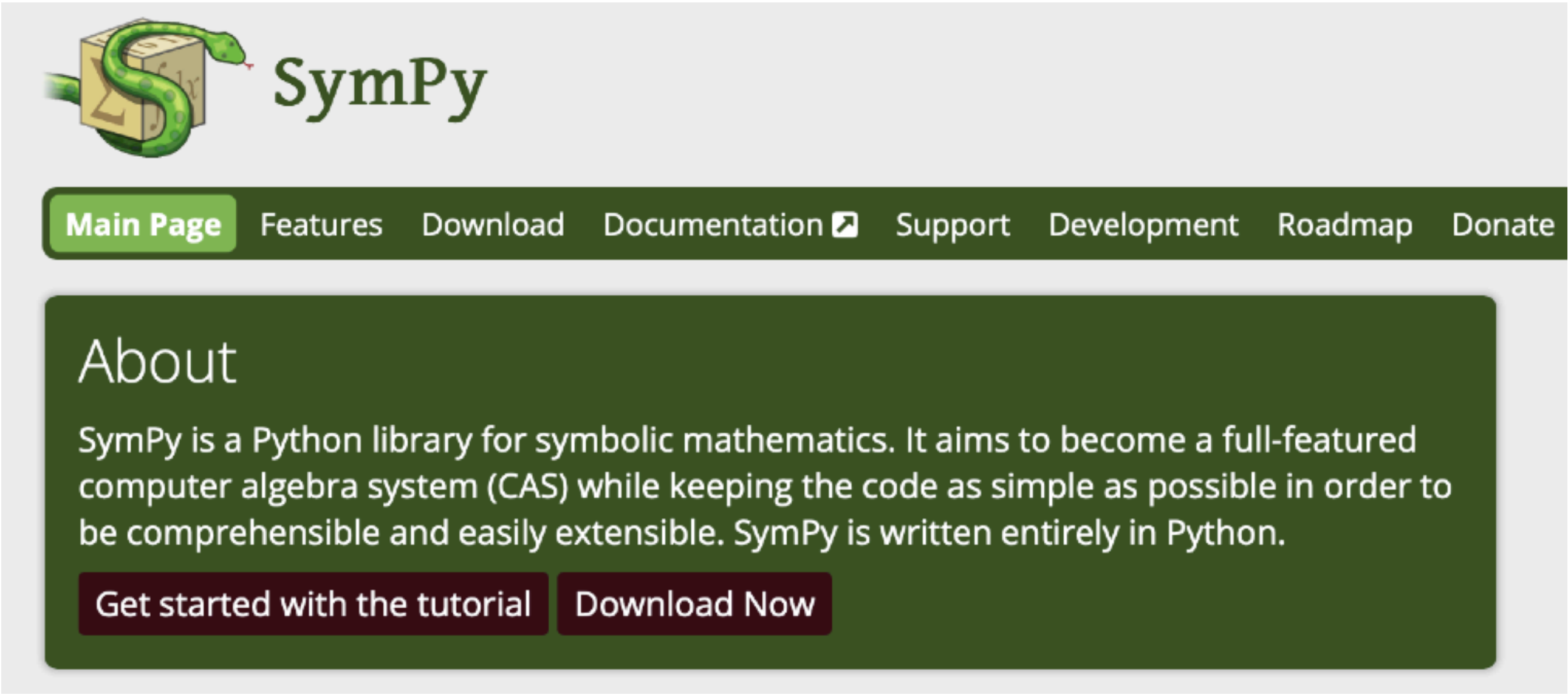


Experiment

Experiment 3: Extended Kalman Filter（每1秒分析一次，使用擴展卡爾曼濾波器）



切線性模型：

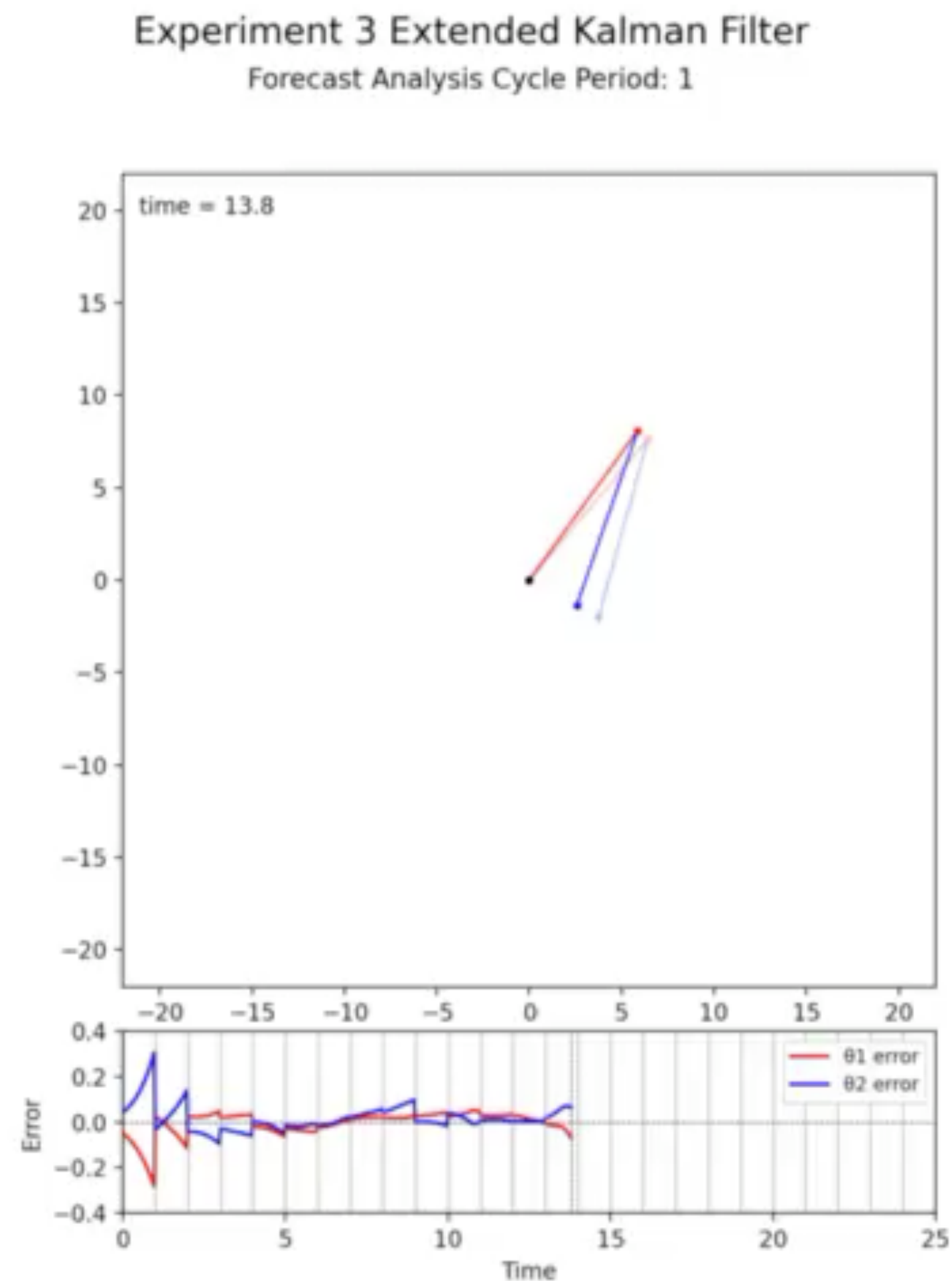
$$\begin{aligned}\theta_{1i} &= \theta_{1i-1} + \dot{\theta}_{1i}\Delta t \\ \theta_{2i} &= \theta_{2i-1} + \dot{\theta}_{2i}\Delta t \\ \dot{\theta}_{1i} &= \dot{\theta}_{1i-1} + \frac{m_2 g \sin \theta_{2i} \cos(\theta_{1i} - \theta_{2i}) - m_2 \sin(\theta_{1i} - \theta_{2i})(l_1 \dot{\theta}_1^2 \cos(\theta_{1i} - \theta_{2i}) + l_2 \dot{\theta}_2^2) - (m_1 + m_2)g \sin \theta_{1i}}{l_1(m_1 + m_2 \sin^2(\theta_{1i} - \theta_{2i}))} \Delta t \\ \dot{\theta}_{2i} &= \dot{\theta}_{2i-1} + \frac{(m_1 + m_2)l_1 \dot{\theta}_1^2 \sin(\theta_{1i} - \theta_{2i}) - g \sin \theta_{2i} + g \sin \theta_{1i} \cos(\theta_{1i} - \theta_{2i}) + m_2 l_2 \dot{\theta}_2^2 \sin(\theta_{1i} - \theta_{2i}) \cos(\theta_{1i} - \theta_{2i})}{l_2(m_1 + m_2 \sin^2(\theta_{1i} - \theta_{2i}))} \Delta t\end{aligned}$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ -\frac{2m_2(-gm_2 \sin(\theta_1 - 2\theta_2) - g(2m_1 + m_2) \sin(\theta_1) - 2m_2(l_1 \dot{\theta}_1^2 \cos(\theta_1 - \theta_2) + l_2 \dot{\theta}_2^2) \sin(\theta_1 - \theta_2)) \sin(2\theta_1 - 2\theta_2)}{l_1(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)^2} + \frac{-gm_2 \cos(\theta_1 - 2\theta_2) - g(2m_1 + m_2) \cos(\theta_1) + 2l_1 m_2 \dot{\theta}_1^2 \sin^2(\theta_1 - \theta_2) - 2m_2(l_1 \dot{\theta}_1^2 \cos(\theta_1 - \theta_2) + l_2 \dot{\theta}_2^2) \cos(\theta_1 - \theta_2)}{l_1(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)} & \frac{2m_2(-gm_2 \sin(\theta_1 - 2\theta_2) - g(2m_1 + m_2) \sin(\theta_1) - 2m_2(l_1 \dot{\theta}_1^2 \cos(\theta_1 - \theta_2) + l_2 \dot{\theta}_2^2) \sin(\theta_1 - \theta_2)) \sin(2\theta_1 - 2\theta_2)}{l_1(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)^2} + \frac{2gm_2 \cos(\theta_1 - 2\theta_2) - 2l_1 m_2 \dot{\theta}_1^2 \sin^2(\theta_1 - \theta_2) + 2m_2(l_1 \dot{\theta}_1^2 \cos(\theta_1 - \theta_2) + l_2 \dot{\theta}_2^2) \cos(\theta_1 - \theta_2)}{l_1(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)} & -\frac{4m_2 \dot{\theta}_1 \sin(\theta_1 - \theta_2) \cos(\theta_1 - \theta_2)}{2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2} & -\frac{4l_2 m_2 \dot{\theta}_2 \sin(\theta_1 - \theta_2)}{l_1(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)} \\ -\frac{4m_2(g(m_1 + m_2) \cos(\theta_1) + l_1 \dot{\theta}_1^2(m_1 + m_2) + l_2 m_2 \dot{\theta}_2^2 \cos(\theta_1 - \theta_2)) \sin(\theta_1 - \theta_2) \sin(2\theta_1 - 