

# AutoML: Beyond AutoML

## Racing for Algorithm Configuration

Bernd Bischl   Frank Hutter   Lars Kotthoff  
Marius Lindauer   Joaquin Vanschoren

# State-of-the-art Algorithm Configuration

SMAC: Sequential Model-based Algorithm Configuration [Hutter et al. 2011]

- Bayesian Optimization +
- aggressive racing +
- adaptive capping (for optimizing runtime)

---

**Algorithm 1** SMAC

---

**Input** : instance set  $\mathcal{I}$ , Algorithm  $\mathcal{A}$  with configuration space  $\Lambda$ , Initial configuration  $\lambda_0$ , performance metric  $c$ , Configuration budget  $b$

run history  $\mathcal{D}_{\text{Hist}} \leftarrow$  initial design based on  $\lambda_0$ ;

//  $\mathcal{D}_{\text{Hist}} = (\lambda, i, c(i, \lambda))_i$

**while**  $b$  remains **do**

|

---

## Algorithm 2 SMAC

---

**Input** : instance set  $\mathcal{I}$ , Algorithm  $\mathcal{A}$  with configuration space  $\Lambda$ , Initial configuration  $\lambda_0$ , performance metric  $c$ , Configuration budget  $b$

run history  $\mathcal{D}_{\text{Hist}} \leftarrow$  initial design based on  $\lambda_0$ ; //  $\mathcal{D}_{\text{Hist}} = (\lambda, i, c(i, \lambda))_i$

**while**  $b$  remains **do**

$\hat{c} \leftarrow$  train empirical performance model based on run history  $\mathcal{D}_{\text{Hist}}$ ;

---

## Algorithm 3 SMAC

---

**Input** : instance set  $\mathcal{I}$ , Algorithm  $\mathcal{A}$  with configuration space  $\Lambda$ , Initial configuration  $\lambda_0$ , performance metric  $c$ , Configuration budget  $b$

run history  $\mathcal{D}_{\text{Hist}} \leftarrow$  initial design based on  $\lambda_0$ ;  $// \mathcal{D}_{\text{Hist}} = (\lambda, i, c(i, \lambda))_i$

**while**  $b$  remains **do**

$\hat{c} \leftarrow$  train empirical performance model based on run history  $\mathcal{D}_{\text{Hist}}$ ;

$\Lambda_{\text{challengers}} \leftarrow$  select configurations based on  $\hat{c}$ ;

---

## Algorithm 4 SMAC

---

**Input** : instance set  $\mathcal{I}$ , Algorithm  $\mathcal{A}$  with configuration space  $\Lambda$ , Initial configuration  $\lambda_0$ , performance metric  $c$ , Configuration budget  $b$

run history  $\mathcal{D}_{\text{Hist}} \leftarrow$  initial design based on  $\lambda_0$ ; //  $\mathcal{D}_{\text{Hist}} = (\lambda, i, c(i, \lambda))_i$

**while**  $b$  remains **do**

$\hat{c} \leftarrow$  train empirical performance model based on run history  $\mathcal{D}_{\text{Hist}}$ ;

$\Lambda_{\text{challengers}} \leftarrow$  select configurations based on  $\hat{c}$ ;

$\hat{\lambda}, \mathcal{D}_{\text{Hist}} \leftarrow$  intensify( $\Lambda_{\text{challengers}}, \hat{\lambda}$ ); // racing and capping

---

## Algorithm 5 SMAC

---

**Input** : instance set  $\mathcal{I}$ , Algorithm  $\mathcal{A}$  with configuration space  $\Lambda$ , Initial configuration  $\lambda_0$ , performance metric  $c$ , Configuration budget  $b$

run history  $\mathcal{D}_{\text{Hist}} \leftarrow$  initial design based on  $\lambda_0$ ; //  $\mathcal{D}_{\text{Hist}} = (\lambda, i, c(i, \lambda))_i$

