

Supplementary Material

1 Performance evaluation (phase detection via IMU vs. camera)

We evaluate the impact of phase detection using IMU on goal metrics estimation using LASSO regression as the estimator. This can be achieved by incorporating IMU-based swimming phases and camera-based swimming phase (CAM) separately and incorporating them as input to the regression model. The cross-validated values (R^2 , RMSE and the relative RMSE in percent) of regression are reported for each swimming technique using both methods for comparison in table A1.

In the worst case (*Push* maximum velocity of butterfly technique), R^2 has decreased 0.08, while it is affected less than 0.05 for most of other goal metrics. Moreover, the relative RMSE has increased no more than 3.5% for any goal metric. This shows that the error of IMU phase detection is small enough, not to affect the goal metrics estimation accuracy.

Table A1 – The results of evaluating LASSO regression for goal metrics estimation using IMU-based or camera-based (CAM) phase detection. The determination coefficient (R^2) and root mean square of error (RMSE) and the relative RMSE (in %) of regression are reported for each swimming technique.

Goal metric	Front crawl				Breaststroke			
	CAM		IMU		CAM		IMU	
	R^2	RMSE (%)	R^2	RMSE (%)	R^2	RMSE (%)	R^2	RMSE (%)
<i>Push</i> maximum velocity (m/s)	0.80	0.133 (5.4)	0.74	0.140 (5.7)	0.81	0.114 (4.6)	0.75	0.131 (5.3)
<i>Glid</i> end velocity (m/s)	0.83	0.105 (8.7)	0.76	0.123 (10.1)	0.70	0.135 (11.0)	0.64	0.139 (11.1)
<i>StPr</i> average velocity (m/s)	0.72	0.075 (4.4)	0.72	0.075 (4.4)	0.64	0.054 (5.8)	0.58	0.058 (5.9)
<i>Swim</i> – average velocity per cycle (m/s)	0.96	0.029 (4.8)	0.89	0.050 (8.3)	0.86	0.062 (5.9)	0.84	0.044 (5.7)
Average velocity of <i>Swim</i> phase (m/s)	0.90	0.044 (2.7)	0.90	0.044 (2.7)	0.76	0.059 (5.1)	0.71	0.061 (5.3)
T_{5m} (s)	0.67	0.155 (7.5)	0.64	0.158 (7.6)	0.77	0.206 (6.8)	0.74	0.209 (6.9)
T_{15m} (s)	0.80	0.345 (4.0)	0.75	0.369 (4.3)	0.82	0.430 (6.7)	0.81	0.430 (6.7)
Lap average velocity (m/s)	0.95	0.031 (2.3)	0.95	0.032 (2.4)	0.90	0.042 (3.8)	0.85	0.038 (3.4)
	Butterfly				Backstroke			
	CAM		IMU		CAM		IMU	
	R^2	RMSE (%)	R^2	RMSE (%)	R^2	RMSE (%)	R^2	RMSE (%)
<i>Push</i> maximum velocity (m/s)	0.79	0.110 (3.8)	0.71	0.149 (5.9)	0.75	0.105 (4.8)	0.72	0.107 (4.9)
<i>Glid</i> end velocity (m/s)	0.81	0.104 (8.5)	0.80	0.111 (9.1)	0.86	0.104 (6.5)	0.84	0.104 (6.4)

<i>StPr</i> average velocity (m/s)	0.75	0.153 (6.7)	0.75	0.152 (6.7)	0.77	0.070 (5.2)	0.75	0.079 (5.3)
<i>Swim</i> – average velocity per cycle (m/s)	0.88	0.067 (4.9)	0.88	0.067 (4.9)	0.89	0.076 (5.7)	0.89	0.076 (5.7)
Average velocity of <i>Swim</i> phase (m/s)	0.79	0.048 (3.3)	0.79	0.049 (3.3)	0.73	0.056 (4.3)	0.73	0.056 (4.3)
T_{5m} (s)	0.66	0.204 (6.8)	0.63	0.209 (7.0)	0.72	0.197 (6.2)	0.71	0.202 (6.4)
T_{15m} (s)	0.86	0.342 (3.5)	0.79	0.344 (4.6)	0.82	0.499 (4.8)	0.77	0.521 (5.0)
Lap average velocity (m/s)	0.86	0.048 (3.3)	0.86	0.049 (3.3)	0.84	0.052 (3.8)	0.80	0.063 (4.6)

2 Parameter selection

Table A2 to A4 represent the parameters that were selected using LASSO method for each swimming phase in breaststroke, butterfly and backstroke techniques. Refer to section 2.1 in the main text for definition of anatomical axes.

Table A2 – Table of the selected parameters for each goal metric in breaststroke technique. The parameters are ordered according to their weights in the regression model.

