## Output

You should output two integers to tell us who the winner is:

- 1. The group the winner was initially in.
- 2. The number of the winner in the group.

For example, the winner was in the  $1^{st}$  group, and was the  $3^{rd}$  pirate in the group, output 1 3.

# Example 1

stdin	stdout
5 2	3 4
6 3	
7 4	
10 3	
3 2	
5 2	

stdin	stdout
7 3	4 3
10 2	
5 3	
4 3	
5 2	
12 4	
21 10	
8 3	

# Problem E. The Museum's Security Grid

Input file: stdin
Output file: stdout

Time limit: 500 milliseconds

Memory limit: 64 MB

The prestigious National Museum of Technology operates a high-tech security system based on an  $m \times n$  grid of laser sensors. Each sensor has a **unique** power level used to detect intruders. However, the chief security officer has noticed that the power levels are unnecessarily high, leading to excessive energy consumption.

To optimize energy efficiency, the power levels must be reconfigured while preserving the system's effectiveness. The new configuration must satisfy the following conditions:

- If a sensor originally had a higher power level than another sensor in the **same row or column**, it must remain more powerful in the new configuration.
- The highest power level in the new configuration must be as low as possible.

As the museum's security consultant, your task is to determine the optimal power levels for each sensor in the grid while ensuring that the conditions above are met.

## Input

Line 1 contains two integers m and n, denoting the number of rows and columns in security grid.

The next m lines each contain n space-separated integers representing the power levels of the sensors in the grid and denote the power levels of the sensors as p. Each power level in the initial configuration is unique.

- $1 \le m, n \le 1000$
- 1
- p is unique
- $m \cdot n < 10^5$

## Output

Output m lines, each containing n space-separated integers, representing the reconfigured security grid.

# Example 1

# Explanation

The original grid is:

#### Programming Design and Optimization 2025 Information Management, National Taiwan University, Saturday, April 19th, 2025

stdin	stdout
2 2	2 1
3 1	1 2
2 5	

$$\begin{bmatrix} 3 & 1 \\ 2 & 5 \end{bmatrix}$$

After reconfiguration, the new grid is:

$$\begin{bmatrix} 2 & 1 \\ 1 & 2 \end{bmatrix}$$

The maximum power level in this new grid is 5, and it can be shown that no smaller power level configuration satisfies the conditions.

## Example 2

stdin	stdout
1 1	1
10	

# Explanation

Since there is only one sensor, it must be assigned the minimum power level of 1.

## Problem F. The Ancient Formula

Input file: stdin
Output file: stdout
Time limit: 1 second
Memory limit: 64 MB

In an archaeological dig, Dr. Yee uncovered a collection of ancient tablets that contained strange chemical formulas written in an old script. After careful translation by his research team, the formulas were finally decoded.

As a modern chemist, Dr. Yee recognized some of the symbols as elements, but the structure seemed unusual. Was this an early attempt at chemical notation, or could it represent something valuable?

Upon further investigation, Dr. Yee noticed that some of the formulas appeared similar to those in his notes. However, the ancient formulas used parentheses and had different groupings, raising the question: Could they be describing the same compound, just with a different notation system?

Can you help Dr. Yee verify whether the ancient formula matches the modern one?

## Input

Line 1 contains two integers  $n_1$  and  $n_2$ , denoting the length of following two formulas.

Line 2 - 3 each contains a string represents ancient and modern formula respectively.

A formula follows these rules:

- An atom is denoted as a uppercase letter and may followed by a lowercase letter.
- An element can be a group of atoms, elements, or both.
- Digits (ranging from 1 to 100) following an atom or element indicate the quantity. If no digit is present, the quantity is assumed to be 1.
- Parentheses are used to group elements and can be followed by a number, indicating how many times the group should be repeated.
- Parentheses may be used to group elements, with a maximum nesting depth of 10.
- The number of every atom in each formula will not exceed  $10^4$ .
- $1 \le n_1, n_2 \le 10^4$

Note: The atoms and elements in these formulas may not necessarily exist on Earth, as Dr. Yee lives in a different universe.

