Pledge: I pledge my honor that I have abided by the Stevens Honor System. -Eric Altenburg

1: Write a proof for the following theorem:

**Theorem 1.** For any natural number n, the number  $n^2 - n$  is even.

*Proof.* Let  $Q(x) = n^2 - n$ . We can then rewrite this to be Q(x) = n(n-1).

Since n can either be even or odd given the first proposition, then n will end up being multiplied by its opposite type—be it even or odd—as seen in Q(x). Therefore, regardless of the number chosen, an even number and an odd number will be multiplied together which always forms an even number.