**while**  $b$  remains **do**

$\hat{c} \leftarrow$  train empirical performance model based on run history  $\mathcal{D}_{\text{Hist}}$ ;

$\Lambda_{\text{challengers}} \leftarrow$  select configurations based on  $\hat{c}$ ;

$\hat{\lambda}, \mathcal{D}_{\text{Hist}} \leftarrow$  intensify( $\Lambda_{\text{challengers}}, \hat{\lambda}$ ); // racing and capping

**return**  $\hat{\lambda}$

---

## Comparisons on $N$ instances [Hutter et al. 2009]

- **Basic(N)** uses a pretty basic comparison:  $better_N(\lambda', \lambda)$ :
  - ▶ Compare  $\lambda'$  and  $\lambda$  based on  $N$  instances



# Comparisons on $N$ instances [Hutter et al. 2009]

- **Basic(N)** uses a pretty basic comparison:  $better_N(\lambda', \lambda)$ :
  - ▶ Compare  $\lambda'$  and  $\lambda$  based on  $N$  instances
  - ▶ How does this relate to cross-validation?

- **Basic( $N$ )** uses a pretty basic comparison:  $better_N(\lambda', \lambda)$ :
  - ▶ Compare  $\lambda'$  and  $\lambda$  based on  $N$  instances
  - ▶ How does this relate to cross-validation?
- Problem: How to set  $N$ ? Problems of large  $N$ ? Small  $N$ ?

- **Basic( $N$ )** uses a pretty basic comparison:  $better_N(\lambda', \lambda)$ :
  - ▶ Compare  $\lambda'$  and  $\lambda$  based on  $N$  instances
  - ▶ How does this relate to cross-validation?
- Problem: How to set  $N$ ? Problems of large  $N$ ? Small  $N$ ?
  - ▶ Problem of large  $N$ : evaluations are slow
  - ▶ Problem of small  $N$ : overfitting to a small set of instances
  - ↪ Tradeoff: Choose  $N$  of moderate size

## Comparisons on $N$ instances [Hutter et al. 2009]

Question: Which  $N$  instances should we use?

- 1  $N$  different instances for each configuration
- 2 The same set of  $N$  instances for the entire run

## Comparisons on $N$ instances [Hutter et al. 2009]

Question: Which  $N$  instances should we use?

- 1  $N$  different instances for each configuration
- 2 The same set of  $N$  instances for the entire run

Answer: the same  $N$  instances, so that we compare apples with apples  
(but: using the same instances can also yield overtuning)

## Comparisons on $N$ instances [Hutter et al. 2009]

Question: Which  $N$  instances should we use?

- 1  $N$  different instances for each configuration
- 2 The same set of  $N$  instances for the entire run

Answer: the same  $N$  instances, so that we compare apples with apples  
(but: using the same instances can also yield overtuning)

If we sampled different instances for each configuration:

- Some configurations would randomly get easier instances
- Those configurations would look better than they really are

Question: For randomized algorithms, how should we set the seeds?

- 1 Sample a new seed for each algorithm run
- 2 Fix the seeds together with the instances

# Comparisons on $N$ instances [Hutter et al. 2009]

Question: For randomized algorithms, how should we set the seeds?

- 1 Sample a new seed for each algorithm run
- 2 Fix the seeds together with the instances

Answer: just like for instances, fix them to compare apples to apples



## Comparisons on $N$ instances [Hutter et al. 2009]

Question: For randomized algorithms, how should we set the seeds?

- 1 Sample a new seed for each algorithm run
- 2 Fix the seeds together with the instances

Answer: just like for instances, fix them to compare apples to apples

In summary, for each run of Basic( $N$ ):

pick  $N$  (instance, seed) pairs and use them for evaluating each  $\lambda$ .

## Comparisons on $N$ instances [Hutter et al. 2009]

Question: For randomized algorithms, how should we set the seeds?

