

MOSEK Rmosek Package

Release 8.0.0.74

MOSEK ApS

CONTENTS

1	Introduction 1.1 Why the Rmosek Package?	. 1
	1.2 License agreement	
2	Installation	3
	2.1 Windows Platforms	
	2.2 UNIX-alike Platforms	. 6
3	Guidelines	9
	3.1 Parallel optimization Using the The Multicore Package	
	3.2 The license system	. 9
4	Basic Tutorials	11
	4.1 The Basics Tutorial	
	4.2 Linear Optimization	
	4.3 Conic Quadratic Optimization	
	4.4 Semidefinite Optimization	
	4.5 Quadratic Optimization	
	4.7 Solution Analysis	
	4.8 Solver Parameters	
5	Nonlinear Tutorials	27
J	5.1 Separable Convex (SCopt) Interface	
6	Managing I/O	31
	6.1 Stream I/O	
	6.2 File I/O	
	6.3 Verbosity	. 32
7	Problem Formulation and Solutions	33
	7.1 Linear Optimization	
	7.2 Conic Quadratic Optimization	
	7.3 Semidefinite Optimization	
	7.4 Quadratic and Quadratically Constrained Optimization	
	7.5 General Convex Optimization	. 41
8	The Optimizers for Continuous Problems	43
	8.1 Presolve	. 43
	8.2 Linear Optimization	. 45
	8.3 Conic Optimization	
	8.4 Nonlinear Convex Optimization	
	8.5 Using Multiple Threads in an Optimizer	. 53
9	The Optimizer for Mixed-integer Problems	55
	9.1 Some Concepts and Facts Related to Mixed-integer Optimization	. 55

9.2	The Mixed-integer Optimizer	6
9.3	Termination Criterion	6
9.4	Parameters Affecting the Termination of the Integer Optimizer	7
9.5	How to Speed Up the Solution Process	7
9.6	Understanding Solution Quality	8
10 A D	I Reference 59	^
		_
10.1		_
10.5		
10.3	The state of the s	
10.4	4 Enumerations	2
11 Su	oported File Formats 159	9
11.	The LP File Format	0
11.5	2 The MPS File Format	5
11.5		
11.4	4 The CBF Format	6
11.		
11.6		
11.		
11.8		
11.0	The goldwon the formation	J
12 Int	erface changes 21:	1
12.	Parameters	1
12.5	2 Constants	3
12.3	8 Response Codes	7
Biblio	graphy 21:	9
APII	ndey 22	1

CHAPTER

ONE

INTRODUCTION

The **MOSEK** Optimization Suite 8.0.0.74 is a powerfull software package capable of solving large-scale optimization problems of the following kind:

- linear,
- convex quadratic,
- conic quadratic (also known as second-order cone),
- semidefinite,
- and general convex.

Integer constrained variables are supported for all problem classes except for semidefinite and general convex problems. In order to obtain an overview of features in the **MOSEK** Optimization Suite consult the product introduction guide.

1.1 Why the Rmosek Package?

The Rmosek Package provides access to most functionalities of **MOSEK** from an R-language software environment. The package is adjusted to the typical R user.

1.2 License agreement

Before using the **MOSEK** software, please read the license agreement available in the distribution at <MSKHOME>/mosek/8/mosek-eula.pdf or on the **MOSEK** website https://mosek.com/sales/license-agreement.

MOSEK uses some third-party open-source libraries. Their license details follows.

zlib

MOSEK includes the zlib library obtained from the zlib website. The license agreement for zlib is shown in Listing 1.1.

Listing 1.1: zlib license.

```
zlib.h -- interface of the 'zlib' general purpose compression library version 1.2.7, May 2nd, 2012
```

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fplib

MOSEK includes the floating point formatting library developed by David M. Gay obtained from the netlib website. The license agreement for *fplib* is shown in Listing 1.2.

Listing 1.2: fplib license.

INSTALLATION

2.1 Windows Platforms

The interface documented here is part of the Rmosek package distributed from http://rmosek.r-forge.r-project.org/. Notice, however, that a pre-compiled binary version of it has not been distributed. Thus a small amount of configuration is necessary in order to install the package. It is not very difficult, but besides the basic installation of R you will need two pieces of software readily available through the Internet. In summary:

- MOSEK (the optimization library we interface to.
- Rtools (the tools needed for R package development

The following is a step-by-step guide through the installation of the package. We skip the installation of **MOSEK** as it has been well documented elsewhere and assume that the target machine already has a working installation. Please refer to the documentation available at https://mosek.com/resources/doc/for-the-verification of this installation.

For additional help installing this interface, the section on packages in the R for Windows FAQ available on the CRAN website may be useful. The R Installation and Administration manual, also published by CRAN on their website, is another good source of information.

2.1.1 Setting Up the Target Machine

Assuming a working installation of R and MOSEK on the machine targeted for the R-to-MOSEK interface, the first step is to download Rtools for Windows. From this program you will need to install the component called R toolset, the $Cygwin\ DLLs$, and the R toolchain.

Note: R toolset and Cygwin DLLs will extend the Windows CMD with Unix-style commands, while the R toolchain (based on MinGW compilers) makes it possible to compile the C++ source code in the package. These components can be replaced by any other Unix-style shell and C++ build chain, but in the remaining guide the use of Rtools will be assumed.

After the installation of Rtools you will have to set the Windowsenvironment variable called PATH, in order to utilize the components. Assuming that the home directory of the Rtools installation was C:\Rtools, the entries shown below will have to be added to the existing PATH variable. Note that all entries in the PATH variable must be separated by a semicolon (;), and that all these entries have to represent folders that exist on the target machine.

- Add C:\Rtools\bin; to enable the R toolset and Cygwin DLLs.
- Add C:\Rtools\gcc-VERSIONbin; (for some VERSION) to enable the R toolchain.

That was it, but before we move on to the installation process, please ensure that the PATH variable also contains the bin folder of all MOSEK installations (32 and/or 64 bit) that you wish this interface to target. This is necessary for automatic configuration to work, and could look something like:

C:\Program\Mosek\8\tools\platform\win64x86\bin

2.1.2 Installing the Package with Automatic Configuration

Automatic configuration works equivalently to calling where mosek in the Windows CMD. It searches the environment variable called PATH for a folder with an executable called mosek. Note that if more than one such folder exists, only the one mentioned first in the PATH variable is chosen. It then determines the most ordinary of the available optimization libraries within this folder (typically mosek.lib or mosek64.lib), along with other relevant information. This configuration should work for all users installing the package on a single architecture (64 or 32 bit) and only requiring the ordinary optimization library. Otherwise, manual configuration of the package will be needed.

Now open R for the architecture (64 or 32 bit) you wish to install the package on. Make sure all your packages are up to date by writing update.packages(), and execute a command similar to the one shown below. This will install the Rmosek package:

Note that this package will have to be installed from *source* as it needs a static link to the **MOSEK** optimization library. This unfortunately means that dependencies (i.e. the *Matrix* package) will also be installed from source if new releases are available. Since it is more time-consuming to install the *Matrix* package from source, it is recommended to start with a call to update.packages(). The availability of the *Matrix* package should not be a problem, as it has been part of the standard R installation since version 2.9.0.

2.1.3 Installing the Package with Manual Configuration

If the automatic configuration does not suit your particular needs, or fails for some reason, a manual configuration may work instead. Unfortunately the configure.vars parameter of the install.packages command does not work on Windows, meaning that the files of the Rmosek source package will have to be edited. This can be difficult for non-savvy users, but have hopefully been documented sufficiently here.

How to manually configure the Rmosek package?

When you download the package from http://rmosek.r-forge.r-project.org/, it comes in a compressed archive called RMOSEK_VERSION.tar.gz for some version number VERSION. In order to configure the package, you will have to go through the following steps. A more thorough explanation of each step will be given afterwards.

- 1. Extract the archive into a directory.
- 2. Setup the local system descriptors, Localsys.txt, for each of the sub-architectures you will be using: 64 bit (e.g. x64) and/or 32 bit (e.g. i386). These files come with a guide written into them that clearly states how this should be done.
- 3. Compress the directory back into an archive.

The first step is to extract the <code>rmosek_VERSION.tar.gz</code> archive that you downloaded. This can either be done by using one of the many tools freely available online, or the <code>tar</code> command that was installed with Rtools. If you choose to use the <code>tar</code> command, you can extract the package by opening Windows CMD and executing a command similar to:

```
tar --no-same-owner -zxvf LOCATION/RMOSEK_VERSION.tar.gz
```

Remember to exchange *LOCATION* and *VERSION* with the correct values. For those not familiar with Windows CMD, we recommend the use of an external tool as this configuration can then be performed entirely within Windows Explorer.

The second step is to tell the package where to find the MOSEK optimization library. Open the extracted directory called Rmosek in either Windows CMD or Windows Explorer, and navigate to the subdirectory called src\setup. If you want to install a 64 bit version of the package (making an interface between 64 bit R and 64 bit MOSEK), open the folder x64 and follow the guide in Localsys.txt. If you want to install a 32 bit version of the package (making an interface between 32 bit R and 32 bit MOSEK), open instead the folder i386 and follow the guide in this Localsys.txt. An example of this is shown below

Listing 2.1: An exampel of local system descriptor.

```
##
## Greetings user of the R-to -MOSEK interface !
##
## If you are sitting on a WINDOWS 64 bit platform , this is the file that
## you will have to setup before this package can be installed .
## (see e.g. the R\text{-to} -MOSEK userguide )
##
##################
## Step 1 of 2 ##
#################
## Please \ substitute \ [\ MOSEK_HOME_PATH\ ] \ below , with the path to the
## platform - specific folder within the MOSEK installation you want to
## use. Note that this path should contain a "bin" and a "h" folder .
## -----
## For example you can write:
## PKG\_MOSEKHOME = C: \ Progra ~1 \ Mosek \ 8 \ tools \ platform \ win64x86
##
## If your computer contains the two directories :
PKG_MOSEKHOME = [ MOSEK_HOME_PATH ]
#################
## Step 2 of 2 ##
#################
## Please substitute [ MOSEK_LIB_FILE ] below , with the name of the library
\hbox{\it \#\# you wish to use within the "bin" folder of your PKG\_MOSEKHOME path.}
\textit{## This "bin" folder must contain a file called [ \textit{MOSEK\_LIB\_FILE }]. \ lib.}
## Continuing the example from above , you can write:
## PKG_MOSEKLIB = mosek64_8_0
## If your computer contains the file:
## C:\ Progra ~1\ Mosek \ |8| tools| platform \ win64x86 \ bin\ mosek64_8_0 .lib
PKG_MOSEKLIB =[ MOSEK_LIB_FILE ]
```

The third and final step is to compress the (previously extracted and now altered) directory called Rmosek, back into the Rmosek_VERSION.tar.gz archive. Again you can either make use of the external tools from step one, or open the Windows CMD and execute a command similar to:

```
tar -zcvf Rmosek_VERSION.tar.gz Rmosek`
```

How to install the manually configured Rmosek package?

Open R, either the console or the graphical user interface, for the architecture (64 or 32 bit) you wish to install the package on. Make sure all your packages are up to date by writing update.packages(),

and execute the following command to install the Rmosek package::

Remember to exchange *LOCATION* and *VERSION* with the correct values. The first argument should be the path to your manually configured package. The second argument tells that the package is local and not in an online repository. The third argument tells that it is a source package and so should be compiled. The fourth and final argument specifies that you only wish to install the package to the specific architecture (64 or 32 bit) of the opened R program. If you wish to install on both architectures, and did configure the package for both 32 and 64 bit, simply remove this last argument.

Notice that if you wish to uninstall the Rmosek package at some point, this can be done as for any other package with the command remove.packages(Rmosek).

2.2 UNIX-alike Platforms

The interface documented here is part of the Rmosek package distributed from http://rmosek.r-forge.r-project.org/. Notice, however, that a pre-compiled binary version of it has not been distributed (Such a binary would have to be built individually for each version of R and MOSEK). Thus a small amount of configuration is necessary in order to install the package. It is not very difficult, but besides the basic installation of R you will need MOSEK (the optimization library we interface to) readily available through the Internet.

The following is a step-by-step guide through the installation of the package. We skip the installation of **MOSEK** as it has been well documented elsewhere and assume that the target machine already has a working installation. Please refer to the documentation available at https://mosek.com/resources/doc/for the verification of this installation.

For additional help on installing this interface, the section on installing packages in the manual *R Installation and Administration*, published on the CRAN website, is a good source of information.

2.2.1 Setting Up the Target Machine

We assume here that you have a working installation of R and **MOSEK** on the machine targeted for the R-to-**MOSEK** interface. The architectures (32 or 64 bit) of these two programs must be exactly the same for consistency. We further assume that the target machine have a build chain (e.g. GCC compilers for C/C++) installed.

For automatic configuration to work, the PATH variable should contain the bin folder of the single MOSEK installation (32 or 64 bit) that you wish this interface to target. This could look something like:

```
~/mosek/8/tools/platform/linux64x86/bin
```

If more than one bin folder from a MOSEK installation are specified, only the first one will be found by automatic configuration. Additional architectures can be added afterwards if necessary.

2.2.2 Installing the Package with Automatic Configuration

Automatic configuration works equivalently to calling which mosek in a terminal window. It searches the environment variable called PATH for a folder with an executable called mosek. Note that if more than one such folder exists, only the one mentioned first in the PATH variable is chosen. It then determines the most ordinary of the available optimization libraries within this folder (typically libmosek or libmosek64 with the extension .so or .dylib), along with other relevant information. This configuration should work for all users only installing the package on a single architecture (64 or 32 bit) and only requiring the ordinary optimization library. Otherwise, manual configuration of the package will be needed.

Now open R for the architecture (64 or 32 bit) you wish to install the package on. Make sure all your packages are up to date by writing update.packages(), and execute a command similar to the one shown below. This will install the Rmosek package::

Note that this package will have to be installed from *source* as it needs a static link to the **MOSEK** optimization library. This unfortunately means that dependencies (i.e. the 'Matrix' package) will also be installed from source if new releases are available. Since it is more time-consuming to install the *Matrix* package from source, it is recommended to start with a call to update.packages(). The availability of the *Matrix* package should not be a problem, as it has been part of the standard R installation since version 2.9.0.

2.2.3 Installing the Package with Manual Configuration

Open R for one of the architectures (64 or 32 bit) you wish to install the package on. Make sure all your packages are up to date by writing update.packages(), and execute a command similar to the one shown below, with a correct definition of PKG_MOSEKHOME and PKG_MOSEKLIB. This will install the Rmosek package:

Remember to exchange the ... of both PKG_MOSEKHOME and PKG_MOSEKLIB with the correct values, explained as follows. The definition of the first argument, PKG_MOSEKHOME, should be the folder in your MOSEK installation, containing a bin and h subdirectory for the platform and architecture matching that of the opened R program. This could for instance look something like:

```
/ \texttt{home/username/mosek/8/tools/platform/linux} 64 \texttt{x} 86
```

Notice that auto-expansions such as \sim does not work, and in case the folder definition contains spaces you will either have to wrap the definition in single-quotes or add backslashes in front of all spaces.

The definition of the argument PKG_MOSEKLIB should be the name of the optimization library in the bin subdirectory that you wish to utilize in the Rmosek package. This library will be statically linked to the package after a successful installation. Note that the name of the optimization library should be specified without the *lib* prefix, and without its file-extension. The PKG_RMOSEKLIB would thus normally be either mosek or mosek64 (linking to respectively libmosek.so and libmosek64.so, or respectively libmosek.dylib and libmosek64.dylib, depending on the Unix-alike system). Using mosek64 requires a 64 bit version of the opened R program and MOSEK installation, while mosek implies 32 bit.

How to install on multiple architectures?

If you wish to install the Rmosek package on multiple sub-architectures, you will first have to follow the above guide and install the package on one of the architectures (e.g. 32 or 64 bit). Afterwards as explained here, it can then be extended to other sub-architectures. This is also explained in *R Installation and Administration* (published on the CRAN website), in the subsection *Multiple sub-architectures* under *Installing packages*. For this to work you will need a preinstalled version of R and **MOSEK** in all the sub-architectures you wish this package to work with.

Open R in the sub-architecture you wish to extend your installation to, and execute a command similar to the one shown below::

```
install.packages("Rmosek", type="source", libs_only=TRUE, repos="http://download.mosek.com/R/8

→", configure.vars="PKG_MOSEKHOME=... PKG_MOSEKLIB=...")
```

Remember to exchange ... of the variables PKG_MOSEKHOME and PKG_RMOSELIB, so that declared MOSEK installation always correspond to the current sub-architecture of the opened R program.

How to install from an offline location?

This is almost the same a described above except that you would have to add the argument repos=NULL to tell R that it should not use an online repository. Also, instead of writing the package name Rmosek, you should write the entire file-location of the package source file which should look something like LOCATION/Rmosek_VERSION.tar.gz.

What are the command-line equivalents?

Sometimes you do not want to open R for all sub-architectures, but instead perform the installation directly from the console. Notice though, that this will require you to download the package source as you will only be able to install from an offline location in this way. In the two commands below you will have to replace SUBARCH_PATH, DIR and VERSION with the correct values, but doing so should be straight forward. Notice that on newer versions of R (>=2.12), you can also use the call R --arch SUBARCH, instead of specifying the SUBARCH_PATH. Remember to exchange . . . of the variables PKG_MOSEKHOME and PKG_MOSEKLIB, with the correct values as previously explained.

For the first architecture::

```
SUBARCH_PATH/R CMD INSTALL DIR/Rmosek_VERSION.tar.gz --no-multiarch --configure-vars="PKG_

$\times \text{MOSEKHOME} = \text{...} \text{ PKG_MOSEKLIB} = \text{...}"
```

For subsequent architectures::

```
SUBARCH_PATH/R CMD INSTALL DIR/Rmosek_VERSION.tar.gz --libs-only --configure-vars="PKG_

$\times MOSEKHOME = \ldots \text{PKG_MOSEKLIB} = \ldots \text{"}$
```

CHAPTER

THREE

GUIDELINES

3.1 Parallel optimization Using the The Multicore Package

The R package called *multicore*, provides functions for parallel execution of R code on machines with multiple cores or CPUs. Windows is not currently supported, but the package should work on most UNIX-alike platforms.

The multicore package works by copying the full memory state of the R session to new processes. While this seems like a large overhead, in practice, the copy is delayed until modification assuring a smooth parallel execution. The downside is that this low-level memory state copy is not safe for all types of resources. As an example, parallel interactions with the GUI or on-screen devices can cause the R session to crash. It is thus recommended only to use the multicore package in console R.

In the Rmosek package a license is an externally acquired resource, and attempts to simply copy the memory state of this resource will provoke a session crash. Thus, licenses should always be released before the time of parallelization.

Note: Always call mosek_clean() before a parallelizing operator. Failure to do so is likely to provoke session crashes.

A consequence of this is that each new process will be using a separate license. That is, your license system should allow 8 licenses to be checked out simultaneously, if you wish to solve 8 optimization problems in parallel. Please note that unlimited academic and commercial licenses are available at **MOSEK**.

3.2 The license system

MOSEK is a commercial product that always needs a valid license to work. A license is typically provided as a license file that allows the user to access the subset of the MOSEK Optimization Suite functionalities it is entitled for, and for the right amount of time. MOSEK uses a third party license manager to implement license checking.

By default a license token remains checked out for the duration of the MOSEK session, i.e.

- 1. a license token is checked out when mosek is called the first time and
- 2. it is returned when R is terminated, or calling mosek_clean.

To change the license systems behavior to returning the license token after each call to \mathbf{MOSEK} set the parameter $MSK_IPAR_CACHE_LICENSE$ to MSK_OFF .

```
prob$iparam <- list(CACHE_LICENSE = "MSK_OFF");</pre>
```

3.2.1 Waiting for a free license

By default an error will be returned if no license token is available. By setting the parameter $MSK_IPAR_LICENSE_WAIT$ MOSEK can be instructed to wait until a license token is available.

```
prob$iparam <- list(LICENSE_WAIT = "MSK_ON");</pre>
```

3.2.2 Manually stopping the license system

The license can be manually released by calling ${\it mosek_clean}\,.$

BASIC TUTORIALS

In this section a number of examples is provided to demonstrate the functionality required for solving linear, conic, semidefinite and quadratic problems as well as mixed integer problems.

- Basic tutorial: This is the simplest tutorial: it solves a linear optimization problem read from file. It will show how
 - setup the \mathbf{MOSEK} environment and problem task,
 - run the solver and
 - check the optimization results.
- Linear optimization tutorial: It shows how to input a linear program. It will show how
 - define variables and their bounds,
 - define constraints and their bounds,
 - define a linear objective function,
 - input a linear program but rows or by column.
 - retrieve the solution.
- Conic quadratic optimization tutorial: The basic steps needed to formulate a conic quadratic program are introduced:
 - define quadratic cones,
 - assign the relevant variables to their cones.
- Semidefinite optimization tutorial: How to input semidefinite optimization problems is the topic of this tutorial, and in particular how to
 - input semidefinite matrices and in sparse format,
 - add semidefinite matrix variable and
 - formulate linear constraints and objective function based on matrix variables.
- Mixed-Integer optimization tutorial: This tutorial shows how integrality conditions can be specified.
- Quadratic optimization tutorial : It shows how to input quadratic terms in the objective function and constraints.
- Solution analysis: This tutorial shows how the user can analyze the solution returned by the solver.
- Parameter setting tutorial : This tutorial shows how to set the solver parameters.

4.1 The Basics Tutorial

The simplest program using the \mathbf{MOSEK} R interface can be described shortly:

- 1. Load a problem into a problem structure (a task).
- 2. Optimize the problem.
- 3. Fetch the result.

Listing 4.1: A simple script that reads a problem from file and solves it.

```
simple <- function( filename)</pre>
 r <- mosek_read(filename, list(usesol=FALSE, useparam=TRUE))</pre>
 if (identical(r$response$code, 0)) {
    print("Successfully read the optimization model")
   prob <- r$prob</pre>
   r <- try(mosek(prob, list(verbose=0)), silent=TRUE)</pre>
    if (inherits(r, "try-error")) {
      stop("Rmosek failed somehow!")
    if (!identical(r$response$code, 0)) {
      cat(paste("**", "Response code:", r$response$code, "\n"))
      cat(paste("**", r$response$msg, "\n"))
      cat("Trying to continue..\n")
    isdef <- try({</pre>
      rbas <- r$sol$bas;</pre>
     rbas$solsta; rbas$prosta; rbas$xx;
    }, silent=TRUE)
    if (inherits(isdef, "try-error")) {
      stop("Basic solution was incomplete!")
    }
    switch(rbas$solsta,
      OPTIMAL = {
        cat("The solution was optimal, I am happy!\n")
      },
      NEAR_OPTIMAL = {
        cat("The solution was close to optimal, very good..\n")
      },
      #OTHERWISE:
        cat(paste("**", "Solution status:", rbas$solsta, "\n"))
        cat(paste("**", "Problem status:", rbas$prosta, "\n"))
        stop("Solution could not be accepted!")
   )
 }
}
```

4.2 Linear Optimization

The simplest optimization problem is a purely linear problem. A *linear optimization problem* is a problem of the following form:

Minimize or maximize the objective function

$$\sum_{j=0}^{n-1} c_j x_j + c^f$$

subject to the linear constraints

$$l_k^c \le \sum_{j=0}^{n-1} a_{kj} x_j \le u_k^c, \quad k = 0, \dots, m-1,$$

and the bounds

$$l_i^x \le x_j \le u_i^x, \quad j = 0, \dots, n - 1,$$

where we have used the problem elements:

- \bullet m and n which are the number of constraints and variables respectively,
- x which is the variable vector of length n,
- \bullet c which is a coefficient vector of size n

$$c = \left[\begin{array}{c} c_0 \\ \vdots \\ c_{n-1} \end{array} \right],$$

- c^f which is a constant,
- A which is a $m \times n$ matrix of coefficients is given by

$$A = \begin{bmatrix} a_{0,0} & \cdots & a_{0,(n-1)} \\ \vdots & \cdots & \vdots \\ a_{(m-1),0} & \cdots & a_{(m-1),(n-1)} \end{bmatrix},$$

- l^c and u^c which specify the lower and upper bounds on constraints respectively, and
- l^x and u^x which specifies the lower and upper bounds on variables respectively.

Note: Please note the unconventional notation using 0 as the first index rather than 1. Hence, x_0 is the first element in variable vector x.

4.2.1 Example LO1

The following is an example of a linear optimization problem:

having the bounds

This is easily programmed in R as shown in Listing 4.2. The first line overwrites any previous definitions of the variable *lo1*, preparing for the new problem description. The problem is then defined and finally solved on the last line.

Listing 4.2: R implementation of problem (4.1).

```
get_lo1_solution_variables <- function(maxtime) {</pre>
 lo1 <- list(sense="max", c=c(3,1,5,1))</pre>
 lo1$A <- Matrix(c(3,1,2,0,2,1,3,1,0,2,0,3),
             nrow=3, byrow=TRUE, sparse=TRUE)
 lo1$bc <- rbind(blc=c(30,15,-Inf), buc=c(30,Inf,25));
 lo1$bx <- rbind(blx=c(0,0,0,0)),
                                     bux=c(Inf,10,Inf,Inf));
 lo1$dparam <- list(OPTIMIZER_MAX_TIME=maxtime)</pre>
 r <- try(mosek(lo1, list(verbose=0)), silent=TRUE)
 if (inherits(r, "try-error")) {
    stop("Rmosek failed somehow!")
 }
 if (!identical(r$response$code, 0)) {
    cat(paste("**", "Response code:", r$response$code, "\n"))
    cat(paste("**", r$response$msg, "\n"))
    cat("Trying to continue..\n")
 }
  isdef <- try({
   rbas <- r$sol$bas;
   rbas$solsta; rbas$prosta; rbas$xx;
 }, silent=TRUE)
 if (inherits(isdef, "try-error")) {
   stop("Basic solution was incomplete!")
  switch(rbas$solsta,
   OPTIMAL = {
      cat("The solution was optimal, I am happy!\n")
   NEAR\_OPTIMAL = {
      cat("The solution was close to optimal, very good..\n")
   },
    #OTHERWISE:
    {
      cat(paste("**", "Solution status:", rbas$solsta, "\n"))
      cat(paste("**", "Problem status:", rbas$prosta, "\n"))
      stop("Solution could not be accepted!")
 )
  return(rbas$xx)
```

Notice how the R value Inf is used in both the constraint bounds (blc and buc) and the variable upper bound (bux), to avoid the specification of an actual bound.

From this example the input arguments for the linear program follows easily.

- Objective The string is the objective goal and could be either minimize, min, maximize or max. The dense numeric vector specifies the coefficients in front of the variables in the linear objective function, and the optional constant scalar (reads: c zero) is a constant in the objective corresponding to c^f in problem, that will be assumed zero if not specified.
- Constraint Matrix The sparse matrix is the constraint matrix of the problem with the constraint coefficients written row-wise. Notice that for larger problems it may be more convenient to define an empty sparse matrix and specify the non-zero elements one at a time $A(i,j) = a_{ij}$, rather than writing out the full matrix as done in the lo1 example. E.g. Matrix(0,nrow=30,ncol=50,sparse=TRUE).
- Bounds The constraint bounds with rows blc (constraint lower bound) and buc (constraint upper

bound), as well as the variable bounds with rows blx (variable lower bound) and bux (variable upper bound), are both given as dense numeric matrices. These are equivalent to the bounds of problem, namely l^c , u^c , l^x and u^x .

4.3 Conic Quadratic Optimization

Conic optimization is a generalization of linear optimization, allowing constraints of the type

$$x^t \in \mathcal{K}_t$$

where x^t is a subset of the problem variables and \mathcal{K}_t is a convex cone. Actually, since the set \mathbb{R}^n of real numbers is also a convex cone, all variables can in fact be partitioned into subsets belonging to separate convex cones, simply stated $x \in \mathcal{K}$.

MOSEK can solve conic quadratic optimization problems of the form

where the domain restriction, $x \in \mathcal{K}$, implies that all variables are partitioned into convex cones

$$x = (x^0, x^1, \dots, x^{p-1}), \text{ with } x^t \in \mathcal{K}_t \subseteq \mathbb{R}^{n_t}.$$

For convenience, the user only specify subsets of variables x^t belonging to cones \mathcal{K}_t different from the set \mathbb{R}^{n_t} of real numbers. These cones can be a:

• Quadratic cone:

$$Q^{n} = \left\{ x \in \mathbb{R}^{n} : x_{0} \ge \sqrt{\sum_{j=1}^{n-1} x_{j}^{2}} \right\}.$$

• Rotated quadratic cone:

$$Q_r^n = \left\{ x \in \mathbb{R}^n : 2x_0 x_1 \ge \sum_{j=2}^{n-1} x_j^2, \quad x_0 \ge 0, \quad x_1 \ge 0 \right\}.$$

From these definition it follows that

$$(x_4, x_0, x_2) \in \mathcal{Q}^3$$
,

is equivalent to

$$x_4 \ge \sqrt{x_0^2 + x_2^2}.$$

Furthermore, each variable may belong to one cone at most. The constraint $x_i - x_j = 0$ would however allow x_i and x_j to belong to different cones with same effect.

4.3.1 Example CQO1

We want to solve the following Conic Optimization Problem problem:

minimize
$$x_4 + x_5 + x_6$$

subject to $x_1 + x_2 + 2x_3 = 1$,
 $x_1, x_2, x_3 \geq 0$,
 $x_4 \geq \sqrt{x_1^2 + x_2^2}$,
 $2x_5x_6 \geq x_3^2$ (4.2)

is an example of a conic quadratic optimization problem. The problem involves some linear constraints, a quadratic cone and a rotated quadratic cone.

The first cone is of the quadratic cone type (MSK_CT_QUAD) , while the second is of the rotated quadratic cone type (MSK_CT_RQUAD) . The subindexes of the variables used to define these cones follow naturally as seen in the Listing 4.3.

Listing 4.3: R implementation of model (4.2)

From this example the input arguments for a conic program follow easily. The objective function, the linear constraints and variable bounds should all be specified as for linear programs, and the only addition to this is the quadratic cones specified in the list-typed matrix.

The cones matrix has a column for each cone, and a row for each descriptive element. The first row called , should specify the cone type in a string, being either quadratic QUAD or rotated quadratic RQUAD. Notice that the \mathbf{MOSEK} library cone type prefix $\mathtt{MSK_CT_}$ is optional. The second row called , should specify the subset of variables belonging to the cone in a numeric vector - and the ordering does matter! The i'th element of sub will be the index of the variable referred by x_i , in the cone definitions and . As an example, the rotated quadratic cone with subindexes $\mathtt{c(4,6,2,3)}$ would define the cone

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^4 : 2x_4x_6 \ge x_2^2 + x_3^2, \ x_4 \ge 0, \ x_6 \ge 0 \right\}.$$

Listing 4.4 showed a simple way to specify cones given an explicit representation. In many practical cases, however, cones are more conveniently specified in chunks or within a loop. For this purpose, preallocation should always be preferred as shown here.

Listing 4.4: R implementation of model (4.2) preallocating cones.

```
NUMCONES <- 2
cqo1$cones <- matrix(list(), nrow=2, ncol=NUMCONES)
  rownames(cqo1$cones) <- c("type", "sub")
cqo1$cones[,1] <- list("QUAD", c(5,1,3))
cqo1$cones[,2] <- list("QUAD", c(6,2,4))</pre>
```

4.4 Semidefinite Optimization

Semidefinite optimization is a generalization of conic quadratic optimization, allowing the use of matrix variables belonging to the convex cone of positive semidefinite matrices

$$S_+^r = \left\{ X \in S^r : z^T X z \ge 0, \quad \forall z \in \mathbb{R}^r \right\},$$

where S^r is the set of $r \times r$ real-valued symmetric matrices.

MOSEK can solve semidefinite optimization problems of the form

$$\begin{array}{lll} \text{minimize} & \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \left\langle \overline{C}_j, \overline{X}_j \right\rangle + c^f \\ \text{subject to} & l_i^c & \leq & \sum_{j=0}^{n-1} a_{ij} x_j + \sum_{j=0}^{p-1} \left\langle \overline{A}_{ij}, \overline{X}_j \right\rangle & \leq & u_i^c, & i = 0, \dots, m-1, \\ & l_j^x & \leq & \underbrace{x_j} & \leq & u_j^x, & j = 0, \dots, n-1, \\ & x \in \mathcal{K}, \overline{X}_j \in \mathcal{S}_+^{r_j}, & j = 0, \dots, p-1 \end{array}$$

where the problem has p symmetric positive semidefinite variables $\overline{X}_j \in \mathcal{S}_+^{r_j}$ of dimension r_j with symmetric coefficient matrices $\overline{C}_j \in \mathcal{S}^{r_j}$ and $\overline{A}_{i,j} \in \mathcal{S}^{r_j}$. We use standard notation for the matrix inner product, i.e., for $A, B \in \mathbb{R}^{m \times n}$ we have

$$\langle A, B \rangle := \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} A_{ij} B_{ij}.$$

4.4.1 Example SDO1

The problem

is a mixed semidefinite and conic quadratic programming problem with a 3-dimensional semidefinite variable

$$\overline{X} = \begin{bmatrix} \overline{X}_{00} & \overline{X}_{10} & \overline{X}_{20} \\ \overline{X}_{10} & \overline{X}_{11} & \overline{X}_{21} \\ \overline{X}_{20} & \overline{X}_{21} & \overline{X}_{22} \end{bmatrix} \in \mathcal{S}_{+}^{3},$$

and a conic quadratic variable $(x_0, x_1, x_2) \in \mathcal{Q}^3$. The objective is to minimize

$$2(\overline{X}_{00} + \overline{X}_{10} + \overline{X}_{11} + \overline{X}_{21} + \overline{X}_{22}) + x_0,$$

subject to the two linear constraints

$$\overline{X}_{00} + \overline{X}_{11} + \overline{X}_{22} + x_0 = 1,$$

and

$$\overline{X}_{00} + \overline{X}_{11} + \overline{X}_{22} + 2(\overline{X}_{10} + \overline{X}_{20} + \overline{X}_{21}) + x_1 + x_2 = 1/2.$$

and can be modeled in R as shown in Listing 4.5.

Listing 4.5: R implementation of model (4.3).

```
# One semidefinite matrix variable size 3x3:
sdo1$bardim <- c(N)</pre>
# Block triplet format specifying the lower triangular part
# of the symmetric coefficient matrix 'barc':
sdo1$barc$j <- c(1, 1, 1, 1, 1)
sdo1$barc$k <- c(1, 2, 3, 2, 3)
sdo1$barc$1 <- c(1, 2, 3, 1, 2)
sdo1$barc$v <- c(2, 2, 2, 1, 1)
# Block triplet format specifying the lower triangular part
# of the symmetric coefficient matrix 'barA':
sdo1$barA$i <- c(1, 1, 1, 2, 2, 2, 2, 2, 2)
sdo1$barA$j <- c(1, 1, 1, 1, 1, 1, 1, 1)
sdo1$barA$k <- c(1, 2, 3, 1, 2, 3, 2, 3, 3)
sdo1$barA$v <- c(1, 1, 1, 1, 1, 1, 1, 1)
r <- mosek(sdo1)
barx <-1.0 * bandSparse(N, k=0:(1-N), symm=TRUE)
barx@x <- r$sol$itr$barx[[1]]</pre>
```

4.5 Quadratic Optimization

MOSEK can solve quadratic and quadratically constrained convex problems. This class of problems can be formulated as follows:

minimize
$$\frac{\frac{1}{2}x^{T}Q^{o}x + c^{T}x + c^{f}}{\text{subject to}}$$
 subject to
$$l_{k}^{c} \leq \frac{\frac{1}{2}x^{T}Q^{k}x + \sum_{j=0}^{n-1}a_{k,j}x_{j}}{l_{j}^{x}} \leq u_{k}^{c}, \quad k = 0, \dots, m-1,$$

$$l_{j}^{x} \leq x_{j} \leq u_{j}^{x}, \quad j = 0, \dots, n-1.$$
 (4.4)

Without loss of generality it is assumed that Q^o and Q^k are all symmetric because

$$x^T Q x = \frac{1}{2} x^T (Q + Q^T) x.$$

This implies that a non-symmetric Q can be replaced by the symmetric matrix $\frac{1}{2}(Q+Q^T)$.

The problem is required to be convex. More precisely, the matrix Q^o must be positive semi-definite and the kth constraint must be of the form

$$l_k^c \le \frac{1}{2} x^T Q^k x + \sum_{j=0}^{n-1} a_{k,j} x_j \tag{4.5}$$

with a negative semi-definite Q^k or of the form

$$\frac{1}{2}x^T Q^k x + \sum_{j=0}^{n-1} a_{k,j} x_j \le u_k^c.$$

with a positive semi-definite Q^k . This implies that quadratic equalities are *not* allowed. Specifying a non-convex problem will result in an error when the optimizer is called.

A matrix is positive semidefinite if the smallest eigenvalue of the matrix is nonnegative. An alternative statement of the positive semidefinite requirement is

$$x^T Q x > 0, \quad \forall x.$$

If Q is not positive semidefinite, then **MOSEK** will not produce reliable results or work at all.

One way of checking whether Q is positive semidefinite is to check whether all the eigenvalues of Q are nonnegative.

4.5.1 Example: Quadratic Objective

minimize
$$x_1^2 + 0.1x_2^2 + x_3^2 - x_1x_3 - x_2$$
 subject to $1 \le x_1 + x_2 + x_3$
$$x > 0.$$
 (4.6)

For the example (4.6) implies that

$$Q = \left[\begin{array}{ccc} 2 & 0 & -1 \\ 0 & 0.2 & 0 \\ -1 & 0 & 2 \end{array} \right], c = \left[\begin{array}{c} 0 \\ -1 \\ 0 \end{array} \right], A = \left[\begin{array}{ccc} 1 & 1 & 1 \end{array} \right],$$

and that

$$l^c = 1, u^c = \infty, l^x = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$
 and $u^x = \begin{bmatrix} \infty \\ \infty \\ \infty \end{bmatrix}$

Please note the explicit $\frac{1}{2}$ in the objective function of (4.4) which implies that diagonal elements must be doubled in Q, i.e. $Q_{11} = 2$, whereas the coefficient in (4.6) is 1 in front of x_1^2 .

Important: MOSEK assumes that the Q matrix is symmetric, i.e. $Q = Q^T$, and that Q is positive semidefinite.

Please note that there are quadratic terms in both constraints. This problem can be solved using mosek as reported in Listing 4.6.

Listing 4.6: Script implementing problem (4.6)

4.6 Integer Optimization

An optimization problem where one or more of the variables are constrained to integer values is denoted an integer optimization problem.

Section 4.6.2 shows how to input an initial feasible solution to help the solver.

4.6.1 Example MILO1

In this section the example

$$\begin{array}{llll} \text{maximize} & x_0 + 0.64x_1 \\ \text{subject to} & 50x_0 + 31x_1 & \leq & 250, \\ & & 3x_0 - 2x_1 & \geq & -4, \\ & & x_0, x_1 \geq 0 & \text{and integer} \end{array} \tag{4.7}$$

is used to demonstrate how to solve a problem with integer variables.

The example (4.7) is almost identical to a linear optimization problem (see 4.2) except for some variables being integer constrained. Therefore, only the specification of the integer constraints requires something new compared to the linear optimization problem discussed previously.

This is easily programmed in R using the piece code shown in Listing 4.7,

Listing 4.7: R implementation of problem (4.7).

where x_1 and x_2 are pointed out as integer variables.

The input arguments follow those of a linear or conic program with the additional identification of the integer variables. The column vector **intsub** should simply contain indexes to the subset of variables for which integrality is required. For instance if x should be a binary $\{0,1\}$ -variable, its index in the problem formulation should be added to **intsub**, and its bounds $0 \le x \le 1$ should be specified explicitly.

If executed correctly you should be able to see the log of the interface and optimization process printed to the screen. The output structure will only include an integer solution <code>int</code>, since we are no longer in the continuous domain for which the interior-point algorithm operates. The structure also contains the problem status as well as the solution status based on certificates found by the **MOSEK** optimization library.

Solving a mixed-integer optimization program could easily result in long running time. It is therefore of interest to consider a termination criterion based on the maximum running time. This is possible setting the MSK_DPAR_MIO_MAX_TIME. See Section 4.8 for more details on how to set solver parameters.

4.6.2 Specifying an initial solution

Integer optimization problems are generally hard to solve, but the solution time can often be reduced by providing an initial solution for the solver. It is not necessary to specify the whole solution. By setting the MSK_IPAR_MIO_CONSTRUCT_SOL parameter to MSK_ON and inputting values for the integer variables only, will force **MOSEK** to compute the remaining continuous variable values.

If the specified integer solution is infeasible or incomplete, MOSEK will simply ignore it.

Consider the problem

maximize
$$7x_0 + 10x_1 + x_2 + 5x_3$$
 subject to
$$x_0 + x_1 + x_2 + x_3 \le 2.5$$

$$x_0, x_1, x_2 \in \mathbb{Z}$$

$$x_0, x_1, x_2, x_3 \ge 0$$

$$(4.8)$$

The following example demonstrates how to optimize the problem using a feasible starting solution generated by selecting the integer values as $x_0 = 0, x_1 = 2, x_2 = 0$.

4.7 Solution Analysis

The main purpose of **MOSEK** is to solve optimization problems and therefore the most fundamental question to be asked is whether the solution reported by **MOSEK** is a solution to the desired optimization problem.

There can be several reasons why it might be not case. The most prominent reasons are:

- A wrong problem. The problem inputted to **MOSEK** is simply not the right problem, i.e. some of the data may have been corrupted or the model has been incorrectly built.
- Numerical issues. The problem is badly scaled or otherwise badly posed.
- Other reasons. E.g. not enough memory or an explicit user request to stop.

The first step in verifying that **MOSEK** reports the expected solution is to inspect the solution summary generated by **MOSEK** (see Section 4.7.1). The solution summary provides information about

- the problem and solution statuses,
- objective value and infeasibility measures for the primal solution, and
- objective value and infeasibility measures for the dual solution, where applicable.

If the summary reports conflicting information (e.g. a solution status that does not match the actual solution), or the cause for terminating the solver before a solution was found cannot be traced back to the reasons stated above, it may be caused by a bug in the solver; in this case, please contact **MOSEK** support (see Section 1.2).

If it has been verified that **MOSEK** solves the problem correctly but the solution is still not as expected, next step is to verify that the primal solution satisfies all the constraints. Hence, using the original problem it must be determined whether the solution satisfies all the required constraints in the model. For instance assume that the problem has the constraints

$$x_1 + 2x_2 + x_3 \le 1,$$

 $x_1, x_2, x_3 \ge 0$

and MOSEK reports the optimal solution

$$x_1 = x_2 = x_3 = 1.$$

Then clearly the solution violates the constraints. The most likely explanation is that the model does not match the problem entered into **MOSEK**, for instance

$$x_1 - 2x_2 + x_3 \le 1$$

may have been inputted instead of

$$x_1 + 2x_2 + x_3 \le 1$$
.

A good way to debug such an issue is to dump the problem to *OPF file* and check whether the violated constraint has been specified correctly.

Verifying that a feasible solution is optimal can be harder. However, for continuous problems, i.e. problems without any integer constraints, optimality can verified using a dual solution. Normally, **MOSEK** will report a dual solution; if that is feasible and has the same objective value as the primal solution, then the primal solution must be optimal.

An alternative method is to find another primal solution that has better objective value than the one reported to MOSEK. If that is possible then either the problem is badly posed or there is bug in MOSEK.

4.7.1 The Solution Summary

Due to **MOSEK** employs finite precision floating point numbers then reported solution is an approximate optimal solution. Therefore after solving an optimization problem it is relevant to investigate how good an approximation the solution is. For a convex optimization problem that is an easy task because the optimality conditions are:

- The primal solution must satisfy all the primal constraints.
- The dual solution much satisfy all the dual constraints.
- The primal and dual objective values must be identical.

Therefore, the **MOSEK** solution summary displays that information that makes it possible to verify the optimality conditions. Indeed the solution summary reports how much primal and dual solutions violate the primal and constraints respectively. In addition the objective values assoctated with each solution repoted.

In case of a linear optimization problem the solution summary may look like

```
Basic solution summary
Problem status : PRIMAL_AND_DUAL_FEASIBLE
Solution status : OPTIMAL
Primal. obj: -4.6475314286e+002 nrm: 5e+002 Viol. con: 1e-014 var: 1e-014
Dual. obj: -4.6475314543e+002 nrm: 1e+001 Viol. con: 4e-009 var: 4e-016
```

The interpretaion of the solution summary is as follows:

- Information for the basic solution is reported.
- The problem status is primal and dual feasible which means the problem has an optimal solution.
- The solution status is optimal.
- Next information about the primal solution is reported. The information consists of the objective value, the infinity norm of the primal solution and violation measures. The violation for the constraints (con:) is the maximal violation in any of the constraints. Whereas the violations for the variables (var:) is the maximal bound violation for any of the variables. In this case the primal violations for the constraints and variables are small meaning the solution is an almost feasible solution. Observe due to the rounding errors it can be expected that the violations are proportional to the size (nrm:) of the solution.
- Similarly for the dual solution the violations are small and hence the dual solution is almost feasible.
- Finally, it can be seen that the primal and dual objective values are almost identical.

To summarize in this case a primal and a dual solution only violate the primal and dual constraints slightly. Moreover, the primal and dual objective values are almost identical and hence it can be concluded that the reported solution is a good approximation to the optimal solution.

The reason the size (=norms) of the solution are shown is that it shows some about conditioning of the problem because if the primal and/or dual solution has very large norm then the violations and objective values are sensitive to small pertubations in the problem data. Therefore, the problem is unstable and care should be taken before using the solution.

Now what happens if the problem does not have an optimal solution e.g. is primal infeasible. In such a case the solution summary may look like

```
Interior-point solution summary
Problem status : PRIMAL_INFEASIBLE
Solution status : PRIMAL_INFEASIBLE_CER
Dual. obj: 6.7319732555e+000 nrm: 8e+000 Viol. con: 3e-010 var: 2e-009
```

i.e. MOSEK reports that the solution is a certificate of primal infeasibility but a certificate of primal infeasibility what does that mean? It means that the dual solution is a Farkas type certificate. Recall

Farkas' Lemma says

$$\begin{array}{rcl} Ax & = & b, \\ x & \geq & 0 \end{array}$$

if and only if a y exists such that

$$\begin{array}{lcl}
A^T y & \leq & 0, \\
b^T y & > & 0.
\end{array}
\tag{4.9}$$

Observe the infeasibility certificate has the same form as a regular dual solution and therefore the certificate is stored as a dual solution. In order to check quality of the primal infeasibility certificate it should be checked whether satisfies (4.9). Hence, the dual objective value is b^Ty should be strictly positive and the maximal violation in $A^Ty \leq 0$ should be a small. In this case we conclude the certificate is of high quality because the dual objective is postive and large compared to the violations. Note the Farkas certificate is a ray so any postive multiple of that ray is also certificate. This implies the absolute of the value objective value and the violation is not relevant.

In the case a problem is dual infeasible then the solution summary may look like

```
Basic solution summary
Problem status : DUAL_INFEASIBLE
Solution status : DUAL_INFEASIBLE_CER
Primal. obj: -2.00000000000e-002 nrm: 1e+000 Viol. con: 0e+000 var: 0e+000
```

Observe when a solution is a certificate of dual infeasibility then the primal solution contains the certificate. Moreoever, given the problem is a minimization problem the objective value should be negative and large compared to the worst violation if the certificate is strong.

Listing 4.8 shows how to use these function to determine the quality of the solution.

Listing 4.8: An example of solution quality analysis.

```
lo1 <- list(sense="max", c=c(3,1,5,1))
lo1$A <- Matrix(c(3,1,2,0,2,1,3,1,0,2,0,3),</pre>
             nrow=3, byrow=TRUE, sparse=TRUE)
lo1$bc <- rbind(blc=c(30,15,-Inf), buc=c(30,Inf,25));</pre>
lo1$bx <- rbind(blx=c(0,0,0,0)),
                                    bux=c(Inf,10,Inf,Inf));
## Note we need to obtain details of the solution to inspect primal/dual obj fun value
r <- try(mosek(lo1, list(verbose=0, soldetail=2)), silent=TRUE)
if (inherits(r, "try-error")) {
  stop("Rmosek failed somehow!")
}
if (!identical(r$response$code, 0)) {
 cat(paste("**", "Response code:", r$response$code, "\n"))
  cat(paste("**", r$response$msg, "\n"))
  cat("Trying to continue..\n")
}
isdef <- try({</pre>
 itr <- r$sol$itr;</pre>
  itr$solsta; itr$prosta; itr$xx; itr$sol;
 }, silent=TRUE)
if (inherits(isdef, "try-error")) {
    stop("Interior solution was incomplete!")
}
if (itr$solsta == "OPTIMAL" |
    itr$solsta == "NEAR_OPTIMAL" ) {
```

```
cat("The solution was (near) optimal, I am happy!\n")
 pobj<- r$sol$itr$pobjval</pre>
 dobj<- r$sol$itr$dobjval
                <- abs(dobj-pobj)
  abs_obj_gap
               <- abs_obj_gap/(1.0 + min(abs(pobj),abs(dobj)))
 rel_obj_gap
 max_primal_viol <- max( itr$maxinfeas$pcon, itr$maxinfeas$pbound)</pre>
 max_primal_viol <- max( max_primal_viol , itr$maxinfeas$pbarvar)</pre>
 max_primal_viol <- max( max_primal_viol , itr$maxinfeas$pcone)</pre>
 max_dual_viol <- max( itr$maxinfeas$dcon, itr$maxinfeas$dbound)</pre>
 max_dual_viol <- max( max_dual_viol , itr$maxinfeas$dbarvar)</pre>
 max_dual_viol <- max( max_dual_viol , itr$maxinfeas$dcone)</pre>
  ## Assume the application needs the solution to be within
  ## 1e-6 of optimality in an absolute sense. Another approach
  ## would be looking at the relative objective gap
  cat("\n\n")
  cat("Customized solution information.\n")
  cat(" Absolute objective gap: ",abs_obj_gap,"\n")
  cat(" Relative objective gap: ",rel_obj_gap,"\n")
 cat(" Max primal violation : ",max_primal_viol,"\n")
 cat(" Max dual violation : ",max_dual_viol,"\n")
 accepted <- TRUE
 if (rel_obj_gap>1e-6){
   print ("Warning: The relative objective gap is LARGE.")
   accepted <- FALSE
  ## We will accept a primal infeasibility of 1e-8 and
  ## dual infeasibility of 1e-6. These number should chosen problem
  ## dependent.
 if ( max_primal_viol>1e-8) {
   print ("Warning: Primal violation is too LARGE")
   accepted <- FALSE
 if ( max_dual_viol>1e-6 ) {
   print ("Warning: Dual violation is too LARGE.")
   accepted <- FALSE
 }
 if ( accepted ) {
   numvar <- task.getnumvar()</pre>
   print ("Optimal primal solution")
   print(rbas$xx)
 }
} else {
   #Print detailed information about the solution
   cat(paste("**", "Solution status:", rbas$solsta, "\n"))
    cat(paste("**", "Problem status:", rbas$prosta, "\n"))
   stop("Solution could not be accepted!")
```

4.7.2 The Solution Summary for Mixed-Integer Problems

The solution summary for a mixed-integer problem may look like

Listing 4.9: Example of solution summary for a mixed-integer problem.

```
Integer solution solution summary
Problem status : PRIMAL_FEASIBLE
Solution status : INTEGER_OPTIMAL
Primal. obj: 3.4016000000e+005 nrm: 1e+000 Viol. con: 0e+000 var: 0e+000 itg: 3e-014
```

The main diffrence compared to the continous case covered previously is that no information about the dual solution is provided. Simply because there is no dual solution available for a mixed integer problem. In this case it can be seen that the solution is highly feasible because the violations are small. Moreoever, the solution is denoted integer optimal. Observe *itg:* 3e-014 implies that all the integer constrained variables are at most 3e – 014 from being an exact integer.

4.8 Solver Parameters

The **MOSEK** API provides many parameters to tune and customize the solver behaviour. Parameters are grouped depending on their type: integer, double or string. In general, it should not be necessary to change any of the parameters but if required, it is easily done. A complete list of all parameters is found in Section 10.2.

We will show how to access and set the integer parameter that define the logging verbosity of the solver, i.e. MSK_IPAR_LOG , and the algorithm used by MOSEK, i.e. $MSK_IPAR_OPTIMIZER$.

Note: The very same concepts and procedures apply to string and double valued parameters.

We need to set to 0 the parameter MSK_IPAR_LOG. Notice that in Rmosek the MSK_IPAR_, MSK_DPAR_ and MSK_SPAR_ prefixes for parameter names have been removed in favor of the iparam, dparam and sparam structures. Parameters are case-insensitive.

Assuming a problem named lo1 has been defined, we can suppress solver verbosity as follow

```
lo1$iparam <- list(LOG = 0);</pre>
```

For more information about other parameter related functions, please browse the API reference in Section 10.

Setting a parameter to NULL will remove it from the list according to the R language definition. Setting a parameter to NA or NaN, will on the other hand keep it on the list, only to be ignored by the interface with warnings confirming that this took place. Errors will be generated when a parameter name is not recognized or when the value defined for it is not within its feasible range.

NONLINEAR TUTORIALS

This chapter provides information about how to solve general convex nonlinear optimization problems using MOSEK. By general nonlinear problems it is meant problems that cannot be formulated as a conic quadratic optimization or a convex quadratically constrained optimization problem.

In general it is recommended not to use nonlinear optimizer unless needed. The reasons are

- MOSEK has no way of checking whether the formulated problem is convex and if this assumption is not satisfied the optimizer will not work.
- The nonlinear optimizer requires 1st and 2nd order derivative information which is hard to provide correctly i.e. it is nontrivial to program the code that computes the derivative information.
- The algorithm employed for nonlinear optimization problems is not as good as the one employed for conic problems i.e. conic problems has special that can be exploited to make the optimizer faster and more robust.

This leads to following advices in decreasing order of importance.

- 1. Consider reformulating the problem to a conic quadratic optimization problem if at all possible. In particular many problems involving polynomial terms can easily be reformulated to conic quadratic form.
- 2. Consider reformulating the problem to a separable optimization problem because that simplifies the issue with verifying convexity and computing 1st and 2nd order derivatives significantly. In most cases problems on separable form also solves faster because of the simpler structure of the functions.
- 3. Finally, if the problem cannot be reformulated to separable form then use a modelling language like AMPL or GAMS. The reason is the modeling language will do all the computing of function values and derivatives. This eliminates an important source of errors. Therefore, it is strongly recommended to use a modelling language at the prototype stage.

5.1 Separable Convex (SCopt) Interface

The **MOSEK** rmosek API provides a way to add simple non-linear functions composed from a limited set of non-linear terms. Non-linear terms can be mixed with quadratic terms in objective and constraints.

We consider a normal linear problem with additional non-linear terms z:

minimize
$$z_0(x) + c^T x$$
 subject to
$$l_i^c \leq z_i(x) + a_i^T x \leq u_i^c, \ i = 1 \dots m$$

$$x \in \mathbb{R}^n \quad z : \mathbb{R}^n \to \mathbb{R}^{(m+1)}$$

Using the separable non-linear interface it is possible to add non-linear functions of the form

$$z_i(x) = \sum_{k=1}^{K_i} w_k^i(x_{p_{ik}}), \ w_k^i : \mathbb{R} \to \mathbb{R}$$

In other words, each non-linear function z_i is a sum of separable functions w_k^i of one variable each. A limited set of functions are supported; each w_k^i can be one of the separable functions:

Table 5.1: Functions supported by the SCopt interface.

Separable function	Operator name	
$fx\ln(x)$	ent	Entropy function
$\int e^{gx+h}$	exp	Exponential function
$f \ln(gx + h)$	log	Logarithm
$f(x+h)^g$	pow	Power function

where f, g and h are constants.

This formulation does not guarantee convexity. For **MOSEK** to be able to solve the problem, following requirements must be met:

- If the objective is minimized, the sum of non-linear terms must be convex, otherwise it must be concave
- Any constraint bounded below must be concave, and any constraint bounded above must be convex.
- Each separable term must be twice differentiable within the bounds of the variable it is applied to.

If these are not satisfied **MOSEK** may not be able to solve the problem or produce a meaningful status report. For details see Section 5.1.1.

Important: When to use the SCopt API:

- When conic can absolutely not be used.
- when a conic formulation would be significantly larger

Problems: less stable, less predictable, harder to debug, worse status info

5.1.1 Ensuring Convexity and Differentiability

Some simple rules can be set up to ensure that the problem satisfies \mathbf{MOSEK} 's convexity and differentiability requirements. First of all, for any variable x_i used in a separable term, the variable bounds must define a range within which the function is twice differentiable.

We can define these bounds as follows:

Separable function	Operator name	Safe x bounds
$fx\ln(x)$	ent	0 < x.
fe^{gx+h}	exp	$-\infty < x < \infty$.
$f \ln(gx + h)$	log	If $g > 0$: $-h/g < x$.
$\int m(gx + n)$	109	If $g < 0$: $x < -h/g$.
		If $g > 0$ and integer: $-\infty < x < \infty$.
$f(x+h)^g$	pow	If $g < 0$ and integer: either $-h < x$ or $x < -h$.
		Otherwise: $-h < x$.

To ensure convexity, we require that each $z_i(x)$ is either a sum of convex terms or a sum of concave terms. The following table lists convexity for the relevant ranges for f > 0 — changing the sign of f switches concavity/convexity.

Separable function	Operator name	Convexity conditions
$fx \ln(x)$	ent	Convex within safe bounds.
fe^{gx+h}	exp	Convex for all x .
$f \ln(gx+h)$	log	Concave within safe bounds.
		If g is even integer: convex within
$f(x+h)^g$	pow	safe bounds.
		If g is odd integer:
		• concave if $(-\infty, -h)$,
		• convex if $(-h, \infty)$
		If $0 < g < 1$: concave within safe
		bounds.
		Otherwise: convex within safe
		bounds.

5.1.2 SCopt Example

Subsequently, we will use the following example to demonstrate the solution of a separable convex optimization problem using \mathbf{MOSEK}

maximize
$$\exp(x_2) - \ln(x_1)$$

subject to $x_2 \ln(x_2) \ge 0$
 $x_1^{\sqrt{2}} - x_2 \le 0$
 $x_1, x_2 \ge \frac{1}{2}$. (5.1)

This problem is obviously separable. Moreover, note that all nonlinear functions are well defined for x values satisfying the variable bounds strictly, i.e.

$$x_1, x_2 > 0.$$

This assures that function evaluation errors will not occur during the optimization process because **MOSEK** will only evaluate $\ln(x_1)$ and $x_2 \ln(x_2)$ for $x_1, x_2 > 0$.

The method employed above can often be used to make convex optimization problems separable even if these are not formulated as such initially. The reader might object that this approach is inefficient because additional constraints and variables are introduced to make the problem separable. However, in our experience this drawback is offset largely by the much simpler structure of the nonlinear functions. Particularly, the evaluation of the nonlinear functions, their gradients and Hessians is much easier in the separable case.

From this example the input arguments for a separable convex program follow easily. The linear part of the objective function and constraints, as well as the constraint and variable bounds, should all be specified as for linear programs (see Section 4.2.). The only addition to this is the list called *opro* containing the list-typed operator matrices (for objective) and (for constraints).

```
## type j f g h
opro[,1] <- list("LOG", 1, -1.0, 1.0, 0.0)
opro[,2] <- list("EXP", 2, 1.0, 1.0, 0.0)
```

The operator matrices have a column for each operator and a row for each descriptive element. The opromatrix have five rows called $\{type, j, f, g, h\}$, while the oprc matrix have six rows called $\{type, i, j, f, g, h\}$. Row should specify the operator type in a string, being either, exponential EXP, logarithm LOG or power POW. Row (not in opro) should specify the index of the constraint to which the non-linear term should be added. Row should specify the variable index of the operator. Rows , and should specify the coefficients of the operator.

```
## type i j f g h
oprc[,1] <- list("ENT", 1, 2, 1.0, 0.0, 0.0)
oprc[,2] <- list("POW", 2, 1, 1.0, 0.5, 0.0)
```

Note that the definition of the entropy operator, was the only operator defined without g and h. Thus, for entropy operators, these two unused rows in the operator matrix can be set to either zero or any empty definition (NULL, NA or NaN).

The complete source code follows in Listing 5.1.

Listing 5.1: Implementation of problem (5.1).

```
sco1 <- list(sense = "min")</pre>
sco1$c <- c(0,0)
sco1$A <- Matrix( c(0, 0,</pre>
                    0,-1), nrow=2, byrow=TRUE, sparse=TRUE)
sco1$bc <- rbind(blc = c(-Inf , 0.),
                 buc = c(0., Inf)
sco1$bx <- rbind(blx = rep(0.5, 2),
                 bux = rep(1.0, 2))
NUMOPRO <- 2; NUMOPRC <- 2;
opro <- matrix(list(), nrow=5, ncol=NUMOPRO)</pre>
oprc <- matrix(list(), nrow=6, ncol=NUMOPRC)</pre>
rownames(opro) <- c("type","j","f","g","h")
rownames(oprc) <- c("type","i","j","f","g","h")
                   type j
                              f
                                   9
opro[,1] <- list("LOG", 1, -1.0, 1.0, 0.0)
opro[,2] <- list("EXP", 2,
                             1.0, 1.0, 0.0)
                   type i
                             2, 1.0, 0.0, 0.0)
oprc[,1] <- list("ENT", 1,
oprc[,2] <- list("POW", 2,</pre>
                              1, 1.0, 0.5, 0.0)
sco1$scopt <- list(opro=opro, oprc=oprc)</pre>
r <- mosek(sco1)
```

MANAGING I/O

The main purpose of this chapter is to give an overview on the logging and I/O features provided by the **MOSEK** package.

- Section 6.1 contains information about the log streams provided by MOSEK.
- File I/O is discussed in Section 6.2.
- How to tune the logging verbosity is the topic of Section 6.3.

6.1 Stream I/O

MOSEK execution produces a certain amount of loggging at environment and task level. This means that the logging from each environement and task can be isolated from the others.

The log messages are partitioned in three streams:

- messages
- warnings
- errors

These streams are aggregated in the log stream. See MSKstreamtypee.

6.2 File I/O

MOSEK supports a range of problem and solution formats listed in Section 11. One such format is **MOSEK**'s native binary *Task format* which supports all features that **MOSEK** supports.

The file format used in I/O operations is deduced from extension - as in problemname.task - unless the parameter $MSK_IPAR_WRITE_DATA_FORMAT$ is specified to something else. Problem files with an additional .gz extension - as in problemname.task.gz - are moreover assumed to use GZIP compression, and are automatically compressed, respectively decompressed, when written or read.

Example

If something is wrong with a problem or a solution, one option is to output the problem to the human-readable *OPF format* and inspect it by hand. For instance, one may use the <code>mosek_write</code> function to write the problem to a file immediately before optimizing it:

```
r <- mosek_write(lo1, "lo1.opf")
```

This will write the problem in 1o1 to the file 1o1.opf. Similarly, using mosek_read is possible to read a problem from file. For instance the following code line

```
r <- mosek_read("lo1.opf")
```

will import a problem stored in the file lo1.opf in an object called prob.

6.3 Verbosity

The logging verbosity can be controlled by setting the relevant parameters, as for instance

- MSK_IPAR_LOG,
- MSK_IPAR_LOG_INTPNT,
- MSK_IPAR_LOG_MIO,
- MSK_IPAR_LOG_CUT_SECOND_OPT,
- MSK_IPAR_LOG_SIM, and
- MSK_IPAR_LOG_SIM_MINOR.

Each parameter control the output level of a specific functionality or algorithm. The main switch is MSK_IPAR_LOG which affect the whole output. The actual log level for a specific functionality is determined as the minimum between MSK_IPAR_LOG and the relevant parameter. For instance, the log level for the output produce by the interior-point algorithm is tuned by the $MSK_IPAR_LOG_INTPNT$: the actual log level is defined by the minimum between MSK_IPAR_LOG and $MSK_IPAR_LOG_INTPNT$.

Tuning the solver verbosity may require adjusting several parameters. It must be noticed that verbose logging is supposed to be of interest during debugging and tuning, and it is consider the default setting. When output is no more of interest, user can easily disable using MSK_IPAR_LOG.

Moreover, it must be understood that larger values of MSK_IPAR_LOG do not necessarily result in an increased output.

By default MOSEK will reduce the amount of log information after the first optimization on a given task. To get full log output on subsequent optimizations set $MSK_IPAR_LOG_CUT_SECOND_OPT$ to zero.

PROBLEM FORMULATION AND SOLUTIONS

In this chapter we will discuss the following issues:

- The formal definitions of the problem types that MOSEK can solve.
- The solution information produced by MOSEK.
- The information produced by MOSEK if the problem is infeasible.

7.1 Linear Optimization

A linear optimization problem can be written as

where

- \bullet m is the number of constraints.
- \bullet *n* is the number of decision variables.
- $x \in \mathbb{R}^n$ is a vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear part of the objective function.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.

A primal solution (x) is (primal) feasible if it satisfies all constraints in (7.1). If (7.1) has at least one primal feasible solution, then (7.1) is said to be (primal) feasible.