## Output

Two formulas are considered to represent the same compound if they contain exactly the same atoms in identical quantities, regardless of how they are grouped. Therefore, the output will be either "Yes" or "No".

#### Example 1

stdin	stdout
10 8	No
(X3(OR)2)3	
X8(OR2)3	

## Explanation

Expanding the formulas:

- (X3(OR)2)3 expands as:
  - X3 is repeated 3 times  $\rightarrow$  X9
  - (OR) 2 expands to O2R2, and repeating this 3 times gives O6R6.

So, the full expansion is X906R6.

- X8(OR2)3 expands as:
  - X8 remains as is.
  - (OR2)3 expands to O3R6.

So, the full expansion is X803R6.

Since the number of atoms does not match, the two formulas represent different compounds.

## Example 2

stdin	stdout
9 15	Yes
S02(ORe)4	
(ORe)2S(ORe)2O2	

## Explanation

Expanding both formulas:

- S02(ORe)4 expands to S106Re4.
- (ORe)2S(ORe)2O2 expands to S106Re4.

Since both formulas contain the same elements in the same quantities, they represent the same compound.

# Problem G. Magic Potion Battle

Input file: stdin
Output file: stdout

Time limit: 500 milliseconds

Memory limit: 64 MB

In the dark ages of wizardry, the legendary sorcerers Merlin and Morgana engaged in a fierce **Magic Potion Battle**. In this battle, they took turns casting spells to destroy potion bottles infused with magical essence.

The game follows these rules:

- Merlin and Morgana take turns destroying exactly one potion bottle per turn.
- Merlin always plays first.
- The game ends immediately if the total amount of magical essence destroyed becomes divisible by 3. The player who made that move loses.
- If all potions are destroyed and the total essence is **not divisible by 3**, Morgana **automatically wins**.

Both players play **optimally**, meaning they make the best possible moves to maximize their chances of winning.

Your task is to determine whether Merlin can guarantee a win, or if Morgana will inevitably win. Print "true" if Merlin wins and "false" if Morgana wins.

#### Input

Line 1 contains a single integer n ( $1 \le n \le 100000$ ), representing the number of potion bottles.

Line 2 contains n space-separated integers, where the  $i^{th}$  integer represents the magical essence in the  $i^{th}$  potion bottle. Each integer k satisfies  $1 \le k \le 10000$ .

# Output

Print "Yes" if Merlin can force a win; otherwise, print "No".

stdin	stdout
2	Yes
2 1	

#### **Explanation**

The game proceeds as follows:

- Turn 1: Merlin removes either potion bottle.
- Turn 2: Morgana removes the remaining bottle.

The sum of the destroyed potion bottles is 2 + 1 = 3, which is divisible by 3. Since Morgana made the move that resulted in this, she **loses**, and Merlin wins.

## Example 2

stdin	stdout
5	No
5 1 2 4 3	

## **Explanation**

One possible sequence of moves for Morgana to win:

- **Turn 1:** Merlin removes the potion with value 1. Sum = 1.
- Turn 2: Morgana removes the potion with value 3. Sum = 1 + 3 = 4.
- Turn 3: Merlin removes the potion with value 4. Sum = 1 + 3 + 4 = 8.
- Turn 4: Morgana removes the potion with value 2. Sum = 1 + 3 + 4 + 2 = 10.
- Turn 5: Merlin removes the potion with value 5. Sum = 1 + 3 + 4 + 2 + 5 = 15.

Since 15 is divisible by 3, Merlin loses, meaning Morgana wins. Thus, the output is "No".

# Problem H. Ingenious Missions

Input file: stdin
Output file: stdout
Time limit: 1 second
Memory limit: 64 MB

You are the mastermind behind a covert operations unit tasked with executing high-stakes missions. Your team has a fixed number of agents and a list of m planned missions.

