

Exploring the (Metric) Space of Jets with CMS Open Data

CERN EP/IT Data Science Seminar

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Center for Theoretical Physics

Massachusetts Institute of Technology

Joint work with Patrick Komiske, Radha Mastandrea, Preksha Naik, and Jesse Thaler

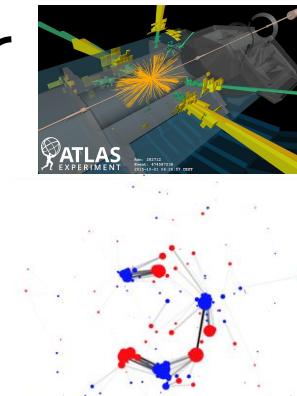
[\[1902.02346\]](#), to appear in PRL

[19xx.xxxxx]

June 19, 2019

Outline

Part I Introduction



When are two jets similar?

The Energy Mover's Distance

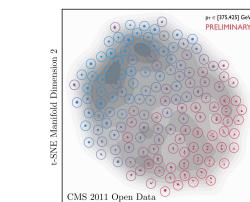


Movie Time

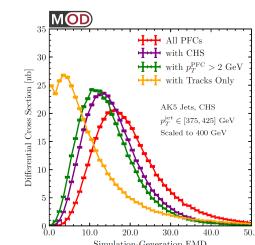
Part II Application



Jets in CMS Open Data



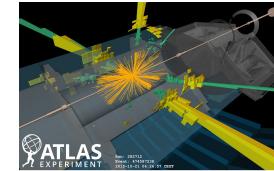
Exploring the Space of Jets



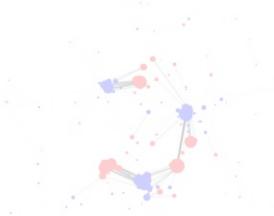
Quantifying Detector Effects

Outline

Part I Introduction



When are two jets similar?



The Energy Mover's Distance



Movie Time

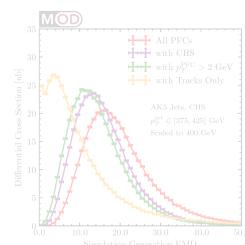
Part II Application



Jets in CMS Open Data

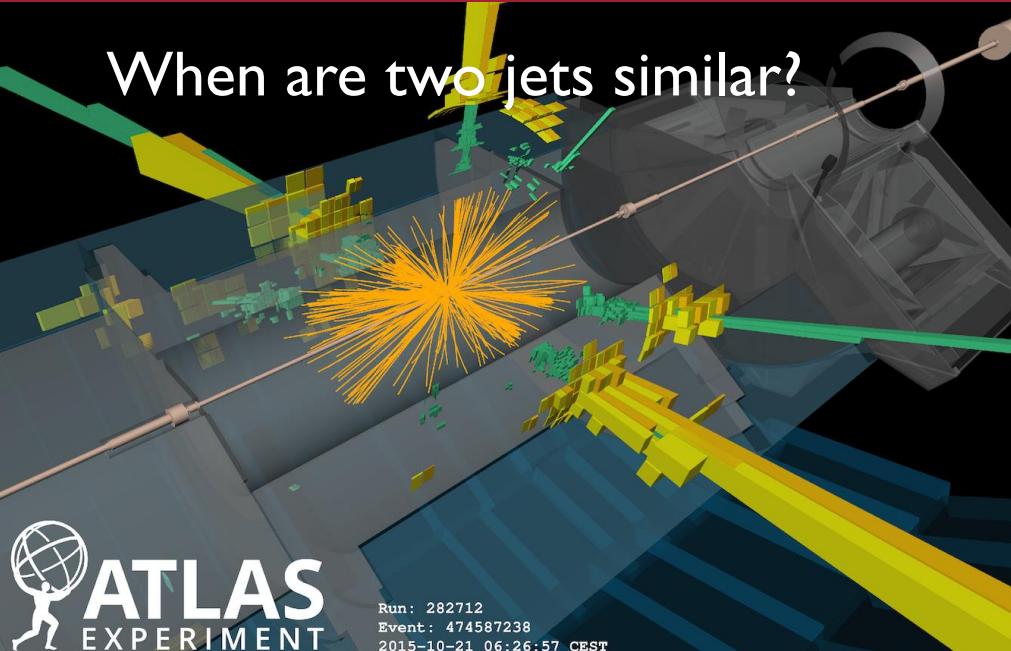


Exploring the Space of Jets



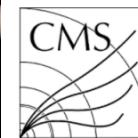
Quantifying Detector Effects

When are two jets similar?

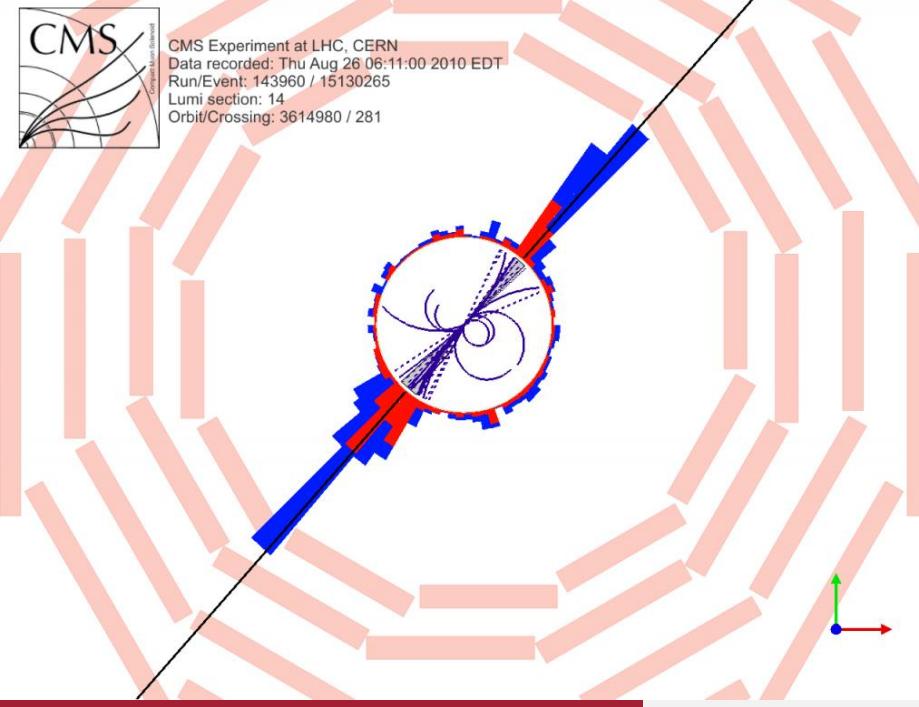
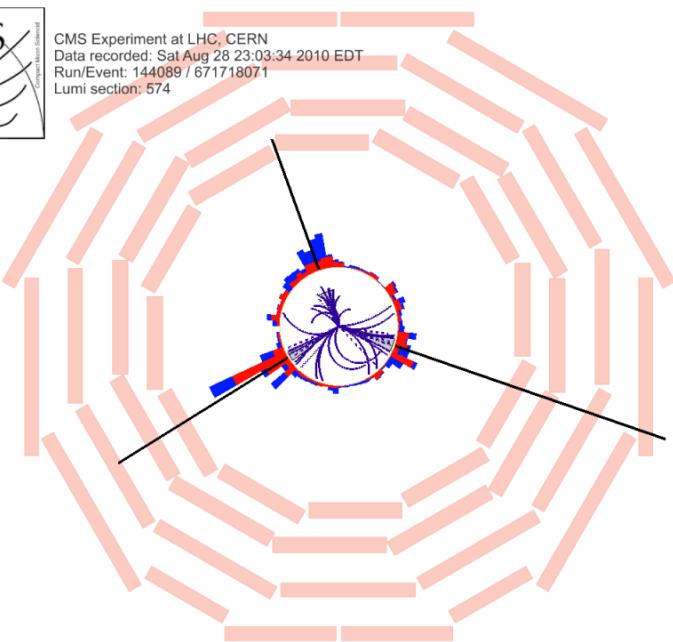


 **ATLAS**
EXPERIMENT

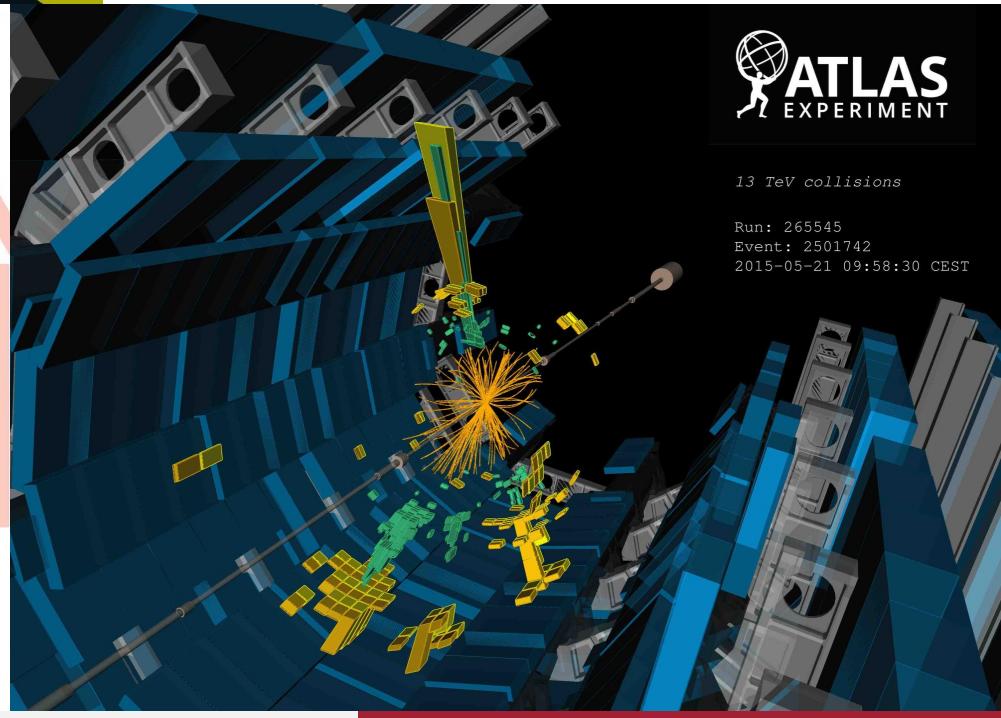
Run: 282712
Event: 474587238
2015-10-21 06:26:57 CEST



CMS Experiment at LHC, CERN
Data recorded: Sat Aug 28 23:03:34 2010 EDT
Run/Event: 144089 / 671718071
Lumi section: 574



 CMS
Experiment at LHC, CERN
Data recorded: Thu Aug 26 06:11:00 2010 EDT
Run/Event: 143960 / 15130265
Lumi section: 14
Orbit/Crossing: 3614980 / 281

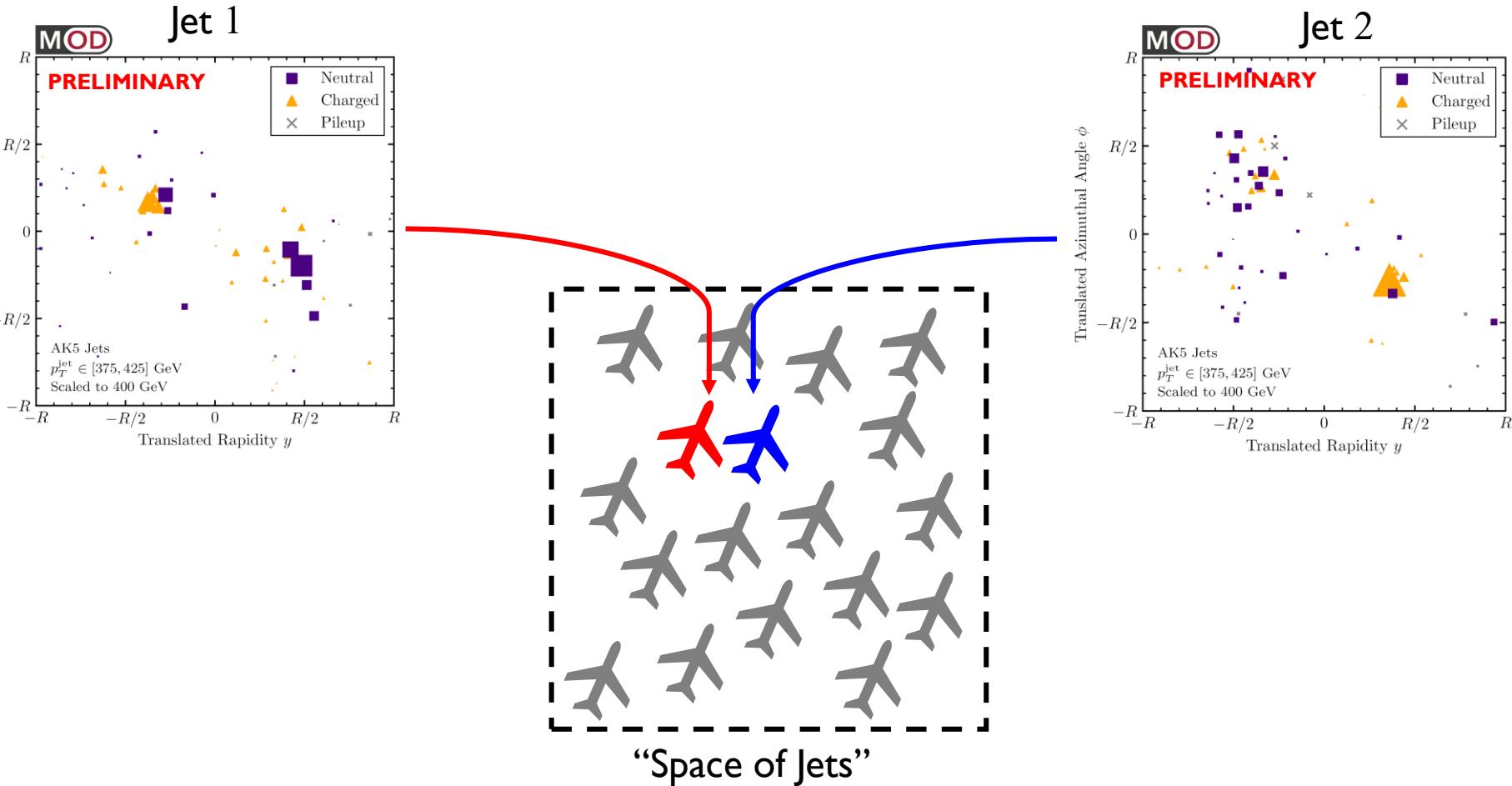


 **ATLAS**
EXPERIMENT

13 TeV collisions
Run: 265545
Event: 2501742
2015-05-21 09:58:30 CEST

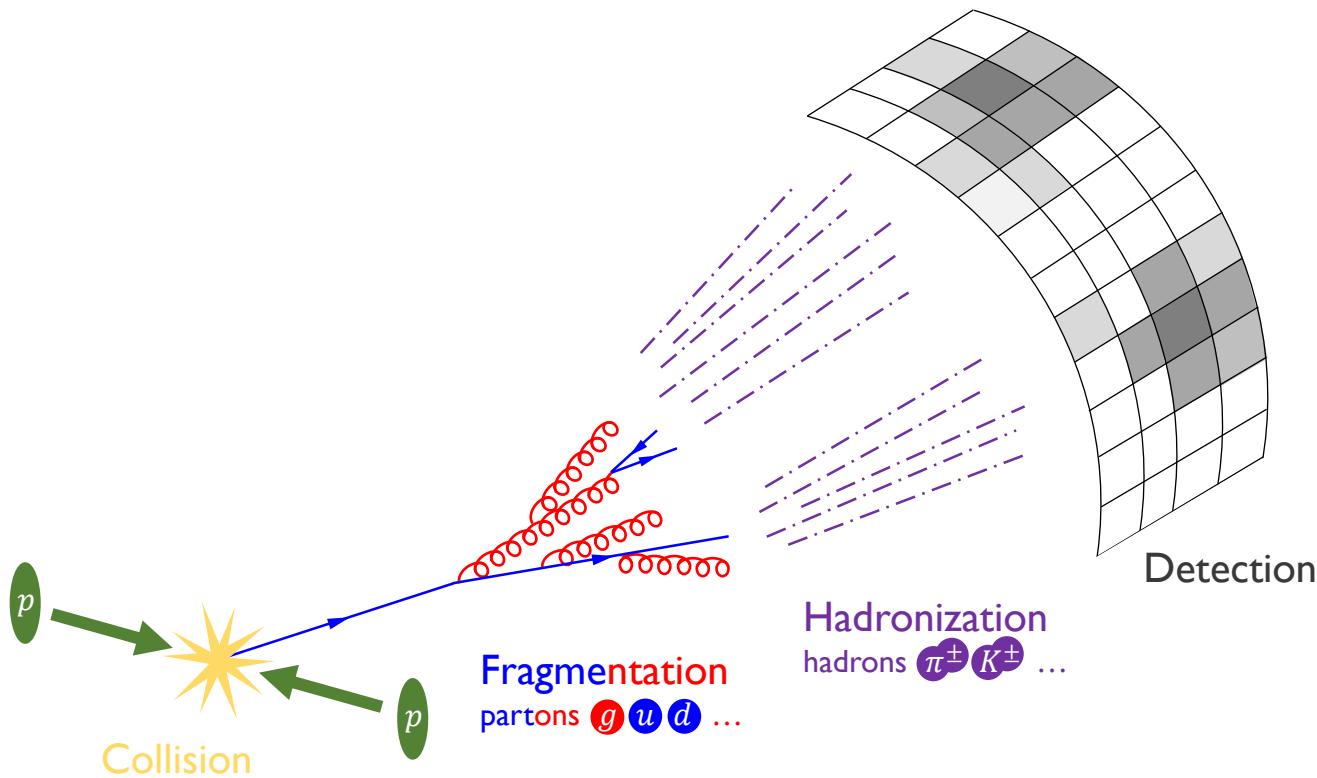
When are two jets similar?

These two jets “look” similar, but have different numbers of particles, flavors, and locations.
How do we quantify this?



When are two jets similar?