- 1 Sample a new seed for each algorithm run
- 2 Fix the seeds together with the instances

Answer: just like for instances, fix them to compare apples to apples

In summary, for each run of Basic( $N$ ):

pick  $N$  (instance, seed) pairs and use them for evaluating each  $\lambda$ .  
(Different Basic( $N$ ) runs can use different instances and seeds.)

# The concept of overtuning

Very related to overfitting in machine learning

- Performance improves on the training set
- Performance does not improve on the test set, and may even degrade

# The concept of overtuning

Very related to overfitting in machine learning

- Performance improves on the training set
- Performance does not improve on the test set, and may even degrade

More pronounced for heterogeneous benchmark sets

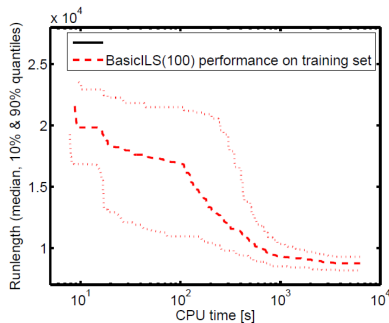
- But it even happens for very homogeneous sets
- Indeed, one can even overfit on a single instance, to the [seeds](#) used for training

# Overtuning Visualized

- Example: minimizing SLS solver runlengths for a single SAT instance
- Training cost, e.g., with  $N=100$ :  
average runlengths across 100 runs with different seeds
- Test cost of  $\hat{\lambda}$  here based on 1000 new seeds

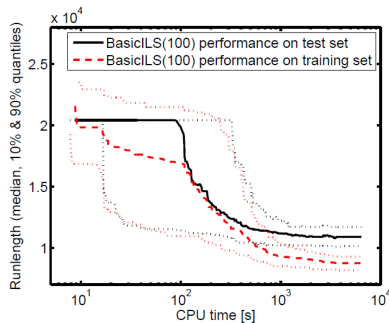
# Overtuning Visualized

- Example: minimizing SLS solver runlengths for a single SAT instance
- Training cost, e.g., with  $N=100$ :  
average runlengths across 100 runs with different seeds
- Test cost of  $\hat{\lambda}$  here based on 1000 new seeds



# Overtuning Visualized

- Example: minimizing SLS solver runlengths for a single SAT instance
- Training cost, e.g., with  $N=100$ :  
average runlengths across 100 runs with different seeds
- Test cost of  $\hat{\lambda}$  here based on 1000 new seeds



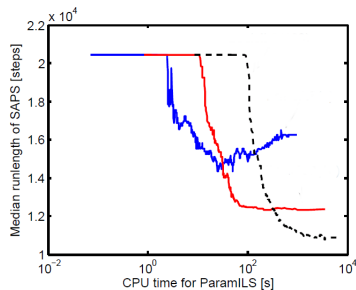
## Basic(N) Test Results with Various N

- Example: minimizing SLS solver runlengths for a single SAT instance
- Training cost, e.g., with  $N=?$ :  
average runlengths across  $N$  runs with different seeds
- Test cost of  $\hat{\lambda}$  here based on 1000 new seeds



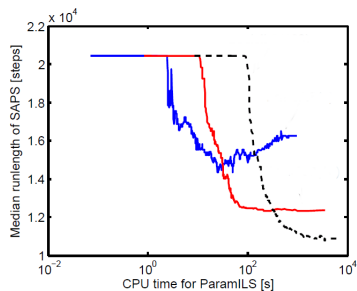
# Basic(N) Test Results with Various N

- Example: minimizing SLS solver runlengths for a single SAT instance
- **Training cost**, e.g., with  $N=?$ :  
average runlengths across  $N$  runs with different seeds
- **Test cost** of  $\hat{\lambda}$  here based on 1000 new seeds



# Basic(N) Test Results with Various N

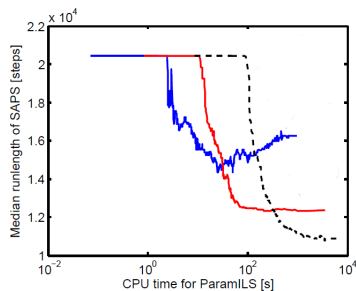
- Example: minimizing SLS solver runlengths for a single SAT instance
- **Training cost**, e.g., with  $N=?$ :  
average runlengths across  $N$  runs with different seeds
- **Test cost** of  $\hat{\lambda}$  here based on 1000 new seeds



Which of these results corresponds to  $N = 1$ ,  
 $N = 10$ , and  $N = 100$ ?

