#### AutoML: Interpretability

Overview: Automated Empirical Analysis

Bernd Bischl Frank Hutter Lars Kotthoff <u>Marius Lindauer</u> Joaquin Vanschoren

#### Idea

- Big challenge of ML: Interpretability
  - ▶ In some applications, it is required to "understand" a prediction
  - ▶ Users have less trust in systems, they can't understand

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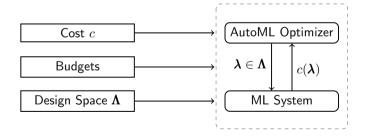
- Big challenge of ML: Interpretability
  - ▶ In some applications, it is required to "understand" a prediction
  - Users have less trust in systems, they can't understand
- AutoML is even worse?
  - AutoML is a black-box that automates the design of another blackbox (ML)
  - ▶ Also ML-developers have an basic understanding of the design of their ML pipelines
- Automated empirical interpretability helps to
  - understand the finally returned ML system
  - understand the AutoML process

- Insights:
  - AutoML is yet another optimization problem
  - ▶ (Most) AutoML approach are iterative in nature
- --- AutoML generates a lot of empirical data

Cost cBudgets

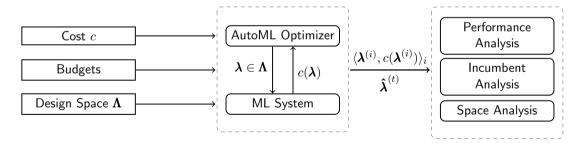
Design Space  $\Lambda$ 

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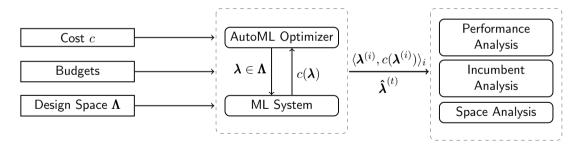




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 $\rightsquigarrow$  Let's use this data to learn something about our AutoML problem

### Basic Examples

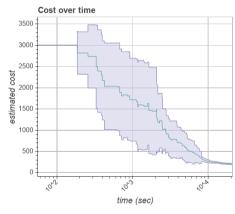
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  - ML pipeline with its components
  - ► Neural architecture

# Basic Examples

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  - ML pipeline with its components
  - ► Neural architecture
- ullet Compare what changed between  $\lambda_{\mathsf{def}}$  and  $\hat{\lambda}$

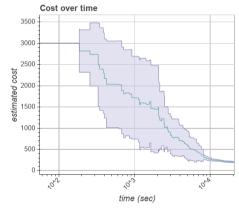
#### Basic Examples

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  - ML pipeline with its components
  - ► Neural architecture
- ullet Compare what changed between  $\lambda_{\mathsf{def}}$  and  $\hat{\lambda}$
- $oldsymbol{\circ}$  Show  $oldsymbol{\hat{\lambda}}$  on different budgets (if you used a multi-fideltiy approach)

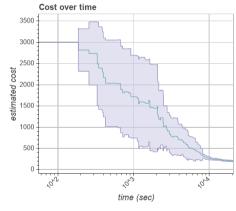


Source: [Lindauer et al. 2019]

 Study how your AutoML tool improves cost (or loss) over time

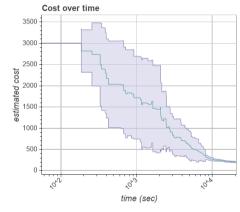


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- Allows to identify whether
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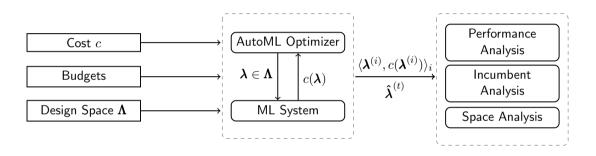
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- Study how your AutoML tool improves cost (or loss) over time
- Allows to identify whether
  - you need less time next time or
  - the AutoML system is still improving; so you should give it more time
- Notes:
  - ▶ Plot on log-scale to see details in the beginning
  - If you done several runs, plot distribution (e.g., median and 25/75%-quartiles)

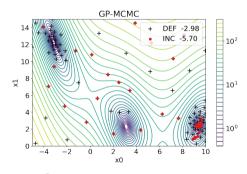
# AutoML: Interpretability

Studying the AutoML Optimization Process

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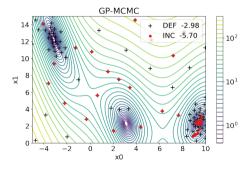


ightharpoonup focus on how the AutoML optimizer samples from the design space  $\Lambda$ 



