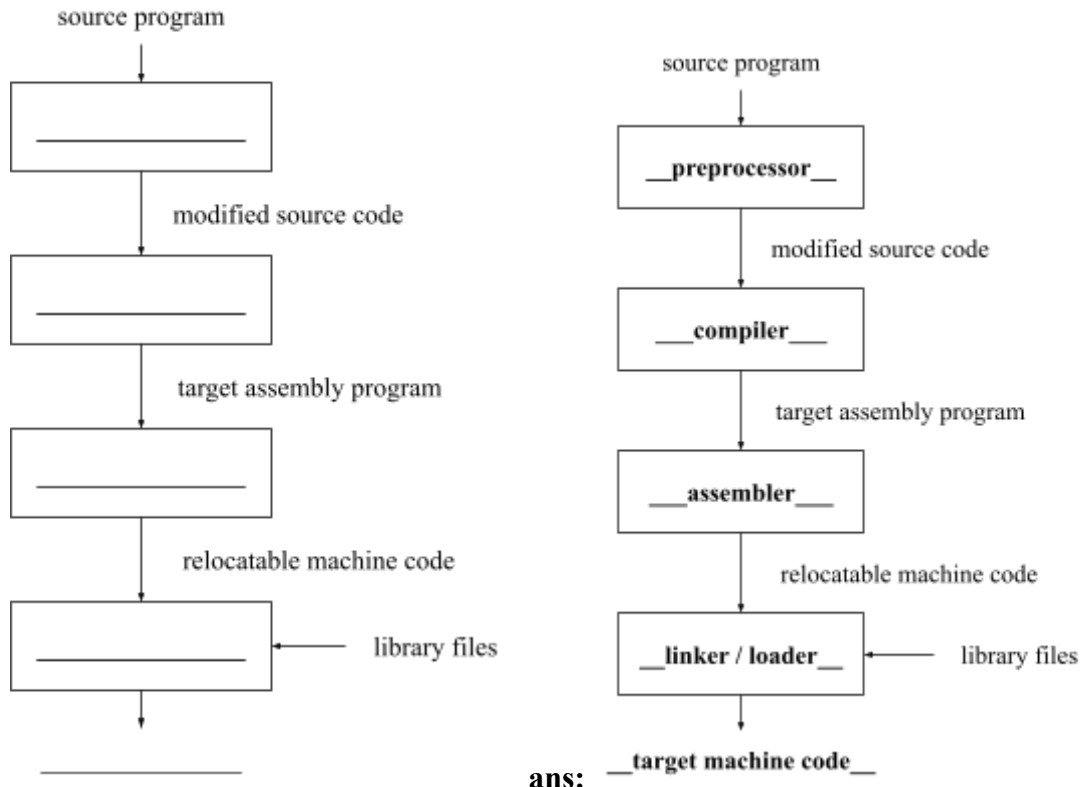


2024 NCKU CSIE Compiler Midterm Exam (total score: 120)

Student ID: _____ Name: _____

1. (10%) Compiler Process. Please fill in the blanks below. (2% * 5 blanks)



- 沒有特別標示順序則由上往下對照批改

2. (25%) Regular Expression.

limitation:

- all your answer Regular Expression should < 36 characters
- enumerating all cases and predefined variable are **not allowed**

- a. (5%) choose corresponding (a) ~ (g) for sub-question (1) ~ (7) (hint!)

ans: c f a g d b e

(1) X	C	(a) match X a~b times
(2) [*X]	f	(b) match all uppercase except X
(3) X[a,b]	a	(c) match X
(4) *X	g	(d) match X at the end
(5) X\$	d	(e) match all digits
(6) [A-WY-Z]	b	(f) match except X
(7) [0-9]	e	(g) match X at the start

- b. (5%) All strings that only contain lowercase a **and** b, except string "ab"
- For example: "ba", "aaaaaaaab", "ababababa", "bbabab"
 - Not including, for example: "a", "b", "ab", "abc", "aaaaaa"

ans: $a[ab]^+b \mid [ab]^+ba[ab]^+$

ans: $[ab]^+(abb \mid ba \mid aab)[ab]^+$

ps: $[ab] = (a|b)$

- c. (5%) Defines a C-like, fixed-decimal literal with no superfluous leading or trailing zeros.