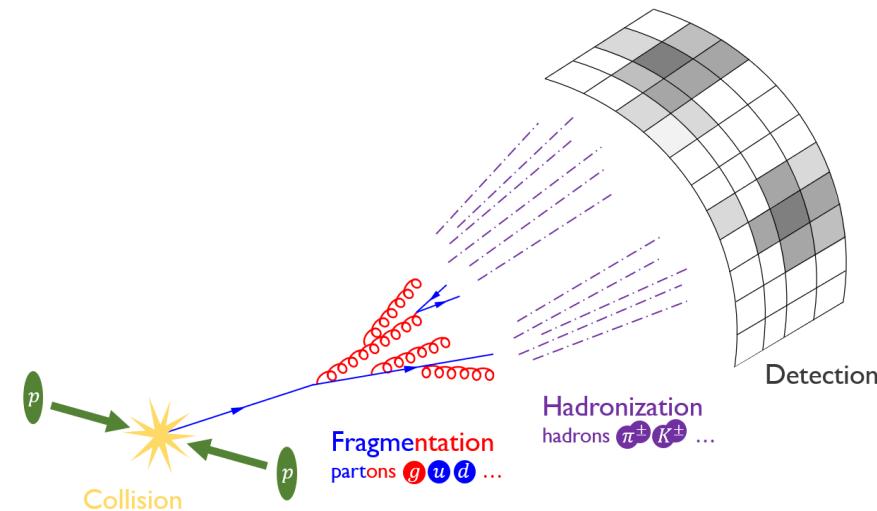
How a jet gets its shape



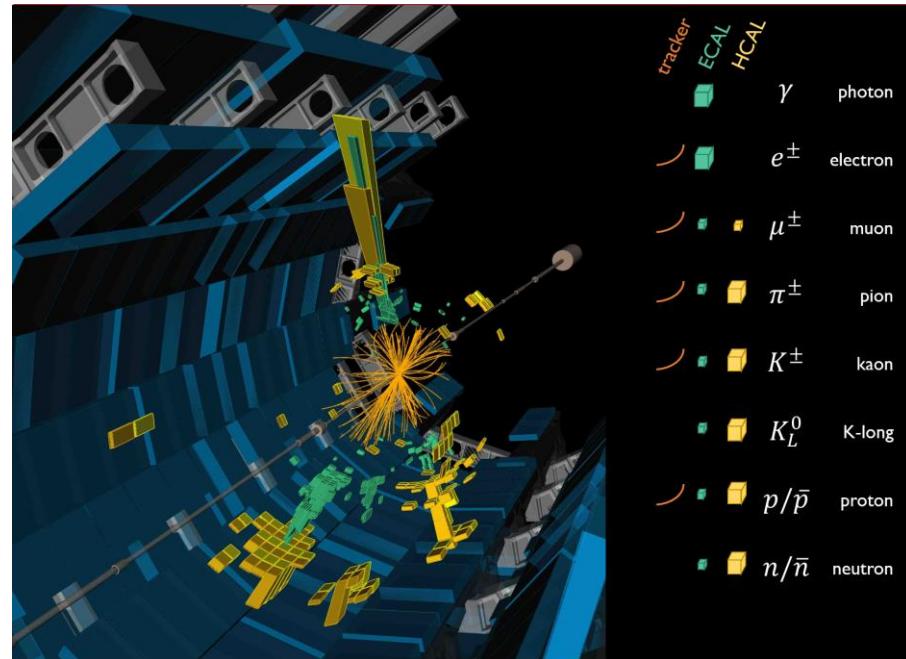
When are two jets similar?

A jet is...

Theoretically: very complicated



Experimentally: very complicated



However:

The energy flow (distribution of energy) is the information that is robust to:
fragmentation, hadronization, detector effects, ...

[\[N.A. Sveshnikov, F.V. Tkachov, 9512370\]](#)

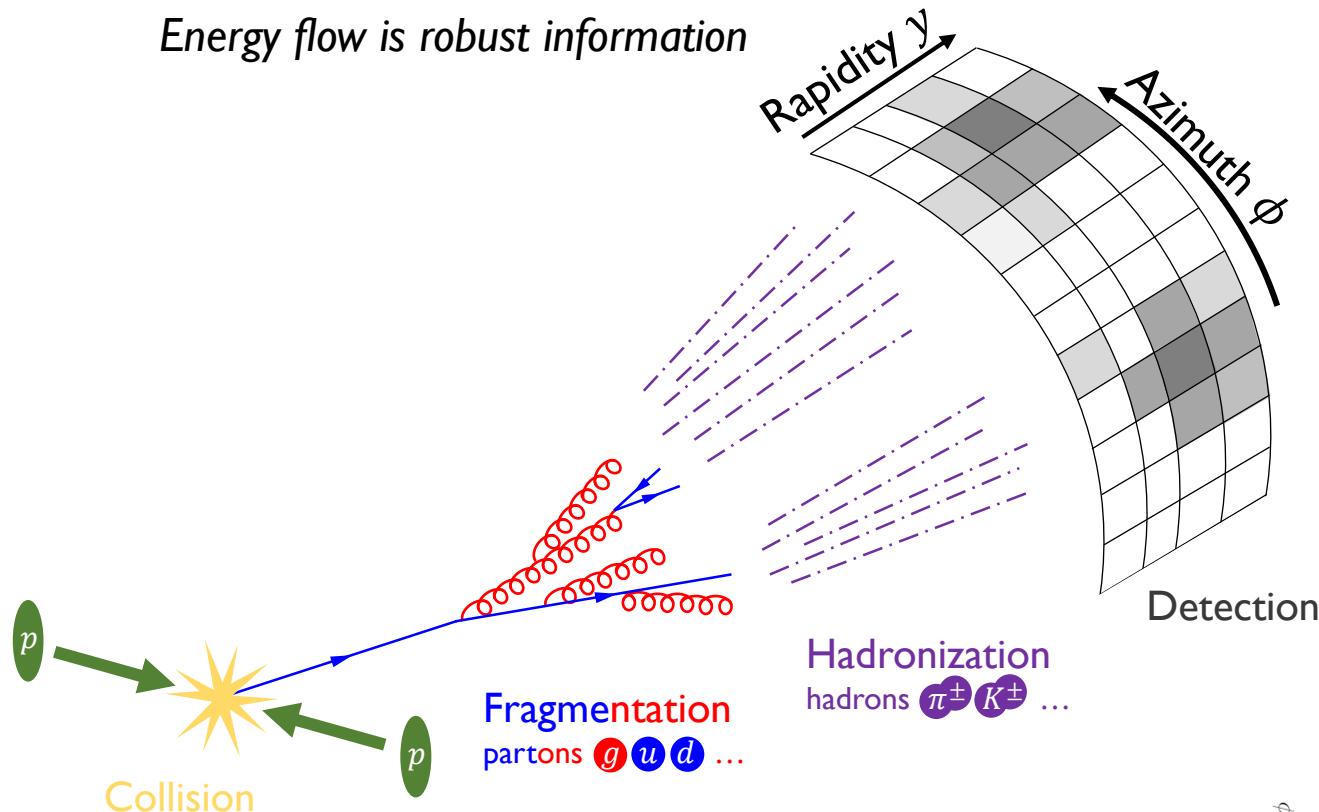
[\[F.V. Tkachov, 9601308\]](#)

[\[P.S. Cherzor, N.A. Sveshnikov, 9710349\]](#)

Energy flow \Leftrightarrow Infrared and Collinear (IRC) Safe information

When are two jets similar?

Energy flow is robust information

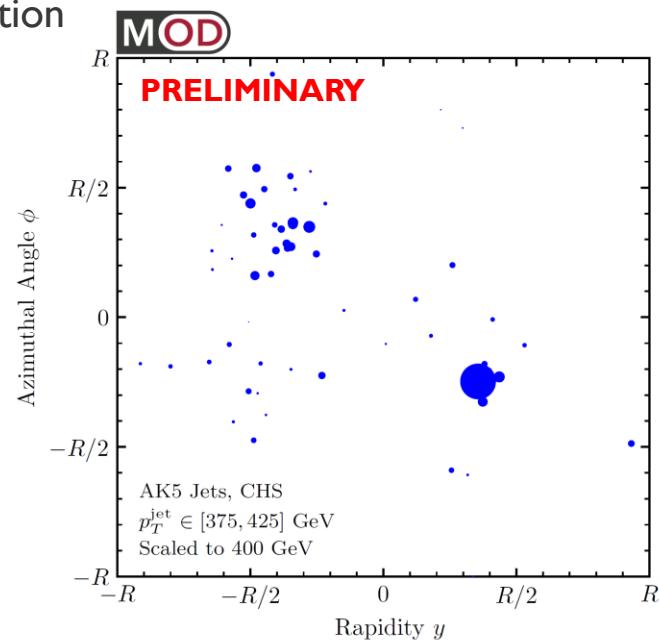
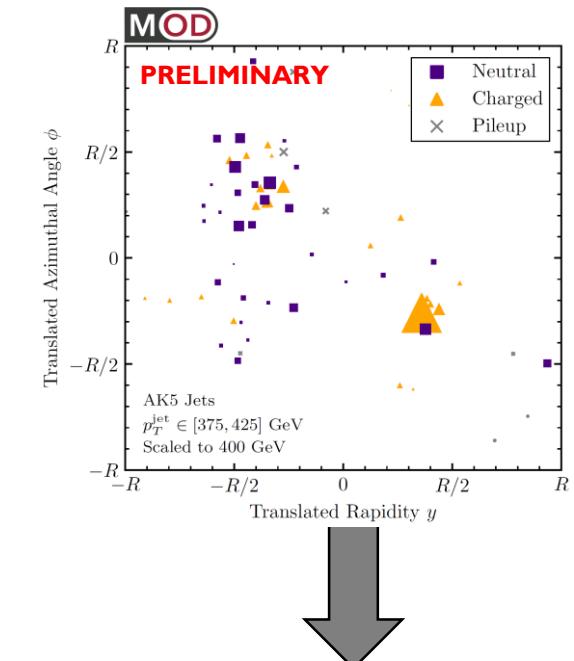


Treat jets as distributions of energy:

Ignoring particle flavor, charge...

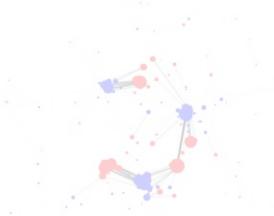
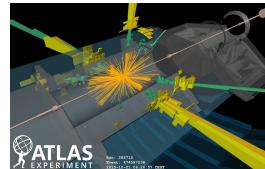
$$\sum_{i=1}^M E_i \delta(\hat{p}_i)$$

↑
energy ↑
direction



Outline

Part I Introduction



When are two jets similar?

When they have similar distributions of energy

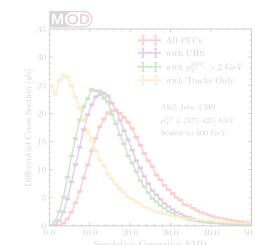
The Energy Mover's Distance

Part II Application



Jets in CMS Open Data

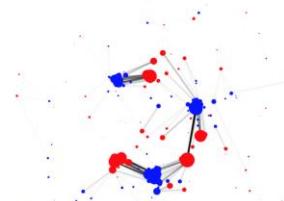
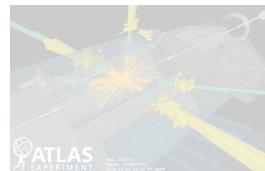
Exploring the Space of Jets



Quantifying Detector Effects

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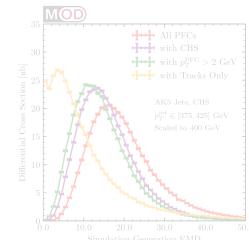
Movie Time

Part II Application



Jets in CMS Open Data

Exploring the Space of Jets



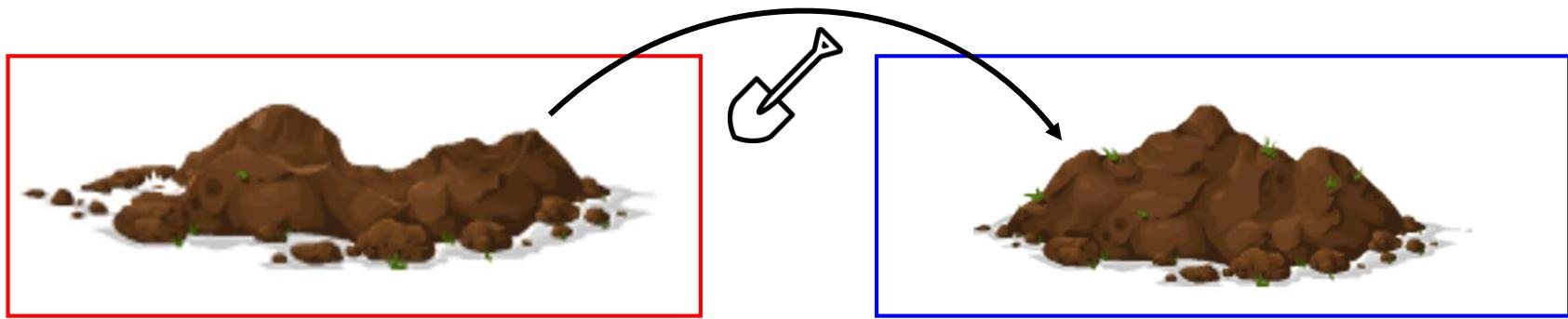
Quantifying Detector Effects

The Energy Mover's Distance

Review: *The Earth Mover's Distance*

Earth Mover's Distance: the minimum “work” ($\text{stuff} \times \text{distance}$) to rearrange one pile of dirt into another

[[Peleg, Werman, Rom](#)]
[[Rubner, Tomasi, Guibas](#)]



Metric on the space of (normalized) distributions: *symmetric, non-negative, triangle inequality*

Distributions are close in EMD \Leftrightarrow their expectation values are close.

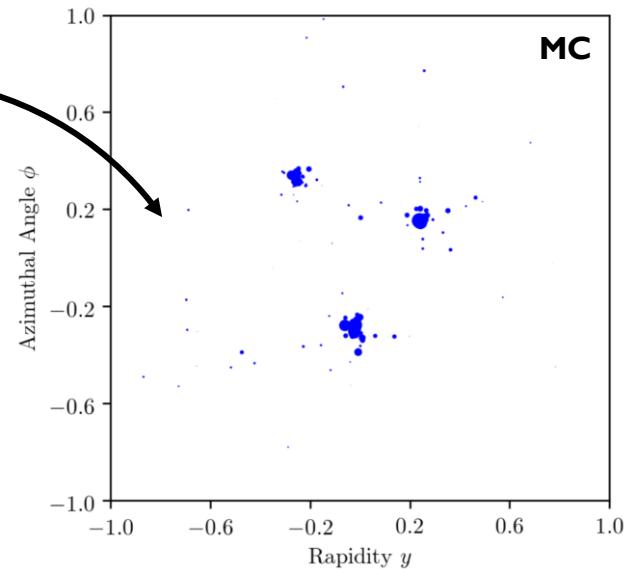
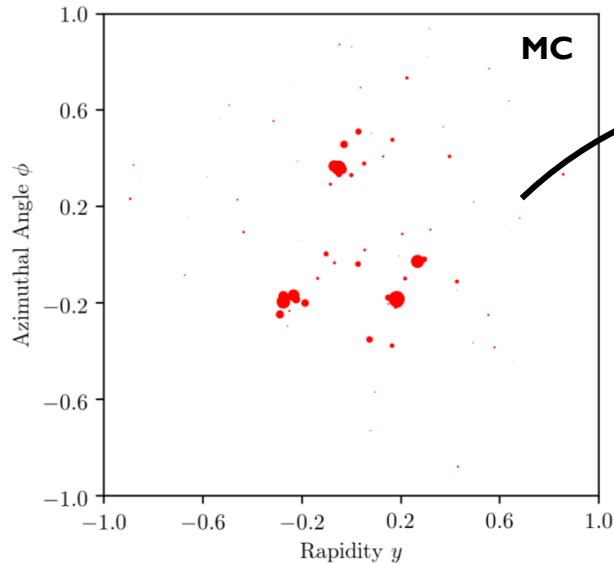
Also known as the 1-Wasserstein metric.

The Energy Mover's Distance

From Earth to Energy

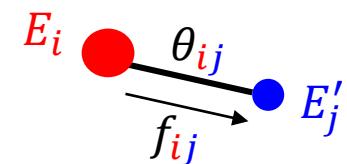
Energy Mover's Distance: the minimum “work” (**energy** \times angle) to rearrange one event (pile of energy) into another

[Komiske, EMM, Thaler, 1902.02346]



$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_{i=1}^M \sum_{j=1}^{M'} f_{ij} \frac{\theta_{ij}}{R}$$

Difference in
radiation pattern

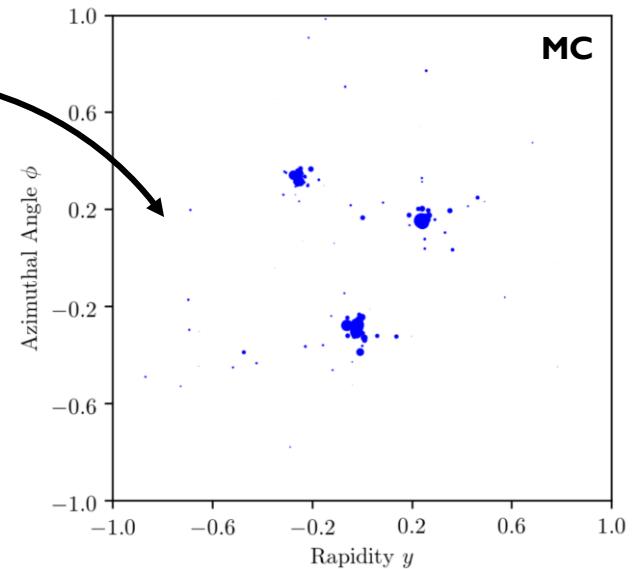
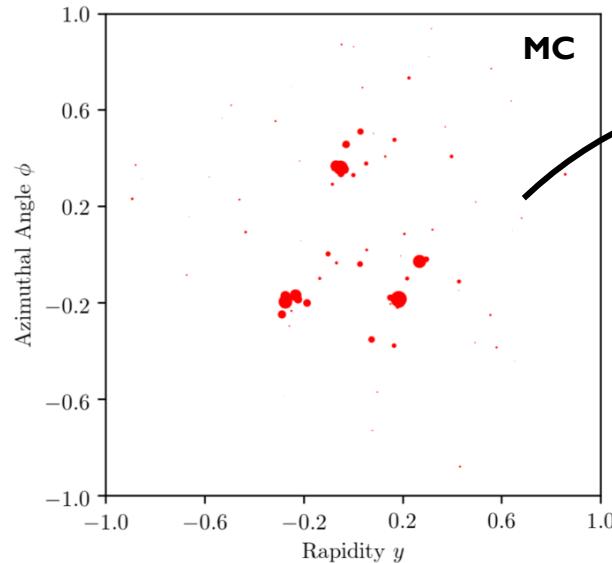


The Energy Mover's Distance

From Earth to Energy

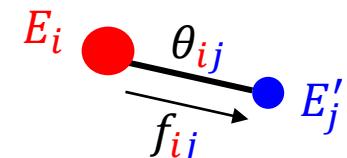
Energy Mover's Distance: the minimum “work” (**energy** \times angle) to rearrange one event (pile of energy) into another

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$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_{i=1}^M \sum_{j=1}^{M'} f_{ij} \frac{\theta_{ij}}{R} + \left| \sum_{i=1}^M E_i - \sum_{j=1}^{M'} E'_j \right|$$

Difference in radiation pattern Difference in total energy

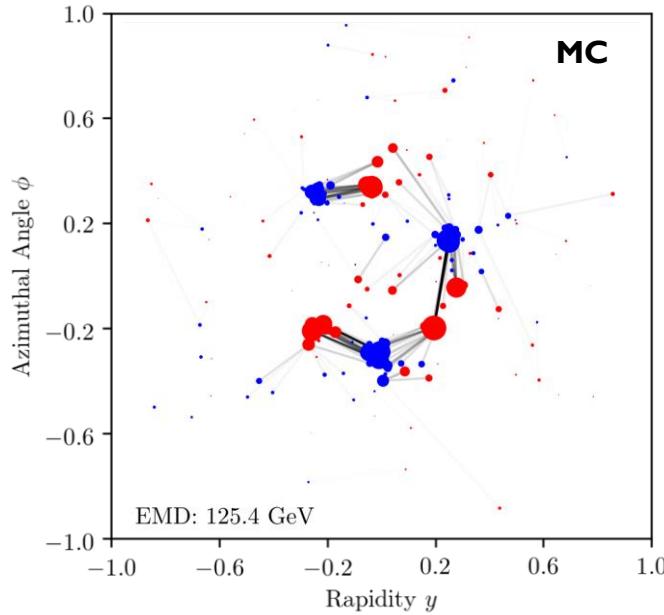


The Energy Mover's Distance

From Earth to Energy

Energy Mover's Distance: the minimum “work” (**energy** \times angle) to rearrange one event (pile of energy) into another

[P.T. Komiske, EMM, J. Thaler, 1902.02346]



$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_{i=1}^M \sum_{j=1}^{M'} f_{ij} \frac{\theta_{ij}}{R} + \left| \sum_{i=1}^M E_i - \sum_{j=1}^{M'} E'_j \right|$$

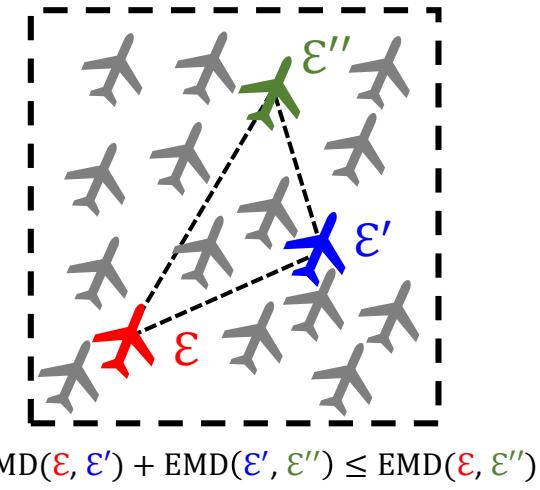
Difference in radiation pattern Difference in total energy

EMD has dimensions of energy

True metric as long as $R \geq \frac{1}{2} \theta_{\max}$
 $R \geq$ the jet radius, for conical jets

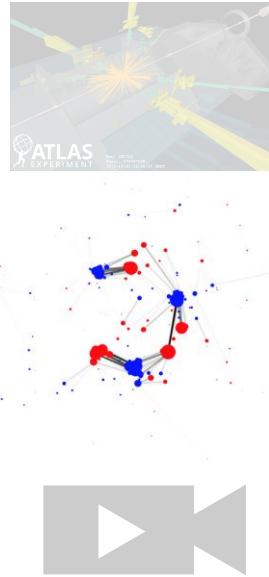
Solvable via Optimal Transport problem.

