2020 1124 Exploratory Data Analysis

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1 Predicting Concrete Compressive Strength - Exploratory Data Analysis

1.1 Dataset Citation

This dataset was retrieved from the UC Irvine Machine Learning Repository from the following URL: https://archive.ics.uci.edu/ml/datasets/Concrete+Compressive+Strength.

The dataset was donated to the UCI Repository by Prof. I-Cheng Yeh of Chung-Huah University, who retains copyright for the following published paper: I-Cheng Yeh, "Modeling of strength of high performance concrete using artificial neural networks," Cement and Concrete Research, Vol. 28, No. 12, pp. 1797-1808 (1998). Additional papers citing this dataset are listed at the reference link above.

1.2 Civil Engineering Domain Knowledge

1.2.1 Concrete Mix Design

The challenge of the dataset is to be able to predict the compressive strength of concrete given initial quantities of its components and the age after mixing and installation. The engineering term for the relative amounts of each material contained within a concrete mix is called the "mix design." The following materials comprise a mix design: * Cementitious materials (e.g. Portland cement, fly ash, etc.) * Coarse Aggregate (e.g. crushed rock, stone, gravel, etc.) * Fine aggregate (i.e. sand) * Water * Admixtures (materials to increase plasticity, prevent freezing, prevent corrosion, etc.)

Fly ash is a cementitious material that is typically lower cost but has different engineering characteristics than Portland cement. In this dataset, we are also provided data for "superplasticizer," an admixture, and "blast furnace slag," a byproduct of the concrete manufacturing process.

The data is provided in raw scientific quantities (kilograms of each material per cubic meter of mixed concrete). While this is useful from a scientific perspective, it is not in the standard engineering format that is used in the United States. Engineers typically specify concrete mix designs by certain minimum or maximum values for the following quantities: * Maximum water-to-cement (w/c) ratio – This is the ratio of all cementitious materials (Portland cement + fly ash) to the amount of water in the mix, by weight. It is widely accepted that the w/c ratio has the highest impact on the compressive strength of concrete. The lower the w/c ratio, the higher the compressive strength of the cured concrete should be. * Minimum sacks per cubic yard – A sack (sk) is a unit of measure for the weight of one cubic foot of Portland cement, usually around 94 pounds. * Maximum fly ash percentage – This is the ratio of fly ash to total cementitious materials, expressed as a percentage by weight. Engineers typically specify "no more than 25% fly ash substitution," for example.

1.2.2 Concrete Mixing, Curing, and Testing

Once the components are mixed, the water reacts with the cementitious materials in a process called hydration. The water-cementitious materials mixture is a paste that binds with the coarse and fine aggregates to create the high-strength material that we know as concrete. The period of time after which the components are mixed and during which hydration occurs is known as curing.

If the concrete is kept moist following mixture and installation (by, for example, covering it with moistened cloth or burlap), the compressive strength of the material will increase, following approximately a logarithmic curve as a function of time for a given mix design. However, installers rarely keep the concrete moist for longer than a week or a month due to water and labor costs.

We are not provided the length of time that the concrete was kept moist in this dataset. We do know, however, that the testing information provided was from concrete cylinder sampling. During construction, engineers typically sample concrete in cylinders and send them to a state-certified engineering laboratory. The lab holds the cylinders until the specified testing time, then they test them for compressive strength. Given this industry-standard practice, we assume in this analysis that the concrete was not moist-cured for any length of time.

The industry standard for concrete compressive strength is a 28-day cure. In this analysis, we expect that the concrete gains compressives trength rapidly from day of mixing until day 28, following which it will increase only very slightly over time.

1.3 Data Preprocessing

From an engineering and constructability perspective, it does not make sense to list the data as static kg/m^3 quantities. Rather, it is more practical to express quantities in terms of an engineering mix design; that is, to express each component as a percentage of the entire mix by weight. Furthermore, we expect the w/c ratio and fly ash-to-cement ratios also to play an important role in the overall compressive strength performance of the mixture.

For this reason, we have two separate data files. The first, 2020_1123_Concrete_Data_Loaded_Original.csv, contains the original data in an unaltered state, with only the column names shortened for ease-of-use in Python.