- For example: 123.456, 1200.08, 1.0, 0.0

- Not including, for example: 114514, 000.00, 120.800, 001.100

ans: $(0 \mid [1-9][0-9]^*)\.(0 \mid [0-9]^*[1-9])$

- d. (5%) Please represent with a Regular Expression any string that meets all of the following criteria: **Starts** with an 'A', followed by **three to five** digits, **then** a hyphen '-', and **ends** with **four** uppercase English letters.

- For example: "A23651-TSMC", "A231-APEX", "A8093-PTSD"

- Not including, for example: "aA23651-ADCD", "A19-COVID",
"A23651-GuRa", "P7612-compiler"

ans: $^A[0-9]\{3,5\}-[A-Z]\{4\}$$

- e. (5%) Please represent with a Regular Expression any string that meets all of the following criteria: The string with substring that **one or more** uppercase English letters, followed immediately by **exactly one** non-digit.

- For example:

- in "regADDSC#\$\$@", the substring "ADDSC#";

- in "face_me@SEKIRO!", the substring "SEKIRO!";

- in "a!~DF\$ac", the substring "DF\$";

- in "bb()ZELDa", the substring "ZELDa"

ans: $[A-Z]^+[^0-9]$

3. (25%) DFA / NFA. (for b. and c., you only need to present the automata graph)
- a. (5%) Please explain the difference between DFA and NFA in two aspects:

- as for Determinism vs. Nondeterminism. (3%)

ans: 提到每一個 **token** 都只有一種可能的 **transition** 即給分

- as for performance considerations (time / the number of states / construction...). (2%)

ans:

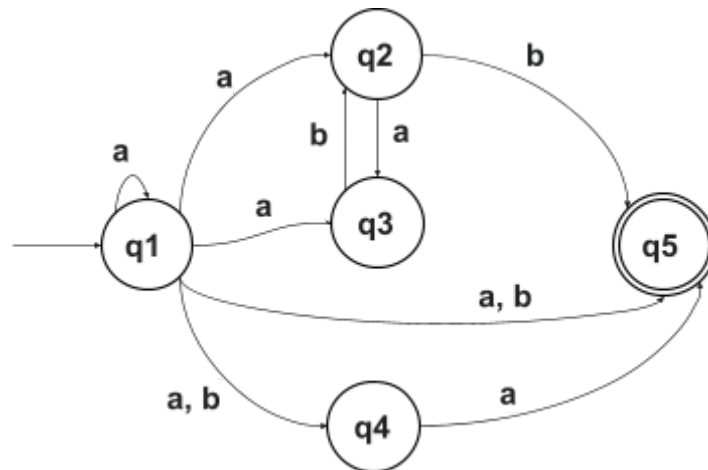
就時間而言, 由於 **DFA** 的每個 **state** 對每個輸入 **token** 的 **transition** 都是預先定義且只有一種可能, 無需在運行時進行選擇或回溯因此所耗時間通常比 **NFA** 少。

就 **state** 的數量和建構複雜度而言, 若沒有特定前提就沒有標準答案, 會依據你提出原因的合理性批改。

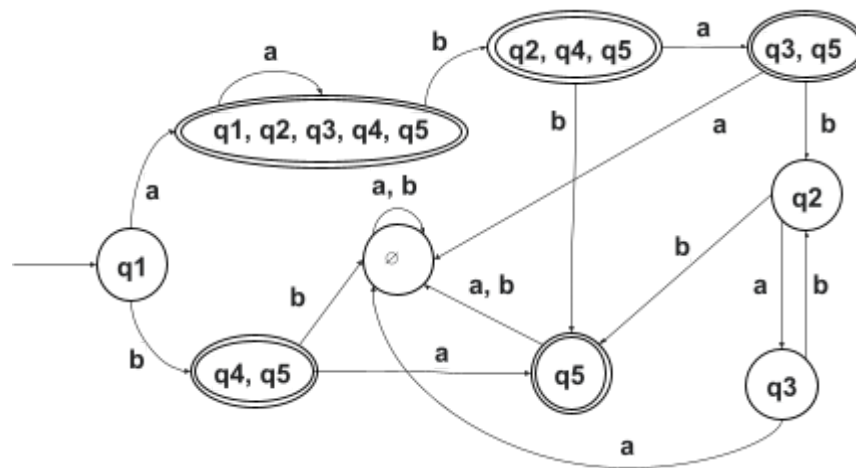
1. 因為 **NFA** 有非確定性的性質 (即不只一種可的 **transition**) 和 **ϵ -transition**, 讓 **transition** 可以無限擴增, 使得 **state** 數量通常比 **DFA** 多。但也因以上性質, 對人類來說較易讀, 也不需將所有 **transition** 畫出來, 建構較 **DFA** 簡單。

