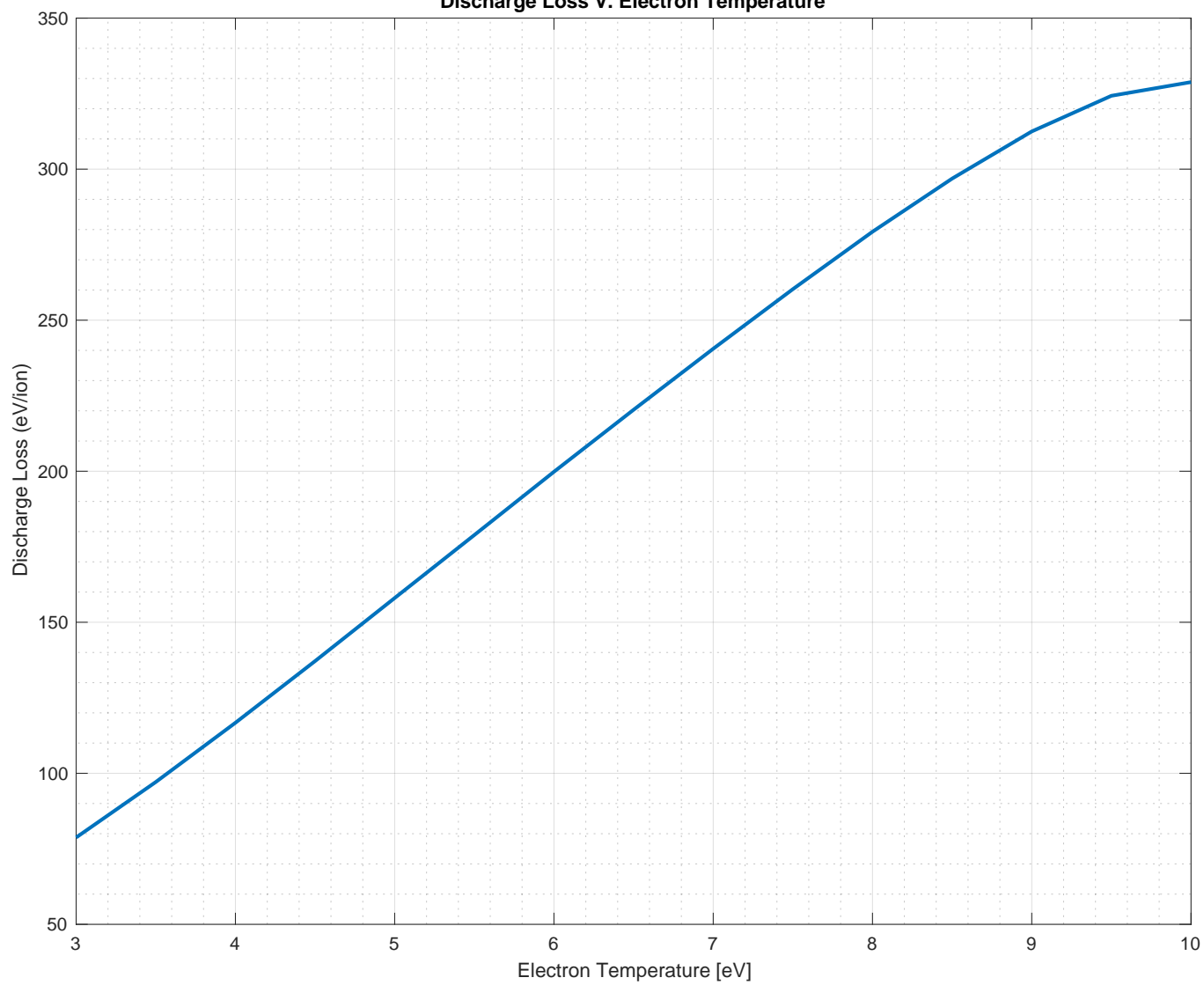


```

1 function hw8p1
2 r = 0.05; %Chamber Radius [m]
3 l = 0.15; % Chamber Length [m]
4 A = pi*r^2; %Grid Area [m^2]
5 A_a = pi*r^2 + 2*pi*r*l; %Anode Area [m^2]
6 T_g = 0.8; %Grid Transparency
7 n_o = 10^18; %Neutral Particle Density [m^-3]
8 V = A*l; % Volume [m^3]
9 Ui = 12.13;% Ionization Potential [eV]
10 Ue = 10; % Excitation Potential [eV]
11 m =9.10938e-31;
12 M = 2.18e-25;
13
14 k = 1.38064852e-23; % Boltzmann Constant [J/K]
15 k2 = 8.6173303e-5; % Boltzmann Constant [eV/K]
16
17 Te = [3 3.5 4 4.5 5 5.5 6 6.5 7 7.5 8 8.5 9 9.5 10]; % Electron Temperature [eV]
18 OVi = [1.08e-15 2.13e-15 3.59e-15 5.43e-15 7.61e-15 1.01e-14 1.28e-14 1.57e-14 1.88e-14 2.20
e-14 2.53e-14 2.86e-14 3.20e-14 3.55e-14 3.90e-14];% Ionization Rate Coefficient [m^3/s]
19 OVe = [2.66e-15 4.66e-15 7.12e-15 9.93e-15 1.30e-14 1.61e-14 1.94e-14 2.26e-14 2.57e-14 2.87
e-14 3.14e-14 3.34e-14 3.41e-14 3.21e-14 2.48e-14];% Excitation Rate Coefficient [m^3/s]
20
21 for i = 1:length(Te)
22     v_a = sqrt((k/k2)*Te(i))/M);
23     eta_d(i) = (((2*n_o*OVi(i)*V)/(T_g*A*v_a))*(Ui + (OVe(i)/OVi(i))*Ue))+((1/(T_g))*(2.5*Te
(i) + 2*Te(i)*log((A_a/A)*sqrt((2*M)/(m*pi)))));
24 end
25
26 plot(Te,eta_d,'linewidth',2)
27 title('Discharge Loss V. Electron Temperature')
28 ylabel('Discharge Loss (eV/ion)')
29 xlabel('Electron Temperature [eV]')
30 grid on
31 grid minor
32
33 set(gcf,'paperorientation','landscape');
34 set(gcf,'paperunits','normalized');
35 set(gcf,'paperposition',[0 0 1 1]);
36 print(gcf,'-dpdf','Problem1.pdf')
37 end

