The Bubble Algorithm Library: A Performance Evaluation

Group 5

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Contents

1	I Introduction															3
2	2 Hypotheses															3
3	B Materials & Me	${ m thods}$														4
	3.1 Variables								 	 						4
	3.1.1 Indep	endent variables							 	 						4
	3.1.2 Deper	ndent variables							 	 						4
	3.1.3 Contr	ol variables							 	 						4
	3.2 Design								 	 						5
																5
																6
	3.4.1 Projec	ct structure							 	 						6
	3.4.2 Source	e code, artifacts,	and	stat	tisti	cal:	files		 	 						7
	3.4.3 Result	ts reproduction s	steps						 	 						7
		rray size														8
		me														8
																8
		5														8
4	4 Results															8
	4.1 Data Sorting	and Array Size							 	 						8
	4.2 Data Type .							 •	 	 				•		9
5	5 Discussion															10
	5.1 Data Sorting								 	 						10
																10
	·															10
6	6 Conclusions															10

7	App	pendix												
	7.1	Bubble Sort Algorithms	1											
	7.2	Class Experiments	1											
	7.3	Summary Results	2											
	7.4	Data Sorting vs Array Size	2											
	7.5	Data Sorting vs Algorithm	2											

1 Introduction

Algorithm (in honour to mathematician Muhammad ibn Mūsā al-Khwārizmī)is the term used to refer to a set of ordered and finite well-defined instructions that enclose a process to do or achieve something specific. Algorithms, for example, can be seen as simple as a recipe for cooking a delicious meal, as complex as a flight collision avoidance system, or as beautiful as the creation of life. So when you think about algorithms, you realize that are simply part of everyday life. When we face the pragmatic side of an algorithm, we notice that is process or a technique for solving a given problem based on completing a set of tasks [9].

Programming languages serve as a natural-like language interface for programmers to encode algorithms that allow a general-purpose computer to execute the tasks designed to solve the proposed problems [8, 7]. In this way, these programs enable humans to simplify things while expanding their capabilities.

In computer science, the main question is how much time algorithms take to solve a problem. Generally, computer scientists determine the answer to this question based on the set of components that the algorithm acts on. For example, the processing time of an algorithm that finds the largest set in a database is relative to the size of the list. However, for the "slow" formula for sorting the numbers in the database from the smallest to largest, the execution time would be relative to the shape of the size of the list. This variation depends on whether the list is pre-sorted from the smallest to largest element, which is the worst case if the list is sorted from largest to smallest. The most representative scenario in real life is when the list is randomly sorted. In such a case, the average case scenario is considered. However, there is a general tendency among computer scientists to consider the complexity of an algorithm as the worst-case scenario, based on the concept of Murphy's Law, which states, "Anything that can go wrong will go wrong."

There are several ways to evaluate the execution of an algorithm, and the following categories are relevant to this research: Completeness, Optimality, Experience Quality, and Infinite Quality. An algorithm that is *complete* usually promises to obtain the solution, if there is one. An *optimal* al-

gorithm, is not only capable to find a solution, but to perform within the lowest cost (i.e. smallest Big O notation) [1, 3].

The minute quality of the algorithm quantifies the time it takes to finish the formula as an absolute number/length of the sequence. The *infinite quality* of the algorithm quantifies the amount of space it takes for the algorithm to successfully complete the formula.

Algorithmic efficiency refers to the features of an algorithm that are related to the number of computational resources required by the approach. It is possible to optimize a computer program such that it runs faster while using less memory, power, and other resources. Algorithmic efficiency is the same as technical productivity in a recurrent or continuous operation [5].

The biggest drawback of the algorithm formula is the hardware that has to hold all those nodes, compared to the level-first search algorithm, which has a minimal footprint. This leads to an exponentially infinite quality that can exhaust the free hardware on the computer within a few hours. Thus, the formula is impractical for significantly large problems.

Bubble, Inc. has requested us to analyze the execution time performance of their three in-place Bubble Sort algorithm candidates to choose which unique implementation we recommend to include in the library they are creating for Java developers.

This report describes our experiment's design decisions, the process we followed, the results we obtained, and our final recommendation.

2 Hypotheses

- Data sorting: When consider the input data, the complexity of the sorting of the data has an influence in the performance (running time) in any of the sorting algorithms being the presorted data in an ascending- the fastest, random- the average, and descending-data the slowest.
- Array size: When considering the length of the arrays, the running time will be directly proportional to the size of the input data. Being a large input-data set (10,000 elements) the slowest, compared to the smallest input

data set (100 elements). A middle size inputdata with 1,000 elements is also to be considered.

- Data type: There are two major considerations regarding data-type: Size and Nature. When considering the nature of data, the data with highest complexity (as a reference type), string, will take the slowest running time, whereas data-type of a number nature will run faster. Among these floating-point-number (4 Bytes) will have the slowest running time, followed by integer-number (4 Bytes) and short-number (2 Bytes) as the fastest number. Thus, the performance (time) will proceed as: string > float > integer > short.
- Algorithm (complexity): When considering the coding and algorithm complexity, the Bubble sort pass per item algorithm falls in the O(n²) will take the longest time, whereas a more refined Bubble sort until no change algorithm will run faster. The Bubble sort while needed algorithm will be the fastest, as it implements only if it is necessary to run a bubble sorting.

3 Materials & Methods

All experiments were performed in accordance with instructions from the course in Experimentation and Evaluation 2022 as part of the curriculum program for bachelor's in informatics of the Università della Svizzera italiana, Lugano, Switzerland.

3.1 Variables

3.1.1 Independent variables

Three major bubble sorting algorithms, provided by Prof. Dr. Gabriele Bavota, were evaluated and compared one another in this study (See Appendix Bubble Sort Algorithms):

- 1. Bubble sort pass per item
- 2. Bubble sort until no change
- 3. Bubble sort while needed

Variable	Levels
Algorithms	BubbleSortPassPerItem
	BubbleSortUntilNoChange
	BubbleSortWhileNeeded
Data Type	Floating-point number
	Integer
	Short
	String
Array Size	100 elements
	1,000 elements
	10,000 elements
Data Sorting	Ascending
Data Softing	
	Descending
	Random

Table 1: Independent variables. Four major independent variables where including in the study (left panel). Notice that input data of Floating-point number contains four decimals (i.e. 123.0000); integer contains numbers from -2,147,483,648 to 2,147,483,647; short contains numbers from -32,768 to 32,767). Strings contains only alphabetical words with length of five characters (Data Type, right panel).

3.1.2 Dependent variables

Variable	Measurement scale
Running time	nanoseconds (ns)

Table 2: Dependent variables. The performance of an algorithm is measured by the computation running time in ns (10^{-9} s) .

3.1.3 Control variables

The control variables can be found in table 3. Different factors within the machinery can be considered during the implementation of the sorting algorithms and measurement of the processing time (ns).

Each algorithm was run equally with a number of 1000 iterations times prior to data acquisition in order to prepare the system. All algorithms were executed using a Mac Mini Apple M1 chip (M1, 2020) with 8-Core GPU Family Apple 7 and 16-core Neural Engine, LPD DDR4 and 16 GB memory macOS Monterey v. 12.3 (21E230).

Any active software was reduced to contain only the necessary programs for the basic computer functioning. Data acquisition and data collection were performed without additional software and by using Java Virtual Machine with implementation of the version 17.0.1 of the Java SE Platform as specified by JSR 392. No internet connection of any kind was supplied during data acquisition. Data was collected and exported for off-line statistical analysis. A full repository of the implementation and supplementary material can be found on GitHub.

Variable	Fixed value								
Machine	Apple Mac Mini								
CPU	Apple M1 (2020) 8-core CPU								
Controller	iBoot-7459.101.2								
Graphics	Apple M1 8-core GPU, GPU Family Apple 7 Built-in bus								
Memory	16 GB LPDDR4								
Operating System	macOS Monterrey v.12.3 (21E230)								
Java version	17.0.1, 2021-10-19 LTS								
Java TM SE Runtime Environment	Build 17.0.1+12-LTS-39								
Java HotSpot TM	64-Bit Server VM, mixed mode, sharing								

Table 3: Control variables. The hardware and software properties of the machine needs to be considered when running the algorithms in different machines. Some machines have *per se* a better performance than others. A general description of the hardware and software used during experimentation is described above.

3.2 Design

Type of study: Experiment

Number of factors: Multi-Factor Design

We chose to analyze the Bubble Sort implementations with four different data types in distinct combinations of array sizes. This allowed us to measure our independent variable in three different configurations per stage, by reorganizing the data ordering each time.

The experiment was executed in sequence, one group after the other, as no multi-threading was implemented.

These groups could be considered dissimilar because of their technical nature of belonging to different types of objects. Nonetheless, randomized generation was our source of each group's population, and then, by configuration, we achieved homogenization by synchronizing the other independent variables. Figure 1 shows a simplified view of the groups configuration.

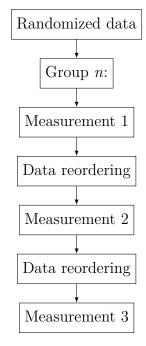


Figure 1: Simplified view of a multiple level experiment with multiple independent variables. Each group represent a combination of data type and array size. Every measurement represents the evaluation of the dependent variable with each of the algorithms. Each data reordering represents the order reorganization prior to each measurement.

3.3 Apparatus

The experimentation software was programmed and compiled on a MacBook Pro (15-inch, 2019) running macOS Catalina 10.15.7 (19H1715), with a 2.6 GHz 6-Core Intel Core i7 CPU and 6 GB 2400 MHz DDR4 of memory; wiht IntelliJ IDEA 2021.3.2 (Ultimate Edition) Build #IU-213.6777.52, built on January 28, 2022, and Java's JDK v.17 was used for the compilation.

All algorithms were executed using a Mac Mini Apple M1 chip (M1, 2020) with 8-Core GPU Family Apple 7, 16 GB LPD DDR4 memory, and macOS Monterrey v.12.3 (21E230).

3.4 Procedure

To run the experiment, we created an application that automates the initialization of our data and the execution of the measurements, results collection, and data processing.

The program allows the experiments to be fully — In the case of the strings, it will is customized by parameters-passing on invocation within words from the pre-filtered data. the restriction of a fixed set of data types. — After all randomized data are

The user can set the following variables declaring flags for:

- the number of iterations to run each instance of source data for each Bubble Sorting algorithm to evaluate
- the seed to initialize the randomized data generator
- the length of the strings to assess, the array sizes to use
- the last *n* number of results from the executed iterations to be considered for the data evaluation

The usage of the application is as follows:

```
java -jar BubbleSortExperiments.jar
  [-i <iterations>] [-s <seed>] [-l
  <string length>] [-a <array sizes>]
  [-n <last number of results>] [-h]
  [-r]
```

If the user does not provide any of those values, the system will execute with these default values:

• iterations: 1,000

• seed: Java standard random seed

• string length: 5 characters

• last number of results: 30

The user can also call the program with the -r flag to get a basic overview of the statistics of every iteration, or if needed, with the -h flag to get the usage details.