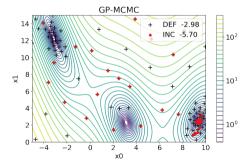
Source: [Lindauer et al. 2019]

Plot of a 1D or 2D function



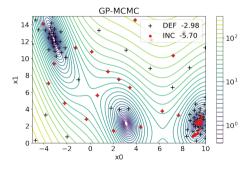
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- Plot of a 1D or 2D function
- Background shows the ground truth (real function values)



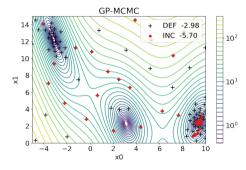
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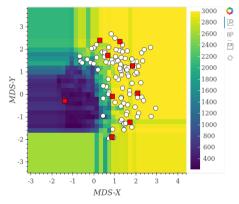
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- Plot of a 1D or 2D function
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- Typical approach in Bayesian Optimization community



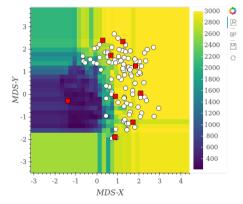
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- Plot of a 1D or 2D function
- Background shows the ground truth (real function values)
- Dots are sampled points in the search space
- Typical approach in Bayesian Optimization community
- → Impossible for higher dimensional problems?

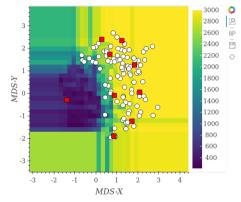


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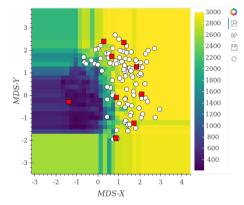
• Same idea as before but we have to project N-D into 2-D



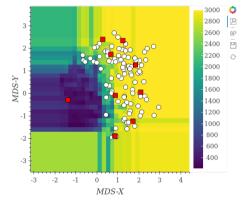
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  - 1 Use an MDS to project down to 2-D



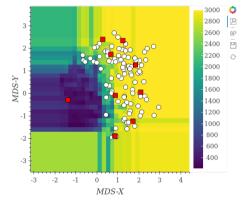
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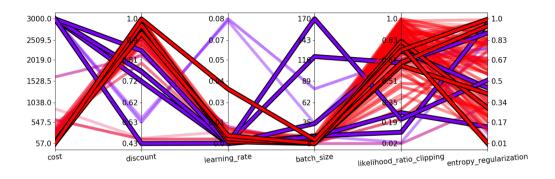


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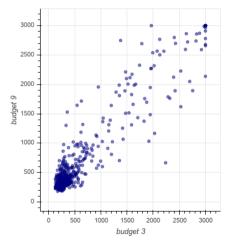
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  - Extension: Animation by showing how points get added over time

#### Parallel Coordinate Plot [Golovin et al. 2017]



- Each coordinate is one hyperparameter;
- Except the most left one: cost or loss

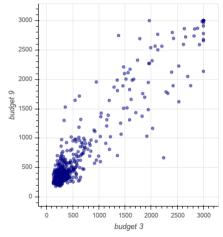
# Multi-Fidelity Checks



Source: [Lindauer et al. 2019]

- Challenge of multi-fidelity approaches:
  - ► How to choose the fidelities (a.k.a. budgets)

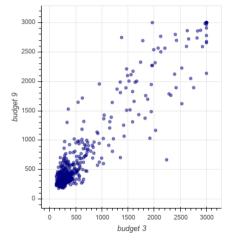
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# Multi-Fidelity Checks



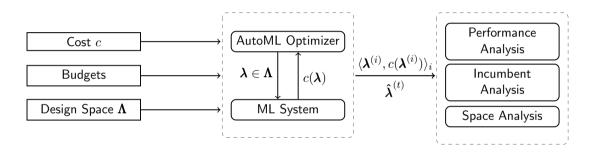
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- Challenge of multi-fidelity approaches:
  - ► How to choose the fidelities (a.k.a. budgets)
- Important Property:
  - Decisions on small budgets should be reasonable for higher budgets
- Analysis:
  - Scatter plot of performance on Budget X vs. Budget Y
  - Each dot is sampled hyperparameter configuration
  - **3** Compute rank correlation (here: 0.69)