# Basic(N) Test Results with Various N

- Example: minimizing SLS solver runlengths for a single SAT instance
- Training cost, e.g., with  $N=?$ :  
average runlengths across  $N$  runs with different seeds
- Test cost of  $\hat{\lambda}$  here based on 1000 new seeds

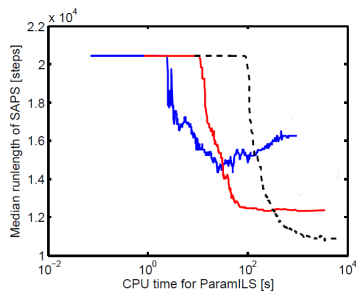


Which of these results corresponds to  $N = 1$ ,  $N = 10$ , and  $N = 100$ ?

- 1  $N=1$ : blue,  $N=10$ : red,  $N=100$  dashed black
- 2  $N=1$ : dashed black,  $N=10$ : red,  $N=100$  blue

# Basic(N) Test Results with Various N

- Example: minimizing SLS solver runlengths for a single SAT instance
- Training cost, e.g., with  $N=?$ :  
average runlengths across  $N$  runs with different seeds
- Test cost of  $\hat{\lambda}$  here based on 1000 new seeds



Which of these results corresponds to  $N = 1$ ,  $N = 10$ , and  $N = 100$ ?

- 1  $N=1$ : blue,  $N=10$ : red,  $N=100$  dashed black
- 2  $N=1$ : dashed black,  $N=10$ : red,  $N=100$  blue

Correct Answer: 1

# Aggressive Racing (inspired by FocusedILS) [Hutter et al. 2009]

Intuition: get the best of both worlds

- Perform more runs for good configurations
  - to avoid overtuning
- Quickly reject poor configurations
  - to make progress more quickly

# Aggressive Racing (inspired by FocusedILS) [Hutter et al. 2009]

Intuition: get the best of both worlds

- Perform more runs for good configurations
  - to avoid overtuning
- Quickly reject poor configurations
  - to make progress more quickly

Definition:  $N(\lambda)$  and  $c_N(\lambda)$

$N(\lambda)$  denotes the number of runs executed for  $\lambda$  so far.

$\hat{c}_N(\lambda)$  denotes the cost estimate of  $\lambda$  based on  $N$  runs.

# Aggressive Racing (inspired by FocusedILS) [Hutter et al. 2009]

Intuition: get the best of both worlds

- Perform more runs for good configurations
  - to avoid overtuning
- Quickly reject poor configurations
  - to make progress more quickly

Definition:  $N(\lambda)$  and  $c_N(\lambda)$

$N(\lambda)$  denotes the number of runs executed for  $\lambda$  so far.

$\hat{c}_N(\lambda)$  denotes the cost estimate of  $\lambda$  based on  $N$  runs.

In the beginning:  $N(\lambda) = 0$  for every configuration  $\lambda$

## Definition: domination

$\lambda^{(1)}$  dominates  $\lambda^{(2)}$  if

- $N(\lambda^{(1)}) \geq N(\lambda^{(2)})$  and
- $\hat{c}_{N(\lambda^{(2)})}(\lambda^{(1)}) \leq \hat{c}_{N(\lambda^{(2)})}(\lambda^{(2)})$ .

I.e.: we have at least as many runs for  $\lambda^{(1)}$  and its cost is at least as low.