Your goal is to select a subset of missions to achieve at least a total benefit of r while using at most n agents in total.

Each mission has specific requirements:

- A mission requires a certain number of agents and yields a corresponding benefit.
- Each mission can be executed at most once.
- Each agent can be assigned to at most one mission.

The order in which missions are selected does not matter; only the set of missions chosen determines the outcome.

## Input

Line 1 contains three integers n, r, m, denoting the number of agents available, the minimum required benefit, and the number of missions, respectively.

The next m lines each contain two integers g and b, denoting the **agents required to execute** the mission, the benefit received from the mission, respectively.

- 1 < n, r, m < 100
- $1 \le g, b \le 100$

## Output

Print a single integer, the total number of valid mission schemes modulo  $10^9 + 7$ .

stdin	stdout
5 3 3	5
2 2	
2 3	
1 1	

## Explanation

There are 3 missions:

- Mission 0: Requires 2 agents, yields a benefit of 2.
- Mission 1: Requires 2 agents, yields a benefit of 3.
- Mission 2: Requires 1 agent, yields a benefit of 1.

Your objective is to achieve at least a total benefit of 3, using at most 5 agents. Possible valid schemes:

#### 1. Select Mission 1 only:

- Agents used: 2, total benefit: 3.
- Valid.

#### 2. Select Missions 0 and 1:

- Agents used: 4, total benefit: 5.
- Valid.

#### 3. Select Missions 1 and 2:

- Agents used: 3, total benefit: 4.
- Valid.

#### 4. Select Missions 0 and 2:

- Agents used: 3, total benefit: 3.
- Valid.

#### 5. Select Missions 0, 1, and 2:

- Agents used: 5, total benefit: 6.
- Valid.

#### Invalid schemes:

- 1. Select Mission 0 only: Agents used = 2, total benefit = 2.
  - Invalid (benefit < 3).
- 2. Select Mission 2 only: Agents used = 1, total benefit = 1.
  - Invalid (benefit < 3).

In conclusion, there are 5 valid schemes. The output is:

 $\mathbf{5}$ 

**Side Note:** A scheme where no missions are selected is always invalid, as it yields no benefit.

# Problem I. Block Builder's Challenge: The Rainfall Simulator

Input file: stdin
Output file: stdout
Time limit: 1 second
Memory limit: 64 MB

In the popular game "Block Builder's Challenge", players design landscapes using cubic blocks arranged in a grid. After completing a creation, the game enters the "Rainfall Simulation" phase, where water falls from the sky and fills the terrain's low points. The objective is to calculate how much water is trapped within the block structure.

Your task is to determine the **total volume of trapped water** after rainfall, following these rules:

- The landscape is represented as an  $m \times n$  grid.
- Each grid cell contains a non-negative integer representing the height of a block.
- Water flows downward and seeks the lowest available space.
- Water can only flow horizontally or vertically (not diagonally).
- Water can escape if it reaches the edges of the grid.
- One unit of water fills one cubic unit of space.

#### Input

Line 1 contains two integers m and n, representing the grid dimensions.

The next m lines contain n space-separated integers, where each integer represents the height of a block. The constraints are:

- $1 \le m, n \le 200$
- $0 < \text{height} < 10^4$

## Output

Print a single integer, the total volume of water (in cubic units) that is trapped after rainfall.

## Example 1

stdin	stdout
3 6	4
1 4 3 1 3 2	
3 2 1 3 2 4	
2 3 3 2 3 1	

## Explanation

After the rainfall:

- Water collects in low areas but can escape at the edges.
- The total trapped water volume is 4 cubic units.

# Example 2

stdin	stdout
5 5	10
3 3 3 3 3	
3 2 2 2 3	
3 2 1 2 3	
3 2 2 2 3	
3 3 3 3 3	

## Explanation

This terrain forms a **closed basin** with walls of height 3:

- Water fills up to level 3 inside the basin.
- The total volume of trapped water is  ${f 10}$  cubic units.