#### AutoML: Interpretability

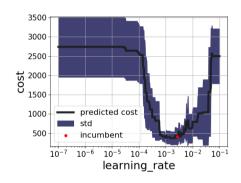
Incumbent Analysis and Local Hyperparameter Importance

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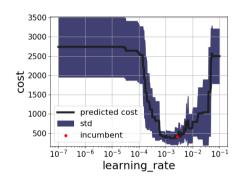
→ focus on why is the eventually returned configuration a good choice

#### Local Importance [Biedenkapp et al. 2018]



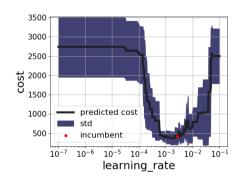
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- Typical question of users:
  - ▶ How would the performance change if we change hyperparameter  $\lambda_i$ ?
- Problem: Running full study is often too expensive
  - ► Each run of an ML-system is potential expensive
  - Key Ideas:
    - Re-use probabilistic models as trained in BO
    - Plot performance change around  $\hat{\pmb{\lambda}}^{(t)}$  along each dimension

# Quantifying Local Importance [Biedenkapp et al. 2018]

$$VAR_{\lambda}(i) = \sum_{v \in \Lambda} (\mathbb{E}_{v \sim \Lambda_i}[L(\lambda)] - L(\lambda[\lambda_i := v]))^2$$
(1)

### Quantifying Local Importance [Biedenkapp et al. 2018]

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$$LPI(i \mid \lambda) = \frac{VAR_{\lambda}(i)}{\sum_{j} VAR_{\lambda}(j)}$$
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While fixing all other hyperparameters to the incumbent value, the hyperparameter with the highest variance is the most important one

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  - As given in the documentation
  - Or as always used in the last time

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 $\lambda^{\text{(end)}} = [0.98, 2.42, 1, 42]$ 

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- Cheap approach: Assess  $\lambda^{(end)}$  with each hyperparameter value from  $\lambda^{(start)}$
- ullet Expensive approach: Try all mixtures of  $oldsymbol{\lambda}^{( ext{end})}$  and  $oldsymbol{\lambda}^{( ext{start})}$ 
  - Only feasible for small spaces and fairly cheap ML systems
- ullet Trade-off: Find a way from  $oldsymbol{\lambda}^{(start)}$  to  $oldsymbol{\lambda}^{(end)}$  in a greedy fashion [Fawcett and Hoos. 2016]

Given:

$$m{\lambda}^{( extsf{start})} = [1, 1, 0, 100] \qquad L_{ extsf{start}} = 20\% \ m{\lambda}^{( ext{end})} = [0.98, 2.42, 1, 42] \quad L_{ ext{end}} = 4\%$$

Given:

$$m{\lambda}^{({\sf start})} = [1, 1, 0, 100] \qquad L_{\sf start} = 20\% \ m{\lambda}^{({\sf end})} = [0.98, 2.42, 1, 42] \qquad L_{\sf end} = 4\%$$

$$\lambda^{(1)} = [0.98, 1, 0, 100] \quad L_1 = 19\%$$

Given:

$$m{\lambda}^{( extsf{start})} = [1, 1, 0, 100] \qquad L_{ extsf{start}} = 20\% \ m{\lambda}^{( ext{end})} = [0.98, 2.42, 1, 42] \quad L_{ ext{end}} = 4\%$$

$$\lambda^{(1)} = [0.98, 1, 0, 100] \quad L_1 = 19\%$$
  
 $\lambda^{(2)} = [1, 2.42, 0, 100] \quad L_2 = 20\%$ 

Given:

$$m{\lambda}^{( extsf{start})} = [1, 1, 0, 100] \qquad L_{ extsf{start}} = 20\% \ m{\lambda}^{( ext{end})} = [0.98, 2.42, 1, 42] \quad L_{ ext{end}} = 4\%$$

$$\lambda^{(1)} = [0.98, 1, 0, 100] \quad L_1 = 19\%$$
 $\lambda^{(2)} = [1, 2.42, 0, 100] \quad L_2 = 20\%$ 
 $\lambda^{(3)} = [1, 1, 1, 100] \quad L_3 = 7\%$ 