# Aggressive Racing (inspired by FocusedILS) [Hutter et al. 2009]

## Definition: domination

$\lambda^{(1)}$  dominates  $\lambda^{(2)}$  if

- $N(\lambda^{(1)}) \geq N(\lambda^{(2)})$  and
- $\hat{c}_{N(\lambda^{(2)})}(\lambda^{(1)}) \leq \hat{c}_{N(\lambda^{(2)})}(\lambda^{(2)})$ .

I.e.: we have at least as many runs for  $\lambda^{(1)}$  and its cost is at least as low.

## *better*( $\lambda', \hat{\lambda}$ ) in a nutshell

- $\hat{\lambda}$  is the current configuration to beat (incumbent)

# Aggressive Racing (inspired by FocusedILS) [Hutter et al. 2009]

## Definition: domination

$\lambda^{(1)}$  dominates  $\lambda^{(2)}$  if

- $N(\lambda^{(1)}) \geq N(\lambda^{(2)})$  and
- $\hat{c}_{N(\lambda^{(2)})}(\lambda^{(1)}) \leq \hat{c}_{N(\lambda^{(2)})}(\lambda^{(2)})$ .

I.e.: we have at least as many runs for  $\lambda^{(1)}$  and its cost is at least as low.

## *better*( $\lambda', \hat{\lambda}$ ) in a nutshell

- $\hat{\lambda}$  is the current configuration to beat (incumbent)
- Perform runs of  $\lambda'$  until either
  - ▶  $\hat{\lambda}$  dominates  $\lambda' \rightsquigarrow$  reject  $\lambda'$ , or
  - ▶  $\lambda'$  dominates  $\hat{\lambda} \rightsquigarrow$  change current incumbent ( $\hat{\lambda} \leftarrow \lambda'$ )

# Aggressive Racing (inspired by FocusedILS) [Hutter et al. 2009]

## Definition: domination

$\lambda^{(1)}$  dominates  $\lambda^{(2)}$  if

- $N(\lambda^{(1)}) \geq N(\lambda^{(2)})$  and
- $\hat{c}_{N(\lambda^{(2)})}(\lambda^{(1)}) \leq \hat{c}_{N(\lambda^{(2)})}(\lambda^{(2)})$ .

I.e.: we have at least as many runs for  $\lambda^{(1)}$  and its cost is at least as low.

## *better*( $\lambda', \hat{\lambda}$ ) in a nutshell

- $\hat{\lambda}$  is the current configuration to beat (incumbent)
- Perform runs of  $\lambda'$  until either
  - ▶  $\hat{\lambda}$  dominates  $\lambda' \rightsquigarrow$  reject  $\lambda'$ , or
  - ▶  $\lambda'$  dominates  $\hat{\lambda} \rightsquigarrow$  change current incumbent ( $\hat{\lambda} \leftarrow \lambda'$ )
- Over time: perform extra runs of  $\hat{\lambda}$  to gain more confidence in it

# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10

# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$			
$\lambda''$			

# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$	2		

# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$	2	10	

# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$	2	10	
$\rightarrow$ reject, since $\hat{c}_2(\lambda') = 6 > \hat{c}_2(\hat{\lambda}) = 2.5$			



# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$	2	10	
$\rightarrow$ reject, since $\hat{c}_2(\lambda') = 6 > \hat{c}_2(\hat{\lambda}) = 2.5$			
$\lambda''$	3		

# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$	2	10	
$\rightarrow$ reject, since $\hat{c}_2(\lambda') = 6 > \hat{c}_2(\hat{\lambda}) = 2.5$			
$\lambda''$	3	1	

# Toy Example

- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$	2	10	
$\rightarrow$ reject, since $\hat{c}_2(\lambda') = 6 > \hat{c}_2(\hat{\lambda}) = 2.5$			
$\lambda''$	3	1	5