# Problem J. The Interplanetary Network

Input file: stdin
Output file: stdout
Time limit: 1 second
Memory limit: 64 MB

The year is 2184, and humanity has successfully colonized multiple planets in the solar system. The Interplanetary Communication Network (ICN) consists of N space stations connected by M bidirectional communication channels. Each channel has a specific bandwidth capacity.

The ICN Administration seeks to establish a **minimum-cost network** that connects all space stations while ensuring its reliability. However, given the harsh space environment and potential meteor strikes, they must classify the communication channels into two types:

- Critical Channels: If any of these channels are damaged, the total cost of maintaining a connected network will increase.
- Backup-Ready Channels: These channels can be seamlessly integrated into a minimum-cost network if a critical channel fails, without increasing the total cost.

Your task is to:

- Identify all **critical channels** that, if damaged, would increase the minimum network maintenance cost.
- Identify all **backup-ready channels** that can replace critical channels without increasing the total cost.

## Input

Line 1 contains two integers N and M, denoting the number of space stations and communication channels:

$$2 \le N \le 100, \quad 1 \le M \le \min(200, \frac{N(N-1)}{2}).$$

The next M lines each contain three integers u, v, w, representing a communication channel:

- u and v are space stations connected by the channel  $(0 \le u, v < N)$ .
- w is the bandwidth capacity of the channel  $(1 \le w \le 1000)$ .
- Each channel connects **two distinct** space stations.
- There is at most **one direct channel** between any pair of stations.
- All space stations are **initially connected** through at least one path.

## Output

The output consists of two lines:

- The first line contains the set of **critical channels** (space-separated indices).
- The second line contains the set of backup-ready channels (space-separated indices).
- If either set is empty, print no channels for that line.

# Example 1

stdin	stdout
5 7	0 1
0 1 1	2 3 4 5
1 2 1	
2 3 2	
0 3 2	
0 4 3	
3 4 3	
1 4 6	

#### Explanation

The minimum-cost network has a total maintenance cost of 7 units.

- Channels 0 and 1 are critical because removing either would increase the minimum network cost.
- Channels 2, 3, 4, and 5 are backup-ready since they can replace a critical channel without increasing the cost.

stdin	stdout
4 4	no channels
0 1 1	0 1 2 3
1 2 1	
2 3 1	
0 3 1	

## Problem K. NTU Class Picking

Input file: stdin
Output file: stdout
Time limit: 1 second
Memory limit: 64 MB

At NTU, students must use an online system to register for their classes each semester. However, the system has a significant limitation: students cannot insert a class between existing ones directly. Instead, they must manually shift other classes to make space.

The rules for class selection are as follows:

- Classes are arranged in a sequential order, with each class occupying a unique position.
- To insert a class at position P, all existing classes at position P and beyond must be shifted down by one position.
- To delete a class at position P, the position remains empty, leaving a gap.
- Each move consists of shifting a class exactly one position up or down.

Given a sequence of insertion and deletion commands, determine the minimum number of moves required to achieve the final class arrangement.

#### Input

Line 1 contains an integer N ( $1 \le N \le 1000$ ), denoting the number of operations.

Next N lines, each contains a command:

- I P  $\rightarrow$  Insert a class at position P (1 < P < 1000).
- **D** P  $\rightarrow$  Delete a class at position P ( $1 \le P \le 1000$ ).

## Output

Print a single integer, the minimum number of moves required to execute all operations.

## Example 1

## Explanation

- 1. Insert class at **position**  $1 \to \{\underline{A}\}$ .
- 2. Insert class at **position 2**  $\rightarrow$  { $A, \underline{B}$ }.
- 3. Insert class at **position 3**  $\rightarrow$  {A, B, C}.
- 4. Insert class at **position 1**: Shift A, B, C down by  $1 \{\underline{D}, A, B, C\}$  (3 moves).
- 5. Delete class at **position**  $1 \to \{A, B, C\}$  (removal itself is not counted).