2\theta_2)}{l_2(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)^2} + \frac{2(-g(m_1 + m_2) \sin(\theta_1) - l_2 m_2 \dot{\theta}_2^2 \sin(\theta_1 - \theta_2)) \sin(\theta_1 - \theta_2)}{l_2(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)} + \frac{2(g(m_1 + m_2) \cos(\theta_1) + l_1 \dot{\theta}_1^2(m_1 + m_2) + l_2 m_2 \dot{\theta}_2^2 \cos(\theta_1 - \theta_2)) \cos(\theta_1 - \theta_2)}{l_2(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)} & \frac{2m_2 \dot{\theta}_2^2 \sin^2(\theta_1 - \theta_2)}{2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2} + \frac{4m_2(g(m_1 + m_2) \cos(\theta_1) + l_1 \dot{\theta}_1^2(m_1 + m_2) + l_2 m_2 \dot{\theta}_2^2 \cos(\theta_1 - \theta_2)) \sin(\theta_1 - \theta_2) \sin(2\theta_1 - 2\theta_2)}{l_2(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)^2} & -\frac{2(g(m_1 + m_2) \cos(\theta_1) + l_1 \dot{\theta}_1^2(m_1 + m_2) + l_2 m_2 \dot{\theta}_2^2 \cos(\theta_1 - \theta_2)) \cos(\theta_1 - \theta_2)}{l_2(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)} & -\frac{4l_1 \dot{\theta}_1(m_1 + m_2) \sin(\theta_1 - \theta_2)}{l_2(2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2)} & -\frac{4m_2 \dot{\theta}_2 \sin(\theta_1 - \theta_2) \cos(\theta_1 - \theta_2)}{2m_1 - m_2 \cos(2\theta_1 - 2\theta_2) + m_2} \end{bmatrix}$$

