

1

$L(G) = \{\alpha | \alpha \in (a, b, c)^+, \text{ onde a soma de } a\text{'s e } c\text{'s é par se } \alpha \text{ inicia por } b, \text{ senão } |\alpha| \text{ é ímpar}\}$

$S ::= a < A > | b < C > | c < A >$
 $A ::= a < B > | b < B > | c < B > | \varepsilon$
 $B ::= a < A > | b < A > | c < A >$
 $C ::= a < D > | b < C > | c < D > | \varepsilon$
 $D ::= a < C > | b < D > | c < C >$

2

$L(G) = \{\alpha | \alpha \in a^x b^y c^z \text{ onde } x + z \text{ é ímpar e } x, y, z > 0\}$

$S ::= a < A >$
 $A ::= a < B > | b < C >$
 $B ::= a < A > | b < D >$
 $C ::= b < C > | c < E >$
 $D ::= b < D > | c < F >$
 $E ::= c < F >$
 $F ::= c < E > | \varepsilon$

3

$L(G) = \{\alpha | \alpha \in (a, b, c)^+, \text{ onde a soma de } a\text{'s e } c\text{'s é par se } \alpha \text{ inicia por } b, \text{ senão } |\alpha| \text{ é ímpar e } c \text{ nunca antecede } a\}$

$S ::= a < E > | b < A > | c < G >$
 $A ::= a < B > | b < A > | c < D > | \varepsilon$
 $B ::= a < A > | b < B > | c < C >$
 $C ::= b < A > | c < D > | \varepsilon$
 $D ::= b < A > | c < C >$
 $E ::= a < F > | b < F > | c < H > | \varepsilon$
 $F ::= a < E > | b < E > | c < G >$
 $G ::= b < F > | c < H > | \varepsilon$
 $H ::= b < E > | c < G >$

4

$L(G) = \{\alpha | \alpha \in (0...9, ', ', ', +, -)^+ \text{ onde } \alpha \in \mathbb{R}\}$

$digito \leq 0...9$
 $S' ::= + < S > | - < S > | digito < A >$
 $S ::= digito < A >$
 $A ::= digito < B > | . < D > | , < G > | \varepsilon$
 $B ::= digito < C > | . < D > | , < G > | \varepsilon$
 $C ::= . < D > | , < G > | \varepsilon$
 $D ::= digito < E >$
 $E ::= digito < F >$
 $F ::= digito < C >$
 $G ::= digito < H >$
 $H ::= digito < H > | \epsilon$

Exemplo GLC

$L(G) = \{\alpha | \alpha \in a^x c^y \text{ onde } x > y\}$

$S ::= a < S > | c < A >$
 $A ::= a < A > | \varepsilon$

$L(G) = \{\alpha | \alpha \in a^x c^y \text{ onde } x! = y\}$
 $S ::= a < S > c | a < A > | < B > c$
 $A ::= a < A > | \varepsilon$
 $B ::= < B > c | \varepsilon$
 $L(G) = \{\alpha | \alpha \in a^x b^y c^z \text{ onde } x! = z \text{ e } y > 0\}$
 $S ::= a < S > c | a < A > | < B > c$
 $A ::= a < A > | b < C >$
 $B ::= < B > c | b < C >$
 $C ::= b < C > | \varepsilon$
 $L(G) = \{\alpha | \alpha \in a^x b^y c^z \text{ onde } y = x + z \text{ e } x, z > 0\}$
 $S ::= < A > < B >$
 $A ::= a < A > b | ab$
 $B ::= b < B > c | bc$
 $L(G) = \{\alpha | \alpha \in (a, b, c)^+ \text{ onde o número de } a\text{'s é igual ao número de } c\text{'s}\}$
 $S ::= a < > | b < > | c < > | \varepsilon$
 $A ::= < B > < C > < B > \mathbf{a} < B > < C > < B > \mathbf{c} < C > < B > | < B > < C > < B > \mathbf{c} < B > < C > < B > \mathbf{a} < B > < C > < B > | \varepsilon | < B >$
 $B ::= b < B > | \varepsilon$
 $L(G) = \{\alpha | \alpha \in (a^{2i+1}b^{i+3}/i > 0) \cup (a^{i+4}b^{i+3}/i \geq 0)\}$
 $S ::= aaa < A > bbbb | aaaa < B > bbb$
 $A ::= aa < A > b | \varepsilon$
 $B ::= a < B > b | \varepsilon$
 $L(G) = \{\alpha | \alpha \in (\text{para, var, =, até, \{, \}, opl, op, se, então, senão})^+ \text{ onde } \alpha \text{ permite estruturas aninhadas de condição e iteração}\}$
 $S ::= A | B | op$
 $A ::= \text{se opl então } S \ C$
 $B ::= \text{para } var = var \text{ até var } \{S\}$
 $C ::= \text{senão } \{S\} | \varepsilon$