~1ms to compute EMD for two jets with 100 particles.



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When are two jets similar?

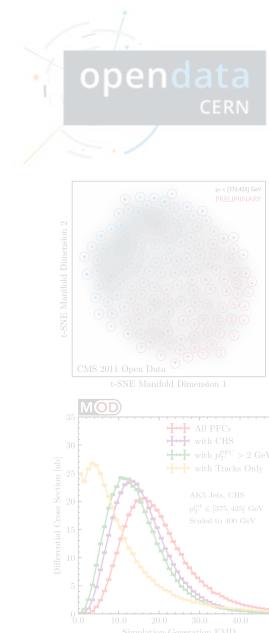
When they have similar distributions of energy

The Energy Mover's Distance

Work to rearrange one event into another.

Movie Time

Part II Application



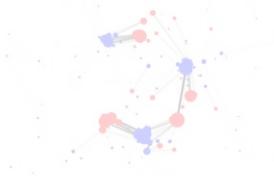
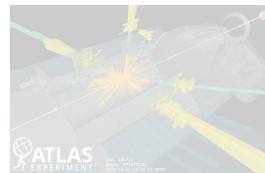
Jets in CMS Open Data

Exploring the Space of Jets

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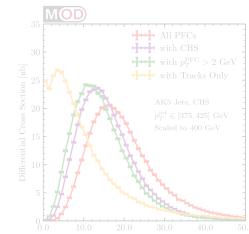
Movie Time

Part II Application



Jets in CMS Open Data

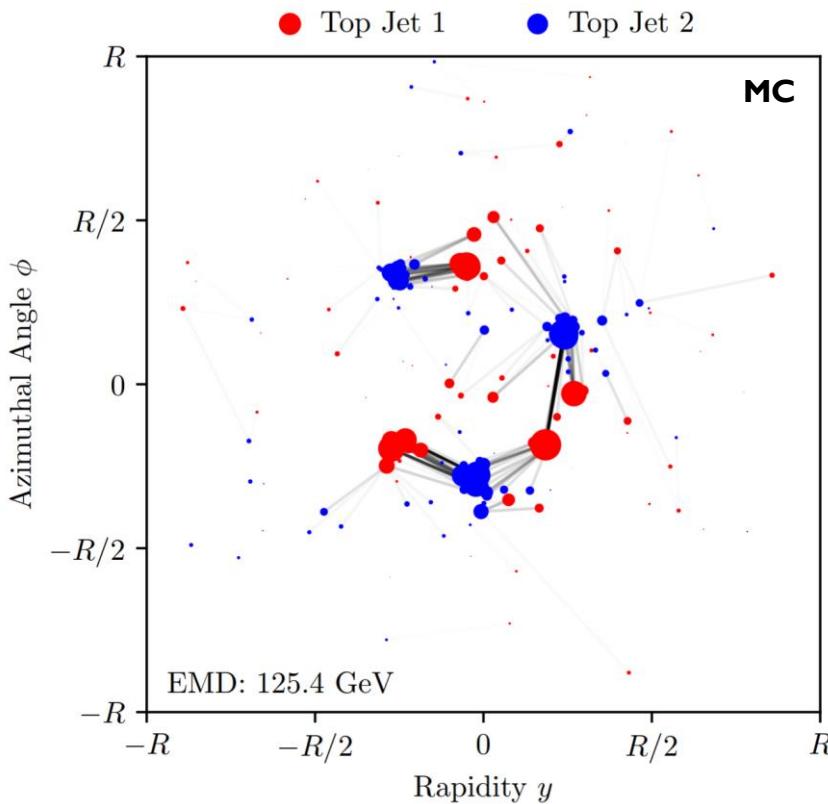
Exploring the Space of Jets



Quantifying Detector Effects

Movie Time: Visualizing the EMD

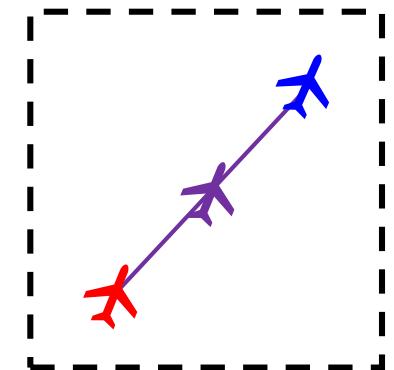
Taking a walk in the space of events



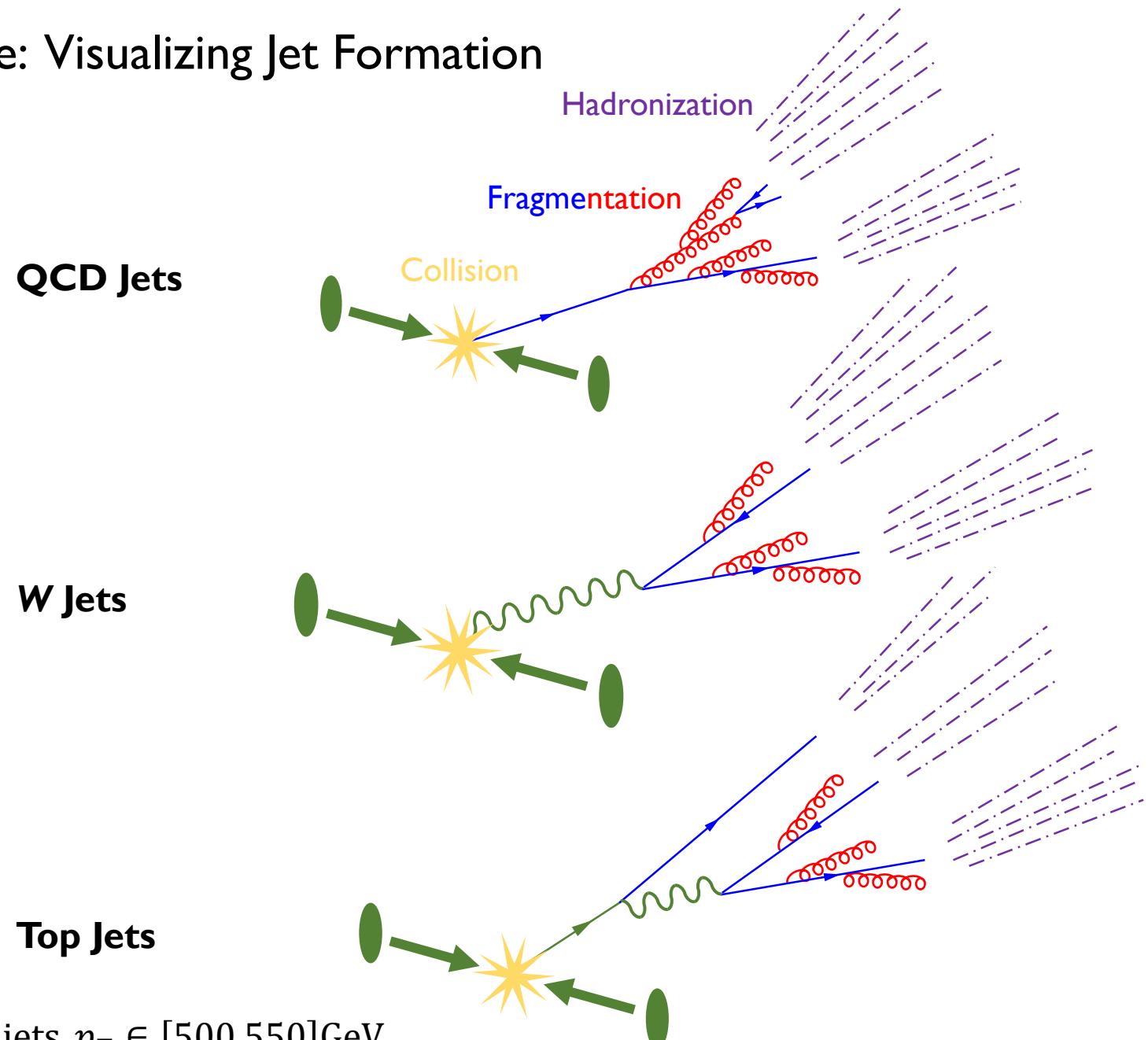
EMD is the cost of an optimal transport problem.

We also get the *shortest path* between the events.

Interpolate along path to visualize!

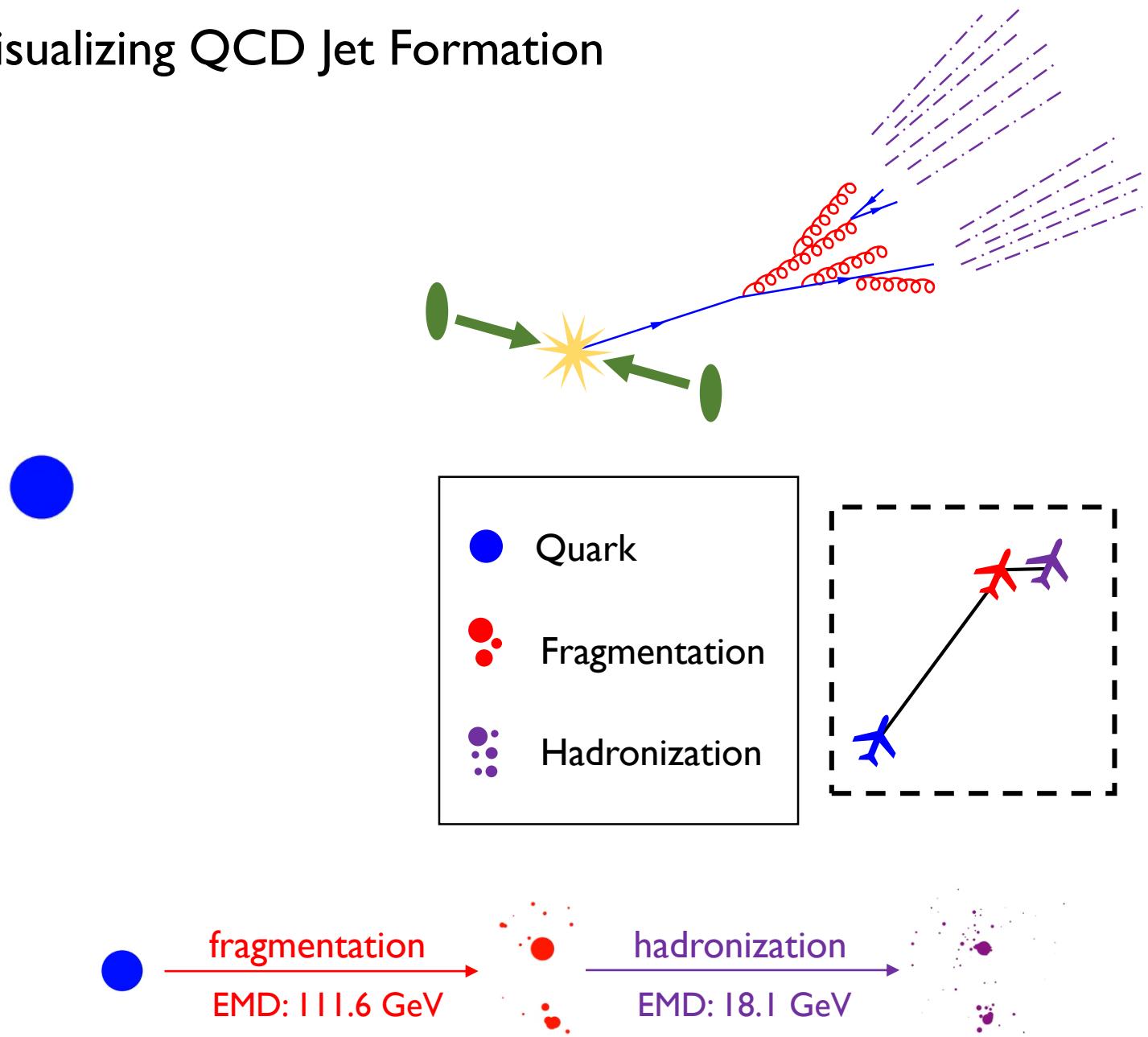


Movie Time: Visualizing Jet Formation

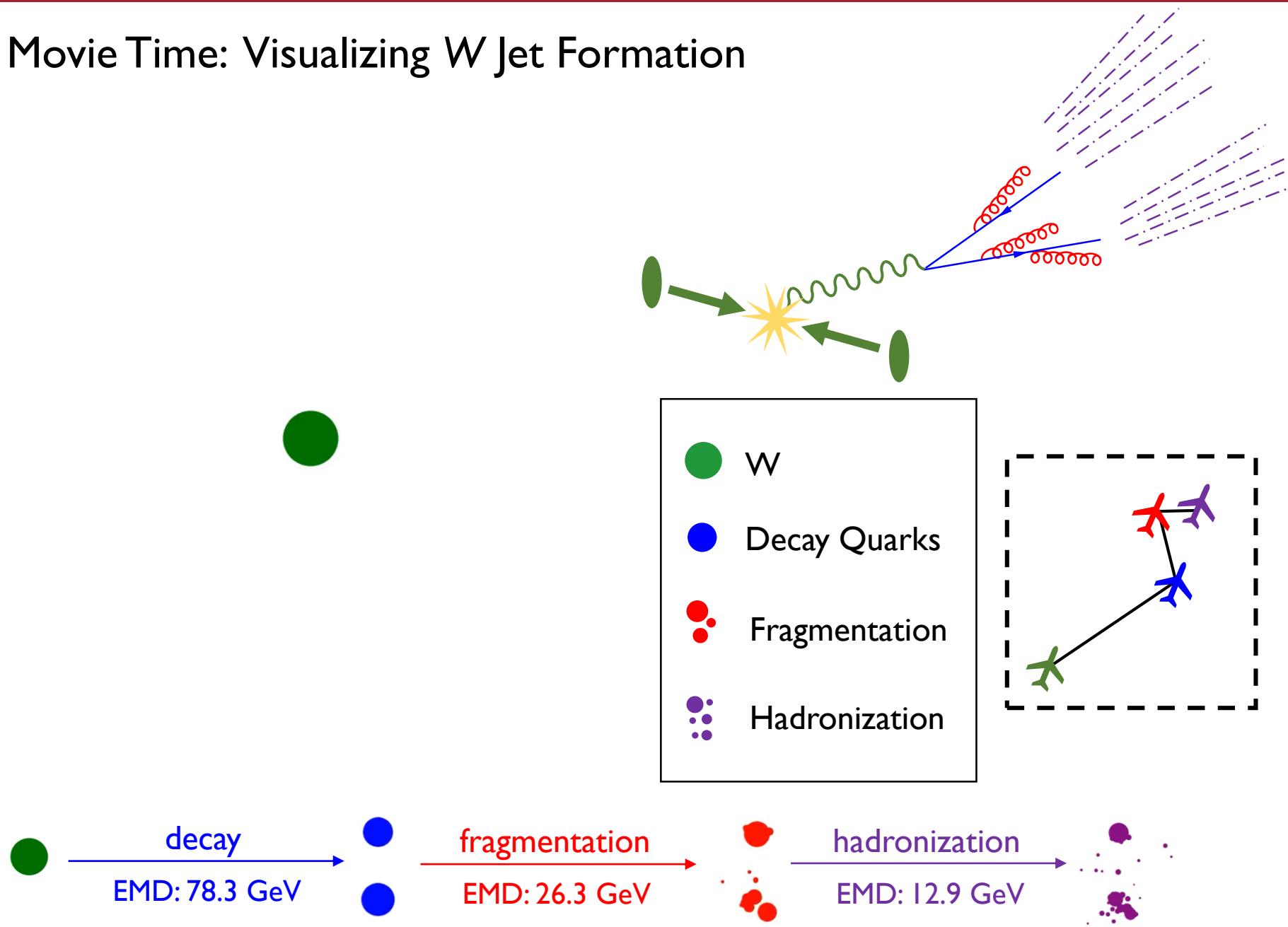


Pythia 8, $R = 1.0$ jets, $p_T \in [500,550]\text{GeV}$

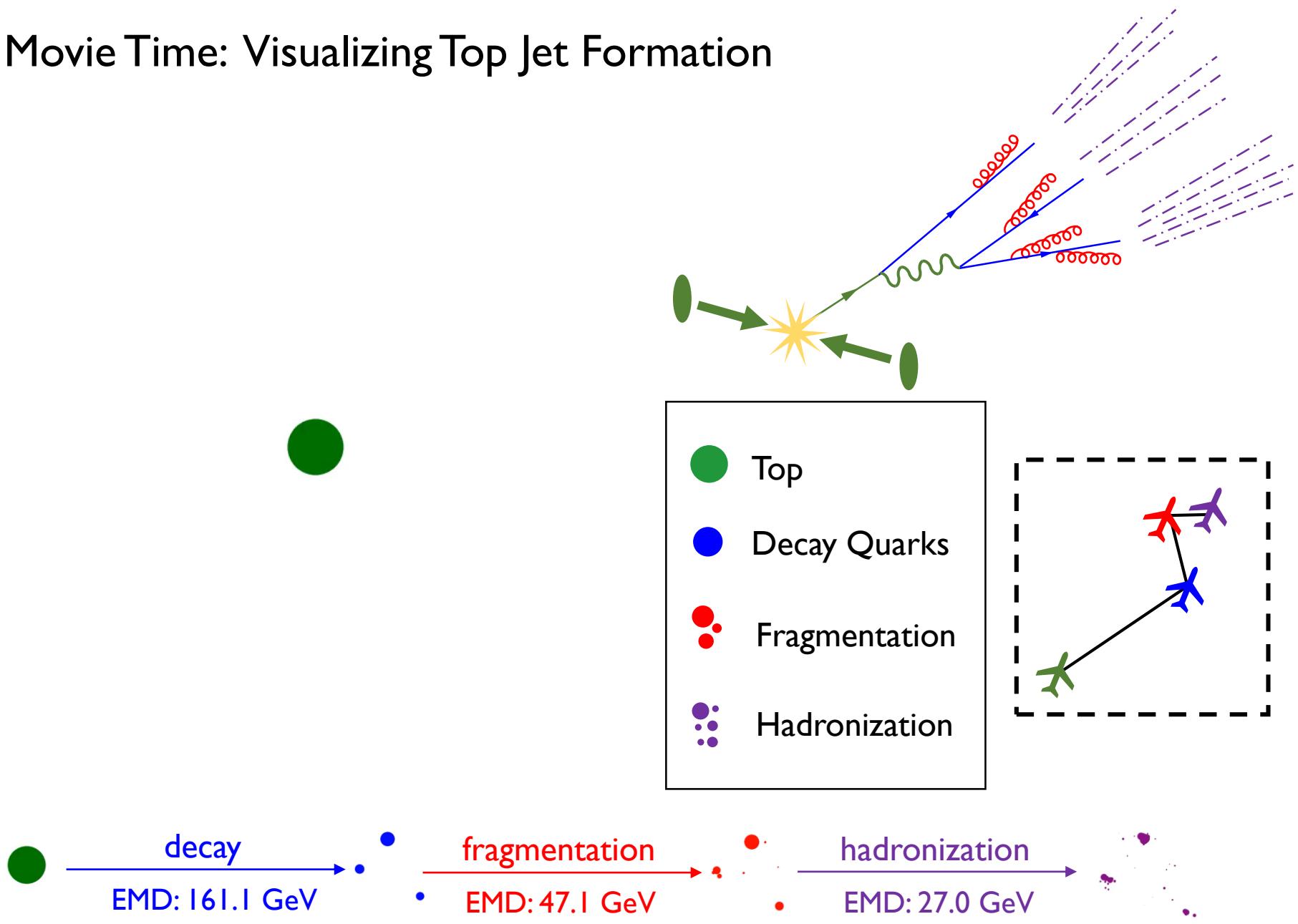
Movie Time: Visualizing QCD Jet Formation