In case (7.1) does not have a feasible solution, the problem is said to be (primal) infeasible

7.1.1 Duality for Linear Optimization

Corresponding to the primal problem (7.1), there is a dual problem

$$\begin{array}{lll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ & A^T y + s_l^x - s_u^x &= c, \\ \text{subject to} & -y + s_l^c - s_u^c &= 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x &\geq 0. \end{array} \tag{7.2}$$

If a bound in the primal problem is plus or minus infinity, the corresponding dual variable is fixed at 0, and we use the convention that the product of the bound value and the corresponding dual variable is 0. E.g.

$$l_i^x = -\infty \quad \Rightarrow \quad (s_l^x)_j = 0 \text{ and } l_i^x \cdot (s_l^x)_j = 0.$$

This is equivalent to removing variable $(s_l^x)_i$ from the dual problem. A solution

$$(y, s_{l}^{c}, s_{u}^{c}, s_{l}^{x}, s_{u}^{x})$$

to the dual problem is feasible if it satisfies all the constraints in (7.2). If (7.2) has at least one feasible solution, then (7.2) is (dual) feasible, otherwise the problem is (dual) infeasible.

A Primal-dual Feasible Solution

A solution

$$(x, y, s_l^c, s_u^c, s_l^x, s_u^x)$$

is denoted a primal-dual feasible solution, if (x) is a solution to the primal problem (7.1) and $(y, s_l^c, s_u^c, s_l^x, s_u^x)$ is a solution to the corresponding dual problem (7.2).

The Duality Gap

Let

$$(x^*, y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

be a primal-dual feasible solution, and let

$$(x^c)^* := Ax^*.$$

For a primal-dual feasible solution we define the duality gap as the difference between the primal and the dual objective value,

$$c^{T}x^{*} + c^{f} - \left\{ (l^{c})^{T}(s_{l}^{c})^{*} - (u^{c})^{T}(s_{u}^{c})^{*} + (l^{x})^{T}(s_{l}^{x})^{*} - (u^{x})^{T}(s_{u}^{x})^{*} + c^{f} \right\}$$

$$= \sum_{i=0}^{m-1} \left[(s_{l}^{c})_{i}^{*}((x_{i}^{c})^{*} - l_{i}^{c}) + (s_{u}^{c})_{i}^{*}(u_{i}^{c} - (x_{i}^{c})^{*}) \right]$$

$$+ \sum_{j=0}^{m-1} \left[(s_{l}^{x})_{j}^{*}(x_{j} - l_{j}^{x}) + (s_{u}^{x})_{j}^{*}(u_{j}^{x} - x_{j}^{*}) \right] \ge 0$$

$$(7.3)$$

where the first relation can be obtained by transposing and multiplying the dual constraints (7.2) by x^* and $(x^c)^*$ respectively, and the second relation comes from the fact that each term in each sum is nonnegative. It follows that the primal objective will always be greater than or equal to the dual objective.

An Optimal Solution

It is well-known that a linear optimization problem has an optimal solution if and only if there exist feasible primal and dual solutions so that the duality gap is zero, or, equivalently, that the *complementarity conditions*

$$\begin{array}{rclcrcl} (s_{u}^{c})_{i}^{*}((x_{i}^{c})^{*}-l_{i}^{c}) & = & 0, & i=0,\ldots,m-1, \\ (s_{u}^{c})_{i}^{*}(u_{i}^{c}-(x_{i}^{c})^{*}) & = & 0, & i=0,\ldots,m-1, \\ (s_{l}^{x})_{j}^{*}(x_{j}^{*}-l_{j}^{x}) & = & 0, & j=0,\ldots,n-1, \\ (s_{u}^{x})_{j}^{*}(u_{j}^{x}-x_{j}^{*}) & = & 0, & j=0,\ldots,n-1, \end{array}$$

are satisfied.

If (7.1) has an optimal solution and **MOSEK** solves the problem successfully, both the primal and dual solution are reported, including a status indicating the exact state of the solution.

7.1.2 Infeasibility for Linear Optimization

Primal Infeasible Problems

If the problem (7.1) is infeasible (has no feasible solution), **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the modified dual problem

maximize
$$(l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x$$

subject to
$$A^T y + s_l^x - s_u^x = 0,$$

$$-y + s_l^c - s_u^c = 0,$$

$$s_l^c, s_u^c, s_l^x, s_u^x \ge 0,$$
(7.4)

such that the objective value is strictly positive, i.e. a solution

$$(y^*, (s_l^c)^*, (s_u^c)^*, (s_l^x)^*, (s_u^x)^*)$$

to (7.4) so that

$$(l^c)^T(s_l^c)^* - (u^c)^T(s_u^c)^* + (l^x)^T(s_l^x)^* - (u^x)^T(s_u^x)^* > 0.$$

Such a solution implies that (7.4) is unbounded, and that its dual is infeasible. As the constraints to the dual of (7.4) are identical to the constraints of problem (7.1), we thus have that problem (7.1) is also infeasible.

Dual Infeasible Problems

If the problem (7.2) is infeasible (has no feasible solution), **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the modified primal problem

minimize
$$c^T x$$

subject to $\hat{l}^c \leq Ax \leq \hat{u}^c$, $\hat{l}^x \leq x \leq \hat{u}^x$, (7.5)

where

$$\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

and

$$\hat{l}_{j}^{x} = \left\{ \begin{array}{ll} 0 & \text{if } l_{j}^{x} > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_{j}^{x} := \left\{ \begin{array}{ll} 0 & \text{if } u_{j}^{x} < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

such that

$$c^T x < 0$$
.

Such a solution implies that (7.5) is unbounded, and that its dual is infeasible. As the constraints to the dual of (7.5) are identical to the constraints of problem (7.2), we thus have that problem (7.2) is also infeasible.

Primal and Dual Infeasible Case

In case that both the primal problem (7.1) and the dual problem (7.2) are infeasible, **MOSEK** will report only one of the two possible certificates — which one is not defined (**MOSEK** returns the first certificate found).

Minimalization vs. Maximalization

When the objective sense of problem (7.1) is maximization, i.e.

the objective sense of the dual problem changes to minimization, and the domain of all dual variables changes sign in comparison to (7.2). The dual problem thus takes the form

minimize
$$(l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f$$
 subject to
$$A^T y + s_l^x - s_u^x = c, \\ -y + s_l^c - s_u^c = 0, \\ s_l^c, s_u^c, s_l^x, s_u^x \leq 0.$$

This means that the duality gap, defined in (7.3) as the primal minus the dual objective value, becomes nonpositive. It follows that the dual objective will always be greater than or equal to the primal objective. The primal infeasibility certificate will be reported by **MOSEK** as a solution to the system

$$A^{T}y + s_{l}^{x} - s_{u}^{x} = 0,$$

$$-y + s_{l}^{c} - s_{u}^{c} = 0,$$

$$s_{l}^{c}, s_{u}^{c}, s_{l}^{x}, s_{u}^{x} \leq 0,$$
(7.6)

such that the objective value is strictly negative

$$(l^c)^T(s_l^c)^* - (u^c)^T(s_u^c)^* + (l^x)^T(s_l^x)^* - (u^x)^T(s_u^x)^* < 0.$$

Similarly, the certificate of dual infeasibility is an x satisfying the requirements of (7.5) such that $c^T x > 0$.

7.2 Conic Quadratic Optimization

Conic quadratic optimization is an extension of linear optimization (see Section 7.1) allowing conic domains to be specified for subsets of the problem variables. A conic quadratic optimization problem can be written as

minimize
$$c^T x + c^f$$

subject to $l^c \le Ax \le u^c$,
 $l^x \le x \le u^x$, (7.7)

where set \mathcal{K} is a Cartesian product of convex cones, namely $\mathcal{K} = \mathcal{K}_1 \times \cdots \times \mathcal{K}_p$. Having the domain restriction, $x \in \mathcal{K}$, is thus equivalent to

$$x^t \in \mathcal{K}_t \subseteq \mathbb{R}^{n_t}$$
,

where $x = (x^1, ..., x^p)$ is a partition of the problem variables. Please note that the *n*-dimensional Euclidean space \mathbb{R}^n is a cone itself, so simple linear variables are still allowed.

MOSEK supports only a limited number of cones, specifically:

- The \mathbb{R}^n set.
- The quadratic cone:

$$Q^{n} = \left\{ x \in \mathbb{R}^{n} : x_{1} \ge \sqrt{\sum_{j=2}^{n} x_{j}^{2}} \right\}.$$

• The rotated quadratic cone:

$$Q_r^n = \left\{ x \in \mathbb{R}^n : 2x_1 x_2 \ge \sum_{j=3}^n x_j^2, \quad x_1 \ge 0, \quad x_2 \ge 0 \right\}.$$

Although these cones may seem to provide only limited expressive power they can be used to model a wide range of problems as demonstrated in [MOSEKApS12].

7.2.1 Duality for Conic Quadratic Optimization

The dual problem corresponding to the conic quadratic optimization problem (7.7) is given by

where the dual cone \mathcal{K}^* is a Cartesian product of the cones

$$\mathcal{K}^* = \mathcal{K}_1^* \times \cdots \times \mathcal{K}_n^*$$

where each \mathcal{K}_t^* is the dual cone of \mathcal{K}_t . For the cone types **MOSEK** can handle, the relation between the primal and dual cone is given as follows:

• The \mathbb{R}^n set:

$$\mathcal{K}_t = \mathbb{R}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \{ s \in \mathbb{R}^{n_t} : \quad s = 0 \}.$$

• The quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : s_1 \ge \sqrt{\sum_{j=2}^{n_t} s_j^2} \right\}.$$

• The rotated quadratic cone:

$$\mathcal{K}_t = \mathcal{Q}_r^{n_t} \quad \Leftrightarrow \quad \mathcal{K}_t^* = \mathcal{Q}_r^{n_t} = \left\{ s \in \mathbb{R}^{n_t} : 2s_1 s_2 \ge \sum_{j=3}^{n_t} s_j^2, \quad s_1 \ge 0, \quad s_2 \ge 0 \right\}.$$

Please note that the dual problem of the dual problem is identical to the original primal problem.

7.2.2 Infeasibility for Conic Quadratic Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see Section 7.1.2).

Primal Infeasible Problems

If the problem (7.7) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is the certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{array}{lll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ \text{subject to} & & & & & & & \\ & & & & & & & & \\ & & & & & & & & \\ & & & & & & & & \\ & & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\ & & \\ & & & \\$$

such that the objective value is strictly positive.

Dual infeasible problems

If the problem (7.8) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

where

$$\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

and

$$\hat{l}_{j}^{x} = \left\{ \begin{array}{ll} 0 & \text{if } l_{j}^{x} > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_{j}^{x} := \left\{ \begin{array}{ll} 0 & \text{if } u_{j}^{x} < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

such that the objective value is strictly negative.

7.3 Semidefinite Optimization

Semidefinite optimization is an extension of conic quadratic optimization (see Section 7.2) allowing positive semidefinite matrix variables to be used in addition to the usual scalar variables. A semidefinite optimization problem can be written as

minimize
$$\sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \left\langle \overline{C}_j, \overline{X}_j \right\rangle + c^f$$
subject to $l_i^c \leq \sum_{j=0}^{n-1} a_{ij} x_j + \sum_{j=0}^{p-1} \left\langle \overline{A}_{ij}, \overline{X}_j \right\rangle \leq u_i^c, \quad i = 0, \dots, m-1$

$$l_j^x \leq \underbrace{x_j} \qquad \leq u_j^x, \quad j = 0, \dots, n-1$$

$$x \in \mathcal{K}, \overline{X}_j \in \mathcal{S}_+^{r_j}, \qquad j = 0, \dots, p-1$$

$$(7.9)$$

where the problem has p symmetric positive semidefinite variables $\overline{X}_j \in \mathcal{S}_+^{r_j}$ of dimension r_j with symmetric coefficient matrices $\overline{C}_j \in \mathcal{S}^{r_j}$ and $\overline{A}_{i,j} \in \mathcal{S}^{r_j}$. We use standard notation for the matrix inner product, i.e., for $U, V \in \mathbb{R}^{m \times n}$ we have

$$\langle U, V \rangle := \sum_{i=0}^{m-1} \sum_{j=0}^{n-1} U_{ij} V_{ij}.$$

With semidefinite optimization we can model a wide range of problems as demonstrated in [MOSEKApS12].

7.3.1 Duality for Semidefinite Optimization

The dual problem corresponding to the semidefinite optimization problem (7.9) is given by

maximize
$$(l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f$$
 subject to
$$c - A^T y + s_u^x - s_l^x = s_n^x,$$

$$\overline{C}_j - \sum_{i=0}^m y_i \overline{A}_{ij} = \overline{S}_j,$$
 $j = 0, \dots, p-1$ (7.10)
$$s_l^c - s_u^c = y,$$

$$s_l^c, s_u^c, s_l^x, s_u^x \ge 0,$$

$$s_n^x \in \mathcal{K}^*, \ \overline{S}_j \in \mathcal{S}_+^{r_j},$$
 $j = 0, \dots, p-1$

where $A \in \mathbb{R}^{m \times n}$, $A_{ij} = a_{ij}$, which is similar to the dual problem for conic quadratic optimization (see Section 7.2.1), except for the addition of dual constraints

$$\left(\overline{C}_j - \sum_{i=0}^m y_i \overline{A}_{ij}\right) \in \mathcal{S}_+^{r_j}.$$

Note that the dual of the dual problem is identical to the original primal problem.

7.3.2 Infeasibility for Semidefinite Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of the infeasibility. This works exactly as for linear problems (see Section 7.1.2).

Primal Infeasible Problems

If the problem (7.9) is infeasible, **MOSEK** will report a certificate of primal infeasibility: The dual solution reported is a certificate of infeasibility, and the primal solution is undefined.

A certificate of primal infeasibility is a feasible solution to the problem

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x \\ \text{subject to} & \\ & A^T y + s_l^x - s_u^x + s_n^x = 0, \\ & \sum_{i=0}^{m-1} y_i \overline{A}_{ij} + \overline{S}_j = 0, \\ & -y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0, \\ & s_n^c \in \mathcal{K}^*, \quad \overline{S}_j \in \mathcal{S}_+^{r_j}, & j = 0, \dots, p-1 \\ \end{array}$$

such that the objective value is strictly positive.

Dual Infeasible Problems

If the problem (7.10) is infeasible, **MOSEK** will report a certificate of dual infeasibility: The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

$$\begin{array}{lll} \text{minimize} & \sum_{j=0}^{n-1} c_j x_j + \sum_{j=0}^{p-1} \left\langle \overline{C}_j, \overline{X}_j \right\rangle \\ \text{subject to} & \hat{l}_i^c & \leq & \sum_{j=1}^n a_{ij} x_j + \sum_{j=0}^{p-1} \left\langle \overline{A}_{ij}, \overline{X}_j \right\rangle & \leq & \hat{u}_i^c, \quad i = 0, \dots, m-1 \\ & \hat{l}^x & \leq & x & \leq & \hat{u}^x, \\ & x \in \mathcal{K}, & \overline{X}_j \in \mathcal{S}_+^{r_j}, & j = 0, \dots, p-1 \end{array}$$

where

$$\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c >; -\infty, \\ -\infty & \text{otherwise,} \end{array} \right. \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c <; \infty, \\ \infty & \text{otherwise,} \end{array} \right.$$

and

$$\hat{l}_j^x = \left\{ \begin{array}{ll} 0 & \text{if } l_j^x >; -\infty, \\ -\infty & \text{otherwise,} \end{array} \right. \quad \text{and} \quad \hat{u}_j^x := \left\{ \begin{array}{ll} 0 & \text{if } u_j^x <; \infty, \\ \infty & \text{otherwise,} \end{array} \right.$$

such that the objective value is strictly negative.

7.4 Quadratic and Quadratically Constrained Optimization

A convex quadratic and quadratically constrained optimization problem is an optimization problem of the form

where Q^o and all Q^k are symmetric matrices. Moreover for convexity, Q^o must be a positive semidefinite matrix and Q^k must satisfy

$$\begin{array}{rcl} -\infty < l_k^c & \Rightarrow & Q^k \text{ is negative semidefinite,} \\ u_k^c < \infty & \Rightarrow & Q^k \text{ is positive semidefinite,} \\ -\infty < l_k^c \leq u_k^c < \infty & \Rightarrow & Q^k = 0. \end{array}$$

The convexity requirement is very important and MOSEK checks whether it is fullfiled.

7.4.1 A Recommendation

Any convex quadratic optimization problem can be reformulated as a conic quadratic optimization problem, see [MOSEKApS12] and in particular [And13]. In fact MOSEK does such conversion internally as a part of the solution process for the following reasons:

- the conic optimizer is numerically more robust than the one for quadratic problems.
- the conic optimizer is usually faster because quadratic cones are simpler than quadratic functions, even though the conic reformulation usually has more constraints and variables than the original quadratic formulation.
- it is easy to dualize the conic formulation if deemed worthwhile potentially leading to (huge) computational savings.

However, instead of relying on the automatic reformulation we recommend to formulate the problem as conic problem from scratch because:

- it saves the computational overhead of the reformulation including the convexity check. A conic problem is convex by construction and hence no convexity check is needed for conic problems.
- usually the modeller can do a better reformulation than the automatic method because the modeller can exploit the knowledge of what is being modelled.

To summarize we recommend to formulate quadratic problems and in particular quadratically constrained problems directly in conic form.

7.4.2 Duality for Quadratic and Quadratically Constrained Optimization

The dual problem corresponding to the quadratic and quadratically constrained optimization problem (7.11) is given by

$$\begin{array}{ll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + \frac{1}{2} x^T \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x + c^f \\ \text{subject to} & A^T y + s_l^x - s_u^x + \left\{ \sum_{k=0}^{m-1} y_k Q^k - Q^o \right\} x = c, \\ & - y + s_l^c - s_u^c = 0, \\ & s_l^c, s_u^c, s_u^x, s_u^x \geq 0. \end{array}$$

The dual problem is related to the dual problem for linear optimization (see Section 7.1.1), but depends on the variable x which in general can not be eliminated. In the solutions reported by **MOSEK**, the value of x is the same for the primal problem (7.11) and the dual problem (7.12).

7.4.3 Infeasibility for Quadratic and Quadratically Constrained Optimization

In case **MOSEK** finds a problem to be infeasible it reports a certificate of infeasibility. This works exactly as for linear problems (see Section 7.1.2).

Primal Infeasible Problems

If the problem (7.11) with all $Q^k = 0$ is infeasible, **MOSEK** will report a certificate of primal infeasibility. As the constraints are the same as for a linear problem, the certificate of infeasibility is the same as for linear optimization (see Section 7.1.2.1).

Dual Infeasible Problems

If the problem (7.12) with all $Q^k = 0$ is infeasible, **MOSEK** will report a certificate of dual infeasibility. The primal solution reported is the certificate of infeasibility, and the dual solution is undefined.

A certificate of dual infeasibility is a feasible solution to the problem

where

$$\hat{l}_i^c = \left\{ \begin{array}{ll} 0 & \text{if } l_i^c > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_i^c := \left\{ \begin{array}{ll} 0 & \text{if } u_i^c < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

and

$$\hat{l}_{j}^{x} = \left\{ \begin{array}{ll} 0 & \text{if } l_{j}^{x} > -\infty, \\ -\infty & \text{otherwise,} \end{array} \right\} \quad \text{and} \quad \hat{u}_{j}^{x} := \left\{ \begin{array}{ll} 0 & \text{if } u_{j}^{x} < \infty, \\ \infty & \text{otherwise,} \end{array} \right\}$$

such that the objective value is strictly negative.

7.5 General Convex Optimization

 \mathbf{MOSEK} is capable of solving smooth (twice differentiable) convex nonlinear optimization problems of the form

$$\begin{array}{lll} \text{minimize} & & f(x) + c^T x + c^f \\ \text{subject to} & l^c & \leq & g(x) + Ax & \leq & u^c, \\ & l^x & \leq & x & \leq & u^x, \end{array}$$

where

- *m* is the number of constraints.
- \bullet *n* is the number of decision variables.
- $x \in \mathbb{R}^n$ is a vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear part objective function.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.

- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $f: \mathbb{R}^n \to \mathbb{R}$ is a nonlinear function.
- $g: \mathbb{R}^n \to \mathbb{R}^m$ is a nonlinear vector function.

This means that the i-th constraint has the form

$$l_i^c \le g_i(x) + \sum_{j=1}^n a_{ij} x_j \le u_i^c.$$

The linear term Ax is included in g(x) since it can be handled much more efficiently as a separate entity when optimizing.

The nonlinear functions f and g must be smooth in all $x \in [l^x; u^x]$. Moreover, f(x) must be a convex function and $g_i(x)$ must satisfy

$$\begin{array}{rcl} -\infty < l_i^c & \Rightarrow & g_i(x) \text{ is concave,} \\ u_i^c < \infty & \Rightarrow & g_i(x) \text{ is convex,} \\ -\infty < l_i^c \leq u_i^c < \infty & \Rightarrow & g_i(x) = 0. \end{array}$$

7.5.1 Duality for General convex Optimization

Similar to the linear case, **MOSEK** reports dual information in the general nonlinear case. Indeed in this case the Lagrange function is defined by

$$\begin{array}{lcl} L(x,s_l^c,s_u^c,s_u^x,s_u^x) &:=& f(x)+c^Tx+c^f\\ &-(s_l^c)^T(g(x)+Ax-l^c)-(s_u^c)^T(u^c-g(x)-Ax)\\ &-(s_l^x)^T(x-l^x)-(s_u^x)^T(u^x-x), \end{array}$$

and the dual problem is given by

$$\begin{array}{lll} \text{maximize} & L(x, s_{l}^{c}, s_{u}^{c}, s_{l}^{x}, s_{u}^{x}) \\ \text{subject to} & \nabla_{x} L(x, s_{l}^{c}, s_{u}^{c}, s_{l}^{x}, s_{u}^{x})^{T} & = & 0, \\ & s_{l}^{c}, s_{u}^{c}, s_{l}^{x}, s_{u}^{x} \geq 0, \end{array}$$

which is equivalent to

$$\begin{array}{lll} \text{maximize} & (l^c)^T s_l^c - (u^c)^T s_u^c + (l^x)^T s_l^x - (u^x)^T s_u^x + c^f \\ & + f(x) - g(x)^T y - (\nabla f(x)^T - \nabla g(x)^T y)^T x \\ \text{subject to} & A^T y + s_l^x - s_u^x - (\nabla f(x)^T - \nabla g(x)^T y) & = c, \\ & - y + s_l^c - s_u^c & = 0, \\ & s_l^c, s_u^c, s_l^x, s_u^x \geq 0. \end{array}$$

In this context we use the following definition for scalar functions

$$\nabla f(x) = \left[\frac{\partial f(x)}{\partial x_1}, \dots, \frac{\partial f(x)}{\partial x_n}\right],$$

and accordingly for vector functions

$$\nabla g(x) = \begin{bmatrix} \nabla g_1(x) \\ \vdots \\ \nabla g_m(x) \end{bmatrix}.$$

THE OPTIMIZERS FOR CONTINUOUS PROBLEMS

The most essential part of **MOSEK** is the optimizers. Each optimizer is designed to solve a particular class of problems, i.e. linear, conic, or general nonlinear problems. The purpose of the present chapter is to discuss which optimizers are available for the continuous problem classes and how the performance of an optimizer can be tuned, if needed. This chapter deals with the optimizers for *continuous problems* with no integer variables.

When the optimizer is called, it roughly performs the following steps:

- 1. Presolve: Preprocessing to reduce the size of the problem.
- 2. Dualizer: Choosing whether to solve the primal or the dual form of the problem.
- 3. Scaling: Scaling the problem for better numerical stability.
- 4. Optimize: Solve the problem using selected method.

The first three preprocessing steps are transparent to the user, but useful to know about for tuning purposes. In general, the purpose of the preprocessing steps is to make the actual optimization more efficient and robust.

Using multiple threads

The interior-point optimizers in **MOSEK** have been parallelized. This means that if you solve linear, quadratic, conic, or general convex optimization problem using the interior-point optimizer, you can take advantage of multiple CPU's.

By default MOSEK will automatically select the number of threads to be employed when solving the problem. However, the number of threads employed can be changed by setting the parameter $MSK_IPAR_NUM_THREADS$. This should never exceed the number of cores on the computer.

The speed-up obtained when using multiple threads is highly problem and hardware dependent, and consequently, it is advisable to compare single threaded and multi threaded performance for the given problem type to determine the optimal settings.

For small problems, using multiple threads is not be worthwhile and may even be counter productive.

8.1 Presolve

Before an optimizer actually performs the optimization the problem is preprocessed using the so-called presolve. The purpose of the presolve is to

- 1. remove redundant constraints,
- 2. eliminate fixed variables,
- 3. remove linear dependencies,
- 4. substitute out (implied) free variables, and

5. reduce the size of the optimization problem in general.

After the presolved problem has been optimized the solution is automatically postsolved so that the returned solution is valid for the original problem. Hence, the presolve is completely transparent. For further details about the presolve phase, please see [AA95] and [AGMX96].

It is possible to fine-tune the behavior of the presolve or to turn it off entirely. If presolve consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This is done by setting the parameter $MSK_IPAR_PRESOLVE_USE$ to $MSK_PRESOLVE_MODE_OFF$.

The two most time-consuming steps of the presolve are

- the eliminator, and
- the linear dependency check.

Therefore, in some cases it is worthwhile to disable one or both of these.

Numerical issues in the presolve

During the presolve the problem is reformulated so that it hopefully solves faster. However, in rare cases the presolved problem may be harder to solve then the original problem. The presolve may also be infeasible although the original problem is not.

If it is suspected that presolved problem is much harder to solve than the original then it is suggested to first turn the eliminator off by setting the parameter $MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES$ to 0. If that does not help, then trying to turn presolve off may help.

Since all computations are done in finite prescision then the presolve employs some tolerances when concluding a variable is fixed or constraint is redundant. If it happens that \mathbf{MOSEK} incorrectly concludes a problem is primal or dual infeasible, then it is worthwhile to try to reduce the parameters $MSK_DPAR_PRESOLVE_TOL_X$ and $MSK_DPAR_PRESOLVE_TOL_S$. However, if reducing the parameters actually helps then this should be taken as an indication that the problem is badly formulated.

Eliminator

The purpose of the eliminator is to eliminate free and implied free variables from the problem using substitution. For instance, given the constraints

$$\begin{array}{rcl} y & = & \sum_j x_j, \\ y, x & \geq & 0, \end{array}$$

y is an implied free variable that can be substituted out of the problem, if deemed worthwhile. If the eliminator consumes too much time or memory compared to the reduction in problem size gained it may be disabled. This can be done by setting the parameter $MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES$ to 0. In rare cases the eliminator may cause that the problem becomes much hard to solve.

Linear dependency checker

The purpose of the linear dependency check is to remove linear dependencies among the linear equalities. For instance, the three linear equalities

$$\begin{array}{rcl} x_1 + x_2 + x_3 & = & 1, \\ x_1 + 0.5x_2 & = & 0.5, \\ 0.5x_2 + x_3 & = & 0.5 \end{array}$$

contain exactly one linear dependency. This implies that one of the constraints can be dropped without changing the set of feasible solutions. Removing linear dependencies is in general a good idea since it reduces the size of the problem. Moreover, the linear dependencies are likely to introduce numerical problems in the optimization phase.

It is best practise to build models without linear dependencies. If the linear dependencies are removed at the modeling stage, the linear dependency check can safely be disabled by setting the parameter $MSK_IPAR_PRESOLVE_LINDEP_USE$ to MSK_OFF .

Dualizer

All linear, conic, and convex optimization problems have an equivalent dual problem associated with them. **MOSEK** has built-in heuristics to determine if it is most efficient to solve the primal or dual problem. The form (primal or dual) solved is displayed in the **MOSEK** log. Should the internal heuristics not choose the most efficient form of the problem it may be worthwhile to set the dualizer manually by setting the parameters:

- MSK_IPAR_INTPNT_SOLVE_FORM: In case of the interior-point optimizer.
- \bullet $\textit{MSK_IPAR_SIM_SOLVE_FORM}$: In case of the simplex optimizer.

Note that currently only linear problems may be dualized.

Scaling

Problems containing data with large and/or small coefficients, say 1.0e + 9 or 1.0e - 7, are often hard to solve. Significant digits may be truncated in calculations with finite precision, which can result in the optimizer relying on inaccurate calculations. Since computers work in finite precision, extreme coefficients should be avoided. In general, data around the same *order of magnitude* is preferred, and we will refer to a problem, satisfying this loose property, as being *well-scaled*. If the problem is not well scaled, **MOSEK** will try to scale (multiply) constraints and variables by suitable constants. **MOSEK** solves the scaled problem to improve the numerical properties.

The scaling process is transparent, i.e. the solution to the original problem is reported. It is important to be aware that the optimizer terminates when the termination criterion is met on the scaled problem, therefore significant primal or dual infeasibilities may occur after unscaling for badly scaled problems. The best solution of this issue is to reformulate the problem, making it better scaled.

By default MOSEK heuristically chooses a suitable scaling. The scaling for interior-point and simplex optimizers can be controlled with the parameters $MSK_IPAR_INTPNT_SCALING$ and $MSK_IPAR_SIM_SCALING$ respectively.

8.2 Linear Optimization

8.2.1 Optimizer Selection

Two different types of optimizers are available for linear problems: The default is an interior-point method, and the alternatives are simplex methods. The optimizer can be selected using the parameter $MSK_IPAR_OPTIMIZER$.

8.2.2 The Interior-point Optimizer

The purpose of this section is to provide information about the algorithm employed in **MOSEK** interior-point optimizer.

In order to keep the discussion simple it is assumed that MOSEK solves linear optimization problems of standard form

minimize
$$c^T x$$

subject to $Ax = b$, $x \ge 0$. (8.1)

This is in fact what happens inside **MOSEK**; for efficiency reasons **MOSEK** converts the problem to standard form before solving, then converts it back to the input form when reporting the solution.

Since it is not known beforehand whether problem (8.1) has an optimal solution, is primal infeasible or is dual infeasible, the optimization algorithm must deal with all three situations. This is the reason that **MOSEK** solves the so-called homogeneous model

$$Ax - b\tau = 0,$$

$$A^{T}y + s - c\tau = 0,$$

$$-c^{T}x + b^{T}y - \kappa = 0,$$

$$x, s, \tau, \kappa \geq 0,$$

$$(8.2)$$

where y and s correspond to the dual variables in (8.1), and τ and κ are two additional scalar variables. Note that the homogeneous model (8.2) always has solution since

$$(x, y, s, \tau, \kappa) = (0, 0, 0, 0, 0)$$

is a solution, although not a very interesting one.

Any solution

$$(x^*, y^*, s^*, \tau^*, \kappa^*)$$

to the homogeneous model (8.2) satisfies

$$x_j^* s_j^* = 0$$
 and $\tau^* \kappa^* = 0$.

Moreover, there is always a solution that has the property

$$\tau^* + \kappa^* > 0.$$

First, assume that $\tau^* > 0$. It follows that

$$\begin{array}{cccc} A \frac{x^*}{\tau^*} & = & b, \\ A^T \frac{y^*}{\tau^*} + \frac{s^*}{\tau^*} & = & c, \\ -c^T \frac{x^*}{\tau^*} + b^T \frac{y}{\tau^*} & = & 0, \\ x^*, s^*, \tau^*, \kappa^* & \geq & 0. \end{array}$$

This shows that $\frac{x^*}{\tau^*}$ is a primal optimal solution and $(\frac{y^*}{\tau^*}, \frac{s^*}{\tau^*})$ is a dual optimal solution; this is reported as the optimal interior-point solution since

$$(x, y, s) = \left\{ \frac{x^*}{\tau^*}, \frac{y^*}{\tau^*}, \frac{s^*}{\tau^*} \right\}$$

is a primal-dual optimal solution.

On other hand, if $\kappa^* > 0$ then

$$\begin{array}{rcl} Ax^* & = & 0, \\ A^Ty^* + s^* & = & 0, \\ -c^Tx^* + b^Ty^* & = & \kappa^*, \\ x^*, s^*, \tau^*, \kappa^* & \geq & 0. \end{array}$$

This implies that at least one of

$$-c^T x^* > 0 \tag{8.3}$$

or

$$b^T y^* > 0 (8.4)$$

is satisfied. If (8.3) is satisfied then x^* is a certificate of dual infeasibility, whereas if (8.4) is satisfied then y^* is a certificate of dual infeasibility.

In summary, by computing an appropriate solution to the homogeneous model, all information required for a solution to the original problem is obtained. A solution to the homogeneous model can be computed using a primal-dual interior-point algorithm [And09].

Interior-point Termination Criterion

For efficiency reasons it is not practical to solve the homogeneous model exactly. Hence, an exact optimal solution or an exact infeasibility certificate cannot be computed and a reasonable termination criterion has to be employed.

In every iteration, k, of the interior-point algorithm a trial solution

$$(x^k, y^k, s^k, \tau^k, \kappa^k)$$

to homogeneous model is generated where

$$x^k, s^k, \tau^k, \kappa^k > 0.$$

Whenever the trial solution satisfies the criterion

$$\left\| A \frac{x^{k}}{\tau^{k}} - b \right\|_{\infty} \leq \epsilon_{p} (1 + \|b\|_{\infty}),
\left\| A^{T} \frac{y^{k}}{\tau^{k}} + \frac{s^{k}}{\tau^{k}} - c \right\|_{\infty} \leq \epsilon_{d} (1 + \|c\|_{\infty}), \text{ and}
\min \left(\frac{(x^{k})^{T} s^{k}}{(\tau^{k})^{2}}, \left| \frac{c^{T} x^{k}}{\tau^{k}} - \frac{b^{T} y^{k}}{\tau^{k}} \right| \right) \leq \epsilon_{g} \max \left(1, \frac{\min(\left| c^{T} x^{k} \right|, \left| b^{T} y^{k} \right|)}{\tau^{k}} \right),$$
(8.5)

the interior-point optimizer is terminated and

$$\frac{(x^k, y^k, s^k)}{\tau^k}$$

is reported as the primal-dual optimal solution. The interpretation of (8.5) is that the optimizer is terminated if

- $\frac{x^k}{\tau^k}$ is approximately primal feasible,
- $\bullet \ \left\{ \frac{y^k}{\tau^k}, \frac{s^k}{\tau^k} \right\}$ is approximately dual feasible, and
- the duality gap is almost zero.

On the other hand, if the trial solution satisfies

$$-\epsilon_i c^T x^k > \frac{\|c\|_{\infty}}{\max\left(1, \|b\|_{\infty}\right)} \|Ax^k\|_{\infty}$$

then the problem is declared dual infeasible and x^k is reported as a certificate of dual infeasibility. The motivation for this stopping criterion is as follows: First assume that $\|Ax^k\|_{\infty} = 0$; then x^k is an exact certificate of dual infeasibility. Next assume that this is not the case, i.e.

$$||Ax^k||_{\infty} > 0,$$

and define

$$\bar{x} := \epsilon_i \frac{\max\left(1, \|b\|_{\infty}\right)}{\|Ax^k\|_{\infty} \|c\|_{\infty}} x^k.$$

It is easy to verify that

$$||A\bar{x}||_{\infty} = \epsilon_i \frac{\max(1, ||b||_{\infty})}{||c||_{\infty}} \text{ and } -c^T \bar{x} > 1,$$

which shows \bar{x} is an approximate certificate of dual infeasibility where ε_i controls the quality of the approximation. A smaller value means a better approximation.

Finally, if

$$\epsilon_i b^T y^k > \frac{\|b\|_{\infty}}{\max\left(1, \|c\|_{\infty}\right)} \left\|A^T y^k + s^k\right\|_{\infty}$$

then y^k is reported as a certificate of primal infeasibility.

It is possible to adjust the tolerances ε_p , ε_d , ε_g and ε_i using parameters; see Table 8.1 for details.

Table 8.1: Parameters employed in termination criterion

ToleranceParameter	name
$arepsilon_p$	MSK_DPAR_INTPNT_TOL_PFEAS
$arepsilon_d$	MSK_DPAR_INTPNT_TOL_DFEAS
ε_g	MSK_DPAR_INTPNT_TOL_REL_GAP
$arepsilon_i$	MSK_DPAR_INTPNT_TOL_INFEAS

The default values of the termination tolerances are chosen such that for a majority of problems appearing in practice it is not possible to achieve much better accuracy. Therefore, tightening the tolerances usually is not worthwhile. However, an inspection of (8.5) reveals that quality of the solution is dependent on $||b||_{\infty}$ and $||c||_{\infty}$; the smaller the norms are, the better the solution accuracy.

The interior-point method as implemented by **MOSEK** will converge toward optimality and primal and dual feasibility at the same rate [And09]. This means that if the optimizer is stopped prematurely then it is very unlikely that either the primal or dual solution is feasible. Another consequence is that in most cases all the tolerances, ε_p , ε_d and ε_q , have to be relaxed together to achieve an effect.

In some cases the interior-point method terminates having found a solution not too far from meeting the optimality condition (8.5). A solution is defined as near optimal if scaling ε_p , ε_d and ε_g by any number $\varepsilon_n \in [1.0, +\infty]$ conditions (8.5) are satisfied.

A near optimal solution is therefore of lower quality but still potentially valuable. If for instance the solver stalls, i.e. it can make no more significant progress towards the optimal solution, a near optimal solution could be available and be good enough for the user.

The basis identification discussed in Section 8.2.2.2 requires an optimal solution to work well; hence basis identification should be turned off if the termination criterion is relaxed.

To conclude the discussion in this section, relaxing the termination criterion is usually not worthwhile.

Basis Identification

An interior-point optimizer does not return an optimal basic solution unless the problem has a unique primal and dual optimal solution. Therefore, the interior-point optimizer has an optimal post-processing step that computes an optimal basic solution starting from the optimal interior-point solution. More information about the basis identification procedure may be found in [AY96]. In the following we provide an overall idea of the procedure.

There are some cases in which a basic solution could be more valuable:

- a basic solution is often more accurate than an interior-point solution,
- a basic solution can be used to warm-start the simplex algorithm in case of reoptimization,
- a basic solution is in general more sparse, i.e. more variables are fixed to zero. This is particularly appealing when solving continuous relaxation of mixed integer problems, as well as in all applications in which sparser solutions are preferred.

To illustrate how the basis identification routine works, we use the following trivial example:

minimize
$$x + y$$

subject to $x + y = 1$,
 $x, y > 0$.

It is easy to see that all feasible solutions are also optimal. In particular, there are two basic solutions namely

$$\begin{array}{rcl} (x_1^*,y_1^*) & = & (1,0), \\ (x_2^*,y_2^*) & = & (0,1). \end{array}$$

The interior point algorithm will actually converge to the center of the optimal set, i.e. to $(x^*, y^*) = (1/2, 1/2)$ (to see this in **MOSEK** deactivate *Presolve*).

In practice, when the algorithm gets close to the optimal solution, it is possible to construct in polynomial time an initial basis for the simplex algorithm from the current interior point solution. This basis is used to warm-start the simplex algorithm that will provide the optimal basic solution.

In most cases the constructed basis is optimal, or very few iterations are required by the simplex algorithm to make it optimal and hence the final *clean* phase be short. However, in some cases for nasty problems e.g. ill-conditioned problems the additional simplex clean up phase may take of lot a time.

By default **MOSEK** performs a basis identification. However, if a basic solution is not needed, the basis identification procedure can be turned off. The parameters

- MSK_IPAR_INTPNT_BASIS,
- MSK_IPAR_BI_IGNORE_MAX_ITER, and
- MSK_IPAR_BI_IGNORE_NUM_ERROR

control when basis identification is performed.

The type of simplex algorithm to be used can be tuned by the $MSK_IPAR_BI_CLEAN_OPTIMIZER$ parameter i.e. primal or dual simplex, and the maximum number of iterations can be set by the $MSK_IPAR_BI_MAX_ITERATIONS$.

Finally, it should be mentioned that there is no guarantee on which basic solution will be returned.

The Interior-point Log

Below is a typical log output from the interior-point optimizer presented:

```
Optimizer - threads
                                    : 1
Optimizer
         - solved problem
                                    : the dual
Optimizer - Constraints
                                    : 2
Optimizer - Cones
                                    : 0
                                   : 6
Optimizer - Scalar variables
                                                        conic
                                                                               : 0
                                                                               : 0
Optimizer - Semi-definite variables: 0
                                                        scalarized
          - setup time
                                                        dense det. time
Factor
                                   : 0.00
                                                                               : 0.00
           - ML order time
                                                                               : 0.00
Factor
                                   : 0.00
                                                        GP order time
Factor
           - nonzeros before factor : 3
                                                        after factor
                                                                               : 3
Factor
           - dense dim.
                                    : 0
                                                                               : 7.00e+001
                                                        flops
ITE PFEAS
            DFEAS
                      GFEAS
                               PRSTATUS
                                          POBJ
                                                            DOBJ
                                                                              MU
                                                                                       TIME
                                          0.00000000e+000 -2.208000000e+003 1.0e+000 0.00
   1.0e+000 8.6e+000 6.1e+000 1.00e+000
    1.1e+000 2.5e+000 1.6e-001 0.00e+000
                                          -7.901380925e+003 -7.394611417e+003 2.5e+000 0.00
2
   1.4e-001 3.4e-001 2.1e-002 8.36e-001
                                          -8.113031650e+003 -8.055866001e+003 3.3e-001 0.00
3
   2.4e-002 5.8e-002 3.6e-003 1.27e+000
                                          -7.777530698e+003 -7.766471080e+003 5.7e-002 0.01
4
   1.3e-004 3.2e-004 2.0e-005 1.08e+000
                                          -7.668323435e+003 -7.668207177e+003 3.2e-004 0.01
5
   1.3e-008 3.2e-008 2.0e-009 1.00e+000
                                          -7.668000027e+003 -7.668000015e+003 3.2e-008 0.01
                                         -7.667999994e+003 -7.667999994e+003 3.2e-012 0.01
   1.3e-012 3.2e-012 2.0e-013 1.00e+000
```

The first line displays the number of threads used by the optimizer and second line tells that the optimizer chose to solve the dual problem rather than the primal problem. The next line displays the problem dimensions as seen by the optimizer, and the Factor... lines show various statistics. This is followed by the iteration log.

Using the same notation as in Section 8.2.2 the columns of the iteration log have the following meaning:

- ITE: Iteration index.
- PFEAS: $\|Ax^k b\tau^k\|_{\infty}$. The numbers in this column should converge monotonically towards to zero but may stall at low level due to rounding errors.
- DFEAS: $\|A^Ty^k + s^k c\tau^k\|_{\infty}$. The numbers in this column should converge monotonically toward to zero but may stall at low level due to rounding errors.

- GFEAS: $|-c^Tx^k+b^Ty^k-\kappa^k|$. The numbers in this column should converge monotonically toward to zero but may stall at low level due to rounding errors.
- PRSTATUS: This number converges to 1 if the problem has an optimal solution whereas it converges to -1 if that is not the case.
- POBJ: $c^T x^k / \tau^k$. An estimate for the primal objective value.
- DOBJ: $b^T y^k / \tau^k$. An estimate for the dual objective value.
- MU: $\frac{(x^k)^T s^k + \tau^k \kappa^k}{n+1}$. The numbers in this column should always converge monotonically to zero.
- TIME: Time spend since the optimization started.

8.2.3 The simplex Based Optimizer

An alternative to the interior-point optimizer is the simplex optimizer.

The simplex optimizer uses a different method that allows exploiting an initial guess for the optimal solution to reduce the solution time. Depending on the problem it may be faster or slower to use an initial guess; see section 8.2.4 for a discussion.

MOSEK provides both a primal and a dual variant of the simplex optimizer — we will return to this later

Simplex Termination Criterion

The simplex optimizer terminates when it finds an optimal basic solution or an infeasibility certificate. A basic solution is optimal when it is primal and dual feasible; see Section 7.1 and 7.1.1 for a definition of the primal and dual problem. Due to the fact that computations are performed in finite precision **MOSEK** allows violation of primal and dual feasibility within certain tolerances. The user can control the allowed primal and dual tolerances with the parameters $MSK_DPAR_BASIS_TOL_X$ and $MSK_DPAR_BASIS_TOL_S$.

Starting From an Existing Solution

When using the simplex optimizer it may be possible to reuse an existing solution and thereby reduce the solution time significantly. When a simplex optimizer starts from an existing solution it is said to perform a *warm-start*. If the user is solving a sequence of optimization problems by solving the problem, making modifications, and solving again, **MOSEK** will warm-start automatically.

Setting the parameter MSK_IPAR_OPTIMIZER to MSK_OPTIMIZER_FREE_SIMPLEX instructs MOSEK to select automatically between the primal and the dual simplex optimizers. Hence, MOSEK tries to choose the best optimizer for the given problem and the available solution.

By default **MOSEK** uses presolve when performing a warm-start. If the optimizer only needs very few iterations to find the optimal solution it may be better to turn off the presolve.

Numerical Difficulties in the Simplex Optimizers

Though MOSEK is designed to minimize numerical instability, completely avoiding it is impossible when working in finite precision. MOSEK counts a "numerical unexpected behavior" event inside the optimizer as a *set-back*. The user can define how many set-backs the optimizer accepts; if that number is exceeded, the optimization will be aborted. Set-backs are implemented to avoid long sequences where the optimizer tries to recover from an unstable situation.

Set-backs are, for example, repeated singularities when factorizing the basis matrix, repeated loss of feasibility, degeneracy problems (no progress in objective) and other events indicating numerical difficulties. If the simplex optimizer encounters a lot of set-backs the problem is usually badly scaled; in such

a situation try to reformulate into a better scaled problem. Then, if a lot of set-backs still occur, trying one or more of the following suggestions may be worthwhile:

- Raise tolerances for allowed primal or dual feasibility: Hence, increase the value of
 - MSK_DPAR_BASIS_TOL_X, and
 - MSK_DPAR_BASIS_TOL_S.
- Raise or lower pivot tolerance: Change the MSK_DPAR_SIMPLEX_ABS_TOL_PIV parameter.
- Switch optimizer: Try another optimizer.
- Switch off crash: Set both MSK_IPAR_SIM_PRIMAL_CRASH and MSK_IPAR_SIM_DUAL_CRASH to 0.
- Experiment with other pricing strategies: Try different values for the parameters
 - MSK_IPAR_SIM_PRIMAL_SELECTION and
 - MSK_IPAR_SIM_DUAL_SELECTION.
- If you are using warm-starts, in rare cases switching off this feature may improve stability. This is controlled by the $MSK_IPAR_SIM_HOTSTART$ parameter.
- Increase maximum set backs allowed controlled by MSK_IPAR_SIM_MAX_NUM_SETBACKS.
- If the problem repeatedly becomes infeasible try switching off the special degeneracy handling. See the parameter $MSK_IPAR_SIM_DEGEN$ for details.

8.2.4 The Interior-point or the Simplex Optimizer?

Given a linear optimization problem, which optimizer is the best: The primal simplex, the dual simplex or the interior-point optimizer?

It is impossible to provide a general answer to this question. However, the interior-point optimizer behaves more predictably: it tends to use between 20 and 100 iterations, almost independently of problem size, but cannot perform warm-start, while simplex can take advantage of an initial solution, but is less predictable for cold-start. The interior-point optimizer is used by default.

8.2.5 The Primal or the Dual Simplex Variant?

MOSEK provides both a primal and a dual simplex optimizer. Predicting which simplex optimizer is faster is impossible, however, in recent years the dual optimizer has seen several algorithmic and computational improvements, which, in our experience, makes it faster on average than the primal simplex optimizer. Still, it depends much on the problem structure and size.

Setting the MSK_IPAR_OPTIMIZER parameter to MSK_OPTIMIZER_FREE_SIMPLEX instructs MOSEK to choose which simplex optimizer to use automatically.

To summarize, if you want to know which optimizer is faster for a given problem type, you should try all the optimizers.

8.3 Conic Optimization

8.3.1 The Interior-point Optimizer

For conic optimization problems only an interior-point type optimizer is available. The interior-point optimizer is an implementation of the so-called homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see [ART03].

Interior-point Termination Criteria

The parameters controlling when the conic interior-point optimizer terminates are shown in Table 8.2.

Table 8.2: Parameters employed in termination criterion.

Parameter name	Purpose	
MSK_DPAR_INTPNT_CO_TOL_PFEAS	Controls primal feasibility	
MSK_DPAR_INTPNT_CO_TOL_DFEAS	Controls dual feasibility	
MSK_DPAR_INTPNT_CO_TOL_REL_GAP	Controls relative gap	
MSK_DPAR_INTPNT_TOL_INFEAS	Controls when the problem is declared infeasible	
MSK_DPAR_INTPNT_CO_TOL_MU_RED	Controls when the complementarity is reduced enough	

8.4 Nonlinear Convex Optimization

8.4.1 The Interior-point Optimizer

For quadratic, quadratically constrained, and general convex optimization problems an interior-point type optimizer is available. The interior-point optimizer is an implementation of the homogeneous and self-dual algorithm. For a detailed description of the algorithm, please see [AY98], [AY99].

The Convexity Requirement

Continuous nonlinear problems are required to be convex. For quadratic problems **MOSEK** test this requirement before optimizing. Specifying a non-convex problem results in an error message.

The following parameters are available to control the convexity check:

- MSK_IPAR_CHECK_CONVEXITY: Turn convexity check on/off.
- MSK_DPAR_CHECK_CONVEXITY_REL_TOL: Tolerance for convexity check.
- MSK_IPAR_LOG_CHECK_CONVEXITY: Turn on more log information for debugging.

The Differentiabilty Requirement

The nonlinear optimizer in **MOSEK** requires both first order and second order derivatives. This of course implies care should be taken when solving problems involving non-differentiable functions.

For instance, the function

$$f(x) = x^2$$

is differentiable everywhere whereas the function

$$f(x) = \sqrt{x}$$

is only differentiable for x>0. In order to make sure that \mathbf{MOSEK} evaluates the functions at points where they are differentiable, the function domains must be defined by setting appropriate variable bounds.

In general, if a variable is not ranged \mathbf{MOSEK} will only evaluate that variable at points strictly within the bounds. Hence, imposing the bound

in the case of \sqrt{x} is sufficient to guarantee that the function will only be evaluated in points where it is differentiable.

However, if a function is differentiable on a closed range, specifying the variable bounds is not sufficient. Consider the function

$$f(x) = \frac{1}{x} + \frac{1}{1 - x}. ag{8.6}$$

In this case the bounds

$$0 \le x \le 1$$

will not guarantee that \mathbf{MOSEK} only evaluates the function for x between 0 and 1 . To force \mathbf{MOSEK} to strictly satisfy both bounds on ranged variables set the parameter $\mathit{MSK_IPAR_INTPNT_STARTING_POINT}$ to $\mathit{MSK_STARTING_POINT_SATISFY_BOUNDS}$.

For efficiency reasons it may be better to reformulate the problem than to force **MOSEK** to observe ranged bounds strictly. For instance, (8.6) can be reformulated as follows

$$\begin{array}{rcl} f(x) & = & \frac{1}{x} + \frac{1}{y} \\ 0 & = & 1 - x - y \\ 0 & \leq & x \\ 0 & \leq & y. \end{array}$$

Interior-point Termination Criteria

The parameters controlling when the general convex interior-point optimizer terminates are shown in Table 8.3.

Parameter name	Purpose	
MSK_DPAR_INTPNT_NL_TOL_PFEAS	VL_TOL_PFEAS Controls primal feasibility	
MSK_DPAR_INTPNT_NL_TOL_DFEAS	Controls dual feasibility	
MSK_DPAR_INTPNT_NL_TOL_REL_GAP	Controls relative gap	
MSK_DPAR_INTPNT_TOL_INFEAS	Controls when the problem is declared infeasible	
MSK DPAR INTPNT NI. TOI. MIJ RED	Controls when the complementarity is reduced enough	

Table 8.3: Parameters employed in termination criteria.

8.5 Using Multiple Threads in an Optimizer

If multiple cores are available then it is possible for **MOSEK** to take advantage of them to speed up the computation. However, please note the speedup achieved is going to be dependent on the problem characteristics e.g. the size of problem. Typically for smallish problems no speedup is obtained by exploiting multiple cores. In fact forcing **MOSEK** to use one core can increase speed because parallel overhead is avoided.

8.5.1 Thread Safety

The **MOSEK** API is thread-safe provided that a task is only modified or accessed from one thread at any given time. Also accessing two or more separate tasks from threads at the same time is safe. Sharing an environment between threads is safe.

8.5.2 Determinism

The optimizers are run-to-run deterministic which means if a problem is solved twice on the same computer using the same parameter setting and exactly the same input then exactly the same results is obtained. One qualification is that no time limits must be imposed because the time taken to perform an operation on a computer is dependent on many factors such as the current workload.

8.5.3 The Parallelized Interior-point Optimizer

By default the interior-point optimizer exploits multiple cores using multithreading. Hence, big tasks such as large dense matrix multiplication may be divided into several independent smaller tasks that can be computed independently. However, there is a computational overhead associated with exploiting multiple threads e.g. cost of the additional coordination etc. Therefore, it may be advantageous to turn off the mutithreading for smallish problem using the parameter <code>MSK_IPAR_INTPNT_MULTI_THREAD</code>.

Moreover, when the interior-point optimizer is allowed to exploit multiple threads, then the parameter $MSK_IPAR_NUM_THREADS$ controls the maximum number of threads (and therefore the number of cores) that MOSEK will employ.

THE OPTIMIZER FOR MIXED-INTEGER PROBLEMS

A problem is a mixed-integer optimization problem when one or more of the variables are constrained to be integer valued. **MOSEK** can solve mixed-integer

- linear.
- quadratic and quadratically constrained, and
- conic qudratic

problems.

Readers unfamiliar with integer optimization are recommended to consult some relevant literature, e.g. the book [Wol98] by Wolsey.

9.1 Some Concepts and Facts Related to Mixed-integer Optimization

It is important to understand that in a worst-case scenario, the time required to solve integer optimization problems grows exponentially with the size of the problem. For instance, assume that a problem contains n binary variables, then the time required to solve the problem in the worst case may be proportional to 2^n . The value of 2^n is huge even for moderate values of n.

In practice this implies that the focus should be on computing a near optimal solution quickly rather than on locating an optimal solution. Even if the problem is only solved approximately, it is important to know how far the approximate solution is from an optimal one. In order to say something about the quality of an approximate solution the concept of *relaxation* is important.

The mixed-integer optimization problem

$$z^* = \underset{\text{subject to}}{\text{minimize}} c^T x$$

$$x \ge 0$$

$$x_j \in \mathbb{Z}, \quad \forall j \in \mathcal{J},$$

$$(9.1)$$

has the continuous relaxation

$$\begin{array}{llll} \underline{z} & = & \text{minimize} & c^T x \\ & & \text{subject to} & Ax & = & b, \\ & & & x \geq 0 \end{array}$$

The continuos relaxation is identical to the mixed-integer problem with the restriction that some variables must be integers removed.

There are two important observations about the continuous relaxation. First, the continuous relaxation is usually much faster to optimize than the mixed-integer problem. Secondly if \hat{x} is any feasible solution to (9.1) and

$$\bar{z} := c^T \hat{x}$$

then

$$\underline{z} \le z^* \le \bar{z}$$
.

This is an important observation since if it is only possible to find a near optimal solution within a reasonable time frame then the quality of the solution can nevertheless be evaluated. The value \underline{z} is a lower bound on the optimal objective value. This implies that the obtained solution is no further away from the optimum than $\overline{z} - \underline{z}$ in terms of the objective value.

Whenever a mixed-integer problem is solved **MOSEK** reports this lower bound so that the quality of the reported solution can be evaluated.

9.2 The Mixed-integer Optimizer

The mixed-integer optimizer can handle problems with linear, quadratic objective and constraints and conic constraints. However, a problem can not contain both quadratic objective or constraints and conic constraints

The mixed-integer optimizer is specialized for solving linear and conic optimization problems. It can also solve pure quadratic and quadratically constrained problems; these problems are automatically converted to conic problems before being solved.

The mixed-integer optimizer is run-to-run deterministic. This means that if a problem is solved twice on the same computer with identical options then the obtained solution will be bit-for-bit identical for the two runs. However, if a time limit is set then this may not be case since the time taken to solve a problem is not deterministic. The mixed-integer optimizer is parallelized i.e. it can exploit multiple cores during the optimization.

The solution process can be split into these phases:

- 1. **Presolve:** In this phase the optimizer tries to reduce the size of the problem and improve the formulation using preprocessing techniques. The presolve stage can be turned off using the $MSK_IPAR_PRESOLVE_USE$ parameter
- 2. Cut generation: Valid inequalities (cuts) are added to improve the lower bound
- 3. Heuristic: Using heuristics the optimizer tries to guess a good feasible solution. Heuristics can be controlled by the parameter $MSK_IPAR_MIO_HEURISTIC_LEVEL$
- 4. Search: The optimal solution is located by branching on integer variables

9.3 Termination Criterion

In general, it is time consuming to find an exact feasible and optimal solution to an integer optimization problem, though in many practical cases it may be possible to find a sufficiently good solution. Therefore, the mixed-integer optimizer employs a relaxed feasibility and optimality criterion to determine when a satisfactory solution is located.

A candidate solution that is feasible for the continuous relaxation is said to be an integer feasible solution if the criterion

$$\min(x_i - |x_i|, \lceil x_i \rceil - x_i) \le \delta_1 \quad \forall j \in \mathcal{J}$$

is satisfied, meaning that x_j is at most δ_1 from the nearest integer.

Whenever the integer optimizer locates an integer feasible solution it will check if the criterion

$$\bar{z} - z \le \max(\delta_2, \delta_3 \max(10^{-10}, |\bar{z}|))$$

is satisfied. If this is the case, the integer optimizer terminates and reports the integer feasible solution as an optimal solution. Please note that \underline{z} is a valid lower bound determined by the integer optimizer during the solution process, i.e.

$$\underline{z} \leq z^*$$
.

The lower bound \underline{z} normally increases during the solution process.

9.3.1 Relaxed Termination

If an optimal solution cannot be located within a reasonable time, it may be advantageous to employ a relaxed termination criterion after some time. Whenever the integer optimizer locates an integer feasible solution and has spent at least the number of seconds defined by the MSK_DPAR_MIO_DISABLE_TERM_TIME parameter on solving the problem, it will check whether the criterion

$$\bar{z} - \underline{z} \le \max(\delta_4, \delta_5 \max(10^{-10}, |\bar{z}|))$$

is satisfied. If it is satisfied, the optimizer will report that the candidate solution is **near optimal** and then terminate. Please note that since this criterion depends on timing, the optimizer will not be run to run deterministic.

9.4 Parameters Affecting the Termination of the Integer Optimizer.

All δ tolerances can be adjusted using suitable parameters — see Table 9.1.

Table 9.1: Tolerances for the mixed-integer optimizer.

Tolerance	Parameter name
δ_1	MSK_DPAR_MIO_TOL_ABS_RELAX_INT
δ_2	MSK_DPAR_MIO_TOL_ABS_GAP
δ_3	MSK_DPAR_MIO_TOL_REL_GAP
δ_4	MSK_DPAR_MIO_NEAR_TOL_ABS_GAP
δ_5	MSK_DPAR_MIO_NEAR_TOL_REL_GAP

In Table 9.2 some other parameters affecting the integer optimizer termination criterion are shown. Please note that if the effect of a parameter is delayed, the associated termination criterion is applied only after some time, specified by the MSK_DPAR_MIO_DISABLE_TERM_TIME parameter.

Table 9.2: Other parameters affecting the integer optimizer termination criterion.

Parameter name	De-	Explanation
	layed	
MSK_IPAR_MIO_MAX_NUM_BRANCHES	Yes	Maximum number of branches allowed.
MSK_IPAR_MIO_MAX_NUM_RELAXS	Yes	Maximum number of relaxations allowed.
MSK_IPAR_MIO_MAX_NUM_SOLUTIONS	Yes	Maximum number of feasible integer solutions
		allowed.

9.5 How to Speed Up the Solution Process

As mentioned previously, in many cases it is not possible to find an optimal solution to an integer optimization problem in a reasonable amount of time. Some suggestions to reduce the solution time are:

- Relax the termination criterion: In case the run time is not acceptable, the first thing to do is to relax the termination criterion see Section 9.3 for details.
- Specify a good initial solution: In many cases a good feasible solution is either known or easily computed using problem specific knowledge. If a good feasible solution is known, it is usually worthwhile to use this as a starting point for the integer optimizer.
- Improve the formulation: A mixed-integer optimization problem may be impossible to solve in one form and quite easy in another form. However, it is beyond the scope of this manual to discuss good formulations for mixed-integer problems. For discussions on this topic see for example [Wol98].

9.6 Understanding Solution Quality

To determine the quality of the solution one should check the following:

- The solution status key returned by MOSEK
- The *optimality gap*: A measure of how much the located solution can deviate from the optimal solution to the problem
- Feasibility. How much the solution violates the constraints of the problem

The *optimality gap* is a measure for how close the solution is to the optimal solution. The optimality gap is given by

 $\epsilon = |(\text{objective value of feasible solution}) - (\text{objective bound})|.$

The objective value of the solution is guarantied to be within ϵ of the optimal solution.

The optimality gap can be retrieved through the solution item $MSK_DINF_MIO_OBJ_ABS_GAP$. Often it is more meaningful to look at the optimality gap normalized with the magnitude of the solution. The relative optimality gap is available in $MSK_DINF_MIO_OBJ_REL_GAP$.

API REFERENCE

10.1 Command Reference

The Rmosek interface is composed by a small set of functions and structures.

- Function list
- Structures and data types list

10.1.1 Functions

- mosek
- mosek_version
- mosek_clean
- mosek_read
- mosek_write

r = mosek(prob, opts)

Solve an optimization problem using the MOSEK optimization library.

Parameters

- •[in] prob (problem) a struct describing the optimization problem.
- •[in] opts (options) the solver options

Return

•r (result) - a struct that contains the result of the optimization

```
ver = mosek_version()
```

Retrieves a string containing the version number of the utilized \mathbf{MOSEK} optimization library. Return

•ver (int) - The version number.

mosek_clean()

Forces the early release of any previously acquired **MOSEK** license. If you do not share a limited number of licenses among multiple users, you do not need to use this function. The acquisition of a new **MOSEK** license will automatically take place at the next call to the function <code>mosek</code> given a valid problem description, using a small amount of extra time.

For advanced users: If you utilize the .Call convention directly, i.e. bypassing the mosek R-function definition, an Rf_error will result in an unclean memory space. For this reason you can also use this function to tidy up uncleaned resources in case an error occurs. Otherwise this cleaning will not happen until the next call to mosek or until the library is unloaded. This usage have not been documented elsewhere.

out = mosek_read(filepath, opts = list())

Interprets a model from any standard modeling fileformat (e.g. lp, opf, mps, task, etc.), controlled by a set of options. The result contains an optimization problem which is compliant with the input specifications of function <code>mosek</code>.

Parameters

- •[in] filepath (string) A string describing the path to file, either absolute or relative to the working directory. The specified location will be the source of the optimization model to be read.
- •[in] opts (io_options) The options could have any name, and are, in fact, often input directly as an anonymous list.

Return

 \bullet out (result) – The resulting function output variable, returned by the interface, holds the response of the function call.

r = mosek_write(prob, filepath, opts)

Outputs a model of an optimization problem in a file format (see Section 11), controlled by a set of options. The modeling file format is selected based on the extension of the modelfile.

Parameters

- •[in] prob (problem) The input variable could have any name, but should be a list object describing the optimization problem using the same fields as for the mosek function.
- •[in] filepath (string) The input variable should be a string describing the path to modelfile. This path can either be absolute or relative to the working directory, and will overwrite any existing data on this location. The specified location will be the destination of the exported model.
- •[in] opts (io_options) The options could have any name, and are, in fact, often specified directly as an anonymous list.

Return

•r (result) - Function return information.

10.1.2 Structures and Data Types

rescode

The return code type. See Section 10.3.

problem

A list object describing the optimization problem using the following fields.

Fields

- •sense (string) Objective sense, e.g. "max" or "min"
- •c (numeric_vector) Objective coefficient array.
- •c0 (numeric) Objective constant.
- •A (matrix_sparse) Constraint sparse matrix.
- •bc (matrix) Lower and upper constraint bounds
- •bx (matrix) Lower and upper variable bounds
- •cones (matrix_list) Conic constraints
- •bardim (numeric_vector) Semidefinite variable dimensions
- •barc (list) Semidefinite objective coefficients
- •barA (list) Semidefinite constraint coefficients
- •intsub (numeric_vector) Integer variable indexes
- •qobj (list) [optional] Quadratic convex optimization

- •scopt (list) [optional] Separable convex optimization
- •iparam (list) Integer parameter list
- •dparam (list) Double parameter list
- •sparam (list) String parameter list
- •sol (solver_solutions) Initial solution struct

options

The options could have any name, and are, in fact, often input directly as an anonymous list. Fields

- •verbose (numeric) Output logging verbosity
- •usesol (bool) Whether to use the initial solution
- •useparam (bool) Whether to use the specified parameter settings
- •soldetail (numeric) Level of detail used to describe solutions
- •getinfo (bool) Whether to extract MOSEK information items
- •writebefore (string) Filepath used to export model
- •writeafter (string) Filepath used to export model and solution

solver_solutions

It contains informations about initial/final solutions.

Warning: Fields availability depends on the type of problem/algorithm.

Fields

- •itr (solution_info) Interior solution
- •bas (solution_info) Basic solution
- •int (solution_info) Integer solution

solution_info

Fields

- •solsta (string) Solution status
- •prosta (string) Problem status
- •skc (string_vector) Linear constraint status keys
- •skx (string_vector) Variable bound status keys
- •skn (string_vector) Conic constraint status keys (not in basic solution)
- •xc (numeric_vector) Constraint activities
- •xx (numeric_vector) Variable activities
- •barx (numeric_vector) Semidefinite variable activities (not in basic solution)
- •slc (numeric_vector) Dual variable for constraint lower bounds (not in integer solution)
- •suc (numeric_vector) Dual variable for constraint upper bounds (not in integer solution)
- •slx (numeric_vector) Dual variable for variable lower bounds (not in integer solution)
- •sux (numeric_vector) Dual variable for variable lower bounds (not in integer solution)
- •snx (numeric_vector) Dual variable of conic constraints (not in basic or integer solution)
- •bars (numeric_vector) Dual variable of semidefinite domains (not in basic or integer solution)

- •pobjval (numeric) Primal objective value (Only available if requested by option soldetail)
- •dobjval (numeric) Dual objective value (not fo integer solution)
- •pobjbound (numeric) Best primal objective bound from relaxations (only for integer solution)
- •maxinfeas (infeas_info) Maximal solution infeasibilities

infeas_info

It contains information about the maximal solution infeasibilty for several problem items.

