

CS3243 Tutorial 1

Eric Han

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Eric Han

4th Year PhD Student

- I cannot be there due to National Service commitments; I will save the rest of the introductions for the next week.
- Today's tutorial will be covered by the relief tutor.
- Feel free to telegram me @Eric_Vader/on our group, if you have any concerns.

Expectations

Expectations of you

1. Fill the seats from the front.
2. Come prepared to the Tutorial.
 - 2.1 You will be asked at random to discuss your answer.
3. Refrain from taking pictures of the slides.
 - 3.1 Learn to take good notes.
 - 3.2 The slides will *not* be distributed.
4. Try to be on time.

Any comments or suggestions for the lessons going forward?

Question 1 - Recap

- **Fully / Partially Observable:** Is the complete state of the environment accessible to the agent's sensors
- **Single / Multi-Agent:** Are there more than one actor in the environment? (competitive vs cooperative)
- **Deterministic / Stochastic:** Is the next state determined by the current state and action by the agent?
- **Episodic / Sequential:** Is the next episode dependent on the action taken previously?
- **Static / Dynamic:** Can the environment change while the agent is deliberating?
- **Discrete / Continuous:** Is the state of the environment discretized or varying continuously?

Easiest: Fully, Single, Deterministic, Episodic, Static

Question 1a

Determine the properties of the above problem from the perspective of an intelligent agent planning a solution. Complete the table below.

Question 1a - Answer

Environment Characteristic	Sudoku Puzzle Generation
Fully / Partially Observable	Fully Observable
Single / Multi-Agent	Single agent
Deterministic / Stochastic	Deterministic
Episodic / Sequential	Episodic / Sequential
Static / Dynamic	Static
Discrete / Continuous	Discrete

Explanation on Episodic / Sequential: Depending on the environment formulation, the next episode is dependent on the previous action.

Question 1b

Define the search space for the problem of generating a Sudoku Puzzle by completing the following.

- Give the representation of a state in this problem.
- Using the state representation defined above, specify the initial state and goal state(s).
- Define its actions.
- Using the state representation and actions defined above, specify the transition function T . (In other words, when each of the actions defined above is applied to a current state, what is the resulting state?).

Question 1b - Answer

Sample Environment Formulation:

- **State Space:** $A \in \{0, \dots, 9\}^{9 \times 9}$ where 0 is blank
- **Initial State:** A valid Sudoku Puzzle, completely filled without 0.
- **Final State:** A goal state is $T \in \{0, 1, \dots\}$ steps away from the initial state.
- **Action:** Removing the value $a \in \{1, \dots, 9\}$ at (i, j) in A
- **Transition Model:** $A - E_{i,j}(a)$, where $E_{i,j}(a)$ is zeros everywhere but a at (i, j)

Sample: There is no right answer, there are several correct representations; as long as requirements are fulfilled.

Question 2a

Recap

AIMA Chapter 3, on graph search and tree-like search.

Question

Describe the difference between Tree Search and Graph Search algorithms.

Question 2a

Recap

AIMA Chapter 3, on graph search and tree-like search.

Question

Describe the difference between Tree Search and Graph Search algorithms.

Answer

Graph search will not explore redundant paths, only exploring:

1. unvisited states
2. visited states, but via less than optimal paths

Tree search will explore all paths, including redundant paths.

Question 2b

Recap

Revise DFS and BFS algorithms.

Question

- i. Depth-First Search with tree-based implementation
- ii. Depth-First Search with graph-based implementation
- iii. Breadth-First Search with tree-based implementation
- iv. Breadth-First Search with graph-based implementation

Question 2b

Recap

Revise DFS and BFS algorithms.

Question

- i. Depth-First Search with tree-based implementation
- ii. Depth-First Search with graph-based implementation
- iii. Breadth-First Search with tree-based implementation
- iv. Breadth-First Search with graph-based implementation

Answer

- i. S-C-E-D-B-E-D-D-A-F-G
- ii. S-C-E-D-B-A-F-G
- iii. S-B-C-A-D-E-E-F-D-D-G
- iv. S-B-C-A-D-E-F-G

Bonus Qn: Which implementation is typically used in practice?

Question 3

Recap

AIMA Chapter 3, on uniform search

Question

Prove that the **Uniform-Cost Search** algorithm is optimal as long as each action cost exceeds some small positive constant ϵ .

Question 3 - Answer

Given that $\text{cost } \ell(a, b) > \epsilon$ between 2 nodes a and b , Invariant hypothesis: For each visited node, $g(u)$ is the least cost from the source s to u .

Base case: When there is one visited node, its trivially true.

Assuming the hypothesis to be true, for all $u \in U$ visited nodes, $g(u)$ is with the least cost. For any V frontier nodes that is unvisited, we choose v where $\ell(u, v)$ is smallest; The cost to v is $g(v) = g(u) + \ell(u, v)$. Assume that $g(v)$ is not the least cost, then there will be a shorter path through some other node w . If w is visited then $g(u)$ must go through w , which contradicts. If w is unvisited, then $\ell(u, w) < \ell(u, v)$ which contradicts as w would have been chosen first.

Hence, if $\text{cost } \ell(a, b) > \epsilon$, $g(.)$ is the optimal cost to the source.

Question 4

Formulate the above as a search problem. More specifically, define the following:

- State representation
- Initial state
- Actions
- Transition model
- Step cost
- Goal test

Recap

Question 1b.

Question 4 - Answer

There is no right answer, but minimally:

- **State representation:** describes how pieces are
 - connected to the neighbours
 - represented
- **Initial state:** representation varies but must not have any initial connections.
- **Actions:** considers that legal connections, ie. you cannot simply take any two puzzle pieces.
- **Transition model:** Correctly mutates the current state that maintains semantics.
- **Step cost:** step cost is any positive, non-zero number.
- **Goal test:** checks must consider pieces with 2/3/4 sides are correctly connected.

Absolute positioning is acceptable, but the solution *must* consider orientation.

Question 5

Recap

Question 2b.

Question

Determine the final path found from the start (S) to the goal (G)?

Question 5

Recap

Question 2b.

Question

Determine the final path found from the start (S) to the goal (G)?

Answer

S-B-F-H-D-G