Total moves: 8.

stdin	stdout
5	8
I 1	
I 2	
I 3	
I 1	
D 1	

## Example 2

stdin	stdout
5	6
I 1	
I 2	
I 3	
D 2	
I 1	

## Explanation

- 1. Insert class at **position**  $1 \to \{\underline{A}\}$ .
- 2. Insert class at **position 2**  $\rightarrow$  { $A, \underline{B}$ }.
- 3. Insert class at **position 3**  $\rightarrow$  { $A, B, \underline{C}$ }.
- 4. Delete class at **position 2**  $\rightarrow$  { $A, \_, C$ } (creates a gap).
- 5. Insert class at **position 1**: Shift A down by  $1 \{\underline{D}, A, C\}$  (1 move).

Total moves: 6.

#### Notes

- Each class occupies exactly one position and cannot overlap unless deleted.
- Empty spaces may remain after deletions.
- Moves are counted only when shifting existing classes up or down.

## Problem L. NTU I'm Forest Master

Input file: stdin
Output file: stdout
Time limit: 2.5 seconds

Memory limit: 64 MB

Your uncle, Roger, a humble lumberyard farmer, sells the best part of his forest to earn a living. However, there is one big problem: he has absolutely no idea how to handle it!

For years, he has been growing trees and selling them blindly, never knowing whether he was cutting down the most valuable part of the forest. But this year, during the Lunar New Year, something changed. As you were trying to survive the usual storm of nosy relatives asking about your studies, uncle Roger overheard that you were studying at **NTUIM**.

With his eyes full of hope (and possibly tears), he asked for your help, being the good niece and nephew(haiyaa), you agreed. Now, it's time to use your programming skills to help uncle Roger maximize his profits!

You need to help uncle Roger manage his forest by keeping track of the growth and changes in tree heights over time. The forest consists of N trees planted in a straight line, each with an initial height. Over time, various events such as fertilization or natural disasters will alter the trees' heights.

And sometimes, uncle Roger may wonder which part is the **most valuable segment** of the forest, of fixed length LN, to determine which part to sell. The value of a segment is determined by the following formula:

Value = 
$$(\max(H_L, H_{L+1}, \dots, H_{L+LN-1}) \times P_1) + (\sum_{i=L}^{L+LN-1} H_i \times P_2)$$

Where:

- $\max(H_L, H_{L+1}, \dots, H_{L+LN-1})$ ,  $\sum_{i=L}^{L+LN-1} H_i$  is the maximum and sum of tree height in the segment, respectively.
- $P_1$  and  $P_2$  are the given price coefficients.

Your task is to track the changes of the forest and help your uncle.

#### Input

The first line contains two integers:

- $N (1 \le N \le 20000)$  Number of trees in the forest.
- $Q \ (1 \le Q \le 100000)$  Number of operations to be performed.

The second line contains N integers:

$$H_1$$
  $H_2$   $\dots$   $H_N$ 

•  $H_i$  ( $0 \le H_i \le 100$ ) - The initial height of the  $i^{th}$  tree.

The 3 to Q+2 lines contain operation in one of the following formats:

#### 1. Fertilization/Natural Disaster

$$1/2$$
  $L$   $R$   $v$ 

- Increase/Decrease the height of all trees in range [L, R] by v.
- Constraints:  $1 \le L \le R \le N$ ,  $1 \le v \le 10$ .

#### 2. Query of Most Valuable Segment

$$3 LN P_1 P_2$$

- Find the best value segment of length LN.
- Constraints:  $1 \le LN \le min(1000, N)$ ,  $1 \le P_1$ ,  $P_2 \le 1000$ .
- There will be at most 100 query operation.

#### Output

If there is a query operation, print the segment of length LN that has the highest value. Print the best segment in the format:

Where:

- L, R is the starting index and ending index of the best segment.
- V is the maximum value of the segment.