The second file, 2020_1123_Concrete_Data_Loaded_Transformed.csv, contains the following columns, which are related to the original by the relationships listed below. The total mass was calculated as cement + blast furnace slag + fly ash + water + superplasticizer + coarse aggregate + fine aggregate. The columns are the following: * Cementitious_Ratio = (Cement + Fly Ash)/(Total Mass) * Slag_Ratio = (Blast Furnace Slag)/(Total Mass) * Fly_Ash_Ratio = (Fly Ash)/(Cement + Fly Ash) * Water_to_Cementitious_Ratio = (Water)/(Cement + Fly Ash) * Superplasticizer_Ratio = (Superplasticizer)/(Total Mass) * Coarse_Aggregate_Ratio = (Coarse Aggregate)/(Total mass) * Sand_Ratio = (Fine Aggregate)/(Total Mass) * The Age and Concrete Compressive Strength columns retain the same data as the original file

The purpose of converting the original data into these quantities is just to gain deeper insights into the engineering properties of the materials during exploratory data analysis. But since the quantities are calculated based on the total mass (a quantity derived from the sum of the features), there is multicollinearity; therefore, in any modeling, we will need to use the raw scientific values in kg/m³ (with scaling).

1.4 Exploratory Data Analysis

1.4.1 Import the Relevant Libraries

```
[1]: import numpy as np
     import pandas as pd
     import seaborn as sns
     import matplotlib.pyplot as plt
     %matplotlib inline
     sns.set()
```

1.4.2 Import the Data

```
[2]: df1 = pd.read csv('2020 1123 Concrete Data Loaded Original.csv')
     df2 = pd.read_csv('2020_1123_Concrete_Data_Loaded_Transformed.csv')
     original_data = df1.copy()
     ratio_data = df2.copy()
```

Exploring the Original Data

```
[3]: original_data.head()
[3]:
        Cement
                Blast_Furnace_Slag Fly_Ash Water
                                                      Superplasticizer
         540.0
                                0.0
                                         0.0
                                               162.0
                                                                    2.5
     1
         540.0
                                0.0
                                         0.0 162.0
                                                                    2.5
                                         0.0 228.0
     2
         332.5
                              142.5
                                                                    0.0
     3
         332.5
                              142.5
                                         0.0 228.0
                                                                    0.0
         198.6
                                         0.0 192.0
                              132.4
                                                                    0.0
        Coarse_Aggregate Fine_Aggregate Age
                                                 Compressive_Strength
     0
                  1040.0
                                    676.0
                                            28
                                                                 79.99
                                    676.0
     1
                  1055.0
                                            28
                                                                 61.89
                                    594.0
     2
                   932.0
                                           270
                                                                 40.27
     3
                   932.0
                                    594.0
                                           365
                                                                 41.05
                   978.4
                                    825.5
                                           360
                                                                 44.30
```

```
original_data.describe()
```

```
[4]:
                          Blast_Furnace_Slag
                 Cement
                                                   Fly_Ash
                                                                   Water
            1030.000000
                                 1030.000000
                                               1030.000000
                                                             1030.000000
     count
             281.167864
                                   73.895825
                                                 54.188350
                                                              181.567282
    mean
     std
             104.506364
                                   86.279342
                                                 63.997004
                                                               21.354219
    min
             102.000000
                                    0.000000
                                                  0.000000
                                                              121.800000
     25%
             192.375000
                                    0.000000
                                                  0.000000
                                                              164.900000
     50%
             272.900000
                                   22.000000
                                                  0.000000
                                                              185.000000
     75%
             350.000000
                                  142.950000
                                                118.300000
                                                              192.000000
             540.000000
                                                200.100000
     max
                                  359.400000
                                                              247.000000
```