When invoked, the program looks on the disk for all pre-filtered files available, and if they match the string length, it will load it into memory. If no matching file exists, it will process an external file containing 370,103 unique strings and generate the corresponding filtered version. The files is located in data/all_strings.txt inside the working directory. The original file is publicly available¹.

The program then initializes the arrays that will hold the data to sort for each array size and type and populate them with randomly generated data. In the case of the strings, it will randomly take the words from the pre-filtered data.

After all randomized data arrays are generated according to the current array size and data type, the program is ready to enter the next phase, where data ordering comes to play.

One ordering type at a time, the program will create clones of the corresponding random array and run them sequentially through the provided Bubble Sort algorithms. Because the Enums are also sorted by default, the ascending array is processed first, the descending second, and the random third.

When finished, it continues to the following data type. When all data types for that array size are done, it will iterate again with the next array size if there is more than one.

Before the sorter in evaluation processes each configuration, an arbitrary total of seven garbage collection invocations are performed, aiming at clearing up the memory heap of unused objects [6].

Then a timer in nanoseconds precision is started and stopped right after the sorter finishes. Execution time is then calculated and collected in a Result class instance, which is pushed into a Result Stack. The measurements are collected for further processing to extract statistical data in the next stage.

The entire process concludes when a CSV file is generated and persisted on the hard drive.

3.4.1 Project structure

The source code of the experimentation program is structured inside the main package *ch.usi.ee*, where the *Main.java* class resides.

¹https://github.com/dwyl/english-words/
blob/master/words_alpha.txt

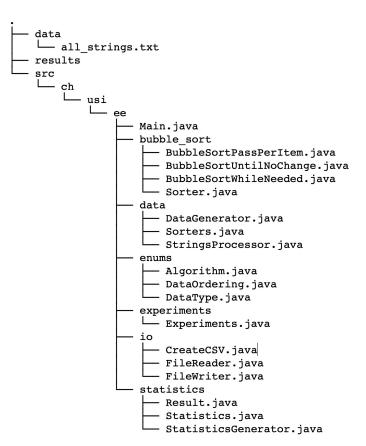


Figure 2: Package and classes structure of the project

The rest of the project was structured in six sub packages, considering future extensibility and maintainability. Here is their high level description:

- **bubble_sort**: contains the *sort* interface and the three implementations provided of Bubble Sort.
- data: contains the strings source file for the String processor, and the data generators and pre-sorter
- enums: contains Enum classes to describe the algorithms that can be tested, and the available data orderings and data types
- **experiments**: holds the class that executes the experiments
- io: manages all input and output data from and to the hard disk, as well as the creation of CSV files
- **statistics**: handles result holders and statistics generation

3.4.2 Source code, artifacts, and statistical files

When all the results are gathered, a custom-built statistics package is used to generate statistical data that is dumped in a CSV file that is timestamped and written in the folder results/ inside the working directory.

The source code of the experimentation software is available on GitHub². It contains also the project files for the IDE described in 3.2.

A pre-compiled JAR file can be downloaded from there 3 as well.

We made available on the repository all the files used for data analysis⁴, including the original output CSV file and a set of ten runs to corroborate for results consistency of the application.

3.4.3 Results reproduction steps

To reproduce the results the following instructions must be followed:

- a) Compile the source code according to the hardware specifications, IDE, and JDK described in 3.2. Alternatively, use the provided JAR file from 3.4.1.
- b) Place the JAR file in the desired folder.
- c) Create a subfolder named *data/* and copy into it the file *all_strings.txt*, also described in 3.4.1.
- d) Invoke the JAR file with the following command on a system with the characteristics described in:

```
java -jar
   BubbleSortExperiments.jar -i
   1000 -s 17072021 -1 5 -a
   100,1000,10000 -n 30
```

e) After the experiment is finished, a timestamped CSV results file will be available in the subfolder named results/

```
2https://github.com/erickgarro/
EE-Bubble-Sort-Experiments
  3https://github.com/erickgarro/
EE-Bubble-Sort-Experiments/blob/main/
artifacts/BubbleSortExperiments.jar
  4https://github.com/erickgarro/
EE-Bubble-Sort-Experiments/tree/main/
statistical_files
```

3.5 Input data array size

Each bubble sort algorithm requires input of an array of type Comparable, an interface that makes the comparison between objects more effortless [4]. As such, they can contain objects of other data types. For example, our case had String (with a predefined length of five with alphabetical characters), floating-point-, integer-, and short-numbers.

Three representative lengths of the array were chosen (100, 1000, and 10000).

In addition, the data within the array was presorted following an ascending, descending or random order (java.util.Random).

3.6 Processing time

The performance of each Bubble algorithm is determined by using Java System.nanoTime(). During data acquisition, to avoid external added time, the time was calculated by the difference between processing time preceding and after running each Bubble sorter algorithm. Thus, an actual total processing time per iteration (See Class Experiments line 201-206, elapsedTime) was considered for the data analysis.

Each bubble sorting algorithm was run $\sim 1,000$ each time (total iterations) before collecting data. A total of thirty processing time acquisitions (last thirty per experimental set) were collected per experimental set. The collected data was summarized in a table (See Summary Results) and exported a single CSV file for offline analysis.

3.7 Data Entry

The Class Experiments contributed to the processing and collecting of the data with the performance (processing time, ns) of the multiple combination of each of the independent variables.

Each of the bubble sort algorithms took as input an array of elements belonging to a combination of one of each of the following categories: Data type, array size, and data sorting (See Fig. 3).

We constructed multiple combinations or configurations for the data input iteratively for each measurement as follows: first, we choose data type, then array size, and last data ordering. After each data configuration was complete, we ran it through each sorter in order, as described in 3.3.

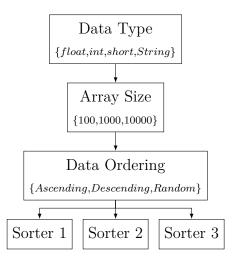


Figure 3: Input data. Each of the input data was the product of a combination of the main variables (See Independent variables). Data type consisted of floating-point-, integer- or, short-number or String of length five. Array size has 100, 1,000 or 10,000 elements. Data sorting arranges the data arrays in ascending, descending or random order. Sorter is a comparable option among three algorithms BubbleSortPassPerItem, BubbleSortUntilNoChange or BubbleSortWhileNeeded

3.8 Data analysis

The data was analysed by using functions within Java Statistical Packages and IBM® SPSS® Statistics version 27, 64-bit edition. The paired-sample t-test was used to compared data within the same experimental group input, whereas the Wilcoxon-Mann-Whitney test were used for comparison between different groups. The results are presented as mean \pm SEM (standard error of the mean) with the level of significance set as *p < 0.05.

4 Results

4.1 Data Sorting and Array Size

Data sorting has a fundamental role when considering the size of the array that will be sorted in each algorithm. As shown in figure 4, the array data inputed into the algorithms performs better on data pre-sorted on an ascending manner (n=36 experiments, 3.85×10^7 ns $\pm 1.61 \times 10^8$ ns). This behaviour was observed for each algorithm, particularly when array data size was 1000 and 10000 elements (See Data Sorting vs Array Size). The second most efficient array-sorting-data input was the descending sorting (n=36 experiments, 1.086×10^8 ns $\pm 1.92 \times 10^8$ ns), followed by random sorting (n=36

experiments, $1.39 \times 10^8 \text{ ns} \pm 2.78 \times 10^8 \text{ ns}$).

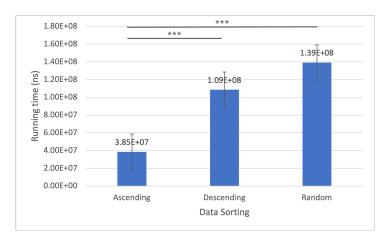


Figure 4: Data sorting. The processing time (ns) of three main array input sorted by ascending, descending or random (n=36 total experiments. 12 experiments per case). All data including array size, data type and algorithm type were added in the analysis. Notice that the ascending sorting has a better performance compared to descending or random sorting arrays. Mean±SEM. ***, P<0.001 by Mann-Whitney test.

When taking into consideration each bubble sort algorithm and the pre-ordering of data, we observe once more the advantage that ascending pre-sorted array presented compared to descending or random array inputs. The processing time of the bubble sort until no change (n=12 experiments, $1.65 \times 10^4 \pm$ 3.13×10^4 ns) and bubble sort while needed (n=12) experiments, $1.63 \times 10^4 \pm 3.39 \times 10^4$ ns) algorithms, which were relatively similar each other, were significantly different compared to its pair-set algorithm, bubble sort pass per item, or any other combination for the descending or random array. In the case of descending- vs random-sorted arrays, as shown in figure 5, the data presented a similar behaviour. Despite the relatively rapid processing time in the descending-bubble sort while needed algorithm (Fig. 5 center, WN, descending) compared with its pair algorithms, the values were not significantly different one another.

4.2 Data Type

The leading six worst performance, as running time (ns), experiments were strings. In fact, the worst performance observed among of all data series was an array random-sorted of strings running the bubble sort until no change algorithm, followed by string random bubble sort pass per item algorithm. We observed that String data type (n=27 experiments, $3.66 \times 10^5 \pm 7.47 \times 10^5$ ns) has the worst processing time

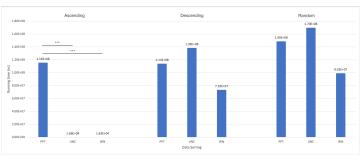


Figure 5: Data sorting per algorithm. The processing time (ns) resulting of the input-array data pre-sorted as ascending, descending or random where compared with each of the three bubble sort algorithms (BS) 1) BS per item (PPT) 2) BS until no change (UNC) 3) BS while needed (WN). The processing time (ns) of three main array input sorted by ascending, descending or random (n=36 total experiments). Four experiments were grouped in each set, each corresponding to data type:floating-point-, integer-, short-number, or String. The ascending sorting has a better performance compared to descending or random sorting arrays. Mean±SEM. *, P<0.05; ***, P<0.001 by Mann-Whitney test.

comparing to its pairs floating-point number (n=27 experiments, $2.49 \times 10^4 \pm 5.68 \times 10^4$ ns), integer number ((n=27 experiments, $2.47 \times 10^4 \pm 6.88 \times 10^4$ ns)), short number (n=27 experiments, $5.83 \times 10^4 \pm 1.40 \times 10^5$ ns). As shown in figure 6, string was significantly different from any of its pair sample data types, discriminating array size or type of algorithm.