# Toy Example

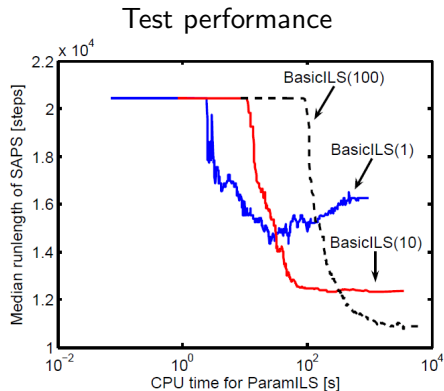
- Let  $\hat{\lambda}$  be the incumbent (evaluated on  $i^{(1)}, i^{(2)}, i^{(3)}$ )
- We'll look at challengers  $\lambda'$  and  $\lambda''$

	$i^{(1)}$	$i^{(2)}$	$i^{(3)}$
$\hat{\lambda}$	3	2	10
$\lambda'$	2	10	
$\rightarrow$ reject, since $\hat{c}_2(\lambda') = 6 > \hat{c}_2(\hat{\lambda}) = 2.5$			
$\lambda''$	3	1	5

- new incumbent:  $\hat{\lambda} \leftarrow \lambda''$
- Perform an additional run for new  $\hat{\lambda}$  to increase confidence over time

# Racing achieves the best of both worlds

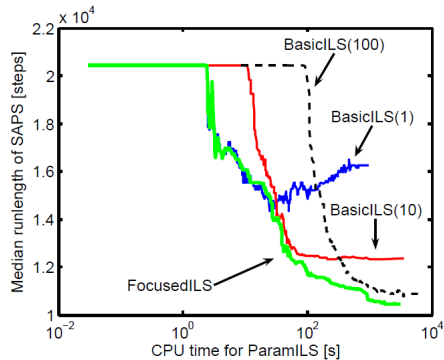
Aggressive racing (aka FocusedILS): Fast progress and no overtuning



# Racing achieves the best of both worlds

Aggressive racing (aka FocusedILS): Fast progress and no overtuning

Test performance



# Overview of Racing

---

**Input** : candidate configurations  $\Lambda_{new}$ , cutoff  $\kappa_{max}$ , previously evaluated runs  $\mathcal{D}_{Hist}$ , budget  $T$ , incumbent  $\hat{\lambda}$   
**while**  $\Lambda_{new}$  *not empty* **do**  
     $\lambda^{(t)} \leftarrow \text{getNext}(\Lambda_{new});$

---

# Overview of Racing

---

**Input** : candidate configurations  $\Lambda_{new}$ , cutoff  $\kappa_{max}$ , previously evaluated runs  $\mathcal{D}_{Hist}$ , budget  $T$ , incumbent  $\hat{\lambda}$

**while**  $\Lambda_{new}$  *not empty* **do**

- $\lambda^{(t)} \leftarrow \text{getNext}(\Lambda_{new});$
- $i, s \leftarrow$  instance and seed drawn uniformly at random;
- $c \leftarrow \text{EvaluateRun}(\hat{\lambda}, i, s, \kappa_{max});$
- $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\hat{\lambda}, i, s, c);$



# Overview of Racing

---

**Input** : candidate configurations  $\Lambda_{new}$ , cutoff  $\kappa_{max}$ , previously evaluated runs  $\mathcal{D}_{Hist}$ , budget  $T$ , incumbent  $\hat{\lambda}$

**while**  $\Lambda_{new}$  *not empty* **do**

- $\lambda^{(t)} \leftarrow \text{getNext}(\Lambda_{new});$
- $i, s \leftarrow$  instance and seed drawn uniformly at random;
- $c \leftarrow \text{EvaluateRun}(\hat{\lambda}, i, s, \kappa_{max});$
- $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\hat{\lambda}, i, s, c);$
- while** *true* **do**
  - $\mathcal{I}^+, \mathbf{s}^+ \leftarrow \text{getAlreadyEvaluatedOn}(\hat{\lambda}, \mathcal{D}_{Hist});$
  - $\mathcal{I}^{(t)}, \mathbf{s}^{(t)} \leftarrow \text{getAlreadyEvaluatedOn}(\lambda^{(t)}, \mathcal{D}_{Hist});$
  - $i^{(t)}, s^{(t)} \leftarrow$  drawn uniformly at random from  $\mathcal{I}^+ \setminus \mathcal{I}^{(t)}$  and  $\mathbf{s}^+ \setminus \mathbf{s}^{(t)};$

