

Consider throwing  $n$  balls into  $n$  bins uniformly at random. Let  $X$  be the number of balls in the first bin.

- a) What is the expected value of  $X$ ?
- b) What is the variance of  $X$ ?

What is the covariance of  $X$  and  $X^3$  where  $X$  is a uniformly distributed variable on the interval  $[0, 1]$ ? (i.e.  $X \sim U[0, 1]$ )

## 1 Halting Problem

Basically problem comes down to reducing any given problem to the halting problem. We can do this by describing a program that halts if we reach the desired input, and not otherwise. Generally, things where we need to determine something about *how* a program executes (for instance, executing a specific line) is uncomputable, and things that can be tracked (like how much memory a program uses) can be computable.