

$$\nabla^2 = \nabla \cdot \nabla = \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$$

$$(\nabla^2) f = \partial_x^2 f + \partial_y^2 f + \partial_z^2 f$$

$$\nabla \cdot (\nabla f) = \partial_x^2 f + \partial_y^2 f + \partial_z^2 f$$

$$\nabla^2 = \nabla \cdot \nabla = \frac{2}{r} \frac{\partial}{\partial r} + \frac{1}{r^2 \tan(\theta)} \frac{\partial}{\partial \theta} + \frac{\partial^2}{\partial r^2} + r^{-2} \frac{\partial^2}{\partial \theta^2} + \frac{1}{r^2 \sin^2(\theta)} \frac{\partial^2}{\partial \phi^2}$$

$$(\nabla^2) f = \frac{1}{r^2} \left(r^2 \partial_r^2 f + 2r \partial_r f + \partial_\theta^2 f + \frac{\partial_\theta f}{\tan(\theta)} + \frac{\partial_\phi^2 f}{\sin^2(\theta)} \right)$$

$$\nabla \cdot (\nabla f) = \frac{1}{r^2} \left(r^2 \partial_r^2 f + 2r \partial_r f + \partial_\theta^2 f + \frac{\partial_\theta f}{\tan(\theta)} + \frac{\partial_\phi^2 f}{\sin^2(\theta)} \right)$$

$$\left[\boldsymbol{e}_x \frac{\partial}{\partial x} + \boldsymbol{e}_y \frac{\partial}{\partial y} + \boldsymbol{e}_z \frac{\partial}{\partial z}, \right. \\ \left. \boldsymbol{e}_x \frac{\partial}{\partial x} + \boldsymbol{e}_y \frac{\partial}{\partial y} + \boldsymbol{e}_z \frac{\partial}{\partial z} \right]$$

$$F$$

$$F^r \boldsymbol{e}_r + F^\theta \boldsymbol{e}_\theta + F^\phi \boldsymbol{e}_\phi$$

$$F$$

$$\begin{aligned} \nabla \cdot (\nabla f) = & F^r \boldsymbol{e}_r \\ & + F^\theta \boldsymbol{e}_\theta \\ & + F^\phi \boldsymbol{e}_\phi \end{aligned}$$

$$F$$

$$\left(\begin{array}{l} F^r \boldsymbol{e}_r \\ + F^\theta \boldsymbol{e}_\theta \\ + F^\phi \boldsymbol{e}_\phi \\ F^r \boldsymbol{e}_r \\ + F^\theta \boldsymbol{e}_\theta \\ + F^\phi \boldsymbol{e}_\phi \end{array} \right)$$