# Overview of Racing

---

**Input** : candidate configurations  $\Lambda_{new}$ , cutoff  $\kappa_{max}$ , previously evaluated runs  $\mathcal{D}_{Hist}$ , budget  $T$ , incumbent  $\hat{\lambda}$

**while**  $\Lambda_{new}$  not empty **do**

$\lambda^{(t)} \leftarrow \text{getNext}(\Lambda_{new});$

$i, s \leftarrow$  instance and seed drawn uniformly at random;

$c \leftarrow \text{EvaluateRun}(\hat{\lambda}, i, s, \kappa_{max});$

$\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\hat{\lambda}, i, s, c);$

**while** true **do**

$\mathcal{I}^+, s^+ \leftarrow \text{getAlreadyEvaluatedOn}(\hat{\lambda}, \mathcal{D}_{Hist});$

$\mathcal{I}^{(t)}, s^{(t)} \leftarrow \text{getAlreadyEvaluatedOn}(\lambda^{(t)}, \mathcal{D}_{Hist});$

$i^{(t)}, s^{(t)} \leftarrow$  drawn uniformly at random from  $\mathcal{I}^+ \setminus \mathcal{I}^{(t)}$  and  $s^+ \setminus s^{(t)};$

$c_i \leftarrow \text{EvaluateRun}(\lambda^{(t)}, i^{(t)}, s^{(t)}, \kappa_{max});$

$\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\lambda^{(t)}, i^{(t)}, s^{(t)}, c^{(t)});$

# Overview of Racing

---

**Input** : candidate configurations  $\Lambda_{new}$ , cutoff  $\kappa_{max}$ , previously evaluated runs  $\mathcal{D}_{Hist}$ , budget  $T$ , incumbent  $\hat{\lambda}$

**while**  $\Lambda_{new}$  *not empty* **do**

- $\lambda^{(t)} \leftarrow \text{getNext}(\Lambda_{new});$
- $i, s \leftarrow$  instance and seed drawn uniformly at random;
- $c \leftarrow \text{EvaluateRun}(\hat{\lambda}, i, s, \kappa_{max});$
- $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\hat{\lambda}, i, s, c);$
- while** *true* **do**
  - $\mathcal{I}^+, s^+ \leftarrow \text{getAlreadyEvaluatedOn}(\hat{\lambda}, \mathcal{D}_{Hist});$
  - $\mathcal{I}^{(t)}, s^{(t)} \leftarrow \text{getAlreadyEvaluatedOn}(\lambda^{(t)}, \mathcal{D}_{Hist});$
  - $i^{(t)}, s^{(t)} \leftarrow$  drawn uniformly at random from  $\mathcal{I}^+ \setminus \mathcal{I}^{(t)}$  and  $s^+ \setminus s^{(t)};$
  - $c_i \leftarrow \text{EvaluateRun}(\lambda^{(t)}, i^{(t)}, s^{(t)}, \kappa_{max});$
  - $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\lambda^{(t)}, i^{(t)}, s^{(t)}, c^{(t)});$
  - if** *average cost of  $\lambda^{(t)}$  > average cost of  $\hat{\lambda}$  across  $\mathcal{I}^{(t)}$  and  $s^{(t)}$*  **then**
    - $\perp$  break;

# Overview of Racing

---

**Input** : candidate configurations  $\Lambda_{new}$ , cutoff  $\kappa_{max}$ , previously evaluated runs  $\mathcal{D}_{Hist}$ , budget  $T$ , incumbent  $\hat{\lambda}$