Movie Time: Visualizing W Jet Formation

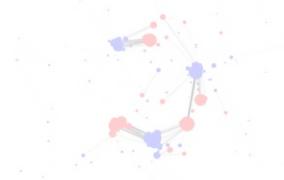
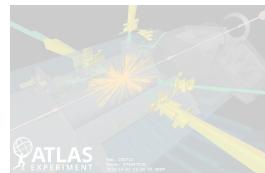


Movie Time: Visualizing Top Jet Formation



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Part I Introduction



When are two jets similar?

When they have similar distributions of energy

The Energy Mover's Distance

Work to rearrange one event into another.

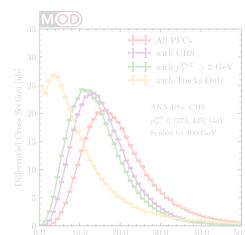
Movie Time

Visualize energy movement and jet formation.

Jets in CMS Open Data



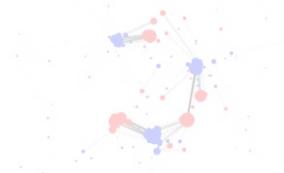
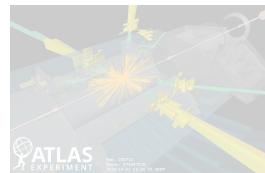
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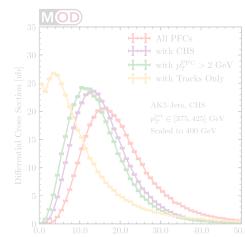
Movie Time

Visualize energy movement and jet formation.



Jets in CMS Open Data

Exploring the Space of Jets



Quantifying Detector Effects

CMS Open Data

An amazing resource for physics exploration and proof-of-principle studies.



opendata.cern.ch

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About ▾

Explore more than **1 petabyte**
of open data from particle physics!

jet primary dataset

search examples: [collision datasets](#), [keywords:education](#), [energy:7TeV](#)

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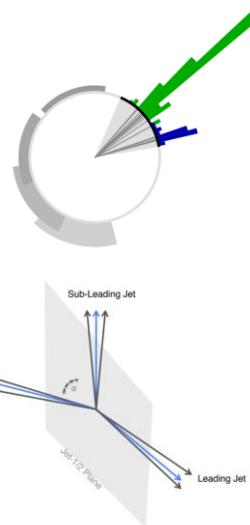
Focus on

[ATLAS](#)
[ALICE](#)
[CMS](#)
[LHCb](#)
[OPERA](#)

▼ Get started ▼

CMS Open Data

Many exciting physics applications with the CMS Open Data already.



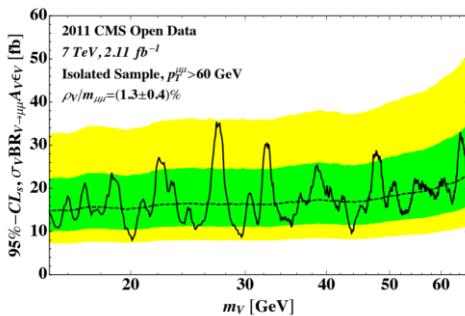
Exposing the QCD splitting function

[\[Tripathee, Xue, Larkoski, Marzani, Thaler, 1704.05842\]](#)

[\[Larkoski, Marzani, Thaler, Tripathee, Xue, 1704.05066\]](#)

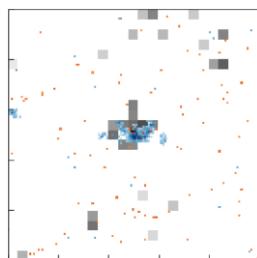
Looking for parity violation in jets

[\[Lester, Schott, 1904.11195\]](#)



Searching for dimuon resonances

[\[Cesarotti, Soreq, Strassler, Thaler, Xue, 1902.04222\]](#)



Analyzing collision data with deep learning techniques

[\[Madrazo, Cacha, Iglesias, de Lucas, 1708.07034\]](#)

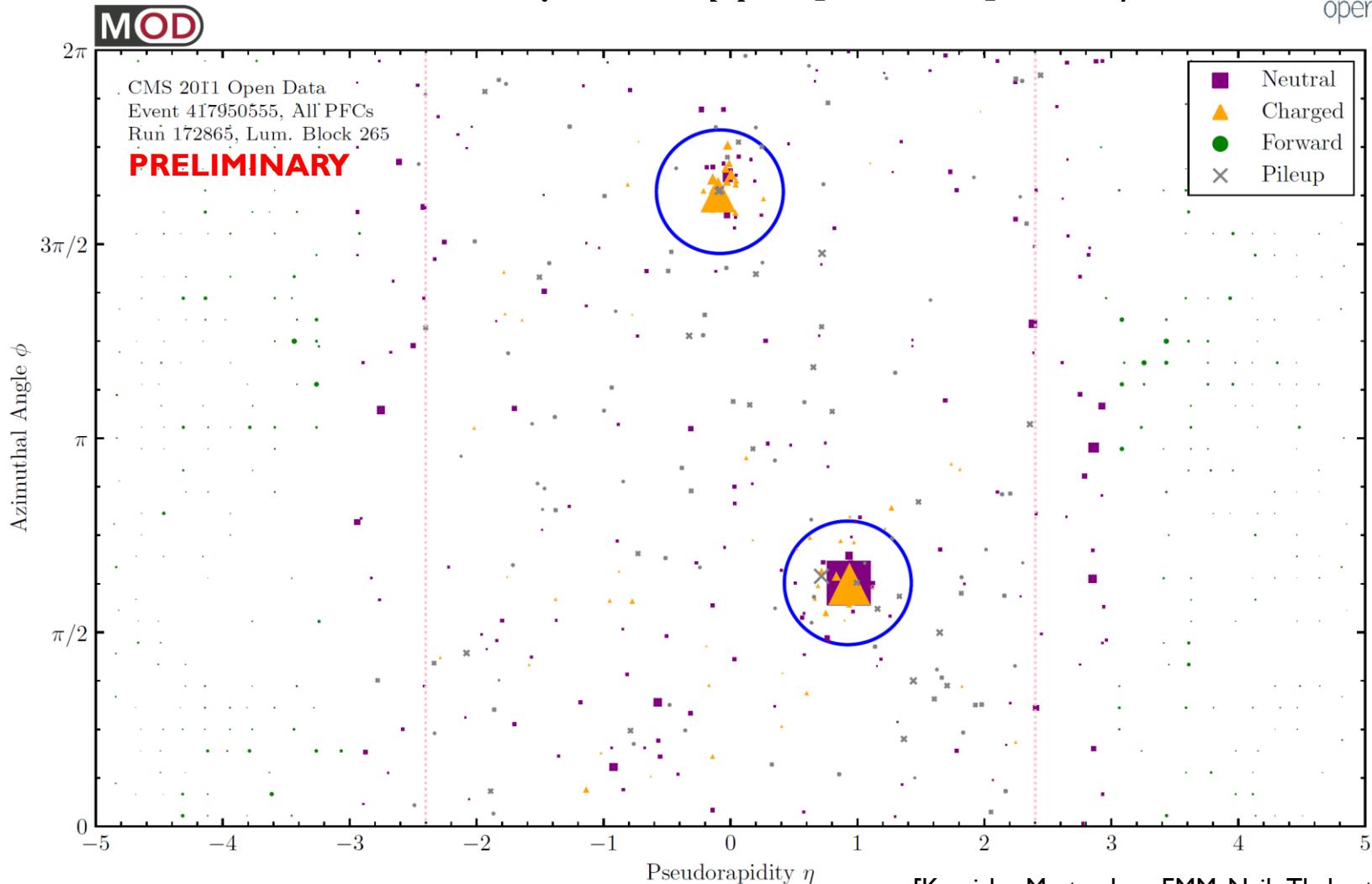
[\[Andrews, Paulini, Gleyzer, Poczos, 1807.11916\]](#)

[\[Andrews, et al., 1902.08276\]](#)

CMS 2011 A Jet Primary Dataset (+ Simulation)

2.3 fb^{-1} of 7 TeV proton-proton collision data. [\[link\]](#)

~1 million $R = 0.5$ jets with $p_T \in [375, 425]\text{GeV}$, $|\eta| < 1.9$



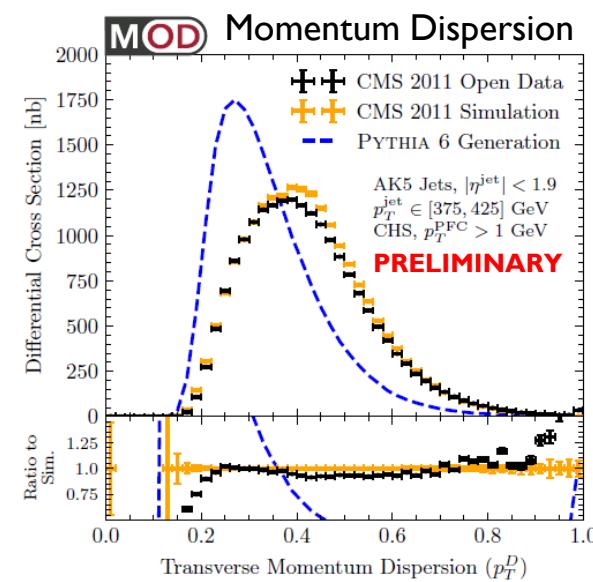
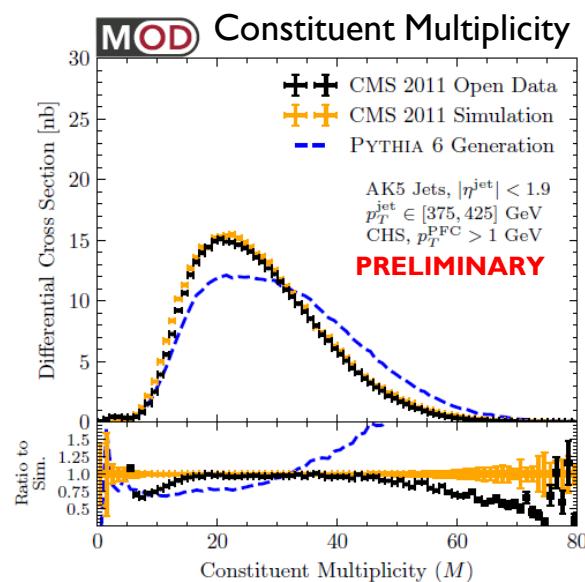
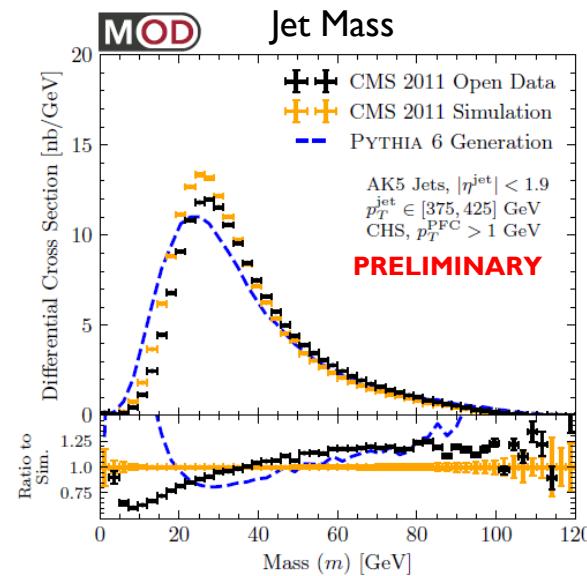
Jet Substructure Observables

Study jet substructure at truth and detector level.

$$m^2 = \left(\sum_{i \in \text{Jet}} p_i^\mu \right)^2$$

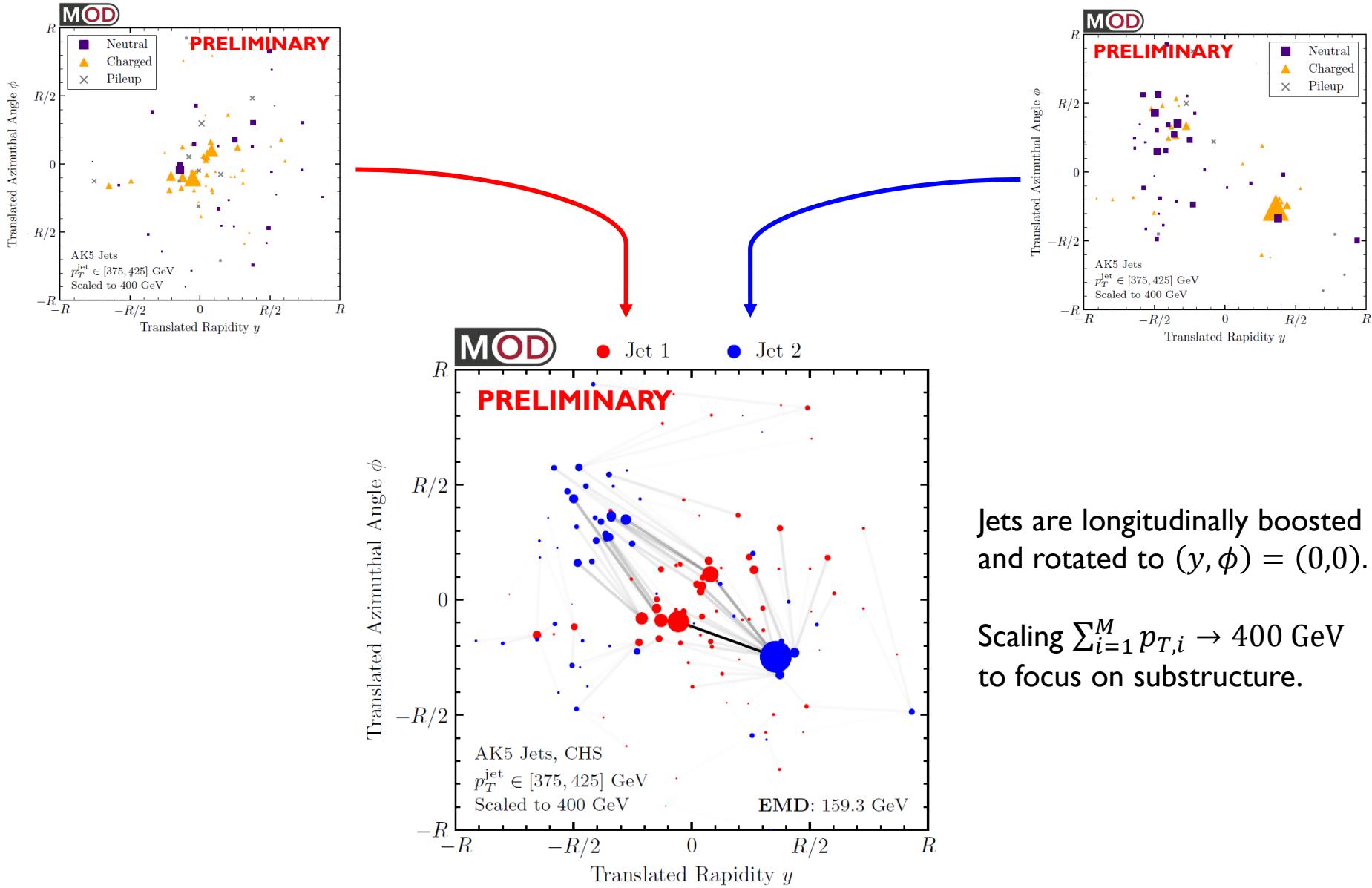
$$M = \sum_{i \in \text{Jet}} 1$$

$$p_T^D = \frac{\sum_{i \in \text{Jet}} p_{T,i}^2}{\left(\sum_{i \in \text{Jet}} p_{T,i} \right)^2}$$



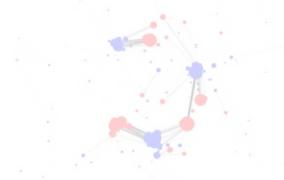
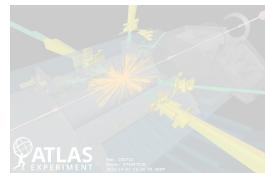
Similar to: [\[Larkoski, Marzani, Thaler, Tripathee, Xue, 1704.05066\]](#)

Comparing Jets in CMS Open Data



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When are two jets similar?

When they have similar distributions of energy

The Energy Mover's Distance

Work to rearrange one event into another.

Movie Time

Visualize energy movement and jet formation.