還好我沒有用手算^^

Experiment

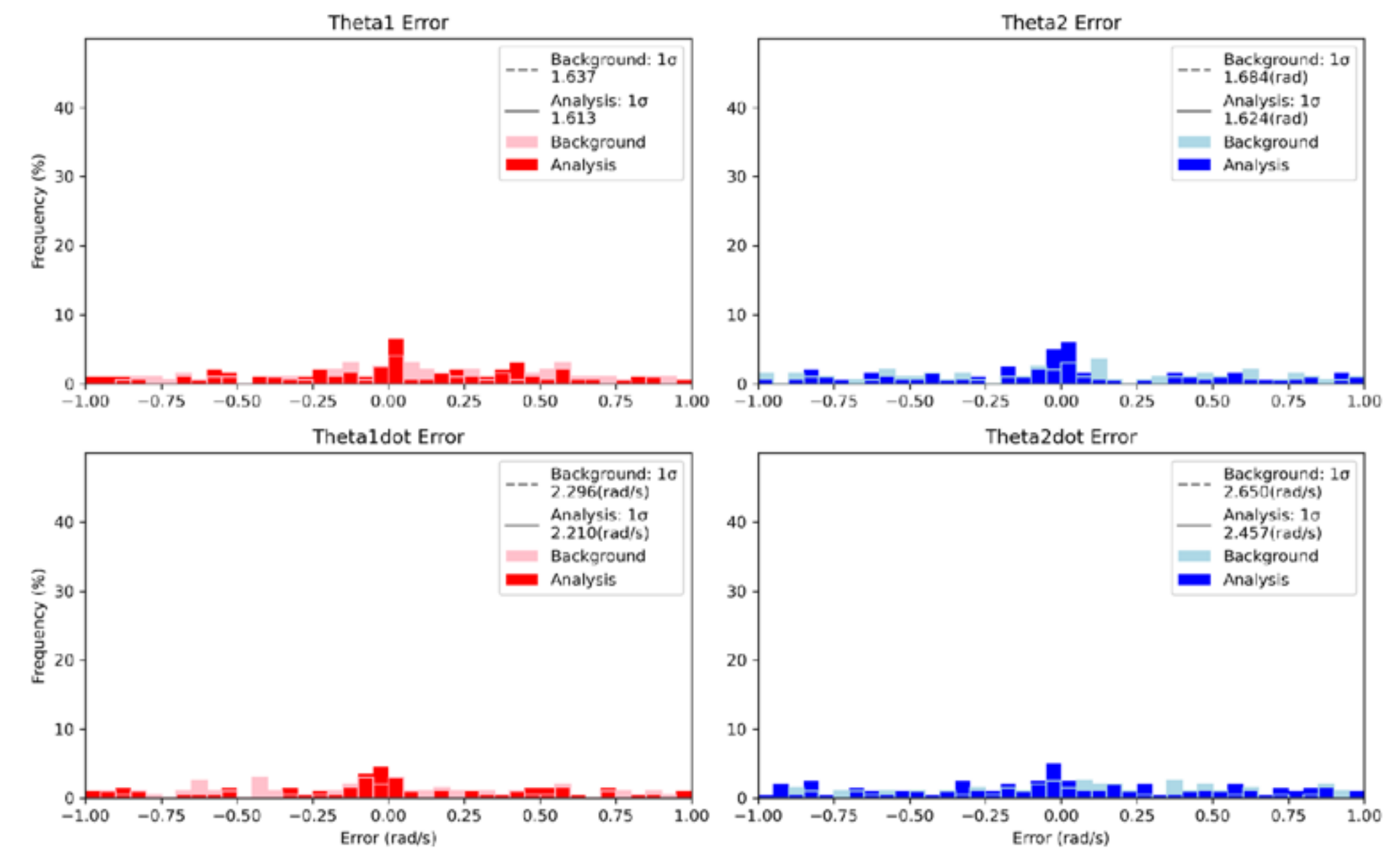
Experiment 3: Extended Kalman Filter (每1秒分析一次，使用擴展卡爾曼濾波器)



註：初始的 $\mathbf{B} = \mathbf{R}$

分析誤差相較於背景誤差改變了多少？

Experiment 3: Analysis vs Background



此實驗相較於觀測即分析時

θ_1 分析標準差：0.0361.613 (rad)

θ_2 分析標準差：0.0361.624 (rad)

$\dot{\theta}_1$ 分析標準差：0.0482.210 (rad/s)

$\dot{\theta}_2$ 分析標準差：0.0482.457 (rad/s)