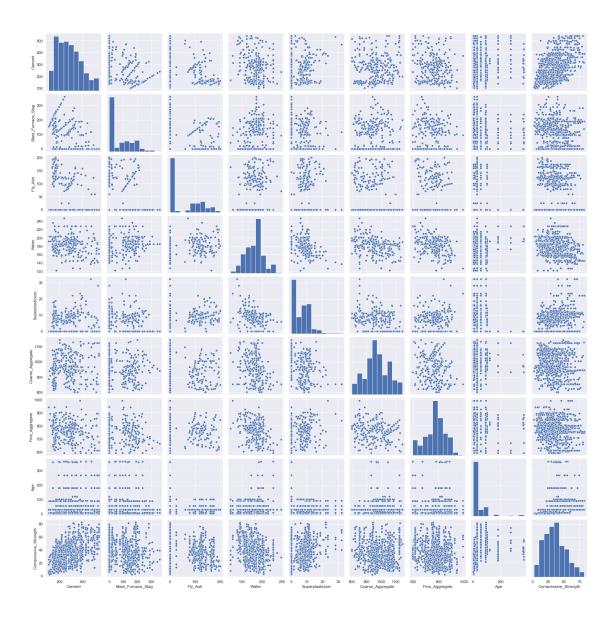
	Superplasticizer	Coarse_Aggregate	Fine_Aggregate	Age	\
count	1030.000000	1030.000000	1030.000000	1030.000000	
mean	6.204660	972.918932	773.580485	45.662136	
std	5.973841	77.753954	80.175980	63.169912	
min	0.000000	801.000000	594.000000	1.000000	
25%	0.000000	932.000000	730.950000	7.000000	
50%	6.400000	968.000000	779.500000	28.000000	
75%	10.200000	1029.400000	824.000000	56.000000	
max	32.200000	1145.000000	992.600000	365.000000	

	Compressive_Strength
count	1030.000000
mean	35.817961
std	16.705742
min	2.330000
25%	23.710000
50%	34.445000
75%	46.135000
max	82.600000

Let us examine the original data file by plotting pair plots. This will show us any potential relationships between the different dataset features and will help us give a cursory check for multicollinearity.

```
[5]: sns.pairplot(original_data)
```

[5]: <seaborn.axisgrid.PairGrid at 0x1acd7c169a0>



We can see that there is a clear positive linear relationship between cement and compressive strength, and an inverse linear relationship between water and compressive strength, both of which were expected. There may be relationships between superplasticizer and fly ash, but this will be further explored in the transformed data analysis.

There may be direct multicollinear relationships between blast furnace slag and cement and slag and fly ash. This makes sense, considering that the blast furnace slag is a byproduct of the concrete manufacturing process.