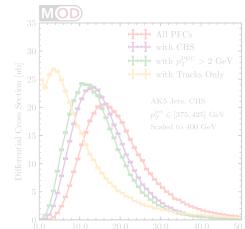


Jets in CMS Open Data

A great resource for physics exploration

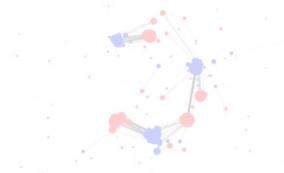
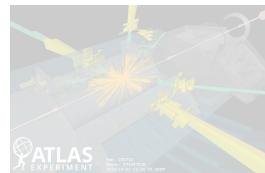
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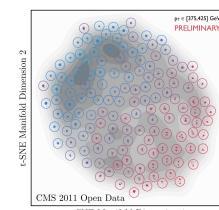
Movie Time

Visualize energy movement and jet formation.

Jets in CMS Open Data

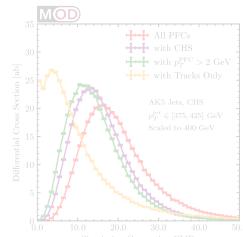
A great resource for physics exploration

Part II Application

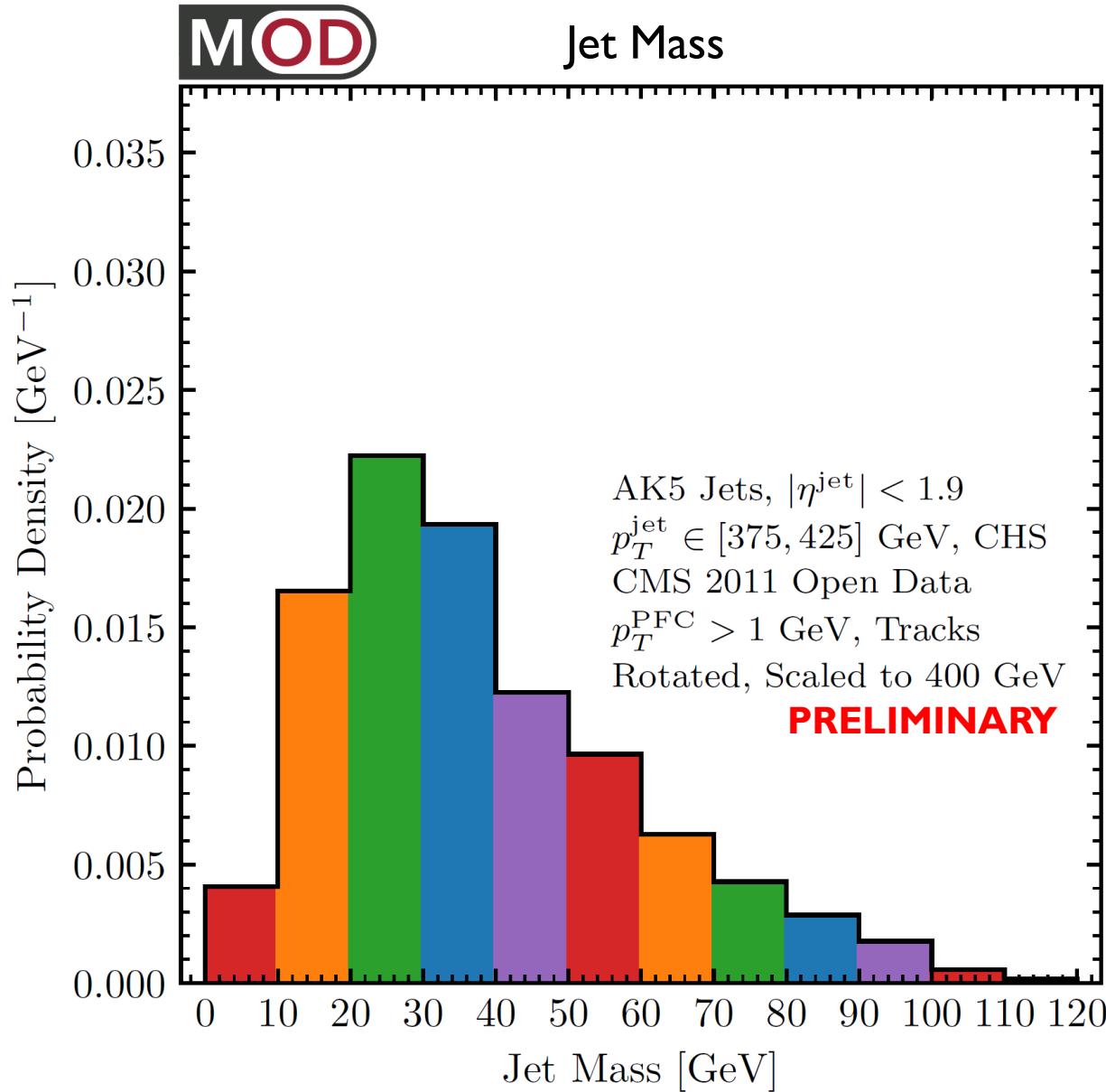
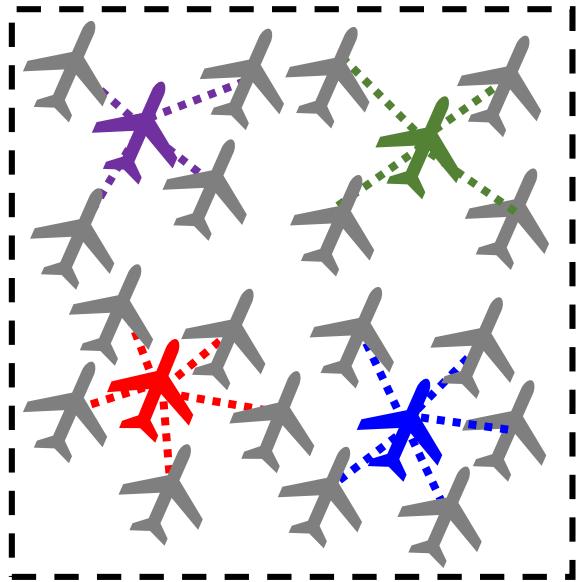


Exploring the Space of Jets

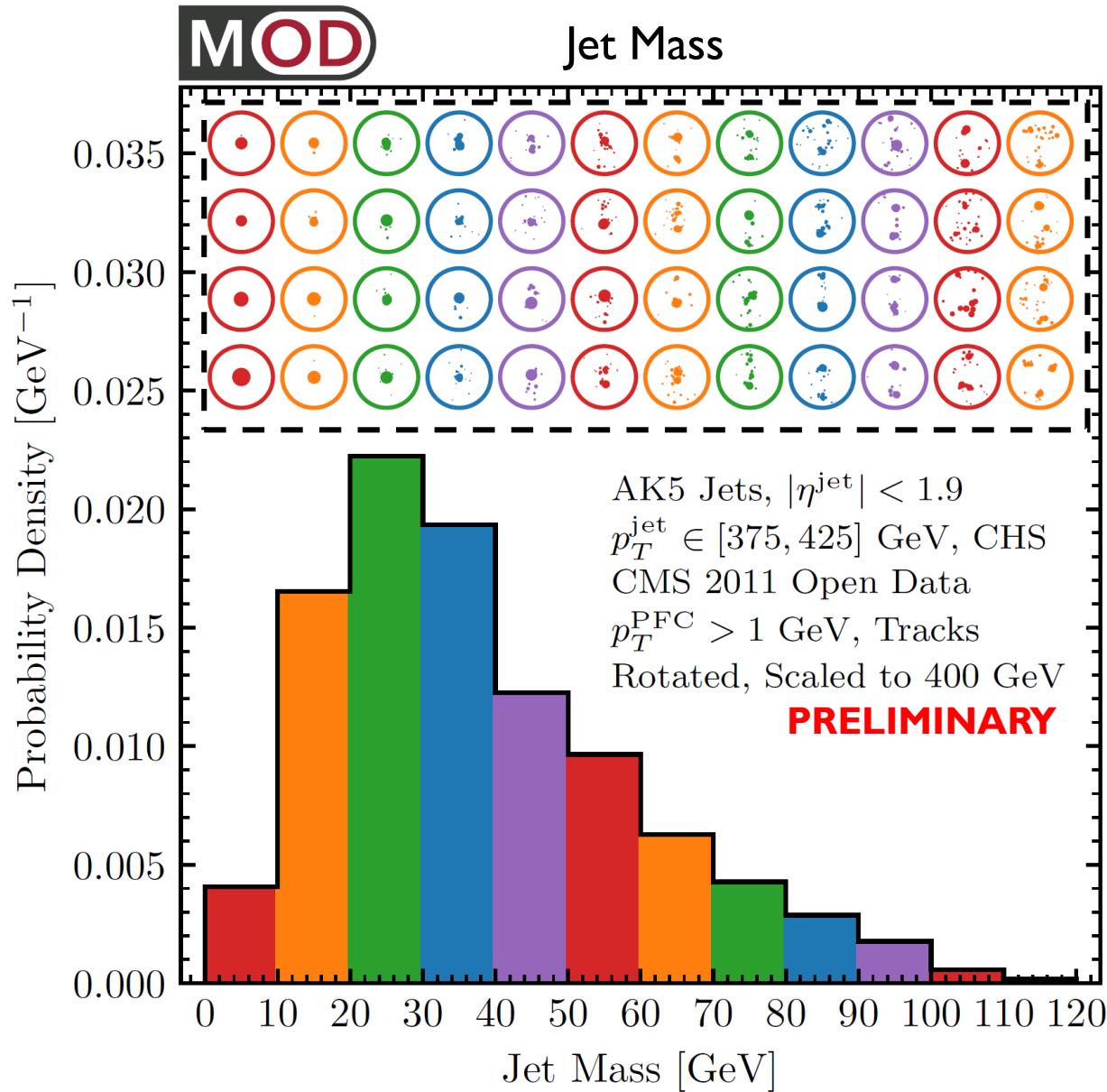
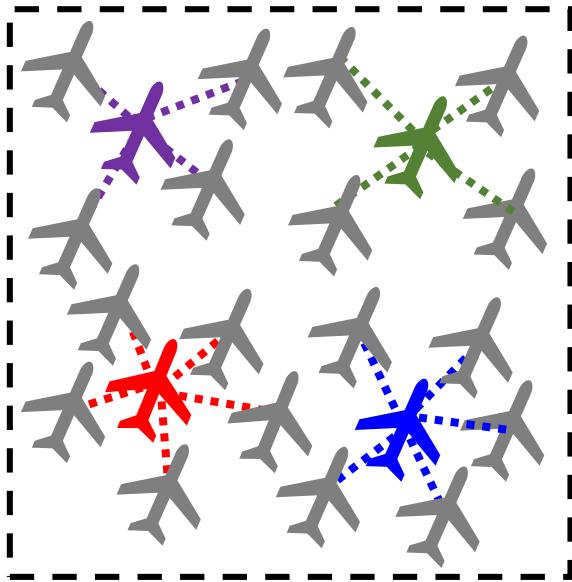
Quantifying Detector Effects



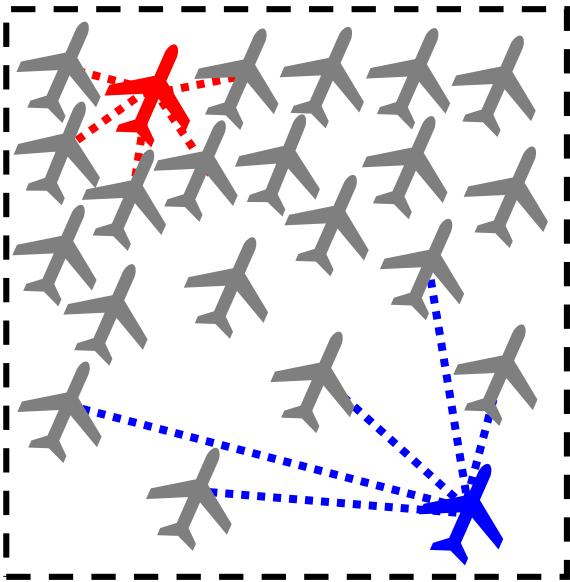
Most Representative Jets: K-medoids



Most Representative Jets: K-medoids



Towards Anomaly Detection



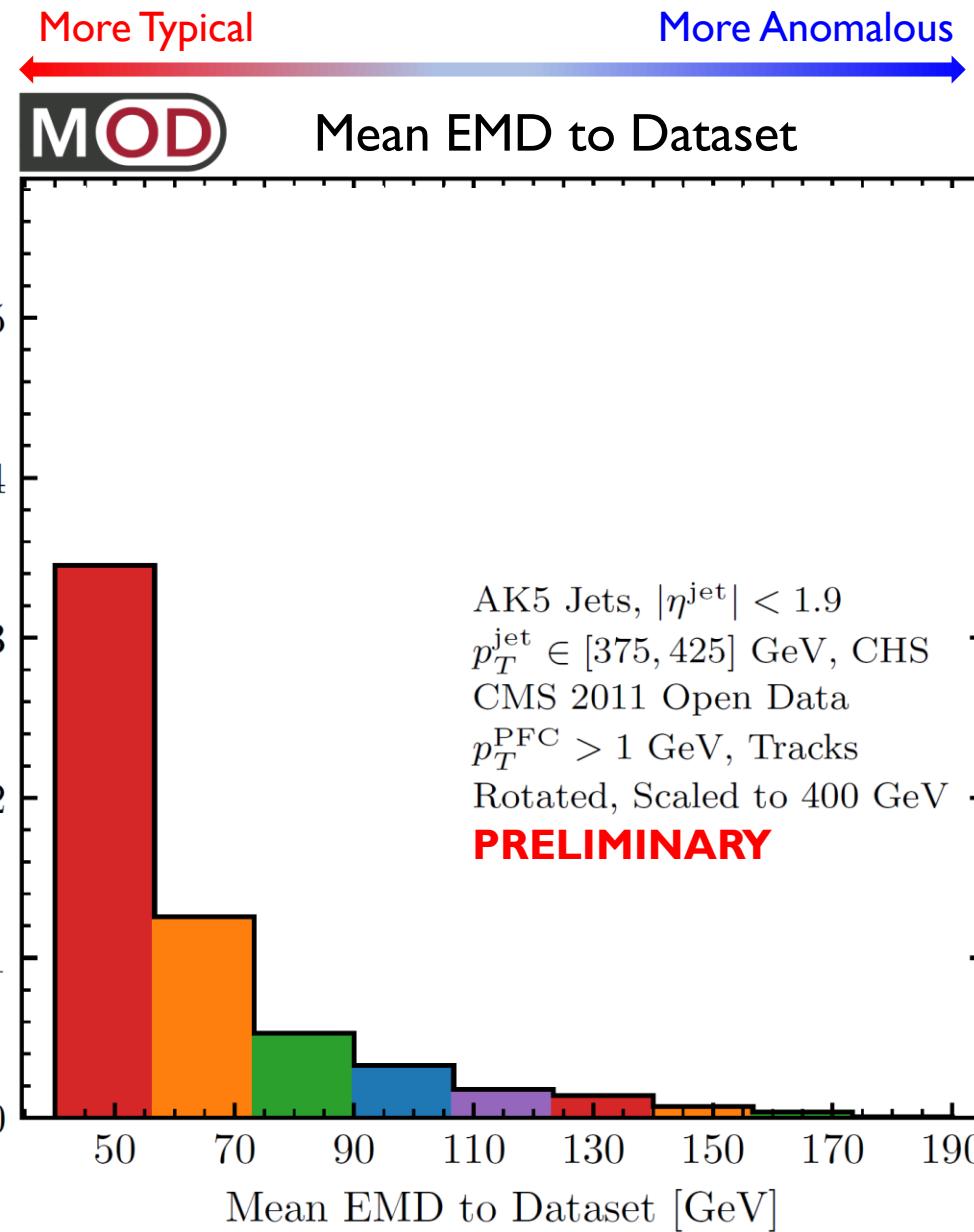
Complements recent developments in anomaly detection for collider physics.

[\[Collins, Howe, Nachman, 1805.02664\]](#)

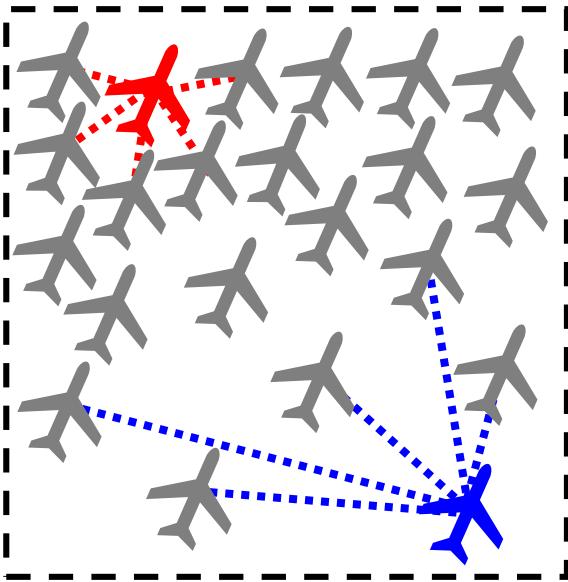
[\[Heimel, Kasieczka, Plehn, Thompson, 1808.08979\]](#)

[\[Farina, Nakai, Shih, 1808.08992\]](#)

[\[Cerri, Nguyen, Pierini, Spiropulu, Vlimant, 1811.10276\]](#)



Towards Anomaly Detection



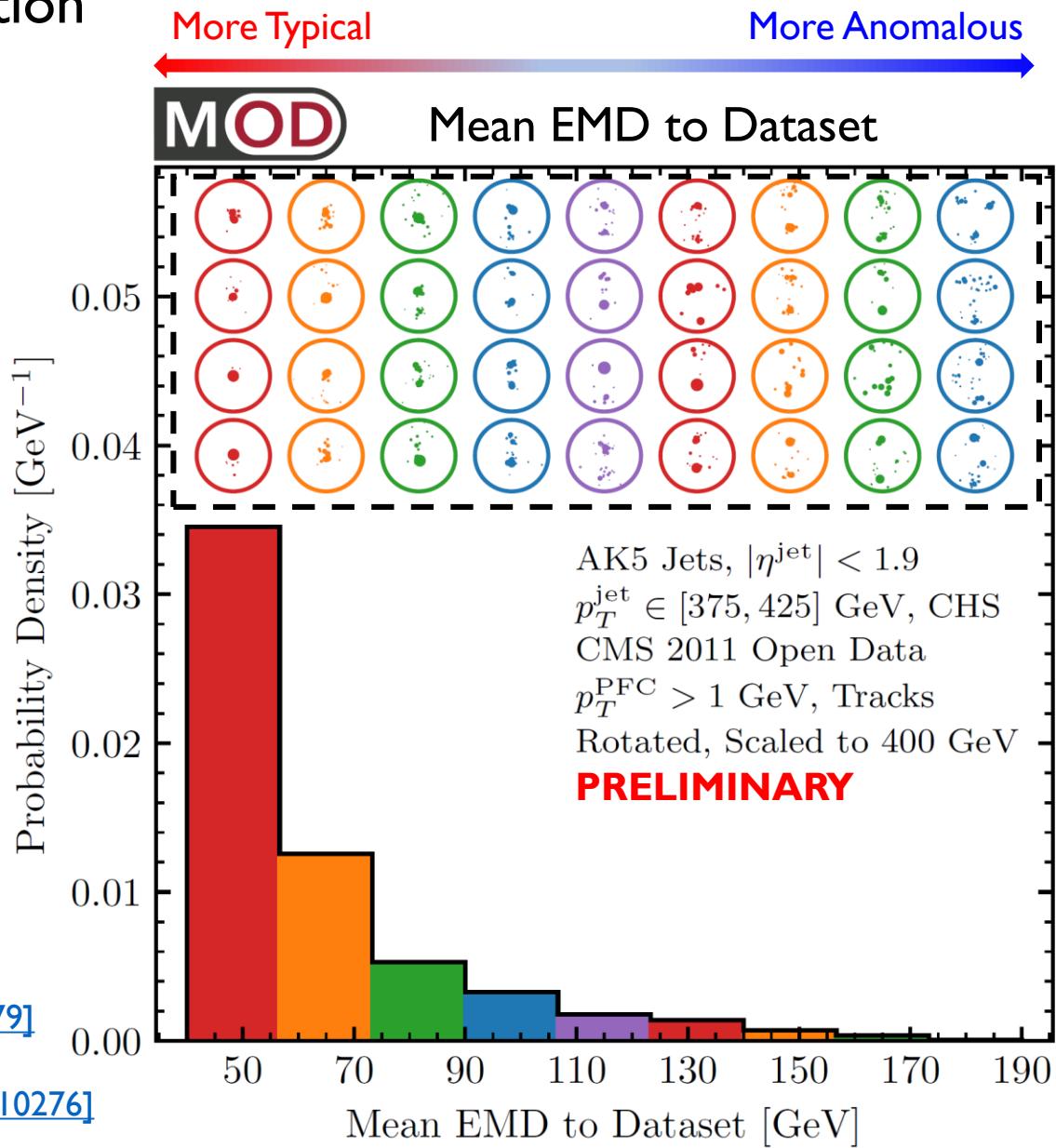
Complements recent developments in anomaly detection for collider physics.