Note: This struct is only available if the option soldetail is specified.

Fields

- •pbound (numeric) In primal inequality constraints
- •peq (numeric) In primal equality constraints
- •pcone (numeric) In primal cone constraints
- •dbound (numeric) In dual inequality constraints
- •deq (numeric) In dual equality constraints
- •dcone (numeric) In dual cone constraints
- •int (numeric) In integer variables

io_options

It is used to specify options for input/output operations.

Fields

- •verbose (numeric) Output logging verbosity
- •usesol (bool) Whether to write an initial solution
- •useparam (bool) Whether to write all parameter settings
- •getinfo (bool) Whether to extract MOSEK information items
- •scofile (string) Source of operators read to scopt
- •matrixformat (matrix_sparse) The sparse format of the constraint matrix (only used by mosek_read).

result

It contains results for most of the Rmosek functions.

Note: Some fields are available only for specific functions.

Fields

- •response (rescode) Response from the MOSEK optimization library.
- •code (numeric) ID-code of response
- •msg (string) Human-readable message
- •prob (problem) Problem description (only available in mosek_read)
- \bullet sol ($solution_info$) Available solutions (algorithm/problem dependent) (only available in mosek)
- •iinfo (numeric_list) Integer information list (Only available if requested by option getinfo).
- •dinfo (numeric_list) Double information list (Only available if requested by option getinfo).

10.2 Parameters

All parameters (alphabetical order)

- double parameters
- integer parameters
- string parameters

Parameters grouped by topic

Note: some parameters may appear in more than one group.

- Conic interior-point method
- Interior-point method
- ullet Mixed-integer optimization
- Overall solver
- Solution input/output
- Termination criterion
- Analysis
- Optimization system
- $\bullet \ \ Primal \ simplex \ optimizer$
- Output information
- Progress call-back
- Basis identification
- Presolve
- $\bullet \ \ Data \ input/output$
- Infeasibility report
- Simplex optimizer
- ullet Nonlinear convex method
- ullet Dual simplex optimizer
- License manager
- ullet Debugging
- \bullet Data check
- \bullet Logging

10.2.1 Parameters List (alphabetically)

Double Parameters

MSK_DPAR_ANA_SOL_INFEAS_TOL

If a constraint violates its bound with an amount larger than this value, the constraint name, index and violation will be printed by the solution analyzer.

Accepted Values: $[0.0 ; +\inf]$

Default Value: 1e-6

10.2. Parameters 63

Groups: Analysis

MSK_DPAR_BASIS_REL_TOL_S

Maximum relative dual bound violation allowed in an optimal basic solution.

Accepted Values: $[0.0 ; +\inf]$

Default Value: 1.0e-12

Groups: Simplex optimizer, Termination criterion

MSK_DPAR_BASIS_TOL_S

Maximum absolute dual bound violation in an optimal basic solution.

Accepted Values: [1.0e-9;+inf]

Default Value: 1.0e-6

Groups: Simplex optimizer, Termination criterion

MSK_DPAR_BASIS_TOL_X

Maximum absolute primal bound violation allowed in an optimal basic solution.

Accepted Values: $[1.0e-9;+\inf]$

Default Value: 1.0e-6

Groups: Simplex optimizer, Termination criterion

MSK_DPAR_CHECK_CONVEXITY_REL_TOL

This parameter controls when the full convexity check declares a problem to be non-convex. Increasing this tolerance relaxes the criteria for declaring the problem non-convex.

A problem is declared non-convex if negative (positive) pivot elements are detected in the Cholesky factor of a matrix which is required to be PSD (NSD). This parameter controls how much this non-negativity requirement may be violated.

If d_i is the pivot element for column i, then the matrix Q is considered to not be PSD if:

$$d_i \leq -|Q_{ii}|$$
 check convexity rel tol

Accepted Values: $[0;+\inf]$

Default Value: 1e-10

 ${\tt Groups:} \quad \textit{Interior-point method}$

MSK_DPAR_DATA_SYM_MAT_TOL

Absolute zero tolerance for elements in in suymmetric matrixes. If any value in a symmetric matrix is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Accepted Values: [1.0e-16;1.0e-6]

Default Value: 1.0e-12

Groups: Data check

MSK_DPAR_DATA_SYM_MAT_TOL_HUGE

An element in a symmetric matrix which is larger than this value in absolute size causes an error.

Accepted Values: $[0.0;+\inf]$

Default Value: 1.0e20

Groups: Data check

MSK_DPAR_DATA_SYM_MAT_TOL_LARGE

An element in a symmetric matrix which is larger than this value in absolute size causes a warning message to be printed.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e10

Groups: Data check

MSK_DPAR_DATA_TOL_AIJ

Absolute zero tolerance for elements in A. If any value A_{ij} is smaller than this parameter in absolute terms **MOSEK** will treat the values as zero and generate a warning.

Accepted Values: [1.0e-16;1.0e-6]

Default Value: 1.0e-12

Groups: Data check

MSK_DPAR_DATA_TOL_AIJ_HUGE

An element in A which is larger than this value in absolute size causes an error.

Accepted Values: $[0.0 ; +\inf]$

 ${\tt Default\ Value:} \qquad 1.0e20$

Groups: Data check

MSK_DPAR_DATA_TOL_AIJ_LARGE

An element in A which is larger than this value in absolute size causes a warning message to be printed.

Accepted Values: $[0.0 ; +\inf]$

Default Value: 1.0e10

Groups: Data check

MSK_DPAR_DATA_TOL_BOUND_INF

Any bound which in absolute value is greater than this parameter is considered infinite.

Accepted Values: $[0.0;+\inf]$

Default Value: 1.0e16

Groups: Data check

MSK_DPAR_DATA_TOL_BOUND_WRN

If a bound value is larger than this value in absolute size, then a warning message is issued.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e8

Groups: Data check

MSK_DPAR_DATA_TOL_CJ_LARGE

An element in c which is larger than this value in absolute terms causes a warning message to be printed.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e8

Groups: Data check

${\tt MSK_DPAR_DATA_TOL_C_HUGE}$

An element in c which is larger than the value of this parameter in absolute terms is considered to be huge and generates an error.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e16

Groups: Data check

10.2. Parameters 65

MSK_DPAR_DATA_TOL_QIJ

Absolute zero tolerance for elements in Q matrices.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e-16

Groups: Data check

MSK_DPAR_DATA_TOL_X

Zero tolerance for constraints and variables i.e. if the distance between the lower and upper bound is less than this value, then the lower and upper bound is considered identical.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e-8

Groups: Data check

MSK_DPAR_INTPNT_CO_TOL_DFEAS

Dual feasibility tolerance used by the conic interior-point optimizer.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion, Conic interior-point method

MSK_DPAR_INTPNT_CO_TOL_INFEAS

Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-10

Groups: Interior-point method, Termination criterion, Conic interior-point method

MSK_DPAR_INTPNT_CO_TOL_MU_RED

Relative complementarity gap feasibility tolerance used by the conic interior-point optimizer.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion, Conic interior-point method

MSK_DPAR_INTPNT_CO_TOL_NEAR_REL

If MOSEK cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Accepted Values: $[1.0; +\inf]$

Default Value: 1000

Groups: Interior-point method, Termination criterion, Conic interior-point method

MSK_DPAR_INTPNT_CO_TOL_PFEAS

Primal feasibility tolerance used by the conic interior-point optimizer.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion, Conic interior-point method

MSK_DPAR_INTPNT_CO_TOL_REL_GAP

Relative gap termination tolerance used by the conic interior-point optimizer.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-7

Groups: Interior-point method, Termination criterion, Conic interior-point method

MSK_DPAR_INTPNT_NL_MERIT_BAL

Controls if the complementarity and infeasibility is converging to zero at about equal rates.

Accepted Values: [0.0;0.99]

Default Value: 1.0e-4

Groups: Interior-point method, Nonlinear convex method

MSK_DPAR_INTPNT_NL_TOL_DFEAS

Dual feasibility tolerance used when a nonlinear model is solved.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion, Nonlinear convex method

MSK_DPAR_INTPNT_NL_TOL_MU_RED

Relative complementarity gap tolerance.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-12

Groups: Interior-point method, Termination criterion, Nonlinear convex method

MSK_DPAR_INTPNT_NL_TOL_NEAR_REL

If the MOSEK nonlinear interior-point optimizer cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Accepted Values: $[1.0; +\inf]$

Default Value: 1000.0

Groups: Interior-point method, Termination criterion, Nonlinear convex method

MSK_DPAR_INTPNT_NL_TOL_PFEAS

Primal feasibility tolerance used when a nonlinear model is solved.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion, Nonlinear convex method

MSK_DPAR_INTPNT_NL_TOL_REL_GAP

Relative gap termination tolerance for nonlinear problems.

Accepted Values: $[1.0e-14;+\inf]$

Default Value: 1.0e-6

 ${\tt Groups:} \quad \textit{Termination criterion, Interior-point method, Nonlinear convex method}$

MSK_DPAR_INTPNT_NL_TOL_REL_STEP

Relative step size to the boundary for general nonlinear optimization problems.

Accepted Values: [1.0e-4;0.9999999]

Default Value: 0.995

Groups: Interior-point method, Nonlinear convex method

MSK_DPAR_INTPNT_QO_TOL_DFEAS

Dual feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem..

Accepted Values: [0.0;1.0]

10.2. Parameters 67

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_QO_TOL_INFEAS

Controls when the conic interior-point optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible.

Accepted Values: [0.0;1.0]
Default Value: 1.0e-10

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_QO_TOL_MU_RED

Relative complementarity gap feasibility tolerance used when interior-point optimizer is applied to a quadratic optimization problem.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_QO_TOL_NEAR_REL

If MOSEK cannot compute a solution that has the prescribed accuracy, then it will multiply the termination tolerances with value of this parameter. If the solution then satisfies the termination criteria, then the solution is denoted near optimal, near feasible and so forth.

Accepted Values: $[1.0; +\inf]$

Default Value: 1000

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_QO_TOL_PFEAS

Primal feasibility tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Accepted Values: [0.0; 1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_QO_TOL_REL_GAP

Relative gap termination tolerance used when the interior-point optimizer is applied to a quadratic optimization problem.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

 ${\tt Groups:} \quad \textit{Interior-point method, Termination criterion}$

MSK_DPAR_INTPNT_TOL_DFEAS

Dual feasibility tolerance used for linear and quadratic optimization problems.

Accepted Values: [0.0;1.0]

Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_TOL_DSAFE

Controls the initial dual starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it might be worthwhile to increase this value.

Accepted Values: $[1.0e-4;+\inf]$

Default Value: 1.0

Groups: Interior-point method

MSK_DPAR_INTPNT_TOL_INFEAS

Controls when the optimizer declares the model primal or dual infeasible. A small number means the optimizer gets more conservative about declaring the model infeasible. A value of 0.0 means the optimizer must have an exact certificate of infeasibility and this is very unlikely to happen.

Accepted Values: [0.0;1.0] Default Value: 1.0e-10

Groups: Interior-point method, Termination criterion, Nonlinear convex method

MSK_DPAR_INTPNT_TOL_MU_RED

Relative complementarity gap tolerance.

Accepted Values: [0.0;1.0] Default Value: 1.0e-16

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_TOL_PATH

Controls how close the interior-point optimizer follows the central path. A large value of this parameter means the central is followed very closely. On numerical unstable problems it may be worthwhile to increase this parameter.

Accepted Values: [0.0; 0.9999]

Default Value: 1.0e-8

Groups: Interior-point method

MSK_DPAR_INTPNT_TOL_PFEAS

Primal feasibility tolerance used for linear and quadratic optimization problems.

Accepted Values: [0.0;1.0] Default Value: 1.0e-8

Groups: Interior-point method, Termination criterion

MSK_DPAR_INTPNT_TOL_PSAFE

Controls the initial primal starting point used by the interior-point optimizer. If the interior-point optimizer converges slowly and/or the constraint or variable bounds are very large, then it may be worthwhile to increase this value.

Accepted Values: $[1.0e-4;+\inf]$

Default Value: 1.0

Groups: Interior-point method

MSK_DPAR_INTPNT_TOL_REL_GAP

Relative gap termination tolerance.

Accepted Values: $[1.0e-14;+\inf]$

Default Value: 1.0e-8

 ${\tt Groups:} \quad \textit{Termination criterion, Interior-point method}$

MSK_DPAR_INTPNT_TOL_REL_STEP

Relative step size to the boundary for linear and quadratic optimization problems.

Accepted Values: [1.0e-4; 0.999999]

Default Value: 0.9999

Groups: Interior-point method

MSK_DPAR_INTPNT_TOL_STEP_SIZE

If the step size falls below the value of this parameter, then the interior-point optimizer assumes that it is stalled. In other words the interior-point optimizer does not make any progress and therefore it is better stop.

Accepted Values: [0.0 ; 1.0]

Groups: Interior-point method

1.0e-6

MSK_DPAR_LOWER_OBJ_CUT

Default Value:

If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [$MSK_DPAR_LOWER_OBJ_CUT$, $MSK_DPAR_UPPER_OBJ_CUT$], then \mathbf{MOSEK} is terminated.

Accepted Values: $[-\inf; +\inf]$

Default Value: -1.0e30

Groups: Termination criterion

MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH

If the lower objective cut is less than the value of this parameter value, then the lower objective cut i.e. $MSK_DPAR_LOWER_OBJ_CUT$ is treated as $-\infty$.

Accepted Values: [-inf;+inf]

Default Value: -0.5e30

Groups: Termination criterion

MSK_DPAR_MIO_DISABLE_TERM_TIME

This parameter specifies the number of seconds n during which the termination criteria governed by

- •MSK_IPAR_MIO_MAX_NUM_RELAXS
- $\bullet \textit{MSK_IPAR_MIO_MAX_NUM_BRANCHES}$
- MSK_DPAR_MIO_NEAR_TOL_ABS_GAP
- •MSK_DPAR_MIO_NEAR_TOL_REL_GAP

is disabled since the beginning of the optimization.

A negative value is identical to infinity i.e. the termination criteria are never checked.

Accepted Values: [-inf;+inf]

Default Value: -1.0

Groups: Mixed-integer optimization, Termination criterion

MSK_DPAR_MIO_MAX_TIME

This parameter limits the maximum time spent by the mixed-integer optimizer. A negative number means infinity.

Accepted Values: [-inf;+inf]

 ${\tt Default\ Value:} \quad {\tt -1.0}$

Groups: Mixed-integer optimization, Termination criterion

MSK_DPAR_MIO_NEAR_TOL_ABS_GAP

Relaxed absolute optimality tolerance employed by the mixed-integer optimizer. This termination criteria is delayed. See $MSK_DPAR_MIO_DISABLE_TERM_TIME$ for details.

Accepted Values: $[0.0; +\inf]$

 ${\tt Default\ Value:} \quad 0.0$

Groups: Mixed-integer optimization

MSK_DPAR_MIO_NEAR_TOL_REL_GAP

The mixed-integer optimizer is terminated when this tolerance is satisfied. This termination criteria is delayed. See $MSK_DPAR_MIO_DISABLE_TERM_TIME$ for details.

Accepted Values: $[0.0 ; +\inf]$

Default Value: 1.0e-3

Groups: Mixed-integer optimization, Termination criterion

MSK_DPAR_MIO_REL_GAP_CONST

This value is used to compute the relative gap for the solution to an integer optimization problem.

Accepted Values: [1.0e-15;+inf]

Default Value: 1.0e-10

Groups: Mixed-integer optimization, Termination criterion

MSK_DPAR_MIO_TOL_ABS_GAP

Absolute optimality tolerance employed by the mixed-integer optimizer.

Accepted Values: $[0.0; +\inf]$

Default Value: 0.0

Groups: Mixed-integer optimization

MSK_DPAR_MIO_TOL_ABS_RELAX_INT

Absolute relaxation tolerance of the integer constraints. I.e. $\min(|x| - \lfloor x \rfloor, \lceil x \rceil - |x|)$ is less than the tolerance then the integer restrictions assumed to be satisfied.

Accepted Values: [1e-9;+inf]

Default Value: 1.0e-5

Groups: Mixed-integer optimization

MSK_DPAR_MIO_TOL_FEAS

Feasibility tolerance for mixed integer solver.

Accepted Values: [1e-9;1e-3]

Default Value: 1.0e-6

Groups: Mixed-integer optimization

MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT

If the relative improvement of the dual bound is smaller than this value, the solver will terminate the root cut generation. A value of 0.0 means that the value is selected automatically.

Accepted Values: [0.0;1.0]

Default Value: 0.0

 ${\tt Groups:} \quad \textit{Mixed-integer optimization}$

MSK_DPAR_MIO_TOL_REL_GAP

Relative optimality tolerance employed by the mixed-integer optimizer.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e-4

Groups: Mixed-integer optimization, Termination criterion

MSK_DPAR_OPTIMIZER_MAX_TIME

Maximum amount of time the optimizer is allowed to spent on the optimization. A negative number means infinity.

Accepted Values: [-inf;+inf]

Default Value: -1.0

Groups: Termination criterion

MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP

Absolute tolerance employed by the linear dependency checker.

Accepted Values: $[0.0 ; +\inf]$

Default Value: 1.0e-6

Groups: Presolve

MSK_DPAR_PRESOLVE_TOL_AIJ

Absolute zero tolerance employed for a_{ij} in the presolve.

Accepted Values: $[1.0e-15;+\inf]$

Default Value: 1.0e-12

 ${\tt Groups:} \quad \textit{Presolve}$

MSK_DPAR_PRESOLVE_TOL_REL_LINDEP

Relative tolerance employed by the linear dependency checker.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e-10

 ${\tt Groups:} \quad \textit{Presolve}$

MSK_DPAR_PRESOLVE_TOL_S

Absolute zero tolerance employed for s_i in the presolve.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e-8

Groups: Presolve

MSK_DPAR_PRESOLVE_TOL_X

Absolute zero tolerance employed for x_i in the presolve.

Accepted Values: $[0.0; +\inf]$

Default Value: 1.0e-8

 ${\tt Groups:} \quad \textit{Presolve}$

MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL

This parameter determines when columns are dropped in incomplete Cholesky factorization during reformulation of quadratic problems.

Accepted Values: $[0;+\inf]$

Default Value: 1e-15

Groups: Interior-point method

MSK_DPAR_SEMIDEFINITE_TOL_APPROX

Tolerance to define a matrix to be positive semidefinite.

Accepted Values: $[1.0e-15;+\inf]$

Default Value: 1.0e-10

Groups: Data check

MSK_DPAR_SIMPLEX_ABS_TOL_PIV

Absolute pivot tolerance employed by the simplex optimizers.

Accepted Values: $[1.0e-12 ; +\inf]$

Default Value: 1.0e-7

Groups: Simplex optimizer

MSK_DPAR_SIM_LU_TOL_REL_PIV

Relative pivot tolerance employed when computing the LU factorization of the basis in the simplex optimizers and in the basis identification procedure.

A value closer to 1.0 generally improves numerical stability but typically also implies an increase in the computational work.

Accepted Values: [1.0e-6;0.999999]

Default Value: 0.01

Groups: Basis identification, Simplex optimizer

MSK_DPAR_UPPER_OBJ_CUT

If either a primal or dual feasible solution is found proving that the optimal objective value is outside, the interval [$MSK_DPAR_LOWER_OBJ_CUT$, $MSK_DPAR_UPPER_OBJ_CUT$], then \mathbf{MOSEK} is terminated.

Accepted Values: [-inf;+inf]

Default Value: 1.0e30

Groups: Termination criterion

MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH

If the upper objective cut is greater than the value of this parameter, then the upper objective cut $MSK_DPAR_UPPER_OBJ_CUT$ is treated as ∞ .

Accepted Values: $[-\inf; +\inf]$

Default Value: 0.5e30

Groups: Termination criterion

Integer Parameters

MSK_IPAR_ANA_SOL_BASIS

Controls whether the basis matrix is analyzed in solution analyzer.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

 ${\tt Groups:} \quad \textit{Analysis}$

MSK_IPAR_ANA_SOL_PRINT_VIOLATED

Controls whether a list of violated constraints is printed.

All constraints violated by more than the value set by the parameter MSK_DPAR_ANA_SOL_INFEAS_TOL will be printed.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Analysis

MSK_IPAR_AUTO_SORT_A_BEFORE_OPT

Controls whether the elements in each column of A are sorted before an optimization is performed. This is not required but makes the optimization more deterministic.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Debugging

MSK_IPAR_AUTO_UPDATE_SOL_INFO

Controls whether the solution information items are automatically updated after an optimization is performed.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Optimization system

MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE

If a slack variable is in the basis, then the corresponding column in the basis is a unit vector with -1 in the right position. However, if this parameter is set to MSK_ON , -1 is replaced by 1.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Simplex optimizer

MSK_IPAR_BI_CLEAN_OPTIMIZER

Controls which simplex optimizer is used in the clean-up phase.

Accepted Values: MSKoptimizertypee

Default Value: MSK_OPTIMIZER_FREE

Groups: Basis identification, Overall solver

MSK_IPAR_BI_IGNORE_MAX_ITER

If the parameter $MSK_IPAR_INTPNT_BASIS$ has the value $MSK_BI_NO_ERROR$ and the interior-point optimizer has terminated due to maximum number of iterations, then basis identification is performed if this parameter has the value MSK_ON .

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Interior-point method, Basis identification

MSK_IPAR_BI_IGNORE_NUM_ERROR

If the parameter $MSK_IPAR_INTPNT_BASIS$ has the value $MSK_BI_NO_ERROR$ and the interior-point optimizer has terminated due to a numerical problem, then basis identification is performed if this parameter has the value MSK_ON .

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

 ${\tt Groups:} \quad \textit{Interior-point method, Basis identification}$

MSK_IPAR_BI_MAX_ITERATIONS

Controls the maximum number of simplex iterations allowed to optimize a basis after the basis identification.

Accepted Values: $[0 ; +\inf]$ Default Value: 1000000

Groups: Basis identification, Termination criterion

MSK_IPAR_CACHE_LICENSE

Specifies if the license is kept checked out for the lifetime of the mosek environment (MSK_-ON) or returned to the server immediately after the optimization (MSK_-OFF) .

By default the license is checked out for the lifetime of the \mathbf{MOSEK} environment by the first call to the optimizer.

Check-in and check-out of licenses have an overhead. Frequent communication with the license server should be avoided.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON
Groups: License manager

MSK_IPAR_CHECK_CONVEXITY

Specify the level of convexity check on quadratic problems

Accepted Values: MSKcheckconvexitytypee
Default Value: MSK_CHECK_CONVEXITY_FULL
Groups: Data check, Nonlinear convex method

MSK_IPAR_COMPRESS_STATFILE

Control compression of stat files.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

MSK_IPAR_INFEAS_GENERIC_NAMES

Controls whether generic names are used when an infeasible subproblem is created.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Infeasibility report

MSK_IPAR_INFEAS_PREFER_PRIMAL

If both certificates of primal and dual infeasibility are supplied then only the primal is used when this option is turned on.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON
Groups: Overall solver

MSK_IPAR_INFEAS_REPORT_AUTO

Controls whether an infeasibility report is automatically produced after the optimization if the problem is primal or dual infeasible.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

 ${\tt Groups:} \quad \textit{Data input/output, Solution input/output}$

MSK_IPAR_INFEAS_REPORT_LEVEL

Controls the amount of information presented in an infeasibility report. Higher values imply more information.

Accepted Values: $[0;+\inf]$

Default Value: 1

 ${\tt Groups:} \quad \textit{Infeasibility report, Output information}$

MSK_IPAR_INTPNT_BASIS

Controls whether the interior-point optimizer also computes an optimal basis.

Accepted Values: MSKbasindtypee
Default Value: MSK_BI_ALWAYS

Groups: Interior-point method, Basis identification

MSK_IPAR_INTPNT_DIFF_STEP

Controls whether different step sizes are allowed in the primal and dual space.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Interior-point method

MSK_IPAR_INTPNT_HOTSTART

Currently not in use.

Accepted Values: MSKintpnthotstarte

Default Value: MSK_INTPNT_HOTSTART_NONE

Groups: Interior-point method

MSK_IPAR_INTPNT_MAX_ITERATIONS

Controls the maximum number of iterations allowed in the interior-point optimizer.

Accepted Values: $[0;+\inf]$

Default Value: 400

Groups: Interior-point method, Termination criterion

MSK_IPAR_INTPNT_MAX_NUM_COR

Controls the maximum number of correctors allowed by the multiple corrector procedure. A negative value means that **MOSEK** is making the choice.

Accepted Values: $[-1;+\inf]$

Default Value: -1

Groups: Interior-point method

MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS

Maximum number of steps to be used by the iterative refinement of the search direction. A negative value implies that the optimizer chooses the maximum number of iterative refinement steps.

Accepted Values: [-inf;+inf]

Default Value: -1

Groups: Interior-point method

MSK_IPAR_INTPNT_MULTI_THREAD

Controls whether the interior-point optimizers are allowed to employ multiple threads if more threads is available.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Optimization system

MSK_IPAR_INTPNT_OFF_COL_TRH

Controls how many offending columns are detected in the Jacobian of the constraint matrix.

0	no detection
1	aggressive detection
> 1	higher values mean less aggressive detection

Accepted Values: $[0;+\inf]$

Default Value: 40

 ${\tt Groups:} \quad \textit{Interior-point method}$

MSK_IPAR_INTPNT_ORDER_METHOD

Controls the ordering strategy used by the interior-point optimizer when factorizing the Newton equation system.

Accepted Values: MSKorderingtypee

Default Value: MSK_ORDER_METHOD_FREE

Groups: Interior-point method

MSK_IPAR_INTPNT_REGULARIZATION_USE

Controls whether regularization is allowed.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Interior-point method

MSK_IPAR_INTPNT_SCALING

Controls how the problem is scaled before the interior-point optimizer is used.

Accepted Values: MSKscalingtypee
Default Value: MSK_SCALING_FREE

Groups: Interior-point method

MSK_IPAR_INTPNT_SOLVE_FORM

Controls whether the primal or the dual problem is solved.

Accepted Values: MSKsolveforme

Default Value: MSK_SOLVE_FREE

Groups: Interior-point method

MSK_IPAR_INTPNT_STARTING_POINT

Starting point used by the interior-point optimizer.

Accepted Values: MSKstartpointtypee

Default Value: MSK_STARTING_POINT_FREE

Groups: Interior-point method

MSK_IPAR_LICENSE_DEBUG

This option is used to turn on debugging of the license manager.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: License manager

MSK_IPAR_LICENSE_PAUSE_TIME

If $MSK_IPAR_LICENSE_WAIT = MSK_ON$ and no license is available, then \mathbf{MOSEK} sleeps a number of milliseconds between each check of whether a license has become free.

Accepted Values: [0;1000000]

Default Value: 100

Groups: License manager

MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS

Controls whether license features expire warnings are suppressed.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: License manager, Output information

MSK_IPAR_LICENSE_TRH_EXPIRY_WRN

If a license feature expires in a numbers days less than the value of this parameter then a warning will be issued.

Accepted Values: $[0;+\inf]$

Default Value: 7

MSK_IPAR_LICENSE_WAIT

If all licenses are in use **MOSEK** returns with an error code. However, by turning on this parameter **MOSEK** will wait for an available license.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Overall solver, Optimization system, License manager

MSK IPAR LOG

Controls the amount of log information. The value 0 implies that all log information is suppressed. A higher level implies that more information is logged.

Please note that if a task is employed to solve a sequence of optimization problems the value of this parameter is reduced by the value of $MSK_IPAR_LOG_CUT_SECOND_OPT$ for the second and any subsequent optimizations.

Accepted Values: $[0;+\inf]$

Default Value: 10

Groups: Output information, Logging

MSK_IPAR_LOG_ANA_PRO

Controls amount of output from the problem analyzer.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Analysis, Logging

MSK_IPAR_LOG_BI

Controls the amount of output printed by the basis identification procedure. A higher level implies that more information is logged.

Accepted Values: $[0;+\inf]$

Default Value: 4

Groups: Basis identification, Output information, Logging

MSK_IPAR_LOG_BI_FREQ

Controls how frequent the optimizer outputs information about the basis identification and how frequent the user-defined call-back function is called.

Accepted Values: $[0;+\inf]$

Default Value: 2500

Groups: Basis identification, Output information, Logging

MSK IPAR LOG CHECK CONVEXITY

Controls logging in convexity check on quadratic problems. Set to a positive value to turn logging on. If a quadratic coefficient matrix is found to violate the requirement of PSD (NSD) then a list of negative (positive) pivot elements is printed. The absolute value of the pivot elements is also shown.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Data check, Nonlinear convex method

MSK_IPAR_LOG_CUT_SECOND_OPT

If a task is employed to solve a sequence of optimization problems, then the value of the log levels is reduced by the value of this parameter. E.g MSK_IPAR_LOG and $MSK_IPAR_LOG_SIM$ are reduced by the value of this parameter for the second and any subsequent optimizations.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Output information, Logging

MSK_IPAR_LOG_EXPAND

Controls the amount of logging when a data item such as the maximum number constrains is expanded.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Output information, Logging

MSK_IPAR_LOG_FACTOR

If turned on, then the factor log lines are added to the log.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Output information, Logging

MSK_IPAR_LOG_FEAS_REPAIR

Controls the amount of output printed when performing feasibility repair. A value higher than one means extensive logging.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Output information, Logging

MSK_IPAR_LOG_FILE

If turned on, then some log info is printed when a file is written or read.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Data input/output, Output information, Logging

MSK_IPAR_LOG_HEAD

If turned on, then a header line is added to the log.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Output information, Logging

MSK_IPAR_LOG_INFEAS_ANA

Controls amount of output printed by the infeasibility analyzer procedures. A higher level implies that more information is logged.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Infeasibility report, Output information, Logging

MSK_IPAR_LOG_INTPNT

Controls amount of output printed by the interior-point optimizer. A higher level implies that more information is logged.

Accepted Values: $[0;+\inf]$

Default Value: 4

Groups: Interior-point method, Output information, Logging

MSK_IPAR_LOG_MIO

Controls the log level for the mixed-integer optimizer. A higher level implies that more information is logged.

Accepted Values: $[0;+\inf]$

Default Value: 4

Groups: Mixed-integer optimization, Output information, Logging

MSK_IPAR_LOG_MIO_FREQ

Controls how frequent the mixed-integer optimizer prints the log line. It will print line every time $MSK_IPAR_LOG_MIO_FREQ$ relaxations have been solved.

Accepted Values: [-inf;+inf]

Default Value: 10

Groups: Mixed-integer optimization, Output information, Logging

MSK_IPAR_LOG_OPTIMIZER

Controls the amount of general optimizer information that is logged.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Output information, Logging

MSK_IPAR_LOG_ORDER

If turned on, then factor lines are added to the log.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Output information, Logging

MSK_IPAR_LOG_PRESOLVE

Controls amount of output printed by the presolve procedure. A higher level implies that more information is logged.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Interior-point method, Logging

MSK_IPAR_LOG_RESPONSE

Controls amount of output printed when response codes are reported. A higher level implies that more information is logged.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Output information, Logging

MSK_IPAR_LOG_SENSITIVITY

Controls the amount of logging during the sensitivity analysis.

0.Means no logging information is produced.

1. Timing information is printed.

2. Sensitivity results are printed.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Output information, Logging

MSK_IPAR_LOG_SENSITIVITY_OPT

Controls the amount of logging from the optimizers employed during the sensitivity analysis. 0 means no logging information is produced.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Output information, Logging

MSK_IPAR_LOG_SIM

Controls amount of output printed by the simplex optimizer. A higher level implies that more information is logged.

Accepted Values: $[0;+\inf]$

Default Value: 4

Groups: Simplex optimizer, Output information, Logging

MSK_IPAR_LOG_SIM_FREQ

Controls how frequent the simplex optimizer outputs information about the optimization and how frequent the user-defined call-back function is called.

Accepted Values: $[0;+\inf]$

Default Value: 1000

Groups: Simplex optimizer, Output information, Logging

MSK_IPAR_LOG_SIM_MINOR

Currently not in use.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Simplex optimizer, Output information

MSK_IPAR_LOG_STORAGE

When turned on, MOSEK prints messages regarding the storage usage and allocation.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Output information, Optimization system, Logging

MSK_IPAR_MAX_NUM_WARNINGS

Each warning is shown a limit number times controlled by this parameter. A negative value is identical to infinite number of times.

Accepted Values: [-inf;+inf]

Default Value: 10

Groups: Output information

MSK_IPAR_MIO_BRANCH_DIR

Controls whether the mixed-integer optimizer is branching up or down by default.

Accepted Values: MSKbranchdire

Default Value: MSK_BRANCH_DIR_FREE

Groups: Mixed-integer optimization

MSK_IPAR_MIO_CONSTRUCT_SOL

If set to MSK_ON and all integer variables have been given a value for which a feasible mixed integer solution exists, then MOSEK generates an initial solution to the mixed integer problem by fixing all integer values and solving the remaining problem.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Mixed-integer optimization

MSK_IPAR_MIO_CUT_CLIQUE

Controls whether clique cuts should be generated.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Mixed-integer optimization

MSK_IPAR_MIO_CUT_CMIR

Controls whether mixed integer rounding cuts should be generated.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Mixed-integer optimization

MSK_IPAR_MIO_CUT_GMI

Controls whether GMI cuts should be generated.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Mixed-integer optimization

MSK_IPAR_MIO_CUT_IMPLIED_BOUND

Controls whether implied bound cuts should be generated.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Mixed-integer optimization

MSK_IPAR_MIO_CUT_KNAPSACK_COVER

Controls whether knapsack cover cuts should be generated.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Mixed-integer optimization

MSK_IPAR_MIO_CUT_SELECTION_LEVEL

Controls how aggressively generated cuts are selected to be included in the relaxation.

-1. The optimizer chooses the level of cut selection

0.Generated cuts less likely to be added to the relaxation

1.Cuts are more aggressively selected to be included in the relaxation

Accepted Values: [-1;+1]

Default Value: -1

 ${\tt Groups:} \quad \textit{Mixed-integer optimization}$

MSK_IPAR_MIO_HEURISTIC_LEVEL

Controls the heuristic employed by the mixed-integer optimizer to locate an initial good integer feasible solution. A value of zero means the heuristic is not used at all. A larger value than 0 means that a gradually more sophisticated heuristic is used which is computationally more expensive. A negative value implies that the optimizer chooses the heuristic. Normally a value around 3 to 5 should be optimal.

Accepted Values: $[-\inf; +\inf]$

Default Value: -1

Groups: Mixed-integer optimization

MSK_IPAR_MIO_MAX_NUM_BRANCHES

Maximum number of branches allowed during the branch and bound search. A negative value means infinite.

Accepted Values: [-inf;+inf]

Default Value: -1

Groups: Mixed-integer optimization, Termination criterion

MSK_IPAR_MIO_MAX_NUM_RELAXS

Maximum number of relaxations allowed during the branch and bound search. A negative value means infinite.

Accepted Values: $[-\inf; +\inf]$

Default Value: -1

Groups: Mixed-integer optimization

MSK_IPAR_MIO_MAX_NUM_SOLUTIONS

The mixed-integer optimizer can be terminated after a certain number of different feasible solutions has been located. If this parameter has the value n > 0, then the mixed-integer optimizer will be terminated when n feasible solutions have been located.

Accepted Values: [-inf;+inf]

Default Value: -1

Groups: Mixed-integer optimization, Termination criterion

MSK_IPAR_MIO_MODE

Controls whether the optimizer includes the integer restrictions when solving a (mixed) integer optimization problem.

Accepted Values: MSKmiomodee

Default Value: MSK_MIO_MODE_SATISFIED

Groups: Overall solver

MSK_IPAR_MIO_MT_USER_CB

It true user callbacks are called from each thread used by this optimizer. If false the user callback is only called from a single thread.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Crowns: Ontimination system

Groups: Optimization system

MSK_IPAR_MIO_NODE_OPTIMIZER

Controls which optimizer is employed at the non-root nodes in the mixed-integer optimizer.

Accepted Values: MSKoptimizertypee
Default Value: MSK_OPTIMIZER_FREE

 ${\tt Groups:} \quad \textit{Mixed-integer optimization}$

MSK_IPAR_MIO_NODE_SELECTION

Controls the node selection strategy employed by the mixed-integer optimizer.

Accepted Values: MSKmionodeseltypee

Default Value: MSK_MIO_NODE_SELECTION_FREE

Groups: Mixed-integer optimization

MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE

Enables or disables perspective reformulation in presolve.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Mixed-integer optimization

MSK_IPAR_MIO_PROBING_LEVEL

Controls the amount of probing employed by the mixed-integer optimizer in presolve.

- -1. The optimizer chooses the level of probing employed
 - 0. Probing is disabled
 - 1.A low amount of probing is employed
 - 2.A medium amount of probing is employed
 - 3.A high amount of probing is employed

Accepted Values: $[-\inf; +\inf]$

Default Value: -1

Groups: Mixed-integer optimization

MSK_IPAR_MIO_RINS_MAX_NODES

Controls the maximum number of nodes allowed in each call to the RINS heuristic. The default value of -1 means that the value is determined automatically. A value of zero turns off the heuristic.

Accepted Values: $[-1;+\inf]$

Default Value: -1

Groups: Mixed-integer optimization

MSK_IPAR_MIO_ROOT_OPTIMIZER

Controls which optimizer is employed at the root node in the mixed-integer optimizer.

Accepted Values: MSKoptimizertypee
Default Value: MSK_OPTIMIZER_FREE

Groups: Mixed-integer optimization

MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL

Controls whether presolve can be repeated at root node.

- •-1 The optimizer chooses whether presolve is repeated
- •0 Never repeat presolve
- •1 Always repeat presolve

Accepted Values: [-1;1]

Default Value: -1

 ${\tt Groups:} \quad \textit{Mixed-integer optimization}$

MSK_IPAR_MIO_VB_DETECTION_LEVEL

Controls how much effort is put into detecting variable bounds.

- -1. The optimizer chooses
 - 0.No variable bounds are detected
 - 1. Only detect variable bounds that are directly represented in the problem
 - 2.Detect variable bounds in probing

Accepted Values: [-1;+2]

Default Value: -1

 ${\tt Groups:} \quad \textit{Mixed-integer optimization}$

MSK_IPAR_MT_SPINCOUNT

Set the number of iterations to spin before sleeping.

Accepted Values: [0;1000000000]

Default Value: 0

Groups: Optimization system

MSK_IPAR_NUM_THREADS

Controls the number of threads employed by the optimizer. If set to 0 the number of threads used will be equal to the number of cores detected on the machine.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Optimization system

MSK_IPAR_OPF_MAX_TERMS_PER_LINE

The maximum number of terms (linear and quadratic) per line when an OPF file is written.

Accepted Values: $[0;+\inf]$

Default Value: 5

Groups: Data input/output

MSK_IPAR_OPF_WRITE_HEADER

Write a text header with date and MOSEK version in an OPF file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_OPF_WRITE_HINTS

Write a hint section with problem dimensions in the beginning of an OPF file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON
Groups: Data input/output

MSK_IPAR_OPF_WRITE_PARAMETERS

Write a parameter section in an OPF file.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_OPF_WRITE_PROBLEM

Write objective, constraints, bounds etc. to an OPF file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_OPF_WRITE_SOLUTIONS

Enable inclusion of solutions in the OPF files.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_OPF_WRITE_SOL_BAS

If $MSK_IPAR_OPF_WRITE_SOLUTIONS$ is MSK_ON and a basic solution is defined, include the basic solution in OPF files.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_OPF_WRITE_SOL_ITG

If $MSK_IPAR_OPF_WRITE_SOLUTIONS$ is MSK_ON and an integer solution is defined, write the integer solution in OPF files.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_OPF_WRITE_SOL_ITR

If $MSK_IPAR_OPF_WRITE_SOLUTIONS$ is MSK_ON and an interior solution is defined, write the interior solution in OPF files.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_OPTIMIZER

The parameter controls which optimizer is used to optimize the task.

Accepted Values: MSKoptimizertypee
Default Value: MSK_OPTIMIZER_FREE

Groups: Overall solver

MSK_IPAR_PARAM_READ_CASE_NAME

If turned on, then names in the parameter file are case sensitive.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_PARAM_READ_IGN_ERROR

If turned on, then errors in parameter settings is ignored.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Data input/output

MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL

Controls the maximum amount of fill-in that can be created by one pivot in the elimination phase of the presolve. A negative value menas the parameter value is selected automatically.

Accepted Values: [-inf;+inf]

Default Value: Groups: Presolve

MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES

Control the maximum number of times the eliminator is tried.

Accepted Values: [-inf;+inf]

Default Value: -1

 ${\tt Groups:} \quad \textit{Presolve}$

MSK_IPAR_PRESOLVE_LEVEL

Currently not used.

Accepted Values: [-inf;+inf]

Default Value: -1

Groups: Overall solver, Presolve

MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH

The linear dependency check is potentially computationally expensive.

Accepted Values: [-inf;+inf]

Default Value: 100

Groups: Presolve

MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH

The linear dependency check is potentially computationally expensive.

Accepted Values: [-inf;+inf]

Default Value: 100

Groups: Presolve

MSK_IPAR_PRESOLVE_LINDEP_USE

Controls whether the linear constraints are checked for linear dependencies.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Presolve

MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS

Controls the maximum number of reductions performed by the presolve. The value of the parameter is normally only changed in connection with debugging. A negative value implies that an infinite number of reductions are allowed.

Accepted Values: $[-\inf; +\inf]$

Default Value: -1

MSK IPAR PRESOLVE USE

Controls whether the presolve is applied to a problem before it is optimized.

Accepted Values: MSKpresolvemodee

Default Value: MSK_PRESOLVE_MODE_FREE

Groups: Overall solver, Presolve

MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER

Controls which optimizer that is used to find the optimal repair.

Accepted Values: MSKoptimizertypee
Default Value: MSK_OPTIMIZER_FREE

Groups: Overall solver

MSK_IPAR_READ_DATA_COMPRESSED

If this option is turned on, it is assumed that the data file is compressed.

Accepted Values: MSKcompresstypee

Default Value: MSK_COMPRESS_FREE

 ${\tt Groups:} \quad \textit{Data input/output}$

MSK_IPAR_READ_DATA_FORMAT

Format of the data file to be read.

Accepted Values: MSKdataformate

Default Value: MSK_DATA_FORMAT_EXTENSION

Groups: Data input/output

MSK_IPAR_READ_DEBUG

Turns on additional debugging information when reading files.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_READ_KEEP_FREE_CON

Controls whether the free constraints are included in the problem.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Data input/output

MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU

If this option is turned on, **MOSEK** will drop variables that are defined for the first time in the bounds section.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_READ_LP_QUOTED_NAMES

If a name is in quotes when reading an LP file, the quotes will be removed.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_READ_MPS_FORMAT

Controls how strictly the MPS file reader interprets the MPS format.

Accepted Values: MSKmpsformate

Default Value: MSK_MPS_FORMAT_FREE

Groups: Data input/output

MSK_IPAR_READ_MPS_WIDTH

Controls the maximal number of characters allowed in one line of the MPS file.

Accepted Values: $[80;+\inf]$

Default Value: 1024

Groups: Data input/output

MSK_IPAR_READ_TASK_IGNORE_PARAM

Controls whether **MOSEK** should ignore the parameter setting defined in the task file and use the default parameter setting instead.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_SENSITIVITY_ALL

Not applicable.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Overall solver

MSK_IPAR_SENSITIVITY_OPTIMIZER

Controls which optimizer is used for optimal partition sensitivity analysis.

Accepted Values: MSKoptimizertypee

Default Value: MSK_OPTIMIZER_FREE_SIMPLEX

Groups: Overall solver, Simplex optimizer

MSK_IPAR_SENSITIVITY_TYPE

Controls which type of sensitivity analysis is to be performed.

Accepted Values: MSKsensitivitytypee

Default Value: MSK_SENSITIVITY_TYPE_BASIS

Groups: Overall solver

MSK_IPAR_SIM_BASIS_FACTOR_USE

Controls whether a (LU) factorization of the basis is used in a hot-start. Forcing a refactorization sometimes improves the stability of the simplex optimizers, but in most cases there is a performance penalty.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON
Groups: Simplex optimizer

MSK_IPAR_SIM_DEGEN

Controls how aggressively degeneration is handled.

Accepted Values: MSKsimdegene

Default Value: MSK_SIM_DEGEN_FREE

Groups: Simplex optimizer

MSK_IPAR_SIM_DUAL_CRASH

Controls whether crashing is performed in the dual simplex optimizer.

If this parameter is set to x, then a crash will be performed if a basis consists of more than (100-x) mod f_v entries, where f_v is the number of fixed variables.

Accepted Values: $[0;+\inf]$

Default Value: 90

Groups: Dual simplex optimizer

MSK_IPAR_SIM_DUAL_PHASEONE_METHOD

An experimental feature.

Accepted Values: [0;10]

Default Value: 0

Groups: Simplex optimizer

MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION

The dual simplex optimizer can use a so-called restricted selection/pricing strategy to chooses the outgoing variable. Hence, if restricted selection is applied, then the dual simplex optimizer first choose a subset of all the potential outgoing variables. Next, for some time it will choose the outgoing variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Accepted Values: [0;100]

Default Value: 50

Groups: Dual simplex optimizer

MSK_IPAR_SIM_DUAL_SELECTION

Controls the choice of the incoming variable, known as the selection strategy, in the dual simplex optimizer.

Accepted Values: MSKsimseltypee

Default Value: MSK_SIM_SELECTION_FREE

Groups: Dual simplex optimizer

MSK_IPAR_SIM_EXPLOIT_DUPVEC

Controls if the simplex optimizers are allowed to exploit duplicated columns.

Accepted Values: MSKsimdupvece

Default Value: MSK_SIM_EXPLOIT_DUPVEC_OFF

 ${\tt Groups:} \quad \textit{Simplex optimizer} \\$

MSK_IPAR_SIM_HOTSTART

Controls the type of hot-start that the simplex optimizer perform.

Accepted Values: MSKsimhotstarte

Default Value: MSK_SIM_HOTSTART_FREE

Groups: Simplex optimizer

MSK_IPAR_SIM_HOTSTART_LU

Determines if the simplex optimizer should exploit the initial factorization.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

MSK_IPAR_SIM_INTEGER

An experimental feature.

Accepted Values: [0;10]

Default Value: 0

Groups: Simplex optimizer

MSK_IPAR_SIM_MAX_ITERATIONS

Maximum number of iterations that can be used by a simplex optimizer.

Accepted Values: $[0;+\inf]$ Default Value: 10000000

Groups: Simplex optimizer, Termination criterion

MSK_IPAR_SIM_MAX_NUM_SETBACKS

Controls how many set-backs are allowed within a simplex optimizer. A set-back is an event where the optimizer moves in the wrong direction. This is impossible in theory but may happen due to numerical problems.

Accepted Values: $[0;+\inf]$

Default Value: 250

Groups: Simplex optimizer

MSK_IPAR_SIM_NON_SINGULAR

Controls if the simplex optimizer ensures a non-singular basis, if possible.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Simplex optimizer

MSK_IPAR_SIM_PRIMAL_CRASH

Controls whether crashing is performed in the primal simplex optimizer.

In general, if a basis consists of more than (100-this parameter value)% fixed variables, then a crash will be performed.

Accepted Values: $[0;+\inf]$

Default Value: 90

Groups: Primal simplex optimizer

MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD

An experimental feature.

Accepted Values: [0;10]

Default Value: 0

Groups: Simplex optimizer

MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION

The primal simplex optimizer can use a so-called restricted selection/pricing strategy to chooses the outgoing variable. Hence, if restricted selection is applied, then the primal simplex optimizer first choose a subset of all the potential incoming variables. Next, for some time it will choose the incoming variable only among the subset. From time to time the subset is redefined.

A larger value of this parameter implies that the optimizer will be more aggressive in its restriction strategy, i.e. a value of 0 implies that the restriction strategy is not applied at all.

Accepted Values: [0;100]

 ${\tt Default\ Value:} \quad 50$

Groups: Primal simplex optimizer

MSK_IPAR_SIM_PRIMAL_SELECTION

Controls the choice of the incoming variable, known as the selection strategy, in the primal simplex optimizer.

Accepted Values: MSKsimseltypee

Default Value: MSK_SIM_SELECTION_FREE

Groups: Primal simplex optimizer

MSK_IPAR_SIM_REFACTOR_FREQ

Controls how frequent the basis is refactorized. The value 0 means that the optimizer determines the best point of refactorization.

It is strongly recommended NOT to change this parameter.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Simplex optimizer

MSK_IPAR_SIM_REFORMULATION

Controls if the simplex optimizers are allowed to reformulate the problem.

Accepted Values: MSKsimreforme

Default Value: MSK_SIM_REFORMULATION_OFF

Groups: Simplex optimizer

MSK_IPAR_SIM_SAVE_LU

Controls if the LU factorization stored should be replaced with the LU factorization corresponding to the initial basis.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Simplex optimizer

MSK_IPAR_SIM_SCALING

Controls how much effort is used in scaling the problem before a simplex optimizer is used.

Accepted Values: MSKscalingtypee

Default Value: MSK_SCALING_FREE

Groups: Simplex optimizer

MSK_IPAR_SIM_SCALING_METHOD

Controls how the problem is scaled before a simplex optimizer is used.

 ${\tt Accepted\ Values:} \quad {\tt \it MSKscalingmethode}$

Default Value: MSK_SCALING_METHOD_POW2

Groups: Simplex optimizer

MSK_IPAR_SIM_SOLVE_FORM

Controls whether the primal or the dual problem is solved by the primal-/dual-simplex optimizer.

Accepted Values: MSKsolveforme
Default Value: MSK_SOLVE_FREE

Groups: Simplex optimizer

MSK_IPAR_SIM_STABILITY_PRIORITY

Controls how high priority the numerical stability should be given.

Accepted Values: [0;100]

Default Value: 50

Groups: Simplex optimizer

MSK_IPAR_SIM_SWITCH_OPTIMIZER

The simplex optimizer sometimes chooses to solve the dual problem instead of the primal problem. This implies that if you have chosen to use the dual simplex optimizer and the problem is dualized, then it actually makes sense to use the primal simplex optimizer instead. If this parameter is on and the problem is dualized and furthermore the simplex optimizer is chosen to be the primal (dual) one, then it is switched to the dual (primal).

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Simplex optimizer

MSK_IPAR_SOLUTION_CALLBACK

Indicates whether solution call-backs will be performed during the optimization.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Progress call-back, Overall solver

MSK_IPAR_SOL_FILTER_KEEP_BASIC

If turned on, then basic and super basic constraints and variables are written to the solution file independent of the filter setting.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

 ${\tt Groups:} \hspace{0.5cm} \textit{Solution input/output}$

MSK_IPAR_SOL_FILTER_KEEP_RANGED

If turned on, then ranged constraints and variables are written to the solution file independent of the filter setting.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Solution input/output

MSK_IPAR_SOL_READ_NAME_WIDTH

When a solution is read by **MOSEK** and some constraint, variable or cone names contain blanks, then a maximum name width much be specified. A negative value implies that no name contain blanks.

Accepted Values: [-inf;+inf]

Default Value: -1

Groups: Data input/output, Solution input/output

MSK_IPAR_SOL_READ_WIDTH

Controls the maximal acceptable width of line in the solutions when read by MOSEK.

Accepted Values: $[0;+\inf]$

Default Value: 1024

Groups: Data input/output, Solution input/output

MSK_IPAR_TIMING_LEVEL

Controls the a amount of timing performed inside MOSEK.

Accepted Values: $[0;+\inf]$

Default Value: 1

Groups: Optimization system

MSK_IPAR_WRITE_BAS_CONSTRAINTS

Controls whether the constraint section is written to the basic solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_BAS_HEAD

Controls whether the header section is written to the basic solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_BAS_VARIABLES

Controls whether the variables section is written to the basic solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_DATA_COMPRESSED

Controls whether the data file is compressed while it is written. 0 means no compression while higher values mean more compression.

Accepted Values: $[0;+\inf]$

Default Value: 0

Groups: Data input/output

MSK_IPAR_WRITE_DATA_FORMAT

Controls the file format when writing task data to a file.

Accepted Values: MSKdataformate

Default Value: MSK_DATA_FORMAT_EXTENSION

Groups: Data input/output

MSK_IPAR_WRITE_DATA_PARAM

If this option is turned on the parameter settings are written to the data file as parameters.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_WRITE_FREE_CON

Controls whether the free constraints are written to the data file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_WRITE_GENERIC_NAMES

Controls whether the generic names or user-defined names are used in the data file.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_WRITE_GENERIC_NAMES_IO

Index origin used in generic names.

Accepted Values: $[0;+\inf]$

Default Value: 1

 ${\tt Groups:} \quad \textit{Data input/output}$

MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS

Controls if the writer ignores incompatible problem items when writing files.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF
Groups: Data input/output

MSK_IPAR_WRITE_INT_CONSTRAINTS

Controls whether the constraint section is written to the integer solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_INT_HEAD

Controls whether the header section is written to the integer solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_INT_VARIABLES

Controls whether the variables section is written to the integer solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_LP_FULL_OBJ

Write all variables, including the ones with 0-coefficients, in the objective.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_WRITE_LP_LINE_WIDTH

Maximum width of line in an LP file written by MOSEK.

Accepted Values: $[40;+\inf]$

Default Value: 80

Groups: Data input/output

MSK_IPAR_WRITE_LP_QUOTED_NAMES

If this option is turned on, then MOSEK will quote invalid LP names when writing an LP file.

Accepted Values: MSKonoffkeye

 $\begin{tabular}{lll} {\tt Default Value:} & {\tt \it MSK_ON} \\ {\tt Groups:} & {\tt \it Data\ input/output} \\ \end{tabular}$

MSK_IPAR_WRITE_LP_STRICT_FORMAT

Controls whether LP output files satisfy the LP format strictly.

Accepted Values: MSKonoffkeye

MSK_IPAR_WRITE_LP_TERMS_PER_LINE

Maximum number of terms on a single line in an LP file written by MOSEK. 0 means unlimited.

Accepted Values: $[0;+\inf]$

Default Value: 10

Groups: Data input/output

MSK_IPAR_WRITE_MPS_FORMAT

Controls in which format the MPS is written.

Accepted Values: MSKmpsformate

Default Value: MSK_MPS_FORMAT_FREE

Groups: Data input/output

MSK_IPAR_WRITE_MPS_INT

Controls if marker records are written to the MPS file to indicate whether variables are integer restricted.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_WRITE_PRECISION

Controls the precision with which double numbers are printed in the MPS data file. In general it is not worthwhile to use a value higher than 15.

Accepted Values: $[0;+\inf]$

Default Value: 15

 ${\tt Groups:} \quad \textit{Data input/output}$

MSK_IPAR_WRITE_SOL_BARVARIABLES

Controls whether the symmetric matrix variables section is written to the solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_SOL_CONSTRAINTS

Controls whether the constraint section is written to the solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_SOL_HEAD

Controls whether the header section is written to the solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

 ${\tt Groups:} \quad \textit{Data input/output, Solution input/output}$

MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES

Even if the names are invalid MPS names, then they are employed when writing the solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_OFF

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_SOL_VARIABLES

Controls whether the variables section is written to the solution file.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output, Solution input/output

MSK_IPAR_WRITE_TASK_INC_SOL

Controls whether the solutions are stored in the task file too.

Accepted Values: MSKonoffkeye

Default Value: MSK_ON

Groups: Data input/output

MSK_IPAR_WRITE_XML_MODE

Controls if linear coefficients should be written by row or column when writing in the XML file format.

Accepted Values: MSKxmlwriteroutputtypee Default Value: $MSK_wRITE_XML_MODE_ROW$

 ${\tt Groups:} \quad \textit{Data input/output}$

String Parameters

MSK_SPAR_BAS_SOL_FILE_NAME

Name of the bas solution file.

Accepted Values: Any valid file name.

Groups: Data input/output, Solution input/output

MSK_SPAR_DATA_FILE_NAME

Data are read and written to this file.

Accepted Values: Any valid file name.

Groups: Data input/output

MSK_SPAR_DEBUG_FILE_NAME

MOSEK debug file.

Accepted Values: Any valid file name.

 ${\tt Groups:} \quad \textit{Data input/output}$

MSK_SPAR_INT_SOL_FILE_NAME

Name of the int solution file.

Accepted Values: Any valid file name.

Groups: Data input/output, Solution input/output

MSK_SPAR_ITR_SOL_FILE_NAME

Name of the itr solution file.

Accepted Values: Any valid file name.

Groups: Data input/output, Solution input/output

MSK_SPAR_MIO_DEBUG_STRING

For internal use only.

Accepted Values: Any valid string.

 ${\tt Groups:} \quad \textit{Data input/output}$

MSK_SPAR_PARAM_COMMENT_SIGN

Only the first character in this string is used. It is considered as a start of comment sign in the **MOSEK** parameter file. Spaces are ignored in the string.

Accepted Values: Any valid string.

Default Value: %%

Groups: Data input/output

MSK_SPAR_PARAM_READ_FILE_NAME

Modifications to the parameter database is read from this file.

Accepted Values: Any valid file name.

Groups: Data input/output

MSK_SPAR_PARAM_WRITE_FILE_NAME

The parameter database is written to this file.

Accepted Values: Any valid file name.

Groups: Data input/output

MSK_SPAR_READ_MPS_BOU_NAME

Name of the BOUNDS vector used. An empty name means that the first BOUNDS vector is used.

Accepted Values: Any valid MPS name.

Groups: Data input/output

MSK_SPAR_READ_MPS_OBJ_NAME

Name of the free constraint used as objective function. An empty name means that the first constraint is used as objective function.

Accepted Values: Any valid MPS name.

Groups: Data input/output

MSK_SPAR_READ_MPS_RAN_NAME

Name of the RANGE vector used. An empty name means that the first RANGE vector is used.

Accepted Values: Any valid MPS name.

Groups: Data input/output

MSK_SPAR_READ_MPS_RHS_NAME

Name of the RHS used. An empty name means that the first RHS vector is used.

Accepted Values: Any valid MPS name.

 ${\tt Groups:} \quad \textit{Data input/output}$

MSK_SPAR_REMOTE_ACCESS_TOKEN

An access token used to submit tasks to a remote **MOSEK** server. An access token is a random 32-byte string encoded in base64, i.e. it is a 44 character ASCII string.

Accepted Values: Any valid string.

MSK_SPAR_SENSITIVITY_FILE_NAME

If defined, MOSEK reads this file as a sensitivity analysis data file specifying the type of analysis to be done.

Accepted Values: Any valid string.

Groups: Data input/output

MSK_SPAR_SENSITIVITY_RES_FILE_NAME

Accepted Values: Any valid string.

Groups: Data input/output

MSK_SPAR_SOL_FILTER_XC_LOW

A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having xc[i]>0.5 should be listed, whereas +0.5 means that all constraints having xc[i]>=blc[i]+0.5 should be listed. An empty filter means that no filter is applied.

Accepted Values: Any valid filter.

Groups: Data input/output, Solution input/output

MSK_SPAR_SOL_FILTER_XC_UPR

A filter used to determine which constraints should be listed in the solution file. A value of 0.5 means that all constraints having xc[i]<0.5 should be listed, whereas -0.5 means all constraints having xc[i]<=buc[i]-0.5 should be listed. An empty filter means that no filter is applied.

Accepted Values: Any valid filter.

Groups: Data input/output, Solution input/output

MSK_SPAR_SOL_FILTER_XX_LOW

A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having xx[j] >= 0.5 should be listed, whereas "+0.5" means that all constraints having xx[j] >= blx[j] + 0.5 should be listed. An empty filter means no filter is applied.

Accepted Values: Any valid filter.

Groups: Data input/output, Solution input/output

MSK_SPAR_SOL_FILTER_XX_UPR

A filter used to determine which variables should be listed in the solution file. A value of "0.5" means that all constraints having xx[j]<0.5 should be printed, whereas "-0.5" means all constraints having xx[j]<=bux[j]-0.5 should be listed. An empty filter means no filter is applied.

Accepted Values: Any valid file name.

Groups: Data input/output, Solution input/output

MSK_SPAR_STAT_FILE_NAME

Statistics file name.

Accepted Values: Any valid file name.

Groups: Data input/output

MSK_SPAR_STAT_KEY

Key used when writing the summary file.

Accepted Values: Any valid XML string.

Groups: Data input/output

MSK_SPAR_STAT_NAME

Name used when writing the statistics file.

Accepted Values: Any valid XML string.

Groups: Data input/output

MSK_SPAR_WRITE_LP_GEN_VAR_NAME

Sometimes when an LP file is written additional variables must be inserted. They will have the prefix denoted by this parameter.

Accepted Values: Any valid string.