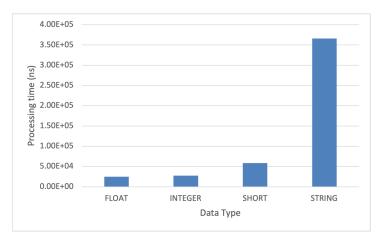


Figure 6: Data Type. The processing time (ns) resulting of the data type floating-point-, integer-, short-number, and string (n=27 total experiments). Four experiments were grouped in each set, each corresponding to data type:floating-point-, integer-, short-number, or String. The ascending sorting has a better performance compared to descending or random sorting arrays. The string has the worst performance, followed by short.

Once we performed a more refined sectioning of the data (See Fig. 7), we clearly observed that the main algorithms contributing to a bad processing time are Bubble Sort Pass Per Item (n=9 experiments,

 $5.89 \times 10^5 \pm 1.40 \times 10^5$ ns) and Bubble Sort Until No Change ((n=9 experiments, $4.13 \times 10^5 \pm 8.26 \times 10^5$ ns)

algorithms, whereas the Bubble Sort while needed algorithm (n=9 experiments, $4.13 \times 10^5 \pm 8.26 \times 10^5$ ns) was significantly faster than its pairs.

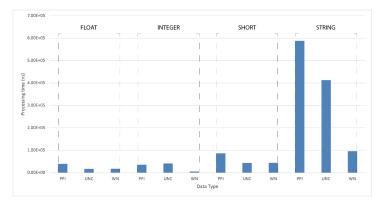


Figure 7: Data Type per algorithm. The processing time (ns) resulting of the data type four data types floating-point-, integer-, short-number, and string where compared with each of the three bubble sort algorithms (BS) 1) BS per item (PPT) 2) BS until no change (UNC) 3) BS while needed (WN). The processing time (ns) of three main array (n=9 per experimental group).

5 Discussion

5.1 Data Sorting

As initially hypothesized, our data (See Data Sorting and Array Size) proves that the data sorted in an ascending manner will have a better performance regardless of the type of algorithm since this is the best case-scenario were the bubble sort algorithm, theoretically, does not have to sort any single element.

One of the aspects we clearly observed is the inefficacy of the the Bubble Sort Pass Per Item algorithm. Despite of having a pre-sorted array of elements, we observed that the processing time was the worst among the three algorithms regardless of data type or size. Another interesting aspect that needs to be highlighted when determine the array sorting is the random sorting.

Opposite to what we initially considered, where the worst complexity would be given by a descending order array, the random sorting presented the slowest running time. A possible attribution to this behaviour is that after several iterations of the a < b comparison will continue to be false, leading to a branch prediction heuristic that will assume the same outcome for the upcoming comparisons[2].

5.2 Array size

In regards to array sizes, we confirmed our hypothesis where the running time would be proportional to the length of the arrays. Larger arrays take longer to be processed. Nonetheless, is notable the repetition of the patter, where in the cases of size 1000 and 10000, Bubble Sort Pass Per Item has the worst performance, and the Bubble Sort Until No Change and Bubble Sort While Needed perform similarly.

5.3 Data type

Recapitulating our hypothesis related to data types, we originally said that in terms of execution time, string > float > integer > short

but we found out that they perform as follows:

string > short > float > integer

String: takes the longest processing time since it is a complex data type (a reference kind, not a number as all the others). It takes longer to fetch information from memory and process it.

Short: short also takes long processing times as the computer architecture (64-bit) is designed to pass data in chunks of 4 Bytes. Then, the fact that short has 2 bytes, does not make it more efficient. On the contrary, it makes the machine (possibly) to save the information in chunks of 4 bytes, take that and extract the (first or second) 2 bytes to pass it. This process is tedious and occupies memory.

Floating-point: either floating or integer contain 4 bytes, however floating point has extra information. It needs to process information (depending on the machinery) by using i.e. one's complement to store data, re transform it as a floating, hence, this processing takes time.

Integer: this is the fastest since the machinery is designed to pass and get numbers.

6 Conclusions

The main focus of this report, presented three algorithm based solutions *Bubble Sort Pass Per Item*

(PPT), Bubble sort until no change (UNC) and Bubble Sort While Needed (WN, See Bubble Sort Algorithms) for complex array data input containing a variation in data types, array sizes and array sorting. We have concluded that the best algorithm that the Bubble Inc. company can use to implement its library is the Bubble Sort While Needed.

Despite the poor execution time presented when including data of either *String* or *short* number type, it shows the least poor performance among the different bubble sort algorithms between all data set

First of all, when we observed the performance of pre-sorted data, the test cases data clearly indicates that the ascending data arrays irrespective of the data type or the pattern length presented a reduced processing data cost.

Second, the array size has a detrimental role in each of the bubble sort algorithms. The input data with a higher array size has a the worst performance. Particularly, this behaviour is clearly observed in the PPI algorithm.

During this study, we acknowledge that we compared small data sets with less than 10,000 elements. However, we noticed a clear pattern when increasing array data size, particularly for PPI. We infer that really complex data input with exponentially increased values would have a low performance, however further experiments with bigger that sets would need to be implemented to conclude this.

Furthermore, when applying complex data types, bigger size arrays perform the least. Therefore, we do not recommend to include this PPI algorithm in the library.

Finally, the data type with integer number has the highest-throughput computational experimental screening. Possibly due to hardware architecture and JVM that favours this performance by facilitating resource allocation and memory processes. We suspected that the memory size demands increase with the size of the input array.

Evidently the implementation of multi-threading and memory allocation would increase the performance of each algorithm. Further studies would be suggested on this regards, possibly by implementing the given bubble sorting algorithms in a language such as C-programming.

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7 Appendix

7.1 Bubble Sort Algorithms

Interface Sorter

```
public interface Sorter<T extends Comparable<T>> {
   public abstract void sort(final T[] items);
}
```

Class Bubble sort pass per item

Class Bubble sort until no change

```
public final class BubbleSortUntilNoChange<T extends Comparable<T>> implements
Sorter<T> {

public void sort(final T[] items) {
    boolean changed;
    do {
        changed = false;
        for (int i = 0; i < items.length-1; i++) {
            if (items[i].compareTo(items[i + 1]) > 0) {
                final T item = items[i];
                items[i] = items[i+1];
               items[i] = item;
                changed = true;
            }
        }
     }
     while (changed);
}
```

Class Bubble sort while needed

```
public final class BubbleSortWhileNeeded<T extends Comparable<T>> implements
      Sorter<T> {
4
      public void sort(final T[] items) {
5
         int n = items.length;
6
         do {
            int maxIndex = 0;
            for (int i = 1; i < n; i++) {</pre>
10
                if (items[i - 1].compareTo(items[i]) > 0) {
11
                   final T item = items[i - 1];
                   items[i - 1] = items[i];
                   items[i] = item;
14
                   maxIndex = i;
15
16
17
            n = maxIndex;
18
         \} while (n > 0);
      }
20
21
```

7.2 Class Experiments

Class Experiments

```
public class Experiments {
30
      * This function executes the experiments and returns the results.
31
      * @param rand The random number generator.
      * @param arraySizes The array sizes to be tested.
      * @param totalIterations The total number of iterations.
35
      * @param dataTypes The data types to be tested.
36
      * @param dataOrderings The data orderings to be tested.
37
       * @param stringsSourceFile The source file for the strings to be selected
      * @return The results of the experiments.
39
      * @throws IOException If the source file is not found.
41
     public static Stack<Result>[] runExperiments(Random rand, Stack<Long>
42
         arraySizes, int totalIterations, DataType[] dataTypes, DataOrdering[]
         dataOrderings, String stringsSourceFile) throws IOException {
         int numberOfAlgorithms = 3;
         String[] filteredStrings = readData(stringsSourceFile);
44
         Stack<Result> BubbleSortPassPerItemResults = new Stack<Result>();
46
         Stack<Result> BubbleSortUntilNoChangeResults = new Stack<Result>();
         Stack<Result> BubbleSortWhileNeededResults = new Stack<Result>();
         Stack<Result>[] allResults = new Stack[numberOfAlgorithms];
49
         Stack<Result> results;
51
         Sorter[] sorters = new Sorter[numberOfAlgorithms];
         sorters[0] = new BubbleSortPassPerItem();
         sorters[1] = new BubbleSortUntilNoChange();
         sorters[2] = new BubbleSortWhileNeeded();
56
         System.out.println("\nRunning experiments...");
57
         Comparable[] randomIntegers = null, sortedIntegers = null, reversedIntegers
            = null;
         Comparable[] randomShorts = null, sortedShorts = null, reversedShorts =
60
            null:
         Comparable[] randomFloats = null, sortedFloats = null, reversedFloats =
61
         Comparable[] randomStrings = null, sortedStrings = null, reversedStrings =
            null;
         // Guards to avoid an error due to the available filtered strings being
64
         long maxArraySize = 0;
         for (int i = 0; i < arraySizes.size(); i++) {</pre>
            if (maxArraySize == 0) {
```

```
maxArraySize = arraySizes.get(i);
   } else {
      if (arraySizes.get(i) > maxArraySize) {
         maxArraySize = arraySizes.get(i);
   }
}
if (arraySizes.lastElement() > filteredStrings.length) {
   System.out.println("\nThe filtered strings source file does not have
      enough strings to fill your largest array size.");
   System.out.println("There are only " + filteredStrings.length + "
      strings in the filtered strings source file.");
   System.out.println("Please, decrease the array sizes of your largest
      array or try a different string size.");
   exit(1);
}
Comparable[] toSort = null;
for (DataType type : dataTypes) {
   for (Long arraySize : arraySizes) {
      int size = arraySize.intValue();
      randomIntegers = generateRandomIntegers(rand, size);
      randomShorts = generateRandomShorts(rand, size);
      randomFloats = generateRandomFloats(rand, size);
      randomStrings = generateRandomStrings(rand, size, filteredStrings);
      System.out.println("\nArray size: "+ size );
      for (DataOrdering ordering : dataOrderings) {
         switch (type)
            case INTEGER:
               switch (ordering) {
                  case RANDOM:
                     toSort = randomIntegers.clone();
                     break;
                  case ASC:
                     sortedIntegers = (Comparable[])
                        Sorters.quickSort(randomIntegers.clone(), 0, size -
                     toSort = sortedIntegers.clone();
                     break:
                  case DESC:
                     reversedIntegers =
                        Sorters.reverseArray(sortedIntegers.clone(),
                        size).clone();
                     toSort = reversedIntegers.clone();
                     break;
                  default:
```

