Recitation 1

21256: Section C

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Intro

- Junior at CMU, studying Math!
- Hobbies: Sports, Gaming, Music

Class Stuff

- OH: Thursday 2:30-3:30 PM, 8:30-9:30 PM
- Office hours are for theory questions/homework help. You may email me to set up an appointment if you wish
- Use Piazza for questions, please make posts public
- Recitation notes and videos will be posted at: www.lieric.com/teaching
- Feel free to email me at ericl2@andrew.cmu.edu if you have any questions or concerns!

Recitation Strategy

- Generally, we will spend 5-10 minutes covering theory, then the rest of recitation doing fun problems. We may occasionally break into groups to work on problems together.
- I will send polls occasionally to see how things are going
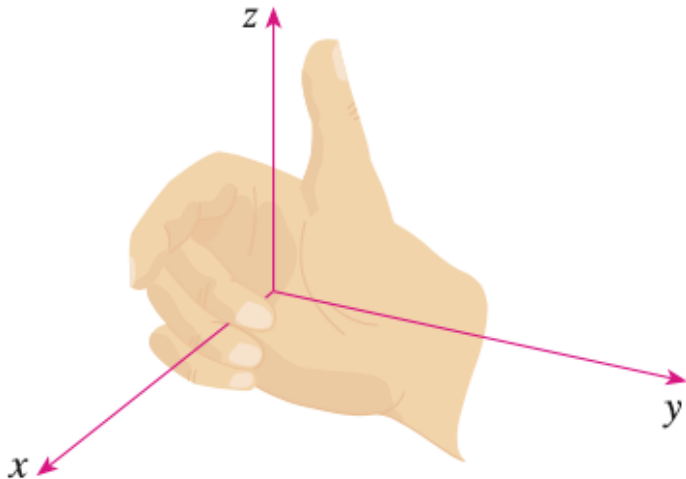- Last 5-10 minutes, I will split you into breakout rooms.

Multivariate Calculus is everywhere, including:

- Machine Learning
- Statistics/Data Science
- Numerical Methods
- Physics
- Portfolio Optimization
- Future classes at CMU

3D Space

Formulas

Distance Formula for Three Dimensions

The distance $|P_1P_2|$ between $P_1(x_1, y_1, z_1)$ and $P_2(x_2, y_2, z_2)$ is:

$$|P_1P_2| = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2 + (z_1 - z_2)^2}$$

Equation of a Sphere

The equation of a sphere centered at $C = (h, k, l)$ and with radius r is:

$$(x - h)^2 + (y - k)^2 + (z - l)^2 = r^2$$

Problems

Problem 1

Find an equation of a sphere with center $(-3, 2, 5)$ and radius 4.
What is the intersection of this sphere with the *yz*-plane?

Problem 2

Find an equation of the sphere that passes through the point $(4, 3, -1)$ and has the center $(3, 8, 1)$.

Show that the following equation represents a sphere, and find its center and radius:

$$x^2 + y^2 + z^2 + 8x - 6y + 2z + 17 = 0$$

Problem 4

Show that the following equation represents a sphere, and find its center and radius:

$$2x^2 + 2y^2 + 2z^2 = 8x - 24z + 1$$

Problem 5

Describe in words the region of $\mathbb{R}^3$ represented by the equation(s) or inequality:

$$0 \leq z \leq 6$$

Problem 6

Describe in words the region of $\mathbb{R}^3$ represented by the equation(s) or inequality:

$$1 \le x^2 + y^2 + z^2 \le 5$$

Problem 7

Describe in words the region of $\mathbb{R}^3$ represented by the equation(s) or inequality:

$$1 \leq x^2 + z^2 \leq 9$$

Problem 8

Write inequalities to describe the following regions:

The region consisting of all points between (but not on) the spheres of radius r and R centered at the origin, where $r < R$:

Questions?