[\[Collins, Howe, Nachman, 1805.02664\]](#)

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[\[Cerri, Nguyen, Pierini, Spiropulu, Vlimant, 1811.10276\]](#)

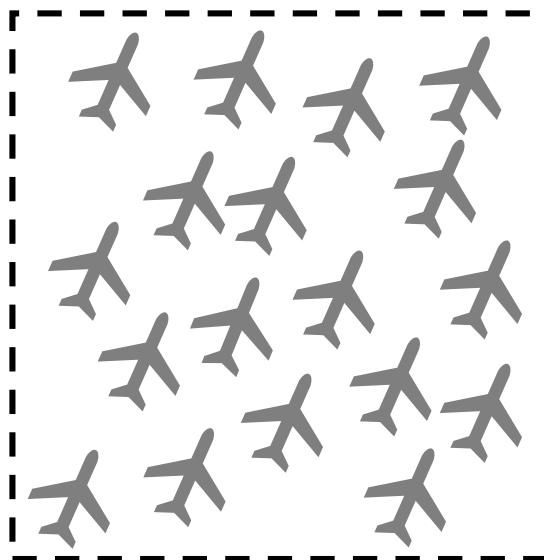


Exploring the Space of Jets: Visualizing the Manifold

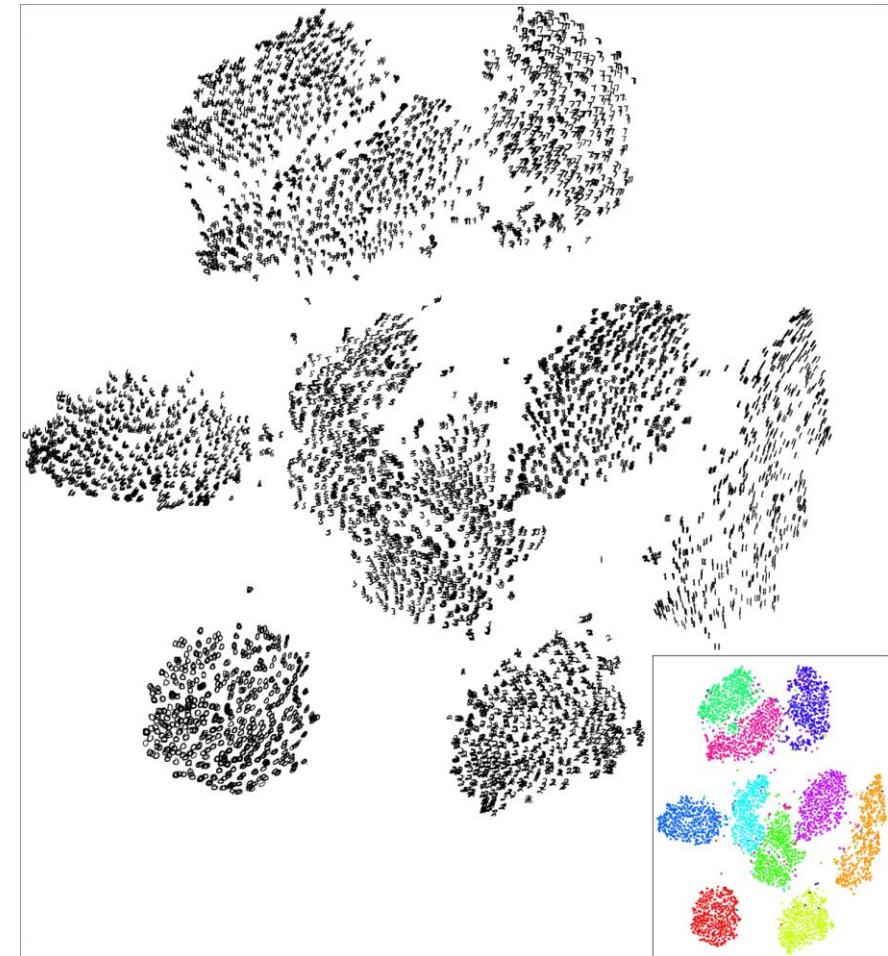
Visualize the space of events with t-Distributed Stochastic Neighbor Embedding (t-SNE).

[L. van der Maaten, G. Hinton]

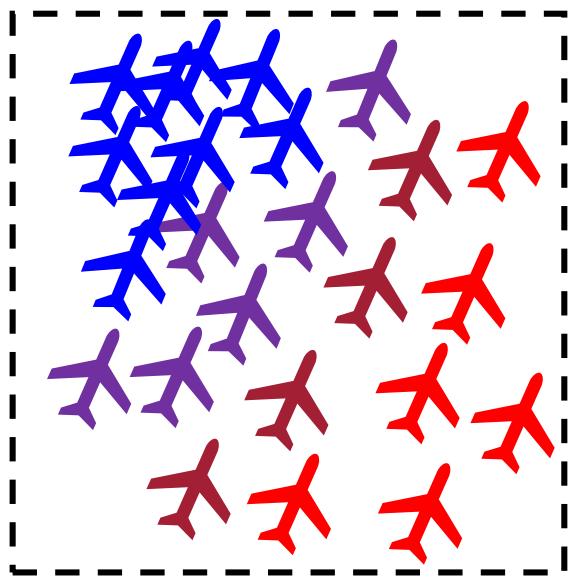
Finds an embedding into a low-dimensional manifold that respects distances.



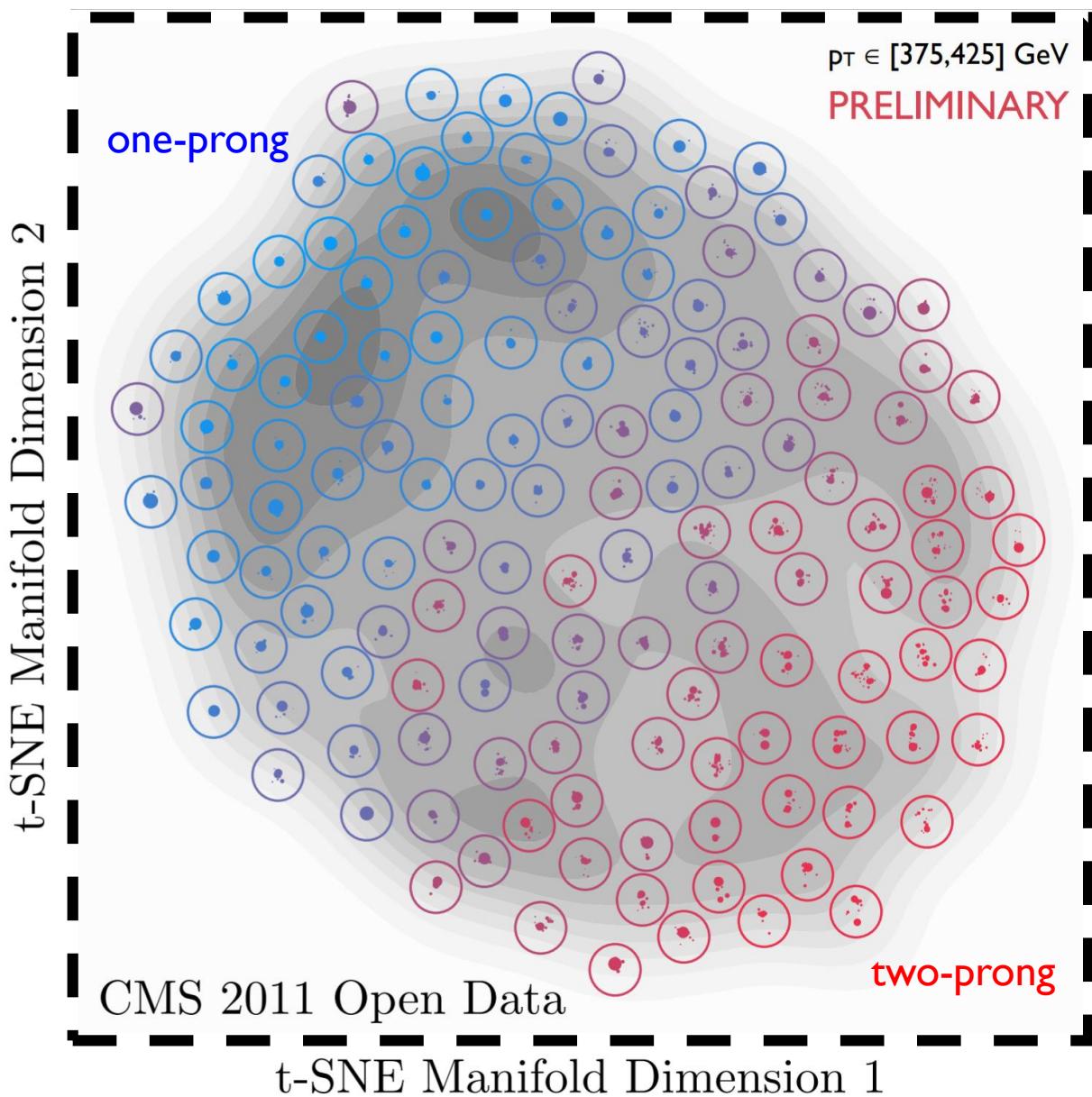
What does the space
of jets look like?



Exploring the Space of Jets: Visualizing the Manifold



What does the space
of jets look like?



Exploring the Space of Jets: Correlation Dimension

VOLUME 50, NUMBER 5

PHYSICAL REVIEW LETTERS

31 JANUARY 1983

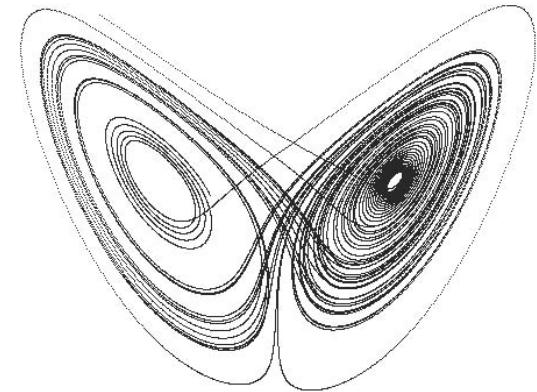
Characterization of Strange Attractors

Peter Grassberger^(a) and Itamar Procaccia

Chemical Physics Department, Weizmann Institute of Science, Rehovot 76100, Israel

(Received 7 September 1982)

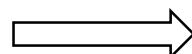
A new measure of strange attractors is introduced which offers a practical algorithm to determine their character from the time series of a single observable. The relation of this new measure to fractal dimension and information-theoretic entropy is discussed.



Intuition:

$$N_{\text{neighboring}}(r) \propto r^{\dim}$$

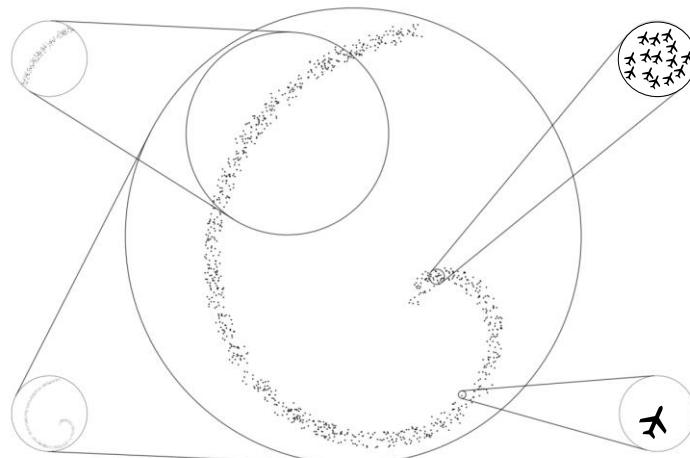
points



$$\dim(r) = r \frac{\partial}{\partial r} \ln N_{\text{neighbors}}(r)$$

$\dim \approx 1$

$\dim \approx 2$



$\dim \approx 2$

(eventually 0)

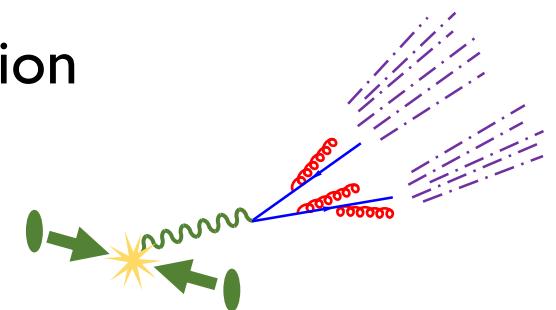
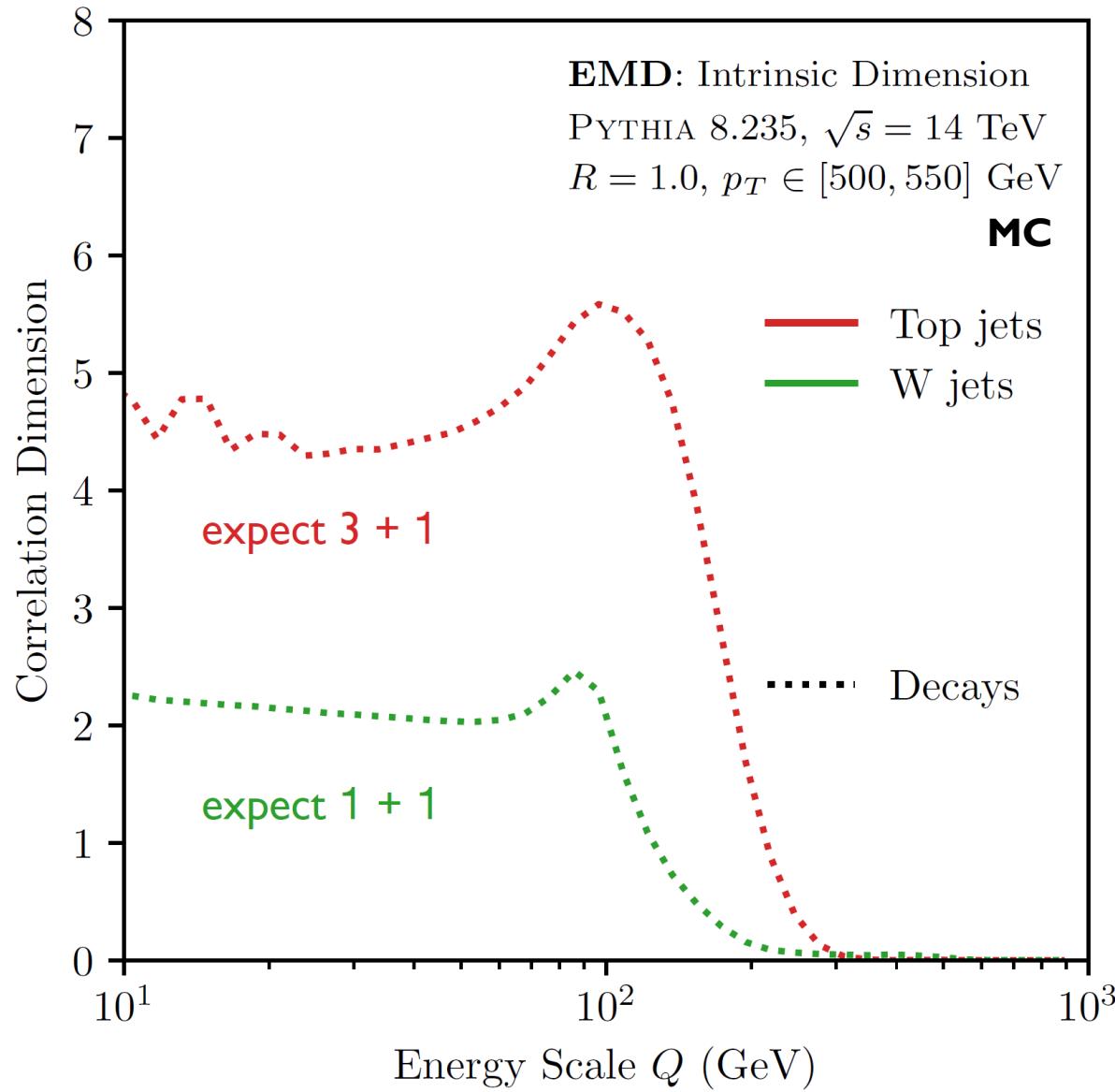
Correlation dimension:

$$\dim(Q) = Q \frac{\partial}{\partial Q} \ln \sum_{i=1}^N \sum_{j=1}^N \Theta[\text{EMD}(\varepsilon_i, \varepsilon_j) < Q]$$

