [nm]}$$

Giving us the general relation that

$$d \ll \delta \ll \lambda$$

Molecular Diameter \ll Average Space Between Particles \ll Mean Free Path