**while**  $\Lambda_{new}$  *not empty* **do**

- $\lambda^{(t)} \leftarrow \text{getNext}(\Lambda_{new});$
- $i, s \leftarrow$  instance and seed drawn uniformly at random;
- $c \leftarrow \text{EvaluateRun}(\hat{\lambda}, i, s, \kappa_{max});$
- $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\hat{\lambda}, i, s, c);$
- while** *true* **do**
  - $\mathcal{I}^+, s^+ \leftarrow \text{getAlreadyEvaluatedOn}(\hat{\lambda}, \mathcal{D}_{Hist});$
  - $\mathcal{I}^{(t)}, s^{(t)} \leftarrow \text{getAlreadyEvaluatedOn}(\lambda^{(t)}, \mathcal{D}_{Hist});$
  - $i^{(t)}, s^{(t)} \leftarrow$  drawn uniformly at random from  $\mathcal{I}^+ \setminus \mathcal{I}^{(t)}$  and  $s^+ \setminus s^{(t)};$
  - $c_i \leftarrow \text{EvaluateRun}(\lambda^{(t)}, i^{(t)}, s^{(t)}, \kappa_{max});$
  - $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\lambda^{(t)}, i^{(t)}, s^{(t)}, c^{(t)});$
  - if** *average cost of  $\lambda^{(t)}$  > average cost of  $\hat{\lambda}$  across  $\mathcal{I}^{(t)}$  and  $s^{(t)}$*  **then**
    - $\perp$  break;
  - else if** *average cost of  $\lambda^{(t)}$  < average cost of  $\hat{\lambda}$  and  $\mathcal{I}^+ = \mathcal{I}^{(t)}$  and  $s^+ = s^{(t)}$*  **then**
    - $\perp \hat{\lambda} \leftarrow \lambda^{(t)};$

# Overview of Racing

---

**Input** : candidate configurations  $\Lambda_{new}$ , cutoff  $\kappa_{max}$ , previously evaluated runs  $\mathcal{D}_{Hist}$ , budget  $T$ , incumbent  $\hat{\lambda}$

**while**  $\Lambda_{new}$  *not empty* **do**

- $\lambda^{(t)} \leftarrow \text{getNext}(\Lambda_{new});$
- $i, s \leftarrow$  instance and seed drawn uniformly at random;
- $c \leftarrow \text{EvaluateRun}(\hat{\lambda}, i, s, \kappa_{max});$
- $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\hat{\lambda}, i, s, c);$
- while** *true* **do**
  - $\mathcal{I}^+, s^+ \leftarrow \text{getAlreadyEvaluatedOn}(\hat{\lambda}, \mathcal{D}_{Hist});$
  - $\mathcal{I}^{(t)}, s^{(t)} \leftarrow \text{getAlreadyEvaluatedOn}(\lambda^{(t)}, \mathcal{D}_{Hist});$
  - $i^{(t)}, s^{(t)} \leftarrow$  drawn uniformly at random from  $\mathcal{I}^+ \setminus \mathcal{I}^{(t)}$  and  $s^+ \setminus s^{(t)};$
  - $c_i \leftarrow \text{EvaluateRun}(\lambda^{(t)}, i^{(t)}, s^{(t)}, \kappa_{max});$
  - $\mathcal{D}_{Hist} \leftarrow \mathcal{D}_{Hist} \cup (\lambda^{(t)}, i^{(t)}, s^{(t)}, c^{(t)});$
  - if** *average cost of  $\lambda^{(t)}$  > average cost of  $\hat{\lambda}$  across  $\mathcal{I}^{(t)}$  and  $s^{(t)}$*  **then**
    - $\perp$  break;
  - else if** *average cost of  $\lambda^{(t)}$  < average cost of  $\hat{\lambda}$  and  $\mathcal{I}^+ = \mathcal{I}^{(t)}$  and  $s^+ = s^{(t)}$*  **then**
    - $\perp \hat{\lambda} \leftarrow \lambda^{(t)};$

**if** *time spent exceeds  $T$  or  $\Lambda_{new}$  is empty* **then**

- $\perp$  **return**  $\hat{\lambda}, \mathcal{D}_{Hist}$