Given:

$$m{\lambda}^{( extsf{start})} = [1, 1, 0, 100] \qquad L_{ extsf{start}} = 20\% \ m{\lambda}^{( ext{end})} = [0.98, 2.42, 1, 42] \quad L_{ ext{end}} = 4\%$$

$$\lambda^{(1)} = [0.98, 1, 0, 100] \quad L_1 = 19\%$$
 $\lambda^{(2)} = [1, 2.42, 0, 100] \quad L_2 = 20\%$ 
 $\lambda^{(3)} = [1, 1, 1, 100] \quad L_3 = 7\%$ 
 $\lambda^{(4)} = [1, 1, 0, 42] \quad L_4 = 16\%$ 

Given:

$$m{\lambda}^{({
m start})} = [1, 1, 0, 100] \qquad L_{{
m start}} = 20\% \ m{\lambda}^{({
m end})} = [0.98, 2.42, 1, 42] \qquad L_{{
m end}} = 4\%$$

1st Iteration:

$$\lambda^{(1)} = [0.98, 1, 0, 100] \quad L_1 = 19\%$$
 $\lambda^{(2)} = [1, 2.42, 0, 100] \quad L_2 = 20\%$ 
 $\lambda^{(3)} = [1, 1, 1, 100] \quad L_3 = 7\%$ 
 $\lambda^{(4)} = [1, 1, 0, 42] \quad L_4 = 16\%$ 

 $\rightsquigarrow$  1st step:  $\lambda_2$  – flipping hyperparameter 3

Given:

$$m{\lambda}^{( ext{start})} = [1, 1, 0, 100] \qquad L_{ ext{start}} = 20\% \ m{\lambda}^{(s1)} = [1, 1, 1, 100] \qquad L = 7\% \ m{\lambda}^{( ext{end})} = [0.98, 2.42, 1, 42] \qquad L_{ ext{end}} = 4\%$$

2nd Iteration:

$$\boldsymbol{\lambda}^{(1)} = [0.98, 1, 1, 100] \quad L_1 = 6\%$$

Given:

$$m{\lambda}^{( ext{start})} = [1, 1, 0, 100] \qquad L_{ ext{start}} = 20\% \ m{\lambda}^{(s1)} = [1, 1, 1, 100] \qquad L = 7\% \ m{\lambda}^{( ext{end})} = [0.98, 2.42, 1, 42] \qquad L_{ ext{end}} = 4\%$$

2nd Iteration:

$$\lambda^{(1)} = [0.98, 1, 1, 100]$$
  $L_1 = 6\%$   
 $\lambda^{(2)} = [1, 2.42, 1, 100]$   $L_2 = 7\%$ 

Given:

$$\begin{array}{lll} \pmb{\lambda}^{(\mathsf{start})} &= [1, 1, 0, 100] & L_{\mathsf{start}} = 20\% \\ \pmb{\lambda}^{(s1)} &= [1, 1, 1, 100] & L = 7\% \\ \pmb{\lambda}^{(\mathsf{end})} &= [0.98, 2.42, 1, 42] & L_{\mathsf{end}} = 4\% \\ \end{array}$$

2nd Iteration:

$$\lambda^{(1)} = [0.98, 1, 1, 100]$$
  $L_1 = 6\%$   
 $\lambda^{(2)} = [1, 2.42, 1, 100]$   $L_2 = 7\%$   
 $\lambda^{(3)} = [1, 1, 1, 42]$   $L_3 = 5\%$ 

 $\rightsquigarrow$  2nd step:  $\lambda_3$  – flipping hyperparameter 4

Given:

$$\begin{array}{lll} \pmb{\lambda}^{(\mathsf{start})} &= [1, 1, 0, 100] & L_{\mathsf{start}} = 20\% \\ \pmb{\lambda}^{(s1)} &= [1, 1, 1, 100] & L = 7\% \\ \pmb{\lambda}^{(s2)} &= [1, 1, 1, 42] & L = 5\% \\ \pmb{\lambda}^{(\mathsf{end})} &= [0.98, 2.42, 1, 42] & L_{\mathsf{end}} = 4\% \\ \end{array}$$

3rd Iteration:

$$\lambda^{(1)} = [0.98, 1, 1, 100]$$
  $L_1 = 4\%$   
 $\lambda^{(2)} = [1, 2.42, 1, 100]$   $L_2 = 5\%$ 