If multiple segments have the same maximum value, print the one with the **smallest starting** index. If there is no segment with positive value, print 0 0 0.

stdin	stdout
5 3	2 5 23
1 3 2 5 4	
1 1 3 2	
2 2 4 1	
3 4 2 1	

#### **Explanation**

After operation 1-2, the forest heights are:

Finding the best segment of length LN = 4:

• Segment [1, 4]:  $\max(3, 4, 3, 4) = 4$ ,  $\sum = 3 + 4 + 3 + 4 = 14$ 

Value = 
$$(4 \times 2) + (14 \times 1) = 8 + 14 = 22$$

• Segment [2, 5]:  $\max(4, 3, 4, 4) = 4$ ,  $\sum = 4 + 3 + 4 + 4 = 15$ 

Value = 
$$(4 \times 2) + (15 \times 1) = 8 + 15 = 23$$

Thus, the best segment is:

2 5 23

#### Example 2

stdin	stdout
5 3	0 0 0
1 2 1 3 0	
2 1 5 8	
3 4 2 1	
1 1 3 2	

## Explanation

After operation 1, the forest heights are:

$$[-7, -6, -7, -5, -8]$$

Finding the best segment of length LN = 4:

• Segment [1, 4]:  $\max(-7, -6, -7, -5) = -5$ ,  $\sum = -7 + (-6) + (-7) + (-5) = -25$ Value =  $(-5 \times 2) + (-25 \times 1) = -10 + (-25) = -35$ 

• Segment [2,5]: 
$$\max(-6, -7, -5, -8) = -5$$
,  $\sum = -6 + (-7) + (-5) + (-8) = -26$   
Value =  $(-5 \times 2) + (-26 \times 1) = -10 + (-26) = -36$ 

Since there is no any segment has positive value, the output is:

0 0 0

# Problem M. The Cursed Envoys and the Race for Awakening

Input file: stdin
Output file: stdout
Time limit: 1 second
Memory limit: 64 MB

In a mysterious world, multiple ancient kingdoms exist, each ruled by powerful monarchs. Every few centuries, the kingdoms send their wisest envoys to participate in the legendary Moonlight Trial—a test designed to break an ancient curse.

- Each of you has a shadow that is either circular or triangular.
- There are at least one person with triangular shadow in each kingdom.
- You can see the shadows of others, but you cannot see your own.
- Every night, during the Moonlight Ritual, you may declare the shape of your shadow. If you are correct, you will awaken; if you are wrong, you will be forever lost in darkness.
- The chosen individuals cannot communicate with each other and must deduce their shadow's shape over time.

The trial's objective is clear: The first kingdom whose envoys all successfully identify their own shadow shapes and break the curse will claim ultimate victory.

#### Input

Line 1 contains an integer K, denoting the number of countries participating the Trial.

Line 2 to K + 1 each contains two interger,  $N_i$  and  $M_i$ , denoting the number of chosen individuals and the number of people with triangular shadows in country i, respectively.

- $1 \le K \le 10000$
- $1 \le M_i \le N_i \le 100000$

## Output

Print a single integer, the number of country that will win the Moonlight Trial.

If there are more than one country that will win, print the country with the most number of people since they have more power.

But if there still are more than one country with the same number of people, print the one with the smaller number since they are lucky.

#### Programming Design and Optimization 2025 Information Management, National Taiwan University, Saturday, April 19th, 2025

stdin	stdout
2	2
10 2	
2 1	

## Example 1

## Explanation

In country 2, there is only one person with a triangular shadow, the one with triangular shadow will find everyone is circular shadow. But there must be one person with triangular shadow, thus itself can determine its shape and awaken. And the second night everyone will find they are all circular shadow.

And in country 1, there are 2 people with triangular shadow, thus they definitely will need more days than country 2 to determine their shape.

Thus, country 2 will win the Moonlight Trial.