Goal metric	Selected parameters
<i>Push</i> maximum velocity	<i>Int</i> (Acc_Y), <i>Max</i> (Gyr_Z), <i>Max</i> (Acc_Y), <i>Range</i> (Acc_Y), <i>SD</i> (φ), <i>Momentum</i> (Acc_Y), <i>Eff</i> (Acc_Y), <i>SD</i> (Acc_Y), <i>Mean</i> (Acc_Y)
<i>Glid</i> end velocity	<i>Glid</i> duration, <i>Int</i> (Acc_Y), <i>Momentum</i> (Acc_Y), <i>Max</i> (Acc_Y), <i>Range</i> (φ), <i>Mean</i> (φ), <i>Range</i> (Acc_Y), <i>SD</i> (φ)
<i>StPr</i> average velocity	<i>Range</i> (Acc_Y), <i>StPr</i> duration, <i>Range</i> (φ), <i>Mean</i> (φ), <i>Eff</i> (Acc_Y), <i>SD</i> (Gyr_Y), <i>Mean</i> (Gyr_Y),
<i>Swim</i> – average velocity per cycle	Cycle duration, DPS, <i>SD</i> (Acc_Y), <i>Range</i> (Gyr_Z), <i>Range</i> (Acc_Y), <i>Range</i> (Gyr_Y)
Average velocity of <i>Swim</i> phase	<i>SD</i> (Acc_Y), Stroke rate, number of strokes, <i>Range</i> (φ), <i>SD</i> (φ)
T_{5m}	<i>Max</i> (Gyr_Z) in <i>Push</i> , <i>Momentum</i> (Acc_Y) in <i>Glid</i> , <i>Max</i> (Gyr_Z) in <i>Glid</i> , <i>SD</i> (φ) in <i>Glid</i> , <i>Range</i> (φ) in <i>Push</i>
T_{15m}	<i>SD</i> (Acc_Y) in <i>StPr</i> , <i>Range</i> (Acc_Y) in <i>Glid</i> , <i>Mean</i> (Gyr_Z) in <i>Glid</i> , <i>Range</i> (φ) in <i>Push</i> , <i>SD</i> (φ) in <i>Push</i> , <i>Range</i> (Acc_Y) in <i>StPr</i> , <i>Max</i> (Gyr_Z) in <i>Push</i> , <i>Max</i> (Acc_Y) in <i>Glid</i>
Lap average velocity	Stroke rate, <i>Max</i> (Acc_Y) in <i>StPr</i> , <i>SD</i> (Acc_Y) in <i>Swim</i> , number of strokes, <i>Max</i> (Acc_Y) in <i>Push</i> , <i>SD</i> (θ) in <i>Swim</i> , <i>Momentum</i> (Acc_Y) in <i>Push</i> , <i>Eff</i> (Acc_Y), <i>Max</i> (Acc_Y) in <i>Glid</i>

Table A3 – Table of the selected parameters for each goal metric in butterfly technique. The parameters are ordered according to their weights in the regression model.

Goal metric	Selected parameters
<i>Push</i> maximum velocity	<i>SD</i> (φ), <i>Int</i> (Acc_Y), <i>SD</i> (Acc_Y), <i>Momentum</i> (Acc_Y), <i>Max</i> (Gyr_Z), <i>Mean</i> (Acc_Y), <i>Max</i> (Acc_Y), <i>Eff</i> (Acc_Y)
<i>Glid</i> end velocity	<i>Glid</i> duration, <i>Int</i> (Acc_Y), <i>Range</i> (φ), <i>Range</i> (Gyr_Z), <i>Mean</i> (φ), <i>Max</i> (Acc_Y),
<i>StPr</i> average velocity	<i>Range</i> (Acc_Y), <i>Eff_dir</i> (Acc_Y), <i>Mean</i> (Gyr_Y), <i>Eff</i> (Acc_Y), <i>Range</i> (Gyr_Y)
<i>Swim</i> – average velocity per cycle	Cycle duration, DPS, <i>SD</i> (Acc_Y), <i>Range</i> (φ), <i>SD</i> (Gyr_Z)
Average velocity of <i>Swim</i> phase	<i>SD</i> (Acc_Y), Stroke rate, number of strokes, <i>Range</i> (φ), <i>SD</i> (φ)
T_{5m}	<i>Range</i> (Gyr_Z) in <i>Glid</i> , <i>Range</i> (Acc_Y) in <i>Glid</i> , <i>Range</i> (φ) in <i>Push</i> , <i>Max</i> (Gyr_Z) in <i>Push</i> , <i>Momentum</i> (Acc_Y) in <i>Push</i> , <i>Push</i> duration, <i>SD</i> (Acc_Y) in <i>Push</i> , <i>Mean</i> (φ) in <i>Glid</i>
T_{15m}	<i>Glid</i> duration, <i>Range</i> (Acc_Y) in <i>StPr</i> , <i>SD</i> (Acc_Y) in <i>StPr</i> , <i>SD</i> (Acc_Y) in <i>Push</i> , <i>Mean</i> (φ) in <i>Push</i> , <i>Momentum</i> (Acc_Y) in <i>Glid</i> , <i>SD</i> (Gyr_Z) in <i>StPr</i> , <i>Mean</i> (Acc_Y) in <i>StPr</i>
Lap average velocity	Stroke rate, <i>SD</i> (Acc_Y) in <i>Swim</i> , number of strokes, <i>Max</i> (Acc_Y) in <i>Push</i> , <i>SD</i> (Gyr_Z) in <i>StPr</i> , <i>Range</i> (φ) in <i>Swim</i> , <i>SD</i> (φ) in <i>Swim</i>