Energy scale Q
dependence

Count neighbors in
ball of radius Q

Exploring the Space of Jets: Correlation Dimension



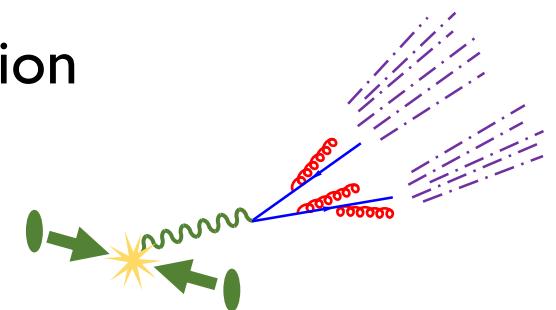
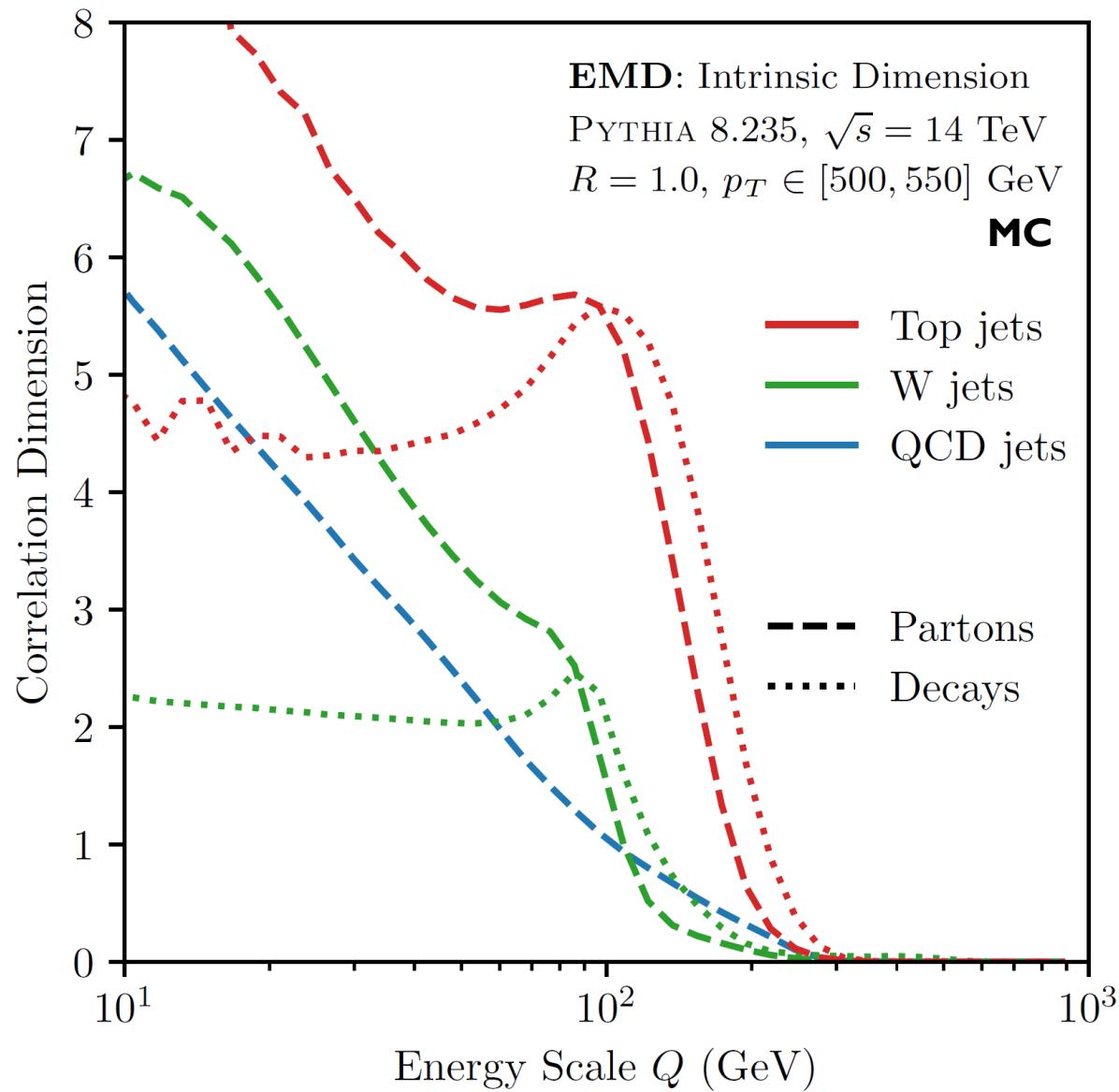
QCD jets are simplest.

W jets are more complicated.

Top jets are most complex.

“Decays” have \sim constant dimension.

Exploring the Space of Jets: Correlation Dimension



QCD jets are simplest.

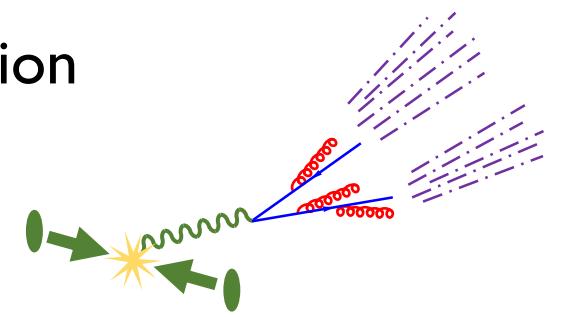
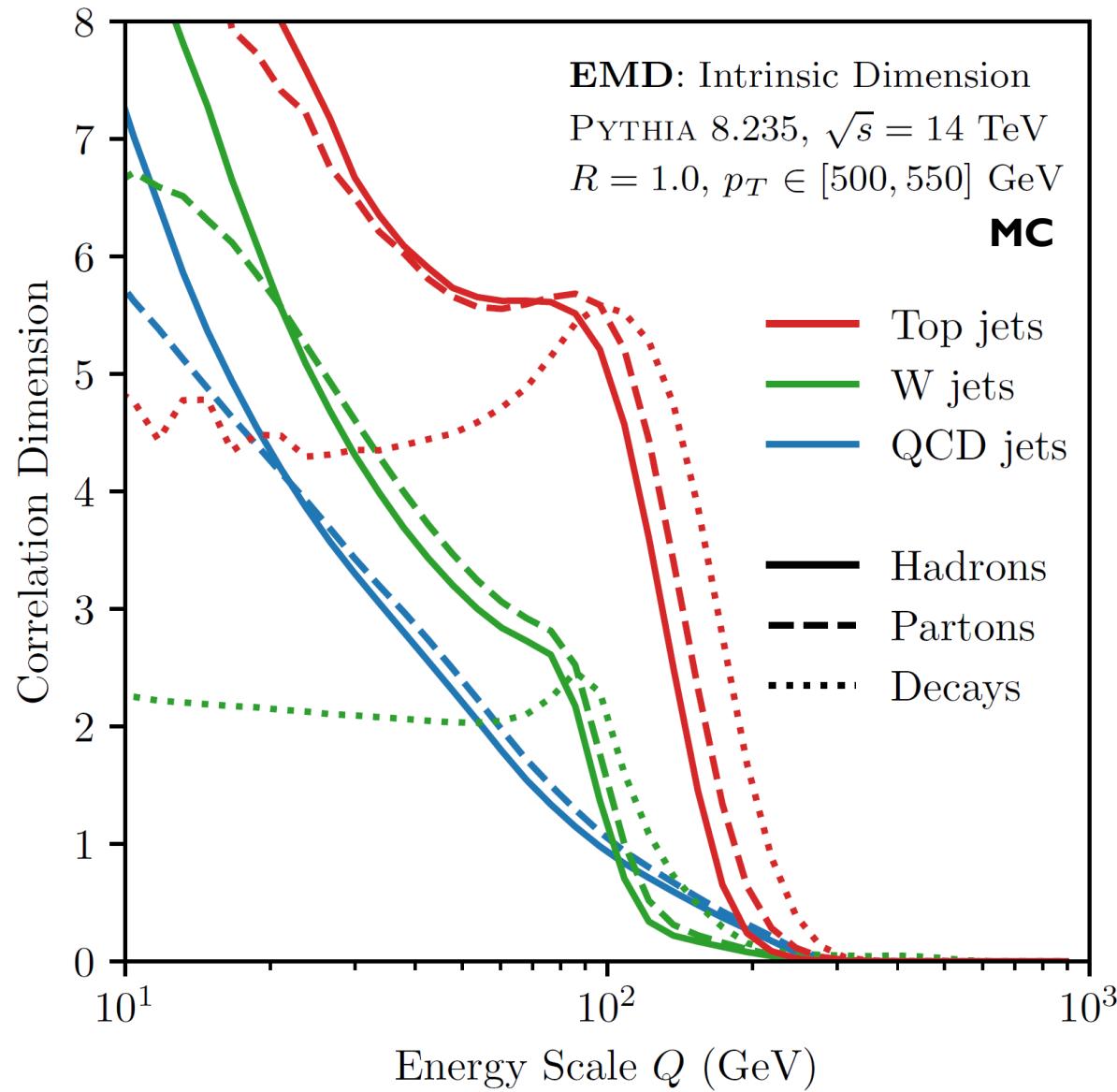
W jets are more complicated.

Top jets are most complex.

“Decays” have ~constant dimension.

Fragmentation becomes more complex at lower energy scales.

Exploring the Space of Jets: Correlation Dimension



QCD jets are simplest.

W jets are more complicated.

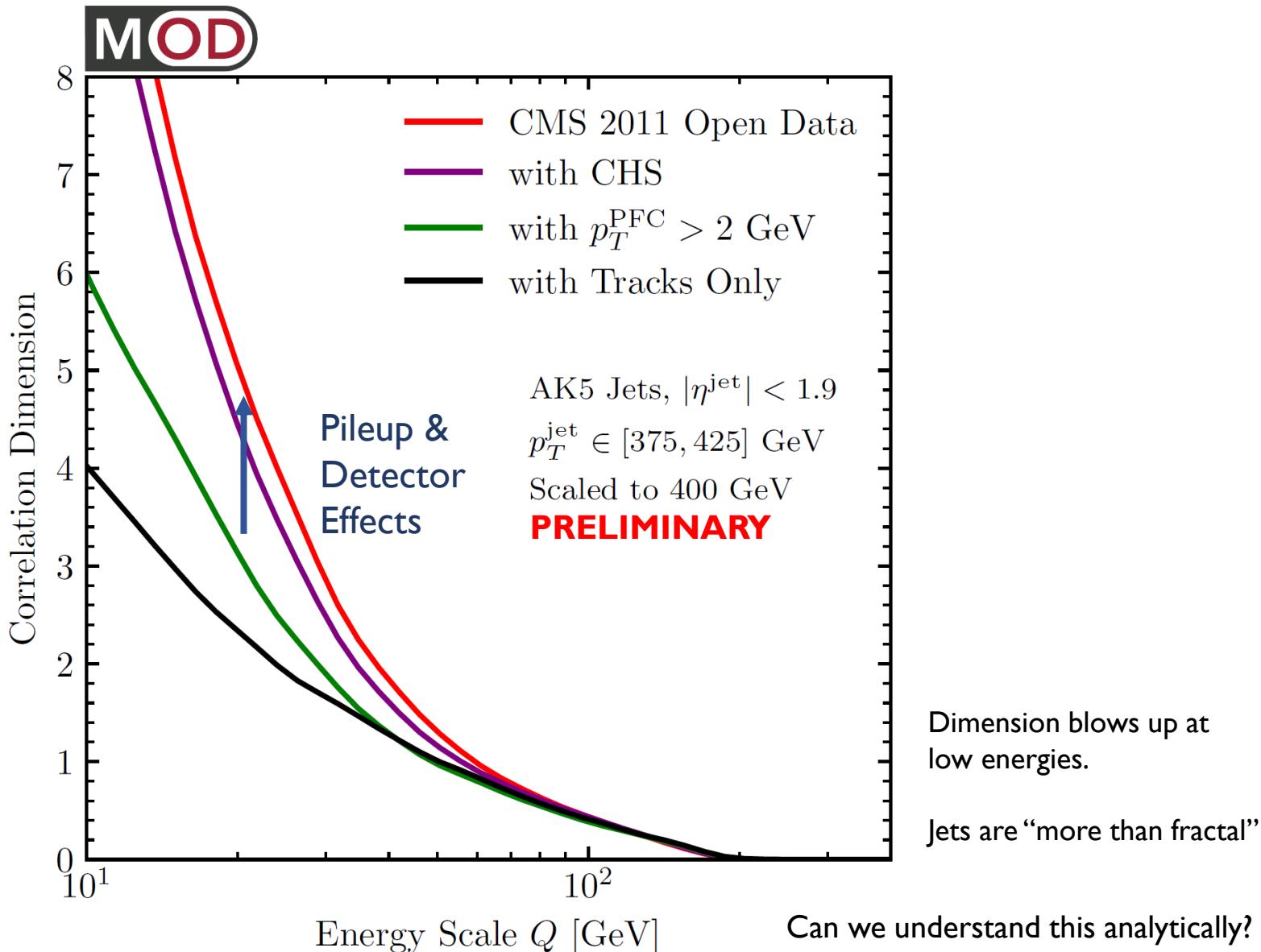
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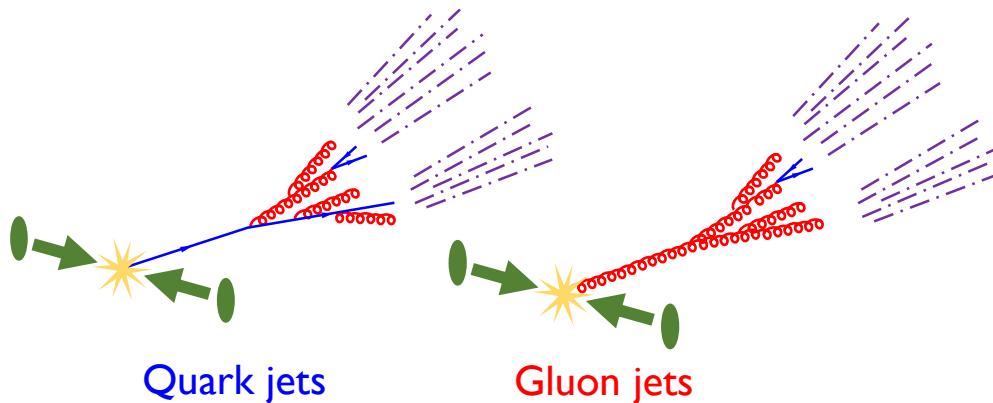
Fragmentation becomes more complex at lower energy scales.

Hadronization becomes relevant at scales around 20 GeV.

Exploring the Space of Jets: Correlation Dimension



Exploring the Space of Jets: Correlation Dimension

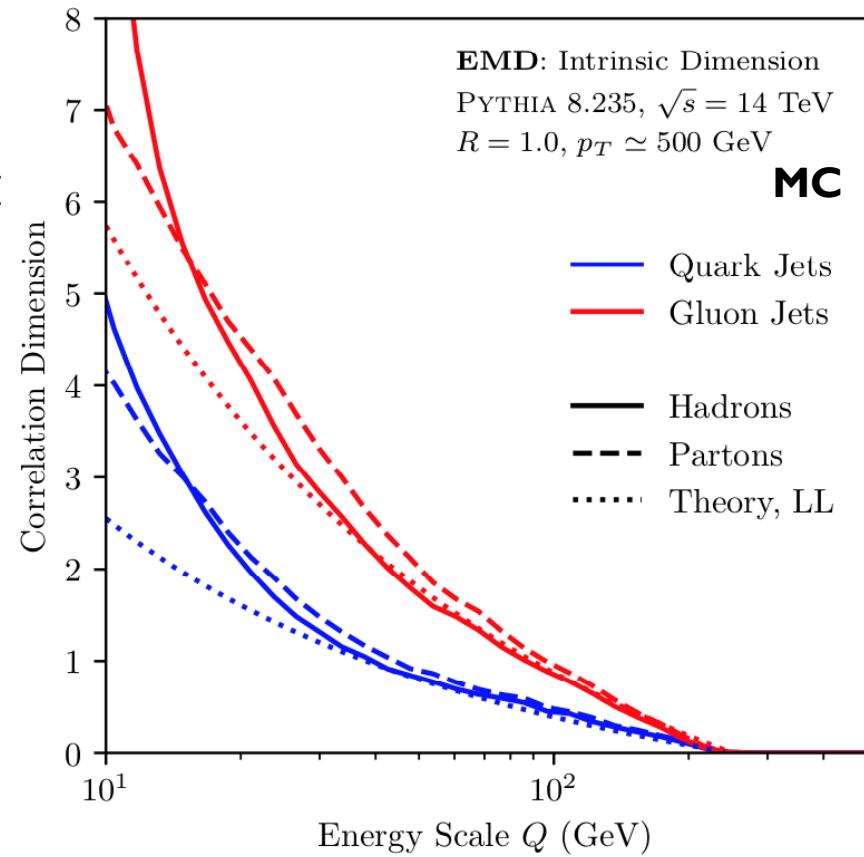


$$\text{At LL: } \dim_{q/g}(Q) = -\frac{8\alpha_s C_{q/g}}{\pi} \ln \frac{Q}{p_T/2}$$

$$+ \text{1-loop running of } \alpha_s$$

$$C_q = C_F = \frac{4}{3}$$

$$C_g = C_A = 3$$

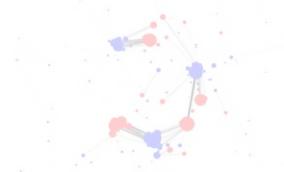
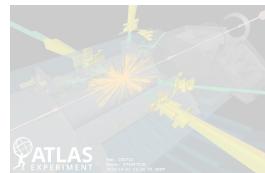


Dimension blows up at low energies.

Jets are “more than fractal”

Outline

Part I Introduction



When are two jets similar?

When they have similar distributions of energy

The Energy Mover's Distance

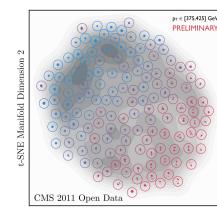
Work to rearrange one event into another.

Movie Time

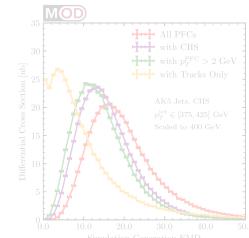
Visualize energy movement and jet formation.

Jets in CMS Open Data

A great resource for physics exploration



Part II Application



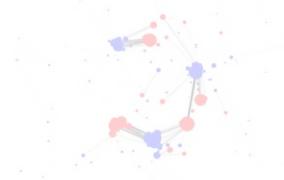
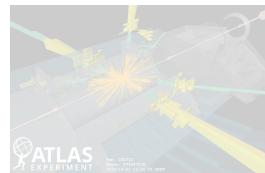
Exploring the Space of Jets

New ways to visualize and probe collider data

Quantifying Detector Effects

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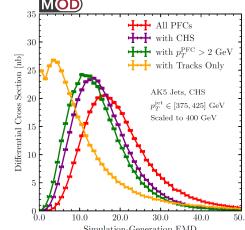
A great resource for physics exploration



Exploring the Space of Jets

New ways to visualize and probe collider data

Quantifying Detector Effects



EMD and IRC-Safe Observables

Events close in EMD are close in any infrared and collinear safe observable!