 $\rightsquigarrow$  2nd step:  $\lambda_3$  – flipping hyperparameter 1

#### Ablation Path:

$$\begin{split} \pmb{\lambda}^{(\mathsf{start})} &= [1, 1, 0, 100] & L_{\mathsf{start}} = 20\% \\ \pmb{\lambda}^{(s1)} &= [1, 1, 1, 100] & L = 7\% \\ \pmb{\lambda}^{(s1)} &= [1, 1, 1, 42] & L = 5\% \\ \pmb{\lambda}^{(s3)} &= [0.98, 1, 1, 42] & L = 4\% \\ \pmb{\lambda}^{(s4)} &= [0.98, 2.42, 1, 42] & L = 4\% \\ \pmb{\lambda}^{(\mathsf{end})} &= [0.98, 2.42, 1, 42] & L_{\mathsf{end}} = 4\% \end{split}$$

#### Algorithm 1 Greedy Ablation

**Input**: Algorithm  $\mathcal A$  with configuration space  $\mathbf \Lambda$ , start configuration  $\mathbf \lambda^{(\mathsf{start})}$ , end configuration  $\mathbf \lambda^{(\mathsf{end})}$ , cost metric c

$$\lambda \leftarrow \lambda^{(\text{start})};$$
 $P \leftarrow [];$ 

#### Algorithm 2 Greedy Ablation

**Input**: Algorithm  $\mathcal A$  with configuration space  $\mathbf \Lambda$ , start configuration  $\mathbf \lambda^{(\mathsf{start})}$ , end configuration  $\mathbf \lambda^{(\mathsf{end})}$ , cost metric c

```
oldsymbol{\lambda} \leftarrow oldsymbol{\lambda}^{(\mathsf{start})}; \ P \leftarrow [] \ ; \ \mathbf{foreach} \ t \in \{1 \dots |oldsymbol{\Lambda}|\} \ \mathbf{do}
```

#### **Algorithm 3** Greedy Ablation

**Input**: Algorithm  $\mathcal A$  with configuration space  $\mathbf \Lambda$ , start configuration  $\mathbf \lambda^{(\mathsf{start})}$ , end configuration  $\mathbf \lambda^{(\mathsf{end})}$ , cost metric c

```
\begin{split} \boldsymbol{\lambda} &\leftarrow \boldsymbol{\lambda}^{(\mathsf{start})}; \\ P &\leftarrow [] \ ; \\ \textbf{foreach} \ t \in \{1 \dots |\boldsymbol{\Lambda}|\} \ \textbf{do} \\ & \begin{vmatrix} \boldsymbol{\lambda}_{\delta}' \leftarrow \mathsf{apply} \ \delta \ \mathsf{to} \ \boldsymbol{\lambda}; \\ \mathsf{evaluate} \ c(\boldsymbol{\lambda}_{\delta}'); \end{vmatrix} \end{split}
```

#### **Algorithm 4** Greedy Ablation

```
Input: Algorithm \mathcal A with configuration space \pmb \Lambda, start configuration \pmb \lambda^{(\mathsf{start})} end configuration \pmb \lambda^{(\mathsf{end})}, cost metric c
```

```
\lambda \leftarrow \lambda^{(\text{start})}:
   P \leftarrow []:
   foreach t \in \{1 \dots |\Lambda|\} do
        foreach \delta \in \Delta(\lambda, \lambda^{(end)}) do
                \lambda'_{\delta} \leftarrow \text{apply } \delta \text{ to } \lambda;
                 evaluate c(\lambda'_{\delta});
         Determine most important change \delta^* \in \arg\min_{\delta \in \Delta(\boldsymbol{\lambda}, \boldsymbol{\lambda}^{(\text{end})})} c(\boldsymbol{\lambda}_{\delta});
           \lambda \leftarrow \text{apply } \delta^* \text{ to } \lambda:
            P.append(\delta^*):
```

#### **Algorithm 5** Greedy Ablation

```
Input: Algorithm \mathcal A with configuration space \pmb \Lambda, start configuration \pmb \lambda^{(\mathsf{start})} end configuration \pmb \lambda^{(\mathsf{end})}, cost metric c
```

```
\lambda \leftarrow \lambda^{(\text{start})}:
   P \leftarrow []:
   foreach t \in \{1 \dots |\Lambda|\} do
        foreach \delta \in \Delta(\lambda, \lambda^{(end)}) do
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            evaluate c(\lambda'_{\delta});
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          \lambda \leftarrow \text{apply } \delta^* \text{ to } \lambda:
           P.append(\delta^*):
 return Ablation path P
```