Default Value: xmskgen
Groups: Data input/output

10.2.2 Conic interior-point method parameters.

- MSK_DPAR_INTPNT_CO_TOL_DFEAS
- MSK_DPAR_INTPNT_CO_TOL_INFEAS
- MSK_DPAR_INTPNT_CO_TOL_MU_RED
- MSK_DPAR_INTPNT_CO_TOL_NEAR_REL
- MSK_DPAR_INTPNT_CO_TOL_PFEAS

• MSK_DPAR_INTPNT_CO_TOL_REL_GAP

10.2.3 Interior-point method parameters.

- MSK_IPAR_BI_IGNORE_MAX_ITER
- MSK_IPAR_BI_IGNORE_NUM_ERROR
- MSK_DPAR_CHECK_CONVEXITY_REL_TOL
- MSK_IPAR_INTPNT_BASIS
- MSK_DPAR_INTPNT_CO_TOL_DFEAS
- MSK_DPAR_INTPNT_CO_TOL_INFEAS
- MSK_DPAR_INTPNT_CO_TOL_MU_RED
- MSK_DPAR_INTPNT_CO_TOL_NEAR_REL
- MSK_DPAR_INTPNT_CO_TOL_PFEAS
- MSK_DPAR_INTPNT_CO_TOL_REL_GAP
- MSK_IPAR_INTPNT_DIFF_STEP
- MSK_IPAR_INTPNT_HOTSTART
- MSK_IPAR_INTPNT_MAX_ITERATIONS
- MSK_IPAR_INTPNT_MAX_NUM_COR
- MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS
- MSK_DPAR_INTPNT_NL_MERIT_BAL
- MSK_DPAR_INTPNT_NL_TOL_DFEAS
- MSK_DPAR_INTPNT_NL_TOL_MU_RED
- MSK_DPAR_INTPNT_NL_TOL_NEAR_REL
- MSK_DPAR_INTPNT_NL_TOL_PFEAS
- MSK_DPAR_INTPNT_NL_TOL_REL_GAP
- MSK_DPAR_INTPNT_NL_TOL_REL_STEP
- MSK_IPAR_INTPNT_OFF_COL_TRH
- MSK_IPAR_INTPNT_ORDER_METHOD
- MSK_DPAR_INTPNT_QO_TOL_DFEAS
- MSK_DPAR_INTPNT_QO_TOL_INFEAS
- MSK_DPAR_INTPNT_QO_TOL_MU_RED
- MSK_DPAR_INTPNT_QO_TOL_NEAR_REL
- MSK_DPAR_INTPNT_QO_TOL_PFEAS
- MSK_DPAR_INTPNT_QO_TOL_REL_GAP
- MSK_IPAR_INTPNT_REGULARIZATION_USE
- MSK_IPAR_INTPNT_SCALING
- MSK_IPAR_INTPNT_SOLVE_FORM
- MSK_IPAR_INTPNT_STARTING_POINT
- MSK_DPAR_INTPNT_TOL_DFEAS
- MSK_DPAR_INTPNT_TOL_DSAFE

- MSK_DPAR_INTPNT_TOL_INFEAS
- MSK_DPAR_INTPNT_TOL_MU_RED
- MSK_DPAR_INTPNT_TOL_PATH
- MSK_DPAR_INTPNT_TOL_PFEAS
- MSK_DPAR_INTPNT_TOL_PSAFE
- MSK_DPAR_INTPNT_TOL_REL_GAP
- MSK_DPAR_INTPNT_TOL_REL_STEP
- MSK_DPAR_INTPNT_TOL_STEP_SIZE
- MSK_IPAR_LOG_INTPNT
- MSK_IPAR_LOG_PRESOLVE
- MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL

10.2.4 Mixed-integer optimization parameters.

- MSK_IPAR_LOG_MIO
- MSK_IPAR_LOG_MIO_FREQ
- MSK_IPAR_MIO_BRANCH_DIR
- MSK_IPAR_MIO_CONSTRUCT_SOL
- MSK_IPAR_MIO_CUT_CLIQUE
- MSK_IPAR_MIO_CUT_CMIR
- MSK_IPAR_MIO_CUT_GMI
- MSK_IPAR_MIO_CUT_IMPLIED_BOUND
- MSK_IPAR_MIO_CUT_KNAPSACK_COVER
- MSK_IPAR_MIO_CUT_SELECTION_LEVEL
- MSK_DPAR_MIO_DISABLE_TERM_TIME
- MSK_IPAR_MIO_HEURISTIC_LEVEL
- MSK_IPAR_MIO_MAX_NUM_BRANCHES
- MSK_IPAR_MIO_MAX_NUM_RELAXS
- MSK_IPAR_MIO_MAX_NUM_SOLUTIONS
- MSK_DPAR_MIO_MAX_TIME
- MSK_DPAR_MIO_NEAR_TOL_ABS_GAP
- MSK_DPAR_MIO_NEAR_TOL_REL_GAP
- MSK_IPAR_MIO_NODE_OPTIMIZER
- MSK_IPAR_MIO_NODE_SELECTION
- MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE
- MSK_IPAR_MIO_PROBING_LEVEL
- MSK_DPAR_MIO_REL_GAP_CONST
- MSK_IPAR_MIO_RINS_MAX_NODES
- MSK_IPAR_MIO_ROOT_OPTIMIZER
- MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL

- MSK_DPAR_MIO_TOL_ABS_GAP
- MSK_DPAR_MIO_TOL_ABS_RELAX_INT
- MSK_DPAR_MIO_TOL_FEAS
- MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT
- MSK_DPAR_MIO_TOL_REL_GAP
- MSK_IPAR_MIO_VB_DETECTION_LEVEL

10.2.5 Overall solver parameters.

- MSK_IPAR_BI_CLEAN_OPTIMIZER
- MSK_IPAR_INFEAS_PREFER_PRIMAL
- MSK_IPAR_LICENSE_WAIT
- MSK_IPAR_MIO_MODE
- MSK_IPAR_OPTIMIZER
- MSK_IPAR_PRESOLVE_LEVEL
- MSK_IPAR_PRESOLVE_USE
- MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER
- MSK_IPAR_SENSITIVITY_ALL
- MSK_IPAR_SENSITIVITY_OPTIMIZER
- MSK_IPAR_SENSITIVITY_TYPE
- MSK_IPAR_SOLUTION_CALLBACK

10.2.6 Solution input/output parameters.

- MSK_SPAR_BAS_SOL_FILE_NAME
- MSK_IPAR_INFEAS_REPORT_AUTO
- MSK_SPAR_INT_SOL_FILE_NAME
- MSK_SPAR_ITR_SOL_FILE_NAME
- MSK_IPAR_SOL_FILTER_KEEP_BASIC
- MSK_IPAR_SOL_FILTER_KEEP_RANGED
- MSK_SPAR_SOL_FILTER_XC_LOW
- MSK_SPAR_SOL_FILTER_XC_UPR
- MSK_SPAR_SOL_FILTER_XX_LOW
- MSK_SPAR_SOL_FILTER_XX_UPR
- MSK_IPAR_SOL_READ_NAME_WIDTH
- MSK_IPAR_SOL_READ_WIDTH
- MSK_IPAR_WRITE_BAS_CONSTRAINTS
- MSK_IPAR_WRITE_BAS_HEAD
- MSK_IPAR_WRITE_BAS_VARIABLES
- MSK_IPAR_WRITE_INT_CONSTRAINTS

- MSK_IPAR_WRITE_INT_HEAD
- MSK_IPAR_WRITE_INT_VARIABLES
- MSK_IPAR_WRITE_SOL_BARVARIABLES
- MSK_IPAR_WRITE_SOL_CONSTRAINTS
- MSK_IPAR_WRITE_SOL_HEAD
- MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES
- MSK_IPAR_WRITE_SOL_VARIABLES

10.2.7 Termination criterion parameters.

- MSK_DPAR_BASIS_REL_TOL_S
- MSK_DPAR_BASIS_TOL_S
- MSK_DPAR_BASIS_TOL_X
- MSK_IPAR_BI_MAX_ITERATIONS
- MSK_DPAR_INTPNT_CO_TOL_DFEAS
- MSK_DPAR_INTPNT_CO_TOL_INFEAS
- MSK_DPAR_INTPNT_CO_TOL_MU_RED
- MSK_DPAR_INTPNT_CO_TOL_NEAR_REL
- MSK_DPAR_INTPNT_CO_TOL_PFEAS
- MSK_DPAR_INTPNT_CO_TOL_REL_GAP
- MSK_IPAR_INTPNT_MAX_ITERATIONS
- MSK_DPAR_INTPNT_NL_TOL_DFEAS
- MSK_DPAR_INTPNT_NL_TOL_MU_RED
- MSK_DPAR_INTPNT_NL_TOL_NEAR_REL
- MSK_DPAR_INTPNT_NL_TOL_PFEAS
- MSK_DPAR_INTPNT_NL_TOL_REL_GAP
- MSK_DPAR_INTPNT_QO_TOL_DFEAS
- MSK_DPAR_INTPNT_QO_TOL_INFEAS
- MSK_DPAR_INTPNT_QO_TOL_MU_RED
- MSK_DPAR_INTPNT_QO_TOL_NEAR_REL
- MSK_DPAR_INTPNT_QO_TOL_PFEAS
- MSK_DPAR_INTPNT_QO_TOL_REL_GAP
- MSK_DPAR_INTPNT_TOL_DFEAS
- MSK_DPAR_INTPNT_TOL_INFEAS
- MSK_DPAR_INTPNT_TOL_MU_RED
- MSK_DPAR_INTPNT_TOL_PFEAS
- MSK_DPAR_INTPNT_TOL_REL_GAP
- MSK_DPAR_LOWER_OBJ_CUT
- MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH
- MSK_DPAR_MIO_DISABLE_TERM_TIME

- MSK_IPAR_MIO_MAX_NUM_BRANCHES
- MSK_IPAR_MIO_MAX_NUM_SOLUTIONS
- MSK_DPAR_MIO_MAX_TIME
- MSK_DPAR_MIO_NEAR_TOL_REL_GAP
- MSK_DPAR_MIO_REL_GAP_CONST
- MSK_DPAR_MIO_TOL_REL_GAP
- MSK_DPAR_OPTIMIZER_MAX_TIME
- MSK_IPAR_SIM_MAX_ITERATIONS
- MSK_DPAR_UPPER_OBJ_CUT
- MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH

10.2.8 Analysis parameters.

- MSK_IPAR_ANA_SOL_BASIS
- MSK_DPAR_ANA_SOL_INFEAS_TOL
- MSK_IPAR_ANA_SOL_PRINT_VIOLATED
- MSK_IPAR_LOG_ANA_PRO

10.2.9 Optimization system parameters.

- MSK_IPAR_AUTO_UPDATE_SOL_INFO
- MSK_IPAR_INTPNT_MULTI_THREAD
- MSK_IPAR_LICENSE_WAIT
- MSK_IPAR_LOG_STORAGE
- MSK_IPAR_MIO_MT_USER_CB
- MSK_IPAR_MT_SPINCOUNT
- MSK_IPAR_NUM_THREADS
- MSK_IPAR_TIMING_LEVEL

10.2.10 Primal simplex optimizer parameters.

- MSK_IPAR_SIM_PRIMAL_CRASH
- MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION
- MSK_IPAR_SIM_PRIMAL_SELECTION

10.2.11 Output information parameters.

- MSK_IPAR_INFEAS_REPORT_LEVEL
- MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS
- MSK_IPAR_LOG
- MSK_IPAR_LOG_BI
- MSK_IPAR_LOG_BI_FREQ

- MSK_IPAR_LOG_CUT_SECOND_OPT
- MSK_IPAR_LOG_EXPAND
- MSK_IPAR_LOG_FACTOR
- MSK_IPAR_LOG_FEAS_REPAIR
- MSK_IPAR_LOG_FILE
- MSK_IPAR_LOG_HEAD
- MSK_IPAR_LOG_INFEAS_ANA
- MSK_IPAR_LOG_INTPNT
- MSK_IPAR_LOG_MIO
- MSK_IPAR_LOG_MIO_FREQ
- MSK_IPAR_LOG_OPTIMIZER
- MSK_IPAR_LOG_ORDER
- MSK_IPAR_LOG_RESPONSE
- MSK_IPAR_LOG_SENSITIVITY
- MSK_IPAR_LOG_SENSITIVITY_OPT
- MSK_IPAR_LOG_SIM
- MSK_IPAR_LOG_SIM_FREQ
- MSK_IPAR_LOG_SIM_MINOR
- MSK_IPAR_LOG_STORAGE
- MSK_IPAR_MAX_NUM_WARNINGS

10.2.12 Progress call-back parameters.

• MSK_IPAR_SOLUTION_CALLBACK

10.2.13 Basis identification parameters.

- MSK_IPAR_BI_CLEAN_OPTIMIZER
- MSK_IPAR_BI_IGNORE_MAX_ITER
- MSK_IPAR_BI_IGNORE_NUM_ERROR
- MSK_IPAR_BI_MAX_ITERATIONS
- MSK_IPAR_INTPNT_BASIS
- MSK_IPAR_LOG_BI
- MSK_IPAR_LOG_BI_FREQ
- MSK_DPAR_SIM_LU_TOL_REL_PIV

10.2.14 Presolve parameters.

- MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL
- MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES
- MSK_IPAR_PRESOLVE_LEVEL

10.2. Parameters 105

- MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH
- MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH
- MSK_IPAR_PRESOLVE_LINDEP_USE
- MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP
- MSK_DPAR_PRESOLVE_TOL_AIJ
- MSK_DPAR_PRESOLVE_TOL_REL_LINDEP
- MSK_DPAR_PRESOLVE_TOL_S
- MSK_DPAR_PRESOLVE_TOL_X
- MSK_IPAR_PRESOLVE_USE

10.2.15 Data input/output parameters.

- MSK_SPAR_BAS_SOL_FILE_NAME
- MSK_SPAR_DATA_FILE_NAME
- MSK_SPAR_DEBUG_FILE_NAME
- MSK_IPAR_INFEAS_REPORT_AUTO
- MSK_SPAR_INT_SOL_FILE_NAME
- MSK_SPAR_ITR_SOL_FILE_NAME
- MSK_IPAR_LOG_FILE
- MSK_SPAR_MIO_DEBUG_STRING
- MSK_IPAR_OPF_MAX_TERMS_PER_LINE
- MSK_IPAR_OPF_WRITE_HEADER
- MSK_IPAR_OPF_WRITE_HINTS
- MSK_IPAR_OPF_WRITE_PARAMETERS
- MSK_IPAR_OPF_WRITE_PROBLEM
- MSK_IPAR_OPF_WRITE_SOL_BAS
- MSK_IPAR_OPF_WRITE_SOL_ITG
- MSK_IPAR_OPF_WRITE_SOL_ITR
- MSK_IPAR_OPF_WRITE_SOLUTIONS
- MSK_SPAR_PARAM_COMMENT_SIGN
- MSK_IPAR_PARAM_READ_CASE_NAME
- MSK_SPAR_PARAM_READ_FILE_NAME
- MSK_IPAR_PARAM_READ_IGN_ERROR
- MSK_SPAR_PARAM_WRITE_FILE_NAME
- MSK_IPAR_READ_DATA_COMPRESSED
- MSK_IPAR_READ_DATA_FORMAT
- MSK_IPAR_READ_DEBUG
- MSK_IPAR_READ_KEEP_FREE_CON
- MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU
- MSK_IPAR_READ_LP_QUOTED_NAMES

- MSK_SPAR_READ_MPS_BOU_NAME
- MSK_IPAR_READ_MPS_FORMAT
- MSK_SPAR_READ_MPS_OBJ_NAME
- MSK_SPAR_READ_MPS_RAN_NAME
- MSK_SPAR_READ_MPS_RHS_NAME
- MSK_IPAR_READ_MPS_WIDTH
- MSK_IPAR_READ_TASK_IGNORE_PARAM
- MSK_SPAR_SENSITIVITY_FILE_NAME
- MSK_SPAR_SENSITIVITY_RES_FILE_NAME
- MSK_SPAR_SOL_FILTER_XC_LOW
- MSK_SPAR_SOL_FILTER_XC_UPR
- MSK_SPAR_SOL_FILTER_XX_LOW
- MSK_SPAR_SOL_FILTER_XX_UPR
- MSK_IPAR_SOL_READ_NAME_WIDTH
- MSK_IPAR_SOL_READ_WIDTH
- MSK_SPAR_STAT_FILE_NAME
- MSK_SPAR_STAT_KEY
- MSK_SPAR_STAT_NAME
- MSK_IPAR_WRITE_BAS_CONSTRAINTS
- MSK_IPAR_WRITE_BAS_HEAD
- MSK_IPAR_WRITE_BAS_VARIABLES
- MSK_IPAR_WRITE_DATA_COMPRESSED
- MSK_IPAR_WRITE_DATA_FORMAT
- MSK_IPAR_WRITE_DATA_PARAM
- MSK_IPAR_WRITE_FREE_CON
- MSK_IPAR_WRITE_GENERIC_NAMES
- MSK_IPAR_WRITE_GENERIC_NAMES_IO
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_ITEMS
- MSK_IPAR_WRITE_INT_CONSTRAINTS
- MSK_IPAR_WRITE_INT_HEAD
- MSK_IPAR_WRITE_INT_VARIABLES
- MSK_IPAR_WRITE_LP_FULL_OBJ
- MSK_SPAR_WRITE_LP_GEN_VAR_NAME
- MSK_IPAR_WRITE_LP_LINE_WIDTH
- MSK_IPAR_WRITE_LP_QUOTED_NAMES
- MSK_IPAR_WRITE_LP_STRICT_FORMAT
- MSK_IPAR_WRITE_LP_TERMS_PER_LINE
- MSK_IPAR_WRITE_MPS_FORMAT
- MSK_IPAR_WRITE_MPS_INT

10.2. Parameters 107

- MSK_IPAR_WRITE_PRECISION
- MSK_IPAR_WRITE_SOL_BARVARIABLES
- MSK_IPAR_WRITE_SOL_CONSTRAINTS
- MSK_IPAR_WRITE_SOL_HEAD
- MSK_IPAR_WRITE_SOL_IGNORE_INVALID_NAMES
- MSK_IPAR_WRITE_SOL_VARIABLES
- MSK_IPAR_WRITE_TASK_INC_SOL
- MSK_IPAR_WRITE_XML_MODE

10.2.16 Infeasibility report parameters.

- MSK_IPAR_INFEAS_GENERIC_NAMES
- MSK_IPAR_INFEAS_REPORT_LEVEL
- MSK_IPAR_LOG_INFEAS_ANA

10.2.17 Simplex optimizer parameters.

- MSK_DPAR_BASIS_REL_TOL_S
- MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE
- MSK_DPAR_BASIS_TOL_S
- MSK_DPAR_BASIS_TOL_X
- $\bullet \ \textit{MSK_IPAR_LOG_SIM}$
- MSK_IPAR_LOG_SIM_FREQ
- MSK_IPAR_LOG_SIM_MINOR
- MSK_IPAR_SENSITIVITY_OPTIMIZER
- MSK_IPAR_SIM_BASIS_FACTOR_USE
- MSK_IPAR_SIM_DEGEN
- MSK_IPAR_SIM_DUAL_PHASEONE_METHOD
- MSK_IPAR_SIM_EXPLOIT_DUPVEC
- MSK_IPAR_SIM_HOTSTART
- MSK_IPAR_SIM_INTEGER
- MSK_DPAR_SIM_LU_TOL_REL_PIV
- MSK_IPAR_SIM_MAX_ITERATIONS
- $\bullet \quad \mathit{MSK_IPAR_SIM_MAX_NUM_SETBACKS}$
- MSK_IPAR_SIM_NON_SINGULAR
- $\bullet \ \textit{MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD}$
- MSK_IPAR_SIM_REFACTOR_FREQ
- MSK_IPAR_SIM_REFORMULATION
- MSK_IPAR_SIM_SAVE_LU
- MSK_IPAR_SIM_SCALING

- MSK_IPAR_SIM_SCALING_METHOD
- MSK_IPAR_SIM_SOLVE_FORM
- MSK_IPAR_SIM_STABILITY_PRIORITY
- MSK_IPAR_SIM_SWITCH_OPTIMIZER
- MSK_DPAR_SIMPLEX_ABS_TOL_PIV

10.2.18 Nonlinear convex method parameters.

- MSK_IPAR_CHECK_CONVEXITY
- MSK_DPAR_INTPNT_NL_MERIT_BAL
- MSK_DPAR_INTPNT_NL_TOL_DFEAS
- MSK_DPAR_INTPNT_NL_TOL_MU_RED
- MSK_DPAR_INTPNT_NL_TOL_NEAR_REL
- MSK_DPAR_INTPNT_NL_TOL_PFEAS
- MSK_DPAR_INTPNT_NL_TOL_REL_GAP
- MSK_DPAR_INTPNT_NL_TOL_REL_STEP
- MSK_DPAR_INTPNT_TOL_INFEAS
- MSK_IPAR_LOG_CHECK_CONVEXITY

10.2.19 Dual simplex optimizer parameters.

- MSK_IPAR_SIM_DUAL_CRASH
- MSK_IPAR_SIM_DUAL_RESTRICT_SELECTION
- MSK_IPAR_SIM_DUAL_SELECTION

10.2.20 License manager parameters.

- MSK_IPAR_CACHE_LICENSE
- MSK_IPAR_LICENSE_DEBUG
- MSK_IPAR_LICENSE_PAUSE_TIME
- MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS
- MSK_IPAR_LICENSE_WAIT

10.2.21 Debugging parameters.

• MSK_IPAR_AUTO_SORT_A_BEFORE_OPT

10.2.22 Data check parameters.

- MSK_IPAR_CHECK_CONVEXITY
- MSK_DPAR_DATA_SYM_MAT_TOL
- MSK_DPAR_DATA_SYM_MAT_TOL_HUGE
- MSK_DPAR_DATA_SYM_MAT_TOL_LARGE

10.2. Parameters 109

- MSK_DPAR_DATA_TOL_AIJ
- MSK_DPAR_DATA_TOL_AIJ_HUGE
- MSK_DPAR_DATA_TOL_AIJ_LARGE
- MSK_DPAR_DATA_TOL_BOUND_INF
- MSK_DPAR_DATA_TOL_BOUND_WRN
- MSK_DPAR_DATA_TOL_C_HUGE
- $\bullet \quad \mathit{MSK_DPAR_DATA_TOL_CJ_LARGE}$
- MSK_DPAR_DATA_TOL_QIJ
- MSK_DPAR_DATA_TOL_X
- MSK_IPAR_LOG_CHECK_CONVEXITY
- MSK_DPAR_SEMIDEFINITE_TOL_APPROX

10.2.23 Logging parameters.

- MSK_IPAR_LOG
- MSK_IPAR_LOG_ANA_PRO
- MSK_IPAR_LOG_BI
- MSK_IPAR_LOG_BI_FREQ
- MSK_IPAR_LOG_CUT_SECOND_OPT
- MSK_IPAR_LOG_EXPAND
- MSK_IPAR_LOG_FACTOR
- MSK_IPAR_LOG_FEAS_REPAIR
- MSK_IPAR_LOG_FILE
- MSK_IPAR_LOG_HEAD
- MSK_IPAR_LOG_INFEAS_ANA
- MSK_IPAR_LOG_INTPNT
- MSK_IPAR_LOG_MIO
- MSK_IPAR_LOG_MIO_FREQ
- MSK_IPAR_LOG_OPTIMIZER
- MSK_IPAR_LOG_ORDER
- MSK_IPAR_LOG_PRESOLVE
- MSK_IPAR_LOG_RESPONSE
- MSK_IPAR_LOG_SENSITIVITY
- MSK_IPAR_LOG_SENSITIVITY_OPT
- $\bullet \ \textit{MSK_IPAR_LOG_SIM}$
- MSK_IPAR_LOG_SIM_FREQ
- MSK_IPAR_LOG_STORAGE

10.3 Response codes

- Termination codes
- Error codes
- Warning codes

10.3.1 Termination Codes

MSK_RES_OK (0)

No error occurred.

MSK_RES_TRM_INTERNAL (10030)

The optimizer terminated due to some internal reason. Please contact MOSEK support.

MSK_RES_TRM_INTERNAL_STOP (10031)

The optimizer terminated for internal reasons. Please contact MOSEK support.

MSK_RES_TRM_MAX_ITERATIONS (10000)

The optimizer terminated at the maximum number of iterations.

MSK_RES_TRM_MAX_NUM_SETBACKS (10020)

The optimizer terminated as the maximum number of set-backs was reached. This indicates % serious numerical problems and a possibly badly formulated problem.

MSK_RES_TRM_MAX_TIME (10001)

The optimizer terminated at the maximum amount of time.

MSK_RES_TRM_MIO_NEAR_ABS_GAP (10004)

The mixed-integer optimizer terminated because the near optimal absolute gap tolerance was satisfied.

MSK_RES_TRM_MIO_NEAR_REL_GAP (10003)

The mixed-integer optimizer terminated because the near optimal relative gap tolerance was satisfied

MSK_RES_TRM_MIO_NUM_BRANCHES (10009)

The mixed-integer optimizer terminated as to the maximum number of branches was reached.

MSK_RES_TRM_MIO_NUM_RELAXS (10008)

The mixed-integer optimizer terminated as the maximum number of relaxations was reached.

MSK_RES_TRM_NUM_MAX_NUM_INT_SOLUTIONS (10015)

The mixed-integer optimizer terminated as the maximum number of feasible solutions was reached.

MSK_RES_TRM_NUMERICAL_PROBLEM (10025)

The optimizer terminated due to numerical problems.

MSK_RES_TRM_OBJECTIVE_RANGE (10002)

The optimizer terminated on the bound of the objective range.

MSK_RES_TRM_STALL (10006)

The optimizer is terminated due to slow progress.

Stalling means that numerical problems prevent the optimizer from making reasonable progress and that it make no sense to continue. In many cases this happens if the problem is badly scaled or otherwise ill-conditioned. There is no guarantee that the solution will be (near) feasible or near optimal. However, often stalling happens near the optimum, and the returned solution may be of good quality. Therefore, it is recommended to check the status of then solution. If the solution near optimal the solution is most likely good enough for most practical purposes.

Please note that if a linear optimization problem is solved using the interior-point optimizer with basis identification turned on, the returned basic solution likely to have high accuracy, even though the optimizer stalled.

Some common causes of stalling are a) badly scaled models, b) near feasible or near infeasible problems and c) a non-convex problems. Case c) is only relevant for general non-linear problems. It is not possible in general for **MOSEK** to check if a specific problems is convex since such a check would be NP hard in itself. This implies that care should be taken when solving problems involving general user defined functions.

MSK_RES_TRM_USER_CALLBACK (10007)

The optimizer terminated due to the return of the user-defined call-back function.

10.3.2 Error Codes

MSK_RES_ERR_AD_INVALID_CODELIST (3102)

The code list data was invalid.

MSK_RES_ERR_API_ARRAY_TOO_SMALL (3001)

An input array was too short.

MSK_RES_ERR_API_CB_CONNECT (3002)

Failed to connect a callback object.

MSK_RES_ERR_API_FATAL_ERROR (3005)

An internal error occurred in the API. Please report this problem.

MSK_RES_ERR_API_INTERNAL (3999)

An internal fatal error occurred in an interface function.

MSK_RES_ERR_ARG_IS_TOO_LARGE (1227)

The value of a argument is too small.

MSK_RES_ERR_ARG_IS_TOO_SMALL (1226)

The value of a argument is too small.

MSK_RES_ERR_ARGUMENT_DIMENSION (1201)

A function argument is of incorrect dimension.

MSK_RES_ERR_ARGUMENT_IS_TOO_LARGE (5005)

The value of a function argument is too large.

MSK_RES_ERR_ARGUMENT_LENNEQ (1197)

Incorrect length of arguments.

MSK_RES_ERR_ARGUMENT_PERM_ARRAY (1299)

An invalid permutation array is specified.

MSK_RES_ERR_ARGUMENT_TYPE (1198)

Incorrect argument type.

MSK_RES_ERR_BAR_VAR_DIM (3920)

The dimension of a symmetric matrix variable has to greater than 0.

MSK_RES_ERR_BASIS (1266)

An invalid basis is specified. Either too many or too few basis variables are specified.

MSK_RES_ERR_BASIS_FACTOR (1610)

The factorization of the basis is invalid.

MSK_RES_ERR_BASIS_SINGULAR (1615)

The basis is singular and hence cannot be factored.

MSK_RES_ERR_BLANK_NAME (1070)

An all blank name has been specified.

MSK_RES_ERR_CANNOT_CLONE_NL (2505)

A task with a nonlinear function call-back cannot be cloned.

MSK_RES_ERR_CANNOT_HANDLE_NL (2506)

A function cannot handle a task with nonlinear function call-backs.

- $\begin{array}{c} \mathtt{MSK_RES_ERR_CBF_DUPLICATE_ACOORD} & (7116) \\ \\ \mathrm{Duplicate\ index\ in\ ACOORD}. \end{array}$
- MSK_RES_ERR_CBF_DUPLICATE_BCOORD (7115)

 Duplicate index in BCOORD.
- MSK_RES_ERR_CBF_DUPLICATE_CON (7108)

 Duplicate CON keyword.
- MSK_RES_ERR_CBF_DUPLICATE_INT (7110)

 Duplicate INT keyword.
- MSK_RES_ERR_CBF_DUPLICATE_OBJ (7107)
 Duplicate OBJ keyword.
- $\begin{array}{c} \mathtt{MSK_RES_ERR_CBF_DUPLICATE_OBJACOORD} \quad \textbf{(7114)} \\ \mathbf{Duplicate\ index\ in\ OBJCOORD}. \end{array}$
- MSK_RES_ERR_CBF_DUPLICATE_VAR (7109)
 Duplicate VAR keyword.
- MSK_RES_ERR_CBF_INVALID_CON_TYPE (7112)
 Invalid constraint type.
- MSK_RES_ERR_CBF_INVALID_DOMAIN_DIMENSION (7113) Invalid domain dimension.
- MSK_RES_ERR_CBF_INVALID_INT_INDEX (7121)
 Invalid INT index.
- MSK_RES_ERR_CBF_INVALID_VAR_TYPE (7111)
 Invalid variable type.
- MSK_RES_ERR_CBF_NO_VARIABLES (7102) No variables are specified.
- MSK_RES_ERR_CBF_NO_VERSION_SPECIFIED (7105) No version specified.
- MSK_RES_ERR_CBF_OBJ_SENSE (7101)
 An invalid objective sense is specified.
- MSK_RES_ERR_CBF_PARSE (7100)
 An error occurred while parsing an CBF file.
- MSK_RES_ERR_CBF_SYNTAX (7106) Invalid syntax.
- MSK_RES_ERR_CBF_TOO_FEW_CONSTRAINTS (7118)
 Too few constraints defined.
- MSK_RES_ERR_CBF_TOO_FEW_INTS (7119)
 Too few ints are specified.
- MSK_RES_ERR_CBF_TOO_FEW_VARIABLES (7117)
 Too few variables defined.
- $\begin{array}{c} {\tt MSK_RES_ERR_CBF_T00_MANY_CONSTRAINTS} & (7103) \\ {\tt Too\ many\ constraints\ specified}. \end{array}$
- MSK_RES_ERR_CBF_TOO_MANY_INTS (7120)
 Too many ints are specified.
- $\begin{array}{c} {\tt MSK_RES_ERR_CBF_T00_MANY_VARIABLES} \end{array} \ (7104) \\ {\tt Too\ many\ variables\ specified}. \end{array}$
- MSK_RES_ERR_CBF_UNSUPPORTED (7122) Unsupported feature is present.

MSK_RES_ERR_CON_Q_NOT_NSD (1294)

The quadratic constraint matrix is not negative semidefinite as expected for a constraint with finite lower bound. This results in a nonconvex problem. The parameter $MSK_DPAR_CHECK_CONVEXITY_REL_TOL$ can be used to relax the convexity check.

MSK_RES_ERR_CON_Q_NOT_PSD (1293)

The quadratic constraint matrix is not positive semidefinite as expected for a constraint with finite upper bound. This results in a nonconvex problem. The parameter <code>MSK_DPAR_CHECK_CONVEXITY_REL_TOL</code> can be used to relax the convexity check.

MSK_RES_ERR_CONE_INDEX (1300)

An index of a non-existing cone has been specified.

MSK_RES_ERR_CONE_OVERLAP (1302)

One or more of the variables in the cone to be added is already member of another cone. Now assume the variable is x_i then add a new variable say x_k and the constraint

$$x_j = x_k$$

and then let x_k be member of the cone to be appended.

MSK_RES_ERR_CONE_OVERLAP_APPEND (1307)

The cone to be appended has one variable which is already member of another cone.

MSK_RES_ERR_CONE_REP_VAR (1303)

A variable is included multiple times in the cone.

MSK_RES_ERR_CONE_SIZE (1301)

A cone with too few members is specified.

MSK_RES_ERR_CONE_TYPE (1305)

Invalid cone type specified.

MSK_RES_ERR_CONE_TYPE_STR (1306)

Invalid cone type specified.

MSK_RES_ERR_DATA_FILE_EXT (1055)

The data file format cannot be determined from the file name.

MSK_RES_ERR_DUP_NAME (1071)

The same name was used multiple times for the same problem item type.

MSK_RES_ERR_DUPLICATE_AIJ (1385)

An element in the A matrix is specified twice.

MSK_RES_ERR_DUPLICATE_BARVARIABLE_NAMES (4502)

Two barvariable names are identical.

MSK_RES_ERR_DUPLICATE_CONE_NAMES (4503)

Two cone names are identical.

MSK_RES_ERR_DUPLICATE_CONSTRAINT_NAMES (4500)

Two constraint names are identical.

MSK_RES_ERR_DUPLICATE_VARIABLE_NAMES (4501)

Two variable names are identical.

MSK_RES_ERR_END_OF_FILE (1059)

End of file reached.

MSK_RES_ERR_FACTOR (1650)

An error occurred while factorizing a matrix.

MSK_RES_ERR_FEASREPAIR_CANNOT_RELAX (1700)

An optimization problem cannot be relaxed. This is the case e.g. for general nonlinear optimization problems.

MSK_RES_ERR_FEASREPAIR_INCONSISTENT_BOUND (1702)

The upper bound is less than the lower bound for a variable or a constraint. Please correct this before running the feasibility repair.

MSK_RES_ERR_FEASREPAIR_SOLVING_RELAXED (1701)

The relaxed problem could not be solved to optimality. Please consult the log file for further details.

MSK_RES_ERR_FILE_LICENSE (1007)

Invalid license file.

MSK_RES_ERR_FILE_OPEN (1052)

Error while opening a file.

MSK_RES_ERR_FILE_READ (1053)

File read error.

MSK_RES_ERR_FILE_WRITE (1054)

File write error.

MSK_RES_ERR_FIRST (1261)

Invalid first.

MSK_RES_ERR_FIRSTI (1285)

Invalid firsti.

MSK_RES_ERR_FIRSTJ (1287)

Invalid firstj.

MSK_RES_ERR_FIXED_BOUND_VALUES (1425)

A fixed constraint/variable has been specified using the bound keys but the numerical value of the lower and upper bound is different.

MSK_RES_ERR_FLEXLM (1014)

The FLEXIm license manager reported an error.

MSK_RES_ERR_GLOBAL_INV_CONIC_PROBLEM (1503)

The global optimizer can only be applied to problems without semidefinite variables.

MSK_RES_ERR_HUGE_AIJ (1380)

A numerically huge value is specified for an $a_{i,j}$ element in A. The parameter $MSK_DPAR_DATA_TOL_AIJ_HUGE$ controls when an $a_{i,j}$ is considered huge.

MSK_RES_ERR_HUGE_C (1375)

A huge value in absolute size is specified for one c_j .

MSK_RES_ERR_IDENTICAL_TASKS (3101)

Some tasks related to this function call were identical. Unique tasks were expected.

MSK_RES_ERR_IN_ARGUMENT (1200)

A function argument is incorrect.

MSK_RES_ERR_INDEX (1235)

An index is out of range.

MSK_RES_ERR_INDEX_ARR_IS_TOO_LARGE (1222)

An index in an array argument is too large.

MSK_RES_ERR_INDEX_ARR_IS_TOO_SMALL (1221)

An index in an array argument is too small.

MSK_RES_ERR_INDEX_IS_TOO_LARGE (1204)

An index in an argument is too large.

MSK_RES_ERR_INDEX_IS_TOO_SMALL (1203)

An index in an argument is too small.

MSK_RES_ERR_INF_DOU_INDEX (1219)

A double information index is out of range for the specified type.

MSK_RES_ERR_INF_DOU_NAME (1230)

A double information name is invalid.

MSK_RES_ERR_INF_INT_INDEX (1220)

An integer information index is out of range for the specified type.

MSK_RES_ERR_INF_INT_NAME (1231)

An integer information name is invalid.

MSK_RES_ERR_INF_LINT_INDEX (1225)

A long integer information index is out of range for the specified type.

MSK_RES_ERR_INF_LINT_NAME (1234)

A long integer information name is invalid.

MSK_RES_ERR_INF_TYPE (1232)

The information type is invalid.

MSK_RES_ERR_INFEAS_UNDEFINED (3910)

The requested value is not defined for this solution type.

MSK_RES_ERR_INFINITE_BOUND (1400)

A numerically huge bound value is specified.

MSK_RES_ERR_INT64_TO_INT32_CAST (3800)

An 32 bit integer could not cast to a 64 bit integer.

MSK_RES_ERR_INTERNAL (3000)

An internal error occurred. Please report this problem.

MSK_RES_ERR_INTERNAL_TEST_FAILED (3500)

An internal unit test function failed.

MSK_RES_ERR_INV_APTRE (1253)

aptre[j] is strictly smaller than aptrb[j] for some j.

MSK_RES_ERR_INV_BK (1255)

Invalid bound key.

MSK_RES_ERR_INV_BKC (1256)

Invalid bound key is specified for a constraint.

MSK_RES_ERR_INV_BKX (1257)

An invalid bound key is specified for a variable.

MSK_RES_ERR_INV_CONE_TYPE (1272)

Invalid cone type code is encountered.

MSK_RES_ERR_INV_CONE_TYPE_STR (1271)

Invalid cone type string encountered.

MSK_RES_ERR_INV_MARKI (2501)

Invalid value in marki.

MSK_RES_ERR_INV_MARKJ (2502)

Invalid value in markj.

MSK_RES_ERR_INV_NAME_ITEM (1280)

An invalid name item code is used.

MSK_RES_ERR_INV_NUMI (2503)

Invalid numi.

MSK_RES_ERR_INV_NUMJ (2504)

Invalid numj.

MSK_RES_ERR_INV_OPTIMIZER (1550)

An invalid optimizer has been chosen for the problem. This means that the simplex or the conic optimizer is chosen to optimize a nonlinear problem.

MSK_RES_ERR_INV_PROBLEM (1500)

Invalid problem type. Probably a nonconvex problem has been specified.

MSK_RES_ERR_INV_QCON_SUBI (1405)

Invalid value in qcsubi.

MSK_RES_ERR_INV_QCON_SUBJ (1406)

Invalid value in qcsubj.

MSK_RES_ERR_INV_QCON_SUBK (1404)

Invalid value in qcsubk.

MSK_RES_ERR_INV_QCON_VAL (1407)

Invalid value in qcval.

MSK_RES_ERR_INV_QOBJ_SUBI (1401)

Invalid value in qosubi.

MSK_RES_ERR_INV_QOBJ_SUBJ (1402)

Invalid value in qosubj.

MSK_RES_ERR_INV_QOBJ_VAL (1403)

Invalid value in qoval.

MSK_RES_ERR_INV_SK (1270)

Invalid status key code.

MSK_RES_ERR_INV_SK_STR (1269)

Invalid status key string encountered.

MSK_RES_ERR_INV_SKC (1267)

Invalid value in skc.

MSK_RES_ERR_INV_SKN (1274)

Invalid value in skn.

MSK_RES_ERR_INV_SKX (1268)

Invalid value in skx.

MSK_RES_ERR_INV_VAR_TYPE (1258)

An invalid variable type is specified for a variable.

MSK_RES_ERR_INVALID_ACCMODE (2520)

An invalid access mode is specified.

MSK_RES_ERR_INVALID_AIJ (1473)

 $a_{i,j}$ contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK_RES_ERR_INVALID_AMPL_STUB (3700)

Invalid AMPL stub.

MSK_RES_ERR_INVALID_BARVAR_NAME (1079)

An invalid symmetric matrix variable name is used.

MSK_RES_ERR_INVALID_COMPRESSION (1800)

Invalid compression type.

MSK_RES_ERR_INVALID_CON_NAME (1076)

An invalid constraint name is used.

MSK_RES_ERR_INVALID_CONE_NAME (1078)

An invalid cone name is used.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_CONES (4005)

The file format does not support a problem with conic constraints.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_GENERAL_NL (4010)

The file format does not support a problem with general nonlinear terms.

MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_SYM_MAT (4000)

The file format does not support a problem with symmetric matrix variables.

MSK_RES_ERR_INVALID_FILE_NAME (1056)

An invalid file name has been specified.

MSK_RES_ERR_INVALID_FORMAT_TYPE (1283)

Invalid format type.

MSK_RES_ERR_INVALID_IDX (1246)

A specified index is invalid.

MSK_RES_ERR_INVALID_IOMODE (1801)

Invalid io mode.

MSK_RES_ERR_INVALID_MAX_NUM (1247)

A specified index is invalid.

MSK_RES_ERR_INVALID_NAME_IN_SOL_FILE (1170)

An invalid name occurred in a solution file.

MSK_RES_ERR_INVALID_OBJ_NAME (1075)

An invalid objective name is specified.

MSK_RES_ERR_INVALID_OBJECTIVE_SENSE (1445)

An invalid objective sense is specified.

MSK_RES_ERR_INVALID_PROBLEM_TYPE (6000)

An invalid problem type.

MSK_RES_ERR_INVALID_SOL_FILE_NAME (1057)

An invalid file name has been specified.

MSK_RES_ERR_INVALID_STREAM (1062)

An invalid stream is referenced.

MSK_RES_ERR_INVALID_SURPLUS (1275)

Invalid surplus.

MSK_RES_ERR_INVALID_SYM_MAT_DIM (3950)

A sparse symmetric matrix of invalid dimension is specified.

MSK_RES_ERR_INVALID_TASK (1064)

The task is invalid.

MSK_RES_ERR_INVALID_UTF8 (2900)

An invalid UTF8 string is encountered.

MSK_RES_ERR_INVALID_VAR_NAME (1077)

An invalid variable name is used.

MSK_RES_ERR_INVALID_WCHAR (2901)

An invalid wchar string is encountered.

MSK_RES_ERR_INVALID_WHICHSOL (1228)

whichsol is invalid.

MSK_RES_ERR_JSON_DATA (1179)

Inconsistent data in JSON Task file

MSK_RES_ERR_JSON_FORMAT (1178)

Error in an JSON Task file

MSK_RES_ERR_JSON_MISSING_DATA (1180)

Missing data section in JSON task file.

MSK_RES_ERR_JSON_NUMBER_OVERFLOW (1177)

Invalid number entry - wrong type or value overflow.

MSK_RES_ERR_JSON_STRING (1176)

Error in JSON string.

MSK_RES_ERR_JSON_SYNTAX (1175)

Syntax error in an JSON data

MSK_RES_ERR_LAST (1262)

Invalid index last. A given index was out of expected range.

MSK_RES_ERR_LASTI (1286)

Invalid lasti.

MSK_RES_ERR_LASTJ (1288)

Invalid lastj.

MSK_RES_ERR_LAU_ARG_K (7012)

Invalid argument k.

MSK_RES_ERR_LAU_ARG_M (7010)

Invalid argument m.

MSK_RES_ERR_LAU_ARG_N (7011)

Invalid argument n.

MSK_RES_ERR_LAU_ARG_TRANS (7018)

Invalid argument trans.

MSK_RES_ERR_LAU_ARG_TRANSA (7015)

Invalid argument transa.

MSK_RES_ERR_LAU_ARG_TRANSB (7016)

Invalid argument transb.

MSK_RES_ERR_LAU_ARG_UPLO (7017)

Invalid argument uplo.

MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX (7002)

An invalid lower triangular matrix.

MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX (7019)

An invalid sparse symmetric matrix is specified. Note only the lower triangular part with no duplicates is specified.

MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE (7001)

A matrix is not positive definite.

MSK_RES_ERR_LAU_SINGULAR_MATRIX (7000)

A matrix is singular.

MSK_RES_ERR_LAU_UNKNOWN (7005)

An unknown error.

MSK_RES_ERR_LICENSE (1000)

Invalid license.

MSK_RES_ERR_LICENSE_CANNOT_ALLOCATE (1020)

The license system cannot allocate the memory required.

MSK_RES_ERR_LICENSE_CANNOT_CONNECT (1021)

MOSEK cannot connect to the license server. Most likely the license server is not up and running.

MSK_RES_ERR_LICENSE_EXPIRED (1001)

The license has expired.

MSK_RES_ERR_LICENSE_FEATURE (1018)

A requested feature is not available in the license file(s). Most likely due to an incorrect license system setup.

MSK_RES_ERR_LICENSE_INVALID_HOSTID (1025)

The host ID specified in the license file does not match the host ID of the computer.

MSK_RES_ERR_LICENSE_MAX (1016)

Maximum number of licenses is reached.

MSK_RES_ERR_LICENSE_MOSEKLM_DAEMON (1017)

The MOSEKLM license manager daemon is not up and running.

MSK_RES_ERR_LICENSE_NO_SERVER_LINE (1028)

There is no SERVER line in the license file. All non-zero license count features need at least one SERVER line.

MSK_RES_ERR_LICENSE_NO_SERVER_SUPPORT (1027)

The license server does not support the requested feature. Possible reasons for this error include:

- •The feature has expired.
- •The feature's start date is later than today's date.
- •The version requested is higher than feature's the highest supported version.
- •A corrupted license file.

Try restarting the license and inspect the license server debug file, usually called lmgrd.log.

MSK_RES_ERR_LICENSE_SERVER (1015)

The license server is not responding.

MSK_RES_ERR_LICENSE_SERVER_VERSION (1026)

The version specified in the checkout request is greater than the highest version number the daemon supports.

MSK_RES_ERR_LICENSE_VERSION (1002)

The license is valid for another version of **MOSEK**.

MSK_RES_ERR_LINK_FILE_DLL (1040)

A file cannot be linked to a stream in the DLL version.

MSK_RES_ERR_LIVING_TASKS (1066)

All tasks associated with an environment must be deleted before the environment is deleted. There are still some undeleted tasks.

MSK_RES_ERR_LOWER_BOUND_IS_A_NAN (1390)

The lower bound specified is not a number (nan).

MSK_RES_ERR_LP_DUP_SLACK_NAME (1152)

The name of the slack variable added to a ranged constraint already exists.

MSK_RES_ERR_LP_EMPTY (1151)

The problem cannot be written to an LP formatted file.

MSK_RES_ERR_LP_FILE_FORMAT (1157)

Syntax error in an LP file.

MSK_RES_ERR_LP_FORMAT (1160)

Syntax error in an LP file.

MSK_RES_ERR_LP_FREE_CONSTRAINT (1155)

Free constraints cannot be written in LP file format.

MSK_RES_ERR_LP_INCOMPATIBLE (1150)

The problem cannot be written to an LP formatted file.

MSK_RES_ERR_LP_INVALID_CON_NAME (1171)

A constraint name is invalid when used in an LP formatted file.

MSK_RES_ERR_LP_INVALID_VAR_NAME (1154)

A variable name is invalid when used in an LP formatted file.

MSK_RES_ERR_LP_WRITE_CONIC_PROBLEM (1163)

The problem contains cones that cannot be written to an LP formatted file.

MSK_RES_ERR_LP_WRITE_GECO_PROBLEM (1164)

The problem contains general convex terms that cannot be written to an LP formatted file.

MSK_RES_ERR_LU_MAX_NUM_TRIES (2800)

Could not compute the LU factors of the matrix within the maximum number of allowed tries.

MSK_RES_ERR_MAX_LEN_IS_TOO_SMALL (1289)

An maximum length that is too small has been specified.

MSK_RES_ERR_MAXNUMBARVAR (1242)

The maximum number of semidefinite variables specified is smaller than the number of semidefinite variables in the task.

MSK_RES_ERR_MAXNUMCON (1240)

The maximum number of constraints specified is smaller than the number of constraints in the task.

MSK_RES_ERR_MAXNUMCONE (1304)

The value specified for maxnumcone is too small.

MSK_RES_ERR_MAXNUMQNZ (1243)

The maximum number of non-zeros specified for the Q matrices is smaller than the number of non-zeros in the current Q matrices.

MSK_RES_ERR_MAXNUMVAR (1241)

The maximum number of variables specified is smaller than the number of variables in the task.

MSK_RES_ERR_MIO_INTERNAL (5010)

A fatal error occurred in the mixed integer optimizer. Please contact MOSEK support.

MSK_RES_ERR_MIO_INVALID_NODE_OPTIMIZER (7131)

An invalid node optimizer was selected for the problem type.

MSK_RES_ERR_MIO_INVALID_ROOT_OPTIMIZER (7130)

An invalid root optimizer was selected for the problem type.

MSK_RES_ERR_MIO_NO_OPTIMIZER (1551)

No optimizer is available for the current class of integer optimization problems.

MSK_RES_ERR_MIO_NOT_LOADED (1553)

The mixed-integer optimizer is not loaded.

MSK_RES_ERR_MISSING_LICENSE_FILE (1008)

MOSEK cannot license file or a token server. See the MOSEK installation manual for details.

MSK_RES_ERR_MIXED_CONIC_AND_NL (1501)

The problem contains nonlinear terms conic constraints. The requested operation cannot be applied to this type of problem.

MSK_RES_ERR_MPS_CONE_OVERLAP (1118)

A variable is specified to be a member of several cones.

MSK_RES_ERR_MPS_CONE_REPEAT (1119)

A variable is repeated within the CSECTION.

MSK_RES_ERR_MPS_CONE_TYPE (1117)

Invalid cone type specified in a CSECTION.

MSK_RES_ERR_MPS_DUPLICATE_Q_ELEMENT (1121)

Duplicate elements is specified in a Q matrix.

MSK_RES_ERR_MPS_FILE (1100)

An error occurred while reading an MPS file.

MSK_RES_ERR_MPS_INV_BOUND_KEY (1108)

An invalid bound key occurred in an MPS file.

MSK_RES_ERR_MPS_INV_CON_KEY (1107)

An invalid constraint key occurred in an MPS file.

MSK_RES_ERR_MPS_INV_FIELD (1101)

A field in the MPS file is invalid. Probably it is too wide.

MSK_RES_ERR_MPS_INV_MARKER (1102)

An invalid marker has been specified in the MPS file.

MSK_RES_ERR_MPS_INV_SEC_NAME (1109)

An invalid section name occurred in an MPS file.

MSK_RES_ERR_MPS_INV_SEC_ORDER (1115)

The sections in the MPS data file are not in the correct order.

MSK_RES_ERR_MPS_INVALID_OBJ_NAME (1128)

An invalid objective name is specified.

MSK_RES_ERR_MPS_INVALID_OBJSENSE (1122)

An invalid objective sense is specified.

MSK_RES_ERR_MPS_MUL_CON_NAME (1112)

A constraint name was specified multiple times in the ROWS section.

MSK_RES_ERR_MPS_MUL_CSEC (1116)

Multiple CSECTIONs are given the same name.

MSK_RES_ERR_MPS_MUL_QOBJ (1114)

The Q term in the objective is specified multiple times in the MPS data file.

MSK_RES_ERR_MPS_MUL_QSEC (1113)

Multiple QSECTIONs are specified for a constraint in the MPS data file.

MSK_RES_ERR_MPS_NO_OBJECTIVE (1110)

No objective is defined in an MPS file.

MSK_RES_ERR_MPS_NON_SYMMETRIC_Q (1120)

A non symmetric matrice has been speciefied.

MSK_RES_ERR_MPS_NULL_CON_NAME (1103)

An empty constraint name is used in an MPS file.

MSK_RES_ERR_MPS_NULL_VAR_NAME (1104)

An empty variable name is used in an MPS file.

MSK_RES_ERR_MPS_SPLITTED_VAR (1111)

All elements in a column of the A matrix must be specified consecutively. Hence, it is illegal to specify non-zero elements in A for variable 1, then for variable 2 and then variable 1 again.

MSK_RES_ERR_MPS_TAB_IN_FIELD2 (1125)

A tab char occurred in field 2.

MSK_RES_ERR_MPS_TAB_IN_FIELD3 (1126)

A tab char occurred in field 3.

MSK_RES_ERR_MPS_TAB_IN_FIELD5 (1127)

A tab char occurred in field 5.

MSK_RES_ERR_MPS_UNDEF_CON_NAME (1105)

An undefined constraint name occurred in an MPS file.

MSK_RES_ERR_MPS_UNDEF_VAR_NAME (1106)

An undefined variable name occurred in an MPS file.

MSK_RES_ERR_MUL_A_ELEMENT (1254)

An element in A is defined multiple times.

MSK_RES_ERR_NAME_IS_NULL (1760)

The name buffer is a NULL pointer.

MSK_RES_ERR_NAME_MAX_LEN (1750)

A name is longer than the buffer that is supposed to hold it.

MSK_RES_ERR_NAN_IN_BLC (1461)

 l^c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BLX (1471)

 l^x contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BUC (1462)

 u^c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_BUX (1472)

 u^x contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_C (1470)

c contains an invalid floating point value, i.e. a NaN.

MSK_RES_ERR_NAN_IN_DOUBLE_DATA (1450)

An invalid floating point value was used in some double data.

MSK_RES_ERR_NEGATIVE_APPEND (1264)

Cannot append a negative number.

MSK_RES_ERR_NEGATIVE_SURPLUS (1263)

Negative surplus.

MSK_RES_ERR_NEWER_DLL (1036)

The dynamic link library is newer than the specified version.

MSK_RES_ERR_NO_BARS_FOR_SOLUTION (3916)

There is no \bar{s} available for the solution specified. In particular note there are no \bar{s} defined for the basic and integer solutions.

MSK_RES_ERR_NO_BARX_FOR_SOLUTION (3915)

There is no \overline{X} available for the solution specified. In particular note there are no \overline{X} defined for the basic and integer solutions.

MSK_RES_ERR_NO_BASIS_SOL (1600)

No basic solution is defined.

MSK_RES_ERR_NO_DUAL_FOR_ITG_SOL (2950)

No dual information is available for the integer solution.

MSK_RES_ERR_NO_DUAL_INFEAS_CER (2001)

A certificate of infeasibility is not available.

MSK_RES_ERR_NO_INIT_ENV (1063)

env is not initialized.

MSK_RES_ERR_NO_OPTIMIZER_VAR_TYPE (1552)

No optimizer is available for this class of optimization problems.

MSK_RES_ERR_NO_PRIMAL_INFEAS_CER (2000)

A certificate of primal infeasibility is not available.

MSK_RES_ERR_NO_SNX_FOR_BAS_SOL (2953)

 s_n^x is not available for the basis solution.

MSK_RES_ERR_NO_SOLUTION_IN_CALLBACK (2500)

The required solution is not available.

MSK_RES_ERR_NON_UNIQUE_ARRAY (5000)

An array does not contain unique elements.

MSK_RES_ERR_NONCONVEX (1291)

The optimization problem is nonconvex.

MSK_RES_ERR_NONLINEAR_EQUALITY (1290)

The model contains a nonlinear equality which defines a nonconvex set.

MSK_RES_ERR_NONLINEAR_FUNCTIONS_NOT_ALLOWED (1428)

An operation that is invalid for problems with nonlinear functions defined has been attempted.

MSK_RES_ERR_NONLINEAR_RANGED (1292)

Nonlinear constraints with finite lower and upper bound always define a nonconvex feasible set.

MSK_RES_ERR_NR_ARGUMENTS (1199)

Incorrect number of function arguments.

MSK_RES_ERR_NULL_ENV (1060)

env is a NULL pointer.

MSK_RES_ERR_NULL_POINTER (1065)

An argument to a function is unexpectedly a NULL pointer.

MSK_RES_ERR_NULL_TASK (1061)

task is a NULL pointer.

MSK_RES_ERR_NUMCONLIM (1250)

Maximum number of constraints limit is exceeded.

MSK_RES_ERR_NUMVARLIM (1251)

Maximum number of variables limit is exceeded.

MSK_RES_ERR_OBJ_Q_NOT_NSD (1296)

The quadratic coefficient matrix in the objective is not negative semidefinite as expected for a maximization problem. The parameter $MSK_DPAR_CHECK_CONVEXITY_REL_TOL$ can be used to relax the convexity check.

MSK_RES_ERR_OBJ_Q_NOT_PSD (1295)

The quadratic coefficient matrix in the objective is not positive semidefinite as expected for a minimization problem. The parameter $MSK_DPAR_CHECK_CONVEXITY_REL_TOL$ can be used to relax the convexity check.

MSK_RES_ERR_OBJECTIVE_RANGE (1260)

Empty objective range.

MSK_RES_ERR_OLDER_DLL (1035)

The dynamic link library is older than the specified version.

MSK_RES_ERR_OPEN_DL (1030)

A dynamic link library could not be opened.

MSK_RES_ERR_OPF_FORMAT (1168)

Syntax error in an OPF file

MSK_RES_ERR_OPF_NEW_VARIABLE (1169)

Introducing new variables is now allowed. When a [variables] section is present, it is not allowed to introduce new variables later in the problem.

MSK_RES_ERR_OPF_PREMATURE_EOF (1172)

Premature end of file in an OPF file.

MSK_RES_ERR_OPTIMIZER_LICENSE (1013)

The optimizer required is not licensed.

MSK_RES_ERR_OVERFLOW (1590)

A computation produced an overflow i.e. a very large number.

MSK_RES_ERR_PARAM_INDEX (1210)

Parameter index is out of range.

MSK_RES_ERR_PARAM_IS_TOO_LARGE (1215)

The parameter value is too large.

MSK_RES_ERR_PARAM_IS_TOO_SMALL (1216)

The parameter value is too small.

MSK_RES_ERR_PARAM_NAME (1205)

The parameter name is not correct.

MSK_RES_ERR_PARAM_NAME_DOU (1206)

The parameter name is not correct for a double parameter.

MSK_RES_ERR_PARAM_NAME_INT (1207)

The parameter name is not correct for an integer parameter.

MSK_RES_ERR_PARAM_NAME_STR (1208)

The parameter name is not correct for a string parameter.

MSK_RES_ERR_PARAM_TYPE (1218)

The parameter type is invalid.

MSK_RES_ERR_PARAM_VALUE_STR (1217)

The parameter value string is incorrect.

MSK_RES_ERR_PLATFORM_NOT_LICENSED (1019)

A requested license feature is not available for the required platform.

MSK_RES_ERR_POSTSOLVE (1580)

An error occurred during the postsolve. Please contact MOSEK support.

MSK_RES_ERR_PRO_ITEM (1281)

An invalid problem is used.

MSK_RES_ERR_PROB_LICENSE (1006)

The software is not licensed to solve the problem.

MSK_RES_ERR_QCON_SUBI_TOO_LARGE (1409)

Invalid value in qcsubi.

MSK_RES_ERR_QCON_SUBI_TOO_SMALL (1408)

Invalid value in qcsubi.

MSK_RES_ERR_QCON_UPPER_TRIANGLE (1417)

An element in the upper triangle of a Q^k is specified. Only elements in the lower triangle should be specified.

MSK_RES_ERR_QOBJ_UPPER_TRIANGLE (1415)

An element in the upper triangle of Q^o is specified. Only elements in the lower triangle should be specified.

MSK_RES_ERR_READ_FORMAT (1090)

The specified format cannot be read.

MSK_RES_ERR_READ_LP_MISSING_END_TAG (1159)

Syntax error in LP file. Possibly missing End tag.

MSK_RES_ERR_READ_LP_NONEXISTING_NAME (1162)

A variable never occurred in objective or constraints.

MSK_RES_ERR_REMOVE_CONE_VARIABLE (1310)

A variable cannot be removed because it will make a cone invalid.

MSK_RES_ERR_REPAIR_INVALID_PROBLEM (1710)

The feasibility repair does not support the specified problem type.

MSK_RES_ERR_REPAIR_OPTIMIZATION_FAILED (1711)

Computation the optimal relaxation failed. The cause may have been numerical problems.

MSK_RES_ERR_SEN_BOUND_INVALID_LO (3054)

Analysis of lower bound requested for an index, where no lower bound exists.

MSK_RES_ERR_SEN_BOUND_INVALID_UP (3053)

Analysis of upper bound requested for an index, where no upper bound exists.

MSK_RES_ERR_SEN_FORMAT (3050)

Syntax error in sensitivity analysis file.

MSK_RES_ERR_SEN_INDEX_INVALID (3055)

Invalid range given in the sensitivity file.

MSK_RES_ERR_SEN_INDEX_RANGE (3052)

Index out of range in the sensitivity analysis file.

MSK_RES_ERR_SEN_INVALID_REGEXP (3056)

Syntax error in regexp or regexp longer than 1024.

MSK_RES_ERR_SEN_NUMERICAL (3058)

Numerical difficulties encountered performing the sensitivity analysis.

MSK_RES_ERR_SEN_SOLUTION_STATUS (3057)

No optimal solution found to the original problem given for sensitivity analysis.

MSK_RES_ERR_SEN_UNDEF_NAME (3051)

An undefined name was encountered in the sensitivity analysis file.

MSK_RES_ERR_SEN_UNHANDLED_PROBLEM_TYPE (3080)

Sensitivity analysis cannot be performed for the specified problem. Sensitivity analysis is only possible for linear problems.

MSK_RES_ERR_SERVER_CONNECT (8000)

Failed to connect to remote solver server. The server string or the port string were invalid, or the server did not accept connection.

MSK_RES_ERR_SERVER_PROTOCOL (8001)

Unexpected message or data from solver server.

MSK_RES_ERR_SERVER_STATUS (8002)

Server returned non-ok HTTP status code

MSK_RES_ERR_SERVER_TOKEN (8003)

The job ID specified is incorrect or invalid

MSK_RES_ERR_SIZE_LICENSE (1005)

The problem is bigger than the license.

MSK_RES_ERR_SIZE_LICENSE_CON (1010)

The problem has too many constraints to be solved with the available license.

MSK_RES_ERR_SIZE_LICENSE_INTVAR (1012)

The problem contains too many integer variables to be solved with the available license.

MSK_RES_ERR_SIZE_LICENSE_NUMCORES (3900)

The computer contains more cpu cores than the license allows for.

MSK_RES_ERR_SIZE_LICENSE_VAR (1011)

The problem has too many variables to be solved with the available license.

MSK_RES_ERR_SOL_FILE_INVALID_NUMBER (1350)

An invalid number is specified in a solution file.

MSK_RES_ERR_SOLITEM (1237)

The solution item number solitem is invalid. Please note that MSK_SOL_ITEM_SNX is invalid for the basic solution.

MSK_RES_ERR_SOLVER_PROBTYPE (1259)

Problem type does not match the chosen optimizer.

MSK_RES_ERR_SPACE (1051)

Out of space.

MSK_RES_ERR_SPACE_LEAKING (1080)

MOSEK is leaking memory. This can be due to either an incorrect use of MOSEK or a bug.

MSK_RES_ERR_SPACE_NO_INFO (1081)

No available information about the space usage.

MSK_RES_ERR_SYM_MAT_DUPLICATE (3944)

A value in a symmetric matric as been specified more than once.

MSK_RES_ERR_SYM_MAT_HUGE (1482)

A symmetric matrix contains a huge value in absolute size. The parameter $MSK_DPAR_DATA_SYM_MAT_TOL_HUGE$ controls when an $e_{i,j}$ is considered huge.

MSK_RES_ERR_SYM_MAT_INVALID (1480)

A symmetric matrix contains an invalid floating point value, i.e. a NaN or an infinite value.

MSK_RES_ERR_SYM_MAT_INVALID_COL_INDEX (3941)

A column index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_INVALID_ROW_INDEX (3940)

A row index specified for sparse symmetric matrix is invalid.

MSK_RES_ERR_SYM_MAT_INVALID_VALUE (3943)

The numerical value specified in a sparse symmetric matrix is not a value floating value.

MSK_RES_ERR_SYM_MAT_NOT_LOWER_TRINGULAR (3942)

Only the lower triangular part of sparse symmetric matrix should be specified.

MSK_RES_ERR_TASK_INCOMPATIBLE (2560)

The Task file is incompatible with this platform. This results from reading a file on a 32 bit platform generated on a 64 bit platform.

MSK_RES_ERR_TASK_INVALID (2561)

The Task file is invalid.

MSK_RES_ERR_TASK_WRITE (2562)

Failed to write the task file.

MSK_RES_ERR_THREAD_COND_INIT (1049)

Could not initialize a condition.

MSK_RES_ERR_THREAD_CREATE (1048)

Could not create a thread. This error may occur if a large number of environments are created and not deleted again. In any case it is a good practice to minimize the number of environments created

MSK_RES_ERR_THREAD_MUTEX_INIT (1045)

Could not initialize a mutex.

MSK_RES_ERR_THREAD_MUTEX_LOCK (1046)

Could not lock a mutex.

MSK_RES_ERR_THREAD_MUTEX_UNLOCK (1047)

Could not unlock a mutex.

MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC (7153)

The constraint is not conic representable.

MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD (7150)

The matrix defining the quadratric part of constraint is not positive semidefinite.

MSK_RES_ERR_TOCONIC_CONSTRAINT_FX (7151)

The quadratic constraint is an equality, thus not convex.

MSK_RES_ERR_TOCONIC_CONSTRAINT_RA (7152)

The quadratic constraint has finite lower and upper bound, and therefore it is not convex.

MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD (7155)

The matrix defining the quadratric part of the objective function is not positive semidefinite.

MSK_RES_ERR_TOO_SMALL_MAX_NUM_NZ (1245)

The maximum number of non-zeros specified is too small.

MSK_RES_ERR_TOO_SMALL_MAXNUMANZ (1252)

The maximum number of non-zeros specified for A is smaller than the number of non-zeros in the current A.

MSK_RES_ERR_UNB_STEP_SIZE (3100)

A step size in an optimizer was unexpectedly unbounded. For instance, if the step-size becomes unbounded in phase 1 of the simplex algorithm then an error occurs. Normally this will happen only if the problem is badly formulated. Please contact **MOSEK** support if this error occurs.

MSK_RES_ERR_UNDEF_SOLUTION (1265)

MOSEK has the following solution types:

- ulletan interior-point solution,
- •an basic solution,
- •and an integer solution.

Each optimizer may set one or more of these solutions; e.g by default a successful optimization with the interior-point optimizer defines the interior-point solution, and, for linear problems, also the basic solution. This error occurs when asking for a solution or for information about a solution that is not defined.

MSK_RES_ERR_UNDEFINED_OBJECTIVE_SENSE (1446)

The objective sense has not been specified before the optimization.

MSK_RES_ERR_UNHANDLED_SOLUTION_STATUS (6010)

Unhandled solution status.

MSK_RES_ERR_UNKNOWN (1050)

Unknown error.

MSK_RES_ERR_UPPER_BOUND_IS_A_NAN (1391)

The upper bound specified is not a number (nan).

MSK_RES_ERR_UPPER_TRIANGLE (6020)

An element in the upper triangle of a lower triangular matrix is specified.

MSK_RES_ERR_USER_FUNC_RET (1430)

An user function reported an error.

MSK_RES_ERR_USER_FUNC_RET_DATA (1431)

An user function returned invalid data.

MSK_RES_ERR_USER_NLO_EVAL (1433)

The user-defined nonlinear function reported an error.

MSK_RES_ERR_USER_NLO_EVAL_HESSUBI (1440)

The user-defined nonlinear function reported an invalid subscript in the Hessian.

MSK_RES_ERR_USER_NLO_EVAL_HESSUBJ (1441)

The user-defined nonlinear function reported an invalid subscript in the Hessian.

MSK_RES_ERR_USER_NLO_FUNC (1432)

The user-defined nonlinear function reported an error.

MSK_RES_ERR_WHICHITEM_NOT_ALLOWED (1238)

whichitem is unacceptable.

MSK_RES_ERR_WHICHSOL (1236)

The solution defined by which sol does not exists.

MSK_RES_ERR_WRITE_LP_FORMAT (1158)

Problem cannot be written as an LP file.

MSK_RES_ERR_WRITE_LP_NON_UNIQUE_NAME (1161)

An auto-generated name is not unique.

MSK_RES_ERR_WRITE_MPS_INVALID_NAME (1153)

An invalid name is created while writing an MPS file. Usually this will make the MPS file unreadable.

MSK_RES_ERR_WRITE_OPF_INVALID_VAR_NAME (1156)

Empty variable names cannot be written to OPF files.

MSK_RES_ERR_WRITING_FILE (1166)

An error occurred while writing file

MSK_RES_ERR_XML_INVALID_PROBLEM_TYPE (3600)

The problem type is not supported by the XML format.

MSK_RES_ERR_Y_IS_UNDEFINED (1449)

The solution item y is undefined.

10.3.3 Warning Codes

MSK_RES_WRN_ANA_ALMOST_INT_BOUNDS (904)

This warning is issued by the problem analyzer if a constraint is bound nearly integral.

MSK_RES_WRN_ANA_C_ZERO (901)

This warning is issued by the problem analyzer, if the coefficients in the linear part of the objective are all zero.

MSK_RES_WRN_ANA_CLOSE_BOUNDS (903)

This warning is issued by problem analyzer, if ranged constraints or variables with very close upper and lower bounds are detected. One should consider treating such constraints as equalities and such variables as constants.

MSK_RES_WRN_ANA_EMPTY_COLS (902)

This warning is issued by the problem analyzer, if columns, in which all coefficients are zero, are found.

MSK_RES_WRN_ANA_LARGE_BOUNDS (900)

This warning is issued by the problem analyzer, if one or more constraint or variable bounds are very large. One should consider omitting these bounds entirely by setting them to +inf or -inf.

MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG (807)

The initial value for one or more of the integer variables is not feasible.

MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG (810)

The construct solution requires an integer solution.

MSK_RES_WRN_CONSTRUCT_SOLUTION_INFEAS (805)

After fixing the integer variables at the suggested values then the problem is infeasible.

MSK_RES_WRN_DROPPED_NZ_QOBJ (201)

One or more non-zero elements were dropped in the Q matrix in the objective.

MSK_RES_WRN_DUPLICATE_BARVARIABLE_NAMES (852)

Two barvariable names are identical.

MSK_RES_WRN_DUPLICATE_CONE_NAMES (853)

Two cone names are identical.

MSK_RES_WRN_DUPLICATE_CONSTRAINT_NAMES (850)

Two constraint names are identical.

MSK_RES_WRN_DUPLICATE_VARIABLE_NAMES (851)

Two variable names are identical.

MSK_RES_WRN_ELIMINATOR_SPACE (801)

The eliminator is skipped at least once due to lack of space.

MSK_RES_WRN_EMPTY_NAME (502)

A variable or constraint name is empty. The output file may be invalid.

MSK_RES_WRN_IGNORE_INTEGER (250)

Ignored integer constraints.

MSK_RES_WRN_INCOMPLETE_LINEAR_DEPENDENCY_CHECK (800)

The linear dependency check(s) is incomplete. Normally this is not an important warning unless the optimization problem has been formulated with linear dependencies. Linear dependencies may prevent **MOSEK** from solving the problem.

MSK_RES_WRN_LARGE_AIJ (62)

A numerically large value is specified for an $a_{i,j}$ element in A. The parameter $MSK_DPAR_DATA_TOL_AIJ_LARGE$ controls when an $a_{i,j}$ is considered large.

MSK_RES_WRN_LARGE_BOUND (51)

A numerically large bound value is specified.

MSK_RES_WRN_LARGE_CJ (57)

A numerically large value is specified for one c_i .

MSK_RES_WRN_LARGE_CON_FX (54)

An equality constraint is fixed to a numerically large value. This can cause numerical problems.

MSK_RES_WRN_LARGE_LO_BOUND (52)

A numerically large lower bound value is specified.

MSK_RES_WRN_LARGE_UP_BOUND (53)

A numerically large upper bound value is specified.

MSK_RES_WRN_LICENSE_EXPIRE (500)

The license expires.

MSK_RES_WRN_LICENSE_FEATURE_EXPIRE (505)

The license expires.

MSK_RES_WRN_LICENSE_SERVER (501)

The license server is not responding.

MSK_RES_WRN_LP_DROP_VARIABLE (85)

Ignored a variable because the variable was not previously defined. Usually this implies that a variable appears in the bound section but not in the objective or the constraints.

MSK_RES_WRN_LP_OLD_QUAD_FORMAT (80)

Missing '/2' after quadratic expressions in bound or objective.

MSK_RES_WRN_MIO_INFEASIBLE_FINAL (270)

The final mixed-integer problem with all the integer variables fixed at their optimal values is infeasible.

MSK_RES_WRN_MPS_SPLIT_BOU_VECTOR (72)

A BOUNDS vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_MPS_SPLIT_RAN_VECTOR (71)

A RANGE vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_MPS_SPLIT_RHS_VECTOR (70)

An RHS vector is split into several nonadjacent parts in an MPS file.

MSK_RES_WRN_NAME_MAX_LEN (65)

A name is longer than the buffer that is supposed to hold it.

MSK_RES_WRN_NO_DUALIZER (950)

No automatic dualizer is available for the specified problem. The primal problem is solved.

MSK_RES_WRN_NO_GLOBAL_OPTIMIZER (251)

No global optimizer is available.

MSK_RES_WRN_NO_NONLINEAR_FUNCTION_WRITE (450)

The problem contains a general nonlinear function in either the objective or the constraints. Such a nonlinear function cannot be written to a disk file. Note that quadratic terms when inputted explicitly can be written to disk.

MSK_RES_WRN_NZ_IN_UPR_TRI (200)

Non-zero elements specified in the upper triangle of a matrix were ignored.

MSK_RES_WRN_OPEN_PARAM_FILE (50)

The parameter file could not be opened.

MSK_RES_WRN_PARAM_IGNORED_CMIO (516)

A parameter was ignored by the conic mixed integer optimizer.

MSK_RES_WRN_PARAM_NAME_DOU (510)

The parameter name is not recognized as a double parameter.

MSK_RES_WRN_PARAM_NAME_INT (511)

The parameter name is not recognized as a integer parameter.

MSK_RES_WRN_PARAM_NAME_STR (512)

The parameter name is not recognized as a string parameter.

MSK_RES_WRN_PARAM_STR_VALUE (515)

The string is not recognized as a symbolic value for the parameter.

MSK_RES_WRN_PRESOLVE_OUTOFSPACE (802)

The presolve is incomplete due to lack of space.

MSK_RES_WRN_QUAD_CONES_WITH_ROOT_FIXED_AT_ZERO (930)

For at least one quadratic cone the root is fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

MSK_RES_WRN_RQUAD_CONES_WITH_ROOT_FIXED_AT_ZERO (931)

For at least one rotated quadratic cone at least one of the root variables are fixed at (nearly) zero. This may cause problems such as a very large dual solution. Therefore, it is recommended to remove such cones before optimizing the problems, or to fix all the variables in the cone to 0.

MSK_RES_WRN_SOL_FILE_IGNORED_CON (351)

One or more lines in the constraint section were ignored when reading a solution file.

MSK_RES_WRN_SOL_FILE_IGNORED_VAR (352)

One or more lines in the variable section were ignored when reading a solution file.

MSK_RES_WRN_SOL_FILTER (300)

Invalid solution filter is specified.

MSK_RES_WRN_SPAR_MAX_LEN (66)

A value for a string parameter is longer than the buffer that is supposed to hold it.

MSK_RES_WRN_SYM_MAT_LARGE (960)

A numerically large value is specified for an $e_{i,j}$ element in E. The parameter $MSK_DPAR_DATA_SYM_MAT_TOL_LARGE$ controls when an $e_{i,j}$ is considered large.

MSK_RES_WRN_TOO_FEW_BASIS_VARS (400)

An incomplete basis has been specified. Too few basis variables are specified.

MSK_RES_WRN_TOO_MANY_BASIS_VARS (405)

A basis with too many variables has been specified.

MSK_RES_WRN_UNDEF_SOL_FILE_NAME (350)

Undefined name occurred in a solution.

MSK_RES_WRN_USING_GENERIC_NAMES (503)

Generic names are used because a name is not valid. For instance when writing an LP file the names must not contain blanks or start with a digit.

MSK_RES_WRN_WRITE_CHANGED_NAMES (803)

Some names were changed because they were invalid for the output file format.

MSK_RES_WRN_WRITE_DISCARDED_CFIX (804)

The fixed objective term could not be converted to a variable and was discarded in the output file.

MSK_RES_WRN_ZERO_AIJ (63)

One or more zero elements are specified in A.

MSK_RES_WRN_ZEROS_IN_SPARSE_COL (710)

One or more (near) zero elements are specified in a sparse column of a matrix. It is redundant to specify zero elements. Hence, it may indicate an error.

MSK_RES_WRN_ZEROS_IN_SPARSE_ROW (705)

One or more (near) zero elements are specified in a sparse row of a matrix. Since, it is redundant to specify zero elements then it may indicate an error.

10.4 Enumerations

MSKlanguagee

Language selection constants

MSK_LANG_ENG

English language selection

MSK_LANG_DAN

Danish language selection

MSKaccmodee

Constraint or variable access modes

MSK_ACC_VAR

Access data by columns (variable oriented)

MSK ACC CON

Access data by rows (constraint oriented)

${\tt MSKbasindtypee}$

Basis identification

MSK_BI_NEVER

Never do basis identification.

MSK_BI_ALWAYS

Basis identification is always performed even if the interior-point optimizer terminates abnormally.

MSK_BI_NO_ERROR

Basis identification is performed if the interior-point optimizer terminates without an error.

MSK_BI_IF_FEASIBLE

Basis identification is not performed if the interior-point optimizer terminates with a problem status saying that the problem is primal or dual infeasible.

MSK_BI_RESERVERED

Not currently in use.

${\tt MSKboundkeye}$

Bound keys

MSK BK LO

The constraint or variable has a finite lower bound and an infinite upper bound.

MSK_BK_UP

The constraint or variable has an infinite lower bound and an finite upper bound.

MSK_BK_FX

The constraint or variable is fixed.

MSK_BK_FR

The constraint or variable is free.

MSK_BK_RA

The constraint or variable is ranged.

MSKmarke

Mark

MSK_MARK_LO

The lower bound is selected for sensitivity analysis.

MSK_MARK_UP

The upper bound is selected for sensitivity analysis.

MSKsimdegene

Degeneracy strategies

MSK_SIM_DEGEN_NONE

The simplex optimizer should use no degeneration strategy.

MSK_SIM_DEGEN_FREE

The simplex optimizer chooses the degeneration strategy.

MSK_SIM_DEGEN_AGGRESSIVE

The simplex optimizer should use an aggressive degeneration strategy.

MSK_SIM_DEGEN_MODERATE

The simplex optimizer should use a moderate degeneration strategy.

MSK_SIM_DEGEN_MINIMUM

The simplex optimizer should use a minimum degeneration strategy.

MSKtransposee

Transposed matrix.

MSK_TRANSPOSE_NO

No transpose is applied.

MSK_TRANSPOSE_YES

A transpose is applied.

MSKuploe

Triangular part of a symmetric matrix.

MSK_UPLO_LO

Lower part.

MSK_UPLO_UP

Upper part

MSKsimreforme

Problem reformulation.

MSK_SIM_REFORMULATION_ON

Allow the simplex optimizer to reformulate the problem.

MSK_SIM_REFORMULATION_OFF

Disallow the simplex optimizer to reformulate the problem.

MSK_SIM_REFORMULATION_FREE

The simplex optimizer can choose freely.

10.4. Enumerations 133

MSK_SIM_REFORMULATION_AGGRESSIVE

The simplex optimizer should use an aggressive reformulation strategy.

MSKsimdupvece

Exploit duplicate columns.

MSK_SIM_EXPLOIT_DUPVEC_ON

Allow the simplex optimizer to exploit duplicated columns.

MSK_SIM_EXPLOIT_DUPVEC_OFF

Disallow the simplex optimizer to exploit duplicated columns.

MSK_SIM_EXPLOIT_DUPVEC_FREE

The simplex optimizer can choose freely.

MSKsimhotstarte

Hot-start type employed by the simplex optimizer

MSK_SIM_HOTSTART_NONE

The simplex optimizer performs a coldstart.

MSK_SIM_HOTSTART_FREE

The simplex optimize chooses the hot-start type.

MSK_SIM_HOTSTART_STATUS_KEYS

Only the status keys of the constraints and variables are used to choose the type of hot-start.

MSKintpnthotstarte

Hot-start type employed by the interior-point optimizers.

MSK_INTPNT_HOTSTART_NONE

The interior-point optimizer performs a coldstart.

MSK_INTPNT_HOTSTART_PRIMAL

The interior-point optimizer exploits the primal solution only.

MSK_INTPNT_HOTSTART_DUAL

The interior-point optimizer exploits the dual solution only.

MSK_INTPNT_HOTSTART_PRIMAL_DUAL

The interior-point optimizer exploits both the primal and dual solution.

MSKcallbackcodee

Progress call-back codes

MSK_CALLBACK_BEGIN_ROOT_CUTGEN

The call-back function is called when root cut generation is started.

MSK_CALLBACK_IM_ROOT_CUTGEN

The call-back is called from within root cut generation at an intermediate stage.

MSK CALLBACK END ROOT CUTGEN

The call-back function is called when root cut generation is is terminated.

${\tt MSK_CALLBACK_BEGIN_OPTIMIZER}$

The call-back function is called when the optimizer is started.

MSK_CALLBACK_END_OPTIMIZER

The call-back function is called when the optimizer is terminated.

MSK_CALLBACK_BEGIN_PRESOLVE

The call-back function is called when the presolve is started.

MSK_CALLBACK_UPDATE_PRESOLVE

The call-back function is called from within the presolve procedure.

MSK_CALLBACK_IM_PRESOLVE

The call-back function is called from within the presolve procedure at an intermediate stage.

MSK_CALLBACK_END_PRESOLVE

The call-back function is called when the presolve is completed.

MSK_CALLBACK_BEGIN_INTPNT

The call-back function is called when the interior-point optimizer is started.

MSK_CALLBACK_INTPNT

The call-back function is called from within the interior-point optimizer after the information database has been updated.

MSK_CALLBACK_IM_INTPNT

The call-back function is called at an intermediate stage within the interior-point optimizer where the information database has not been updated.

MSK_CALLBACK_END_INTPNT

The call-back function is called when the interior-point optimizer is terminated.

MSK_CALLBACK_BEGIN_CONIC

The call-back function is called when the conic optimizer is started.

MSK_CALLBACK_CONIC

The call-back function is called from within the conic optimizer after the information database has been updated.

MSK_CALLBACK_IM_CONIC

The call-back function is called at an intermediate stage within the conic optimizer where the information database has not been updated.

MSK_CALLBACK_END_CONIC

The call-back function is called when the conic optimizer is terminated.

MSK_CALLBACK_PRIMAL_SIMPLEX

The call-back function is called from within the primal simplex optimizer.

MSK_CALLBACK_DUAL_SIMPLEX

The call-back function is called from within the dual simplex optimizer.

MSK_CALLBACK_BEGIN_BI

The basis identification procedure has been started.

MSK_CALLBACK_IM_BI

The call-back function is called from within the basis identification procedure at an intermediate point.

MSK_CALLBACK_END_BI

The call-back function is called when the basis identification procedure is terminated.

MSK_CALLBACK_BEGIN_PRIMAL_BI

The call-back function is called from within the basis identification procedure when the primal phase is started.

MSK_CALLBACK_IM_PRIMAL_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the primal phase.

MSK_CALLBACK_UPDATE_PRIMAL_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the primal phase.

MSK_CALLBACK_END_PRIMAL_BI

The call-back function is called from within the basis identification procedure when the primal phase is terminated.

MSK_CALLBACK_BEGIN_DUAL_BI

The call-back function is called from within the basis identification procedure when the dual phase is started.

10.4. Enumerations 135

MSK_CALLBACK_IM_DUAL_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the dual phase.

MSK_CALLBACK_UPDATE_DUAL_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the dual phase.

MSK_CALLBACK_END_DUAL_BI

The call-back function is called from within the basis identification procedure when the dual phase is terminated.

MSK_CALLBACK_BEGIN_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the simplex clean-up phase is started.

MSK_CALLBACK_IM_SIMPLEX_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the simplex clean-up phase. The frequency of the call-backs is controlled by the $MSK_IPAR_LOG_SIM_FREQ$ parameter.

MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the primal simplex clean-up phase is started.

MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the primal simplex clean-up phase. The frequency of the call-backs is controlled by the $MSK_IPAR_LOG_SIM_FREQ$ parameter.

MSK_CALLBACK_END_PRIMAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the primal clean-up phase is terminated.

MSK_CALLBACK_BEGIN_PRIMAL_DUAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the primal-dual simplex clean-up phase is started.

MSK_CALLBACK_UPDATE_PRIMAL_DUAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the primal-dual simplex clean-up phase. The frequency of the call-backs is controlled by the $MSK_IPAR_LOG_SIM_FREQ$ parameter.

MSK_CALLBACK_END_PRIMAL_DUAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the primal-dual clean-up phase is terminated.

MSK_CALLBACK_BEGIN_DUAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the dual simplex clean-up phase is started.

MSK_CALLBACK_UPDATE_DUAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure at an intermediate point in the dual simplex clean-up phase. The frequency of the call-backs is controlled by the $MSK_IPAR_LOG_SIM_FREQ$ parameter.

MSK_CALLBACK_END_DUAL_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the dual clean-up phase is terminated.

MSK_CALLBACK_END_SIMPLEX_BI

The call-back function is called from within the basis identification procedure when the simplex clean-up phase is terminated.

MSK_CALLBACK_BEGIN_MIO

The call-back function is called when the mixed-integer optimizer is started.

MSK_CALLBACK_IM_MIO

The call-back function is called at an intermediate point in the mixed-integer optimizer.

MSK_CALLBACK_NEW_INT_MIO

The call-back function is called after a new integer solution has been located by the mixed-integer optimizer.

MSK_CALLBACK_END_MIO

The call-back function is called when the mixed-integer optimizer is terminated.

MSK_CALLBACK_BEGIN_SIMPLEX

The call-back function is called when the simplex optimizer is started.

MSK_CALLBACK_BEGIN_DUAL_SIMPLEX

The call-back function is called when the dual simplex optimizer started.

MSK_CALLBACK_IM_DUAL_SIMPLEX

The call-back function is called at an intermediate point in the dual simplex optimizer.

MSK_CALLBACK_UPDATE_DUAL_SIMPLEX

The call-back function is called in the dual simplex optimizer.

MSK_CALLBACK_END_DUAL_SIMPLEX

The call-back function is called when the dual simplex optimizer is terminated.

MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX

The call-back function is called when the primal simplex optimizer is started.

MSK_CALLBACK_IM_PRIMAL_SIMPLEX

The call-back function is called at an intermediate point in the primal simplex optimizer.

MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX

The call-back function is called in the primal simplex optimizer.

MSK_CALLBACK_END_PRIMAL_SIMPLEX

The call-back function is called when the primal simplex optimizer is terminated.

MSK_CALLBACK_BEGIN_PRIMAL_DUAL_SIMPLEX

The call-back function is called when the primal-dual simplex optimizer is started.

MSK_CALLBACK_IM_PRIMAL_DUAL_SIMPLEX

The call-back function is called at an intermediate point in the primal-dual simplex optimizer.

MSK_CALLBACK_UPDATE_PRIMAL_DUAL_SIMPLEX

The call-back function is called in the primal-dual simplex optimizer.

MSK_CALLBACK_END_PRIMAL_DUAL_SIMPLEX

The call-back function is called when the primal-dual simplex optimizer is terminated.

MSK_CALLBACK_END_SIMPLEX

The call-back function is called when the simplex optimizer is terminated.

MSK_CALLBACK_BEGIN_INFEAS_ANA

The call-back function is called when the infeasibility analyzer is started.

MSK_CALLBACK_END_INFEAS_ANA

The call-back function is called when the infeasibility analyzer is terminated.

MSK_CALLBACK_IM_PRIMAL_SENSIVITY

The call-back function is called at an intermediate stage of the primal sensitivity analysis.

MSK_CALLBACK_IM_DUAL_SENSIVITY

The call-back function is called at an intermediate stage of the dual sensitivity analysis.

MSK_CALLBACK_IM_MIO_INTPNT

The call-back function is called at an intermediate point in the mixed-integer optimizer while running the interior-point optimizer.

10.4. Enumerations 137

MSK_CALLBACK_IM_MIO_PRIMAL_SIMPLEX

The call-back function is called at an intermediate point in the mixed-integer optimizer while running the primal simplex optimizer.

MSK_CALLBACK_IM_MIO_DUAL_SIMPLEX

The call-back function is called at an intermediate point in the mixed-integer optimizer while running the dual simplex optimizer.

MSK_CALLBACK_BEGIN_PRIMAL_SETUP_BI

The call-back function is called when the primal BI setup is started.

MSK_CALLBACK_END_PRIMAL_SETUP_BI

The call-back function is called when the primal BI setup is terminated.

MSK_CALLBACK_BEGIN_DUAL_SETUP_BI

The call-back function is called when the dual BI phase is started.

MSK_CALLBACK_END_DUAL_SETUP_BI

The call-back function is called when the dual BI phase is terminated.

MSK_CALLBACK_BEGIN_PRIMAL_SENSITIVITY

Primal sensitivity analysis is started.

MSK_CALLBACK_END_PRIMAL_SENSITIVITY

Primal sensitivity analysis is terminated.

MSK_CALLBACK_BEGIN_DUAL_SENSITIVITY

Dual sensitivity analysis is started.

MSK_CALLBACK_END_DUAL_SENSITIVITY

Dual sensitivity analysis is terminated.

MSK_CALLBACK_BEGIN_LICENSE_WAIT

Begin waiting for license.

MSK_CALLBACK_END_LICENSE_WAIT

End waiting for license.

MSK_CALLBACK_IM_LICENSE_WAIT

MOSEK is waiting for a license.

${\tt MSK_CALLBACK_BEGIN_QCQO_REFORMULATE}$

Begin QCQO reformulation.

MSK_CALLBACK_END_QCQO_REFORMULATE

End QCQO reformulation.

MSK_CALLBACK_IM_QO_REFORMULATE

The call-back function is called at an intermediate stage of the conic quadratic reformulation.

MSK_CALLBACK_BEGIN_TO_CONIC

Begin conic reformulation.

MSK_CALLBACK_END_TO_CONIC

End conic reformulation.

MSK_CALLBACK_BEGIN_FULL_CONVEXITY_CHECK

Begin full convexity check.

MSK_CALLBACK_END_FULL_CONVEXITY_CHECK

End full convexity check.

MSK_CALLBACK_IM_FULL_CONVEXITY_CHECK

The call-back function is called at an intermediate stage of the full convexity check.

MSK_CALLBACK_BEGIN_PRIMAL_REPAIR

Begin primal feasibility repair.

MSK_CALLBACK_END_PRIMAL_REPAIR

End primal feasibility repair.

MSK_CALLBACK_BEGIN_READ

MOSEK has started reading a problem file.

MSK_CALLBACK_IM_READ

Intermediate stage in reading.

MSK_CALLBACK_END_READ

MOSEK has finished reading a problem file.

MSK_CALLBACK_BEGIN_WRITE

MOSEK has started writing a problem file.

MSK_CALLBACK_END_WRITE

MOSEK has finished writing a problem file.

MSK_CALLBACK_READ_OPF_SECTION

A chunk of Q non-zeros has been read from a problem file.

MSK_CALLBACK_IM_LU

The call-back function is called from within the LU factorization procedure at an intermediate point.

MSK_CALLBACK_IM_ORDER

The call-back function is called from within the matrix ordering procedure at an intermediate point.

MSK_CALLBACK_IM_SIMPLEX

The call-back function is called from within the simplex optimizer at an intermediate point.

MSK_CALLBACK_READ_OPF

The call-back function is called from the OPF reader.

MSK_CALLBACK_WRITE_OPF

The call-back function is called from the OPF writer.

MSK_CALLBACK_SOLVING_REMOTE

The call-back function is called while the task is being solved on a remote server.

${\tt MSKcheckconvexitytypee}$

Types of convexity checks.

MSK_CHECK_CONVEXITY_NONE

No convexity check.

MSK_CHECK_CONVEXITY_SIMPLE

Perform simple and fast convexity check.

MSK_CHECK_CONVEXITY_FULL

Perform a full convexity check.

MSKcompresstypee

Compression types

MSK_COMPRESS_NONE

No compression is used.

MSK_COMPRESS_FREE

The type of compression used is chosen automatically.

MSK_COMPRESS_GZIP

The type of compression used is gzip compatible.

MSKconetypee

Cone types

10.4. Enumerations 139

MSK_CT_QUAD

The cone is a quadratic cone.

MSK_CT_RQUAD

The cone is a rotated quadratic cone.

MSKnametypee

Name types

MSK_NAME_TYPE_GEN

General names. However, no duplicate and blank names are allowed.

MSK_NAME_TYPE_MPS

MPS type names.

MSK_NAME_TYPE_LP

LP type names.

MSKsymmattypee

Cone types

MSK_SYMMAT_TYPE_SPARSE

Sparse symmetric matrix.

MSKdataformate

Data format types

MSK_DATA_FORMAT_EXTENSION

The file extension is used to determine the data file format.

MSK_DATA_FORMAT_MPS

The data file is MPS formatted.

MSK_DATA_FORMAT_LP

The data file is LP formatted.

MSK_DATA_FORMAT_OP

The data file is an optimization problem formatted file.

MSK_DATA_FORMAT_XML

The data file is an XML formatted file.

MSK_DATA_FORMAT_FREE_MPS

The data a free MPS formatted file.

MSK_DATA_FORMAT_TASK

Generic task dump file.

MSK_DATA_FORMAT_CB

Conic benchmark format,

MSK_DATA_FORMAT_JSON_TASK

JSON based task format.

${\tt MSKdinfiteme}$

Double information items

MSK_DINF_BI_TIME

Time spent within the basis identification procedure since its invocation.

MSK_DINF_BI_PRIMAL_TIME

Time spent within the primal phase of the basis identification procedure since its invocation.

MSK_DINF_BI_DUAL_TIME

Time spent within the dual phase basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_TIME

Time spent within the clean-up phase of the basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_PRIMAL_TIME

Time spent within the primal clean-up optimizer of the basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_PRIMAL_DUAL_TIME

Time spent within the primal-dual clean-up optimizer of the basis identification procedure since its invocation.

MSK_DINF_BI_CLEAN_DUAL_TIME

Time spent within the dual clean-up optimizer of the basis identification procedure since its invocation.

MSK_DINF_INTPNT_TIME

Time spent within the interior-point optimizer since its invocation.

MSK_DINF_INTPNT_ORDER_TIME

Order time (in seconds).

MSK_DINF_INTPNT_PRIMAL_OBJ

Primal objective value reported by the interior-point optimizer.

MSK_DINF_INTPNT_DUAL_OBJ

Dual objective value reported by the interior-point optimizer.

MSK_DINF_INTPNT_PRIMAL_FEAS

Primal feasibility measure reported by the interior-point optimizers. (For the interior-point optimizer this measure does not directly related to the original problem because a homogeneous model is employed).

MSK_DINF_INTPNT_DUAL_FEAS

Dual feasibility measure reported by the interior-point optimizer. (For the interior-point optimizer this measure does not directly related to the original problem because a homogeneous model is employed.)

MSK_DINF_INTPNT_OPT_STATUS

This measure should converge to +1 if the problem has a primal-dual optimal solution, and converge to -1 if problem is (strictly) primal or dual infeasible. If the measure converges to another constant, or fails to settle, the problem is usually ill-posed.

MSK_DINF_SIM_TIME

Time spent in the simplex optimizer since invoking it.

MSK_DINF_SIM_PRIMAL_TIME

Time spent in the primal simplex optimizer since invoking it.

MSK_DINF_SIM_DUAL_TIME

Time spent in the dual simplex optimizer since invoking it.

MSK_DINF_SIM_PRIMAL_DUAL_TIME

Time spent in the primal-dual simplex optimizer since invoking it.

MSK_DINF_SIM_OBJ

Objective value reported by the simplex optimizer.

MSK_DINF_SIM_FEAS

Feasibility measure reported by the simplex optimizer.

MSK_DINF_MIO_TIME

Time spent in the mixed-integer optimizer.

MSK_DINF_MIO_ROOT_PRESOLVE_TIME

Time spent in while presolving the root relaxation.

MSK_DINF_MIO_ROOT_OPTIMIZER_TIME

Time spent in the optimizer while solving the root relaxation.

MSK_DINF_MIO_OPTIMIZER_TIME

Total time spent in the optimizer.

MSK_DINF_MIO_HEURISTIC_TIME

Total time spent in the optimizer.

MSK_DINF_TO_CONIC_TIME

Time spent in the last to conic reformulation.

MSK_DINF_MIO_CONSTRUCT_SOLUTION_OBJ

If **MOSEK** has successfully constructed an integer feasible solution, then this item contains the optimal objective value corresponding to the feasible solution.

MSK_DINF_MIO_OBJ_INT

The primal objective value corresponding to the best integer feasible solution. Please note that at least one integer feasible solution must have located i.e. check $|MSK_IINF_MIO_NUM_INT_SOLUTIONS|$.

MSK_DINF_MIO_OBJ_BOUND

The best known bound on the objective function. This value is undefined until at least one relaxation has been solved: To see if this is the case check that $| MSK_IINF_MIO_NUM_RELAX|$ is strictly positive.

MSK_DINF_MIO_OBJ_REL_GAP

Given that the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the relative gap defined by

```
\frac{|(\text{objective value of feasible solution}) - (\text{objective bound})|}{\max(\delta, |(\text{objective value of feasible solution})|)}.
```

where δ is given by the parameter $MSK_DPAR_MIO_REL_GAP_CONST$. Otherwise it has the value -1.0.

MSK_DINF_MIO_OBJ_ABS_GAP

Given the mixed-integer optimizer has computed a feasible solution and a bound on the optimal objective value, then this item contains the absolute gap defined by

|(objective value of feasible solution) – (objective bound)|.

Otherwise it has the value -1.0.

MSK_DINF_MIO_USER_OBJ_CUT

If the objective cut is used, then this information item has the value of the cut.

MSK_DINF_MIO_CMIR_SEPARATION_TIME

Separation time for CMIR cuts.

MSK_DINF_MIO_CLIQUE_SEPARATION_TIME

Separation time for clique cuts.

MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME

Separation time for knapsack cover.

MSK_DINF_MIO_GMI_SEPARATION_TIME

Separation time for GMI cuts.

MSK_DINF_MIO_IMPLIED_BOUND_TIME

Separation time for implied bound cuts.

MSK_DINF_MIO_ROOT_CUTGEN_TIME

Total time for cut generation.

MSK_DINF_MIO_PROBING_TIME

Total time for probing.

MSK_DINF_OPTIMIZER_TIME

Total time spent in the optimizer since it was invoked.

MSK_DINF_PRESOLVE_TIME

Total time (in seconds) spent in the presolve since it was invoked.

MSK_DINF_MIO_DUAL_BOUND_AFTER_PRESOLVE

Value of the dual bound after presolve but before cut generation.

MSK_DINF_PRESOLVE_ELI_TIME

Total time spent in the eliminator since the presolve was invoked.

MSK_DINF_PRESOLVE_LINDEP_TIME

Total time spent in the linear dependency checker since the presolve was invoked.

MSK_DINF_RD_TIME

Time spent reading the data file.

MSK_DINF_SOL_ITR_PRIMAL_OBJ

Primal objective value of the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLCON

Maximal primal bound violation for x^c in the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLVAR

Maximal primal bound violation for x^x in the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLBARVAR

Maximal primal bound violation for \overline{X} in the interior-point solution.

MSK_DINF_SOL_ITR_PVIOLCONES

Maximal primal violation for primal conic constraints in the interior-point solution.

MSK_DINF_SOL_ITR_DUAL_OBJ

Dual objective value of the interior-point solution.

MSK_DINF_SOL_ITR_DVIOLCON

Maximal dual bound violation for x^c in the interior-point solution.

MSK_DINF_SOL_ITR_DVIOLVAR

Maximal dual bound violation for x^x in the interior-point solution.

MSK_DINF_SOL_ITR_DVIOLBARVAR

Maximal dual bound violation for \overline{X} in the interior-point solution.

MSK_DINF_SOL_ITR_DVIOLCONES

Maximal dual violation for dual conic constraints in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_XC

Infinity norm of x^c in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_XX

Infinity norm of x^x in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_BARX

Infinity norm of \overline{X} in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_Y

Infinity norm of y in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SLC

Infinity norm of s_I^c in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SUC

Infinity norm of s_u^c in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SLX

Infinity norm of s_I^x in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SUX

Infinity norm of s_u^X in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_SNX

Infinity norm of s_n^x in the interior-point solution.

MSK_DINF_SOL_ITR_NRM_BARS

Infinity norm of \overline{S} in the interior-point solution.

MSK_DINF_SOL_BAS_PRIMAL_OBJ

Primal objective value of the basic solution.

MSK_DINF_SOL_BAS_PVIOLCON

Maximal primal bound violation for x^c in the basic solution.

MSK_DINF_SOL_BAS_PVIOLVAR

Maximal primal bound violation for x^x in the basic solution.

MSK_DINF_SOL_BAS_DUAL_OBJ

Dual objective value of the basic solution.

MSK_DINF_SOL_BAS_DVIOLCON

Maximal dual bound violation for x^c in the basic solution.

MSK_DINF_SOL_BAS_DVIOLVAR

Maximal dual bound violation for x^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_XC

Infinity norm of x^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_XX

Infinity norm of x^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_BARX

Infinity norm of \overline{X} in the basic solution.

MSK_DINF_SOL_BAS_NRM_Y

Infinity norm of y in the basic solution.

MSK_DINF_SOL_BAS_NRM_SLC

Infinity norm of s_l^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_SUC

Infinity norm of s_u^c in the basic solution.

MSK_DINF_SOL_BAS_NRM_SLX

Infinity norm of s_l^x in the basic solution.

MSK_DINF_SOL_BAS_NRM_SUX

Infinity norm of s_n^X in the basic solution.

MSK_DINF_SOL_ITG_PRIMAL_OBJ

Primal objective value of the integer solution.

MSK_DINF_SOL_ITG_PVIOLCON

Maximal primal bound violation for x^c in the integer solution.

${\tt MSK_DINF_SOL_ITG_PVIOLVAR}$

Maximal primal bound violation for x^x in the integer solution.

MSK_DINF_SOL_ITG_PVIOLBARVAR

Maximal primal bound violation for \overline{X} in the integer solution.

MSK_DINF_SOL_ITG_PVIOLCONES

Maximal primal violation for primal conic constraints in the integer solution.

MSK_DINF_SOL_ITG_PVIOLITG

Maximal violation for the integer constraints in the integer solution.

MSK_DINF_SOL_ITG_NRM_XC

Infinity norm of x^c in the integer solution.

MSK_DINF_SOL_ITG_NRM_XX

Infinity norm of x^x in the integer solution.

MSK_DINF_SOL_ITG_NRM_BARX

Infinity norm of \overline{X} in the integer solution.

MSK_DINF_INTPNT_FACTOR_NUM_FLOPS

An estimate of the number of flops used in the factorization.

MSK_DINF_QCQO_REFORMULATE_TIME

Time spent with conic quadratic reformulation.

MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION

Maximum absolute diagonal perturbation occuring during the QCQO reformulation.

MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING

Worst Cholesky diagonal scaling.

MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING

Worst Cholesky column scaling.

MSK_DINF_PRIMAL_REPAIR_PENALTY_OBJ

The optimal objective value of the penalty function.

MSKfeaturee

License feature

MSK_FEATURE_PTS

Base system.

MSK_FEATURE_PTON

Nonlinear extension.

MSKliinfiteme

Long integer information items.

MSK_LIINF_MIO_PRESOLVED_ANZ

Number of non-zero entries in the constraint matrix of presolved problem.

MSK_LIINF_MIO_SIMPLEX_ITER

Number of simplex iterations performed by the mixed-integer optimizer.

MSK_LIINF_MIO_INTPNT_ITER

Number of interior-point iterations performed by the mixed-integer optimizer.

MSK_LIINF_BI_PRIMAL_ITER

Number of primal pivots performed in the basis identification.

MSK_LIINF_BI_DUAL_ITER

Number of dual pivots performed in the basis identification.

MSK_LIINF_BI_CLEAN_PRIMAL_ITER

Number of primal clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_PRIMAL_DUAL_ITER

Number of primal-dual clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_DUAL_ITER

Number of dual clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_PRIMAL_DEG_ITER

Number of primal degenerate clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_PRIMAL_DUAL_SUB_ITER

Number of primal-dual subproblem clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_PRIMAL_DUAL_DEG_ITER

Number of primal-dual degenerate clean iterations performed in the basis identification.

MSK_LIINF_BI_CLEAN_DUAL_DEG_ITER

Number of dual degenerate clean iterations performed in the basis identification.

MSK_LIINF_INTPNT_FACTOR_NUM_NZ

Number of non-zeros in factorization.

MSK_LIINF_RD_NUMANZ

Number of non-zeros in A that is read.

MSK_LIINF_RD_NUMQNZ

Number of Q non-zeros.

MSK_LIINF_MIO_SIM_MAXITER_SETBACKS

Number of times the simplex optimizer has hit the maximum iteration limit when reoptimizing.

MSKiinfiteme

Integer information items.

MSK_IINF_ANA_PRO_NUM_CON

Number of constraints in the problem.

MSK_IINF_ANA_PRO_NUM_CON_LO

Number of constraints with a lower bound and an infinite upper bound.

MSK_IINF_ANA_PRO_NUM_CON_UP

Number of constraints with an upper bound and an infinite lower bound.

MSK_IINF_ANA_PRO_NUM_CON_RA

Number of constraints with finite lower and upper bounds.

MSK_IINF_ANA_PRO_NUM_CON_EQ

Number of equality constraints.

MSK_IINF_ANA_PRO_NUM_CON_FR

Number of unbounded constraints.

MSK_IINF_ANA_PRO_NUM_VAR

Number of variables in the problem.

MSK_IINF_ANA_PRO_NUM_VAR_LO

Number of variables with a lower bound and an infinite upper bound.

MSK_IINF_ANA_PRO_NUM_VAR_UP

Number of variables with an upper bound and an infinite lower bound. This value is set by

MSK_IINF_ANA_PRO_NUM_VAR_RA

Number of variables with finite lower and upper bounds.

MSK_IINF_ANA_PRO_NUM_VAR_EQ

Number of fixed variables.

MSK_IINF_ANA_PRO_NUM_VAR_FR

Number of free variables.

MSK_IINF_ANA_PRO_NUM_VAR_CONT

Number of continuous variables.

MSK_IINF_ANA_PRO_NUM_VAR_BIN

Number of binary (0-1) variables.

MSK_IINF_ANA_PRO_NUM_VAR_INT

Number of general integer variables.

MSK_IINF_OPTIMIZE_RESPONSE

The response code returned by optimize.

MSK_IINF_INTPNT_ITER

Number of interior-point iterations since invoking the interior-point optimizer.

MSK_IINF_INTPNT_FACTOR_DIM_DENSE

Dimension of the dense sub system in factorization.

MSK_IINF_INTPNT_SOLVE_DUAL

Non-zero if the interior-point optimizer is solving the dual problem.

MSK_IINF_MIO_NODE_DEPTH

Depth of the last node solved.

MSK_IINF_MIO_NUMCON

Number of constraints in the problem solved by the mixed-integer optimizer.

MSK_IINF_MIO_NUMVAR

Number of variables in the problem solved by the mixed-integer optimizer.

MSK_IINF_MIO_NUMINT

Number of integer variables in the problem solved be the mixed-integer optimizer.

MSK_IINF_MIO_PRESOLVED_NUMCONT

Number of continuous variables in the problem solved be the mixed-integer optimizer.

MSK_IINF_MIO_PRESOLVED_NUMBIN

Number of binary variables in the problem solved be the mixed-integer optimizer.

MSK_IINF_MIO_PRESOLVED_NUMCON

Number of constraints in the presolved problem.

MSK_IINF_MIO_PRESOLVED_NUMVAR

Number of variables in the presolved problem.

MSK_IINF_MIO_PRESOLVED_NUMINT

Number of integer variables in the presolved problem.

MSK_IINF_MIO_CLIQUE_TABLE_SIZE

Size of the clique table.

MSK_IINF_MIO_CONSTRUCT_SOLUTION

If this item has the value 0, then **MOSEK** did not try to construct an initial integer feasible solution. If the item has a positive value, then **MOSEK** successfully constructed an initial integer feasible solution.

MSK_IINF_MIO_CONSTRUCT_NUM_ROUNDINGS

Number of values in the integer solution that is rounded to an integer value.

MSK_IINF_MIO_NUM_INT_SOLUTIONS

Number of integer feasible solutions that has been found.

MSK_IINF_MIO_OBJ_BOUND_DEFINED

Non-zero if a valid objective bound has been found, otherwise zero.

MSK_IINF_MIO_NUM_ACTIVE_NODES

Number of active branch bound nodes.

MSK_IINF_MIO_NUM_RELAX

Number of relaxations solved during the optimization.

MSK_IINF_MIO_NUM_BRANCH

Number of branches performed during the optimization.

MSK_IINF_MIO_TOTAL_NUM_CUTS

Total number of cuts generated by the mixed-integer optimizer.

MSK_IINF_MIO_NUM_CMIR_CUTS

Number of Complemented Mixed Integer Rounding (CMIR) cuts.

MSK_IINF_MIO_NUM_CLIQUE_CUTS

Number of clique cuts.

MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS

Number of implied bound cuts.

MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS

Number of clique cuts.

MSK_IINF_MIO_NUM_GOMORY_CUTS

Number of Gomory cuts.

MSK_IINF_MIO_NUM_REPEATED_PRESOLVE

Number of times presolve was repeated at root.

MSK_IINF_MIO_INITIAL_SOLUTION

Is non-zero if an initial integer solution is specified.

MSK_IINF_MIO_USER_OBJ_CUT

If it is non-zero, then the objective cut is used.

MSK_IINF_MIO_RELGAP_SATISFIED

Non-zero if relative gap is within tolerances.

MSK_IINF_MIO_ABSGAP_SATISFIED

Non-zero if absolute gap is within tolerances.

MSK_IINF_MIO_NEAR_RELGAP_SATISFIED

Non-zero if relative gap is within relaxed tolerances.

MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED

Non-zero if absolute gap is within relaxed tolerances.

MSK_IINF_RD_PROTYPE

Problem type.

MSK_IINF_RD_NUMCON

Number of constraints read.

MSK_IINF_RD_NUMVAR

Number of variables read.

MSK_IINF_RD_NUMBARVAR

Number of variables read.

MSK_IINF_RD_NUMINTVAR

Number of integer-constrained variables read.

MSK_IINF_RD_NUMQ

Number of nonempty Q matrices read.

MSK_IINF_SIM_DUAL_DEG_ITER

The number of dual degenerate iterations.

MSK_IINF_SIM_DUAL_INF_ITER

The number of iterations taken with dual infeasibility.

MSK_IINF_SIM_DUAL_HOTSTART_LU

If 1 then a valid basis factorization of full rank was located and used by the dual simplex algorithm.

MSK_IINF_SIM_PRIMAL_ITER

Number of primal simplex iterations during the last optimization.

MSK_IINF_SIM_DUAL_ITER

Number of dual simplex iterations during the last optimization.

MSK_IINF_SIM_PRIMAL_DUAL_ITER

Number of primal dual simplex iterations during the last optimization.

MSK_IINF_INTPNT_NUM_THREADS

Number of threads that the interior-point optimizer is using.

MSK_IINF_SIM_PRIMAL_INF_ITER

The number of iterations taken with primal infeasibility.

MSK_IINF_SIM_PRIMAL_DUAL_INF_ITER

The number of master iterations with dual infeasibility taken by the primal dual simplex algorithm.

MSK_IINF_SIM_PRIMAL_DEG_ITER

The number of primal degenerate iterations.

MSK_IINF_SIM_PRIMAL_DUAL_DEG_ITER

The number of degenerate major iterations taken by the primal dual simplex algorithm.

MSK_IINF_SIM_PRIMAL_HOTSTART

If 1 then the primal simplex algorithm is solving from an advanced basis.

MSK_IINF_SIM_PRIMAL_HOTSTART_LU

If 1 then a valid basis factorization of full rank was located and used by the primal simplex algorithm.

MSK_IINF_SIM_DUAL_HOTSTART

If 1 then the dual simplex algorithm is solving from an advanced basis.

MSK_IINF_SIM_PRIMAL_DUAL_HOTSTART

If 1 then the primal dual simplex algorithm is solving from an advanced basis.

MSK_IINF_SIM_PRIMAL_DUAL_HOTSTART_LU

If 1 then a valid basis factorization of full rank was located and used by the primal dual simplex algorithm.

MSK_IINF_SOL_ITR_PROSTA

Problem status of the interior-point solution. Updated after each optimization.

MSK_IINF_SOL_ITR_SOLSTA

Solution status of the interior-point solution. Updated after each optimization.

MSK_IINF_SOL_BAS_PROSTA

Problem status of the basic solution. Updated after each optimization.

MSK_IINF_SOL_BAS_SOLSTA

Solution status of the basic solution. Updated after each optimization.

MSK_IINF_SOL_ITG_PROSTA

Problem status of the integer solution. Updated after each optimization.

MSK_IINF_SOL_ITG_SOLSTA

Solution status of the integer solution. Updated after each optimization.

MSK_IINF_SIM_NUMCON

Number of constraints in the problem solved by the simplex optimizer.

MSK_IINF_SIM_NUMVAR

Number of variables in the problem solved by the simplex optimizer.

MSK_IINF_OPT_NUMCON

Number of constraints in the problem solved when the optimizer is called.

MSK_IINF_OPT_NUMVAR

Number of variables in the problem solved when the optimizer is called

MSK_IINF_STO_NUM_A_REALLOC

Number of times the storage for storing A has been changed. A large value may indicates that memory fragmentation may occur.

MSK_IINF_RD_NUMCONE

Number of conic constraints read.

MSK_IINF_SIM_SOLVE_DUAL

Is non-zero if dual problem is solved.

MSKinftypee

Information item types

MSK_INF_DOU_TYPE

Is a double information type.

MSK_INF_INT_TYPE

Is an integer.

MSK_INF_LINT_TYPE

Is a long integer.

MSKiomodee

Input/output modes

MSK_IOMODE_READ

The file is read-only.

MSK_IOMODE_WRITE

The file is write-only. If the file exists then it is truncated when it is opened. Otherwise it is created when it is opened.

MSK_IOMODE_READWRITE

The file is to read and written.

MSKbranchdire

Specifies the branching direction.

MSK_BRANCH_DIR_FREE

The mixed-integer optimizer decides which branch to choose.

MSK_BRANCH_DIR_UP

The mixed-integer optimizer always chooses the up branch first.

MSK_BRANCH_DIR_DOWN

The mixed-integer optimizer always chooses the down branch first.

MSK_BRANCH_DIR_NEAR

Branch in direction nearest to selected fractional variable.

MSK_BRANCH_DIR_FAR

Branch in direction farthest from selected fractional variable.

MSK_BRANCH_DIR_ROOT_LP

Chose direction based on root lp value of selected variable.

MSK_BRANCH_DIR_GUIDED

Branch in direction of current incumbent.

MSK_BRANCH_DIR_PSEUDOCOST

Branch based on the pseudocost of the variable.

MSKmiocontsoltypee

Continuous mixed-integer solution type

MSK_MIO_CONT_SOL_NONE

No interior-point or basic solution are reported when the mixed-integer optimizer is used.

MSK_MIO_CONT_SOL_ROOT

The reported interior-point and basic solutions are a solution to the root node problem when mixed-integer optimizer is used.

MSK_MIO_CONT_SOL_ITG

The reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. A solution is only reported in case the problem has a primal feasible solution.

MSK_MIO_CONT_SOL_ITG_REL

In case the problem is primal feasible then the reported interior-point and basic solutions are a solution to the problem with all integer variables fixed at the value they have in the integer solution. If the problem is primal infeasible, then the solution to the root node problem is reported.

MSKmiomodee

Integer restrictions

MSK_MIO_MODE_IGNORED

The integer constraints are ignored and the problem is solved as a continuous problem.

MSK_MIO_MODE_SATISFIED

Integer restrictions should be satisfied.

MSKmionodeseltypee

Mixed-integer node selection types

MSK_MIO_NODE_SELECTION_FREE

The optimizer decides the node selection strategy.

MSK_MIO_NODE_SELECTION_FIRST

The optimizer employs a depth first node selection strategy.

MSK_MIO_NODE_SELECTION_BEST

The optimizer employs a best bound node selection strategy.

MSK_MIO_NODE_SELECTION_WORST

The optimizer employs a worst bound node selection strategy.

MSK_MIO_NODE_SELECTION_HYBRID

The optimizer employs a hybrid strategy.

MSK_MIO_NODE_SELECTION_PSEUDO

The optimizer employs selects the node based on a pseudo cost estimate.

${\tt MSKmpsformate}$

MPS file format type

MSK_MPS_FORMAT_STRICT

It is assumed that the input file satisfies the MPS format strictly.

MSK_MPS_FORMAT_RELAXED

It is assumed that the input file satisfies a slightly relaxed version of the MPS format.

MSK_MPS_FORMAT_FREE

It is assumed that the input file satisfies the free MPS format. This implies that spaces are not allowed in names. Otherwise the format is free.

MSK_MPS_FORMAT_CPLEX

The CPLEX compatible version of the MPS format is employed.

MSKmsgkeye

Message keys

MSK_MSG_READING_FILE

MSK_MSG_WRITING_FILE

MSK_MSG_MPS_SELECTED

${\tt MSKobjsensee}$

Objective sense types

MSK_OBJECTIVE_SENSE_MINIMIZE

The problem should be minimized.

MSK_OBJECTIVE_SENSE_MAXIMIZE

The problem should be maximized.

MSKonoffkeye

On/off

MSK_ON

Switch the option on.

MSK_OFF

Switch the option off.

MSKoptimizertypee

Optimizer types

MSK_OPTIMIZER_FREE

The optimizer is chosen automatically.

MSK_OPTIMIZER_INTPNT

The interior-point optimizer is used.

MSK_OPTIMIZER_CONIC

The optimizer for problems having conic constraints.

MSK_OPTIMIZER_PRIMAL_SIMPLEX

The primal simplex optimizer is used.

MSK_OPTIMIZER_DUAL_SIMPLEX

The dual simplex optimizer is used.

MSK_OPTIMIZER_FREE_SIMPLEX

One of the simplex optimizers is used.

MSK_OPTIMIZER_MIXED_INT

The mixed-integer optimizer.

MSKorderingtypee

Ordering strategies

MSK_ORDER_METHOD_FREE

The ordering method is chosen automatically.

MSK_ORDER_METHOD_APPMINLOC

Approximate minimum local fill-in ordering is employed.

MSK_ORDER_METHOD_EXPERIMENTAL

This option should not be used.

MSK_ORDER_METHOD_TRY_GRAPHPAR

Always try the graph partitioning based ordering.

MSK_ORDER_METHOD_FORCE_GRAPHPAR

Always use the graph partitioning based ordering even if it is worse than the approximate minimum local fill ordering.

MSK_ORDER_METHOD_NONE

No ordering is used.

MSKpresolvemodee

Presolve method.

MSK_PRESOLVE_MODE_OFF

The problem is not presolved before it is optimized.

MSK_PRESOLVE_MODE_ON

The problem is presolved before it is optimized.

MSK_PRESOLVE_MODE_FREE

It is decided automatically whether to presolve before the problem is optimized.

${\tt MSKparametertypee}$

Parameter type

MSK_PAR_INVALID_TYPE

Not a valid parameter.

MSK_PAR_DOU_TYPE

Is a double parameter.

MSK_PAR_INT_TYPE

Is an integer parameter.

${\tt MSK_PAR_STR_TYPE}$

Is a string parameter.

MSKproblemiteme

Problem data items

MSK_PI_VAR

Item is a variable.

MSK_PI_CON

Item is a constraint.

MSK_PI_CONE

Item is a cone.

MSKproblemtypee

Problem types

MSK_PROBTYPE_LO

The problem is a linear optimization problem.

MSK_PROBTYPE_QO

The problem is a quadratic optimization problem.

MSK_PROBTYPE_QCQO

The problem is a quadratically constrained optimization problem.

MSK_PROBTYPE_GECO

General convex optimization.

MSK_PROBTYPE_CONIC

A conic optimization.

MSK_PROBTYPE_MIXED

General nonlinear constraints and conic constraints. This combination can not be solved by \mathbf{MOSEK} .

MSKprostae

Problem status keys

MSK_PRO_STA_UNKNOWN

Unknown problem status.

MSK_PRO_STA_PRIM_AND_DUAL_FEAS

The problem is primal and dual feasible.

MSK_PRO_STA_PRIM_FEAS

The problem is primal feasible.

MSK_PRO_STA_DUAL_FEAS

The problem is dual feasible.

MSK_PRO_STA_NEAR_PRIM_AND_DUAL_FEAS

The problem is at least nearly primal and dual feasible.

MSK_PRO_STA_NEAR_PRIM_FEAS

The problem is at least nearly primal feasible.

MSK_PRO_STA_NEAR_DUAL_FEAS

The problem is at least nearly dual feasible.

MSK_PRO_STA_PRIM_INFEAS

The problem is primal infeasible.

MSK_PRO_STA_DUAL_INFEAS

The problem is dual infeasible.

MSK_PRO_STA_PRIM_AND_DUAL_INFEAS

The problem is primal and dual infeasible.

MSK_PRO_STA_ILL_POSED

The problem is ill-posed. For example, it may be primal and dual feasible but have a positive duality gap.

MSK_PRO_STA_PRIM_INFEAS_OR_UNBOUNDED

The problem is either primal infeasible or unbounded. This may occur for mixed-integer problems.

MSKxmlwriteroutputtypee

XML writer output mode

MSK_WRITE_XML_MODE_ROW

Write in row order.

MSK_WRITE_XML_MODE_COL

Write in column order.

MSKrescodetypee

Response code type

MSK_RESPONSE_OK

The response code is OK.

MSK_RESPONSE_WRN

The response code is a warning.

MSK_RESPONSE_TRM

The response code is an optimizer termination status.

MSK_RESPONSE_ERR

The response code is an error.

MSK_RESPONSE_UNK

The response code does not belong to any class.

${\tt MSKscalingtypee}$

Scaling type

MSK_SCALING_FREE

The optimizer chooses the scaling heuristic.

MSK_SCALING_NONE

No scaling is performed.

MSK_SCALING_MODERATE

A conservative scaling is performed.

MSK_SCALING_AGGRESSIVE

A very aggressive scaling is performed.

MSKscalingmethode

Scaling method

MSK_SCALING_METHOD_POW2

Scales only with power of 2 leaving the mantissa untouched.

MSK_SCALING_METHOD_FREE

The optimizer chooses the scaling heuristic.

MSKsensitivitytypee

Sensitivity types

MSK_SENSITIVITY_TYPE_BASIS

Basis sensitivity analysis is performed.

MSK_SENSITIVITY_TYPE_OPTIMAL_PARTITION

Optimal partition sensitivity analysis is performed.

MSKsimseltypee

Simplex selection strategy

MSK_SIM_SELECTION_FREE

The optimizer chooses the pricing strategy.

MSK_SIM_SELECTION_FULL

The optimizer uses full pricing.

MSK_SIM_SELECTION_ASE

The optimizer uses approximate steepest-edge pricing.

MSK_SIM_SELECTION_DEVEX

The optimizer uses devex steepest-edge pricing (or if it is not available an approximate steepedge selection).

MSK_SIM_SELECTION_SE

The optimizer uses steepest-edge selection (or if it is not available an approximate steep-edge selection).

MSK_SIM_SELECTION_PARTIAL

The optimizer uses a partial selection approach. The approach is usually beneficial if the number of variables is much larger than the number of constraints.

MSKsoliteme

Solution items

MSK_SOL_ITEM_XC

Solution for the constraints.

MSK_SOL_ITEM_XX

Variable solution.

MSK_SOL_ITEM_Y

Lagrange multipliers for equations.

MSK_SOL_ITEM_SLC

Lagrange multipliers for lower bounds on the constraints.

MSK_SOL_ITEM_SUC

Lagrange multipliers for upper bounds on the constraints.

MSK_SOL_ITEM_SLX

Lagrange multipliers for lower bounds on the variables.

MSK_SOL_ITEM_SUX

Lagrange multipliers for upper bounds on the variables.

MSK SOL ITEM SNX

Lagrange multipliers corresponding to the conic constraints on the variables.

${ t MSKsolstae}$

Solution status keys

MSK_SOL_STA_UNKNOWN

Status of the solution is unknown.

MSK_SOL_STA_OPTIMAL

The solution is optimal.

MSK_SOL_STA_PRIM_FEAS

The solution is primal feasible.

MSK_SOL_STA_DUAL_FEAS

The solution is dual feasible.

MSK_SOL_STA_PRIM_AND_DUAL_FEAS

The solution is both primal and dual feasible.

MSK_SOL_STA_NEAR_OPTIMAL

The solution is nearly optimal.

MSK_SOL_STA_NEAR_PRIM_FEAS

The solution is nearly primal feasible.

MSK_SOL_STA_NEAR_DUAL_FEAS

The solution is nearly dual feasible.

MSK_SOL_STA_NEAR_PRIM_AND_DUAL_FEAS

The solution is nearly both primal and dual feasible.

MSK_SOL_STA_PRIM_INFEAS_CER

The solution is a certificate of primal infeasibility.

MSK_SOL_STA_DUAL_INFEAS_CER

The solution is a certificate of dual infeasibility.

MSK_SOL_STA_NEAR_PRIM_INFEAS_CER

The solution is almost a certificate of primal infeasibility.

MSK_SOL_STA_NEAR_DUAL_INFEAS_CER

The solution is almost a certificate of dual infeasibility.

MSK_SOL_STA_PRIM_ILLPOSED_CER

The solution is a certificate that the primal problem is illposed.

MSK_SOL_STA_DUAL_ILLPOSED_CER

The solution is a certificate that the dual problem is illposed.

MSK_SOL_STA_INTEGER_OPTIMAL

The primal solution is integer optimal.

MSK_SOL_STA_NEAR_INTEGER_OPTIMAL

The primal solution is near integer optimal.

MSKsoltypee

Solution types

MSK_SOL_BAS

The basic solution.

MSK_SOL_ITR

The interior solution.

${\tt MSK_SOL_ITG}$

The integer solution.

MSKsolveforme

Solve primal or dual form

MSK_SOLVE_FREE

The optimizer is free to solve either the primal or the dual problem.

MSK_SOLVE_PRIMAL

The optimizer should solve the primal problem.

MSK_SOLVE_DUAL

The optimizer should solve the dual problem.

MSKstakeye

Status keys

MSK_SK_UNK

The status for the constraint or variable is unknown.

MSK_SK_BAS

The constraint or variable is in the basis.

MSK_SK_SUPBAS

The constraint or variable is super basic.

MSK_SK_LOW

The constraint or variable is at its lower bound.

MSK_SK_UPR

The constraint or variable is at its upper bound.

MSK_SK_FIX

The constraint or variable is fixed.

MSK_SK_INF

The constraint or variable is infeasible in the bounds.

MSKstartpointtypee

Starting point types

MSK_STARTING_POINT_FREE

The starting point is chosen automatically.

MSK_STARTING_POINT_GUESS

The optimizer guesses a starting point.

MSK_STARTING_POINT_CONSTANT

The optimizer constructs a starting point by assigning a constant value to all primal and dual variables. This starting point is normally robust.

MSK_STARTING_POINT_SATISFY_BOUNDS

The starting point is chosen to satisfy all the simple bounds on nonlinear variables. If this starting point is employed, then more care than usual should employed when choosing the bounds on the nonlinear variables. In particular very tight bounds should be avoided.

MSKstreamtypee

Stream types

MSK_STREAM_LOG

Log stream. Contains the aggregated contents of all other streams. This means that a message written to any other stream will also be written to this stream.

MSK_STREAM_MSG

Message stream. Log information relating to performance and progress of the optimization is written to this stream.

MSK STREAM ERR

Error stream. Error messages are written to this stream.

MSK_STREAM_WRN

Warning stream. Warning messages are written to this stream.

MSKvaluee

 ${\bf Integer\ values}$

MSK_MAX_STR_LEN

Maximum string length allowed in \mathbf{MOSEK} .

MSK_LICENSE_BUFFER_LENGTH

The length of a license key buffer.

MSKvariabletypee

Variable types

MSK_VAR_TYPE_CONT Is a continuous variable.

 $\label{eq:MSK_VAR_TYPE_INT} {\rm Is \ an \ integer \ variable.}$

SUPPORTED FILE FORMATS

MOSEK supports a range of problem and solution formats listed in Table 11.1 and Table 11.2. The **Task** format is MOSEK's native binary format and it supports all features that MOSEK supports. The **OPF** format is MOSEK's human-readable alternative that supports nearly all features (everything except semidefinite problems). In general, text formats are significantly slower to read, but can be examined and edited directly in any text editor.

Problem formats

See Table 11.1.

Table 11.1: List of supported file formats for optimization problems.

Format Type	Ext.	Binary/Text	LP	QP	CQO	SDP
LP	lp	plain text	X	X		
MPS	mps	plain text	X	X		
OPF	opf	plain text	X	X	X	
CBF	cbf	plain text	X		X	X
Osil	xml	xml text	X	X		
Task format	task	binary	X	X	X	X
Jtask format	jtask	text	X	X	X	X

Solution formats

See Table 11.2.

Table 11.2: List of supported solution formats.

Format Type	Ext.	Binary/Text	Description
	sol	plain text	Interior Solution
SOL	bas	plain text	Basic Solution
	int	plain text	Integer
Jsol format	jsol	text	Solution

Compression

MOSEK supports GZIP compression of files. Problem files with an additional .gz extension are assumed to be compressed when read, and are automatically compressed when written. For example, a file called

problem.mps.gz

will be considered as a GZIP compressed MPS file.

11.1 The LP File Format

MOSEK supports the LP file format with some extensions. The LP format is not a completely well-defined standard and hence different optimization packages may interpret the same LP file in slightly different ways. MOSEK tries to emulate as closely as possible CPLEX's behavior, but tries to stay backward compatible.

The LP file format can specify problems on the form

$$\begin{array}{lll} \text{minimize/maximize} & & c^Tx + \frac{1}{2}q^o(x) \\ \text{subject to} & l^c & \leq & Ax + \frac{1}{2}q(x) & \leq & u^c, \\ l^x & \leq & x & \leq & u^x, \\ & & & x_{\mathcal{J}} \text{ integer,} \end{array}$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.
- $c \in \mathbb{R}^n$ is the linear term in the objective.
- $q^o :\in \mathbb{R}^n \to \mathbb{R}$ is the quadratic term in the objective where

$$q^o(x) = x^T Q^o x$$

and it is assumed that

$$Q^o = (Q^o)^T$$
.

- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $q: \mathbb{R}^n \to \mathbb{R}$ is a vector of quadratic functions. Hence,

$$q_i(x) = x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T$$
.

• $\mathcal{J} \subseteq \{1, 2, \dots, n\}$ is an index set of the integer constrained variables.

11.1.1 File Sections

An LP formatted file contains a number of sections specifying the objective, constraints, variable bounds, and variable types. The section keywords may be any mix of upper and lower case letters.

Objective Function

The first section beginning with one of the keywords

max
maximum
maximize
min
minimum
minimize

defines the objective sense and the objective function, i.e.

$$c^T x + \frac{1}{2} x^T Q^o x.$$

The objective may be given a name by writing

myname:

before the expressions. If no name is given, then the objective is named obj.

The objective function contains linear and quadratic terms. The linear terms are written as:

```
4 x1 + x2 - 0.1 x3
```

and so forth. The quadratic terms are written in square brackets ([]) and are either squared or multiplied as in the examples

```
x1^2
```

and

```
x1 * x2
```

There may be zero or more pairs of brackets containing quadratic expressions.

An example of an objective section is

```
minimize
myobj: 4 x1 + x2 - 0.1 x3 + [ x1^2 + 2.1 x1 * x2 ]/2
```

Please note that the quadratic expressions are multiplied with $\frac{1}{2}$, so that the above expression means

minimize
$$4x_1 + x_2 - 0.1 \cdot x_3 + \frac{1}{2}(x_1^2 + 2.1 \cdot x_1 \cdot x_2)$$

If the same variable occurs more than once in the linear part, the coefficients are added, so that $4 \times 1 + 2 \times 1$ is equivalent to 6×1 . In the quadratic expressions $\times 1 \times 2$ is equivalent to $\times 2 \times 1$ and, as in the linear part, if the same variables multiplied or squared occur several times their coefficients are added.

Constraints

The second section beginning with one of the keywords

```
subj to
subject to
s.t.
st
```

defines the linear constraint matrix A and the quadratic matrices Q^i .

A constraint contains a name (optional), expressions adhering to the same rules as in the objective and a bound:

```
subject to
con1: x1 + x2 + [ x3^2 ]/2 <= 5.1</pre>
```

The bound type (here <=) may be any of <, <=, =, >, >= (< and <= mean the same), and the bound may be any number.

In the standard LP format it is not possible to define more than one bound, but **MOSEK** supports defining ranged constraints by using double-colon (::) instead of a single-colon (:) after the constraint name, i.e.

$$-5 \le x_1 + x_2 \le 5 \tag{11.1}$$

may be written as

```
con:: -5 < x_1 + x_2 < 5
```

By default **MOSEK** writes ranged constraints this way.

If the files must adhere to the LP standard, ranged constraints must either be split into upper bounded and lower bounded constraints or be written as an equality with a slack variable. For example the expression (11.1) may be written as

$$x_1 + x_2 - sl_1 = 0, -5 \le sl_1 \le 5.$$

Bounds

Bounds on the variables can be specified in the bound section beginning with one of the keywords

```
bound bounds
```

The bounds section is optional but should, if present, follow the subject to section. All variables listed in the bounds section must occur in either the objective or a constraint.

The default lower and upper bounds are 0 and $+\infty$. A variable may be declared free with the keyword free, which means that the lower bound is $-\infty$ and the upper bound is $+\infty$. Furthermore it may be assigned a finite lower and upper bound. The bound definitions for a given variable may be written in one or two lines, and bounds can be any number or $\pm\infty$ (written as $+\inf/-\inf/+\inf\inf\inf_{-\inf}$) as in the example

```
bounds

x1 free

x2 <= 5

0.1 <= x2

x3 = 42

2 <= x4 < +inf
```

Variable Types

The final two sections are optional and must begin with one of the keywords

```
bin
binaries
binary
```

and

```
gen
general
```

Under general all integer variables are listed, and under binary all binary (integer variables with bounds 0 and 1) are listed:

```
general
x1 x2
binary
x3 x4
```

Again, all variables listed in the binary or general sections must occur in either the objective or a constraint.

