

题目1

1. 实现PCA算法

: 代码在附录

1) function [pcs, cprs_data, cprs_c] = pca_compress(data, rerr)

: 压缩数据函数

2) function recon_data = pca_reconstruct(pcs, cprs_data, cprs_c)

: 恢复 (重构) 原始数据 , 保存在新文件 "recon_data.xls"

2. CPA (Component Principal Analysis)

```
It is normal regression (non ill-conditioned).
Linear-Regression equation:
y_ =
0.338*x4 - 1.55*x2 - 1.866*x3 - 1.522*x1 + 0.439*x5 - 1.371*x6 - 2.127*x7 + 0.923*x8 - 1.458*x9 - 0.032*x10 + 44.093
F=292.210755
Fa=1.833746
Linear relationship exists
; CI :(y0-10.72, y0+10.72)>>
```

1) 判断是否回归分析: It is normal regression (non ill-conditioned).

2) 实现线性回归

"Linear-Regression equation:

$y_ = 0.338 \cdot x_4 - 1.55 \cdot x_2 - 1.866 \cdot x_3 - 1.522 \cdot x_1 + 0.439 \cdot x_5 - 1.371 \cdot x_6 - 2.127 \cdot x_7 + 0.923 \cdot x_8 - 1.458 \cdot x_9 - 0.032 \cdot x_{10} + 44.093$

3) 检验

F=292.210755

Fa=1.833746

"Linear relationship exists. "

4) 置信区间

CI :(y0-10.72 , y0+10.72)

附录：MATLAB 代码

【hw5】

```
% Read data X,Y & set significance level rerr = 0.05
X=xlsread('counties.xlsx','','C2:P3115');
Y=xlsread('counties.xlsx','','Q2:Q3115');
rerr = 0.05;

% PCA compress
[pcs, cprs_data, cprs_c] = pca_compress(X, rerr);

% PCA reconstruct
pca_reconstruct(pcs, cprs_data, cprs_c);

% excute function
linear_regression(Y,cprs_data',rerr);
```

【linear_regression】

```
function linear_regression(y,x,alpha)
% relevant data of x,y
[N,n]=size(x);
ex=mean(x);
ey=mean(y);
var_x=var(x);
var_y=var(y);

%regression
for i=1:n
    x(:,i)=(x(:,i)-ex(:,i))/sqrt(var_x(:,i));
end

y=(y-ey)/sqrt(var_y);

x=x';
% new relevants
Ye=mean(y);
Xe=mean(x);

[Q,lamda]=eig(x*x');
lamda=abs(sum(lamda));
lamda_max=max(lamda);

t=1;
maxr=find(lamda==lamda_max);
while (lamda(maxr(1))>=lamda_max/10)&&(t<=n)
    Qm(:,t)=Q(:,maxr(1));
    t=t+1;
    Q(:,maxr(1))=[];
    lamda(maxr(1))=[];
    maxr=find(lamda==max(lamda));
    if t==n+1
        maxr=1;
        lamda=0;
    end
end
end

if t==n+1
```

```

fprintf("It is normal regression (non ill-conditioned).\n");
c_ = inv(x*x') * x*y;
c0_ = Ye - mean(x') * c_;
for i=1:n
    c(i) = sqrt(var_y/var_x(i)) * c_(i);
end
c0 = ey - ex*c';
else
fprintf("It is ill-conditioned regression.\n");
z = Qm' * x;
lumda = inv(z*z');
d = lumda * Qm' * x * y;
c_ = Qm * d;
c0_ = Ye - mean(x') * c_;

for i=1:n
    c(i) = sqrt(var_y/var_x(i)) * c_(i);
end
c0 = ey - c*ex';
end

for i=1:n
    x_(i) = sym(['x', num2str(i)]);
end

y_ = 0;

for i=1:n
    y_ = y_ + round(c(i), 3) * x_(i);
end

fprintf('Linear-Regression equation:')
y_ = vpa(y_ + round(c0, 3))

% TSS = ESS + RSS
TSS = 0;
for i=1:N
    TSS = TSS + (y(i) - Ye)^2;
end
ESS = sum((x' * c_ + c0_ - mean(y)).^2);
RSS = TSS - ESS;

% F-test, df=(n, N-n-1)
F = (N-n-1) * ESS / (n * RSS);
Fa = finv(1-alpha, n, N-n-1);
fprintf('F=%f\nFa=%f\nLinear relationship exists\n', F, Fa);
% if F > Fa
% null hypothesis is not true, there be linear relationship
if F > Fa
    S = sqrt(var_y) * sqrt(RSS / (N-n-1));
    Z = norminv(1-alpha/2, 0, 1);
    fprintf('CI : (y0-%4.2f%-y0+%4.2f)', S*Z, S*Z);
else
    fprintf("can't do linear regression");
end
end

```

【pca_compress】

```
function [pcs, cprs_data, cprs_c] = pca_compress(data, rerr)
x = data;
[N, n] = size(x); % the number of row & column
ex = mean(x); % average of x
varx = var(x); % variance of x

%normalization
for i = 1:n
    x(:, i) = (x(:, i) - ex(:, i)) / sqrt(varx(:, i));
end

%eigenvalue
x = x';
[Q, l] = eig(x * x');
r = abs(sum(l));

%getting maximum eigen value, optimal one
t = 1;
k = 0;
ls = sum(r);
maxr = find(r == max(r));
while (k / ls < 1 - rerr) && (t <= n)
    k = k + r(maxr);
    Qm(:, t) = Q(:, maxr);
    t = t + 1;
    Q(:, maxr) = [];
    r(maxr) = [];
    maxr = find(r == max(r));
end

if t == (n + 1)
    sprintf('There isn't linear correlation in the matrix, it couldn't be compressed.')
else
    pcs = Qm;
    cprs_data = Qm' * x;
    cprs_c = [ex' varx'];
end
end
```

【pca_reconstruct】

```
function recon_data = pca_reconstruct(pcs, cprs_data, cprs_c)
[n, ~] = size(pcs);
% reconstruct standard variables
recon_data = pcs * cprs_data;
% normalizing recon_data
for i = 1:n
    recon_data(i, :) = recon_data(i, :) .* sqrt(cprs_c(i, 2)) + cprs_c(i, 1);
end
% rewrite datas in new document
xlswrite('recon_data.xls', recon_data);
end
```