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```
System.out.println("Invalid ordering");
         exit(1);
         break;
   }
  break;
case SHORT:
   switch (ordering) {
      case RANDOM:
         toSort = randomShorts.clone();
         break;
      case ASC:
         sortedShorts = (Comparable[])
            Sorters.quickSort(randomShorts.clone(), 0, size -
         toSort = sortedShorts.clone();
         break:
      case DESC:
         reversedShorts =
            Sorters.reverseArray(sortedShorts.clone(),
            size).clone();
         toSort = reversedShorts.clone();
         break;
      default:
         System.out.println("Sorting order not supported");
         exit(1);
         break;
   break;
case FLOAT:
   switch (ordering) {
      case RANDOM:
         toSort = randomFloats.clone();
         break;
      case ASC:
         sortedFloats = (Comparable[])
            Sorters.quickSort(randomFloats.clone(), 0, size -
            1);
         toSort = sortedFloats.clone();
         break;
      case DESC:
         reversedFloats = Sorters.reverseArray(sortedFloats,
            size).clone();
         toSort = reversedFloats.clone();
         break;
      default:
         System.out.println("Invalid ordering");
         exit(1);
         break;
   }
  break;
case STRING:
   switch (ordering) {
```

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```
case RANDOM:
            toSort = randomStrings.clone();
            break:
         case ASC:
            sortedStrings = (Comparable[])
               Sorters.quickSort(randomStrings.clone(), 0, size -
               1);
            toSort = sortedStrings.clone();
            break;
         case DESC:
            reversedStrings =
               Sorters.reverseArray(sortedStrings.clone(),
               size).clone();
            toSort = reversedStrings.clone();
            break:
         default:
            System.out.println("Invalid ordering");
            exit(1);
            break;
      }
      break;
   default:
      System.out.println("Type not implemented");
      exit(1);
      break;
}
int allResultsArrayIndex = 0;
for (Sorter sorter : sorters) {
   String className =
      sorter.getClass().getName().split("\\.")[sorter.getClass().getName
  Result iteration_result = new Result(type, ordering, className,
      size, totalIterations);
   if (sorter instanceof BubbleSortPassPerItem) {
      iteration result.setAlgorithm(BUBBLE SORT PASS PER ITEM);
      results = BubbleSortPassPerItemResults;
   } else if (sorter instanceof BubbleSortUntilNoChange) {
      iteration_result.setAlgorithm(BUBBLE_SORT_UNTIL_NO_CHANGE);
      results = BubbleSortUntilNoChangeResults;
   } else {
      iteration_result.setAlgorithm(BUBBLE_SORT_WHILE_NEEDED);
      results = BubbleSortWhileNeededResults;
   }
   System.out.print(iteration_result.getAlgorithm() + " | " +
      iteration_result.getDataType() + " | " +
      iteration_result.getDataOrdering() + "... ");
   forceGarbageCollection();
```

