

Métodos Numéricos – Prof. Luis Edo. Amaya

Fórmulas de Diferenciación Numérica	
$n = 2$	$f'(x) = \frac{f(x_0 + h) - f(x_0)}{h} - \frac{h}{2} f''(\xi)$
$n = 3$	$f'(x) = \frac{1}{2h} [-3f(x_0) + 4f(x_0 + h) - f(x_0 + 2h)] - \frac{h^2}{3} f^{(3)}(\xi)$
$n = 3$	$f'(x) = \frac{1}{2h} [f(x_0 + h) - f(x_0 - h)] - \frac{h^2}{6} f^{(3)}(\xi)$
$n = 3$	$f''(x) = \frac{1}{h^2} [f(x_0 - h) - 2f(x_0) + f(x_0 + h)] - \frac{h^2}{12} f^{(4)}(\xi)$
$n = 5$	$f'(x) = \frac{1}{12h} [f(x_0 - 2h) - 8f(x_0 - h) + 8f(x_0 + h) - f(x_0 + 2h)] - \frac{h^4}{30} f^{(5)}(\xi)$
$n = 5$	$f'(x) = \frac{1}{12h} [-25f(x_0) + 48f(x_0 + h) - 36f(x_0 + 2h) + 16f(x_0 + 3h) - 3f(x_0 + 4h)] - \frac{h^4}{5} f^{(5)}(\xi)$

Fórmulas de Integración Numérica		
n	Fórmulas Cerradas	Fórmulas Abiertas
0	$x_i = x_0 + i \cdot h \quad h = \frac{b-a}{n}$	$2hf(x_0) + \frac{h^3}{3} f''(\xi)$
1	$\frac{h}{2} [f(x_0) + f(x_1)] - \frac{h^3}{12} f''(\xi)$	$\frac{3h}{2} [f(x_0) + f(x_1)] + \frac{3h^3}{4} f''(\xi)$
2	$\frac{h}{3} [f(x_0) + 4f(x_1) + f(x_2)] - \frac{h^5}{90} f^{(4)}(\xi)$	$\frac{4h}{3} [2f(x_0) - f(x_1) + 2f(x_2)] + \frac{14h^5}{45} f^{(4)}(\xi)$
3	$\frac{3h}{8} [f(x_0) + 3f(x_1) + 3f(x_2) + f(x_3)] - \frac{3h^5}{80} f^{(4)}(\xi)$	$\frac{5h}{24} [11f(x_0) + f(x_1) + f(x_2) + 11f(x_3)] + \frac{95h^5}{144} f^{(4)}(\xi)$
4	$\frac{2h}{45} [7f(x_0) + 32f(x_1) + 12f(x_2) + 32f(x_3) + 7f(x_4)] - \frac{8h^7}{945} f^{(6)}(\xi)$	$x_i = x_0 + i \cdot h \quad h = \frac{b-a}{n+2}$

Reglas Compuestas	
Simpson	$\frac{h}{3} \left[f(x_0) + 2 \sum_{j=1}^{\left(\frac{n}{2}\right)-1} f(x_{2j}) + 4 \sum_{j=1}^{\left(\frac{n}{2}\right)} f(x_{2j-1}) + f(x_n) \right] - \frac{x_n - x_0}{180} h^4 f^{(4)}(\mu)$
Trapezio	$\frac{h}{2} \left[f(x_0) + 2 \sum_{j=1}^{n-1} f(x_j) + f(x_n) \right] - \frac{x_n - x_0}{12} h^2 f^{(2)}(\mu)$ $h = \frac{x_n - x_0}{n} \quad x_j = x_0 + j \cdot h$
Punto Medio	$2h \sum_{j=0}^{\left(\frac{n}{2}\right)} f(x_{2j}) - \frac{x_n - x_0}{6} h^2 f^{(2)}(\mu)$ $h = \frac{x_n - x_0}{n+2} \quad x_j = x_0 + (j+1)h$