- 1. Explain why you would use spline regressions instead of a higher order polynomial that would be much easier to set up and use? [3 marks]
- 2. Draw a well labelled diagram of a neural network with two hidden layers and X_1, X_2, X_3, X_4 and X_5 as the input variables. [4 marks]
- 3. Define what is meant by a spline and illustrate using two examples. Show that splines are linear smoothers. [5 marks]
- 4. In Kernel regression estimation, one may choose a deterministic or stochastic design depending on the type of the problem at hand.
 - (a) Describe a deterministic design model and give its kernel estimate of the mean function. [3 marks]
 - (b) Describe a stochastic design model and give its kernel estimate of the mean function. [3 marks]
- 5. Given the data

| Χ | 20 | 30 | 15 | 25 | 28 |
|---|------|------|------|------|------|
| Y | 45.6 | 35.3 | 40.3 | 20.0 | 43.2 |

where X and Y are predictor and response variables, respectively. Using a rectangular Kernel function and 3-nearest neighbour (K-NN) find the estimate of

- (a) Density function of X at point x = 29 and at x = 34 [3 marks]
- (b) Regression function at point x = 29 and at x = 34 [3 marks]
- 6. Explain how to check the assumptions of a linear mixed model [3 marks]
- 7. Describe the main steps of the supervised training algorithm [3 marks]