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```
for (int i = 0; i < totalIterations; i++) {</pre>
201
                           long startTime = System.nanoTime();
202
                           sorter.sort(toSort.clone());
203
                           long endTime = System.nanoTime();
204
205
                           long elapsedTime = endTime - startTime;
                           iteration_result.addElapsedTime(i, elapsedTime);
206
                        }
207
208
                        System.out.println("\t\t\Done!");
209
                        results.push(iteration_result);
210
                        allResults[allResultsArrayIndex++] = results;
211
                 }
213
              }
214
215
          }
216
          return allResults;
217
218
       }
219
220
       * Runs garbage collection to free up memory
221
222
       private static void forceGarbageCollection() {
          for (int i = 0; i < 6; i++) {</pre>
^{224}
              System.gc();
225
226
          }
       }
227
228
```

7.3 Summary Results

									results											
Algorithm BUBBLE_SORT_PASS_PER_ITEM	Data Type		Array size		Standard error 42.414082654319000	Mean 6548.63333333333	Minimum time 6417	Maximum time 578959	Median 6500.0	N last iterations		Third quartile 6500.0	Interquartile range 0.0	First result 578959.0	Last result 6459.0	v_0 6500	v_1 6500	v_2 6541	v_3 6500	v_4 7792
BUBBLE_SORT_PASS_PER_ITEM		RANDOM	100		229.06055717179200		13791	356792	13875.0	30		13917.0	83.0	356792.0	13833.0	13833	13875	13875	20875	
BUBBLE_SORT_PASS_PER_ITEM	INTEGER		100		8.943766710003280		17708	22916	17791.0	30		17833.0	83.0	20417.0	17750.0	17708	17792	17792	17875	-
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	INTEGER	ASC RANDOM	1000		3172.806231112320 788.3711830237220	872045.8333333333 1365011.0	863583 1355709	984375 1475083	866459.0 1364459.0	30		870291.0 1368291.0	6457.0 5625.0	870042.0 1365083.0	866583.0 1368291.0	866333 1366166	901084	943875 1363917	917417 1363833	866459 1366708
BUBBLE_SORT_PASS_PER_ITEM	INTEGER	DESC	1000	5184.3019035031800	946.5196991552210	1638734.8	1633042	1777958	1636834.0	30		1638750.0	2500.0	1638792.0	1636834.0	1634042	1633834	1638708	1646041	1638750
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	INTEGER		10000	749024.5210529490 560539.268303964		9.0484857E+07 1.531036513E+08	88916875 151513541	95182500 165465625	9.081675E+07 1.5296175E+08	30		9.090575E+07 1.53479E+08	159000.0 807583.0	8.9725292E+07	9.0891625E+07	90909833 153731500	90845709 153205458	90798917 153597583	90794125 153479000	
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	INTEGER	DESC	10000	560539.268303964 417690.14720494700		1.531036513E+08 1.648164139E+08	151513541	165465625		30			807583.0 70375.0	1.52721708E+08 1.65311916E+08	1.53462625E+08 1.64865958E+08	153731500		153597583 164723958	153479000	
BUBBLE_SORT_PASS_PER_ITEM	FLOAT	ASC	100	189.6646748577310	34.62787359382080	11872.3333333333300	11208	392125	11792.0	30	11708.0	12083.0	375.0	392125.0	12167.0	12084	11667	12083	11834	1195
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	FLOAT	RANDOM	100	41.54510266632590 31.0439831350439			18416 23500	356625 29875	18500.0 23583.0	30		18541.0 23584.0	82.0 1.0	356625.0 29875.0	18459.0 23584.0	18500 23584	18541 23583	18458 23583	18542 23584	1854 2354
BUBBLE_SORT_PASS_PER_ITEM	FLOAT	ASC	1000	3265.585032663450			1098125	1143042	1099458.0	30		1099959.0	1043.0	1143042.0	1099292.0	1098792	1099708	1098834	1099125	
BUBBLE_SORT_PASS_PER_ITEM	FLOAT	RANDOM	1000		610.7205154569480	1847948.6	1838333	1891541	1848584.0	30		1850208.0	3750.0	1857041.0	1848875.0	1850583	1848041	1852000	1851792	
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	FLOAT	DESC	1000	1478.5581794437400		2201636.1	2200667	2343917	2200917.0	30		2202167.0	1334.0 1963584.0	2343917.0 1.14233833E+08	2200875.0 1.11641042E+08	2202292 113677084	2200833 113701792	2201000	2200833 113655875	220087
BUBBLE_SORT_PASS_PER_ITEM	FLOAT	RANDOM	10000	829328.0657304720		2.30328354233333E+08	223750958	233334292		-	2.29883666E+08	2.30734583E+08	850917.0	2.30377334E+08		229773625			230789417	23080079
BUBBLE_SORT_PASS_PER_ITEM	FLOAT	DESC	10000			2.24304140233333E+08	219933292		2.24320292E+08		2.24227583E+08		132084.0	2.20330375E+08	2.24227583E+08	224344083	224241875	224400417	224330000	
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	SHORT	RANDOM	100	48.36119886391940 46.45265211900060	8.829506508587290 8.481055140505590		22541 28750	355000 40375	22709.0 28917.0	30		22750.0 28958.0	42.0 42.0	355000.0 39625.0	22792.0 28875.0	22750 28917	22708 28917	22750 28917	22709 28916	2275
BUBBLE_SORT_PASS_PER_ITEM	SHORT	DESC	100	42.809773027507000		31627.7	31417	40208	31625.0	30		31666.0	82.0	35000.0	31666.0	31625	31708	31666	31666	3162
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	SHORT	ASC RANDOM	1000	3940.707635268910	719.4714881232070 876.8664917171240		2204083 2745750	2385167 2919959	2240334.0 2759917.0	30		2245125.0 2764500.0	6000.0 8083.0	2204083.0 2761750.0	2239042.0 2760459.0	2247584 2765042	2239125 2756708	2243750 2759334	2246208 2759166	
BUBBLE_SORT_PASS_PER_ITEM	SHORT	DESC	1000		1154.2251299112000		3081625	3284208	3119250.0	30		3124917.0	7500.0	3081625.0	3121417.0	3117250	3115416	3114417	3118208	311466
BUBBLE_SORT_PASS_PER_ITEM	SHORT	ASC	10000	96083.37279213410		2.28043227766667E+08	227906541		2.28016125E+08		2.27996416E+08		48084.0				228006875		228026042	
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	SHORT	RANDOM	10000	3036316.7770154700 1123270.0486358600		3.365711944E+08 3.149269263E+08	330380292	511501333 333089833		30		3.39266458E+08 3.159175E+08	5716833.0 1833833.0	3.43793E+08 3.16466166E+08	3.35915375E+08 3.15960042E+08	341383833 315987042		339239583 315869875	341309250 315903958	
BUBBLE_SORT_PASS_PER_ITEM	STRING	ASC	1000		6.097722707882200	3.149269263E+08 38357.0	311741584	333089833	3.14674958E+08 38375.0	30		3.159175E+08 38375.0	1833833.0	3.16466166E+08 309250.0	3.15960042E+08 38334.0	315987042	316003125	315869875	315903958	3162913
BUBBLE_SORT_PASS_PER_ITEM	STRING	RANDOM	100	474.2966500221380			54375	73375	54500.0	30		54542.0	84.0	73375.0	54500.0	54458	54458	54500	54458	571:
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	STRING	DESC	100	493.67092165620700 31462.474841291300	90.1315665918234 5744.235728504680	47684.76666666670 4700395.833333333	47500 4558000	58000 6640458	47584.0 4696416.0	30		47625.0 4713791.0	42.0 29916.0	55709.0 5178167.0	47625.0 4714125.0	47625 4720958	47625 4720333	47542 4834375	47583 4703917	
BUBBLE_SORT_PASS_PER_ITEM	STRING	RANDOM	1000	31820.730209444000			7449542	8015125	7633875.0	30		7656708.0	38166.0	7518750.0	7710917.0	7630500	7678917	7630000	7633875	75902
BUBBLE_SORT_PASS_PER_ITEM	STRING	DESC	1000	13522.708615469300		4939333.366666670 9.47196080566667F±08	4910000	5320167	4938417.0	30		4949042.0	19208.0	5160250.0	4964458.0	4931750	4949791	4919417	4941458	49428
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	STRING	RANDOM	10000			9.47196080566667E+08 1.05015707776667E+09	904143417		9.52158667E+08 1.054430583E+09	30	9.313625E+08 1.045139667E+09		2.7866083E+07 1.1035708E+07		9.26985084E+08 1.067714209E+09	931362500	937516750 1046385167	938995958 1058116916	931792125 1056175375	
BUBBLE_SORT_PASS_PER_ITEM	STRING	DESC	10000	5219019.279548160	952858.1958209630	6.52845247266667E+08	646248291	701548750	6.51061417E+08	30	6.49277833E+08	6.55652542E+08	6374709.0	6.76112583E+08	6.53633625E+08	658944833	655652542	648435000	648773500	64927783
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	INTEGER		100		4.2982382265123300 6.4234639322478400		583	11666	625.0	30		625.0	0.0	11666.0	709.0	625	583	583	625	
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	INTEGER	RANDOM DESC	100		6.4234639322478400 7.733259099260560	16352.8 22234.6333333333300	16250 22125	201666 31708	16375.0 22250.0	30		16375.0 22250.0	42.0 42.0	201666.0 27125.0	16375.0 22166.0	16334 22250	16417 22166	16292 22291	16375 22250	1637
BUBBLE_SORT_UNTIL_NO_CHANGE	INTEGER	ASC	1000		152.21511447315000		1625	6834	1708.0	30	1667.0	1708.0	41.0	6834.0	1750.0	1667	1667	1708	1666	170
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	INTEGER		1000		673.7225300110160 619.4302775460210	1691910.9	1685542 2137666	1813833	1691125.0 2141042.0	30		1694416.0 2147083.0	5250.0 6583.0	1721875.0 2147291.0	1689375.0 2147375.0	1688416 2141667	1689166	1689583 2140458	1698250 2147083	214033
BUBBLE_SORT_UNTIL_NO_CHANGE	INTEGER	ASC	10000		121.09318358648900	18426.4	14625	284083	18500.0	30		18875.0	1000.0	17917.0	18500.0	18250	19000	18083	19042	1808
BUBBLE_SORT_UNTIL_NO_CHANGE	INTEGER	RANDOM	10000	1776292.9831422600		1.84092254233333E+08	181340291	187497750	1.8528125E+08	30		1.85527125E+08	3521416.0	1.83048917E+08	1.81557167E+08	185281250	185708167	185527125	185315542	18536133
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	INTEGER	DESC	10000		44383.50974455700 15.413881430085700	2.16991190333333E+08 2716.633333333333	212844292 2625	218688666 21625	2.16934208E+08 2708.0	30		2.16976375E+08 2709.0	67084.0 42.0	2.13347292E+08 21625.0	2.16928584E+08 2666.0	216954625 2708	216993917 2666	216914333 2667	216918042 2709	21691633
BUBBLE_SORT_UNTIL_NO_CHANGE	FLOAT	RANDOM	100	42.6590618222618	7.788443480686740	20656.933333333300	20542	324750	20666.0	30	20625.0	20667.0	42.0	324750.0	20708.0	20625	20667	20625	20667	2070
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	FLOAT	DESC	100		8.518826644990930 5.683181816162100		27875 1791	34292	28000.0 1875.0	30		28000.0	42.0 42.0	34292.0 6084.0	27958.0	28042	27959 1875	28000	27959	-
BUBBLE_SORT_UNTIL_NO_CHANGE	FLOAT	RANDOM	1000	1570.8165463294000		1861.1 2126815.3333333300	2121333	6084 2193833	2127083.0	30		2127708.0	42.0 2291.0	2134875.0	1833.0 2127208.0	1834 2128375	2127375	1959 2126709	1833 2126625	183 212520
BUBBLE_SORT_UNTIL_NO_CHANGE	FLOAT	DESC	1000		188.16597874099200	2608961.0	2608125	2749791	2608292.0	30		2609708.0	1458.0	2616375.0	2608250.0	2609666	2608250	2608167	2608208	260970
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	FLOAT	RANDOM	10000		135.37855032791900	19756.9 2.52781626433333E+08	16583 250395959	225459	19792.0 2.52482791E+08	30		20333.0 2,52912E+08	1208.0	20917.0 2.56830209E+08	20167.0 2.52167125E+08	20375 254247584	20333 253866958	19375 252086958	20458 253992334	1950 25234420
BUBBLE_SORT_UNTIL_NO_CHANGE		DESC	10000			2.65158047233333E+08	259975041		2.65127417E+08		2.65109583E+08		132292.0	2.6025775E+08		265129833			265114167	
BUBBLE_SORT_UNTIL_NO_CHANGE	SHORT	ASC	100	17.693564429538300			584	13708	667.0	30	666.0	667.0	1.0	13708.0	667.0	667	667	667	667	62
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	SHORT	RANDOM	100	187.95449803964100 534.3584117633240	34.31563945362390 97.56005197180220	32304.2 36223.566666666700	31792 35375	106417 55625	32292.0 36125.0	30	32125.0	32500.0 36167.0	375.0 84.0	106417.0 39417.0	32541.0 36083.0	32500 36041	32042 36292	32125 36208	32500 36208	3229 3620