Lista 1 - Gramáticas Regulares

a

$L(G) = \{x | x \in (a, b)^* \text{ onde o número de } b\text{'s é par}\}$

$S ::= a < B > | b < A > | \varepsilon$

$B ::= a < B > | b < A > | \varepsilon$

$A ::= a < A > | b < B >$

b

$L(G) = \{x | x \in (a, b)^* \text{ onde o número de } b\text{'s é par}\}$

$S ::= a < A > | b < B >$

$A ::= a < A > | b < B >$

$B ::= a < B > | b < A > | \varepsilon$

c

$L(G) = \{x | x \in (a, b, c)^* \text{ onde ocorra pelo menos dois padrões 'ac'}\}$

$S ::= a < B > | b < A > | c < A >$

$A ::= a < B > | b < A > | c < A >$

$B ::= a < B > | b < A > | c < C >$

$C ::= a < D > | b < C > | c < C >$

$D ::= a < D > | b < C > | c < E >$

$E ::= a < E > | b < E > | c < E > | \varepsilon$

d

$L(G) = \{x | x \in (a, b, c)^* \text{ onde ocorra pelo menos um padrão 'abc'}\}$

$S ::= a < B > | b < A > | c < A >$

$A ::= a < B > | b < A > | c < A >$

$B ::= a < B > | b < C > | c < A >$

$C ::= a < B > | b < A > | c < D >$

$D ::= a < D > | b < D > | c < D > | \varepsilon$

e

$L(G) = \{x | x \in (0, 1)^* \text{ onde o número de } 1\text{'s é múltiplo de } 3\}$

$S ::= 0 < S > | 1 < A > | \varepsilon$

$A ::= 0 < A > | 1 < B >$

$B ::= 0 < B > | 1 < S >$

f

$L(G) = \{x | x \in (a, b, c, d)^+ \text{ onde a soma de } a\text{'s e } c\text{'s é ímpar se } x \text{ começa com } a \text{ ou a soma de } a\text{'s e } d\text{'s é par se } x \text{ começa por } b; \text{ se } x \text{ inicia por } c \text{ ou } d \text{ não existe restrição}\}$

$S ::= a < A > | b < C > | c < E > | d < E >$

$A ::= a < B > | b < A > | c < B > | d < A > | \varepsilon$

$B ::= a < A > | b < B > | c < A > | d < B >$

$C ::= a < D > | b < C > | c < C > | d < D > | \varepsilon$

$D ::= a < C > | b < D > | c < D > | d < C >$

$E ::= a < E > | b < E > | c < E > | d < E > | \varepsilon$

Lista 2 - Autômatos Finitos

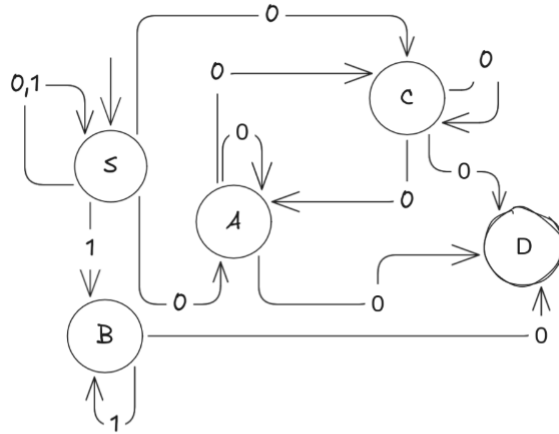
a

$S ::= 0 < S > \mid 1 < S > \mid 0 < A > \mid 0 < C > \mid 1 < B >$

$A ::= 0 < A > \mid 0 < C > \mid 0$

$B ::= 1 < B > \mid 1$

$C ::= 0 < C > \mid 0 < A > \mid 0$



| | 0 | 1 |
|-----|-------|------|
| ->S | S,A,C | S,B |
| A | A,C,D | --- |
| B | --- | B,D |
| C | A,C,D | --- |
| *D | ---- | ---- |

b

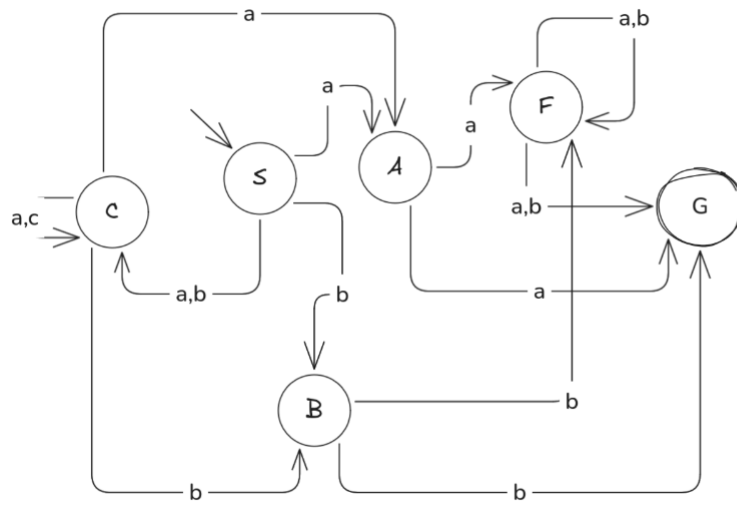
$S ::= a < A > \mid a < C > \mid b < B > \mid b < C >$