Terminating Section

Finally, an LP formatted file must be terminated with the keyword

```
end
```

11.1.2 LP File Examples

Linear example 1o1.1p

```
\ File: lo1.lp
maximize
obj: 3 x1 + x2 + 5 x3 + x4
subject to
c1: 3 x1 + x2 + 2 x3 = 30
c2: 2 x1 + x2 + 3 x3 + x4 >= 15
c3: 2 x2 + 3 x4 <= 25
bounds
0 <= x1 <= +infinity
0 <= x2 <= 10
0 <= x3 <= +infinity
0 <= x4 <= +infinity
end</pre>
```

Mixed integer example milo1.lp

```
maximize
obj: x1 + 6.4e-01 x2
subject to
c1: 5e+01 x1 + 3.1e+01 x2 <= 2.5e+02
c2: 3e+00 x1 - 2e+00 x2 >= -4e+00
bounds
0 <= x1 <= +infinity
0 <= x2 <= +infinity
general
x1 x2
end
```

11.1.3 LP Format peculiarities

Comments

Anything on a line after a \ is ignored and is treated as a comment.

Names

A name for an objective, a constraint or a variable may contain the letters a-z, A-Z, the digits θ - θ and the characters

```
!"#$%&()/,.;?@_'`|~
```

The first character in a name must not be a number, a period or the letter **e** or **E**. Keywords must not be used as names.

MOSEK accepts any character as valid for names, except \0. A name that is not allowed in LP file will be changed and a warning will be issued.

The algorithm for making names LP valid works as follows: The name is interpreted as an utf-8 string. For a unicode character c:

- If c==_ (underscore), the output is __ (two underscores).
- If c is a valid LP name character, the output is just c.
- If c is another character in the ASCII range, the output is _XX, where XX is the hexadecimal code for the character.
- If c is a character in the range 127-65535, the output is _uXXXX, where XXXX is the hexadecimal code for the character.
- If c is a character above 65535, the output is _UXXXXXXXX, where XXXXXXXX is the hexadecimal code for the character.

Invalid utf-8 substrings are escaped as $_{\tt XX'}$, and if a name starts with a period, e or E, that character is escaped as $_{\tt XX}$.

Variable Bounds

Specifying several upper or lower bounds on one variable is possible but **MOSEK** uses only the tightest bounds. If a variable is fixed (with =), then it is considered the tightest bound.

MOSEK Extensions to the LP Format

Some optimization software packages employ a more strict definition of the LP format than the one used by **MOSEK**. The limitations imposed by the strict LP format are the following:

- Quadratic terms in the constraints are not allowed.
- Names can be only 16 characters long.
- Lines must not exceed 255 characters in length.

If an LP formatted file created by MOSEK should satisfy the strict definition, then the parameter

• MSK_IPAR_WRITE_LP_STRICT_FORMAT

should be set; note, however, that some problems cannot be written correctly as a strict LP formatted file. For instance, all names are truncated to 16 characters and hence they may loose their uniqueness and change the problem.

To get around some of the inconveniences converting from other problem formats, **MOSEK** allows lines to contain 1024 characters and names may have any length (shorter than the 1024 characters).

Internally in MOSEK names may contain any (printable) character, many of which cannot be used in LP names. Setting the parameters

- MSK_IPAR_READ_LP_QUOTED_NAMES and
- MSK_IPAR_WRITE_LP_QUOTED_NAMES

allows MOSEK to use quoted names. The first parameter tells MOSEK to remove quotes from quoted names e.g, "x1", when reading LP formatted files. The second parameter tells MOSEK to put quotes around any semi-illegal name (names beginning with a number or a period) and fully illegal name (containing illegal characters). As double quote is a legal character in the LP format, quoting semi-illegal names makes them legal in the pure LP format as long as they are still shorter than 16 characters. Fully illegal names are still illegal in a pure LP file.

11.1.4 The strict LP format

The LP format is not a formal standard and different vendors have slightly different interpretations of the LP format. To make **MOSEK**'s definition of the LP format more compatible with the definitions of other vendors, use the parameter setting

• MSK_IPAR_WRITE_LP_STRICT_FORMAT = MSK_ON

This setting may lead to truncation of some names and hence to an invalid LP file. The simple solution to this problem is to use the parameter setting

• MSK_IPAR_WRITE_GENERIC_NAMES = MSK_ON

which will cause all names to be renamed systematically in the output file.

11.1.5 Formatting of an LP File

A few parameters control the visual formatting of LP files written by **MOSEK** in order to make it easier to read the files. These parameters are

- MSK_IPAR_WRITE_LP_LINE_WIDTH
- MSK_IPAR_WRITE_LP_TERMS_PER_LINE

The first parameter sets the maximum number of characters on a single line. The default value is 80 corresponding roughly to the width of a standard text document.

The second parameter sets the maximum number of terms per line; a term means a sign, a coefficient, and a name (for example + 42 elephants). The default value is 0, meaning that there is no maximum.

Unnamed Constraints

Reading and writing an LP file with **MOSEK** may change it superficially. If an LP file contains unnamed constraints or objective these are given their generic names when the file is read (however unnamed constraints in **MOSEK** are written without names).

11.2 The MPS File Format

MOSEK supports the standard MPS format with some extensions. For a detailed description of the MPS format see the book by Nazareth [Naz87].

11.2.1 MPS File Structure

The version of the MPS format supported by \mathbf{MOSEK} allows specification of an optimization problem of the form

$$l^{c} \leq Ax + q(x) \leq u^{c},$$

$$l^{x} \leq x \leq u^{x},$$

$$x \in \mathcal{K},$$

$$x_{\mathcal{J}} \text{ integer},$$

$$(11.2)$$

where

- $x \in \mathbb{R}^n$ is the vector of decision variables.
- $A \in \mathbb{R}^{m \times n}$ is the constraint matrix.
- $l^c \in \mathbb{R}^m$ is the lower limit on the activity for the constraints.
- $u^c \in \mathbb{R}^m$ is the upper limit on the activity for the constraints.
- $l^x \in \mathbb{R}^n$ is the lower limit on the activity for the variables.
- $u^x \in \mathbb{R}^n$ is the upper limit on the activity for the variables.
- $q: \mathbb{R}^n \to \mathbb{R}$ is a vector of quadratic functions. Hence,

$$q_i(x) = \frac{1}{2}x^T Q^i x$$

where it is assumed that

$$Q^i = (Q^i)^T.$$

Please note the explicit $\frac{1}{2}$ in the quadratic term and that Q^i is required to be symmetric.

- \mathcal{K} is a convex cone.
- $\mathcal{J} \subseteq \{1, 2, \dots, n\}$ is an index set of the integer-constrained variables.

An MPS file with one row and one column can be illustrated like this:

```
*23456789012345678901234567890123456789012345678901234567890
NAME
OBJSENSE
[objsense]
OBJNAME
[objname]
ROWS
? [cname1]
COLUMNS
[vname1]
          [cname1]
                        [value1]
                                      [vname3]
                                                 [value2]
RHS
           [cname1]
                        [value1]
                                      [cname2]
                                                 [value2]
[name]
RANGES
[name]
           [cname1]
                        [value1]
                                      [cname2]
                                                 [value2]
QSECTION
               [cname1]
                                      [vname3]
                                                 [value2]
[vname1]
           [vname2]
                        [value1]
QMATRIX
                        [value1]
[vname1]
           [vname2]
QUADOBJ
           [vname2]
                        [value1]
[vname1]
QCMATRIX
               [cname1]
           [vname2]
[vname1]
                        [value1]
BOUNDS
?? [name]
              [vname1]
                           [value1]
CSECTION
               [kname1]
                            [value1]
                                          [ktype]
[vname1]
ENDATA
```

Here the names in capitals are keywords of the MPS format and names in brackets are custom defined names or values. A couple of notes on the structure:

• Fields: All items surrounded by brackets appear in *fields*. The fields named "valueN" are numerical values. Hence, they must have the format

```
[+|-]XXXXXX.XXXXX[[e|E][+|-]XXX]
where
```

```
.. code-block:: text
X = [0|1|2|3|4|5|6|7|8|9].
```

- Sections: The MPS file consists of several sections where the names in capitals indicate the beginning of a new section. For example, COLUMNS denotes the beginning of the columns section.
- Comments: Lines starting with an * are comment lines and are ignored by MOSEK.
- Keys: The question marks represent keys to be specified later.
- Extensions: The sections QSECTION and CSECTION are specific MOSEK extensions of the MPS format. The sections QMATRIX, QUADOBJ and QCMATRIX are included for sake of compatibility with other vendors extensions to the MPS format.

The standard MPS format is a fixed format, i.e. everything in the MPS file must be within certain fixed positions. **MOSEK** also supports a *free format*. See Section 11.2.9 for details.

Linear example lo1.mps

A concrete example of a MPS file is presented below:

```
* File: lo1.mps
NAME
               lo1
OBJSENSE
    MAX
ROWS
N obj
E c1
G c2
L c3
COLUMNS
                          3
    x1
               obj
                          3
    x1
               c1
               c2
                          2
    x1
               obj
    x2
                          1
    x2
               c1
                          1
    x2
               c2
                          1
    x2
               сЗ
                          2
    xЗ
               obj
                          5
    xЗ
               c1
                          2
    хЗ
               c2
                          3
    x4
               obj
                          1
    x4
               c2
                          1
    x4
               сЗ
                          3
RHS
                          30
    rhs
               c1
               c2
                          15
    rhs
    rhs
               сЗ
                          25
RANGES
BOUNDS
UP bound
               x2
                          10
ENDATA
```

Subsequently each individual section in the MPS format is discussed.

Section NAME

In this section a name ([name]) is assigned to the problem.

OBJSENSE (optional)

This is an optional section that can be used to specify the sense of the objective function. The OBJSENSE section contains one line at most which can be one of the following

MIN
MINIMIZE
MAX
MAXIMIZE

It should be obvious what the implication is of each of these four lines.

OBJNAME (optional)

This is an optional section that can be used to specify the name of the row that is used as objective function. The OBJNAME section contains one line at most which has the form

objname

objname should be a valid row name.

ROWS

A record in the ROWS section has the form

? [cname1]

where the requirements for the fields are as follows:

Field	Starting Position	Max Width	required	Description
?	2	1	Yes	Constraint key
[cname1]	5	8	Yes	Constraint name

Hence, in this section each constraint is assigned an unique name denoted by [cname1]. Please note that [cname1] starts in position 5 and the field can be at most 8 characters wide. An initial key ? must be present to specify the type of the constraint. The key can have the values E, G, L, or N with the following interpretation:

Constraint type	l_i^c	u_i^c
E	finite	l_i^c
G	finite	∞
L	$-\infty$	finite
N	$-\infty$	∞

In the MPS format an objective vector is not specified explicitly, but one of the constraints having the key N will be used as the objective vector c. In general, if multiple N type constraints are specified, then the first will be used as the objective vector c.

COLUMNS

In this section the elements of A are specified using one or more records having the form:

[vname1] [cname1] [value1] [cname2] [value2]
--

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

Hence, a record specifies one or two elements a_{ij} of A using the principle that [vname1] and [cname1] determines j and i respectively. Please note that [cname1] must be a constraint name specified in the ROWS section. Finally, [value1] denotes the numerical value of a_{ij} . Another optional element is specified by [cname2], and [value2] for the variable specified by [vname1]. Some important comments are:

- All elements belonging to one variable must be grouped together.
- Zero elements of A should not be specified.
- At least one element for each variable should be specified.

RHS (optional)

A record in this section has the format

value2]	me2]	[cname2	[value1]	[cname1]	[name]
---------	------	---------	----------	----------	--------

where the requirements for each field are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RHS vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The interpretation of a record is that [name] is the name of the RHS vector to be specified. In general, several vectors can be specified. [cname1] denotes a constraint name previously specified in the ROWS section. Now, assume that this name has been assigned to the i th constraint and v_1 denotes the value specified by [value1], then the interpretation of v_1 is:

Constraint	l_i^c	u_i^c
type		
E	v_1	v_1
G	v_1	
L		v_1
N		

An optional second element is specified by [cname2] and [value2] and is interpreted in the same way. Please note that it is not necessary to specify zero elements, because elements are assumed to be zero.

RANGES (optional)

A record in this section has the form

e2]	[[cname2]		[value1]	.]	[cname1]	name]	[r
-----	---	----------	--	----------	----	----------	-------	----

where the requirements for each fields are as follows:

Field	Starting Position	Max Width	required	Description
[name]	5	8	Yes	Name of the RANGE vector
[cname1]	15	8	Yes	Constraint name
[value1]	25	12	Yes	Numerical value
[cname2]	40	8	No	Constraint name
[value2]	50	12	No	Numerical value

The records in this section are used to modify the bound vectors for the constraints, i.e. the values in l^c and u^c . A record has the following interpretation: [name] is the name of the RANGE vector and [cname1] is a valid constraint name. Assume that [cname1] is assigned to the i th constraint and let v_1 be the value specified by [value1], then a record has the interpretation:

Constraint type	Sign of v_1	l_i^c	u_i^c
E	_	$u_i^c + v_1$	
E	+		$l_i^c + v_1$
G	- or +	$l_i^c + v_1 $	
L	- or +	$u_i^c - v_1 $	
N			

QSECTION (optional)

Within the QSECTION the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the QSECTION has the form

|--|

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value
[vname3]	40	8	No	Variable name
[value2]	50	12	No	Numerical value

A record specifies one or two elements in the lower triangular part of the Q^i matrix where [cname1] specifies the i. Hence, if the names [vname1] and [vname2] have been assigned to the k th and j th variable, then Q^i_{kj} is assigned the value given by [value1] An optional second element is specified in the same way by the fields [vname1], [vname3], and [value2].

The example

$$\begin{array}{ll} \text{minimize} & -x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2) \\ \text{subject to} & x_1 + x_2 + x_3 & \geq & 1, \\ & x > 0 & \end{array}$$

has the following MPS file representation

```
* File: qo1.mps
NAME
ROWS
N obj
G c1
COLUMNS
x1
           c1
                      1.0
x2
           obj
                      -1.0
x2
                      1.0
           c1
x3
           с1
                      1.0
RHS
                      1.0
rhs
           c1
QSECTION
               obj
                      2.0
x1
           x1
                      -1.0
x1
           xЗ
x2
           x2
                      0.2
хЗ
           хЗ
                      2.0
ENDATA
```

Regarding the QSECTIONs please note that:

- Only one QSECTION is allowed for each constraint.
- The QSECTIONs can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QSECTION must already be specified in the COLUMNS section.
- ullet All entries specified in a QSECTION are assumed to belong to the lower triangular part of the quadratic term of Q.

QMATRIX/QUADOBJ (optional)

The QMATRIX and QUADOBJ sections allow to define the quadratic term of the objective function. They differ in how the quadratic term of the objective function is stored:

- ullet QMATRIX It stores all the nonzeros coefficients, without taking advantage of the symmetry of the Q matrix.
- QUADOBJ It only store the upper diagonal nonzero elements of the Q matrix.

A record in both sections has the form:

|--|

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies one elements of the Q matrix in the objective function. Hence, if the names [vname1] and [vname2] have been assigned to the k th and j th variable, then Q_{kj} is assigned the value given by [value1]. Note that a line must apper for each off-diagonal coefficient if using a QMATRIX section, while only one entry is required in a QUADOBJ section. The quadratic part of the objective function will be evaluated as $1/2x^TQx$.

The example

minimize
$$-x_2 + \frac{1}{2}(2x_1^2 - 2x_1x_3 + 0.2x_2^2 + 2x_3^2)$$
 subject to
$$x_1 + x_2 + x_3 \geq 1,$$

$$x > 0$$

has the following MPS file representation using QMATRIX

* F	ile:	qo1_matrix.m	ps
NAM	NAME qo1_qmatrix		
ROW			
	obj		
	c1		
COL	UMNS		
	x1	c1	1.0
	x2	obj	-1.0
	x2	c1	1.0
	x3	c1	1.0
RHS			
	rhs	c1	1.0
QMA	TRIX		
	x1	x1	2.0
	x1	x3	-1.0
	x3	x1	-1.0
	x2	x2	0.2
	x3	x3	2.0
END	ATA		

or the following using QUADOBJ

```
* File: qo1_quadobj.mps
NAME
              qo1_quadobj
ROWS
N obj
G c1
COLUMNS
                         1.0
   x1
              c1
                         -1.0
    x2
              obj
    x2
                         1.0
              c1
   хЗ
                         1.0
              c1
RHS
                         1.0
    rhs
              c1
QUADOBJ
                         2.0
    x1
              x1
              хЗ
                         -1.0
    x1
    x2
              x2
                         0.2
    хЗ
              хЗ
                         2.0
ENDATA
```

Please also note that:

- A QMATRIX/QUADOBJ section can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QMATRIX/QUADOBJ section must already be specified in the COLUMNS section.

11.2.2 QCMATRIX (optional)

A QCMATRIX section allows to specify the quadratic part of a given constraints. Within the QCMATRIX the label [cname1] must be a constraint name previously specified in the ROWS section. The label [cname1] denotes the constraint to which the quadratic term belongs. A record in the QSECTION has the form

```
[vname1] [vname2] [value1]
```

where the requirements for each field are:

Field	Starting Position	Max Width	required	Description
[vname1]	5	8	Yes	Variable name
[vname2]	15	8	Yes	Variable name
[value1]	25	12	Yes	Numerical value

A record specifies an entry of the Q^i matrix where [cname1] specifies the i. Hence, if the names [vname1] and [vname2] have been assigned to the k th and j th variable, then Q^i_{kj} is assigned the value given by [value1]. Moreover, the quadratic term is represented as $1/2x^TQx$.

The example

$$\begin{array}{lll} \text{minimize} & x_2 \\ \text{subject to} & x_1 + x_2 + x_3 & \geq & 1, \\ & \frac{1}{2} \bigl(-2x_1x_3 + 0.2x_2^2 + 2x_3^2 \bigr) & \leq & 10, \\ & x \geq 0 \end{array}$$

has the following MPS file representation

```
* File: qo1.mps
NAME qo1
ROWS
N obj
G c1
L q1
COLUMNS
```

x1	c1	1.0
x2	obj	-1.0
x2	c1	1.0
x3	c1	1.0
RHS		
rhs	c1	1.0
rhs	q1	10.0
QCMATRIX	q1	
x1	x1	2.0
x1	x3	-1.0
x3	x1	-1.0
x2	x2	0.2
x3	x3	2.0
ENDATA		
l		

Regarding the QCMATRIXs please note that:

- Only one QCMATRIX is allowed for each constraint.
- The QCMATRIXs can appear in an arbitrary order after the COLUMNS section.
- All variable names occurring in the QSECTION must already be specified in the COLUMNS section.
- A QCMATRIX does not exploit the symmetry of Q: an off-diagonal entry (i,j) should appear twice.

11.2.3 BOUNDS (optional)

In the BOUNDS section changes to the default bounds vectors l^x and u^x are specified. The default bounds vectors are $l^x=0$ and $u^x=\infty$. Moreover, it is possible to specify several sets of bound vectors. A record in this section has the form

[name] [vname1] [value1]	
alue1]	

where the requirements for each field are:

Field	Starting Position	Max Width	Required	Description
??	2	2	Yes	Bound key
[name]	5	8	Yes	Name of the BOUNDS vector
[vname1]	15	8	Yes	Variable name
[value1]	25	12	No	Numerical value

Hence, a record in the BOUNDS section has the following interpretation: [name] is the name of the bound vector and [vname1] is the name of the variable which bounds are modified by the record. ?? and [value1] are used to modify the bound vectors according to the following table:

??	l_j^x	u_j^x	Made integer (added to ${\mathcal J}$)
FR	$-\infty$	∞	No
FX	v_1	v_1	No
LO	v_1	unchanged	No
MI	$-\infty$	unchanged	No
PL	unchanged	∞	No
UP	unchanged	v_1	No
BV	0	1	Yes
LI	$\lceil v_1 \rceil$	unchanged	Yes
UI	unchanged	$\lfloor v_1 \rfloor$	Yes

 $v_{\it 1}$ is the value specified by [value1].

11.2.4 CSECTION (optional)

The purpose of the CSECTION is to specify the constraint

$$x \in \mathcal{K}$$
.

in (11.2). It is assumed that K satisfies the following requirements. Let

$$x^t \in \mathbb{R}^{n^t}, \quad t = 1, \dots, k$$

be vectors comprised of parts of the decision variables x so that each decision variable is a member of exactly **one** vector x^t , for example

$$x^1 = \left[egin{array}{c} x_1 \ x_4 \ x_7 \end{array}
ight] \quad ext{ and } \quad x^2 = \left[egin{array}{c} x_6 \ x_5 \ x_3 \ x_2 \end{array}
ight].$$

Next define

$$\mathcal{K} := \left\{ x \in \mathbb{R}^n : \quad x^t \in \mathcal{K}_t, \quad t = 1, \dots, k \right\}$$

where \mathcal{K}_t must have one of the following forms

• \mathbb{R} set:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} \right\}.$$

• Quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : x_1 \ge \sqrt{\sum_{j=2}^{n^t} x_j^2} \right\}. \tag{11.3}$$

• Rotated quadratic cone:

$$\mathcal{K}_t = \left\{ x \in \mathbb{R}^{n^t} : 2x_1 x_2 \ge \sum_{j=3}^{n^t} x_j^2, \quad x_1, x_2 \ge 0 \right\}.$$
 (11.4)

In general, only quadratic and rotated quadratic cones are specified in the MPS file whereas membership of the \mathbb{R} set is not. If a variable is not a member of any other cone then it is assumed to be a member of an \mathbb{R} cone.

Next, let us study an example. Assume that the quadratic cone

$$x_4 \ge \sqrt{x_5^2 + x_8^2}$$

and the rotated quadratic cone

$$x_3x_7 \ge x_1^2 + x_0^2, \quad x_3, x_7 \ge 0,$$

should be specified in the MPS file. One CSECTION is required for each cone and they are specified as follows:

k	1	2	3	4	5	6
*2345678	9012345	67890123	45678901234	567890123456	78901234	567890
CSECTION	I k	onea	0.0	QUAD		
x4						
x5						
x8						
CSECTION	I k	oneb	0.0	RQUAD		
x7						
хЗ						
x1						
x0						

This first CSECTION specifies the cone (11.3) which is given the name konea. This is a quadratic cone which is specified by the keyword QUAD in the CSECTION header. The 0.0 value in the CSECTION header is not used by the QUAD cone.

The second CSECTION specifies the rotated quadratic cone (11.4). Please note the keyword RQUAD in the CSECTION which is used to specify that the cone is a rotated quadratic cone instead of a quadratic cone. The 0.0 value in the CSECTION header is not used by the RQUAD cone.

In general, a CSECTION header has the format

|--|

where the requirement for each field are as follows:

Field	Starting Position	Max Width	Required	Description
[kname1]	5	8	Yes	Name of the cone
[value1]	15	12	No	Cone parameter
[ktype]	25		Yes	Type of the cone.

The possible cone type keys are:

Cone type key	Members	Interpretation.	
QUAD	≤ 1	Quadratic cone i.e. (11.3).	
RQUAD	< 2	Rotated quadratic cone i.e. (11.4).	

Please note that a quadratic cone must have at least one member whereas a rotated quadratic cone must have at least two members. A record in the CSECTION has the format

[vname1]

where the requirements for each field are

Field	Starting Position	Max Width	required	Description
[vname1]	2	8	Yes	A valid variable name

The most important restriction with respect to the CSECTION is that a variable must occur in only one CSECTION.

11.2.5 ENDATA

This keyword denotes the end of the MPS file.

11.2.6 Integer Variables

Using special bound keys in the BOUNDS section it is possible to specify that some or all of the variables should be integer-constrained i.e. be members of \mathcal{J} . However, an alternative method is available.

This method is available only for backward compatibility and we recommend that it is not used. This method requires that markers are placed in the COLUMNS section as in the example:

COLUMNS					
x1	obj	-10.0	c1	0.7	
x1	c2	0.5	c3	1.0	
x1	c4	0.1			
* Start	* Start of integer-constrained variables.				
MARK000	'MARKER'		'INTORG'		
x2	obj	-9.0	c1	1.0	
x2	c2	0.8333333333	c3	0.6666667	
x2	c4	0.25			
хЗ	obj	1.0	c6	2.0	
MARKO01	'MARKER'		'INTEND'		

• End of integer-constrained variables.

Please note that special marker lines are used to indicate the start and the end of the integer variables. Furthermore be aware of the following

- IMPORTANT: All variables between the markers are assigned a default lower bound of 0 and a default upper bound of 1. **This may not be what is intended.** If it is not intended, the correct bounds should be defined in the BOUNDS section of the MPS formatted file.
- MOSEK ignores field 1, i.e. MARKO001 and MARK001, however, other optimization systems require them.
- Field 2, i.e. MARKER, must be specified including the single quotes. This implies that no row can be assigned the name MARKER.
- Field 3 is ignored and should be left blank.
- Field 4, i.e. INTORG and INTEND, must be specified.
- It is possible to specify several such integer marker sections within the COLUMNS section.

11.2.7 General Limitations

• An MPS file should be an ASCII file.

11.2.8 Interpretation of the MPS Format

Several issues related to the MPS format are not well-defined by the industry standard. However, **MOSEK** uses the following interpretation:

- If a matrix element in the COLUMNS section is specified multiple times, then the multiple entries are added together.
- If a matrix element in a QSECTION section is specified multiple times, then the multiple entries are added together.

11.2.9 The Free MPS Format

MOSEK supports a free format variation of the MPS format. The free format is similar to the MPS file format but less restrictive, e.g. it allows longer names. However, it also presents two main limitations:

- A name must not contain any blanks.
- By default a line in the MPS file must not contain more than 1024 characters. However, by modifying the parameter MSK_IPAR_READ_MPS_WIDTH an arbitrary large line width will be accepted.

To use the free MPS format instead of the default MPS format the MOSEK parameter $MSK_IPAR_READ_MPS_FORMAT$ should be changed.

11.3 The OPF Format

The Optimization Problem Format (OPF) is an alternative to LP and MPS files for specifying optimization problems. It is row-oriented, inspired by the CPLEX LP format.

Apart from containing objective, constraints, bounds etc. it may contain complete or partial solutions, comments and extra information relevant for solving the problem. It is designed to be easily read and modified by hand and to be forward compatible with possible future extensions.

Intended use

The OPF file format is meant to replace several other files:

- The LP file format: Any problem that can be written as an LP file can be written as an OPF file too; furthermore it naturally accommodates ranged constraints and variables as well as arbitrary characters in names, fixed expressions in the objective, empty constraints, and conic constraints.
- Parameter files: It is possible to specify integer, double and string parameters along with the problem (or in a separate OPF file).
- Solution files: It is possible to store a full or a partial solution in an OPF file and later reload it.

11.3.1 The File Format

The format uses tags to structure data. A simple example with the basic sections may look like this:

```
[comment]
This is a comment. You may write almost anything here...
[/comment]
# This is a single-line comment.

[objective min 'myobj']
x + 3 y + x^2 + 3 y^2 + z + 1
[/objective]

[constraints]
[con 'con01'] 4 &<= x + y [/con]
[/constraints]
[bounds]
[b] -10 &<= x,y &<= 10 [/b]

[cone quad] x,y,z [/cone]
[/bounds]</pre>
```

A scope is opened by a tag of the form [tag] and closed by a tag of the form [/tag]. An opening tag may accept a list of unnamed and named arguments, for examples:

```
[tag value] tag with one unnamed argument [/tag]
[tag arg=value] tag with one named argument in quotes [/tag]
```

Unnamed arguments are identified by their order, while named arguments may appear in any order, but never before an unnamed argument. The value can be a quoted, single-quoted or double-quoted text string, i.e.

```
[tag 'value'] single-quoted value [/tag]
[tag arg='value'] single-quoted value [/tag]
[tag "value"] double-quoted value [/tag]
[tag arg="value"] double-quoted value [/tag]
```

Sections

The recognized tags are

[comment]

A comment section. This can contain *almost* any text: Between single quotes (') or double quotes (") any text may appear. Outside quotes the markup characters ([and]) must be prefixed by backslashes. Both single and double quotes may appear alone or inside a pair of quotes if it is prefixed by a backslash.

[objective]

The objective function: This accepts one or two parameters, where the first one (in the above example min) is either min or max (regardless of case) and defines the objective sense, and the second one (above myobj), if present, is the objective name. The section may contain linear and quadratic expressions. If several objectives are specified, all but the last are ignored.

[constraints]

This does not directly contain any data, but may contain the subsection con defining a linear constraint.

[con] defines a single constraint; if an argument is present ([con NAME]) this is used as the name of the constraint, otherwise it is given a null-name. The section contains a constraint definition written as linear and quadratic expressions with a lower bound, an upper bound, with both or with an equality. Examples:

Constraint names are unique. If a constraint is specified which has the same name as a previously defined constraint, the new constraint replaces the existing one.

[bounds]

This does not directly contain any data, but may contain the subsections b (linear bounds on variables) and cone (quadratic cone).

[b]. Bound definition on one or several variables separated by comma (,). An upper or lower bound on a variable replaces any earlier defined bound on that variable. If only one bound (upper or lower) is given only this bound is replaced. This means that upper and lower bounds can be specified separately. So the OPF bound definition:

```
[b] x,y >= -10 [/b]
[b] x,y <= 10 [/b]
```

results in the bound $-10 \le x, y \le 10$.

[cone]. currently supports the quadratic cone and the rotated quadratic cone.

A conic constraint is defined as a set of variables which belong to a single unique cone.

• A quadratic cone of n variables x_1, \ldots, x_n defines a constraint of the form

$$x_1^2 > \sum_{i=2}^n x_i^2.$$

• A rotated quadratic cone of n variables x_1, \ldots, x_n defines a constraint of the form

$$x_1 x_2 > \sum_{i=3}^{n} x_i^2.$$

A [bounds]-section example:

By default all variables are free.

[variables]

This defines an ordering of variables as they should appear in the problem. This is simply a space-separated list of variable names.

[integer]

This contains a space-separated list of variables and defines the constraint that the listed variables must be integer values.

[hints]

This may contain only non-essential data; for example estimates of the number of variables, constraints and non-zeros. Placed before all other sections containing data this may reduce the time spent reading the file.

In the hints section, any subsection which is not recognized by MOSEK is simply ignored. In this section a hint in a subsection is defined as follows:

```
[hint ITEM] value [/hint]
```

where ITEM may be replaced by numvar (number of variables), numcon (number of linear/quadratic constraints), numanz (number of linear non-zeros in constraints) and numqnz (number of quadratic non-zeros in constraints).

[solutions]

This section can contain a set of full or partial solutions to a problem. Each solution must be specified using a [solution]-section, i.e.

```
[solutions]
[solution]...[/solution] #solution 1
[solution]...[/solution] #solution 2
#other solutions....
[solution]...[/solution] #solution n
[/solutions]
```

Note that a [solution]-section must be always specified inside a [solutions]-section. The syntax of a [solution]-section is the following:

```
[solution SOLTYPE status=STATUS]...[/solution]
```

where SOLTYPE is one of the strings

- interior, a non-basic solution,
- basic, a basic solution,
- integer, an integer solution,

and STATUS is one of the strings

- UNKNOWN,
- OPTIMAL,
- INTEGER_OPTIMAL,
- PRIM_FEAS,
- DUAL_FEAS,
- PRIM_AND_DUAL_FEAS,
- NEAR_OPTIMAL,
- NEAR_PRIM_FEAS,
- NEAR_DUAL_FEAS,
- NEAR_PRIM_AND_DUAL_FEAS,
- PRIM_INFEAS_CER,
- DUAL_INFEAS_CER,
- NEAR_PRIM_INFEAS_CER,
- NEAR_DUAL_INFEAS_CER,
- NEAR_INTEGER_OPTIMAL.

Most of these values are irrelevant for input solutions; when constructing a solution for simplex hot-start or an initial solution for a mixed integer problem the safe setting is UNKNOWN.

A [solution]-section contains [con] and [var] sections. Each [con] and [var] section defines solution information for a single variable or constraint, specified as list of KEYWORD/value pairs, in any order, written as

KEYWORD=value

Allowed keywords are as follows:

- sk. The status of the item, where the value is one of the following strings:
 - LOW, the item is on its lower bound.
 - UPR, the item is on its upper bound.
 - FIX, it is a fixed item.
 - BAS, the item is in the basis.

- SUPBAS, the item is super basic.
- UNK, the status is unknown.
- INF, the item is outside its bounds (infeasible).
- 1v1 Defines the level of the item.
- sl Defines the level of the dual variable associated with its lower bound.
- su Defines the level of the dual variable associated with its upper bound.
- sn Defines the level of the variable associated with its cone.
- y Defines the level of the corresponding dual variable (for constraints only).

A [var] section should always contain the items sk, lvl, sl and su. Items sl and su are not required for integer solutions.

A [con] section should always contain sk, lvl, sl, su and y.

An example of a solution section

• [vendor] This contains solver/vendor specific data. It accepts one argument, which is a vendor ID – for MOSEK the ID is simply mosek – and the section contains the subsection parameters defining solver parameters. When reading a vendor section, any unknown vendor can be safely ignored. This is described later.

Comments using the # may appear anywhere in the file. Between the # and the following line-break any text may be written, including markup characters.

Numbers

Numbers, when used for parameter values or coefficients, are written in the usual way by the printf function. That is, they may be prefixed by a sign (+ or -) and may contain an integer part, decimal part and an exponent. The decimal point is always . (a dot). Some examples are

```
1
1.0
.0
1.
1e10
1e+10
1e-10
```

Some *invalid* examples are

```
e10 # invalid, must contain either integer or decimal part
. # invalid
.e10 # invalid
```

More formally, the following standard regular expression describes numbers as used:

```
[+|-]?([0-9]+[.][0-9]*|[.][0-9]+)([eE][+|-]?[0-9]+)?
```

Names

Variable names, constraint names and objective name may contain arbitrary characters, which in some cases must be enclosed by quotes (single or double) that in turn must be preceded by a backslash. Unquoted names must begin with a letter (a-z or A-Z) and contain only the following characters: the letters a-z and A-Z, the digits 0-9, braces ({ and }) and underscore (_).

Some examples of legal names:

```
an_unquoted_name
another_name{123}
'single quoted name'
"double quoted name"
"name with \\"quote\\" in it"
"name with []s in it"
```

11.3.2 Parameters Section

In the vendor section solver parameters are defined inside the parameters subsection. Each parameter is written as

```
[p PARAMETER_NAME] value [/p]
```

where PARAMETER_NAME is replaced by a MOSEK parameter name, usually of the form MSK_IPAR_..., MSK_DPAR_... or MSK_SPAR_..., and the value is replaced by the value of that parameter; both integer values and named values may be used. Some simple examples are

11.3.3 Writing OPF Files from MOSEK

To write an OPF file set the parameter $MSK_IPAR_WRITE_DATA_FORMAT$ to $MSK_DATA_FORMAT_OP$ as this ensures that OPF format is used.

Then modify the following parameters to define what the file should contain:

MSK_IPAR_OPF_WRITE_SOL_BAS	Include basic solution, if defined.			
MSK_IPAR_OPF_WRITE_SOL_ITG	Include integer solution, if defined.			
MSK_IPAR_OPF_WRITE_SOL_ITR	Include interior solution, if defined.			
MSK_IPAR_OPF_WRITE_SOLUTION	SInclude solutions if they are defined. If this is off, no solutions are			
	included.			
MSK_IPAR_OPF_WRITE_HEADER	Include a small header with comments.			
MSK_IPAR_OPF_WRITE_PROBLEM	Include the problem itself — objective, constraints and bounds.			
MSK_IPAR_OPF_WRITE_PARAMETER\$ include all parameter settings.				
MSK_IPAR_OPF_WRITE_HINTS	Include hints about the size of the problem.			

11.3.4 Examples

This section contains a set of small examples written in OPF and describing how to formulate linear, quadratic and conic problems.

Linear Example 101.opf

Consider the example:

having the bounds

In the OPF format the example is displayed as shown in Listing 11.1.

Listing 11.1: Example of an OPF file for a linear problem.

```
[comment]
 The lo1 example in OPF format
[/comment]
[hints]
 [hint NUMVAR] 4 [/hint]
  [hint NUMCON] 3 [/hint]
  [hint NUMANZ] 9 [/hint]
[/hints]
[variables disallow_new_variables]
 x1 x2 x3 x4
[/variables]
[objective maximize 'obj']
  3 x1 + x2 + 5 x3 + x4
[/objective]
[constraints]
 [con 'c1'] 3 x1 + x2 + 2 x3 = 30 [/con]
  [con 'c2'] 2 x1 + x2 + 3 x3 + x4 >= 15 [/con]
 [con 'c3']
                  2 x2 + 3 x4 <= 25 [/con]
[/constraints]
[bounds]
 [b] 0 \ll * [/b]
  [b] 0 \le x2 \le 10 [/b]
[/bounds]
```

Quadratic Example qo1.opf

An example of a quadratic optimization problem is

$$\begin{array}{ll} \text{minimize} & x_1^2 + 0.1x_2^2 + x_3^2 - x_1x_3 - x_2 \\ \text{subject to} & 1 & \leq & x_1 + x_2 + x_3, \\ & & x \geq 0. \end{array}$$

This can be formulated in opf as shown below.

Listing 11.2: Example of an OPF file for a quadratic problem.

```
[comment]
 The qo1 example in OPF format
[/comment]
[hints]
  [hint NUMVAR] 3 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
  [hint NUMQNZ] 4 [/hint]
[/hints]
[variables disallow_new_variables]
 x1 x2 x3
[/variables]
[objective minimize 'obj']
 \# The quadratic terms are often written with a factor of 1/2 as here,
 # but this is not required.
   - x2 + 0.5 ( 2.0 x1 ^ 2 - 2.0 x3 * x1 + 0.2 x2 ^ 2 + 2.0 x3 ^ 2 )
[/objective]
[constraints]
  [con 'c1'] 1.0 \le x1 + x2 + x3 [/con]
[/constraints]
[bounds]
 [b] 0 <= * [/b]
[/bounds]
```

Conic Quadratic Example cqo1.opf

Consider the example:

minimize
$$x_3 + x_4 + x_5$$

subject to $x_0 + x_1 + 2x_2 = 1$, $x_0, x_1, x_2 \ge 0$, $x_3 \ge \sqrt{x_0^2 + x_1^2}$, $2x_4x_5 \ge x_2^2$.

Please note that the type of the cones is defined by the parameter to [cone ...]; the content of the cone-section is the names of variables that belong to the cone. The resulting OPF file is in Listing 11.3.

Listing 11.3: Example of an OPF file for a conic quadratic problem.

```
[comment]
  The cqo1 example in OPF format.
[/comment]

[hints]
  [hint NUMVAR] 6 [/hint]
  [hint NUMCON] 1 [/hint]
  [hint NUMANZ] 3 [/hint]
[/hints]

[variables disallow_new_variables]
  x1 x2 x3 x4 x5 x6
[/variables]
```

```
[objective minimize 'obj']
  x4 + x5 + x6
[/objective]
[constraints]
 [con 'c1'] x1 + x2 + 2e+00 x3 = 1e+00 [/con]
[/constraints]
[bounds]
 # We let all variables default to the positive orthant
 [b] 0 \le * [/b]
 # ...and change those that differ from the default
 [b] x4,x5,x6 free [/b]
 # Define quadratic cone: x4 \ge sqrt(x1^2 + x2^2)
 [cone quad 'k1'] x4, x1, x2 [/cone]
 # Define rotated quadratic cone: 2 x5 x6 >= x3^2
 [cone rquad 'k2'] x5, x6, x3 [/cone]
[/bounds]
```

Mixed Integer Example milo1.opf

Consider the mixed integer problem:

This can be implemented in OPF with the file in Listing 11.4.

Listing 11.4: Example of an OPF file for a mixed-integer linear problem.

```
[comment]
 The milo1 example in OPF format
[/comment]
[hints]
  [hint NUMVAR] 2 [/hint]
  [hint NUMCON] 2 [/hint]
  [hint NUMANZ] 4 [/hint]
[/hints]
[variables disallow_new_variables]
 x1 x2
[/variables]
[objective maximize 'obj']
  x1 + 6.4e-1 x2
[/objective]
[constraints]
  [con 'c1'] 5e+1 x1 + 3.1e+1 x2 \le 2.5e+2 [/con]
  [con 'c2'] -4 \le 3 x1 - 2 x2 [/con]
[/constraints]
[bounds]
  [b] 0 <= * [/b]
[/bounds]
```

[integer]
 x1 x2
[/integer]

11.4 The CBF Format

This document constitutes the technical reference manual of the *Conic Benchmark Format* with file extension: .cbf or .CBF. It unifies linear, second-order cone (also known as conic quadratic) and semidefinite optimization with mixed-integer variables. The format has been designed with benchmark libraries in mind, and therefore focuses on compact and easily parsable representations. The problem structure is separated from the problem data, and the format moreover facilitates benchmarking of hotstart capability through sequences of changes.

11.4.1 How Instances Are Specified

This section defines the spectrum of conic optimization problems that can be formulated in terms of the keywords of the CBF format.

In the CBF format, conic optimization problems are considered in the following form:

min / max
$$g^{obj}$$

 $g_i \in \mathcal{K}_i, \quad i \in \mathcal{I},$
s.t. $G_i \in \mathcal{K}_i, \quad i \in \mathcal{I}^{PSD},$
 $\frac{x_j}{X_j} \in \mathcal{K}_j, \quad j \in \mathcal{J},$
 $X_j \in \mathcal{K}_j, \quad j \in \mathcal{J}^{PSD}$. (11.5)

- Variables are either scalar variables, x_j for $j \in \mathcal{J}$, or variables, \overline{X}_j for $j \in \mathcal{J}^{PSD}$. Scalar variables can also be declared as integer.
- Constraints are affine expressions of the variables, either scalar-valued g_i for $i \in \mathcal{I}$, or matrix-valued G_i for $i \in \mathcal{I}^{PSD}$

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$
$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i.$$

• The **objective function** is a scalar-valued affine expression of the variables, either to be minimized or maximized. We refer to this expression as g^{obj}

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj}.$$

CBF format can represent the following cones \mathcal{K} :

• Free domain - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n\}$$
, for $n \ge 1$.

• Positive orthant - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_i \ge 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \ge 1.$$

• Negative orthant - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j \leq 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \geq 1.$$

• Fixpoint zero - A cone in the linear family defined by

$$\{x \in \mathbb{R}^n \mid x_j = 0 \text{ for } j = 1, \dots, n\}, \text{ for } n \ge 1.$$

• Quadratic cone - A cone in the second-order cone family defined by

$$\left\{ \left(\begin{array}{c} p \\ x \end{array}\right) \in \mathbb{R} \times \mathbb{R}^{n-1}, \ p^2 \ge x^T x, \ p \ge 0 \right\}, \ \text{for } n \ge 2.$$

• Rotated quadratic cone - A cone in the second-order cone family defined by

$$\left\{ \begin{pmatrix} p \\ q \\ x \end{pmatrix} \in \mathbb{R} \times \mathbb{R} \times \mathbb{R}^{n-2}, \ 2pq \ge x^T x, \ p \ge 0, \ q \ge 0 \right\}, \text{ for } n \ge 3.$$

11.4.2 The Structure of CBF Files

This section defines how information is written in the CBF format, without being specific about the type of information being communicated.

All information items belong to exactly one of the three groups of information. These information groups, and the order they must appear in, are:

- 1. File format.
- 2. Problem structure.
- 3. Problem data.

The first group, file format, provides information on how to interpret the file. The second group, problem structure, provides the information needed to deduce the type and size of the problem instance. Finally, the third group, problem data, specifies the coefficients and constants of the problem instance.

Information items

The format is composed as a list of information items. The first line of an information item is the KEYWORD, revealing the type of information provided. The second line - of some keywords only - is the HEADER, typically revealing the size of information that follows. The remaining lines are the BODY holding the actual information to be specified.



The KEYWORD determines how each line in the HEADER and BODY is structured. Moreover, the number of lines in the BODY follows either from the KEYWORD, the HEADER, or from another information item required to precede it.

Embedded hotstart-sequences

A sequence of problem instances, based on the same problem structure, is within a single file. This is facilitated via the CHANGE within the problem data information group, as a separator between the information items of each instance. The information items following a CHANGE keyword are appending to, or changing (e.g., setting coefficients back to their default value of zero), the problem data of the preceding instance.

The sequence is intended for benchmarking of hotstart capability, where the solvers can reuse their internal state and solution (subject to the achieved accuracy) as warmpoint for the succeeding instance. Whenever this feature is unsupported or undesired, the keyword CHANGE should be interpreted as the end of file.

File encoding and line width restrictions

The format is based on the US-ASCII printable character set with two extensions as listed below. Note, by definition, that none of these extensions can be misinterpreted as printable US-ASCII characters:

- A line feed marks the end of a line, carriage returns are ignored.
- Comment-lines may contain unicode characters in UTF-8 encoding.

The line width is restricted to 512 bytes, with 3 bytes reserved for the potential carriage return, line feed and null-terminator.

Integers and floating point numbers must follow the ISO C decimal string representation in the standard C locale. The format does not impose restrictions on the magnitude of, or number of significant digits in numeric data, but the use of 64-bit integers and 64-bit IEEE 754 floating point numbers should be sufficient to avoid loss of precision.

Comment-line and whitespace rules

The format allows single-line comments respecting the following rule:

• Lines having first byte equal to '#' (US-ASCII 35) are comments, and should be ignored. Comments are only allowed between information items.

Given that a line is not a comment-line, whitespace characters should be handled according to the following rules:

- Leading and trailing whitespace characters should be ignored.
 - The seperator between multiple pieces of information on one line, is either one or more whitespace characters.
- Lines containing only whitespace characters are empty, and should be ignored. Empty lines are only allowed between information items.

11.4.3 Problem Specification

The problem structure

The problem structure defines the objective sense, whether it is minimization and maximization. It also defines the index sets, \mathcal{J} , \mathcal{J}^{PSD} , \mathcal{I} and \mathcal{I}^{PSD} , which are all numbered from zero, $\{0, 1, \ldots\}$, and empty until explicitly constructed.

• Scalar variables are constructed in vectors restricted to a conic domain, such as $(x_0, x_1) \in \mathbb{R}^2_+$, $(x_2, x_3, x_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$x \in \mathcal{K}_1^{n_1} \times \mathcal{K}_2^{n_2} \times \cdots \times \mathcal{K}_k^{n_k}$$

which in the CBF format becomes:

```
VAR
n k
K1 n1
K2 n2
...
Kk nk
```

where $\sum_{i} n_{i} = n$ is the total number of scalar variables. The list of supported cones is found in Table 11.3. Integrality of scalar variables can be specified afterwards.

• **PSD variables** are constructed one-by-one. That is, $X_j \succeq \mathbf{0}^{n_j \times n_j}$ for $j \in \mathcal{J}^{PSD}$, constructs a matrix-valued variable of size $n_j \times n_j$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes:

```
PSDVAR
N
n1
n2
...
nN
```

where N is the total number of PSD variables.

• Scalar constraints are constructed in vectors restricted to a conic domain, such as $(g_0, g_1) \in \mathbb{R}^2_+$, $(g_2, g_3, g_4) \in \mathcal{Q}^3$, etc. In terms of the Cartesian product, this generalizes to

$$g \in \mathcal{K}_1^{m_1} \times \mathcal{K}_2^{m_2} \times \dots \times \mathcal{K}_k^{m_k}$$

which in the CBF format becomes:

```
CON
m k
K1 m1
K2 m2
..
Kk mk
```

where $\sum_{i} m_{i} = m$ is the total number of scalar constraints. The list of supported cones is found in Table 11.3.

• **PSD constraints** are constructed one-by-one. That is, $G_i \succeq \mathbf{0}^{m_i \times m_i}$ for $i \in \mathcal{I}^{PSD}$, constructs a matrix-valued affine expressions of size $m_i \times m_i$ restricted to be symmetric positive semidefinite. In the CBF format, this list of constructions becomes

```
PSDCON
M m1
m2
...
mM
```

where M is the total number of PSD constraints.

With the objective sense, variables (with integer indications) and constraints, the definitions of the many affine expressions follow in problem data.

Problem data

The problem data defines the coefficients and constants of the affine expressions of the problem instance. These are considered zero until explicitly defined, implying that instances with no keywords from this

information group are, in fact, valid. Duplicating or conflicting information is a failure to comply with the standard. Consequently, two coefficients written to the same position in a matrix (or to transposed positions in a symmetric matrix) is an error.

The affine expressions of the objective, g^{obj} , of the scalar constraints, g_i , and of the PSD constraints, G_i , are defined separately. The following notation uses the standard trace inner product for matrices, $\langle X, Y \rangle = \sum_{i,j} X_{ij} Y_{ij}$.

• The affine expression of the objective is defined as

$$g^{obj} = \sum_{j \in \mathcal{J}^{PSD}} \langle F_j^{obj}, X_j \rangle + \sum_{j \in \mathcal{J}} a_j^{obj} x_j + b^{obj},$$

in terms of the symmetric matrices, F_j^{obj} , and scalars, a_j^{obj} and b^{obj} .

• The affine expressions of the scalar constraints are defined, for $i \in \mathcal{I}$, as

$$g_i = \sum_{j \in \mathcal{J}^{PSD}} \langle F_{ij}, X_j \rangle + \sum_{j \in \mathcal{J}} a_{ij} x_j + b_i,$$

in terms of the symmetric matrices, F_{ij} , and scalars, a_{ij} and b_i .

• The affine expressions of the PSD constraints are defined, for $i \in \mathcal{I}^{PSD}$, as

$$G_i = \sum_{j \in \mathcal{J}} x_j H_{ij} + D_i,$$

in terms of the symmetric matrices, H_{ij} and D_i .

List of cones

The format uses an explicit syntax for symmetric positive semidefinite cones as shown above. For scalar variables and constraints, constructed in vectors, the supported conic domains and their minimum sizes are given as follows.

Table 11.3: Cones available in the CBF format

Name	CBF keyword	Cone family
Free domain	F	linear
Positive orthant	L+	linear
Negative orthant	L-	linear
Fixpoint zero	L=	linear
Quadratic cone	Q	second-order
Rotated quadratic cone	QR	second-order

11.4.4 File Format Keywords

VER

Description: The version of the Conic Benchmark Format used to write the file.

HEADER: None

BODY: One line formatted as:

INT

This is the version number.

Must appear exactly once in a file, as the first keyword.

OBJSENSE

Description: Define the objective sense.

HEADER: None

BODY: One line formatted as:

STR

having MIN indicates minimize, and MAX indicates maximize. Capital letters are required.

Must appear exactly once in a file.

PSDVAR

Description: Construct the PSD variables.

HEADER: One line formatted as:

INT

This is the number of PSD variables in the problem.

BODY: A list of lines formatted as:

INT

This indicates the number of rows (equal to the number of columns) in the matrix-valued PSD variable. The number of lines should match the number stated in the header.

VAR

Description: Construct the scalar variables.

HEADER: One line formatted as:

INT INT

This is the number of scalar variables, followed by the number of conic domains they are restricted to.

BODY: A list of lines formatted as:

STR INT

This indicates the cone name (see Table 11.3), and the number of scalar variables restricted to this cone. These numbers should add up to the number of scalar variables stated first in the header. The number of lines should match the second number stated in the header.

INT

Description: Declare integer requirements on a selected subset of scalar variables.

HEADER: one line formatted as:

INT

This is the number of integer scalar variables in the problem.

BODY: a list of lines formatted as:

INT

This indicates the scalar variable index $j \in \mathcal{J}$. The number of lines should match the number stated in the header.

Can only be used after the keyword VAR.

PSDCON

Description: Construct the PSD constraints.

HEADER: One line formatted as:

INT

This is the number of PSD constraints in the problem.

BODY: A list of lines formatted as:

INT

This indicates the number of rows (equal to the number of columns) in the matrix-valued affine expression of the PSD constraint. The number of lines should match the number stated in the header.

Can only be used after these keywords: PSDVAR, VAR.

CON

Description: Construct the scalar constraints.

HEADER: One line formatted as:

INT INT

This is the number of scalar constraints, followed by the number of conic domains they restrict to.

BODY: A list of lines formatted as:

STR INT

This indicates the cone name (see Table 11.3), and the number of affine expressions restricted to this cone. These numbers should add up to the number of scalar constraints stated first in the header. The number of lines should match the second number stated in the header.

Can only be used after these keywords: PSDVAR, VAR

OBJFCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices F_j^{obj} , as used in the objective.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT REAL

This indicates the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

OBJACOORD

Description: Input sparse coordinates (pairs) to define the scalars, a_j^{obj} , as used in the objective.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT REAL

This indicates the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

OBJBCOORD

Description: Input the scalar, b^{obj} , as used in the objective.

HEADER: None.

BODY: One line formatted as:

REAL

This indicates the coefficient value.

FCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, F_{ij} , as used in the scalar constraints.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT INT REAL

This indicates the scalar constraint index $i \in \mathcal{I}$, the PSD variable index $j \in \mathcal{J}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

ACOORD

Description: Input sparse coordinates (triplets) to define the scalars, a_{ij} , as used in the scalar constraints.

 ${\tt HEADER:}$ One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT REAL

This indicates the scalar constraint index $i \in \mathcal{I}$, the scalar variable index $j \in \mathcal{J}$ and the coefficient value. The number of lines should match the number stated in the header.

BCOORD

Description: Input sparse coordinates (pairs) to define the scalars, b_i , as used in the scalar constraints.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT REAL

This indicates the scalar constraint index $i \in \mathcal{I}$ and the coefficient value. The number of lines should match the number stated in the header.

HCOORD

Description: Input sparse coordinates (quintuplets) to define the symmetric matrices, H_{ij} , as used in the PSD constraints.

HEADER: One line formatted as:

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as

INT INT INT INT REAL

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the scalar variable index $j \in \mathcal{J}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

DCOORD

Description: Input sparse coordinates (quadruplets) to define the symmetric matrices, D_i , as used in the PSD constraints.

HEADER: One line formatted as

INT

This is the number of coordinates to be specified.

BODY: A list of lines formatted as:

INT INT INT REAL

This indicates the PSD constraint index $i \in \mathcal{I}^{PSD}$, the row index, the column index and the coefficient value. The number of lines should match the number stated in the header.

CHANGE

Start of a new instance specification based on changes to the previous. Can be interpreted as the end of file when the hotstart-sequence is unsupported or undesired.

BODY: None Header: None

11.4.5 CBF Format Examples

Minimal Working Example

The conic optimization problem (11.6), has three variables in a quadratic cone - first one is integer - and an affine expression in domain 0 (equality constraint).

minimize
$$5.1 x_0$$

subject to $6.2 x_1 + 7.3 x_2 - 8.4 \in \{0\}$
 $x \in \mathcal{Q}^3, x_0 \in \mathbb{Z}.$ (11.6)

Its formulation in the Conic Benchmark Format begins with the version of the CBF format used, to safeguard against later revisions.

```
VER
1
```

Next follows the problem structure, consisting of the objective sense, the number and domain of variables, the indices of integer variables, and the number and domain of scalar-valued affine expressions (i.e., the equality constraint).

```
OBJSENSE
MIN

VAR
3 1
Q 3

INT
1
0

CON
1 1
L= 1
```

Finally follows the problem data, consisting of the coefficients of the objective, the coefficients of the constraints, and the constant terms of the constraints. All data is specified on a sparse coordinate form.

```
OBJACOORD

1
0 5.1

ACOORD
2
0 1 6.2
0 2 7.3

BCOORD
1
0 -8.4
```

This concludes the example.

Mixing Linear, Second-order and Semidefinite Cones

The conic optimization problem (11.7), has a semidefinite cone, a quadratic cone over unordered subindices, and two equality constraints.

The equality constraints are easily rewritten to the conic form, $(g_0, g_1) \in \{0\}^2$, by moving constants such that the right-hand-side becomes zero. The quadratic cone does not fit under the VAR keyword in this variable permutation. Instead, it takes a scalar constraint $(g_2, g_3, g_4) = (x_1, x_0, x_2) \in \mathcal{Q}^3$, with scalar variables constructed as $(x_0, x_1, x_2) \in \mathbb{R}^3$. Its formulation in the CBF format is reported in the following list

```
# File written using this version of the Conic Benchmark Format:
#
      | Version 1.
VER
1
# The sense of the objective is:
     | Minimize.
OBJSENSE
MIN
# One PSD variable of this size:
      | Three times three.
PSDVAR
1
3
# Three scalar variables in this one conic domain:
      | Three are free.
VAR
3 1
F 3
# Five scalar constraints with affine expressions in two conic domains:
     | Two are fixed to zero.
#
      | Three are in conic quadratic domain.
CON
5 2
L= 2
QЗ
# Five coordinates in F^{obj}_j coefficients:
     | F^{obj}[0][0,0] = 2.0
      | F^{obj}[0][1,0] = 1.0
#
      | and more...
OBJFCOORD
0 0 0 2.0
0 1 0 1.0
0 1 1 2.0
```

```
0 2 1 1.0
0 2 2 2.0
# One coordinate in a^{obj}_j coefficients:
\# | a^{obj}[1] = 1.0
OBJACOORD
1
1 1.0
# Nine coordinates in F_ij coefficients:
      | F[0,0][0,0] = 1.0
      | F[0,0][1,1] = 1.0
      | and more...
FCOORD
0 0 0 0 1.0
0 0 1 1 1.0
0 0 2 2 1.0
1 0 0 0 1.0
1 0 1 0 1.0
1 0 2 0 1.0
1 0 1 1 1.0
1 0 2 1 1.0
1 0 2 2 1.0
# Six coordinates in a_ij coefficients:
      | a[0,1] = 1.0
      | a[1,0] = 1.0
#
#
      | and more...
ACOORD
0 1 1.0
1 0 1.0
1 2 1.0
2 1 1.0
3 0 1.0
4 2 1.0
# Two coordinates in b_i coefficients:
      | b[0] = -1.0
      | b[1] = -0.5
BCOORD
0 -1.0
1 -0.5
```

Mixing Semidefinite Variables and Linear Matrix Inequalities

The standard forms in semidefinite optimization are usually based either on semidefinite variables or linear matrix inequalities. In the CBF format, both forms are supported and can even be mixed as shown in.

minimize
$$\left\langle \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 1 \\ 1 & 0 \end{bmatrix}, X_1 \right\rangle + x_1 + x_2 + 1$$
subject to
$$\left\langle \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, X_1 \right\rangle - x_1 - x_2 \qquad \geq 0.0,$$

$$x_1 \begin{bmatrix} 0 & 1 \\ 1 & 3 \end{bmatrix} + x_2 \begin{bmatrix} 3 & 1 \\ 1 & 0 \end{bmatrix} - \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \geq \mathbf{0},$$

$$X_1 \succeq \mathbf{0}.$$

$$(11.8)$$

Its formulation in the CBF format is written in what follows

```
# File written using this version of the Conic Benchmark Format:
#
      | Version 1.
VER
1
# The sense of the objective is:
    | Minimize.
OBJSENSE
MIN
# One PSD variable of this size:
     | Two times two.
PSDVAR
1
2
# Two scalar variables in this one conic domain:
     | Two are free.
VAR
2 1
# One PSD constraint of this size:
# | Two times two.
PSDCON
1
2
# One scalar constraint with an affine expression in this one conic domain:
     | One is greater than or equal to zero.
CON
1 1
L+ 1
# Two coordinates in F^{obj}_j coefficients:
# | F^{obj}[0][0,0] = 1.0
#
     | F^{obj}[0][1,1] = 1.0
OBJFCOORD
2
0 0 0 1.0
0 1 1 1.0
# Two coordinates in a^{obj}_j coefficients:
     | a^{obj}[0] = 1.0
     | a^{obj}[1] = 1.0
OBJACOORD
0 1.0
1 1.0
# One coordinate in b^{obj} coefficient:
     | b^{obj} = 1.0
OBJBCOORD
# One coordinate in F_ij coefficients:
# | F[0,0][1,0] = 1.0
FCOORD
0 0 1 0 1.0
# Two coordinates in a_ij coefficients:
     | a[0,0] = -1.0
```

```
| a[0,1] = -1.0
ACOORD
2
0 0 -1.0
0 1 -1.0
# Four coordinates in H_ij coefficients:
     | H[0,0][1,0] = 1.0
      | H[0,0][1,1] = 3.0
      and more...
HCOORD
0 0 1 0 1.0
0 0 1 1 3.0
0 1 0 0 3.0
0 1 1 0 1.0
# Two coordinates in D_i coefficients:
     | D[0][0,0] = -1.0
      | D[0][1,1] = -1.0
DCOORD
0 0 0 -1.0
0 1 1 -1.0
```

Optimization Over a Sequence of Objectives

The linear optimization problem (11.9), is defined for a sequence of objectives such that hotstarting from one to the next might be advantages.

$$\begin{array}{lll} \text{maximize}_k & g_k^{obj} \\ \text{subject to} & 50 \, x_0 + 31 & \leq & 250 \,, \\ & 3 \, x_0 - 2 x_1 & \geq & -4 \,, \\ & x \in \mathbb{R}_+^2, \end{array} \tag{11.9}$$

given,

```
1. g_0^{obj} = x_0 + 0.64x_1.

2. g_1^{obj} = 1.11x_0 + 0.76x_1.

3. g_2^{obj} = 1.11x_0 + 0.85x_1.
```

Its formulation in the CBF format is reported in Listing 11.5.

Listing 11.5: Problem (11.9) in CBF format.

```
# File written using this version of the Conic Benchmark Format:
#    | Version 1.
VER
1
# The sense of the objective is:
#    | Maximize.
OBJSENSE
MAX
# Two scalar variables in this one conic domain:
#    | Two are nonnegative.
VAR
2 1
L+ 2
```

```
# Two scalar constraints with affine expressions in these two conic domains:
     | One is in the nonpositive domain.
#
      | One is in the nonnegative domain.
CON
2 2
L- 1
L+ 1
# Two coordinates in a^{obj}_j coefficients:
      | a^{obj}[0] = 1.0
      | a^{obj}[1] = 0.64
OBJACOORD
0 1.0
1 0.64
# Four coordinates in a_ij coefficients:
    | a[0,0] = 50.0
     | a[1,0] = 3.0
     | and more...
ACOORD
0 0 50.0
1 0 3.0
0 1 31.0
1 1 -2.0
# Two coordinates in b_i coefficients:
| b[0] = -250.0
     | b[1] = 4.0
BCOORD
0 -250.0
1 4.0
# New problem instance defined in terms of changes.
\# Two coordinate changes in a^{obj}_j coefficients. Now it is:
     | a^{obj}[0] = 1.11
      | a^{obj}[1] = 0.76
OBJACOORD
0 1.11
1 0.76
# New problem instance defined in terms of changes.
CHANGE
# One coordinate change in a^{obj}_j coefficients. Now it is:
      | a^{obj}[0] = 1.11
      | a^{obj}[1] = 0.85
OBJACOORD
1 0.85
```

11.5 The XML (OSiL) Format

MOSEK can write data in the standard OSiL xml format. For a definition of the OSiL format please see http://www.optimizationservices.org/.

Only linear constraints (possibly with integer variables) are supported. By default output files with the extension .xml are written in the OSiL format.

The parameter $MSK_IPAR_WRITE_XML_MODE$ controls if the linear coefficients in the A matrix are written in row or column order.

11.6 The Task Format

The Task format is MOSEK's native binary format. It contains a complete image of a MOSEK task, i.e.

- Problem data: Linear, conic quadratic, semidefinite and quadratic data
- Problem item names: Variable names, constraints names, cone names etc.
- Parameter settings
- Solutions

There are a few things to be aware of:

- The task format *does not* support General Convex problems since these are defined by arbitrary user-defined functions.
- Status of a solution read from a file will always be unknown.

The format is based on the TAR (USTar) file format. This means that the individual pieces of data in a .task file can be examined by unpacking it as a TAR file. Please note that the inverse may not work: Creating a file using TAR will most probably not create a valid **MOSEK** Task file since the order of the entries is important.

11.7 The JSON Format

MOSEK provides the possibility to read/write problems in valid JSON format.

JSON (JavaScript Object Notation) is a lightweight data-interchange format. It is easy for humans to read and write. It is easy for machines to parse and generate. It is based on a subset of the JavaScript Programming Language, Standard ECMA-262 3rd Edition - December 1999. JSON is a text format that is completely language independent but uses conventions that are familiar to programmers of the C-family of languages, including C, C++, C#, Java, JavaScript, Perl, Python, and many others. These properties make JSON an ideal data-interchange language.

The official JSON website http://www.json.org provides plenty of information along with the format definition.

MOSEK defines two JSON-like formats:

- jtask
- \bullet jsol

Warning: Despite being text-based human-readable formats, *jtask* and *jsol* files will include no indentation and no new-lines, in order to keep the files as compact as possible. We therefore strongly advise to use JSON viewer tools to inspect *jtask* and *jsol* files.

11.7.1 jtask format

It stores a problem instance. The jtask format contains the same information as a task format.

Even though a jtask file is human-readable, we do not recommend users to create it by hand, but to rely on **MOSEK**.

11.7.2 jsol format

It stores a problem solution. The jsol format contains all solutions and information items.

11.7.3 A jtask example

In Listing 11.6 we present a file in the jtask format that corresponds to the sample problem from lollp. The listing has been formatted for readability.