BUBBLE_SORT_UNTIL_NO_CHANGE	SHORT	ASC	1000		4.177900411911690		2708	5375	2792.0	30		2792.0	1.0	5375.0	2792.0	2791	2792	2792	2791	283
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	SHORT	RANDOM	1000	11587.77599642540 4507.082701334280	2115.62876818637 822.8769546873670	3748383.3 3483615.3	3722292 3426333	3919625 3646625	3747125.0 3483791.0	30		3753750.0 3486250.0	12792.0 6958.0	3770041.0 3426333.0	3750875.0 3486250.0	3744834 3480917	3747541 3479250	3752375 3485750	3747125 3483584	373525 348633
BUBBLE_SORT_UNTIL_NO_CHANGE	SHORT	ASC	10000		161.17426283374200	30206.9	27041	216834	30208.0	30		30542.0	959.0	31041.0	29917.0	30250	29083	30458	29333	3029
BUBBLE_SORT_UNTIL_NO_CHANGE	SHORT	RANDOM	10000			4.19288336166667E+08	414477625	428032458		30			2550833.0	4.19954667E+08		418102167		417242958	419049583	
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	SHORT	DESC	10000		61061.849182024400 3.778986734660600	3.50167963866667E+08 601.3333333333333	349862458 542	363880500 16042	3.50090959E+08 584.0	30		3.50146291E+08 625.0	132291.0	3.50607334E+08 16042.0	3.50121875E+08 584.0	351415833 625	350174000 625	349991291 584	349982417 584	35027208
BUBBLE_SORT_UNTIL_NO_CHANGE		RANDOM	100		9.521960971393490		62291	83792	62500.0	30		62542.0	84.0	78917.0	62500.0	62458	62416	62542	62541	6245
BUBBLE_SORT_UNTIL_NO_CHANGE	STRING	DESC	100	796.7245927336920		60008.3	59666	70125	59875.0	30		59875.0	42.0	67833.0	59875.0	59833	59875	59875	59875	5983
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	STRING	RANDOM	1000	51.21636023338200 46710.357509467000	9.350785271044630 8528.105492355310		7833 8810500	16792 9415459	7959.0 8879458.0	30		8000.0 8904459.0	42.0 49417.0	16792.0 9077458.0	8041.0 8995000.0	7917 8882875	8000 8879458	8000 8840292	7959 8864958	804 883291
BUBBLE_SORT_UNTIL_NO_CHANGE	STRING	DESC	1000	24126.306385262400	4404.840745496390	6515695.933333333	6469792	7101584	6516584.0	30	6498750.0	6529667.0	30917.0	6721583.0	6592375.0	6529666	6521625	6479083	6516584	650133
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	STRING	ASC RANDOM	10000		142.73214605868800	111306.96666666700	110875	362125 1242305167	111083.0 1.16447525E+09	30		111167.0	167.0 2.0866833E+07	132917.0	111000.0 1.150147083E+09	111084	111000	110959	111291 1156897500	11108
BUBBLE_SORT_UNTIL_NO_CHANGE	STRING	DESC	10000			8.14977881966667E+08	799788250	1010318625		30			2.0866833E+07 1.4167E+07	8.29415417E+08		819919167	833343583	823664667	825680208	
BUBBLE_SORT_WHILE_NEEDED	INTEGER	ASC	100	20.090793911640200	3.668060341197600	651.4	583	10042	666.0	30	625.0	667.0	42.0	8459.0	625.0	666	625	667	667	66
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	INTEGER	RANDOM	100		6.001311585040450 4.978550287278720		9916 14125	149459 21584	10000.0 14209.0	30		10041.0	82.0 42.0	60000.0 17083.0	10000.0 14250.0	10000	9958 14250	9958 14250	10041	1000
BUBBLE_SORT_WHILE_NEEDED	INTEGER	ASC	1000	26.198897347450000	4.783242352986870	1530.53333333333300	1458	3875	1541.0	30		1542.0	42.0	3875.0	1583.0	1500	1542	1542	1500	158
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	INTEGER	RANDOM	1000	3362.6643959812600 4144.2659965306300	613.9357143328070 756.6359902004840	1040548.4 1393137.5	1034750	1137000	1040209.0 1391542.0	30		1042250.0 1396000.0	4084.0 4583.0	1063125.0 1484125.0	1042667.0	1043916		1039666	1049375	103891
BUBBLE_SORT_WHILE_NEEDED	INTEGER	ASC	1000	4144.2659965306300 102.57807866314400	18.728109196447800	1393137.5	1388666	1510625 162667	1391542.0	30	1391417.0	1396000.0	4583.0 125.0	1484125.0	1398375.0 13958.0	1396000 14125	1391417 13958	1388750 13959	1391584 13958	139145
BUBBLE_SORT_WHILE_NEEDED		RANDOM	10000		34861.85121178230		100876250		1.03010417E+08		1.02914459E+08		154374.0		1.03010417E+08				102917167	
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	INTEGER	DESC	10000		13268.503428854300 18.358346572850400	1.38600515233333E+08 2568.0	138558042 2458	143366583 29875	1.38572208E+08 2542.0	30		1.38574916E+08 2542.0	8499.0 42.0	1.41321E+08 29084.0	1.38874291E+08 2500.0	138566791 2541	138572000	138571125 2833	138567000 2500	13856629
BUBBLE_SORT_WHILE_NEEDED	FLOAT	RANDOM	100		39.367226922346900	14711.1	14333	210417	14666.0	30		14708.0	42.0 83.0	210417.0	14667.0	14667	14708	14708	14667	1466
BUBBLE_SORT_WHILE_NEEDED	FLOAT	DESC	100		6.339108478035090		17666	22959	17750.0	30		17750.0	0.0		17750.0	17750	17709	17750	17792	
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	FLOAT	RANDOM	1000		4.451237863619350 961.4968289079270		1708 1462417	4708 1751417	1834.0 1476750.0	30		1834.0 1480791.0	1.0 8416.0	4708.0 1482166.0	1833.0 1474375.0	1833 1472375	1834 1475209	1833 1469292	1833 1469375	14804
BUBBLE_SORT_WHILE_NEEDED	FLOAT	DESC	1000	730.9417547854880	133.4510957728070	1721938.8666666700	1721458	1776500	1721625.0	30	1721583.0	1721709.0	126.0	1727375.0	1721709.0	1721542	1721667	1721625	1721625	172154
BUBBLE_SORT_WHILE_NEEDED	FLOAT	ASC	10000		18.208586700500100		15875	170583		30			83.0	30500.0 2.18166459E+08	16375.0	16333	16333	16292	16334	163
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	FLOAT	RANDOM	10000		149530.24958424300	2.15960808433333E+08 1.752410042E+08	212605458 174764833	224306167 175540666	2.15872E+08 1.75222041E+08		2.15580792E+08 1.75210083E+08		751500.0 26750.0			217294667 175214583		215760500 175223167	215613834 175206167	
BUBBLE_SORT_WHILE_NEEDED	SHORT	ASC	100	52.36900058452730	9.561227644715610	690.233333333333	625	11958	667.0	30	666.0	708.0	42.0	11958.0	708.0	667	708	666	666	8
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	SHORT	RANDOM	100		5.683338220916770 5.465789224974910		18791 22458	84792 37041	19208.0 22583.0	30		19208.0 22583.0	42.0 41.0	52833.0 37041.0	19208.0 22584.0	19208 22583	19167 22583	19250 22500	19166 22625	1916
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	SHORT	ASC	1000		5.465789224974910 5.192462485821800		22458 2625	37041 4708					41.0		22584.0 2750.0	22583 2709	22583 2709	22500 2708	22625 2708	
BUBBLE_SORT_WHILE_NEEDED	SHORT	RANDOM	1000	4417.574504056370	806.5350684437900	1834300.03333333300	1824375	1915791	1834042.0	30	1831125.0	1836291.0	5166.0	1836541.0	1826291.0	1840542	1831125	1833000	1834125	18362
BUBBLE_SORT_WHILE_NEEDED BUBBLE SORT WHILE NEEDED	SHORT	DESC	1000		622.4753483442510 18.128242749510600		2252333 25916	2412709 192542	2256334.0 26125.0	30		2262000.0	6916.0 84.0	2264000.0 34375.0	2262125.0 26459.0	2262083	2255125	2255084 26167	2255166 26125	22595
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	SHORT	RANDOM	10000			26131.9333333333300 2.45400586266667E+08	25916 239462584		26125.0 2.45950084E+08		26083.0 2.44155084E+08	26167.0 2.46936375E+08		34375.0 2.41166042E+08		26041 243426084	26125 249442500		26125 245710584	260 2469363
BUBBLE_SORT_WHILE_NEEDED	SHORT	DESC	10000	146191.158969648	26690.731825166600	2.25302298666667E+08	224455125	233275292	2.252505E+08	30	2.25208959E+08	2.25361083E+08	152124.0	2.25429541E+08	2.25182625E+08	225165916	225208959	225351042	225226250	2253866
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	STRING	ASC RANDOM	100		4.162193154077770		541 37708	7208 51625	583.0 37834.0	30		625.0 37875.0	42.0 83.0	7208.0 51625.0	583.0 37792.0	583 37875	583 37750	583 37917	625 37750	
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	STRING	DESC	100		239.57613256811800	38151.36666666670 33968.1	37708 33166	51625 44875	37834.0 33959.0	30		37875.0 34000.0	83.0 42.0	51625.0 38583.0	37792.0 34000.0	37875 33958	37750 33875	37917 33959	37750 33916	378
BUBBLE_SORT_WHILE_NEEDED	STRING	ASC	1000	147.2437170891250	26.882901766874200	7862.43333333333	7625	17875	7875.0	30	7709.0	7958.0	249.0	17875.0	7708.0	7791	7917	8041	8042	775
BUBBLE_SORT_WHILE_NEEDED	STRING	RANDOM	1000		2578.3015397307200		5107916 3246750	5494750 3887792	5131375.0 3305542.0	30		5141250.0	18875.0 9125.0	5144166.0 3246750.0	5125375.0 3307000.0	5130291 3310458	5134542 3305542	5115833 3296875	5151959	
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	STRING	ASC	1000		1195.080429588400 4625.425075837380		3246750 111250	3887792 362875	3305542.0 115875.0	30		3309916.0 116333.0	9125.0 875.0	3246750.0 134666.0	3307000.0 117208.0	3310458 115334	3305542 115459	3296875 115416	3310458 115583	
BUBBLE_SORT_WHILE_NEEDED	STRING	RANDOM	10000	1528227.6506405200	279014.9190863130	6.16295773566667E+08	612332708	633548125	6.163005E+08	30	6.14820333E+08	6.17332292E+08	2511959.0	6.31998084E+08	6.16927209E+08	614667541	613983583	614464084	614782000	61441487
BUBBLE_SORT_WHILE_NEEDED	STRING	DESC	10000	3177005.307756930	580039.1574573700	3.32219454166667E+08	327676042	337849125	3.3429425E+08	30	3.28619875E+08	3.35237708E+08	6617833.0	3.32443375E+08	3.36352209E+08	329368209	328559208	328388958	328078584	32916958

Al-	v_5		v_7	v_8	v_9	v_10	v_11	v_12	v_13	v_14	v_15	v_16	v_17	v_18	v_19	v_20	v_21	v_22	v_23	v_24	v_25	v_26	v_27	v_28	v_29
Algorithm BUBBLE_SORT_PASS_PER_ITEM	6500	6500	6500	6500	6500	6500	6500	6500	6625	6500	6500	6500	6542	6500	6500	6500	6500	6500	6500	6500	6500	6500	6500	6500	6459
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	13959 17750	13958 17750	13917 17791	13833 17791	14000 17791	13958 17791	13833 17875	13917 17750	14042 17875	13875 17750	13833 17875	13834 17792	13917 17750	13917 17791	13875 17833	13834 17709	13917 17917	13875 17792	13834 17792	13875 17833	13875 17791	13833 17791	13875 17791	13916 17791	13833 17750
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	863750 1372667	870417 1363042	863750 1363709	863834 1359083	866458 1362666	867208 1360708	870667 1368291	874917 1369541	866458 1375916	864875 1359083	863750 1363875	866459 1362666	863708 1365416	870291 1363833	863708 1368959	866417 1364667	870875 1358917	868125 1368958	863708 1370708	868125 1359667	866416 1364459	865416 1367417	866500 1356667	863792 1368375	866583 1368291
BUBBLE_SORT_PASS_PER_ITEM	1636792	1634417	1636833	1648291	1636208	1636500	1636875	1634125	1643542	1641375	1635750	1636417	1638750	1563833	1636625	1637791	1636250	1636292	1658625	1633042	1636667	1638042	1636959	1644000	1636834
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	91080250 152756292	90802375 152923041	91349667 152715625	90934125 152532750	89261500 152613208	89115250 152563834	89170167 152772958	89153917 153116417	89201042 153522958	89018792 152777083	89089500 152615208	90746750 152187083	90967583 153591084	90905750 154080333	90879583 152961750	90816750 152594042	90800209 154263250		90840000	90902708 152386500	90910209 153125750	90808583 152671417	91097666 152747708	90811500 152917958	90891625 153462625
BUBBLE_SORT_PASS_PER_ITEM	164717167	164679792	164705958	164705833	164714959	164807708	167031916	164740167	164765417	164698000	164749500	164695042	164907291	164694875	164671500	164729708	164679333	164681792	164914417	164704625	164730750	164645667	164742625	164741875	164865958