```

Discharge Loss V. Electron Temperature



```

1 function hw8p2
2 clc;clear;
3
4 M = 2.18e-25; % Ion Mass [kg]
5 n_o = 10^13 * (1/1e-6); %Neutral Xenon Gass Density [m^-3]
6 Volume = 10^4*1e-6; % Plasma Volume [m^3]
7 Area = 200*0.0001; % Ion Loss Area [m^2]
8
9 k = 1.38064852e-23; % Boltzmann Constant [J/K]
10 k2 = 8.6173303e-5; % Boltzmann Constant [eV/K]
11
12 K = (k/k2);
13 EE = (2*n_o*Volume)/Area;
14
15 OVi_low = 1.08e-16;
16 OVi_high = 1.2775e-16; % From Hand Calculations
17 Te_low = 2;
18 Te_high = 2.03125; % From Hand Calculations
19
20 %Assuming linear relation between ionization rates.
21 while Te_high-Te_low > .00000001
22     ovi = (OVi_high+OVi_low)/2;
23     t = (Te_high+Te_low)/2;
24     Te_new = (EE^2 * ovi^2)*(M/K);
25     if Te_new >= t
26         OVi_high = ovi;
27         Te_high = t;
28     else
29         OVi_low = ovi;
30         Te_low = t;
31     end
32 end
33
34 Te_guess = Te_low;
35 OVi = OVi_high
36 Te_calculated = (EE^2 * OVi^2)*(M/K)
37
38 end