$A ::= \neg a < F > \mid a$

$B ::= b < F > \mid b$

$C ::= a < A > \mid a < C > \mid b < B > \mid b < C >$

$F ::= a < F > \mid b < F > \mid a \mid b$



| | a | b |
|----|------|-----|
| >S | A,C | C |
| A | F,G | --- |
| B | ---- | F,G |
| C | A,C | B,C |
| F | F,G | F,G |
| *G | ---- | --- |

Lista de exercícios nova

0.1 4 - autômatos finitos

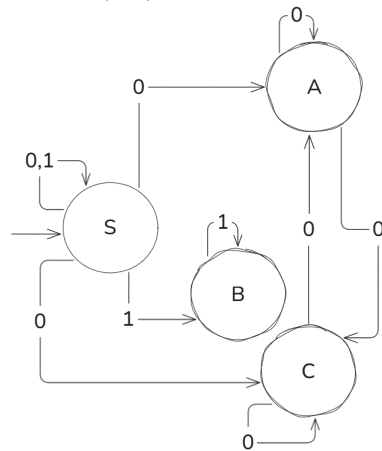
a

$S ::= 0S|1S|0A|0C|1B$

$A ::= 0A|0C|0$

$B ::= 1B|1$

$C ::= 0C|0A|0$



AFND

| | 0 | 1 |
|-----------------|---------|------|
| $\rightarrow S$ | S, A, C | S, B |
| A | A, C, F | - |
| B | - | B, F |
| C | A, C, F | - |
| $*F$ | - | - |

AFD

| | 0 | 1 |
|-----------------|-----------------|--------------|
| $\rightarrow S$ | $[S, A, C]$ | $[S, B]$ |
| $[S, A, C]$ | $*[S, A, C, F]$ | $[S, B]$ |
| $*[S, A, C, F]$ | $*[S, A, C, F]$ | $[S, B]$ |
| $[S, B]$ | $[S, A, C]$ | $*[S, B, F]$ |
| $*[S, B, F]$ | $[S, A, C]$ | $*[S, B, F]$ |

b

$S ::= aA|aC|bB|bC$

$A ::= aF|a$

$B ::= bF|b$

$C ::= aA|aC|bB|bC$

$F ::= aF|bF|a|b$

AFND

| | a | b |
|-----------------|--------|--------|
| $\rightarrow S$ | A, C | B, C |
| A | F, K | - |
| B | - | F, K |
| C | A, C | B, C |
| F | F, K | F, K |
| $*K$ | - | - |

AFD

| | a | b |
|-----------------|-----------------|-----------------|
| $\rightarrow S$ | $[A, C]$ | $[B, C]$ |
| $[A, C]$ | $*[F, K]$ | $[B, C]$ |
| $[B, C]$ | $[A, C]$ | $*[B, C, F, K]$ |
| $*[F, K]$ | $*[F, K]$ | $*[F, K]$ |
| $*[B, C, F, K]$ | $*[A, C, F, K]$ | $*[B, C, F, K]$ |
| $*[A, C, F, K]$ | $*[A, C, F, K]$ | $*[B, C, F, K]$ |

c

$S ::= aA|bB$
 $A ::= aS|aC|a$
 $B ::= bS|bD|b$
 $C ::= aB$
 $D ::= bA$

AFND

| | a | b |
|-----------------|-----------|-----------|
| $\rightarrow S$ | A | B |
| A | S, C, F | - |
| B | - | S, D, F |
| C | B | - |
| D | - | A |
| F | - | - |

AFD

| a | b |
|---|---|
|---|---|

d

$S ::= 0 < B > | 1 < A > | 1|\varepsilon$

$A ::= 0 < B > | \varepsilon$

$B ::= 0 < C > | 0 | 1 < D >$

$C ::= 0 < B > | 1 < A > | 1$

$D ::= 1 < C > | 1$

| | AFND | |
|-----------------|------|------|
| | 0 | 1 |
| $\rightarrow S$ | B | A,X |
| $*X$ | - | - |
| $*A$ | B | - |
| B | C, X | D |
| C | B | A,X |
| D | - | C, X |

| | AFD | |
|-------------------|------|------|
| | 0 | 1 |
| $\rightarrow^* S$ | B | [AX] |
| B | [CX] | D |
| $*[AX]$ | B | - |
| $*[CX]$ | B | [AX] |
| D | - | [CX] |

e f