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	11708 18459	11750 18500	11708 18459	11709 18500	11875 18584	11709	11750 18500	12125 18542	12042 18500	11917 18458	11709 18500	11708 18500	12166 18458	12125 18541	11708 18500	11708 18583	11667 18500	11792 18458	12167 18458	12167 18542	11709 18417	11667 18500	11708 18500	12083 18500	12167 18459
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	23625 1098250	23584 1099458	23542 1100083	23583 1099167	23583 1099042	23584 1099959	23583 1100042	23583 1099708	23584 1098916	23583 1098875	23583 1102708	23584 1098917	23500 1099459	23584	23625 1099666	23542 1098375	23625 1098750	23583 1099709	23542 1098792	23625 1099458	23583 1099583	23500 1117084	23625 1100167	23583 1100292	23584 1099292
BUBBLE_SORT_PASS_PER_ITEM	1841833	1843000	1847125	1848417	1848167	1851333	1849208	1842209	1850208	1853583	1849542	1848542	1849042	1847584	1846458	1848708	1841000	1850708	1847542	1845709	1853208	1841583	1848584	1849416	1848875
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	2203708 113675833	2200792 113989167	2200917 113472625	2200917 113861583	2202167 113560334	2200833 114417375	2201000 111517625	2200875 111242542	2200875 111358125	2202291 111890750	2206500 111802209	2200833 111738250	2200750 111755709	2200875 112083000	2202042 111473250	2200833 111920750	2200875 111303666	2200875 111499584	2202292	2200959 111688125	2206250 111596750	2200750 111976083	2201000 111950916	2203166 111420125	2200875 111641042
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	229361667 224332625	229899000 224138625	229975083	229969042 224397958	231339209	230381875	230562584	229938792 224216500	230102959	230213333	232016833	229230625 224275166	229883666	232821959 224333250	230101250	231006542	229342708	230112375	229952292 224229667	229798375	230190000	229453542 224409708	230734583	232161167	230174708
BUBBLE_SORT_PASS_PER_ITEM	224332625	224136625	224359667	224397958	224244709	224203750	224320292	224216500	224365292	224272875	224359584	224275166	22708	224333250	224222333	224216833	224206125	224395083	224226667	224267750	224281833	22750	224280625	224329791	22792
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT_PASS_PER_ITEM	28958 31542	28958 31625	28917	28917 31625	28875 31625	29000	28875 31708	28959 31625	28875 31584	28917 31583	28875 31666	29000 31625	28917 31708	28917 31625	29000 31625	28917 31667	28875 31584	28958 31625	28834 31625	29042 31541	28917 31625	28917 31583	28917 31625	28917 31584	28875 31666
BUBBLE_SORT_PASS_PER_ITEM	2239708	2240459	2246292	2239083	2238709	2239416	2251334	2239416	2240084	2247041	2240834	2241333	2238708	2245125	2239875	2240334	2250125	2236166	2236834	2244000	2248250	2239375	2238750	2242000	2239042
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	2765750 3114875	2758334 3116958	2754833 3143125	2764500 3119250	2759917 3115500	2757541 3119250	2766334 3118542	2764750 3125125	2758625 3126583	2767750 3122542	2766625 3117834	2752791 3119583	2762959 3133916	2757875 3117459	2760916 3128750	2761500 3124416	2751750 3117417		2756417 3117458	2754250 3118583	2762375 3124917	2768333 3120083	2753583 3128167	2754750 3117583	2760459 3121417
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	228005625 338715875	227950500 337503417	228161375 340300708	228044500 339150500	228022791 340847541	228007834 339266458	228168583 339436375	228029083 339442791	227991958 338006459	228013417 334190791	228041875 336273250	228146041 335408709	227941917 333008625	228016125 334218667	227966375 332834583	228068542 334112458	228000375 333158250		228043083 331940208	228180500 334658292	227996416 333387375	227968125 334999334	228001542 333165875	227962791 333549625	228426084 335915375
BUBBLE_SORT_PASS_PER_ITEM	315917500	315884625	316226708	312899208	312778292	313483791	313914417	313376625	314443958	314566250	314510083	314096541	314918292	314300625	314644625		313838375		314083667	314523208	317201833	315962542		315876166	315960042
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	38334 54458	38375 54500	38292 54500	38375 54500	38375 54458	38375 54542	38375 54416	38375 54500	38292 54500	38375 54583	38375 54500	38375 54500	38375 54542	38334 54458	38333 54500	38417 54666	38333 54667	38375 54416	38333 54417	38334 54542	38375 54458	38334 54500	38458 54542	38333 54583	38334 54500
BUBBLE_SORT_PASS_PER_ITEM	47583	47542	47625	47625	47584	47625	47542	47541	47667	47583	47583	47583	47584	47708	47625	47500	47583	47625	47584	47625	47584	47541	50334	47584	47625
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_PASS_PER_ITEM	4722084 7633334	4688750 7582333	4707542 7656708	4711833 7622834	4731208 7622750	4686417 7590750	4696416 7618542	4725542 7573500	4713791 7616417	4660459 7577041	4688791 7631250	4668959 7670000	4694625 7642417	4659166 7616250	4673125 7641792	4680584 7657125	4697791 7649625	4670542 7636917	4686791 7686667	4692459 7656084	4702042 7662750	4672083 7663208	4692959 7650250	4683875 7626875	4714125 7710917
BUBBLE_SORT_PASS_PER_ITEM BUBBLE SORT PASS PER ITEM	4959000 927648375	4921208 927346167	4935417 956319208	4929834 964623292	4966125 967148792	4920084 964333375	4937500 961990041	4935084 957906417	4949042 971874208	4922041 962815209	4941750 955056666	4935750 960958459	4959208 954026500	4925292 959228583	4944708 958529500	4928417 953544083	4950125 952158667	4934459 949046958	4942750 951585583	4935583 943534875	4957750 931644167	4914167 929913292	4938417 929494208	4946541 927931208	4964458 926985084
BUBBLE_SORT_PASS_PER_ITEM	1035032375	1033169000	1038406500	1031076416	1045139667	1060388417	1054430583	1056737959	1054864583	1055929083	1055711125	1039710917	1035982375	1045440042	1036085583	1046382750	1055777750	1052264583	1052293709	1055267500	1056654041	1052391209	1054174625	1058354916	1067714209
BUBBLE_SORT_PASS_PER_ITEM BUBBLE_SORT_UNTIL_NO_CHANGE	647045167 583	647557167 625	651282458 625	650535542 625	649981416 583	649354250 584	652281958 583	649755125 625	650673750 625	648031209 625	649947750 625	648584375 625	651889000 625	652449292 625	651061417 625	650740625 625	653853333 625	657026167 625	667030750 625	667938708 625	659795542 625	658523750 625	656635417 625	648665917 625	653633625 709
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	16375 22209	16292 22250	16333 22250	16416 22208	16333 22250	16375 22166	16333 22250	16292 22292	16375 22208	16375 22250	16333 22333	16333 22208	16375 22167	16333 22250	16334 22250	16375 22208	16375 22250	16333 22250	16334 22167	16375 22292	16375 22250	16333 22209	16417 22208	16292 22291	16375 22166
BUBBLE_SORT_UNTIL_NO_CHANGE	1709	1708	1666	1666	1708	1667	1709	1875	1709	1708	1666	1708	1667	1667	1667	1709	1667	1667	1667	1708	1708	1667	1667	6333	1750
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	1689791 2145083	1692416 2140625	1690083 2147250	1696000 2140375	1689916 2142291	1695791 2148125	1688583 2140292	1686584 2140792	1697208 2140500	1688166 2151542	1691125 2140500	1694083 2137708	1694416 2141042	1691416 2147417	1687208 2144750	1691917 2140667	1688584 2140375	1703208 2147416	1688166 2142333	1693625 2141000	1690625 2147666	1690834 2140541	1695042 2140583	1693042 2144834	1689375 2147375
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	19583	17834	18875	17917	17875 185276625	18959	19041	18625	17875	18583	17542 185418250	18833	17791	20500	18500	18959	17917	18625	17583	18542	17833	17625	18792	17625	18500 181557167
BUBBLE_SORT_UNTIL_NO_CHANGE	216961833	216912209	216934208	216906334	216949208	216935875	216909291	216912625	216980291	217116000	216906167	216961292	217119959	216981458	216908958	216915042	216903167	216987500	216907292	218268292		216908875	216976375	216906333	216928584
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	20667	3000 20583	2708 20666	2667 20666	2709 20666	2708 20625	20708	2667 20625	2667 20583	20709	2666 20625	2666 20625	20750	2667 20667	2666 20667	2708 20625	2709 20667	20709	20583	2667 20666	2709 20666	2750	2959 20667	20584	2666 20708
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	27959 1875	28042 1833	28000 1875	27917 1916	28000 1875	27958 1875	28084 1917	27958 1875	28000 1833	27958 1834	27958 1875	28042 1875	28084 1833	28042 1875	28125 1833	28000 1875	27958 1833	28000 1875	27958 1833	27959 1875	28000 1833	27959 1834	28000 1875	28000 1834	27958 1833
BUBBLE_SORT_UNTIL_NO_CHANGE	2127167	2126958	2127583	2124667	2126959	2128375	2130167	2127709	2124292	2124083	2124583	2125209	2125417	2127708	2130166	2126083	2129084	2127542	2126208	2127958	2127083	2127333	2125834	2124791	2127208
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	2608292 20416	2608292 19583	2609708 18958	2608583 20583	2611375 19292	2608250 20417	2609667 18833	2608208 20417	2608208 19167	2608292 20208	2609584 18833	2608208 22167	2610416 19125	2612166 20083	2609833 19042	2608250 19750	2608291 18792	2608333 19834	2609709 18833	2608250 18833	2608459 19875	2608208 20208	2609791 19792	2608208 19458	2608250 20167
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	252355084 265339375	251882334 265155125	252395125 265050000	252279084 265114417	252425000 265269000	252912000 265138625	251798541 265127417	252293625 265120292	253801500 265259500	252102416 265116708	251950250 265112042	254573625 265087792	254240666 265241875	252880709 265132750	252403542 265095625	252178000 265138458	252709750 265286375			252267334 265308333	252804000 265123625	252817459 265109583	252691041 265040583	252482791 265311041	252167125 265128041
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	625 32292	667 32750	667 32209	667 32125	667 32584	625 32500	625 32334	667 32208	625 32083	666 32417	666 32125	666 32291	666 32291	625 32041	667 32334	667 32042	667 32250	667 32459	667 32208	625 32541	667 32500	667 32292	667 32250	667 32000	667 32541
BUBBLE_SORT_UNTIL_NO_CHANGE	36083	39083	36042	36125	36125	36042	36166	36125	36125	36083	36125	36083	36167	36083	36125	36167	36167	36083	36166	36000	36167	36084	36125	36125	36083
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	2791 3748667	2834 3740958	2791 3739500	2792 3753750	2750 3742291	2791 3731667	2792 3780791	2792 3728084	2791 3745000	2834 3739958	2750 3773708	2791 3737583	2792 3741542	2792 3745042	2791 3774625	2750 3744083	2791 3754125	2792 3752083	2792 3740542	2791 3744250	2833 3756625	2792 3754208	2750 3754959	2750 3749458	2792 3750875
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE SORT UNTIL NO CHANGE	3484167 28958	3478708 29417	3481125	3488917 29417	3479292 30500	3479292 29917	3498041 30542	3479042 29750	3486042 30375	3483833 29500	3486167 31334	3479291 30208	3480459 30708	3486333 29541	3478708 31834	3490792 29666	3479542	3489250 29583	3483791 29708	3480000	3487750 29791	3479167 33417	3486208 29833	3480458	3486250 29917
BUBBLE_SORT_UNTIL_NO_CHANGE	422907583	419151625	418085875	418400042	416983708	419338833	419128708	417760375	417659833	421200542	418971375	422503959	421921084	420285375	417458334	417076500	418052250	420987250	417491083	417313917	417734542	419784500	419346208	423103292	422150125