Table A4 – Table of the selected parameters for each goal metric in backstroke technique. The parameters are ordered according to their weights in the regression model.

Goal metric	Selected parameters
<i>Push</i> maximum velocity	<i>Max (Acc_Y), Mean (φ), SD (φ), Momentum (Acc_Y), SD (Acc_Y), Max (Gyr_Z), Mean (Acc_Y), Int (Acc_Y)</i>
<i>Glid</i> end velocity	<i>Int (Acc_Y), Momentum (Acc_Y), Mean (Gyr_Z), Glid duration, SD (φ), SD (Acc_Y), Range (φ)</i>
<i>StPr</i> average velocity	<i>Range (Acc_Y), Eff(Acc_Y), SD (Gyr_Z), StPr duration, Range (Gyr_Y)</i>
<i>Swim</i> – average velocity per cycle	<i>Cycle duration, DPS, SD (Acc_Y)</i>
Average velocity of <i>Swim</i> phase	<i>Stroke rate, SD (Acc_Y), number of strokes, Range (φ)</i>
<i>T</i> _{5m}	<i>Momentum (Acc_Y) in Push, SD (Acc_Y) in Push, Push duration, Mean (φ) in Glid, Mean (φ) in Push</i>
<i>T</i> _{15m}	<i>Max (Acc_Y) in Push, Momentum (Acc_Y) in Push, SD (Acc_Y) in StPr, Eff(Acc_Y) in StPr, Glid duration, Int (Acc_Y) in Glid, SD (Acc_Y) in Glid, Range (Gyr_Z) in StPr,</i>
Lap average velocity	<i>Stroke rate, Momentum (Acc_Y) in Push, Max (Acc_Y) in Push, Range (Gyr_Z) in StPr</i>

3 Glossary of terms

Here is the table of glossary of all the terms used for swimming performance evaluation using one sacrum IMU.

Table A5 – Table of glossary

Term	Definition
<i>IMU</i>	Inertial measurement unit
<i>CAM</i>	Camera
<i>Acc</i>	Acceleration data (m/s^2)
<i>Gyr</i>	Angular velocity data ($^\circ/s$)
<i>Acc_X, Acc_Y, Acc_Z</i>	Acceleration on X, Y or Z axis of global frame
<i>Gyr_X, Gyr_Y, Gyr_Z</i>	Angular velocity on X, Y or Z axis of global frame
φ	Pitch angle
θ	Roll angle
ψ	Yaw angle
<i>q</i>	Quaternion
<i>LASSO</i>	least absolute shrinkage and selection operator
<i>RMSE</i>	Root mean square error
<i>Swimming bout</i>	The swimming parts (in any swimming technique) during a training session that includes one or more laps.
<i>Swimming lap</i>	The wall-to-wall period of swimming (in any swimming technique) that starts with wall push-off and ends when the swimmer touches the wall.
<i>Swimming technique</i>	The technique of swimming which is one among this list: Front crawl, Breaststroke, Butterfly, Backstroke
<i>Swimming phase</i>	Each lap is divided in four swimming phases (wall push-off, glide, strokes preparation and swimming)
<i>Push</i>	Wall push-off phase
<i>Glid</i>	Glide phase
<i>StPr</i>	Strokes preparation phase
<i>Swim</i>	Swimming phase
<i>T_{5m}</i>	Time to reach 5 meters from the wall
<i>T_{15m}</i>	Time to reach 15 meters from the wall
<i>SD</i>	The standard deviation of a parameter
<i>Max</i>	Maximum value of a parameter
<i>Int</i>	The integral of a parameter
<i>DPS</i>	Distance per stroke
<i>Eff</i>	Efficiency defined as the ratio of positive to negative forward acceleration
<i>Eff_{dir}</i>	Directional efficiency defined as the ratio of forward acceleration to total acceleration