```

```

1 function hw8p3
2 e = 1.60217662e-19; % Electron Charge [J]
3 r_inner = .10/2;    % Inner Radius [m]
4 r_outer = .15/2;    % Outer Radius [m]
5 Ae = (pi*r_outer^2)-(pi*r_inner^2); % Exit Area [m^2]
6 ni = 5e17;          % Ion Plasma Density [m^-3]
7 B = 200;            % Radial Magnetic Field [G]
8 m =9.10938e-31;     % Electron Mass [kg]
9 M = 2.18e-25;       % Ion Mass [kg]
10 Te = 20;            % Electron Temperature [eV]
11 Vd = 300;           % Discharge Chamber Potential [V]
12
13 k = 1.38064852e-23; % Boltzmann Constant [J/K]
14 k2 = 8.6173303e-5;  % Boltzmann Constant [eV/K]
15
16 %Part A
17 Ii = ni*e * sqrt((2*e*Vd)/(M))*Ae; % Beam Current [A]
18 P = Ii*Vd;                    % Beam Power [W]
19
20 %Part B
21 r_L = ((m*1000)/(e*B))*sqrt((8*(k/k2)*Te)/(pi*m))*1000*10; % Larmor Radius [mm]
22
23 %Part C
24 wB = (e*B)/(m); % Cyclotron Frequency [1/s]
25 Q = 6.5e-13/((3/2)*Te)^2; % Collisional Cross Section
26 vth = sqrt((8*(k/k2)*Te)/(pi*m)); % Collision Speed
27 nu = ni*Q*vth; % Collision Frequency [1/s]
28
29 omega = sqrt(wB^2/nu^2); % Hall Parameter
30
31 %Part D
32 gamma= 0.9; % Thrust Coefficient Factor
33 eta_m = 0.8; % Mass Utilization Efficiency
34
35
36 mdot_i = (Ii*M)/e;
37 vi = sqrt((2*e*Vd)/(M));
38 Isp = (gamma*eta_m*vi)/9.81;
39 T = gamma*mdot_i*vi;
40
41 %Part E
42 IH = ni*e*((.15-.1)/2)*(Vd/(B*10^-4));
43 I_H = (Ii/(2*pi*((r_inner+r_outer)/2)*(B*10^-4)))*sqrt((M*Vd)/(2*e));
44 end

```

```

1 function hw8p5
2 m = 9.10938e-31;
3 M = 2.18e-25;           % Ion Mass [kg]
4 k = 1.3806e-23;         % Boltzmann Constant [J/K]
5 k2 = 8.6173e-5;         % Boltzmann Constant [eV/K]
6 K = (k/k2);             % Boltzmann Constant [J/eV]
7 n_o = 10^13 * (1/1e-6); % Neutral Xenon Gas Density [m^-3]
8 Volume = 10^4 * 1e-6;   % Plasma Volume [m^3]
9 Area = 200 * 0.0001;    % Ion Loss Area [m^2]
10 EE = (2 * n_o * Volume) / Area;
11 eo = 8.854e-12;         % Vacuum Dielectric Constant [C^2/Nm^2]
12 h = 6.6262e-34;        % Planks Constant [Js]
13 qe = 1.60217662e-19;   % Electron Charge [C]
14 ao = (eo * h^2) / (pi * m * qe^2); % Atomic Cross Section [m^2]
15 Q = pi * ao^2 * 4.38;   % Emperical Cross Section [m^2]
16 %% This approach uses equations fitted to the empiracle ionization distributions to
    calculate the maxwellian distribution given a specific value of Te.
17 Te_low = 1; Te_high = 3;
18 while Te_high - Te_low > .00000000000001
19     Te = (Te_low + Te_high) / 2;
20     if Te < 5
21         %Maxwellian Ionization Rate Coefficient
22         MOVi = 10^-20 * ((3.97 + 0.643 * Te - 0.0368 * Te^2) * exp(-12.127 / Te)) * sqrt((8 * K * Te) / (pi * m));
23     else
24         %Maxwellian Ionization Rate Coefficient
25         MOVi = 10^-20 * (-(1.031e-4 * Te^2) + 6.386 * exp(-12.127 / Te)) * sqrt((8 * K * Te) / (pi * m));
26     end
27     Vth = sqrt((8 * K * Te) / (pi * m));
28     OVi = 0.0005 * Q * Vth + 0.9995 * MOVi;
29     Te_new = (EE^2 * OVi^2) * (M / K);
30     if Te_new >= Te
31         Te_high = Te;
32     else
33         Te_low = Te;
34     end
35 end
36 %% This approach assumes a linear relation between the maxwellian ionizaion reaction rates
    and solves for a new ionization coefficient rate. With this, Te is recalculated and
    compared to the guessed Te value.
37 Te_low = 1.5; Te_high = 2; OVi_low = 1.16e-17; OVi_high = 1.08e-16;
38 while Te_high - Te_low > .00000000000001
39     ovi = (OVi_high + OVi_low) / 2;
40     t = (Te_high + Te_low) / 2;
41     Vth = sqrt((8 * K * Te) / (pi * m));
42     OVI = 0.0005 * Q * Vth + 0.9995 * ovi;
43     Te_new = (EE^2 * OVI^2) * (M / K);
44     if Te_new >= t
45         OVi_high = ovi;
46         Te_high = t;
47     else
48         OVi_low = ovi;
49         Te_low = t;
50     end end end

```