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The present work was submitted to the Machine Learning on Graphs Group at the Chair of Computer Science 6, RWTH Aachen University

# **A Theoretical and Empirical Investigation into the Equivalence of Graph Neural Networks and the Weisfeiler-Leman Algorithm**

From the Faculty of Mathematics, Physics, and Computer Science approved for the purpose of obtaining the academic degree of Bachelor of Sciences.

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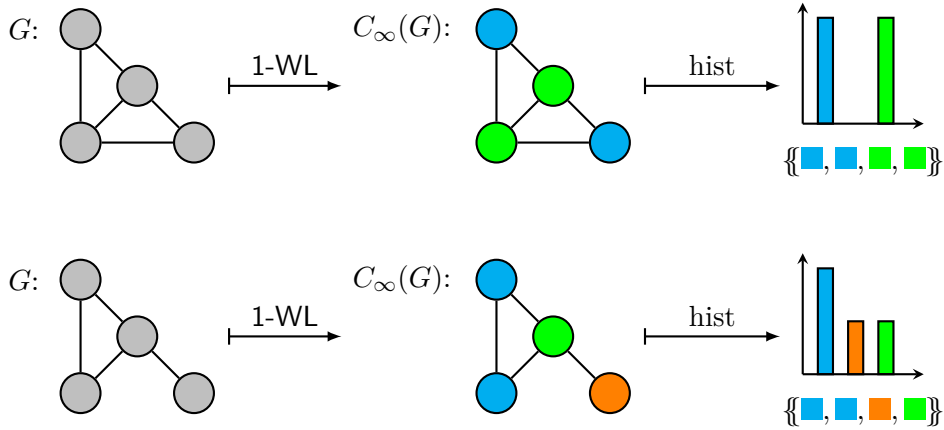
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Table 1: Overview of the mean absolute error and the standard deviation (logMAE) on large-scale (multi-target) molecular regression tasks. We highlighted the lowest error for the 1-WL+NN and GNN models for each dataset.

Method	Dataset			
	ALCHEMY	ALCHEMY (10K)	ZINC	ZINC (10K)
1-WL+NN	0.600 $\pm$ 0.004 -0.625 $\pm$ 0.032	0.305 $\pm$ 0.001 -1.740 $\pm$ 0.042	0.229 $\pm$ 0.003	0.465 $\pm$ 0.009
GNN	0.523 $\pm$ 0.016 -0.705 $\pm$ 0.035	0.282 $\pm$ 0.002 -1.890 $\pm$ 0.031	0.104 $\pm$ 0.005	0.298 $\pm$ 0.034

Table 2: Accuracy and standard deviation in percent achieved by the best-performing 1-WL+NN, 1-WL:GNN, and GNN model on each classification dataset.

Model	Dataset					
	ENZYMES	IMDB-BINARY	MUTAG	NCI1	PROTEINS	REDDIT-BINARY
1-WL+NN	48.3 $\pm$ 8.1	72.4 $\pm$ 4.1	85.1 $\pm$ 8.6	83.6 $\pm$ 2.2	75.2 $\pm$ 3.9	78.4 $\pm$ 2.7
GNN	34.4 $\pm$ 7.0	74.7 $\pm$ 3.8	84.6 $\pm$ 8.7	79.9 $\pm$ 2.2	74.3 $\pm$ 5.1	86.9 $\pm$ 3.2



test Morris et al. [2019]

# Bibliography

- [1] C. Morris, M. Ritzert, M. Fey, W. L. Hamilton, J. E. Lenssen, G. Rattan, and M. Grohe. Weisfeiler and leman go neural: Higher-order graph neural networks. In *Proceedings of the AAAI conference on artificial intelligence*, volume 33, pages 4602–4609, 2019.