2. 如果以任意 **DFA** 都是 **NFA** 來看, 那麼 **NFA** 的 **state** 數量會小於等於 **DFA** 的 **state** 數量, 一個 **NFA** 可以被轉換成一個等價的 **DFA**, 即兩者識別相同的 **RE**。在轉換過程中, 對原有 **n** 個狀態的 **NFA** 來說, 其等價的 **DFA** 最多可能有 **2ⁿ** 個狀態。轉換後, 對電腦來說較易判讀, 速度也較快。

b. (10%) Transform below NFA to the **minimized** DFA.



ans:

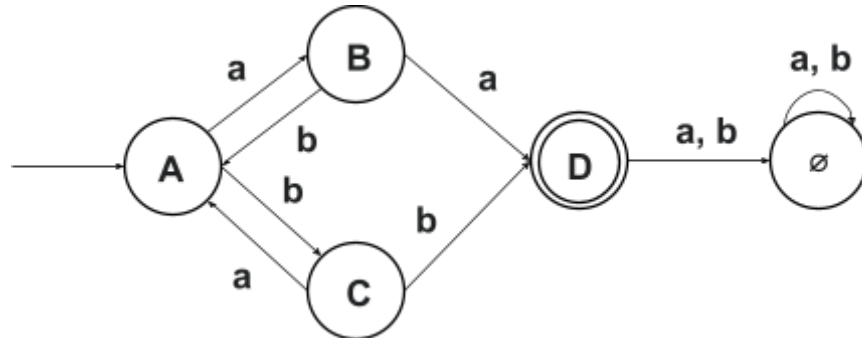


- 空集合 state 沒畫到, 其他 state, edge 皆正確扣 3%
- 沒有畫到 input edge、accept 的雙圈圈皆扣 2%
- 少 edge / 多 edge / 簡化錯 state (新 state 的集合有多 / 少舊 state) 皆扣 2%
- 空集合 state 沒有回到自己的 edge (吃 a, b) 扣 1%
- state 數、edge 數對, 定義集合寫錯扣 5%

c. (10%) Transform below Regular Expression to the **minimized** DFA.

$(ab|ba)^*(aa|bb)$

Hint: you'll finally have **less than 10 states** when the DFA is minimized, and you should clearly write down your definition of every state in the automata.



- 由於提示的 state 數量有誤，小於 10 個但非最簡酌情扣 5-7%
- 空集合 state 沒畫到，其他 state, edge 皆正確扣 3%
- 空集合 state 沒有回到自己的 edge(吃 a, b)扣 1%
- 沒有畫到 input edge、accept 的雙圈圈皆扣 2%
- aa, bb 不能 accept 則全扣

4. (10%) Let G be the grammar:

$$S \rightarrow aB|bA$$

$$A \rightarrow a|aS|bAA$$

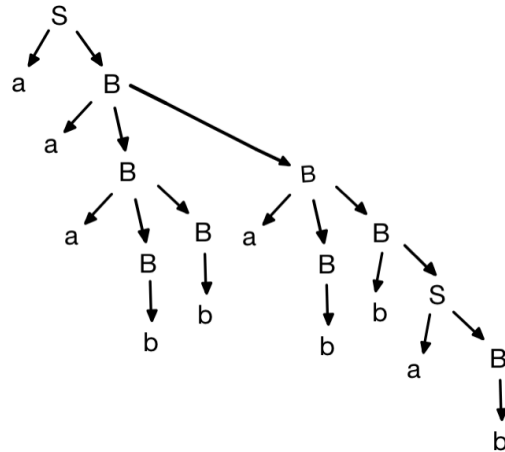
$$B \rightarrow b|bS|aBB$$

Find the leftmost derivation (3% *2) and parse tree (2% *2) for each following string.

a. (5%) aaabbabbab

ans:

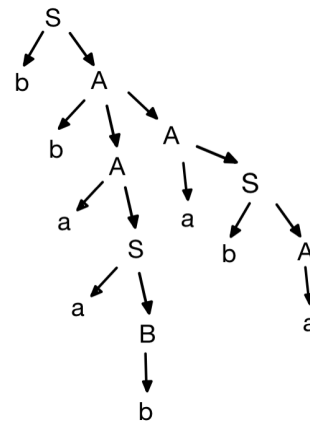
$S \rightarrow aB$
 $\rightarrow aaBB$
 $\rightarrow aaaBBB$
 $\rightarrow aaabBB$
 $\rightarrow aaabbB$
 $\rightarrow aaabbaBB$
 $\rightarrow aaabbabB$
 $\rightarrow aaabbabbS$
 $\rightarrow aaabbabbaB$
 $\rightarrow aaabbabbab$



b. (5%) bbaababa

ans:

$S \rightarrow bA$
 $\rightarrow bbAA$
 $\rightarrow bbaSA$
 $\rightarrow bbaaBA$
 $\rightarrow bbaabA$
 $\rightarrow bbaabaS$
 $\rightarrow bbaababA$
 $\rightarrow bbaababa$



- 多寫出其他 parse 的分支扣 1%
- 直接拆解 $A \rightarrow a|aaB|abA|bAA\dots$ 扣 2%
- 沒有遵守 leftmost 步驟(跳太快)扣 1%

5. (40%) For the following grammar, please do top-down parsing:

START \rightarrow EXPR \$

EXPR \rightarrow OP VAR | VAR OP M_VAR

VAR \rightarrow int | flo | (EXPR)

OP \rightarrow + | *

M_VAR \rightarrow VAR M_VAR | λ

START \rightarrow (1)

EXPR \rightarrow (2) | (3)

VAR \rightarrow (4) | (5) | (6)

OP \rightarrow (7) | (8)

M_VAR \rightarrow (9) | (10)

- (15%) First set
- (15%) Follow set
- (10%) LL(1) parsing table

FIRST	FOLLOW	Nonterminal
{+, *, int, flo, (}	{ \$ }	START
{+, *, int, flo, (}	{ \$,) }	EXPR
{int, flo, (}	{ \$, +, *, int, flo, (,) }	VAR
{+, *}	{int, flo, (, \$,) }	OP
{int, flo, (, ' }	{ \$,) }	M_VAR

註:答案中 FOLLOW(START) 要改為 { λ }

Nonterminal	int	flo	()	+	*	\$
START	START \rightarrow EXPR	START \rightarrow EXPR	START \rightarrow EXPR		START \rightarrow EXPR	START \rightarrow EXPR	
EXPR	EXPR \rightarrow VAR OP M_VAR	EXPR \rightarrow VAR OP M_VAR	EXPR \rightarrow VAR OP M_VAR		EXPR \rightarrow OP VAR	EXPR \rightarrow OP VAR	
VAR	VAR \rightarrow int	VAR \rightarrow flo	VAR \rightarrow (EXPR)				
OP					OP \rightarrow +	OP \rightarrow *	
M_VAR	M_VAR \rightarrow VAR M_VAR	M_VAR \rightarrow VAR M_VAR	M_VAR \rightarrow VAR M_VAR	M_VAR \rightarrow ' '			M_VAR \rightarrow ' '

	int	flo	()	+	*	\$
START	1	1	1		1	1	
EXPR	3	3	3		2	2	
VAR	4	5	6				
OP					7	8	
M_VAR	9	9	9	10			10

6. (10%) Given the grammar (upper cases are non-terminal, and the lower cases are terminal):

$$A \rightarrow Au \mid Ag \mid Ar \mid Be \mid Cs$$
$$B \rightarrow Bo \mid Ba \mid Al \mid Co$$
$$C \rightarrow Cu \mid Cr \mid At$$

Please convert left recursion to right recursion.

$$A \rightarrow BeA'$$
$$\mid CsA'$$
$$B \rightarrow CsA'lB'$$
$$\mid CoB'$$
$$A' \rightarrow uA'$$
$$\mid gA'$$
$$\mid rA'$$
$$\mid \epsilon$$
$$B' \rightarrow oB'$$
$$\mid aB'$$
$$\mid eA'lB'$$
$$\mid \epsilon$$
$$C \rightarrow uC$$
$$\mid rC$$
$$\mid sA'lB'eA'tC$$
$$\mid oB'eA'tC$$
$$\mid sA'tC$$
$$\mid \epsilon$$