## Example 2

stdin	stdout
2	1
3 1	
2 1	

## Explanation

Since we know those two country will all identify their shadows in the same night, but country 1 has more people.

Thus, country 1 will win the Moonlight Trial.

# Problem N. Signal Synchronization in the Sky Port

Input file: stdin
Output file: stdout
Time limit: 1 second
Memory limit: 64 MB

In the futuristic Sky Port, thousands of aerial drones arrive and depart every second. Each drone is equipped with a synchronization chip that ensures it remains in alignment with two different transmission frequencies used by the control tower.

To ensure flight safety, a master synchronization array c must be generated. This array serves as an encrypted signal. Each drone will decode this signal using their own decoding window.

Here is how the synchronization system operates:

- The control tower provides two sequences a and b, each of length N, representing the plaintext message that drones of type-A and type-B should be able to recover.
- Each type-A drone extracts its message by XOR-ing every contiguous subarray of  $k_1$  elements (in circular fashion) from the array c.
- Each type-B drone extracts its message by XOR-ing every contiguous subarray of  $k_2$  elements (also circular) from the array c.

Your job is to generate such an array c of N non-negative integers, so that:

- XOR of every  $k_1$ -length contiguous subsequence (circular) of c equals the value in a.
- XOR of every  $k_2$ -length contiguous subsequence (circular) of c equals the value in b.

It is promised that there exists at least one valid c extracted to recover both messages.

## XOR Explanation

XOR, denoted  $\oplus$ , is a binary operation. For two bits a and b, the operation is defined as:

$$a \oplus b = \begin{cases} 1, & \text{if } a \neq b; \\ 0, & \text{if } a = b. \end{cases}$$

When doing XOR on integers, it is performed bitwise on their binary. For example, computing the XOR of two integers, 12 and 10. We first convert 12 and 10 to binary representation:

$$12_{10} = 1100_2$$
 and  $10_{10} = 1010_2$ .

And recall that for two bits, the XOR operation  $\oplus$  in binary operation.

Thus the result in binary and its decimal of  $12 \oplus 10$  is:

$$(0\,1\,1\,0)_2 = 0\cdot 2^3 + 1\cdot 2^2 + 1\cdot 2^1 + 0\cdot 2^0 = 0 + 4 + 2 + 0 = (6)_{10} \quad \Rightarrow 12 \oplus 10 = 6.$$

#### Input

Line 1 contains three integers N,  $k_1$ , and  $k_2$ .

Line 2 contains N integers  $a_1, a_2, \ldots, a_N$  the message to be extracted by type-A drones.

Line 3 contains N integers  $b_1, b_2, \ldots, b_N$  the message to be extracted by type-B drones.

- $1 \le N \le 10^5$
- $1 \le k_1, k_2 \le N \land k_1 \ne k_2$
- $0 \le a_i, b_i < 2^{30}$

#### Output

Print N non-negative integers  $c_1, c_2, \ldots, c_N$  representing the encrypted signal such that the XOR constraints allow recovery of both messages.

If there are multiple valid arrays, print any one of them. any number you write to the output must be in the range of  $[0, 2^{30})$ , or you'll get a "Wrong Answer".

#### Example 1

stdin	stdout
5 2 4	2 0 2 3 1
2 2 1 2 3	
3 0 2 0 1	

## Explanation

To recover each  $a_i$ , type-A drones perform XOR on every window of  $k_1 = 2$  elements from c:

- $c_1 \oplus c_2 = 3 \oplus 1 = 2 = a_1$
- $c_2 \oplus c_3 = 1 \oplus 0 = 1 = a_2 \dots$

Type-B drones apply XOR on  $k_2 = 4$ -element windows, and the values match perfectly with b.

Thus, the encrypted array is valid.

stdin	stdout
7 2 5	3 1 0 5 5 4 4
2 1 5 0 1 0 7	
2 5 0 3 7 2 3	