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  - Common observations:
    - lacksquare Some hyperparameters might not matter ( $oldsymbol{\lambda}_2$  in the example)

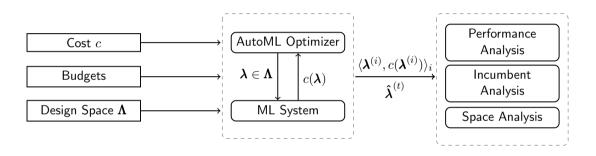
- ullet Even this greedy ablation requires  $\mathcal{O}(n^2)$  steps
- → We can also speedup that up by using surrogate models
  [Biedenkapp et al. 2017]
  - Common observations:
    - **①** Some hyperparameters might not matter ( $\lambda_2$  in the example)
    - Often only a few of the hyperparameters have an big impact

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- We can also speedup that up by using surrogate models [Biedenkapp et al. 2017]
- Common observations:
  - **①** Some hyperparameters might not matter ( $\lambda_2$  in the example)
  - Often only a few of the hyperparameters have an big impact
  - You have plateaus in your ablation path because of interaction effects

## AutoML: Interpretability

Global Hyperparameter Importance

Bernd Bischl Frank Hutter Lars Kotthoff <u>Marius Lindauer</u> Joaquin Vanschoren



→ focus on which hyperparameters are important across the entire search space

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- Advantages:
  - Very cheap to do, since we only have to query the surrogate model several times
- Potential drawback:
  - ► The surrogate model might overfit to different subsets of the hyperparameters (if we don't provide sufficient data)

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#### fANOVA [Sobobl. 1993]

Write performance predictions as a sum of components:

$$\hat{y}(\boldsymbol{\lambda}_1, \dots, \boldsymbol{\lambda}_n) = \hat{f}_0 + \sum_{i=1}^n \hat{f}_i(\boldsymbol{\lambda}_i) + \sum_{i \neq j} \hat{f}_{ij}(\boldsymbol{\lambda}_i, \boldsymbol{\lambda}_j) + \dots$$

$$\hat{y}(\boldsymbol{\lambda}_1, \dots, \boldsymbol{\lambda}_n) = \text{average response} + \text{main effects} +$$
2-D interaction effects + higher order effects

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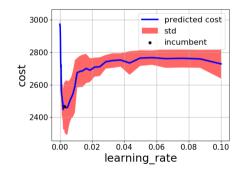
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 $\hat{y}(\boldsymbol{\lambda}_1,\ldots,\boldsymbol{\lambda}_n) = \text{average response} + \text{main effects} + \text{2-D interaction effects} + \text{higher order effects}$ 

#### Variance Decomposition

$$V = \frac{1}{||\boldsymbol{\Lambda}||} \int_{\boldsymbol{\lambda}_1} \dots \int_{\boldsymbol{\lambda}_n} [(\hat{y}(\boldsymbol{\lambda}) - \hat{f}_0)^2] d\boldsymbol{\lambda}_1 \dots d\boldsymbol{\lambda}_n$$

• The fANOVA and variance decomposition can be done efficiently in linear time if the surrogate model is a random forest [Hutter et al. 2014]

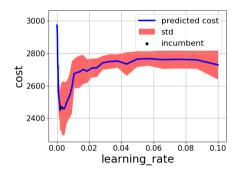
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predicted cost is marginalized over all other hyperparameter effects

Source: [Lindauer et al. 2019]

The fANOVA and variance decomposition can be done efficiently in linear time
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- predicted cost is marginalized over all other hyperparameter effects
- Warning: The optimum on these curves does not have to be the global optimum across all hyperparameters

 How much of the variance can be explained by a hyperparameter (or combinations of hyperparamaters) marginalized over all other parameters?

Table: Exemplary analysis of PPO on cartpole

Hyperparameter	Explained Variance
Discount rate	19.3 %
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Likelihood ration clipping	3.4%
discount rate & batch size	10.4%
discount rate & likelihood ration clipping	4.4%

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- Implicit assumption: the surrogate model models the space fairly well
- Global analysis and local analysis of hyperparameter importance does not always agree [Biedenkapp et al. 2018]
- You should run both to get a good understanding of why an AutoML tool chose a configuration