Listing 11.6: A formatted *jtask* file for the lol.lp example.

```
{
    "$schema": "http://mosek.com/json/schema#",
    "Task/INFO":{
        "taskname":"lo1",
        "numvar":4,
        "numcon":3,
        "numcone":0,
        "numbarvar":0,
        "numanz":9,
        "numsymmat":0,
         "mosekver":[
            8,
            0,
            0,
             9
    },
    "Task/data":{
        "var":{
             "name":[
                 "x1",
                 "x2",
                 "x3",
                 "x4"
            ],
             "bk":[
                 "lo",
                 "ra",
                 "lo",
                 "lo"
            ],
             "bl":[
                 0.0,
                 0.0,
                 0.0,
                 0.0
            ],
             "bu":[
                 1e+30,
                 1e+1,
                 1e+30,
                 1e+30
            ],
```

```
"type":[
        "cont",
"cont",
         "cont",
         "cont"
    ]
},
"con":{
    "name":[
        "c1",
         "c2",
         "c3"
    ],
    "bk":[
        "fx",
        "lo",
         "up"
    ],
    "bl":[
        3e+1,
        1.5e+1,
             -1e+30
    ],
    "bu":[
        3e+1,
        1e+30,
        2.5e+1
    ]
},
"objective":{
    "sense":"max",
    "name":"obj",
    "c":{
         "subj":[
            0,
            1,
             2,
             3
        ],
         "val":[
            3e+0,
             1e+0,
             5e+0,
             1e+0
        ]
    },
    "cfix":0.0
},
"A":{
    "subi":[
        Ο,
        Ο,
         0,
         1,
         1,
        1,
        1,
        2,
        2
    ],
    "subj":[
        0,
```

```
2,
            0,
            1,
            2,
            3,
            1,
            3
        ],
        "val":[
            3e+0.
            1e+0.
            2e+0,
            2e+0,
            1e+0,
            3e+0,
            1e+0,
            2e+0.
            3e+0
        1
    }
},
"Task/parameters":{
    "iparam":{
        "ANA_SOL_BASIS": "ON",
        "ANA_SOL_PRINT_VIOLATED":"OFF",
        "AUTO_SORT_A_BEFORE_OPT":"OFF",
        "AUTO_UPDATE_SOL_INFO":"OFF",
        "BASIS_SOLVE_USE_PLUS_ONE":"OFF",
        "BI_CLEAN_OPTIMIZER": "OPTIMIZER_FREE",
        "BI_IGNORE_MAX_ITER":"OFF",
        "BI_IGNORE_NUM_ERROR": "OFF",
        "BI_MAX_ITERATIONS":1000000,
        "CACHE_LICENSE": "ON",
        "CHECK_CONVEXITY": "CHECK_CONVEXITY_FULL",
        "COMPRESS_STATFILE":"ON",
        "CONCURRENT_NUM_OPTIMIZERS":2,
        "CONCURRENT_PRIORITY_DUAL_SIMPLEX":2,
        "CONCURRENT_PRIORITY_FREE_SIMPLEX":3,
        "CONCURRENT_PRIORITY_INTPNT":4,
        "CONCURRENT_PRIORITY_PRIMAL_SIMPLEX":1,
        "FEASREPAIR_OPTIMIZE": "FEASREPAIR_OPTIMIZE_NONE",
        "INFEAS_GENERIC_NAMES": "OFF",
        "INFEAS_PREFER_PRIMAL": "ON",
        "INFEAS_REPORT_AUTO":"OFF",
        "INFEAS_REPORT_LEVEL":1,
        "INTPNT_BASIS": "BI_ALWAYS",
        "INTPNT_DIFF_STEP":"ON",
        "INTPNT_FACTOR_DEBUG_LVL":0,
        "INTPNT_FACTOR_METHOD":0,
        "INTPNT_HOTSTART": "INTPNT_HOTSTART_NONE",
        "INTPNT_MAX_ITERATIONS":400,
        "INTPNT_MAX_NUM_COR":-1,
        "INTPNT_MAX_NUM_REFINEMENT_STEPS":-1,
        "INTPNT_OFF_COL_TRH":40,
        "INTPNT_ORDER_METHOD": "ORDER_METHOD_FREE",
        "INTPNT_REGULARIZATION_USE":"ON",
        "INTPNT_SCALING": "SCALING_FREE",
        "INTPNT_SOLVE_FORM": "SOLVE_FREE",
        "INTPNT_STARTING_POINT": "STARTING_POINT_FREE",
        "LIC_TRH_EXPIRY_WRN":7,
        "LICENSE_DEBUG": "OFF",
        "LICENSE_PAUSE_TIME":0,
        "LICENSE_SUPPRESS_EXPIRE_WRNS":"OFF"
```

```
"LICENSE_WAIT": "OFF",
"LOG":10,
"LOG_ANA_PRO":1,
"LOG_BI":4,
"LOG_BI_FREQ":2500,
"LOG_CHECK_CONVEXITY":0,
"LOG_CONCURRENT":1,
"LOG_CUT_SECOND_OPT":1,
"LOG_EXPAND":0,
"LOG_FACTOR":1,
"LOG_FEAS_REPAIR":1,
"LOG_FILE":1,
"LOG_HEAD":1,
"LOG_INFEAS_ANA":1,
"LOG_INTPNT":4,
"LOG_MIO":4,
"LOG_MIO_FREQ":1000,
"LOG_OPTIMIZER":1,
"LOG_ORDER":1,
"LOG PRESOLVE":1.
"LOG_RESPONSE":0,
"LOG_SENSITIVITY":1,
"LOG_SENSITIVITY_OPT":0,
"LOG_SIM":4,
"LOG_SIM_FREQ":1000,
"LOG_SIM_MINOR":1,
"LOG_STORAGE":1,
"MAX_NUM_WARNINGS":10,
"MIO_BRANCH_DIR": "BRANCH_DIR_FREE",
"MIO_CONSTRUCT_SOL": "OFF",
"MIO_CUT_CLIQUE": "ON",
"MIO_CUT_CMIR": "ON",
"MIO_CUT_GMI": "ON",
"MIO_CUT_KNAPSACK_COVER": "OFF",
"MIO_HEURISTIC_LEVEL":-1,
"MIO_MAX_NUM_BRANCHES":-1,
"MIO_MAX_NUM_RELAXS":-1,
"MIO_MAX_NUM_SOLUTIONS":-1,
"MIO_MODE":"MIO_MODE_SATISFIED",
"MIO_MT_USER_CB":"ON",
"MIO_NODE_OPTIMIZER": "OPTIMIZER_FREE",
"MIO_NODE_SELECTION": "MIO_NODE_SELECTION_FREE",
"MIO_PERSPECTIVE_REFORMULATE": "ON",
"MIO_PROBING_LEVEL":-1,
"MIO_RINS_MAX_NODES":-1,
"MIO_ROOT_OPTIMIZER":"OPTIMIZER_FREE",
\verb"MIO_ROOT_REPEAT_PRESOLVE_LEVEL":-1,\\
"MT_SPINCOUNT":0,
"NUM_THREADS":0,
"OPF_MAX_TERMS_PER_LINE":5,
"OPF_WRITE_HEADER": "ON",
"OPF_WRITE_HINTS": "ON",
"OPF_WRITE_PARAMETERS": "OFF",
"OPF_WRITE_PROBLEM": "ON",
"OPF_WRITE_SOL_BAS": "ON",
"OPF_WRITE_SOL_ITG":"ON",
"OPF_WRITE_SOL_ITR":"ON",
"OPF_WRITE_SOLUTIONS": "OFF",
"OPTIMIZER": "OPTIMIZER_FREE",
"PARAM_READ_CASE_NAME":"ON",
"PARAM_READ_IGN_ERROR":"OFF",
"PRESOLVE_ELIMINATOR_MAX_FILL":-1,
"PRESOLVE_ELIMINATOR_MAX_NUM_TRIES":-1,
```

```
"PRESOLVE_LEVEL":-1,
"PRESOLVE_LINDEP_ABS_WORK_TRH":100,
"PRESOLVE_LINDEP_REL_WORK_TRH":100,
"PRESOLVE_LINDEP_USE": "ON"
"PRESOLVE_MAX_NUM_REDUCTIONS":-1,
"PRESOLVE_USE": "PRESOLVE_MODE_FREE",
"PRIMAL_REPAIR_OPTIMIZER": "OPTIMIZER_FREE",
"QO_SEPARABLE_REFORMULATION": "OFF",
"READ_DATA_COMPRESSED": "COMPRESS_FREE",
"READ_DATA_FORMAT": "DATA_FORMAT_EXTENSION",
"READ_DEBUG": "OFF",
"READ_KEEP_FREE_CON": "OFF",
"READ_LP_DROP_NEW_VARS_IN_BOU":"OFF",
"READ_LP_QUOTED_NAMES": "ON",
"READ_MPS_FORMAT": "MPS_FORMAT_FREE",
"READ_MPS_WIDTH":1024,
"READ_TASK_IGNORE_PARAM":"OFF",
"SENSITIVITY_ALL": "OFF",
"SENSITIVITY_OPTIMIZER": "OPTIMIZER_FREE_SIMPLEX",
"SENSITIVITY_TYPE": "SENSITIVITY_TYPE_BASIS",
"SIM_BASIS_FACTOR_USE": "ON",
"SIM_DEGEN": "SIM_DEGEN_FREE".
"SIM_DUAL_CRASH":90,
"SIM_DUAL_PHASEONE_METHOD":0,
"SIM_DUAL_RESTRICT_SELECTION":50,
"SIM_DUAL_SELECTION": "SIM_SELECTION_FREE",
"SIM_EXPLOIT_DUPVEC": "SIM_EXPLOIT_DUPVEC_OFF",
"SIM_HOTSTART": "SIM_HOTSTART_FREE",
"SIM_HOTSTART_LU": "ON",
"SIM_INTEGER":0,
"SIM_MAX_ITERATIONS":10000000,
"SIM_MAX_NUM_SETBACKS":250,
"SIM_NON_SINGULAR": "ON",
"SIM_PRIMAL_CRASH":90,
"SIM_PRIMAL_PHASEONE_METHOD":0,
"SIM_PRIMAL_RESTRICT_SELECTION":50,
"SIM_PRIMAL_SELECTION": "SIM_SELECTION_FREE",
"SIM_REFACTOR_FREQ":0,
"SIM_REFORMULATION": "SIM_REFORMULATION_OFF",
"SIM_SAVE_LU":"OFF",
"SIM_SCALING": "SCALING_FREE",
"SIM_SCALING_METHOD": "SCALING_METHOD_POW2",
"SIM_SOLVE_FORM": "SOLVE_FREE",
"SIM_STABILITY_PRIORITY":50,
"SIM_SWITCH_OPTIMIZER":"OFF"
"SOL_FILTER_KEEP_BASIC":"OFF"
"SOL_FILTER_KEEP_RANGED":"OFF",
\verb"SOL_READ_NAME_WIDTH":-1,\\
"SOL_READ_WIDTH": 1024,
"SOLUTION_CALLBACK":"OFF",
"TIMING_LEVEL":1,
"WRITE_BAS_CONSTRAINTS": "ON",
"WRITE_BAS_HEAD": "ON",
"WRITE_BAS_VARIABLES": "ON",
"WRITE_DATA_COMPRESSED":0,
"WRITE_DATA_FORMAT": "DATA_FORMAT_EXTENSION",
"WRITE_DATA_PARAM":"OFF",
"WRITE_FREE_CON": "OFF",
"WRITE_GENERIC_NAMES":"OFF",
"WRITE_GENERIC_NAMES_IO":1,
"WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS": "OFF",
"WRITE_IGNORE_INCOMPATIBLE_ITEMS": "OFF",
"WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS":"OFF"
```

```
"WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS": "OFF",
    "WRITE_INT_CONSTRAINTS": "ON",
    "WRITE_INT_HEAD": "ON",
    "WRITE_INT_VARIABLES":"ON",
    "WRITE_LP_FULL_OBJ":"ON",
    "WRITE_LP_LINE_WIDTH":80,
    "WRITE_LP_QUOTED_NAMES": "ON",
    "WRITE_LP_STRICT_FORMAT": "OFF",
    "WRITE_LP_TERMS_PER_LINE":10,
    "WRITE_MPS_FORMAT": "MPS_FORMAT_FREE",
    "WRITE_MPS_INT":"ON",
    "WRITE_PRECISION":15,
    "WRITE_SOL_BARVARIABLES": "ON",
    "WRITE_SOL_CONSTRAINTS": "ON",
    "WRITE_SOL_HEAD": "ON",
    "WRITE_SOL_IGNORE_INVALID_NAMES": "OFF",
    "WRITE_SOL_VARIABLES":"ON",
    "WRITE_TASK_INC_SOL":"ON",
    "WRITE_XML_MODE": "WRITE_XML_MODE_ROW"
},
"dparam":{
    "ANA_SOL_INFEAS_TOL":1e-6,
    "BASIS_REL_TOL_S":1e-12,
    "BASIS_TOL_S":1e-6,
    "BASIS_TOL_X":1e-6,
    "CHECK_CONVEXITY_REL_TOL":1e-10,
    "DATA_TOL_AIJ":1e-12,
    "DATA_TOL_AIJ_HUGE":1e+20,
    "DATA_TOL_AIJ_LARGE":1e+10,
    "DATA_TOL_BOUND_INF":1e+16,
    "DATA_TOL_BOUND_WRN":1e+8,
    "DATA_TOL_C_HUGE": 1e+16,
    "DATA_TOL_CJ_LARGE": 1e+8,
    "DATA_TOL_QIJ":1e-16,
    "DATA_TOL_X":1e-8,
    "FEASREPAIR_TOL": 1e-10,
    "INTPNT_CO_TOL_DFEAS":1e-8,
    "INTPNT_CO_TOL_INFEAS":1e-10,
    "INTPNT_CO_TOL_MU_RED":1e-8,
    "INTPNT_CO_TOL_NEAR_REL":1e+3,
    "INTPNT_CO_TOL_PFEAS":1e-8,
    "INTPNT_CO_TOL_REL_GAP":1e-7,
    "INTPNT_NL_MERIT_BAL":1e-4,
    "INTPNT_NL_TOL_DFEAS":1e-8,
    "INTPNT_NL_TOL_MU_RED":1e-12,
    "INTPNT_NL_TOL_NEAR_REL":1e+3,
    "INTPNT_NL_TOL_PFEAS":1e-8,
    "INTPNT_NL_TOL_REL_GAP":1e-6,
    "INTPNT_NL_TOL_REL_STEP":9.95e-1,
    "INTPNT_QO_TOL_DFEAS":1e-8,
    "INTPNT_QO_TOL_INFEAS":1e-10,
    "INTPNT_QO_TOL_MU_RED":1e-8,
    "INTPNT_QO_TOL_NEAR_REL":1e+3,
    "INTPNT_QO_TOL_PFEAS":1e-8,
    "INTPNT_QO_TOL_REL_GAP":1e-8,
    "INTPNT_TOL_DFEAS":1e-8,
    "INTPNT_TOL_DSAFE":1e+0,
    "INTPNT_TOL_INFEAS":1e-10,
    "INTPNT_TOL_MU_RED":1e-16,
    "INTPNT_TOL_PATH":1e-8,
    "INTPNT_TOL_PFEAS":1e-8,
    "INTPNT_TOL_PSAFE":1e+0,
    "INTPNT_TOL_REL_GAP":1e-8,
```

```
"INTPNT_TOL_REL_STEP":9.999e-1,
            "INTPNT_TOL_STEP_SIZE":1e-6,
            "LOWER_OBJ_CUT":-1e+30,
            "LOWER_OBJ_CUT_FINITE_TRH":-5e+29,
            "MIO_DISABLE_TERM_TIME":-1e+0,
            "MIO_MAX_TIME":-1e+0,
            "MIO_MAX_TIME_APRX_OPT":6e+1,
            "MIO_NEAR_TOL_ABS_GAP":0.0,
            "MIO_NEAR_TOL_REL_GAP":1e-3,
            "MIO_REL_GAP_CONST":1e-10,
            "MIO_TOL_ABS_GAP":0.0,
            "MIO_TOL_ABS_RELAX_INT":1e-5,
            "MIO_TOL_FEAS":1e-6,
            "MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT": 0.0,
            "MIO_TOL_REL_GAP":1e-4,
            "MIO_TOL_X":1e-6,
            "OPTIMIZER_MAX_TIME":-1e+0,
            "PRESOLVE_TOL_ABS_LINDEP":1e-6,
            "PRESOLVE_TOL_AIJ":1e-12,
            "PRESOLVE_TOL_REL_LINDEP":1e-10,
            "PRESOLVE_TOL_S":1e-8,
            "PRESOLVE_TOL_X":1e-8,
            "QCQO_REFORMULATE_REL_DROP_TOL":1e-15,
            "SEMIDEFINITE_TOL_APPROX":1e-10,
            "SIM_LU_TOL_REL_PIV":1e-2,
            "SIMPLEX_ABS_TOL_PIV":1e-7,
            "UPPER_OBJ_CUT":1e+30,
            "UPPER_OBJ_CUT_FINITE_TRH":5e+29
        },
        "sparam":{
            "BAS_SOL_FILE_NAME":"",
            "DATA_FILE_NAME": "examples/tools/data/lo1.mps",
            "DEBUG_FILE_NAME":"",
            "INT_SOL_FILE_NAME":""
            "ITR_SOL_FILE_NAME":"",
            "MIO_DEBUG_STRING":"",
            "PARAM_COMMENT_SIGN":"%%",
            "PARAM_READ_FILE_NAME":""
            "PARAM_WRITE_FILE_NAME":"",
            "READ_MPS_BOU_NAME":"",
            "READ_MPS_OBJ_NAME":""
            "READ_MPS_RAN_NAME":"",
            "READ_MPS_RHS_NAME":""
            "SENSITIVITY_FILE_NAME":"",
            "SENSITIVITY_RES_FILE_NAME":"",
            "SOL_FILTER_XC_LOW":"",
            "SOL_FILTER_XC_UPR":"",
            "SOL_FILTER_XX_LOW":"",
            "SOL_FILTER_XX_UPR":"",
            "STAT_FILE_NAME":"",
            "STAT_KEY":"",
            "STAT_NAME":"",
            "WRITE_LP_GEN_VAR_NAME": "XMSKGEN"
        }
   }
}
```

11.8 The Solution File Format

MOSEK provides several solution files depending on the problem type and the optimizer used:

- basis solution file (extension .bas) if the problem is optimized using the simplex optimizer or basis identification is performed,
- interior solution file (extension .sol) if a problem is optimized using the interior-point optimizer and no basis identification is required,
- integer solution file (extension .int) if the problem contains integer constrained variables.

All solution files have the format:

: <problem name> PROBLEM STATUS : <status of the problem> SOLUTION STATUS : <status of the solution> OBJECTIVE NAME : <name of the objective function> PRIMAL OBJECTIVE : <pri>: <pri>imal objective value corresponding to the solution> DUAL OBJECTIVE : <dual objective value corresponding to the solution> CONSTRAINTS INDEX NAME AT ACTIVITY LOWER LIMIT UPPER LIMIT DUAL LOWER DUAL UPPER <name> ?? <a value> <a value> <a value> <a value> <a value> VARIABLES INDEX NAME AT ACTIVITY LOWER LIMIT UPPER LIMIT DUAL LOWER DUAL UPPER CONIC →DUAL ?? <a value> <a value> <a value> <a value> <a value> <a value>

In the example the fields? and <> will be filled with problem and solution specific information. As can be observed a solution report consists of three sections, i.e.

- HEADER In this section, first the name of the problem is listed and afterwards the problem and solution status are shown. Next the primal and dual objective values are displayed.
- CONSTRAINTS For each constraint i of the form

$$l_i^c \le \sum_{j=1}^n a_{ij} x_j \le u_i^c, \tag{11.10}$$

the following information is listed:

- INDEX: A sequential index assigned to the constraint by MOSEK
- NAME: The name of the constraint assigned by the user.
- AT: The status of the constraint. In Table 11.4 the possible values of the status keys and their interpretation are shown.

Table 11.4: Status keys.

Status key	Interpretation
UN	Unknown status
BS	Is basic
SB	Is superbasic
LL	Is at the lower limit (bound)
UL	Is at the upper limit (bound)
EQ	Lower limit is identical to upper limit
**	Is infeasible i.e. the lower limit is greater than the upper limit.

- ACTIVITY: the quantity $\sum_{j=1}^{n} a_{ij}x_{j}^{*}$, where x^{*} is the value of the primal solution.
- LOWER LIMIT: the quantity l_i^c (see (11.10).)
- UPPER LIMIT: the quantity u_i^c (see (11.10).)
- DUAL LOWER: the dual multiplier corresponding to the lower limit on the constraint.
- DUAL UPPER: the dual multiplier corresponding to the upper limit on the constraint.

• VARIABLES The last section of the solution report lists information about the variables. This information has a similar interpretation as for the constraints. However, the column with the header CONIC DUAL is included for problems having one or more conic constraints. This column shows the dual variables corresponding to the conic constraints.

Example: lo1.sol

In Listing 11.7 we show the solution file for the lol.opf problem.

Listing 11.7: An example of .sol file.

27.4.267					
NAME :	:				
	OPTIMAL				
	obj				
	8.33333333e+01				
DUAL OBJECTIVE :	8.33333332e+01				
CONSTRAINTS					
INDEX NAME	AT ACTIVITY	LOWER LIMIT	UPPER LIMIT	ш	
→DUAL LOWER	DUAL UPPER				
0 c1	EQ 3.0000000000000e+01	3.00000000e+01	3.00000000e+01	-0.	
→00000000000000e+00	-2.4999999741654e+00				
1 c2	SB 5.33333333049188e+01	1.50000000e+01	NONE	2.	
→09157603759397e-10	-0.0000000000000e+00				
2 c3	UL 2.4999999842049e+01	NONE	2.50000000e+01	-0.	
→00000000000000e+00	-3.33333332895110e-01				
VARIABLES					
INDEX NAME	AT ACTIVITY	LOWER LIMIT	UPPER LIMIT	Ш	
→DUAL LOWER	DUAL UPPER				
0 x1	LL 1.67020427073508e-09	0.0000000e+00	NONE	-4.	
→49999999528055e+00	-0.0000000000000e+00				
1 x2	LL 2.93510446280504e-09	0.0000000e+00	1.00000000e+01	-2.	
→16666666494916e+00	6.20863861687316e-10				
2 x3	SB 1.49999999899425e+01	0.00000000e+00	NONE	-8.	
→79123177454657e-10	-0.0000000000000e+00				
	SB 8.33333332273116e+00	0.0000000e+00	NONE	-1.	
→69795978899185e-09					

TWELVE

INTERFACE CHANGES

The section show interface-specific changes to the **MOSEK** Rmosek Package in version 8. See the release notes for general changes and new features of the **MOSEK** Optimization Suite.

12.1 Parameters

Added

- MSK_DPAR_DATA_SYM_MAT_TOL
- MSK_DPAR_DATA_SYM_MAT_TOL_HUGE
- MSK_DPAR_DATA_SYM_MAT_TOL_LARGE
- MSK_DPAR_INTPNT_QO_TOL_DFEAS
- MSK_DPAR_INTPNT_QO_TOL_INFEAS
- MSK_DPAR_INTPNT_QO_TOL_MU_RED
- MSK_DPAR_INTPNT_QO_TOL_NEAR_REL
- MSK_DPAR_INTPNT_QO_TOL_PFEAS
- MSK_DPAR_INTPNT_QO_TOL_REL_GAP
- MSK_DPAR_SEMIDEFINITE_TOL_APPROX
- MSK_IPAR_INTPNT_MULTI_THREAD
- MSK_IPAR_LICENSE_TRH_EXPIRY_WRN
- MSK_IPAR_LOG_ANA_PRO
- MSK_IPAR_MIO_CUT_CLIQUE
- MSK_IPAR_MIO_CUT_GMI
- MSK_IPAR_MIO_CUT_IMPLIED_BOUND
- MSK_IPAR_MIO_CUT_KNAPSACK_COVER
- MSK_IPAR_MIO_CUT_SELECTION_LEVEL
- MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE
- MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL
- MSK_IPAR_MIO_VB_DETECTION_LEVEL
- MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL

Removed

- MSK_DPAR_FEASREPAIR_TOL
- MSK_DPAR_MIO_HEURISTIC_TIME
- MSK_DPAR_MIO_MAX_TIME_APRX_OPT
- MSK_DPAR_MIO_REL_ADD_CUT_LIMITED
- MSK_DPAR_MIO_TOL_MAX_CUT_FRAC_RHS
- MSK_DPAR_MIO_TOL_MIN_CUT_FRAC_RHS
- MSK_DPAR_MIO_TOL_REL_RELAX_INT
- MSK_DPAR_MIO_TOL_X
- MSK_DPAR_NONCONVEX_TOL_FEAS
- MSK_DPAR_NONCONVEX_TOL_OPT
- MSK_IPAR_ALLOC_ADD_QNZ
- MSK_IPAR_CONCURRENT_NUM_OPTIMIZERS
- MSK_IPAR_CONCURRENT_PRIORITY_DUAL_SIMPLEX
- MSK_IPAR_CONCURRENT_PRIORITY_FREE_SIMPLEX
- MSK_IPAR_CONCURRENT_PRIORITY_INTPNT
- MSK_IPAR_CONCURRENT_PRIORITY_PRIMAL_SIMPLEX
- MSK_IPAR_FEASREPAIR_OPTIMIZE
- MSK_IPAR_INTPNT_FACTOR_DEBUG_LVL
- MSK_IPAR_INTPNT_FACTOR_METHOD
- MSK_IPAR_LIC_TRH_EXPIRY_WRN
- MSK_IPAR_LOG_CONCURRENT
- MSK_IPAR_LOG_NONCONVEX
- MSK_IPAR_LOG_PARAM
- MSK_IPAR_LOG_SIM_NETWORK_FREQ
- MSK_IPAR_MIO_BRANCH_PRIORITIES_USE
- MSK_IPAR_MIO_CONT_SOL
- MSK_IPAR_MIO_CUT_CG
- MSK_IPAR_MIO_CUT_LEVEL_ROOT
- MSK_IPAR_MIO_CUT_LEVEL_TREE
- MSK_IPAR_MIO_FEASPUMP_LEVEL
- MSK_IPAR_MIO_HOTSTART
- MSK_IPAR_MIO_KEEP_BASIS
- MSK_IPAR_MIO_LOCAL_BRANCH_NUMBER
- MSK_IPAR_MIO_OPTIMIZER_MODE
- MSK_IPAR_MIO_PRESOLVE_AGGREGATE
- MSK_IPAR_MIO_PRESOLVE_PROBING
- MSK_IPAR_MIO_PRESOLVE_USE

- MSK_IPAR_MIO_STRONG_BRANCH
- MSK_IPAR_MIO_USE_MULTITHREADED_OPTIMIZER
- MSK_IPAR_NONCONVEX_MAX_ITERATIONS
- MSK_IPAR_PRESOLVE_ELIM_FILL
- MSK_IPAR_PRESOLVE_ELIMINATOR_USE
- MSK_IPAR_QO_SEPARABLE_REFORMULATION
- MSK_IPAR_READ_ANZ
- MSK_IPAR_READ_CON
- MSK_IPAR_READ_CONE
- MSK_IPAR_READ_MPS_KEEP_INT
- MSK_IPAR_READ_MPS_OBJ_SENSE
- MSK_IPAR_READ_MPS_RELAX
- MSK_IPAR_READ_QNZ
- MSK_IPAR_READ_VAR
- MSK_IPAR_WARNING_LEVEL
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_CONIC_ITEMS
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_NL_ITEMS
- MSK_IPAR_WRITE_IGNORE_INCOMPATIBLE_PSD_ITEMS
- MSK_SPAR_FEASREPAIR_NAME_PREFIX
- MSK_SPAR_FEASREPAIR_NAME_SEPARATOR
- MSK_SPAR_FEASREPAIR_NAME_WSUMVIOL

12.2 Constants

Added

- MSK_BRANCH_DIR_FAR
- MSK_BRANCH_DIR_GUIDED
- MSK_BRANCH_DIR_NEAR
- MSK_BRANCH_DIR_PSEUDOCOST
- $\bullet \ \textit{MSK_BRANCH_DIR_ROOT_LP}$
- MSK_CALLBACK_BEGIN_ROOT_CUTGEN
- MSK_CALLBACK_BEGIN_TO_CONIC
- MSK_CALLBACK_END_ROOT_CUTGEN
- MSK_CALLBACK_END_TO_CONIC
- MSK_CALLBACK_IM_ROOT_CUTGEN
- MSK_CALLBACK_SOLVING_REMOTE
- MSK_DATA_FORMAT_JSON_TASK
- MSK_DINF_MIO_CLIQUE_SEPARATION_TIME

12.2. Constants 213

- MSK_DINF_MIO_CMIR_SEPARATION_TIME
- MSK_DINF_MIO_GMI_SEPARATION_TIME
- MSK_DINF_MIO_IMPLIED_BOUND_TIME
- MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME
- MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION
- MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING
- MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING
- MSK_DINF_SOL_BAS_NRM_BARX
- MSK_DINF_SOL_BAS_NRM_SLC
- MSK_DINF_SOL_BAS_NRM_SLX
- MSK_DINF_SOL_BAS_NRM_SUC
- MSK_DINF_SOL_BAS_NRM_SUX
- MSK_DINF_SOL_BAS_NRM_XC
- MSK_DINF_SOL_BAS_NRM_XX
- MSK_DINF_SOL_BAS_NRM_Y
- MSK_DINF_SOL_ITG_NRM_BARX
- MSK_DINF_SOL_ITG_NRM_XC
- MSK_DINF_SOL_ITG_NRM_XX
- MSK_DINF_SOL_ITR_NRM_BARS
- MSK_DINF_SOL_ITR_NRM_BARX
- MSK_DINF_SOL_ITR_NRM_SLC
- MSK_DINF_SOL_ITR_NRM_SLX
- MSK_DINF_SOL_ITR_NRM_SNX
- MSK_DINF_SOL_ITR_NRM_SUC
- MSK_DINF_SOL_ITR_NRM_SUX
- MSK_DINF_SOL_ITR_NRM_XC
- MSK_DINF_SOL_ITR_NRM_XX
- MSK_DINF_SOL_ITR_NRM_Y
- MSK_DINF_TO_CONIC_TIME
- MSK_IINF_MIO_ABSGAP_SATISFIED
- MSK_IINF_MIO_CLIQUE_TABLE_SIZE
- MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED
- MSK_IINF_MIO_NEAR_RELGAP_SATISFIED
- MSK_IINF_MIO_NODE_DEPTH
- MSK_IINF_MIO_NUM_CMIR_CUTS
- MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS
- MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS
- MSK_IINF_MIO_NUM_REPEATED_PRESOLVE
- MSK_IINF_MIO_PRESOLVED_NUMBIN

- MSK_IINF_MIO_PRESOLVED_NUMCON
- MSK_IINF_MIO_PRESOLVED_NUMCONT
- MSK_IINF_MIO_PRESOLVED_NUMINT
- MSK_IINF_MIO_PRESOLVED_NUMVAR
- MSK_IINF_MIO_RELGAP_SATISFIED
- MSK_LIINF_MIO_PRESOLVED_ANZ
- MSK_LIINF_MIO_SIM_MAXITER_SETBACKS
- MSK_MPS_FORMAT_CPLEX
- MSK_SOL_STA_DUAL_ILLPOSED_CER
- MSK_SOL_STA_PRIM_ILLPOSED_CER

Changed

- MSK_SOL_STA_INTEGER_OPTIMAL
- MSK_SOL_STA_NEAR_INTEGER_OPTIMAL
- MSK_LICENSE_BUFFER_LENGTH

Removed

- MSK_CALLBACKCODE_BEGIN_CONCURRENT
- MSK_CALLBACKCODE_BEGIN_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_BEGIN_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_BEGIN_NETWORK_SIMPLEX
- MSK_CALLBACKCODE_BEGIN_NONCONVEX
- MSK_CALLBACKCODE_BEGIN_SIMPLEX_NETWORK_DETECT
- MSK_CALLBACKCODE_END_CONCURRENT
- MSK_CALLBACKCODE_END_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_END_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_END_NETWORK_SIMPLEX
- MSK_CALLBACKCODE_END_NONCONVEX
- MSK_CALLBACKCODE_END_SIMPLEX_NETWORK_DETECT
- MSK_CALLBACKCODE_IM_MIO_PRESOLVE
- MSK_CALLBACKCODE_IM_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_IM_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_IM_NONCONVEX
- MSK_CALLBACKCODE_NONCOVEX
- MSK_CALLBACKCODE_UPDATE_NETWORK_DUAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_NETWORK_PRIMAL_SIMPLEX
- MSK_CALLBACKCODE_UPDATE_NONCONVEX
- MSK_DINFITEM_CONCURRENT_TIME

12.2. Constants 215

- MSK_DINFITEM_MIO_CG_SEPERATION_TIME
- MSK_DINFITEM_MIO_CMIR_SEPERATION_TIME
- MSK_DINFITEM_SIM_NETWORK_DUAL_TIME
- MSK_DINFITEM_SIM_NETWORK_PRIMAL_TIME
- MSK_DINFITEM_SIM_NETWORK_TIME
- MSK_FEATURE_PTOM
- MSK_FEATURE_PTOX
- MSK_IINFITEM_CONCURRENT_FASTEST_OPTIMIZER
- MSK_IINFITEM_MIO_NUM_BASIS_CUTS
- MSK_IINFITEM_MIO_NUM_CARDGUB_CUTS
- MSK_IINFITEM_MIO_NUM_COEF_REDC_CUTS
- MSK_IINFITEM_MIO_NUM_CONTRA_CUTS
- MSK_IINFITEM_MIO_NUM_DISAGG_CUTS
- MSK_IINFITEM_MIO_NUM_FLOW_COVER_CUTS
- MSK_IINFITEM_MIO_NUM_GCD_CUTS
- MSK_IINFITEM_MIO_NUM_GUB_COVER_CUTS
- MSK_IINFITEM_MIO_NUM_KNAPSUR_COVER_CUTS
- MSK_IINFITEM_MIO_NUM_LATTICE_CUTS
- MSK_IINFITEM_MIO_NUM_LIFT_CUTS
- MSK_IINFITEM_MIO_NUM_OBJ_CUTS
- MSK_IINFITEM_MIO_NUM_PLAN_LOC_CUTS
- MSK_IINFITEM_SIM_NETWORK_DUAL_DEG_ITER
- MSK_IINFITEM_SIM_NETWORK_DUAL_HOTSTART
- MSK_IINFITEM_SIM_NETWORK_DUAL_HOTSTART_LU
- MSK_IINFITEM_SIM_NETWORK_DUAL_INF_ITER
- MSK_IINFITEM_SIM_NETWORK_DUAL_ITER
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_DEG_ITER
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_HOTSTART
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_HOTSTART_LU
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_INF_ITER
- MSK_IINFITEM_SIM_NETWORK_PRIMAL_ITER
- MSK_IINFITEM_SOL_INT_PROSTA
- MSK_IINFITEM_SOL_INT_SOLSTA
- MSK_IINFITEM_STO_NUM_A_CACHE_FLUSHES
- MSK_IINFITEM_STO_NUM_A_TRANSPOSES
- MSK_MIOMODE_LAZY
- MSK_OPTIMIZERTYPE_CONCURRENT
- MSK_OPTIMIZERTYPE_MIXED_INT_CONIC
- MSK_OPTIMIZERTYPE_NETWORK_PRIMAL_SIMPLEX

- MSK_OPTIMIZERTYPE_NONCONVEX
- MSK_OPTIMIZERTYPE_PRIMAL_DUAL_SIMPLEX

12.3 Response Codes

Added

- MSK_RES_ERR_DUPLICATE_AIJ (1385)
- MSK_RES_ERR_JSON_DATA (1179)
- MSK_RES_ERR_JSON_FORMAT (1178)
- MSK_RES_ERR_JSON_MISSING_DATA (1180)
- MSK_RES_ERR_JSON_NUMBER_OVERFLOW (1177)
- MSK_RES_ERR_JSON_STRING (1176)
- MSK_RES_ERR_JSON_SYNTAX (1175)
- MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MATRIX (7002)
- MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MATRIX (7019)
- MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE (7001)
- MSK_RES_ERR_MIXED_CONIC_AND_NL (1501)
- MSK_RES_ERR_SERVER_CONNECT (8000)
- MSK_RES_ERR_SERVER_PROTOCOL (8001)
- MSK_RES_ERR_SERVER_STATUS (8002)
- MSK_RES_ERR_SERVER_TOKEN (8003)
- MSK_RES_ERR_SYM_MAT_HUGE (1482)
- MSK_RES_ERR_SYM_MAT_INVALID (1480)
- MSK_RES_ERR_TASK_WRITE (2562)
- MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC (7153)
- MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD (7150)
- MSK_RES_ERR_TOCONIC_CONSTRAINT_FX (7151)
- MSK_RES_ERR_TOCONIC_CONSTRAINT_RA (7152)
- MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD (7155)
- MSK_RES_WRN_SYM_MAT_LARGE (960)

Removed

- MSK_RES_ERR_AD_INVALID_OPERAND
- MSK_RES_ERR_AD_INVALID_OPERATOR
- MSK_RES_ERR_AD_MISSING_OPERAND
- MSK_RES_ERR_AD_MISSING_RETURN
- MSK_RES_ERR_CONCURRENT_OPTIMIZER
- MSK_RES_ERR_INV_CONIC_PROBLEM

- MSK_RES_ERR_INVALID_BRANCH_DIRECTION
- MSK_RES_ERR_INVALID_BRANCH_PRIORITY
- MSK_RES_ERR_INVALID_NETWORK_PROBLEM
- MSK_RES_ERR_MBT_INCOMPATIBLE
- MSK_RES_ERR_MBT_INVALID
- MSK_RES_ERR_MIXED_PROBLEM
- MSK_RES_ERR_NO_DUAL_INFO_FOR_ITG_SOL
- MSK_RES_ERR_ORD_INVALID
- MSK_RES_ERR_ORD_INVALID_BRANCH_DIR
- MSK_RES_ERR_TOCONIC_CONVERSION_FAIL
- MSK_RES_ERR_TOO_MANY_CONCURRENT_TASKS
- MSK_RES_WRN_TOO_MANY_THREADS_CONCURRENT

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220 Bibliography

Enumerations	MSK_CALLBACK_BEGIN_PRIMAL_SENSITIVITY, 138
MSKaccmodee, 132	MSK_CALLBACK_BEGIN_PRIMAL_SETUP_BI, 138
MSK_ACC_CON, 132	MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX, 137
MSK_ACC_VAR, 132	MSK_CALLBACK_BEGIN_PRIMAL_SIMPLEX_BI, 136
MSKbasindtypee, 132	MSK_CALLBACK_BEGIN_QCQO_REFORMULATE, 138
MSK_BI_ALWAYS, 132	MSK_CALLBACK_BEGIN_READ, 139
MSK_BI_IF_FEASIBLE, 132	MSK_CALLBACK_BEGIN_ROOT_CUTGEN, 134
MSK_BI_NEVER, 132	MSK_CALLBACK_BEGIN_SIMPLEX, 137
MSK_BI_NO_ERROR, 132	MSK_CALLBACK_BEGIN_SIMPLEX_BI, 136
MSK_BI_RESERVERED, 132	MSK_CALLBACK_BEGIN_TO_CONIC, 138
MSKboundkeye, 132	MSK_CALLBACK_BEGIN_WRITE, 139
MSK_BK_FR, 133	MSK_CALLBACK_CONIC, 135
MSK_BK_FX, 133	MSK_CALLBACK_DUAL_SIMPLEX, 135
MSK_BK_LO, 132	MSK_CALLBACK_END_BI, 135
MSK_BK_RA, 133	MSK_CALLBACK_END_CONIC, 135
MSK_BK_UP, 133	MSK_CALLBACK_END_DUAL_BI, 136
MSKbranchdire, 150	MSK_CALLBACK_END_DUAL_SENSITIVITY, 138
MSK_BRANCH_DIR_DOWN, 150	MSK_CALLBACK_END_DUAL_SETUP_BI, 138
MSK_BRANCH_DIR_FAR, 150	MSK_CALLBACK_END_DUAL_SIMPLEX, 137
MSK_BRANCH_DIR_FREE, 150	MSK_CALLBACK_END_DUAL_SIMPLEX_BI, 136
MSK_BRANCH_DIR_GUIDED, 150	MSK_CALLBACK_END_FULL_CONVEXITY_CHECK, 138
MSK_BRANCH_DIR_NEAR, 150	MSK_CALLBACK_END_INFEAS_ANA, 137
MSK_BRANCH_DIR_PSEUDOCOST, 150	MSK_CALLBACK_END_INTPNT, 135
MSK_BRANCH_DIR_ROOT_LP, 150	MSK_CALLBACK_END_LICENSE_WAIT, 138
MSK_BRANCH_DIR_UP, 150	MSK_CALLBACK_END_MIO, 137
MSKcallbackcodee, 134	MSK_CALLBACK_END_OPTIMIZER, 134
MSK_CALLBACK_BEGIN_BI, 135	MSK_CALLBACK_END_PRESOLVE, 134
MSK_CALLBACK_BEGIN_CONIC, 135	MSK_CALLBACK_END_PRIMAL_BI, 135
MSK_CALLBACK_BEGIN_DUAL_BI, 135	MSK_CALLBACK_END_PRIMAL_DUAL_SIMPLEX, 137
MSK_CALLBACK_BEGIN_DUAL_SENSITIVITY, 138	MSK_CALLBACK_END_PRIMAL_DUAL_SIMPLEX_BI,
MSK_CALLBACK_BEGIN_DUAL_SETUP_BI, 138	136
MSK_CALLBACK_BEGIN_DUAL_SIMPLEX, 137	MSK_CALLBACK_END_PRIMAL_REPAIR, 138
MSK_CALLBACK_BEGIN_DUAL_SIMPLEX_BI, 136	MSK_CALLBACK_END_PRIMAL_SENSITIVITY, 138
MSK_CALLBACK_BEGIN_FULL_CONVEXITY_CHECK,	MSK_CALLBACK_END_PRIMAL_SETUP_BI, 138
138	MSK_CALLBACK_END_PRIMAL_SIMPLEX, 137
MSK_CALLBACK_BEGIN_INFEAS_ANA, 137	MSK_CALLBACK_END_PRIMAL_SIMPLEX_BI, 136
MSK_CALLBACK_BEGIN_INTPNT, 135	MSK_CALLBACK_END_QCQO_REFORMULATE, 138
MSK_CALLBACK_BEGIN_LICENSE_WAIT, 138	MSK_CALLBACK_END_READ, 139
MSK_CALLBACK_BEGIN_MIO, 136	MSK_CALLBACK_END_ROOT_CUTGEN, 134
MSK_CALLBACK_BEGIN_OPTIMIZER, 134	MSK_CALLBACK_END_SIMPLEX, 137
MSK_CALLBACK_BEGIN_PRESOLVE, 134	MSK_CALLBACK_END_SIMPLEX_BI, 136
MSK_CALLBACK_BEGIN_PRIMAL_BI, 135	MSK_CALLBACK_END_TO_CONIC, 138
	MSK_CALLBACK_END_WRITE, 139
MSK_CALLBACK_BEGIN_PRIMAL_DUAL_SIMPLEX, 137 MSK_CALLBACK_BEGIN_PRIMAL_DUAL_SIMPLEX_BI,	MSK_CALLBACK_IM_BI, 135
136	MSK_CALLBACK_IM_CONIC, 135
MSK_CALLBACK_BEGIN_PRIMAL_REPAIR, 138	MSK_CALLBACK_IM_DUAL_BI, 135
TION_ORDEDAON_DEGIN_I RITHEL_REPAIR, 190	MSK_CALLBACK_IM_DUAL_SENSIVITY, 137
	,

MSK_CALLBACK_IM_DUAL_SIMPLEX, 137	MSK_DATA_FORMAT_XML, 140
MSK_CALLBACK_IM_FULL_CONVEXITY_CHECK, 138	MSKdinfiteme, 140
MSK_CALLBACK_IM_INTPNT, 135	MSK_DINF_BI_CLEAN_DUAL_TIME, 141
MSK_CALLBACK_IM_LICENSE_WAIT, 138	MSK_DINF_BI_CLEAN_PRIMAL_DUAL_TIME, 141
MSK_CALLBACK_IM_LU, 139	MSK_DINF_BI_CLEAN_PRIMAL_TIME, 140
MSK_CALLBACK_IM_MIO, 137	MSK_DINF_BI_CLEAN_TIME, 140
MSK_CALLBACK_IM_MIO_DUAL_SIMPLEX, 138	MSK_DINF_BI_DUAL_TIME, 140
MSK_CALLBACK_IM_MIO_INTPNT, 137	MSK_DINF_BI_PRIMAL_TIME, 140
MSK_CALLBACK_IM_MIO_PRIMAL_SIMPLEX, 137	MSK_DINF_BI_TIME, 140
MSK_CALLBACK_IM_ORDER, 139	MSK_DINF_INTPNT_DUAL_FEAS, 141
MSK_CALLBACK_IM_PRESOLVE, 134	MSK_DINF_INTPNT_DUAL_OBJ, 141
MSK_CALLBACK_IM_PRIMAL_BI, 135	MSK_DINF_INTPNT_FACTOR_NUM_FLOPS, 145
MSK_CALLBACK_IM_PRIMAL_DUAL_SIMPLEX, 137	MSK_DINF_INTPNT_OPT_STATUS, 141
MSK_CALLBACK_IM_PRIMAL_SENSIVITY, 137	MSK_DINF_INTPNT_ORDER_TIME, 141
MSK_CALLBACK_IM_PRIMAL_SIMPLEX, 137	MSK_DINF_INTPNT_PRIMAL_FEAS, 141
MSK_CALLBACK_IM_QO_REFORMULATE, 138	MSK_DINF_INTPNT_PRIMAL_OBJ, 141
MSK_CALLBACK_IM_READ, 139	MSK_DINF_INTPNT_TIME, 141
MSK_CALLBACK_IM_ROOT_CUTGEN, 134	MSK_DINF_MIO_CLIQUE_SEPARATION_TIME, 142
MSK_CALLBACK_IM_SIMPLEX, 139	MSK_DINF_MIO_CMIR_SEPARATION_TIME, 142
MSK_CALLBACK_IM_SIMPLEX_BI, 136	MSK_DINF_MIO_CONSTRUCT_SOLUTION_OBJ, 142
MSK_CALLBACK_INTPNT, 135	MSK_DINF_MIO_DUAL_BOUND_AFTER_PRESOLVE, 142
MSK_CALLBACK_NEW_INT_MIO, 137	MSK_DINF_MIO_GMI_SEPARATION_TIME, 142
MSK_CALLBACK_PRIMAL_SIMPLEX, 135	MSK_DINF_MIO_HEURISTIC_TIME, 142
MSK_CALLBACK_READ_OPF, 139	MSK_DINF_MIO_IMPLIED_BOUND_TIME, 142
MSK_CALLBACK_READ_OPF_SECTION, 139	MSK_DINF_MIO_KNAPSACK_COVER_SEPARATION_TIME,
MSK_CALLBACK_SOLVING_REMOTE, 139	142
MSK_CALLBACK_UPDATE_DUAL_BI, 136	MSK_DINF_MIO_OBJ_ABS_GAP, 142
MSK_CALLBACK_UPDATE_DUAL_SIMPLEX, 137	MSK_DINF_MIO_OBJ_BOUND, 142
MSK_CALLBACK_UPDATE_DUAL_SIMPLEX_BI, 136	MSK_DINF_MIO_OBJ_INT, 142
MSK_CALLBACK_UPDATE_PRESOLVE, 134	MSK_DINF_MIO_OBJ_REL_GAP, 142
MSK_CALLBACK_UPDATE_PRIMAL_BI, 135	MSK_DINF_MIO_OPTIMIZER_TIME, 141
MSK_CALLBACK_UPDATE_PRIMAL_DUAL_SIMPLEX,	MSK_DINF_MIO_PROBING_TIME, 142
137	MSK_DINF_MIO_ROOT_CUTGEN_TIME, 142
MSK_CALLBACK_UPDATE_PRIMAL_DUAL_SIMPLEX_BI,	MSK_DINF_MIO_ROOT_OPTIMIZER_TIME, 141
136	MSK_DINF_MIO_ROOT_PRESOLVE_TIME, 141
MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX, 137	MSK_DINF_MIO_TIME, 141
MSK_CALLBACK_UPDATE_PRIMAL_SIMPLEX_BI, 136	MSK_DINF_MIO_USER_OBJ_CUT, 142
MSK_CALLBACK_WRITE_OPF, 139	
	MSK_DINF_OPTIMIZER_TIME, 142
MSKcheckconvexitytypee, 139	MSK_DINF_PRESOLVE_ELI_TIME, 143
MSK_CHECK_CONVEXITY_FULL, 139	MSK_DINF_PRESOLVE_LINDEP_TIME, 143
MSK_CHECK_CONVEXITY_NONE, 139	MSK_DINF_PRESOLVE_TIME, 142
MSK_CHECK_CONVEXITY_SIMPLE, 139	MSK_DINF_PRIMAL_REPAIR_PENALTY_OBJ, 145
MSKcompresstypee, 139	MSK_DINF_QCQO_REFORMULATE_MAX_PERTURBATION,
MSK_COMPRESS_FREE, 139	145
MSK_COMPRESS_GZIP, 139	${\tt MSK_DINF_QCQO_REFORMULATE_TIME},\ 145$
MSK_COMPRESS_NONE, 139	MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_COLUMN_SCALING,
MSKconetypee, 139	145
MSK_CT_QUAD, 139	MSK_DINF_QCQO_REFORMULATE_WORST_CHOLESKY_DIAG_SCALING,
MSK_CT_RQUAD, 140	145
MSKdataformate, 140	MSK_DINF_RD_TIME, 143
MSK_DATA_FORMAT_CB, 140	MSK_DINF_SIM_DUAL_TIME, 141
MSK_DATA_FORMAT_EXTENSION, 140	MSK_DINF_SIM_FEAS, 141
MSK_DATA_FORMAT_FREE_MPS, 140	MSK_DINF_SIM_OBJ, 141
MSK_DATA_FORMAT_JSON_TASK, 140	MSK_DINF_SIM_PRIMAL_DUAL_TIME, 141
MSK_DATA_FORMAT_LP, 140	MSK_DINF_SIM_PRIMAL_TIME, 141
MSK_DATA_FORMAT_MPS, 140	MSK_DINF_SIM_TIME, 141
MSK_DATA_FORMAT_OP, 140	MSK_DINF_SOL_BAS_DUAL_OBJ, 144
MSK_DATA_FORMAT_TASK, 140	MSK_DINF_SOL_BAS_DVIOLCON, 144

VOV. D.T. COT. D.C. DVTCT-VAD. 144	VGV TTVT IVI DDG WTV VID 10 110
MSK_DINF_SOL_BAS_DVIOLVAR, 144	MSK_IINF_ANA_PRO_NUM_VAR_LO, 146
MSK_DINF_SOL_BAS_NRM_BARX, 144	MSK_IINF_ANA_PRO_NUM_VAR_RA, 146
MSK_DINF_SOL_BAS_NRM_SLC, 144	MSK_IINF_ANA_PRO_NUM_VAR_UP, 146
MSK_DINF_SOL_BAS_NRM_SLX, 144	MSK_IINF_INTPNT_FACTOR_DIM_DENSE, 146
MSK_DINF_SOL_BAS_NRM_SUC, 144	MSK_IINF_INTPNT_ITER, 146
MSK_DINF_SOL_BAS_NRM_SUX, 144	MSK_IINF_INTPNT_NUM_THREADS, 148
MSK_DINF_SOL_BAS_NRM_XC, 144	MSK_IINF_INTPNT_SOLVE_DUAL, 146
MSK_DINF_SOL_BAS_NRM_XX, 144	MSK_IINF_MIO_ABSGAP_SATISFIED, 148
MSK_DINF_SOL_BAS_NRM_Y, 144	MSK_IINF_MIO_CLIQUE_TABLE_SIZE, 147
MSK_DINF_SOL_BAS_PRIMAL_OBJ, 144	MSK_IINF_MIO_CONSTRUCT_NUM_ROUNDINGS, 147
MSK_DINF_SOL_BAS_PVIOLCON, 144	MSK_IINF_MIO_CONSTRUCT_SOLUTION, 147
MSK_DINF_SOL_BAS_PVIOLVAR, 144	MSK_IINF_MIO_INITIAL_SOLUTION, 148
MSK_DINF_SOL_ITG_NRM_BARX, 144	MSK_IINF_MIO_NEAR_ABSGAP_SATISFIED, 148
MSK_DINF_SOL_ITG_NRM_XC, 144	MSK_IINF_MIO_NEAR_RELGAP_SATISFIED, 148
MSK_DINF_SOL_ITG_NRM_XX, 144	MSK_IINF_MIO_NODE_DEPTH, 147
MSK_DINF_SOL_ITG_PRIMAL_OBJ, 144	MSK_IINF_MIO_NUM_ACTIVE_NODES, 147
MSK_DINF_SOL_ITG_PVIOLBARVAR, 144	MSK_IINF_MIO_NUM_BRANCH, 147
MSK_DINF_SOL_ITG_PVIOLCON, 144	MSK_IINF_MIO_NUM_CLIQUE_CUTS, 147
MSK_DINF_SOL_ITG_PVIOLCONES, 144	MSK_IINF_MIO_NUM_CMIR_CUTS, 147
MSK_DINF_SOL_ITG_PVIOLITG, 144	MSK_IINF_MIO_NUM_GOMORY_CUTS, 148
MSK_DINF_SOL_ITG_PVIOLVAR, 144	MSK_IINF_MIO_NUM_IMPLIED_BOUND_CUTS, 147
MSK_DINF_SOL_ITR_DUAL_OBJ, 143	MSK_IINF_MIO_NUM_INT_SOLUTIONS, 147
MSK_DINF_SOL_ITR_DVIOLBARVAR, 143	MSK_IINF_MIO_NUM_KNAPSACK_COVER_CUTS, 147
MSK_DINF_SOL_ITR_DVIOLCON, 143	MSK_IINF_MIO_NUM_RELAX, 147
MSK_DINF_SOL_ITR_DVIOLCONES, 143	MSK_IINF_MIO_NUM_REPEATED_PRESOLVE, 148
MSK_DINF_SOL_ITR_DVIOLVAR, 143	MSK_IINF_MIO_NUMCON, 147
MSK_DINF_SOL_ITR_NRM_BARS, 143	MSK_IINF_MIO_NUMINT, 147
MSK_DINF_SOL_ITR_NRM_BARX, 143	MSK_IINF_MIO_NUMVAR, 147
MSK_DINF_SOL_ITR_NRM_SLC, 143	MSK_IINF_MIO_OBJ_BOUND_DEFINED, 147
MSK_DINF_SOL_ITR_NRM_SLX, 143	MSK_IINF_MIO_PRESOLVED_NUMBIN, 147
MSK_DINF_SOL_ITR_NRM_SNX, 143	MSK_IINF_MIO_PRESOLVED_NUMCON, 147
MSK_DINF_SOL_ITR_NRM_SUC, 143	MSK_IINF_MIO_PRESOLVED_NUMCONT, 147
MSK_DINF_SOL_ITR_NRM_SUX, 143	MSK_IINF_MIO_PRESOLVED_NUMINT, 147
MSK_DINF_SOL_ITR_NRM_XC, 143	MSK_IINF_MIO_PRESOLVED_NUMVAR, 147
MSK_DINF_SOL_ITR_NRM_XX, 143	MSK_IINF_MIO_RELGAP_SATISFIED, 148
MSK_DINF_SOL_ITR_NRM_Y, 143	MSK_IINF_MIO_TOTAL_NUM_CUTS, 147
MSK_DINF_SOL_ITR_PRIMAL_OBJ, 143	MSK_IINF_MIO_USER_OBJ_CUT, 148
MSK_DINF_SOL_ITR_PVIOLBARVAR, 143	MSK_IINF_OPT_NUMCON, 149
MSK_DINF_SOL_ITR_PVIOLCON, 143	MSK_IINF_OPT_NUMVAR, 149
MSK_DINF_SOL_ITR_PVIOLCONES, 143	MSK_IINF_OPTIMIZE_RESPONSE, 146
MSK_DINF_SOL_ITR_PVIOLVAR, 143	MSK_IINF_RD_NUMBARVAR, 148
MSK_DINF_TO_CONIC_TIME, 142	MSK_IINF_RD_NUMCON, 148
$\mathtt{MSKfeaturee},\ 145$	MSK_IINF_RD_NUMCONE, 149
MSK_FEATURE_PTON, 145	MSK_IINF_RD_NUMINTVAR, 148
MSK_FEATURE_PTS, 145	MSK_IINF_RD_NUMQ, 148
MSKiinfiteme, 146	MSK_IINF_RD_NUMVAR, 148
MSK_IINF_ANA_PRO_NUM_CON, 146	MSK_IINF_RD_PROTYPE, 148
MSK_IINF_ANA_PRO_NUM_CON_EQ, 146	MSK_IINF_SIM_DUAL_DEG_ITER, 148
• *	
MSK_IINF_ANA_PRO_NUM_CON_FR, 146	MSK_IINF_SIM_DUAL_HOTSTART, 149
MSK_IINF_ANA_PRO_NUM_CON_LO, 146	MSK_IINF_SIM_DUAL_HOTSTART_LU, 148
MSK_IINF_ANA_PRO_NUM_CON_RA, 146	MSK_IINF_SIM_DUAL_INF_ITER, 148
MSK_IINF_ANA_PRO_NUM_CON_UP, 146	MSK_IINF_SIM_DUAL_ITER, 148
MSK_IINF_ANA_PRO_NUM_VAR, 146	MSK_IINF_SIM_NUMCON, 149
MSK_IINF_ANA_PRO_NUM_VAR_BIN, 146	MSK_IINF_SIM_NUMVAR, 149
MSK_IINF_ANA_PRO_NUM_VAR_CONT, 146	MSK_IINF_SIM_PRIMAL_DEG_ITER, 149
MSK_IINF_ANA_PRO_NUM_VAR_EQ, 146	MSK_IINF_SIM_PRIMAL_DUAL_DEG_ITER, 149
MSK_IINF_ANA_PRO_NUM_VAR_FR, 146	MSK_IINF_SIM_PRIMAL_DUAL_HOTSTART, 149
MSK_IINF_ANA_PRO_NUM_VAR_INT, 146	MSK_IINF_SIM_PRIMAL_DUAL_HOTSTART_LU, 149
	, _o

MSK_IINF_SIM_PRIMAL_DUAL_INF_ITER, 148	MSK_MIO_MODE_IGNORED, 151
MSK_IINF_SIM_PRIMAL_DUAL_ITER, 148	MSK_MIO_MODE_SATISFIED, 151
MSK_IINF_SIM_PRIMAL_HOTSTART, 149	MSKmionodeseltypee, 151
MSK_IINF_SIM_PRIMAL_HOTSTART_LU, 149	MSK_MIO_NODE_SELECTION_BEST, 151
MSK_IINF_SIM_PRIMAL_INF_ITER, 148	MSK_MIO_NODE_SELECTION_FIRST, 151
MSK_IINF_SIM_PRIMAL_ITER, 148	MSK_MIO_NODE_SELECTION_FREE, 151
MSK_IINF_SIM_SOLVE_DUAL, 149	MSK_MIO_NODE_SELECTION_HYBRID, 151
MSK_IINF_SOL_BAS_PROSTA, 149	MSK_MIO_NODE_SELECTION_PSEUDO, 151
MSK_IINF_SOL_BAS_SOLSTA, 149	MSK_MIO_NODE_SELECTION_WORST, 151
MSK_IINF_SOL_ITG_PROSTA, 149	${\tt MSKmpsformate},151$
MSK_IINF_SOL_ITG_SOLSTA, 149	MSK_MPS_FORMAT_CPLEX, 151
MSK_IINF_SOL_ITR_PROSTA, 149	$MSK_MPS_FORMAT_FREE, 151$
MSK_IINF_SOL_ITR_SOLSTA, 149	MSK_MPS_FORMAT_RELAXED, 151
MSK_IINF_STO_NUM_A_REALLOC, 149	$MSK_MPS_FORMAT_STRICT, 151$
${\tt MSKinftypee},149$	MSKmsgkeye, 151
$MSK_INF_DOU_TYPE, 149$	MSK_MSG_MPS_SELECTED, 151
MSK_INF_INT_TYPE, 150	MSK_MSG_READING_FILE, 151
$MSK_INF_LINT_TYPE, 150$	MSK_MSG_WRITING_FILE, 151
MSKintpnthotstarte, 134	${\tt MSKnametypee},140$
MSK_INTPNT_HOTSTART_DUAL, 134	MSK_NAME_TYPE_GEN, 140
MSK_INTPNT_HOTSTART_NONE, 134	MSK_NAME_TYPE_LP, 140
MSK_INTPNT_HOTSTART_PRIMAL, 134	MSK_NAME_TYPE_MPS, 140
MSK_INTPNT_HOTSTART_PRIMAL_DUAL, 134	${\tt MSKobjsensee},151$
${\tt MSKiomodee},150$	MSK_OBJECTIVE_SENSE_MAXIMIZE, 151
${\tt MSK_IOMODE_READ},150$	${\tt MSK_OBJECTIVE_SENSE_MINIMIZE},\ 151$
MSK_IOMODE_READWRITE, 150	${\tt MSKonoffkeye},151$
MSK_IOMODE_WRITE, 150	MSK_OFF , 152
MSKlanguagee, 132	MSK_ON, 151
MSK_LANG_DAN, 132	$ exttt{MSKoptimizertypee}, 152$
MSK_LANG_ENG , 132	MSK_OPTIMIZER_CONIC, 152
${\tt MSKliinfiteme},145$	${\tt MSK_OPTIMIZER_DUAL_SIMPLEX},\ 152$
MSK_LIINF_BI_CLEAN_DUAL_DEG_ITER, 145	MSK_OPTIMIZER_FREE, 152
MSK_LIINF_BI_CLEAN_DUAL_ITER, 145	MSK_OPTIMIZER_FREE_SIMPLEX, 152
MSK_LIINF_BI_CLEAN_PRIMAL_DEG_ITER, 145	MSK_OPTIMIZER_INTPNT, 152
MSK_LIINF_BI_CLEAN_PRIMAL_DUAL_DEG_ITER,	MSK_OPTIMIZER_MIXED_INT, 152
145	MSK_OPTIMIZER_PRIMAL_SIMPLEX, 152
MSK_LIINF_BI_CLEAN_PRIMAL_DUAL_ITER, 145	${ t MSKorderingtypee},152$
MSK_LIINF_BI_CLEAN_PRIMAL_DUAL_SUB_ITER,	${\tt MSK_ORDER_METHOD_APPMINLOC},152$
145	MSK_ORDER_METHOD_EXPERIMENTAL, 152
MSK_LIINF_BI_CLEAN_PRIMAL_ITER, 145	MSK_ORDER_METHOD_FORCE_GRAPHPAR, 152
MSK_LIINF_BI_DUAL_ITER, 145	MSK_ORDER_METHOD_FREE, 152
MSK_LIINF_BI_PRIMAL_ITER, 145	MSK_ORDER_METHOD_NONE, 152
MSK_LIINF_INTPNT_FACTOR_NUM_NZ, 145	MSK_ORDER_METHOD_TRY_GRAPHPAR, 152
MSK_LIINF_MIO_INTPNT_ITER, 145	${\tt MSKparametertypee},152$
MSK_LIINF_MIO_PRESOLVED_ANZ, 145	MSK_PAR_DOU_TYPE, 152
MSK_LIINF_MIO_SIM_MAXITER_SETBACKS, 146	MSK_PAR_INT_TYPE, 153
MSK_LIINF_MIO_SIMPLEX_ITER, 145	MSK_PAR_INVALID_TYPE, 152
MSK_LIINF_RD_NUMANZ, 146	MSK_PAR_STR_TYPE, 153
MSK_LIINF_RD_NUMQNZ, 146	t MSKpresolvemodee, 152
MSKmarke, 133	$\texttt{MSK_PRESOLVE_MODE_FREE},\ 152$
MSK_MARK_LO, 133	MSK_PRESOLVE_MODE_OFF, 152
MSK_MARK_UP, 133	MSK_PRESOLVE_MODE_ON, 152
MSKmiocontsoltypee, 150	${\tt MSKproblemiteme},153$
MSK_MIO_CONT_SOL_ITG, 150	$\texttt{MSK_PI_CON}, 153$
MSK_MIO_CONT_SOL_ITG_REL, 150	MSK_PI_CONE, 153
MSK_MIO_CONT_SOL_NONE, 150	MSK_PI_VAR, 153
MSK_MIO_CONT_SOL_ROOT, 150	${\tt MSKproblemtypee},153$
${\tt MSKmiomodee},151$	MSK_PROBTYPE_CONIC, 153