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	349993708 625	350089583 625	350107125 583	349928500 583	350194333 583	350033083 583	350014000 583	350090959 583	350146291 583	350069834 625	350366459 625	351319334 625	349986792 583	350095958 583	350039792 583	350040292 583	350116750 625	350038541 625	350127500 583	350107208 625	350003459 583	350064708 625	350193833 625	349913375 625	350121875 584
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	62417 59833	62459 59875	62500 59750	62541 59875	62584 59875	62500 59875	62541 59833	62458 59917	62417 59833	62500 59917	62542 59875	62500 59875	62458 59834	62542 59791	62500 59875	62500 59750	62542 59833	62583 59958	62417 59875	62500 59917	62625 59917	62500 59833	62542 59875	62458 64292	62500 59875
BUBBLE_SORT_UNTIL_NO_CHANGE	7959	7875	8042	7916	7958	8000	8084	7958	7958	7959	7916	8000	8000	7917	8041	8083	7917	7959	8041	8000	7958	7958	8000	7959	8041
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	8904459 6523250	8848000 6496250	8919791 6540291	8866417 6509334	8881625 6535375	8814667 6483000	8837416 6496000	8863875 6507250	8901917 6515167	8825375 6469792	8855042 6522875	8876875 6495250	8897458 6519417	8868792 6498750	8868500 6527500	8900166 6510834	8905292 6529667	8849041 6479875	8975125 6506375	8921958 6510125	8865084 6537458	9008625 6532709	8953459 6537250	8884250 6546417	8995000 6592375
BUBBLE_SORT_UNTIL_NO_CHANGE BUBBLE_SORT_UNTIL_NO_CHANGE	111166 1158793375	111000	111167 1175263625	111083 1176755292	111041 1185779250	110959	111000	111125 1186263792	110916	110917	111583 1177966500	111042	111042	111000 1162981292	111125	111042	111917 1165117084	114541	111250 1153087084	110916	111167	113667	111125 1154396792	111000	111000
BUBBLE_SORT_UNTIL_NO_CHANGE	821685375	817470583	824511792	806564750	810044375	806570375	807897959	807518375	808973000	820109041	810691792	806522167	806601041	805578625	802677250	815621542	806882667	812073666	811089792	810423500	808443583	809670584	830086958	827435416	831904084
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	9958	10041	625 9958	10000	10041	625 9958	10042	9959	625 9958	10042	667 9959	625 10000	667 9959	625 10042	10000	10000	625 9958	10000	625 9959	667 10042	10042	625 10000	10000	625 10000	10000
BUBBLE_SORT_WHILE_NEEDED	14291	14208 1542	14209	14208	14208 1542	14250	14208	14209	14208	14250 1542	14208	14209	14208 1500	14250	14208 1541	14291	14208	14209	14208	14208 1542	14209	14250	14209	14208	14250 1583
BUBBLE_SORT_WHILE_NEEDED	1040208	1037916	1039208	1037167	1043375	1041083	1045625	1038958	1040458	1040209	1037208	1040541	1038166	1038666	1047625	1040792	1036250	1040209	1036917	1039541	1035666	1046791	1036541	1042250	1042667
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	1398708 13917	1403000 13875	1391541 13875	1391458 13792	1388709 13792	1391542 13833	1391542 13875	1398708 13959	1393000 13792	1392041 13875	1391541 13917	1388750 13833	1391458 13833	1398959 14250	1388792 13833	1393167 14042	1388875 13875	1388667 13792	1398500 13959	1391500 14083	1391542 13875	1388708 13958	1393083 13875	1402750 13875	1398375 13958
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	102914459 138572208		102961500 138573541	102840000 138571666	102967250 138566750	102834833 138565542		102893416 138572292	103111375 138565334			102936375 138566417	102887333	102939500 138578000		103107166 138566375		103202500		103550916 138572958		102911250 138720292	102989541	102882834 138693583	103010417
BUBBLE_SORT_WHILE_NEEDED	2542	2542	2542	2458	2542	2542	2500	2792	2542	2542	2542	2542	2500	2542	2625	2583	2625	2916	2541	2541	2541	2583	2500	2500	2500
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	14667 17791	14708 17750	14708 17750	15250 17750	14625 17666	14542 17750	15125 17792	14625 17750	14625 17709	14667 17750	14625 17834	14625 17750	14625 17750	14625 17750	14708 17750	14666 17834	15583 17792	14625 17750	14583 17792	14625 17709	14584 17750	14625 17750	14625 17750	14583 17750	14667 17750
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	1833 1485750	1833 1480791	1834 1485125	1917 1485833	1875 1480542	1875 1467292	1916 1471417	1833 1474959	1834 1475750	1875 1483000	1834 1472083	1833 1476750	1833 1476583	1834 1475250	1833 1482333	1875 1473375	1833 1478041	1875 1476875	1833 1469875	1833 1481209	1834 1477125	1833 1470084	1833 1485250	1834 1478709	1833 1474375
BUBBLE_SORT_WHILE_NEEDED	1723125	1721584	1721583	1721625	1721625	1721625	1723041	1721583	1721709	1721583	1721541	1721625	1723042	1721542	1721583	1721583	1721584	1722917	1724708	1721541	1721750	1721583	1721541	1722833	1721709
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	16417 217062625	16375 216562833	16375 215694458	16417 215716584	16375 217643500	16209 216821917	16291 216290750	16333 214669834	16459 216332292	16625 215782750	16709 216322625	16333 215502542	16250 215580792	16333 215670958	16250 214612667	16333 217084000	16333 215974041	16334 215394417	16291 214612750	16250 216074917	16292 216271792	16333 214999292	16417 215872000	16333 214401125	16375 215699875
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	175223333 708	175220166 666	175349709 666	175210083 708	175204292 709	175249917 667	175216959 667	175402625 875	175212125 709	175234542 667	175209750 667	175212083 667	175228000 708	175333542 666	175162542 666	175204125 667	175218792 667	175236833 667	175259833 667	175343833 667	175225625 667	175199333 667	175203417 666	175227500 666	175222041 708
BUBBLE_SORT_WHILE_NEEDED	19208	19209	19167	19208	19208	19167	19209	19208	19250	19166	19166	19208	19209	19167	19166	19166	19250	19167	19208	19208	19250	19125	19208	19166	19208
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	22542 2708	22583 2834	22583 2709	22542 2708	22583 2708	22583 2750	22542 2708	22625 2708	22541 2709	22542 2709	22583 2709	22542 2708	22584 2708	22583 2708	22583 2708	22584 2709	22541 2709	22500 2708	22583 2708	22541 2708	22542 2792	22542 2709	22541 2708	22542 2708	22584 2750
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	1832834 2255167	1837417 2255875	1828417 2262375	1835541 2258000	1845084 2262541	1833375 2256334	1834416 2262000	1827834 2255125	1841250 2259709	1835583 2253125	1830333 2255083	1834042 2252333	1839167 2257042	1828791 2262292	1830709 2255083	1832625 2255167	1829416 2256875	1841334 2265583	1832916 2255083	1832834 2255084	1833542 2262166	1841083 2259000	1834500 2255084	1834584 2255666	1826291 2262125
BUBBLE_SORT_WHILE_NEEDED	26125	26167	26125	26042	26166	26042	26167	26000	26042	26000	26250	26416	26167	26083	26125	26083	26125	26167	26083	26041	26125	26167	26125	26125	26459
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	245950084 225298584	247048416 225191959	244155084 225209375	244236000 225375709	246483708 225196292	247781417 225202750		243984750 225408708	246943250 225370833		248056375 225322209	247522500 225225750	245952000 225361083	245451709 225309458		246490542 225930917	246441959 225476166		245116500 225195000	241730625 225212459		242999042 225350125		240597875 225343375	
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	583 37750	625 37834	625 37750	584 37916	584 37792	625 37791	583 37834	625 37875	583 37833	583 44708	583 37917	625 37958	583 37792	583 37792	583 37875	625 37875	584 40541	625 37833	583 37834	583 37833	666 37708	625 37833	583 37833	583 37875	583 37792
BUBBLE_SORT_WHILE_NEEDED	33916	33959	33959	34000	33916	34000	33959	33958	33958	34042	34000	34000	34000	33958	33917	33959	33916	34250	34000	33958	33959	33834	33958	34000	34000
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	7917 5141250	7708 5127916	7917 5145625	7958 5121417	7791 5141875	7792 5129958	8167 5151042	7791 5118750	7667 5143041	7875 5122334	7791 5138083	8084 5122375	7750 5138833	7875 5112000	8166 5184042	7709 5134042	8084 5132416	7667 5127417	7916 5150250	7708 5121500	7917 5131375	7958 5124167	7708 5137083	7708 5131167	7708 5125375
BUBBLE_SORT_WHILE_NEEDED BUBBLE_SORT_WHILE_NEEDED	3309375 115375	3296708 115333	3314333 115458	3299917	3301292 118125	3304959 115458	3305666 115291	3307167 115500	3306625 115500	3298167 115292	3309916 257209	3303500	3311334 119334	3301500	3327625	3313250 115833	3300791	3296250	3303250 116000	3308084	3303666 118541	3296417 115875	3310042	3299791 121125	3307000 117208
BUBBLE_SORT_WHILE_NEEDED	614323166	615809542	614820333	115500 614465250	615946625	617332292	616799167	616343375	616300500	615612125	617021416		614980917	615350708	116042 615487875	617632875	116084 617981792		619290041	116084 618799500	618252833	618545625	116083 617291708	616986083	616927209
BUBBLE_SORT_WHILE_NEEDED	328597000	328603500	329066208	327676042	328748792	329314916	328619875	328300042	333149208	334848583	335061709	335237708	334373958	334300417	334294250	335409833	335256542	335201792	335439666	335354583	335374542	335358667	334837208	334241833	336352209

7.4 Data Sorting vs Array Size

Data_Ordering	Array_Size	Mean	N	Std. Deviation
ASC	100	7.3834E+3	12	1.1807E+4
	1000	7.4524E+5	12	1.4278E+6
	10000	1.1488E+8	12	2.7164E+8
	Total	3.8543E+7	36	1.6183E+8
DESC	100	2.9638E+4	12	1.3408E+4
	1000	2.9442E+6	12	1.4945E+6
	10000	3.2296E+8	12	2.0592E+8
	Total	1.0865E+8	36	1.9223E+8
RANDOM	100	2.7501E+4	12	1.6699E+4
	1000	3.2956E+6	12	2.5980E+6
	10000	4.1438E+8	12	3.5180E+8
	Total	1.3923E+8	36	2.7899E+8
Total	100	2.1507E+4	36	1.7069E+4
	1000	2.3283E+6	36	2.1850E+6
	10000	2.8407E+8	36	3.0261E+8
	Total	9.5474E+7	108	2.1887E+8

Figure 8: Data sorting vs array size. Report containing the mean values of processing time in nanoseconds for given data-input as arrays sorted by ascending (ASC), descending (DESC) or random(RANDOM). The array size is included with number of elements varying from 100, 1000 or 10000 in each case.

7.5 Data Sorting vs Algorithm

Data_Ordering	Algorithm	Mean	N	Std. Deviation
ASC	BUBBLE_SORT_PASS_PER_I TEM	1.1559E+8	12	2.7131E+8
	BUBBLE_SORT_UNTIL_NO_ CHANGE	1.6564E+4	12	3.1372E+4
	BUBBLE_SORT_WHILE_NEE DED	1.6320E+4	12	3.3931E+4
	Total	3.8543E+7	36	1.6183E+8
DESC	BUBBLE_SORT_PASS_PER_I TEM	1.1408E+8	12	2.0153E+8
	BUBBLE_SORT_UNTIL_NO_ CHANGE	1.3852E+8	12	2.4754E+8
	BUBBLE_SORT_WHILE_NEE DED	7.3344E+7	12	1.1541E+8
	Total	1.0865E+8	36	1.9223E+8
RANDOM	BUBBLE_SORT_PASS_PER_I TEM	1.4866E+8	12	3.0563E+8
	BUBBLE_SORT_UNTIL_NO_ CHANGE	1.6986E+8	12	3.4191E+8
	BUBBLE_SORT_WHILE_NEE DED	9.9188E+7	12	1.8569E+8
	Total	1.3923E+8	36	2.7899E+8
Total	BUBBLE_SORT_PASS_PER_I TEM	1.2611E+8	36	2.5596E+8
	BUBBLE_SORT_UNTIL_NO_ CHANGE	1.0280E+8	36	2.4819E+8
	BUBBLE_SORT_WHILE_NEE DED	5.7516E+7	36	1.2976E+8
	Total	9.5474E+7	108	2.1887E+8

Figure 9: Data sorting vs Algorithm. Report containing the mean values of processing time in nanoseconds for given data-input as arrays sorted by ascending (ASC), descending (DESC) or random(RANDOM). The array size is included with number of elements varying from 100, 1000 or 10000 in each case.