1.4.4 Exploring the Transformed Data

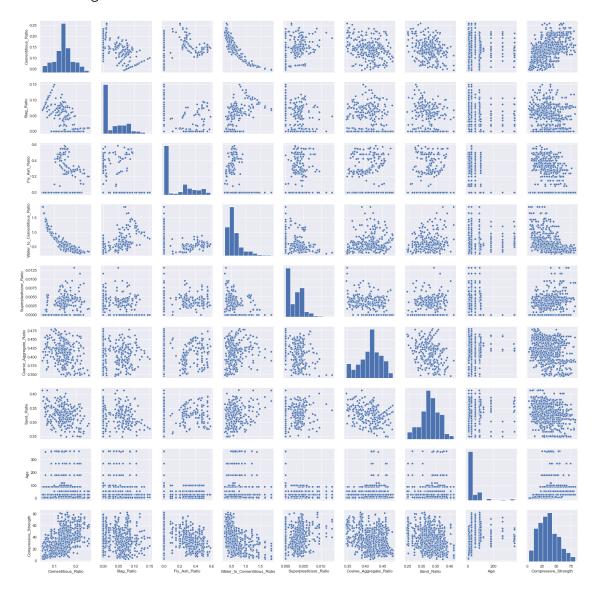
[8]: ratio_data.head()

```
[8]:
        Cementitious_Ratio
                             Slag_Ratio
                                         Fly_Ash_Ratio
                                                          Water_to_Cementitious_Ratio
                   0.205086
                                                     0.0
                                                                               0.400000
     0
                                0.00000
     1
                   0.167391
                                0.00000
                                                     0.0
                                                                               0.483117
     2
                   0.058291
                                0.087436
                                                     0.0
                                                                               1.375358
     3
                   0.145726
                                0.000000
                                                     0.0
                                                                               0.550143
     4
                   0.085350
                                0.056900
                                                     0.0
                                                                               0.966767
        Superplasticizer_Ratio
                                  Coarse_Aggregate_Ratio
                                                            Sand_Ratio
                                                                         Age
     0
                            0.0
                                                              0.251436
                                                 0.461444
                                                                           1
                            0.0
     1
                                                 0.420000
                                                              0.331739
                                                                           1
     2
                            0.0
                                                 0.437179
                                                              0.336924
                                                                           3
     3
                                                 0.437179
                                                              0.336924
                                                                           3
                            0.0
     4
                                                              0.354764
                                                                           3
                            0.0
                                                 0.420474
        Compressive_Strength
     0
                    12.638095
     1
                     6.267337
     2
                     8.063422
     3
                    15.049193
     4
                     9.131420
     ratio data.describe()
[9]:
            Cementitious_Ratio
                                   Slag_Ratio
                                                Fly_Ash_Ratio
     count
                    1030.000000
                                  1030.000000
                                                  1030.000000
                       0.142726
                                     0.031643
                                                     0.155263
     mean
     std
                       0.040513
                                     0.036961
                                                     0.187884
     min
                       0.044815
                                     0.000000
                                                     0.000000
     25%
                       0.124002
                                     0.000000
                                                     0.000000
     50%
                       0.143272
                                     0.009455
                                                     0.000000
     75%
                       0.162794
                                     0.061972
                                                     0.319960
                       0.259517
                                     0.150339
     max
                                                     0.588415
            Water_to_Cementitious_Ratio
                                            Superplasticizer_Ratio
                              1030.000000
                                                        1030.000000
     count
                                 0.611796
                                                           0.002620
     mean
                                 0.278319
                                                           0.002494
     std
     min
                                 0.265918
                                                           0.000000
     25%
                                 0.447540
                                                           0.000000
     50%
                                 0.547837
                                                           0.002727
     75%
                                                           0.004338
                                 0.666639
                                 1.882353
                                                           0.013149
     max
                                                                  Compressive Strength
            Coarse_Aggregate_Ratio
                                       Sand Ratio
                        1030.000000
                                      1030.000000
                                                    1030.000000
                                                                            1030.000000
     count
                           0.415166
                                                                              35.817836
     mean
                                         0.330117
                                                      45.662136
     std
                           0.031021
                                         0.033245
                                                      63.169912
                                                                              16.705679
```

min	0.345890	0.247971	1.000000	2.331808
25%	0.392294	0.311208	7.000000	23.707115
50%	0.420464	0.330543	28.000000	34.442774
75%	0.437623	0.354096	56.000000	46.136287
max	0.479846	0.414147	365.000000	82.599225

[10]: sns.pairplot(ratio_data)

[10]: <seaborn.axisgrid.PairGrid at 0x1acdb440f40>



1.5 Initial Visual Analysis

It is clear from these pair plots that the ratios in the transformed data are much more strongly correlated with compressive strength than the raw values in the original data.

Below are the observed relationships with compressive strength: * Cementitious_Ratio - A clear positive linear relationship. This was assumed from domain knowledge. * Slag_Ratio - Unclear. But it is unlikely that this substance would contribute anything to the engineering properties of the concrete mix. * Fly_Ash_Ratio - A clear inverse linear relationship. While we assumed from domain knowledge that a high fly ash ratio would reduce compressive strength performance, the clear linearity of the relationship is surprising and should be further studied. * Water_to_Cementitious_Ratio - A clear non-linear inverse relationship. We assumed an inverse relationship from domain knowledge, but the nonlinearity of it is surprising. It appears as if there is a steep reduction in compressive strength up to around 1.0 (equal parts water and cement), then it declines less rapidly the more water is added. This should be further studied. * Superplasticizer_Ratio - Unclear, possibly a positive relationship, should be further studied. * Coarse_Aggregate_Ratio - Unclear. * Sand_Ratio - Unclear. * Age - An assumed positive logarithmic relationship from domain knowledge.

1.6 Conclusions & Future Modeling

We will use the original data during modeling in order to avoid the multicollinearity of the transformed data. Cement, fly ash, and water should be kept as separate quantities during modeling. The w/c and other engineering ratios can be analyzed post-modeling (optional). All input values should be scaled and run through an artificial neural network (ANN) in a train-test split. The performance of the ANN model should be compared with the performance of linear models trained on cement vs. compressive strength, fly ash ratio vs. compressive strength, etc. to determine the best model.