$MSK_PROBTYPE_GECO, 153$	MSK_SIM_SELECTION_FULL, 155
$MSK_PROBTYPE_LO, 153$	MSK_SIM_SELECTION_PARTIAL, 155
$MSK_PROBTYPE_MIXED, 153$	MSK_SIM_SELECTION_SE, 155
MSK_PROBTYPE_QCQO, 153	${\tt MSKsoliteme},155$
$MSK_PROBTYPE_QO, 153$	MSK_SOL_ITEM_SLC, 155
MSKprostae, 153	MSK_SOL_ITEM_SLX, 155
MSK_PRO_STA_DUAL_FEAS, 153	MSK_SOL_ITEM_SNX, 155
MSK_PRO_STA_DUAL_INFEAS, 153	MSK_SOL_ITEM_SUC, 155
MSK_PRO_STA_ILL_POSED, 154	MSK_SOL_ITEM_SUX, 155
MSK_PRO_STA_NEAR_DUAL_FEAS, 153	MSK_SOL_ITEM_XC, 155
MSK_PRO_STA_NEAR_PRIM_AND_DUAL_FEAS, 153	MSK_SOL_ITEM_XX, 155
MSK_PRO_STA_NEAR_PRIM_FEAS, 153	MSK_SOL_ITEM_Y, 155
MSK_PRO_STA_PRIM_AND_DUAL_FEAS, 153	MSKsolstae, 155
MSK_PRO_STA_PRIM_AND_DUAL_INFEAS, 154	MSK_SOL_STA_DUAL_FEAS, 155
MSK_PRO_STA_PRIM_FEAS, 153	MSK_SOL_STA_DUAL_ILLPOSED_CER, 156
MSK_PRO_STA_PRIM_INFEAS, 153	MSK_SOL_STA_DUAL_INFEAS_CER, 156
MSK_PRO_STA_PRIM_INFEAS_OR_UNBOUNDED, 154	MSK_SOL_STA_INTEGER_OPTIMAL, 156
MSK_PRO_STA_UNKNOWN, 153	MSK_SOL_STA_NEAR_DUAL_FEAS, 156
MSKrescodetypee, 154	MSK_SOL_STA_NEAR_DUAL_INFEAS_CER, 156
MSK_RESPONSE_ERR, 154	MSK_SOL_STA_NEAR_INTEGER_OPTIMAL, 156
MSK_RESPONSE_OK, 154	$MSK_SOL_STA_NEAR_OPTIMAL, 156$
MSK_RESPONSE_TRM, 154	MSK_SOL_STA_NEAR_PRIM_AND_DUAL_FEAS, 156
MSK_RESPONSE_UNK, 154	MSK_SOL_STA_NEAR_PRIM_FEAS, 156
MSK_RESPONSE_WRN, 154	MSK_SOL_STA_NEAR_PRIM_INFEAS_CER, 156
${\tt MSKscalingmethode},154$	MSK_SOL_STA_OPTIMAL, 155
MSK_SCALING_METHOD_FREE, 154	MSK_SOL_STA_PRIM_AND_DUAL_FEAS, 156
MSK_SCALING_METHOD_POW2, 154	MSK_SOL_STA_PRIM_FEAS, 155
MSKscalingtypee, 154	MSK_SOL_STA_PRIM_ILLPOSED_CER, 156
MSK_SCALING_AGGRESSIVE, 154	MSK_SOL_STA_PRIM_INFEAS_CER, 156
MSK_SCALING_FREE, 154	MSK_SOL_STA_UNKNOWN, 155
MSK_SCALING_MODERATE, 154	MSKsoltypee, 156
MSK_SCALING_NONE, 154	MSK_SOL_BAS, 156
MSKsensitivitytypee, 154	MSK_SOL_ITG, 156
MSK_SENSITIVITY_TYPE_BASIS, 154	MSK_SOL_ITR, 156
MSK_SENSITIVITY_TYPE_OPTIMAL_PARTITION, 155	MSKsolveforme, 156
MSKsimdegene, 133	MSK_SOLVE_DUAL, 156
MSK_SIM_DEGEN_AGGRESSIVE, 133	MSK_SOLVE_FREE, 156
MSK_SIM_DEGEN_FREE, 133	MSK_SOLVE_PRIMAL, 156
MSK_SIM_DEGEN_MINIMUM, 133	MSKstakeye, 156
MSK_SIM_DEGEN_MODERATE, 133	MSK_SK_BAS, 157
MSK_SIM_DEGEN_NONE, 133	MSK_SK_FIX, 157
MSKsimdupvece, 134	MSK_SK_INF, 157
MSK_SIM_EXPLOIT_DUPVEC_FREE, 134	MSK_SK_LOW, 157
MSK_SIM_EXPLOIT_DUPVEC_OFF, 134	MSK_SK_SUPBAS, 157
MSK_SIM_EXPLOIT_DUPVEC_ON, 134	MSK_SK_UNK, 156
MSKsimhotstarte, 134	MSK_SK_UPR, 157
MSK_SIM_HOTSTART_FREE, 134	MSKstartpointtypee, 157
MSK_SIM_HOTSTART_NONE, 134	MSK_STARTING_POINT_CONSTANT, 157
MSK_SIM_HOTSTART_STATUS_KEYS, 134	MSK_STARTING_POINT_FREE, 157
MSKsimreforme, 133	MSK_STARTING_POINT_GUESS, 157
MSK_SIM_REFORMULATION_AGGRESSIVE, 133	MSK_STARTING_POINT_SATISFY_BOUNDS, 157
MSK_SIM_REFORMULATION_FREE, 133	MSKstreamtypee, 157
MSK_SIM_REFORMULATION_OFF, 133	MSK_STREAM_ERR, 157
MSK_SIM_REFORMULATION_ON, 133	$MSK_STREAM_LOG, 157$
${\tt MSKsimseltypee},155$	MSK_STREAM_MSG, 157
MSK_SIM_SELECTION_ASE, 155	MSK_STREAM_WRN, 157
MSK_SIM_SELECTION_DEVEX, 155	MSKsymmattypee, 140
MSK_SIM_SELECTION_FREE, 155	MSK_SYMMAT_TYPE_SPARSE, 140

MSKtransposee, 133	MSK_DPAR_INTPNT_QO_TOL_NEAR_REL, 68
MSK_TRANSPOSE_NO, 133	MSK_DPAR_INTPNT_QO_TOL_PFEAS, 68
MSK_TRANSPOSE_YES, 133	MSK_DPAR_INTPNT_QO_TOL_REL_GAP, 68
MSKuploe, 133	MSK_DPAR_INTPNT_TOL_DFEAS, 68
MSK_UPLO_LO, 133	MSK_DPAR_INTPNT_TOL_DSAFE, 68
MSK_UPLO_UP, 133	MSK_DPAR_INTPNT_TOL_INFEAS, 69
MSKvaluee, 157	MSK_DPAR_INTPNT_TOL_MU_RED, 69
MSK_LICENSE_BUFFER_LENGTH, 157	MSK_DPAR_INTPNT_TOL_PATH, 69
MSK_MAX_STR_LEN, 157	MSK_DPAR_INTPNT_TOL_PFEAS, 69
MSKvariabletypee, 157	MSK_DPAR_INTPNT_TOL_PSAFE, 69
MSK_VAR_TYPE_CONT, 157	MSK_DPAR_INTPNT_TOL_REL_GAP, 69
MSK_VAR_TYPE_INT, 158	MSK_DPAR_INTPNT_TOL_REL_STEP, 69
MSKxmlwriteroutputtypee, 154	MSK_DPAR_INTPNT_TOL_STEP_SIZE, 69
MSK_WRITE_XML_MODE_COL, 154	MSK_DPAR_LOWER_OBJ_CUT, 70
MSK_WRITE_XML_MODE_ROW, 154	MSK_DPAR_LOWER_OBJ_CUT_FINITE_TRH, 70
MBK_WILLE_KML_MODE_ROW, 194	MSK_DPAR_MIO_DISABLE_TERM_TIME, 70
Functions	
	MSK_DPAR_MIO_MAX_TIME, 70
mosek (mosek), 59	MSK_DPAR_MIO_NEAR_TOL_ABS_GAP, 70
mosek_clean (mosek_clean), 59	MSK_DPAR_MIO_NEAR_TOL_REL_GAP, 71
mosek_read (mosek_read), 59	MSK_DPAR_MIO_REL_GAP_CONST, 71
mosek_version (mosek_version), 59	MSK_DPAR_MIO_TOL_ABS_GAP, 71
mosek_write (mosek_write), 60	MSK_DPAR_MIO_TOL_ABS_RELAX_INT, 71
Danie	MSK_DPAR_MIO_TOL_FEAS, 71
Parameters	MSK_DPAR_MIO_TOL_REL_DUAL_BOUND_IMPROVEMENT
Double params, 63	71
MSK_DPAR_ANA_SOL_INFEAS_TOL, 63	MSK_DPAR_MIO_TOL_REL_GAP, 71
MSK_DPAR_BASIS_REL_TOL_S, 64	MSK_DPAR_OPTIMIZER_MAX_TIME, 71
MSK_DPAR_BASIS_TOL_S, 64	MSK_DPAR_PRESOLVE_TOL_ABS_LINDEP, 72
MSK_DPAR_BASIS_TOL_X, 64	MSK_DPAR_PRESOLVE_TOL_AIJ, 72
MSK_DPAR_CHECK_CONVEXITY_REL_TOL, 64	MSK_DPAR_PRESOLVE_TOL_REL_LINDEP, 72
MSK_DPAR_DATA_SYM_MAT_TOL, 64	MSK_DPAR_PRESOLVE_TOL_S, 72
MSK_DPAR_DATA_SYM_MAT_TOL_HUGE, 64	MSK_DPAR_PRESOLVE_TOL_X, 72
MSK_DPAR_DATA_SYM_MAT_TOL_LARGE, 64	MSK_DPAR_QCQO_REFORMULATE_REL_DROP_TOL, 72
MSK_DPAR_DATA_TOL_AIJ, 65	MSK_DPAR_SEMIDEFINITE_TOL_APPROX, 72
MSK_DPAR_DATA_TOL_AIJ_HUGE, 65	MSK_DPAR_SIM_LU_TOL_REL_PIV, 72
MSK_DPAR_DATA_TOL_AIJ_LARGE, 65	MSK_DPAR_SIMPLEX_ABS_TOL_PIV, 72
MSK_DPAR_DATA_TOL_BOUND_INF, 65	MSK_DPAR_UPPER_OBJ_CUT, 73
MSK_DPAR_DATA_TOL_BOUND_WRN, 65	MSK_DPAR_UPPER_OBJ_CUT_FINITE_TRH, 73
MSK_DPAR_DATA_TOL_C_HUGE, 65	Integer params, 73
MSK_DPAR_DATA_TOL_CJ_LARGE, 65	MSK_IPAR_ANA_SOL_BASIS, 73
MSK_DPAR_DATA_TOL_QIJ, 65	MSK_IPAR_ANA_SOL_PRINT_VIOLATED, 73
MSK_DPAR_DATA_TOL_X, 66	MSK_IPAR_AUTO_SORT_A_BEFORE_OPT, 73
MSK_DPAR_INTPNT_CO_TOL_DFEAS, 66	MSK_IPAR_AUTO_UPDATE_SOL_INFO, 73
MSK_DPAR_INTPNT_CO_TOL_INFEAS, 66	MSK_IPAR_BASIS_SOLVE_USE_PLUS_ONE, 74
MSK_DPAR_INTPNT_CO_TOL_MU_RED, 66	MSK_IPAR_BI_CLEAN_OPTIMIZER, 74
MSK_DPAR_INTPNT_CO_TOL_NEAR_REL, 66	MSK_IPAR_BI_IGNORE_MAX_ITER, 74
MSK_DPAR_INTPNT_CO_TOL_PFEAS, 66	MSK_IPAR_BI_IGNORE_NUM_ERROR, 74
MSK_DPAR_INTPNT_CO_TOL_REL_GAP, 66	MSK_IPAR_BI_MAX_ITERATIONS, 74
MSK_DPAR_INTPNT_NL_MERIT_BAL, 67	MSK_IPAR_CACHE_LICENSE, 74
MSK_DPAR_INTPNT_NL_TOL_DFEAS, 67	MSK_IPAR_CHECK_CONVEXITY, 75
MSK_DPAR_INTPNT_NL_TOL_MU_RED, 67	MSK_IPAR_COMPRESS_STATFILE, 75
MSK_DPAR_INTPNT_NL_TOL_NEAR_REL, 67	MSK_IPAR_INFEAS_GENERIC_NAMES, 75
MSK_DPAR_INTPNT_NL_TOL_PFEAS, 67	MSK_IPAR_INFEAS_PREFER_PRIMAL, 75
MSK_DPAR_INTPNT_NL_TOL_REL_GAP, 67	MSK_IPAR_INFEAS_REPORT_AUTO, 75
MSK_DPAR_INTPNT_NL_TOL_REL_STEP, 67	MSK_IPAR_INFEAS_REPORT_LEVEL, 75
MSK_DPAR_INTPNT_QO_TOL_DFEAS, 67	MSK_IPAR_INTPNT_BASIS, 75
MSK_DPAR_INTPNT_QO_TOL_INFEAS, 68	MSK_IPAR_INTPNT_DIFF_STEP, 75
MSK_DPAR_INTPNT_QO_TOL_MU_RED, 68	MSK_IPAR_INTPNT_HOTSTART, 76

```
MSK_IPAR_INTPNT_MAX_ITERATIONS, 76
                                              MSK_IPAR_MIO_PERSPECTIVE_REFORMULATE, 83
MSK_IPAR_INTPNT_MAX_NUM_COR, 76
                                              MSK_IPAR_MIO_PROBING_LEVEL, 84
MSK_IPAR_INTPNT_MAX_NUM_REFINEMENT_STEPS,
                                              MSK_IPAR_MIO_RINS_MAX_NODES, 84
                                              MSK_IPAR_MIO_ROOT_OPTIMIZER, 84
                                              MSK_IPAR_MIO_ROOT_REPEAT_PRESOLVE_LEVEL, 84
MSK_IPAR_INTPNT_MULTI_THREAD, 76
MSK_IPAR_INTPNT_OFF_COL_TRH, 76
                                              MSK_IPAR_MIO_VB_DETECTION_LEVEL, 84
MSK_IPAR_INTPNT_ORDER_METHOD, 76
                                              MSK_IPAR_MT_SPINCOUNT, 85
MSK_IPAR_INTPNT_REGULARIZATION_USE, 76
                                              MSK_IPAR_NUM_THREADS, 85
MSK_IPAR_INTPNT_SCALING, 77
                                              MSK_IPAR_OPF_MAX_TERMS_PER_LINE, 85
MSK_IPAR_INTPNT_SOLVE_FORM, 77
                                              MSK_IPAR_OPF_WRITE_HEADER, 85
                                              {\tt MSK\_IPAR\_OPF\_WRITE\_HINTS},~85
MSK_IPAR_INTPNT_STARTING_POINT, 77
MSK_IPAR_LICENSE_DEBUG, 77
                                              MSK_IPAR_OPF_WRITE_PARAMETERS, 85
MSK_IPAR_LICENSE_PAUSE_TIME, 77
                                              MSK_IPAR_OPF_WRITE_PROBLEM, 85
MSK_IPAR_LICENSE_SUPPRESS_EXPIRE_WRNS, 77
                                              MSK_IPAR_OPF_WRITE_SOL_BAS, 86
MSK_IPAR_LICENSE_TRH_EXPIRY_WRN, 77
                                              MSK_IPAR_OPF_WRITE_SOL_ITG, 86
MSK_IPAR_LICENSE_WAIT, 77
                                              MSK_IPAR_OPF_WRITE_SOL_ITR, 86
MSK_IPAR_LOG, 78
                                              MSK_IPAR_OPF_WRITE_SOLUTIONS, 85
MSK_IPAR_LOG_ANA_PRO, 78
                                              MSK_IPAR_OPTIMIZER, 86
MSK_IPAR_LOG_BI, 78
                                              MSK_IPAR_PARAM_READ_CASE_NAME, 86
                                              MSK_IPAR_PARAM_READ_IGN_ERROR, 86
MSK_IPAR_LOG_BI_FREQ, 78
MSK_IPAR_LOG_CHECK_CONVEXITY, 78
                                              MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_FILL, 86
                                              MSK_IPAR_PRESOLVE_ELIMINATOR_MAX_NUM_TRIES,
MSK_IPAR_LOG_CUT_SECOND_OPT, 78
MSK_IPAR_LOG_EXPAND, 79
MSK_IPAR_LOG_FACTOR, 79
                                              MSK_IPAR_PRESOLVE_LEVEL, 87
                                              MSK_IPAR_PRESOLVE_LINDEP_ABS_WORK_TRH, 87
MSK_IPAR_LOG_FEAS_REPAIR, 79
MSK_IPAR_LOG_FILE, 79
                                              MSK_IPAR_PRESOLVE_LINDEP_REL_WORK_TRH, 87
MSK_IPAR_LOG_HEAD, 79
                                              MSK_IPAR_PRESOLVE_LINDEP_USE, 87
MSK_IPAR_LOG_INFEAS_ANA, 79
                                              MSK_IPAR_PRESOLVE_MAX_NUM_REDUCTIONS, 87
MSK_IPAR_LOG_INTPNT, 79
                                              MSK_IPAR_PRESOLVE_USE, 87
                                              MSK_IPAR_PRIMAL_REPAIR_OPTIMIZER, 87
MSK_IPAR_LOG_MIO, 79
MSK_IPAR_LOG_MIO_FREQ, 80
                                              MSK_IPAR_READ_DATA_COMPRESSED, 87
MSK_IPAR_LOG_OPTIMIZER, 80
                                              MSK_IPAR_READ_DATA_FORMAT, 88
MSK_IPAR_LOG_ORDER, 80
                                              MSK_IPAR_READ_DEBUG, 88
MSK_IPAR_LOG_PRESOLVE, 80
                                              MSK_IPAR_READ_KEEP_FREE_CON, 88
MSK_IPAR_LOG_RESPONSE, 80
                                              MSK_IPAR_READ_LP_DROP_NEW_VARS_IN_BOU, 88
MSK_IPAR_LOG_SENSITIVITY, 80
                                              MSK_IPAR_READ_LP_QUOTED_NAMES, 88
MSK_IPAR_LOG_SENSITIVITY_OPT, 80
                                              MSK_IPAR_READ_MPS_FORMAT, 88
MSK_IPAR_LOG_SIM, 81
                                              MSK_IPAR_READ_MPS_WIDTH, 88
                                              MSK_IPAR_READ_TASK_IGNORE_PARAM, 88
MSK_IPAR_LOG_SIM_FREQ, 81
MSK_IPAR_LOG_SIM_MINOR, 81
                                              MSK_IPAR_SENSITIVITY_ALL, 89
                                              MSK_IPAR_SENSITIVITY_OPTIMIZER, 89
MSK_IPAR_LOG_STORAGE, 81
MSK_IPAR_MAX_NUM_WARNINGS, 81
                                              MSK_IPAR_SENSITIVITY_TYPE, 89
MSK_IPAR_MIO_BRANCH_DIR, 81
                                              MSK_IPAR_SIM_BASIS_FACTOR_USE, 89
MSK_IPAR_MIO_CONSTRUCT_SOL, 81
                                              MSK_IPAR_SIM_DEGEN, 89
MSK_IPAR_MIO_CUT_CLIQUE, 82
                                              MSK_IPAR_SIM_DUAL_CRASH, 89
MSK_IPAR_MIO_CUT_CMIR, 82
                                              MSK_IPAR_SIM_DUAL_PHASEONE_METHOD, 89
                                              {\tt MSK\_IPAR\_SIM\_DUAL\_RESTRICT\_SELECTION},~90
MSK_IPAR_MIO_CUT_GMI, 82
MSK_IPAR_MIO_CUT_IMPLIED_BOUND, 82
                                              MSK_IPAR_SIM_DUAL_SELECTION, 90
MSK_IPAR_MIO_CUT_KNAPSACK_COVER, 82
                                              MSK_IPAR_SIM_EXPLOIT_DUPVEC, 90
MSK_IPAR_MIO_CUT_SELECTION_LEVEL, 82
                                              MSK_IPAR_SIM_HOTSTART, 90
                                              MSK_IPAR_SIM_HOTSTART_LU, 90
MSK_IPAR_MIO_HEURISTIC_LEVEL, 82
                                              MSK_IPAR_SIM_INTEGER, 90
MSK_IPAR_MIO_MAX_NUM_BRANCHES, 83
                                              {\tt MSK\_IPAR\_SIM\_MAX\_ITERATIONS},~90
MSK_IPAR_MIO_MAX_NUM_RELAXS, 83
MSK_IPAR_MIO_MAX_NUM_SOLUTIONS, 83
                                              MSK_IPAR_SIM_MAX_NUM_SETBACKS, 90
MSK_IPAR_MIO_MODE, 83
                                              MSK_IPAR_SIM_NON_SINGULAR, 91
MSK_IPAR_MIO_MT_USER_CB, 83
                                              MSK_IPAR_SIM_PRIMAL_CRASH, 91
MSK_IPAR_MIO_NODE_OPTIMIZER, 83
                                              MSK_IPAR_SIM_PRIMAL_PHASEONE_METHOD, 91
MSK_IPAR_MIO_NODE_SELECTION, 83
                                              MSK_IPAR_SIM_PRIMAL_RESTRICT_SELECTION, 91
```

MSK_SPAR_REMOTE_ACCESS_TOKEN, 98 MSK_SPAR_SENSITIVITY_FILE_NAME, 98 MSK_SPAR_SENSITIVITY_RES_FILE_NAME, 98 MSK_SPAR_SOL_FILTER_XC_LOW, 98 MSK_SPAR_SOL_FILTER_XC_UPR, 98 MSK_SPAR_SOL_FILTER_XX_LOW, 99
MSK_SPAR_SENSITIVITY_RES_FILE_NAME, 98 MSK_SPAR_SOL_FILTER_XC_LOW, 98 MSK_SPAR_SOL_FILTER_XC_UPR, 98 MSK_SPAR_SOL_FILTER_XX_LOW, 99
MSK_SPAR_SOL_FILTER_XC_LOW, 98 MSK_SPAR_SOL_FILTER_XC_UPR, 98 MSK_SPAR_SOL_FILTER_XX_LOW, 99
MSK_SPAR_SOL_FILTER_XC_UPR, 98 MSK_SPAR_SOL_FILTER_XX_LOW, 99
MSK_SPAR_SOL_FILTER_XC_UPR, 98 MSK_SPAR_SOL_FILTER_XX_LOW, 99
MSK_SPAR_SOL_FILTER_XX_LOW, 99
MSK_SPAR_SOL_FILTER_XX_UPR, 99
MSK_SPAR_STAT_FILE_NAME, 99
MSK_SPAR_STAT_KEY, 99
MSK_SPAR_STAT_NAME, 99
MSK_SPAR_WRITE_LP_GEN_VAR_NAME, 99
MSK_SFAK_WRITE_EF_GEN_VAK_NAME, 99
Response codes
•
MSK_RES_OK (ok), 111
MSK_RES_TRM_INTERNAL (trm_internal), 111
MSK_RES_TRM_INTERNAL_STOP
$(trm_internal_stop),\ 111$
MSK_RES_TRM_MAX_ITERATIONS
$(trm_max_iterations), 111$
MSK_RES_TRM_MAX_NUM_SETBACKS
$(trm_max_num_setbacks), 111$
MSK_RES_TRM_MAX_TIME (trm_ max_ time), 111
MSK_RES_TRM_MIO_NEAR_ABS_GAP
(trm mio near abs gap), 111
MSK_RES_TRM_MIO_NEAR_REL_GAP
$(trm_mio_near_rel_gap), 111$
MSK_RES_TRM_MIO_NUM_BRANCHES
(trm_mio_num_branches), 111
MSK_RES_TRM_MIO_NUM_RELAXS
(trm_mio_num_relaxs), 111
MSK_RES_TRM_NUM_MAX_NUM_INT_SOLUTIONS
$(trm_num_max_num_int_solutions),$
111
MSK_RES_TRM_NUMERICAL_PROBLEM
(trm_numerical_problem), 111
MSK_RES_TRM_OBJECTIVE_RANGE
(trm_objective_range), 111
${\tt MSK_RES_TRM_STALL} \ (trm_stall), \ 111$
MSK_RES_TRM_USER_CALLBACK
$(trm_user_callback),\ 112$
MSK_RES_WRN_ANA_ALMOST_INT_BOUNDS
$(wrn_ana_almost_int_bounds), 129$
${\tt MSK_RES_WRN_ANA_C_ZERO} \qquad (wrn_ana_c_zero)$
129
MSK_RES_WRN_ANA_CLOSE_BOUNDS
$(wrn_ana_close_bounds), 129$
MSK_RES_WRN_ANA_EMPTY_COLS
$(wrn \ ana \ empty \ cols), 129$
· — - · · //
MSK_RES_WRN_ANA_LARGE_BOUNDS
MSK_RES_WRN_ANA_LARGE_BOUNDS
, — — - /
MSK_RES_WRN_ANA_LARGE_BOUNDS $(wrn_ana_large_bounds), 129$ MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG
MSK_RES_WRN_ANA_LARGE_BOUNDS (wrn_ana_large_bounds), 129
MSK_RES_WRN_ANA_LARGE_BOUNDS (wrn_ana_large_bounds), 129 MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG (wrn_construct_invalid_sol_itg), 129 MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG
MSK_RES_WRN_ANA_LARGE_BOUNDS (wrn_ana_large_bounds), 129 MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG (wrn_construct_invalid_sol_itg), 129 MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG (wrn_construct_no_sol_itg), 129
$\begin{tabular}{lllll} MSK_RES_WRN_ANA_LARGE_BOUNDS & $(wrn_ana_large_bounds)$, 129 \\ MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG & $(wrn_construct_invalid_sol_itg)$, 129 \\ MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG & $(wrn_construct_no_sol_itg)$, 129 \\ MSK_RES_WRN_CONSTRUCT_SOLUTION_INFEAS \end{tabular}$
MSK_RES_WRN_ANA_LARGE_BOUNDS (wrn_ana_large_bounds), 129 MSK_RES_WRN_CONSTRUCT_INVALID_SOL_ITG (wrn_construct_invalid_sol_itg), 129 MSK_RES_WRN_CONSTRUCT_NO_SOL_ITG (wrn_construct_no_sol_itg), 129

MSK_RES_WRN_DUPLICATE_BARVARIABLE_NAMES	MSK_RES_WRN_OPEN_PARAM_FILE
$(wrn_duplicate_barvariable_names),$	$(wrn_open_param_file), 131$
129	MSK_RES_WRN_PARAM_IGNORED_CMIO
MSK_RES_WRN_DUPLICATE_CONE_NAMES	(wrn_param_ignored_cmio), 131
(wrn_duplicate_cone_names), 129 MSK_RES_WRN_DUPLICATE_CONSTRAINT_NAMES	MSK_RES_WRN_PARAM_NAME_DOU
(wrn_duplicate_constraint_names), 129	(wrn_param_name_dou), 131 MSK_RES_WRN_PARAM_NAME_INT
MSK_RES_WRN_DUPLICATE_VARIABLE_NAMES	(wrn_param_name_int), 131
(wrn_duplicate_variable_names), 129	MSK_RES_WRN_PARAM_NAME_STR
MSK_RES_WRN_ELIMINATOR_SPACE	$(wrn_param_name_str), 131$
$(wrn_eliminator_space), 129$	MSK_RES_WRN_PARAM_STR_VALUE
${\tt MSK_RES_WRN_EMPTY_NAME} \qquad (wrn_empty_name),$	$(wrn_param_str_value), 131$
130	MSK_RES_WRN_PRESOLVE_OUTOFSPACE
MSK_RES_WRN_IGNORE_INTEGER	(wrn_presolve_outofspace), 131 MSK_RES_WRN_QUAD_CONES_WITH_ROOT_FIXED_AT_ZERO
$(wrn_ignore_integer), 130 \\ \texttt{MSK_RES_WRN_INCOMPLETE_LINEAR_DEPENDENCY_CHINEAR}$	
(wrn_incomplete_linear_dependency_chee	, /
130	MSK_RES_WRN_RQUAD_CONES_WITH_ROOT_FIXED_AT_ZERO
MSK_RES_WRN_LARGE_AIJ (wrn_large_aij), 130	$(wrn_rquad_cones_with_root_fixed_at_zero)$
${\tt MSK_RES_WRN_LARGE_BOUND} \overline{(wrn_large_bound)},$	131
130	MSK_RES_WRN_SOL_FILE_IGNORED_CON
MSK_RES_WRN_LARGE_CJ (wrn_large_cj), 130	(wrn_sol_file_ignored_con), 131
MSK_RES_WRN_LARGE_CON_FX	MSK_RES_WRN_SOL_FILE_IGNORED_VAR
(wrn_large_con_fx), 130 MSK_RES_WRN_LARGE_LO_BOUND	(wrn_sol_file_ignored_var), 131 MSK_RES_WRN_SOL_FILTER (wrn_sol_filter), 131
(wrn_large_lo_bound), 130	MSK_RES_WRN_SPAR_MAX_LEN
MSK_RES_WRN_LARGE_UP_BOUND	$(wrn_spar_max_len), 131$
$(wrn_large_up_bound), 130$	MSK_RES_WRN_SYM_MAT_LARGE
MSK_RES_WRN_LICENSE_EXPIRE	$(wrn_sym_mat_large), 131$
(wrn_license_expire), 130	MSK_RES_WRN_TOO_FEW_BASIS_VARS
MSK_RES_WRN_LICENSE_FEATURE_EXPIRE	(wrn_too_few_basis_vars), 131
(wrn_license_feature_expire), 130 MSK_RES_WRN_LICENSE_SERVER	MSK_RES_WRN_TOO_MANY_BASIS_VARS
(wrn_license_server), 130	(wrn_too_many_basis_vars), 131 MSK_RES_WRN_UNDEF_SOL_FILE_NAME
MSK_RES_WRN_LP_DROP_VARIABLE	(wrn_undef_sol_file_name), 131
(wrn lp drop variable), 130	MSK_RES_WRN_USING_GENERIC_NAMES
MSK_RES_WRN_LP_OLD_QUAD_FORMAT	$(wrn_using_generic_names), 131$
$(wrn_lp_old_quad_format), 130$	MSK_RES_WRN_WRITE_CHANGED_NAMES
MSK_RES_WRN_MIO_INFEASIBLE_FINAL	(wrn_write_changed_names), 132
(wrn_mio_infeasible_final), 130	MSK_RES_WRN_WRITE_DISCARDED_CFIX
MSK_RES_WRN_MPS_SPLIT_BOU_VECTOR (wrn mps split bou vector), 130	(wrn_write_discarded_cfix), 132 MSK_RES_WRN_ZERO_AIJ (wrn zero aij), 132
MSK_RES_WRN_MPS_SPLIT_RAN_VECTOR	MSK_RES_WRN_ZEROS_IN_SPARSE_COL
(wrn_mps_split_ran_vector), 130	(wrn_zeros_in_sparse_col), 132
MSK_RES_WRN_MPS_SPLIT_RHS_VECTOR	MSK_RES_WRN_ZEROS_IN_SPARSE_ROW
$(wrn_mps_split_rhs_vector)$, 130	$(wrn_zeros_in_sparse_row), 132$
MSK_RES_WRN_NAME_MAX_LEN	MSK_RES_ERR_AD_INVALID_CODELIST
(wrn_name_max_len), 130	(err_ad_invalid_codelist), 112
MSK_RES_WRN_NO_DUALIZER (wrn_no_dualizer), 130	MSK_RES_ERR_API_ARRAY_TOO_SMALL
MSK_RES_WRN_NO_GLOBAL_OPTIMIZER	(err_api_array_too_small), 112 MSK_RES_ERR_API_CB_CONNECT
(wrn_no_global_optimizer), 130	(err_api_cb_connect), 112
MSK_RES_WRN_NO_NONLINEAR_FUNCTION_WRITE	MSK_RES_ERR_API_FATAL_ERROR
$(wrn_no_nonlinear_function_write),$	$(err_api_fatal_error), 112$
131	${\tt MSK_RES_ERR_API_INTERNAL} (err_api_internal),$
MSK_RES_WRN_NZ_IN_UPR_TRI	112
$(wrn_nz_in_upr_tri)$, 131	MSK_RES_ERR_ARG_IS_TOO_LARGE
	$(err_arg_is_too_large), 112$

MSK_RES_ERR_ARG_IS_TOO_SMALL	MSK_RES_ERR_CBF_TOO_FEW_INTS
(err_arg_is_too_small), 112	(err_cbf_too_few_ints), 113
MSK_RES_ERR_ARGUMENT_DIMENSION	MSK_RES_ERR_CBF_TOO_FEW_VARIABLES
(err_argument_dimension), 112 MSK_RES_ERR_ARGUMENT_IS_TOO_LARGE	(err_cbf_too_few_variables), 113 MSK_RES_ERR_CBF_TOO_MANY_CONSTRAINTS
(err_argument_is_too_large), 112	(err_cbf_too_many_constraints), 113
MSK_RES_ERR_ARGUMENT_LENNEQ	MSK_RES_ERR_CBF_TOO_MANY_INTS
(err argument lenneq), 112	$(err_cbf_too_many_ints), 113$
MSK_RES_ERR_ARGUMENT_PERM_ARRAY	MSK_RES_ERR_CBF_TOO_MANY_VARIABLES
$(err_argument_perm_array),\ 112$	$(err_cbf_too_many_variables), 113$
MSK_RES_ERR_ARGUMENT_TYPE	MSK_RES_ERR_CBF_UNSUPPORTED
(err_argument_type), 112	$(err_cbf_unsupported), 113$
MSK_RES_ERR_BAR_VAR_DIM (err_bar_var_dim),	MSK_RES_ERR_CON_Q_NOT_NSD
MOV DEG EDD DAGTO (h) 110	(err_con_q_not_nsd), 113
MSK_RES_ERR_BASIS (err_basis), 112 MSK_RES_ERR_BASIS_FACTOR (err_basis_factor),	MSK_RES_ERR_CON_Q_NOT_PSD $(err_con_q_not_psd), 114$
112	MSK_RES_ERR_CONE_INDEX (err cone index), 114
MSK_RES_ERR_BASIS_SINGULAR	MSK_RES_ERR_CONE_OVERLAP (err_cone_overlap),
(err_basis_singular), 112	114
MSK_RES_ERR_BLANK_NAME (err_blank_name), 112	MSK_RES_ERR_CONE_OVERLAP_APPEND
MSK_RES_ERR_CANNOT_CLONE_NL	$(err_cone_overlap_append),114$
$(err_cannot_clone_nl),112$	MSK_RES_ERR_CONE_REP_VAR
MSK_RES_ERR_CANNOT_HANDLE_NL	$(err_cone_rep_var), 114$
$(err_cannot_handle_nl), 112$	MSK_RES_ERR_CONE_SIZE (err_cone_size), 114
MSK_RES_ERR_CBF_DUPLICATE_ACOORD	MSK_RES_ERR_CONE_TYPE (err_cone_type), 114
(err_cbf_duplicate_acoord), 112 MSK_RES_ERR_CBF_DUPLICATE_BCOORD	MSK_RES_ERR_CONE_TYPE_STR
(err cbf duplicate bcoord), 113	(err_cone_type_str), 114 MSK_RES_ERR_DATA_FILE_EXT
MSK_RES_ERR_CBF_DUPLICATE_CON	(err data file ext), 114
$(err_cbf_duplicate_con), 113$	MSK_RES_ERR_DUP_NAME (err_dup_name), 114
MSK_RES_ERR_CBF_DUPLICATE_INT	MSK_RES_ERR_DUPLICATE_AIJ
$(err_cbf_duplicate_int), 113$	$(err_duplicate_aij),114$
MSK_RES_ERR_CBF_DUPLICATE_OBJ	MSK_RES_ERR_DUPLICATE_BARVARIABLE_NAMES
(err_cbf_duplicate_obj), 113	(err_duplicate_barvariable_names), 114
MSK_RES_ERR_CBF_DUPLICATE_OBJACOORD	MSK_RES_ERR_DUPLICATE_CONE_NAMES
(err_cbf_duplicate_objacoord), 113 MSK_RES_ERR_CBF_DUPLICATE_VAR	(err_duplicate_cone_names), 114 MSK_RES_ERR_DUPLICATE_CONSTRAINT_NAMES
(err cbf duplicate var), 113	(err duplicate constraint names), 114
MSK_RES_ERR_CBF_INVALID_CON_TYPE	MSK_RES_ERR_DUPLICATE_VARIABLE_NAMES
(err cbf invalid con type), 113	(err_duplicate_variable_names), 114
MSK_RES_ERR_CBF_INVALID_DOMAIN_DIMENSION	MSK_RES_ERR_END_OF_FILE (err_end_of_file),
$(err_cbf_invalid_domain_dimension),$	114
113	MSK_RES_ERR_FACTOR (err_factor), 114
MSK_RES_ERR_CBF_INVALID_INT_INDEX	MSK_RES_ERR_FEASREPAIR_CANNOT_RELAX
(err_cbf_invalid_int_index), 113	(err_feasrepair_cannot_relax), 114
MSK_RES_ERR_CBF_INVALID_VAR_TYPE	MSK_RES_ERR_FEASREPAIR_INCONSISTENT_BOUND (err_feasrepair_inconsistent_bound),
(err_cbf_invalid_var_type), 113 MSK_RES_ERR_CBF_NO_VARIABLES	(err_jeasrepair_inconsisieni_oouna), 114
(err cbf no variables), 113	MSK_RES_ERR_FEASREPAIR_SOLVING_RELAXED
MSK_RES_ERR_CBF_NO_VERSION_SPECIFIED	(err feasrepair solving relaxed), 115
(err_cbf_no_version_specified), 113	MSK_RES_ERR_FILE_LICENSE (err_file_license)
MSK_RES_ERR_CBF_OBJ_SENSE	115
$(err_cbf_obj_sense), 113$	MSK_RES_ERR_FILE_OPEN (err_file_open), 115
MSK_RES_ERR_CBF_PARSE (err_cbf_parse), 113	MSK_RES_ERR_FILE_READ (err_file_read), 115
MSK_RES_ERR_CBF_SYNTAX (err_cbf_syntax), 113	MSK_RES_ERR_FILE_WRITE (err_file_write), 115
MSK_RES_ERR_CBF_TOO_FEW_CONSTRAINTS	MSK_RES_ERR_FIRST (err_first), 115
$(err_cbf_too_few_constraints), 113$	MSK_RES_ERR_FIRSTI (err_firsti), 115 MSK_RES_ERR_FIRSTI (err_firsti) 115

MSK_RES_ERR_FIXED_BOUND_VALUES	${\tt MSK_RES_ERR_INV_PROBLEM} \qquad (err_inv_problem),$
$(err_fixed_bound_values), 115$	116
MSK_RES_ERR_FLEXLM (err_flexlm), 115	MSK_RES_ERR_INV_QCON_SUBI
MSK_RES_ERR_GLOBAL_INV_CONIC_PROBLEM	$(err_inv_qcon_subi), 117$
$(err_global_inv_conic_problem), 115$	MSK_RES_ERR_INV_QCON_SUBJ
MSK_RES_ERR_HUGE_AIJ (err huge aij), 115	$(err_inv_qcon_subj), 117$
MSK_RES_ERR_HUGE_C (err_huge_c), 115	MSK_RES_ERR_INV_QCON_SUBK
MSK_RES_ERR_IDENTICAL_TASKS	$(err_inv_qcon_subk), 117$
$(err_identical_tasks), 115$	MSK_RES_ERR_INV_QCON_VAL (err_inv_qcon_val),
MSK_RES_ERR_IN_ARGUMENT (err in argument),	117
115	MSK_RES_ERR_INV_QOBJ_SUBI
MSK_RES_ERR_INDEX (err_index), 115	$(err_inv_qobj_subi), 117$
MSK_RES_ERR_INDEX_ARR_IS_TOO_LARGE	MSK_RES_ERR_INV_QOBJ_SUBJ
$(err_index_arr_is_too_large), 115$	$(err_inv_qobj_subj), 117$
MSK_RES_ERR_INDEX_ARR_IS_TOO_SMALL	MSK_RES_ERR_INV_QOBJ_VAL (err_inv_qobj_val),
$(err_index_arr_is_too_small), 115$	117
MSK_RES_ERR_INDEX_IS_TOO_LARGE	MSK_RES_ERR_INV_SK (err inv sk), 117
(err_index_is_too_large), 115	MSK_RES_ERR_INV_SK_STR (err_inv_sk_str), 117
MSK_RES_ERR_INDEX_IS_TOO_SMALL	MSK_RES_ERR_INV_SKC (err_inv_skc), 117
$(err_index_is_too_small), 115$	MSK_RES_ERR_INV_SKN (err_inv_skn), 117
MSK_RES_ERR_INF_DOU_INDEX	MSK_RES_ERR_INV_SKX (err_inv_skx), 117
(err inf dou index), 115	MSK_RES_ERR_INV_VAR_TYPE (err_inv_var_type),
MSK_RES_ERR_INF_DOU_NAME	117
(err inf dou name), 115	MSK_RES_ERR_INVALID_ACCMODE
MSK_RES_ERR_INF_INT_INDEX	(err_invalid_accmode), 117
$(err_inf_int_index), 116$	MSK_RES_ERR_INVALID_AIJ (err_invalid_aij), 117
MSK_RES_ERR_INF_INT_NAME	MSK_RES_ERR_INVALID_AMPL_STUB
(err_inf_int_name), 116	(err_invalid_ampl_stub), 117
MSK_RES_ERR_INF_LINT_INDEX	MSK_RES_ERR_INVALID_BARVAR_NAME
(err_inf_lint_index), 116	(err_invalid_barvar_name), 117
MSK_RES_ERR_INF_LINT_NAME	MSK_RES_ERR_INVALID_COMPRESSION
(err_inf_lint_name), 116	(err_invalid_compression), 117
MSK_RES_ERR_INF_TYPE (err_inf_type), 116	MSK_RES_ERR_INVALID_CON_NAME
MSK_RES_ERR_INFEAS_UNDEFINED	(err invalid con name), 117
(err_infeas_undefined), 116	MSK_RES_ERR_INVALID_CONE_NAME
MSK_RES_ERR_INFINITE_BOUND	(err invalid cone name), 117
(err_infinite_bound), 116	MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_CONES
MSK_RES_ERR_INT64_TO_INT32_CAST	(err_invalid_file_format_for_cones),
(err int64 to int32 cast), 116	117
MSK_RES_ERR_INTERNAL (err internal), 116	MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_GENERAL_NI
MSK_RES_ERR_INTERNAL_TEST_FAILED	(err_invalid_file_format_for_general_nl),
(err_internal_test_failed), 116	117
MSK_RES_ERR_INV_APTRE (err inv aptre), 116	MSK_RES_ERR_INVALID_FILE_FORMAT_FOR_SYM_MAT
MSK_RES_ERR_INV_BK (err inv bk), 116	$(err_invalid_file_format_for_sym_mat),$
MSK_RES_ERR_INV_BKC (err inv bkc), 116	117
MSK_RES_ERR_INV_BKX (err inv bkx), 116	MSK_RES_ERR_INVALID_FILE_NAME
MSK_RES_ERR_INV_CONE_TYPE	(err invalid file name), 118
(err_inv_cone_type), 116	MSK_RES_ERR_INVALID_FORMAT_TYPE
MSK_RES_ERR_INV_CONE_TYPE_STR	(err invalid format type), 118
(err_inv_cone_type_str), 116	MSK_RES_ERR_INVALID_IDX (err invalid idx),
MSK_RES_ERR_INV_MARKI (err inv marki), 116	118
MSK_RES_ERR_INV_MARKJ (err_inv_markj), 116	MSK_RES_ERR_INVALID_IOMODE
MSK_RES_ERR_INV_NAME_ITEM	(err invalid iomode), 118
(err_inv_name_item), 116	MSK_RES_ERR_INVALID_MAX_NUM
MSK_RES_ERR_INV_NUMI (err inv numi), 116	(err invalid max num), 118
MSK_RES_ERR_INV_NUMJ (err_inv_numj), 116	MSK_RES_ERR_INVALID_NAME_IN_SOL_FILE
MSK_RES_ERR_INV_OPTIMIZER	(err invalid name in sol file), 118
(err inv optimizer), 116	(611_010000000_1001100_010_3000_1000/, 110
(CII_ 1110_ OptimizeI), 110	

MSK_RES_ERR_INVALID_OBJ_NAME	MSK_RES_ERR_LAU_SINGULAR_MATRIX
(err_invalid_obj_name), 118	(err_lau_singular_matrix), 119
MSK_RES_ERR_INVALID_OBJECTIVE_SENSE	${\tt MSK_RES_ERR_LAU_UNKNOWN} (err_lau_unknown),$
(err_invalid_objective_sense), 118	119
MSK_RES_ERR_INVALID_PROBLEM_TYPE (err invalid problem type), 118	MSK_RES_ERR_LICENSE (err_license), 119 MSK_RES_ERR_LICENSE_CANNOT_ALLOCATE
MSK_RES_ERR_INVALID_SOL_FILE_NAME	(err_license_cannot_allocate), 119
(err_invalid_sol_file_name), 118	MSK_RES_ERR_LICENSE_CANNOT_CONNECT
MSK_RES_ERR_INVALID_STREAM	$(err_license_cannot_connect), 119$
(err_invalid_stream), 118	MSK_RES_ERR_LICENSE_EXPIRED
MSK_RES_ERR_INVALID_SURPLUS (err_invalid_surplus), 118	(err_license_expired), 119 MSK_RES_ERR_LICENSE_FEATURE
MSK_RES_ERR_INVALID_SYM_MAT_DIM	(err_license_feature), 119
$(err_invalid_sym_mat_dim),\ 118$	MSK_RES_ERR_LICENSE_INVALID_HOSTID
${\tt MSK_RES_ERR_INVALID_TASK} (err_invalid_task),$	(err_license_invalid_hostid), 119
118	MSK_RES_ERR_LICENSE_MAX (err_license_max),
MSK_RES_ERR_INVALID_UTF8 (err_invalid_utf8), 118	120 MSK_RES_ERR_LICENSE_MOSEKLM_DAEMON
MSK_RES_ERR_INVALID_VAR_NAME	(err license moseklm daemon), 120
$(err_invalid_var_name), 118$	MSK_RES_ERR_LICENSE_NO_SERVER_LINE
MSK_RES_ERR_INVALID_WCHAR	(err_license_no_server_line), 120
(err_invalid_wchar), 118 MSK_RES_ERR_INVALID_WHICHSOL	MSK_RES_ERR_LICENSE_NO_SERVER_SUPPORT (err_license_no_server_support), 120
(err_invalid_whichsol), 118	MSK_RES_ERR_LICENSE_SERVER
MSK_RES_ERR_JSON_DATA (err_json_data), 118	(err_license_server), 120
${\tt MSK_RES_ERR_JSON_FORMAT} \qquad (err_json_format),$	MSK_RES_ERR_LICENSE_SERVER_VERSION
118	(err_license_server_version), 120
MSK_RES_ERR_JSON_MISSING_DATA (err_json_missing_data), 118	MSK_RES_ERR_LICENSE_VERSION (err_license_version), 120
MSK_RES_ERR_JSON_NUMBER_OVERFLOW	MSK_RES_ERR_LINK_FILE_DLL (err_link_file_dll),
$(err_json_number_overflow),\ 118$	120
MSK_RES_ERR_JSON_STRING (err_json_string), 118	MSK_RES_ERR_LIVING_TASKS (err_living_tasks),
	MSK_RES_ERR_LOWER_BOUND_IS_A_NAN
119	$(err_lower_bound_is_a_nan), 120$
MSK_RES_ERR_LAST (err_last), 119	MSK_RES_ERR_LP_DUP_SLACK_NAME
MSK_RES_ERR_LASTI (err_lasti), 119	(err_lp_dup_slack_name), 120
MSK_RES_ERR_LASTJ (err_lastj), 119 MSK_RES_ERR_LAU_ARG_K (err_lau_arg_k), 119	MSK_RES_ERR_LP_EMPTY (err_lp_empty), 120 MSK_RES_ERR_LP_FILE_FORMAT
MSK_RES_ERR_LAU_ARG_M (err_lau_arg_m), 119	(err_lp_file_format), 120
MSK_RES_ERR_LAU_ARG_N (err_lau_arg_n), 119	${\tt MSK_RES_ERR_LP_FORMAT} \ (err_lp_format), \ 120$
MSK_RES_ERR_LAU_ARG_TRANS	MSK_RES_ERR_LP_FREE_CONSTRAINT
(err_lau_arg_trans), 119 MSK_RES_ERR_LAU_ARG_TRANSA	(err_lp_free_constraint), 120 MSK_RES_ERR_LP_INCOMPATIBLE
$(err_lau_arg_transa)$, 119	(err lp incompatible), 120
MSK_RES_ERR_LAU_ARG_TRANSB	MSK_RES_ERR_LP_INVALID_CON_NAME
$(err_lau_arg_transb)$, 119	$(err_lp_invalid_con_name), 120$
MSK_RES_ERR_LAU_ARG_UPLO (err_lau_arg_uplo),	MSK_RES_ERR_LP_INVALID_VAR_NAME
119 MSK_RES_ERR_LAU_INVALID_LOWER_TRIANGULAR_MA	(err_lp_invalid_var_name), 120 TMSX RES ERR LP WRITE CONIC PROBLEM
$(err_lau_invalid_lower_triangular_matr$	
119	MSK_RES_ERR_LP_WRITE_GECO_PROBLEM
MSK_RES_ERR_LAU_INVALID_SPARSE_SYMMETRIC_MA	· /:
$(err_lau_invalid_sparse_symmetric_max)$ 119	
MSK_RES_ERR_LAU_NOT_POSITIVE_DEFINITE	(err_lu_max_num_tries), 121 MSK_RES_ERR_MAX_LEN_IS_TOO_SMALL
(err_lau_not_positive_definite), 119	$(err_max_len_is_too_small), 121$

MSK_RES_ERR_MAXNUMBARVAR	MSK_RES_ERR_MPS_NULL_CON_NAME
$(err_maxnumbarvar), 121$	$(err_mps_null_con_name),\ 122$
MSK_RES_ERR_MAXNUMCON (err_maxnumcon), 121	MSK_RES_ERR_MPS_NULL_VAR_NAME
$MSK_RES_ERR_MAXNUMCONE$ (err_maxnumcone),	$(err_mps_null_var_name),\ 122$
121	MSK_RES_ERR_MPS_SPLITTED_VAR
MSK_RES_ERR_MAXNUMQNZ (err_maxnumqnz), 121	$(err_mps_splitted_var), 122$
MSK_RES_ERR_MAXNUMVAR (err_ maxnumvar), 121	MSK_RES_ERR_MPS_TAB_IN_FIELD2
MSK_RES_ERR_MIO_INTERNAL (err_mio_internal),	$(err_mps_tab_in_field2), 122$
121	MSK_RES_ERR_MPS_TAB_IN_FIELD3
MSK_RES_ERR_MIO_INVALID_NODE_OPTIMIZER	(err_mps_tab_in_field3), 122
(err_mio_invalid_node_optimizer), 121	MSK_RES_ERR_MPS_TAB_IN_FIELD5
MSK_RES_ERR_MIO_INVALID_ROOT_OPTIMIZER	(err_mps_tab_in_field5), 122
(err_mio_invalid_root_optimizer), 121	MSK_RES_ERR_MPS_UNDEF_CON_NAME
MSK_RES_ERR_MIO_NO_OPTIMIZER	
	(err_mps_undef_con_name), 122
(err_mio_no_optimizer), 121	MSK_RES_ERR_MPS_UNDEF_VAR_NAME
MSK_RES_ERR_MIO_NOT_LOADED	(err_mps_undef_var_name), 122
(err_mio_not_loaded), 121	MSK_RES_ERR_MUL_A_ELEMENT
MSK_RES_ERR_MISSING_LICENSE_FILE	$(err_mul_a_element), 122$
$(err_missing_license_file),\ 121$	MSK_RES_ERR_NAME_IS_NULL
MSK_RES_ERR_MIXED_CONIC_AND_NL	$(err_name_is_null),\ 122$
$(err_mixed_conic_and_nl),\ 121$	MSK_RES_ERR_NAME_MAX_LEN
MSK_RES_ERR_MPS_CONE_OVERLAP	$(err_name_max_len),\ 122$
$(err_mps_cone_overlap), 121$	MSK_RES_ERR_NAN_IN_BLC (err_nan_in_blc), 123
MSK_RES_ERR_MPS_CONE_REPEAT	MSK_RES_ERR_NAN_IN_BLX (err nan in blx), 123
$(err_mps_cone_repeat), 121$	MSK_RES_ERR_NAN_IN_BUC (err_nan_in_buc)
MSK_RES_ERR_MPS_CONE_TYPE	123
(err_mps_cone_type), 121	MSK_RES_ERR_NAN_IN_BUX (err_nan_in_bux)
MSK_RES_ERR_MPS_DUPLICATE_Q_ELEMENT	123
(err_mps_duplicate_q_element), 121	MSK_RES_ERR_NAN_IN_C (err_nan_in_c), 123
MSK_RES_ERR_MPS_FILE (err_ mps_file), 121	MSK_RES_ERR_NAN_IN_DOUBLE_DATA
MSK_RES_ERR_MPS_INV_BOUND_KEY	(err_nan_in_double_data), 123
(err_mps_inv_bound_key), 121	MSK_RES_ERR_NEGATIVE_APPEND
MSK_RES_ERR_MPS_INV_CON_KEY	(err_negative_append), 123
$(err_mps_inv_con_key), 122$	MSK_RES_ERR_NEGATIVE_SURPLUS
MSK_RES_ERR_MPS_INV_FIELD	$(err_negative_surplus), 123$
$(err_mps_inv_field),\ 122$	MSK_RES_ERR_NEWER_DLL (err_newer_dll), 123
MSK_RES_ERR_MPS_INV_MARKER	MSK_RES_ERR_NO_BARS_FOR_SOLUTION
$(err_mps_inv_marker), 122$	$(err_no_bars_for_solution), 123$
MSK_RES_ERR_MPS_INV_SEC_NAME	MSK_RES_ERR_NO_BARX_FOR_SOLUTION
$(err_mps_inv_sec_name), 122$	(err no barx for solution), 123
MSK_RES_ERR_MPS_INV_SEC_ORDER	MSK_RES_ERR_NO_BASIS_SOL (err no basis sol).
(err mps inv sec order), 122	123
MSK_RES_ERR_MPS_INVALID_OBJ_NAME	MSK_RES_ERR_NO_DUAL_FOR_ITG_SOL
(err mps invalid obj name), 122	(err no dual for itg sol), 123
MSK_RES_ERR_MPS_INVALID_OBJSENSE	MSK_RES_ERR_NO_DUAL_INFEAS_CER
(err mps invalid objsense), 122	(err no dual infeas cer), 123
MSK_RES_ERR_MPS_MUL_CON_NAME	MSK_RES_ERR_NO_INIT_ENV (err no init env),
(err mps mul con name), 122	123
MSK_RES_ERR_MPS_MUL_CSEC	MSK_RES_ERR_NO_OPTIMIZER_VAR_TYPE
(err_mps_mul_csec), 122	(err_no_optimizer_var_type), 123
MSK_RES_ERR_MPS_MUL_QOBJ	MSK_RES_ERR_NO_PRIMAL_INFEAS_CER
(err_mps_mul_qobj), 122	(err_no_primal_infeas_cer), 123
MSK_RES_ERR_MPS_MUL_QSEC	MSK_RES_ERR_NO_SNX_FOR_BAS_SOL
$(err_mps_mul_qsec), 122$	$(err_no_snx_for_bas_sol), 123$
MSK_RES_ERR_MPS_NO_OBJECTIVE	MSK_RES_ERR_NO_SOLUTION_IN_CALLBACK
$(err_mps_no_objective), 122$	$(err_no_solution_in_callback), 123$
MSK_RES_ERR_MPS_NON_SYMMETRIC_Q	MSK_RES_ERR_NON_UNIQUE_ARRAY
(orr mns non summetric a) 199	(err non unique array) 193

MSK_RES_ERR_NONCONVEX (err_nonconvex), 123	MSK_RES_ERR_QCON_SUBI_TOO_SMALL
MSK_RES_ERR_NONLINEAR_EQUALITY	$(err_qcon_subi_too_small),\ 125$
(err_nonlinear_equality), 123	MSK_RES_ERR_QCON_UPPER_TRIANGLE
MSK_RES_ERR_NONLINEAR_FUNCTIONS_NOT_ALLOWED (err_nonlinear_functions_not_allowed),	(err_qcon_upper_triangle), 125 MSK_RES_ERR_QOBJ_UPPER_TRIANGLE
124	(err_qobj_upper_triangle), 125
MSK_RES_ERR_NONLINEAR_RANGED	MSK_RES_ERR_READ_FORMAT (err_read_format),
(err_nonlinear_ranged), 124	125
MSK_RES_ERR_NR_ARGUMENTS	MSK_RES_ERR_READ_LP_MISSING_END_TAG
$(err_nr_arguments), 124$	$(err_read_lp_missing_end_tag), 125$
MSK_RES_ERR_NULL_ENV (err_null_env), 124	MSK_RES_ERR_READ_LP_NONEXISTING_NAME
MSK_RES_ERR_NULL_POINTER (err_null_pointer),	$(err_read_lp_nonexisting_name),$ 125
MSK_RES_ERR_NULL_TASK (err_null_task), 124	MSK_RES_ERR_REMOVE_CONE_VARIABLE
MSK_RES_ERR_NUMCONLIM (err_numconlim), 124	(err_remove_cone_variable), 125
MSK_RES_ERR_NUMVARLIM (err_numvarlim), 124	MSK_RES_ERR_REPAIR_INVALID_PROBLEM
MSK_RES_ERR_OBJ_Q_NOT_NSD	$(err_repair_invalid_problem), 125$
$(err_obj_q_not_nsd),\ 124$	MSK_RES_ERR_REPAIR_OPTIMIZATION_FAILED
MSK_RES_ERR_OBJ_Q_NOT_PSD	(err_repair_optimization_failed), 125
(err_obj_q_not_psd), 124 MSK_RES_ERR_OBJECTIVE_RANGE	MSK_RES_ERR_SEN_BOUND_INVALID_LO
(err objective range), 124	(err_sen_bound_invalid_lo), 125 MSK_RES_ERR_SEN_BOUND_INVALID_UP
MSK_RES_ERR_OLDER_DLL (err older dll), 124	(err_sen_bound_invalid_up), 125
MSK_RES_ERR_OPEN_DL (err_open_dl), 124	MSK_RES_ERR_SEN_FORMAT (err_sen_format), 126
MSK_RES_ERR_OPF_FORMAT (err_opf_format), 124	MSK_RES_ERR_SEN_INDEX_INVALID
MSK_RES_ERR_OPF_NEW_VARIABLE	$(err_sen_index_invalid), 126$
(err_opf_new_variable), 124	MSK_RES_ERR_SEN_INDEX_RANGE
MSK_RES_ERR_OPF_PREMATURE_EOF	(err_sen_index_range), 126
(err_opf_premature_eof), 124 MSK_RES_ERR_OPTIMIZER_LICENSE	MSK_RES_ERR_SEN_INVALID_REGEXP (err_sen_invalid_regexp), 126
(err_optimizer_license), 124	MSK_RES_ERR_SEN_NUMERICAL
MSK_RES_ERR_OVERFLOW (err_overflow), 124	(err_sen_numerical), 126
${ t MSK_RES_ERR_PARAM_INDEX} \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \$	MSK_RES_ERR_SEN_SOLUTION_STATUS
124	$(err_sen_solution_status), 126$
MSK_RES_ERR_PARAM_IS_TOO_LARGE	MSK_RES_ERR_SEN_UNDEF_NAME
(err_param_is_too_large), 124 MSK_RES_ERR_PARAM_IS_TOO_SMALL	(err_sen_undef_name), 126 MSK_RES_ERR_SEN_UNHANDLED_PROBLEM_TYPE
(err_param_is_too_small), 124	(err_sen_unhandled_problem_type),
MSK_RES_ERR_PARAM_NAME (err param name),	126
125	MSK_RES_ERR_SERVER_CONNECT
MSK_RES_ERR_PARAM_NAME_DOU	$(err_server_connect), 126$
$(err_param_name_dou),\ 125$	MSK_RES_ERR_SERVER_PROTOCOL
MSK_RES_ERR_PARAM_NAME_INT	(err_server_protocol), 126
(err_param_name_int), 125 MSK_RES_ERR_PARAM_NAME_STR	MSK_RES_ERR_SERVER_STATUS
(err param name str), 125	(err_server_status), 126 MSK_RES_ERR_SERVER_TOKEN (err server token),
MSK_RES_ERR_PARAM_TYPE (err param type), 125	126
MSK_RES_ERR_PARAM_VALUE_STR	MSK_RES_ERR_SIZE_LICENSE (err size license),
$(err_param_value_str), 125$	126
MSK_RES_ERR_PLATFORM_NOT_LICENSED	MSK_RES_ERR_SIZE_LICENSE_CON
(err_platform_not_licensed), 125	(err_size_license_con), 126
MSK_RES_ERR_POSTSOLVE (err_postsolve), 125	MSK_RES_ERR_SIZE_LICENSE_INTVAR
MSK_RES_ERR_PRO_ITEM (err_pro_item), 125 MSK_RES_ERR_PROB_LICENSE (err_prob_license),	(err_size_license_intvar), 126 MSK_RES_ERR_SIZE_LICENSE_NUMCORES
125	(err size license numcores), 126
	MSK_RES_ERR_SIZE_LICENSE_VAR
(err qcon subi too large), 125	(err size license var), 126

MSK_RES_ERR_SOL_FILE_INVALID_NUMBER	MSK_RES_ERR_UNDEF_SOLUTION
$(err_sol_file_invalid_number), 126$	$(err_undef_solution), 128$
MSK_RES_ERR_SOLITEM (err_solitem), 126	MSK_RES_ERR_UNDEFINED_OBJECTIVE_SENSE
MSK_RES_ERR_SOLVER_PROBTYPE	$(err_undefined_objective_sense),\ 128$
$(err_solver_probtype), 126$	MSK_RES_ERR_UNHANDLED_SOLUTION_STATUS
$MSK_RES_ERR_SPACE\ (err_space),\ 126$	$(err_unhandled_solution_status), 128$
MSK_RES_ERR_SPACE_LEAKING	MSK_RES_ERR_UNKNOWN (err_unknown), 128
$(err_space_leaking), 126$	MSK_RES_ERR_UPPER_BOUND_IS_A_NAN
MSK_RES_ERR_SPACE_NO_INFO	$(err_upper_bound_is_a_nan),\ 128$
$(err_space_no_info),\ 127$	MSK_RES_ERR_UPPER_TRIANGLE
MSK_RES_ERR_SYM_MAT_DUPLICATE	$(err_upper_triangle), 128$
$(err_sym_mat_duplicate),\ 127$	MSK_RES_ERR_USER_FUNC_RET
MSK_RES_ERR_SYM_MAT_HUGE	$(err_user_func_ret)$, 128
$(err_sym_mat_huge),127$	MSK_RES_ERR_USER_FUNC_RET_DATA
MSK_RES_ERR_SYM_MAT_INVALID	$(err_user_func_ret_data), 128$
$(err_sym_mat_invalid),\ 127$	MSK_RES_ERR_USER_NLO_EVAL
MSK_RES_ERR_SYM_MAT_INVALID_COL_INDEX	$(err_user_nlo_eval), 128$
$(err_sym_mat_invalid_col_index),\ 127$	MSK_RES_ERR_USER_NLO_EVAL_HESSUBI
MSK_RES_ERR_SYM_MAT_INVALID_ROW_INDEX	$(err_user_nlo_eval_hessubi), 128$
$(err_sym_mat_invalid_row_index),$	MSK_RES_ERR_USER_NLO_EVAL_HESSUBJ
127	$(err_user_nlo_eval_hessubj), 128$
MSK_RES_ERR_SYM_MAT_INVALID_VALUE	MSK_RES_ERR_USER_NLO_FUNC
$(err_sym_mat_invalid_value),\ 127$	$(err_user_nlo_func), 128$
MSK_RES_ERR_SYM_MAT_NOT_LOWER_TRINGULAR	MSK_RES_ERR_WHICHITEM_NOT_ALLOWED
$(err_sym_mat_not_lower_tringular),$	$(err_whichitem_not_allowed),\ 128$
127	MSK_RES_ERR_WHICHSOL (err_whichsol), 128
MSK_RES_ERR_TASK_INCOMPATIBLE	MSK_RES_ERR_WRITE_LP_FORMAT
$(err_task_incompatible),\ 127$	$(err_write_lp_format), 128$
$MSK_RES_ERR_TASK_INVALID$ (err_task_invalid),	MSK_RES_ERR_WRITE_LP_NON_UNIQUE_NAME
127	$(err_write_lp_non_unique_name),$
$MSK_RES_ERR_TASK_WRITE\ (err_task_write),\ 127$	128
MSK_RES_ERR_THREAD_COND_INIT	MSK_RES_ERR_WRITE_MPS_INVALID_NAME
$(err_thread_cond_init), 127$	(err_write_mps_invalid_name), 129
MSK_RES_ERR_THREAD_CREATE	MSK_RES_ERR_WRITE_OPF_INVALID_VAR_NAME
(err_thread_create), 127	$(err_write_opf_invalid_var_name),$
MSK_RES_ERR_THREAD_MUTEX_INIT	129
(err_thread_mutex_init), 127	MSK_RES_ERR_WRITING_FILE (err_writing_file)
MSK_RES_ERR_THREAD_MUTEX_LOCK	129
(err_thread_mutex_lock), 127	MSK_RES_ERR_XML_INVALID_PROBLEM_TYPE
MSK_RES_ERR_THREAD_MUTEX_UNLOCK	(err_xml_invalid_problem_type), 129
(err_thread_mutex_unlock), 127	MSK_RES_ERR_Y_IS_UNDEFINED
MSK_RES_ERR_TOCONIC_CONSTR_NOT_CONIC (err toconic constr not conic), 127	$(err_y_is_undefined), 129$
MSK_RES_ERR_TOCONIC_CONSTR_Q_NOT_PSD	Structures
(err_toconic_constr_q_not_psd), 127	
MSK_RES_ERR_TOCONIC_CONSTRAINT_FX	Infeas_info, 62
$(err\ toconic\ constraint\ fx),\ 127$	Io_options, 62
MSK_RES_ERR_TOCONIC_CONSTRAINT_RA	Options, 61
(err_toconic_constraint_ra), 127	Problem, 60
MSK_RES_ERR_TOCONIC_OBJECTIVE_NOT_PSD	Result, 62
(err_toconic_objective_not_psd), 127	Solution_info, 61
MSK_RES_ERR_TOO_SMALL_MAX_NUM_NZ	Solver_solutions, 61
(err_too_small_max_num_nz), 128	Types
MSK_RES_ERR_TOO_SMALL_MAXNUMANZ	5.
(err_too_small_maxnumanz), 128	rescode, 60
MSK_RES_ERR_UNB_STEP_SIZE	
$(err_unb_step_size), 128$	
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