

the mathematical model for one metronome results:

$$m \left( l \ddot{\theta} + g \sin \theta + \cos \theta \ddot{x} \right) + m l \in \left( \left( \frac{\theta}{\theta_0} \right)^2 - 1 \right) \dot{\theta} = 0$$

for the eq for 4 metronomes

$$m \left( l_1 \ddot{\theta}_1 + g \sin \theta_1 + \cos \theta_1 \ddot{x} \right) + m l_1 \in \left( \left( \frac{\theta_1}{\theta_{10}} \right)^2 - 1 \right) \dot{\theta}_1 = 0$$

$$m \left( l_2 \ddot{\theta}_2 + g \sin \theta_2 + \cos \theta_2 \ddot{x} \right) + m l_2 \in \left( \left( \frac{\theta_2}{\theta_{20}} \right)^2 - 1 \right) \dot{\theta}_2 = 0$$

$$m \left( l_3 \ddot{\theta}_3 + g \sin \theta_3 + \cos \theta_3 \ddot{x} \right) + m l_3 \in \left( \left( \frac{\theta_3}{\theta_{30}} \right)^2 - 1 \right) \dot{\theta}_3 = 0$$

$$m \left( l_4 \ddot{\theta}_4 + g \sin \theta_4 + \cos \theta_4 \ddot{x} \right) + m l_4 \in \left( \left( \frac{\theta_4}{\theta_{40}} \right)^2 - 1 \right) \dot{\theta}_4 = 0$$

$$\ddot{x} \left( M + 4mr \right) + \sum_i^4 m l_i \left( \cos \theta_i \ddot{\theta}_i - \sin \theta_i \dot{\theta}_i^2 \right) = 0$$

$$M(q) \ddot{q} + C(q, \dot{q}) \dot{q} + G(q) = \tau$$

$$M(q) = \begin{bmatrix} I_1 & 0 & 0 & 0 & m l_1 \cos \theta_1 \\ 0 & I_2 & 0 & 0 & m l_2 \cos \theta_2 \\ 0 & 0 & I_3 & 0 & m l_3 \cos \theta_3 \\ 0 & 0 & 0 & I_4 & m l_4 \cos \theta_4 \\ m l_1 \cos \theta_1 & m l_2 \cos \theta_2 & m l_3 \cos \theta_3 & m l_4 \cos \theta_4 & M + 4m \end{bmatrix}$$

$$S_i = \left( \left( \frac{\theta_i}{\theta_{i0}} \right)^2 - 1 \right) m_i l_i^2$$

$$C = \begin{bmatrix} S_1 & 0 & 0 & 0 & 0 \\ 0 & S_2 & 0 & 0 & 0 \\ 0 & 0 & S_3 & 0 & 0 \\ 0 & 0 & 0 & S_4 & 0 \\ R_1 & R_2 & R_3 & R_4 & 0 \end{bmatrix}$$

$$R_i = m_i \dot{\theta}_i l_i \sin \theta_i$$

$$G = \begin{bmatrix} m g l_1 \sin \theta_1 \\ m g l_2 \sin \theta_2 \\ m g l_3 \sin \theta_3 \\ m g l_4 \sin \theta_4 \\ 0 \end{bmatrix}$$