Additive IRC-safe observables: $\mathcal{O}(\mathcal{E}) = \sum_{i=1}^M \textcolor{red}{E}_i \Phi(\hat{n}_i)$

Energy Mover's Distance

$$\text{EMD}(\mathcal{E}, \mathcal{E}') \geq \frac{1}{RL} |\mathcal{O}(\mathcal{E}) - \mathcal{O}(\mathcal{E}')|$$

Difference in observable values

“Lipschitz constant” of Φ
i.e. bound on its derivative

e.g. jet angularities:

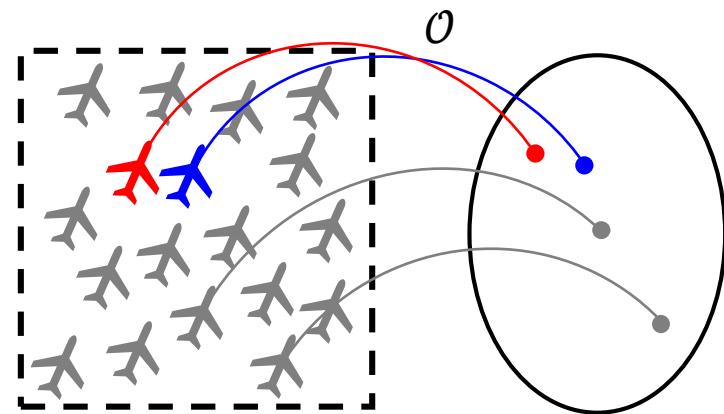
[\[C. Berger, T. Kucs, and G. Sterman, 0303051\]](#)

[\[A. Larkoski, J. Thaler, and W. Waalewijn, 1408.3122\]](#)

For $\beta \geq 1$ jet angularities:

$$|\lambda^{(\beta)}(\mathcal{E}) - \lambda^{(\beta)}(\mathcal{E}')| \leq \beta \text{ EMD}(\mathcal{E}, \mathcal{E}')$$

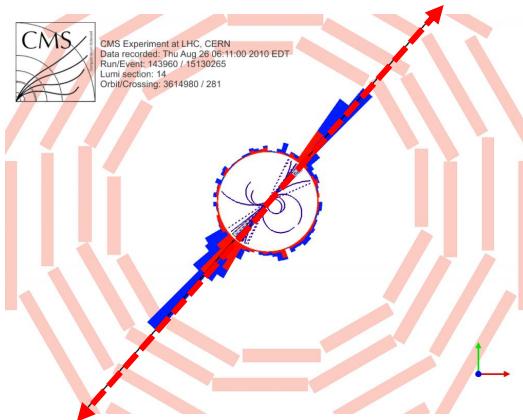
$$\lambda^{(\beta)} = \sum_{i=1}^M \textcolor{red}{E}_i \theta_i^\beta$$



Old Observables in a New Language

Thrust is the EMD between the event and two back-to-back particles.

$$t(\mathcal{E}) = E - \max_{\hat{\mathbf{n}}} \sum_i |\vec{p}_i \cdot \hat{\mathbf{n}}|$$

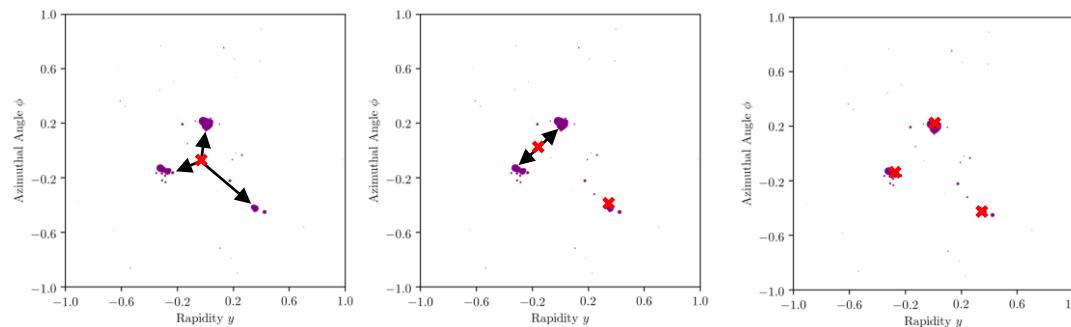


$$t(\mathcal{E}) = \min_{|\mathcal{E}'|=2} \text{EMD}(\mathcal{E}, \mathcal{E}')$$

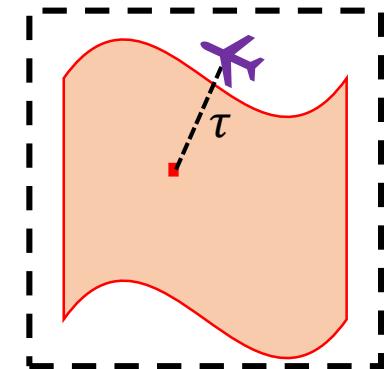
$$\text{with } \theta_{ij} = \hat{p}_i \cdot \hat{p}_j, \quad \hat{p} = \vec{p}/E$$

N-(sub)jettiness is the EMD between the event and the closest N-particle event.

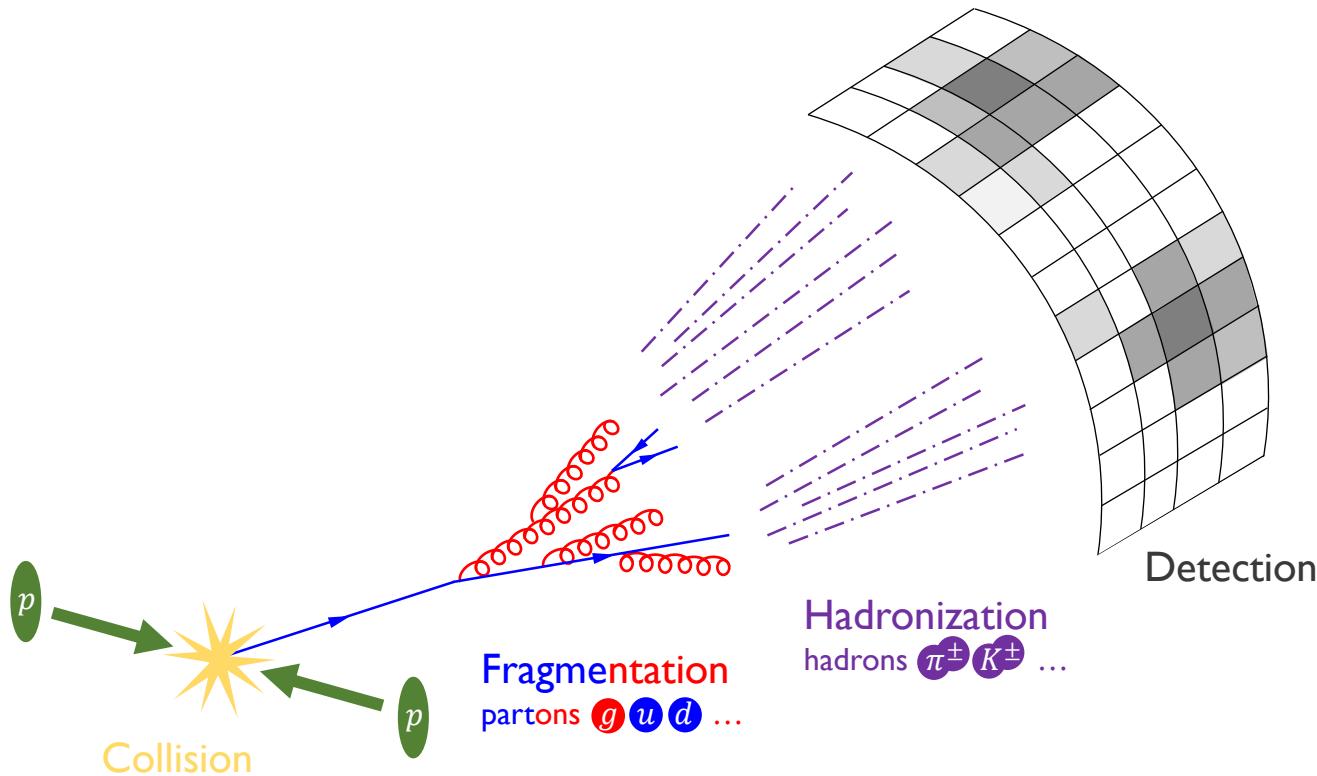
$$\tau_N^{(\beta)}(\mathcal{E}) = \min_{N \text{ axes}} \sum_{i=1}^M E_i \min_k \{\theta_{1,k}^\beta, \theta_{2,k}^\beta, \dots, \theta_{N,k}^\beta\} \longrightarrow \tau_N(\mathcal{E}) = \min_{|\mathcal{E}'|=N} \text{EMD}(\mathcal{E}, \mathcal{E}').$$



$\beta \geq 1$ is p-Wasserstein distance with $p = \beta$.

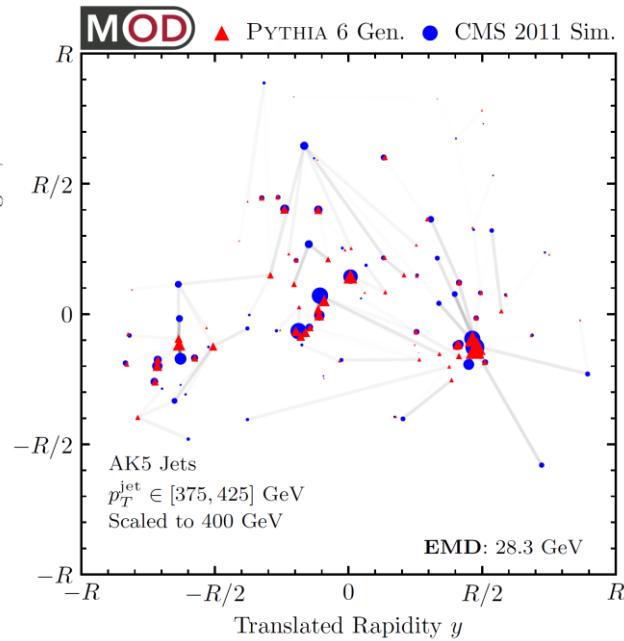


Quantifying Detector Effects

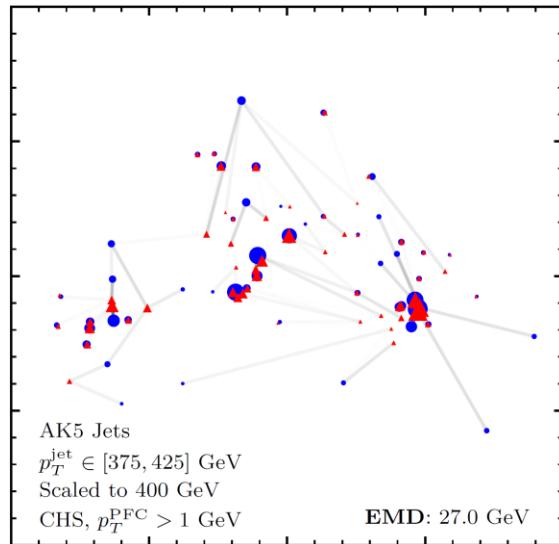


Quantifying Detector Effects with EMD

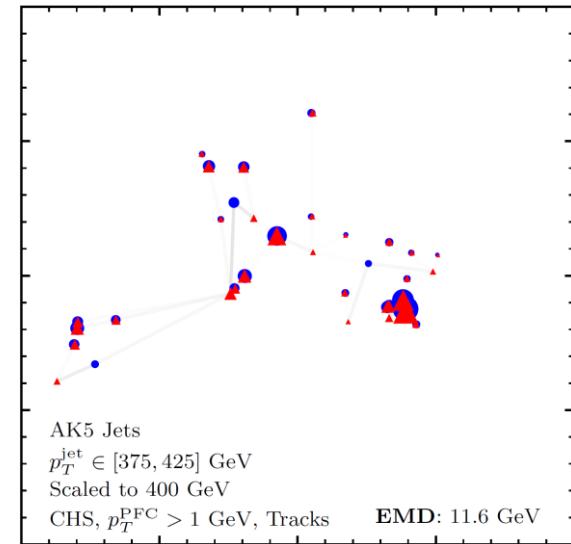
Gen./Sim. EMD: 28.3 GeV



Gen./Sim. EMD: 27.0 GeV



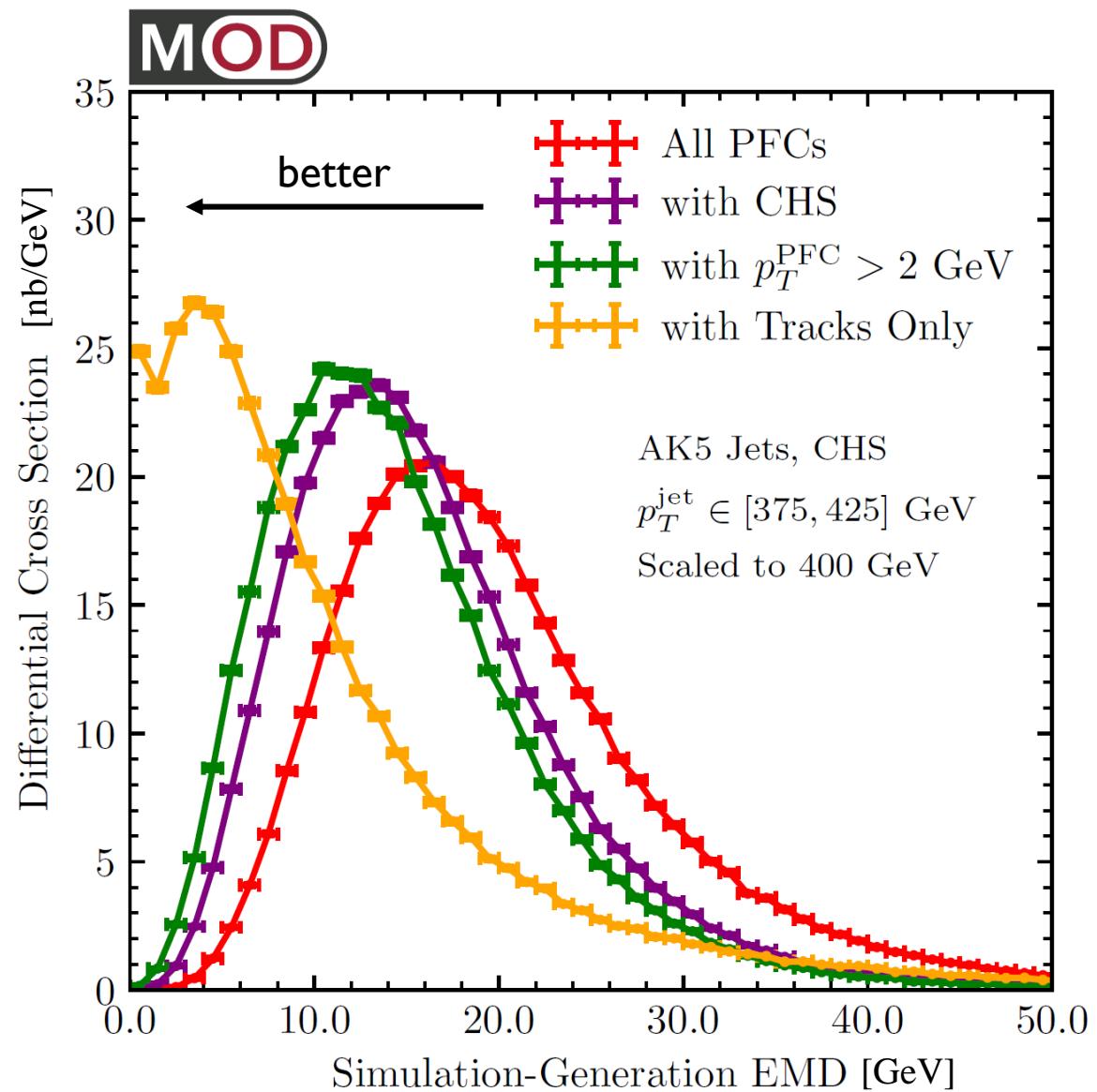
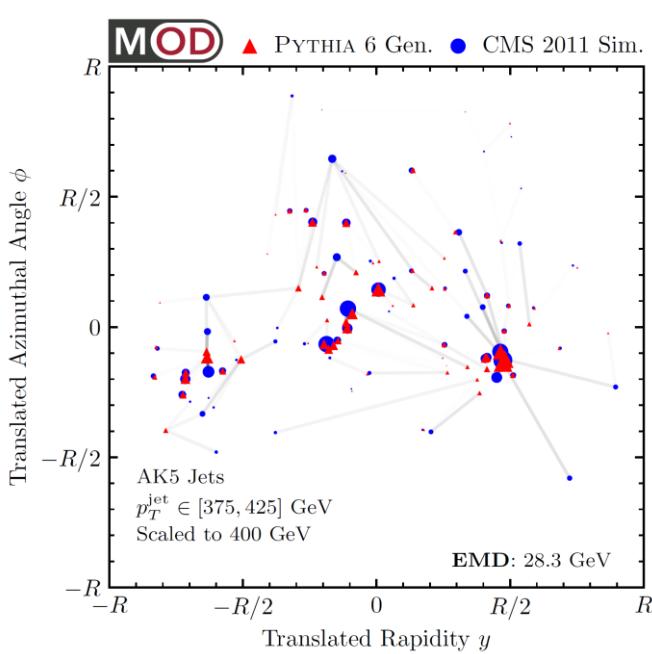
Gen./Sim. EMD: 11.6 GeV



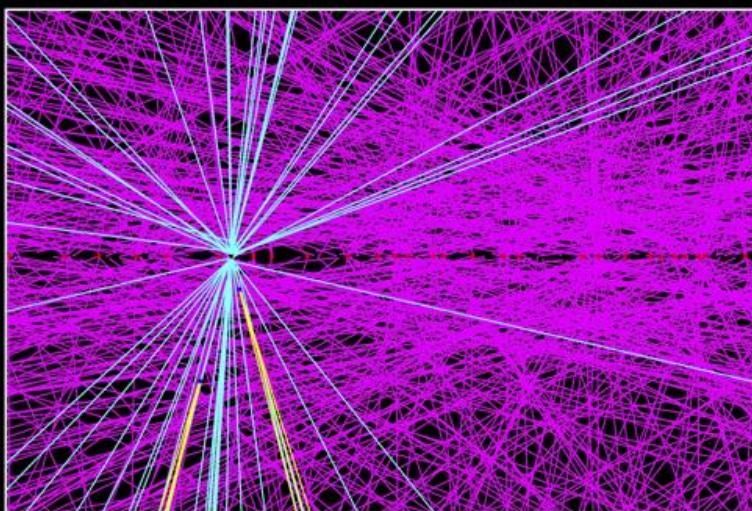
+ charged hadron subtraction
+ $p_T^{\text{PFC}} > 1$ GeV cut

Tracks only

Quantifying Detector Effects with EMD



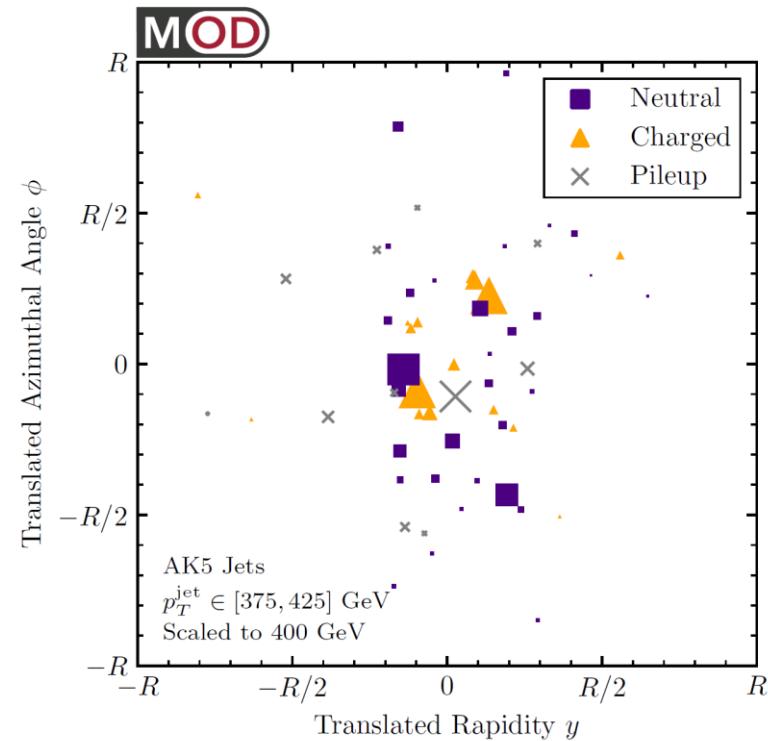
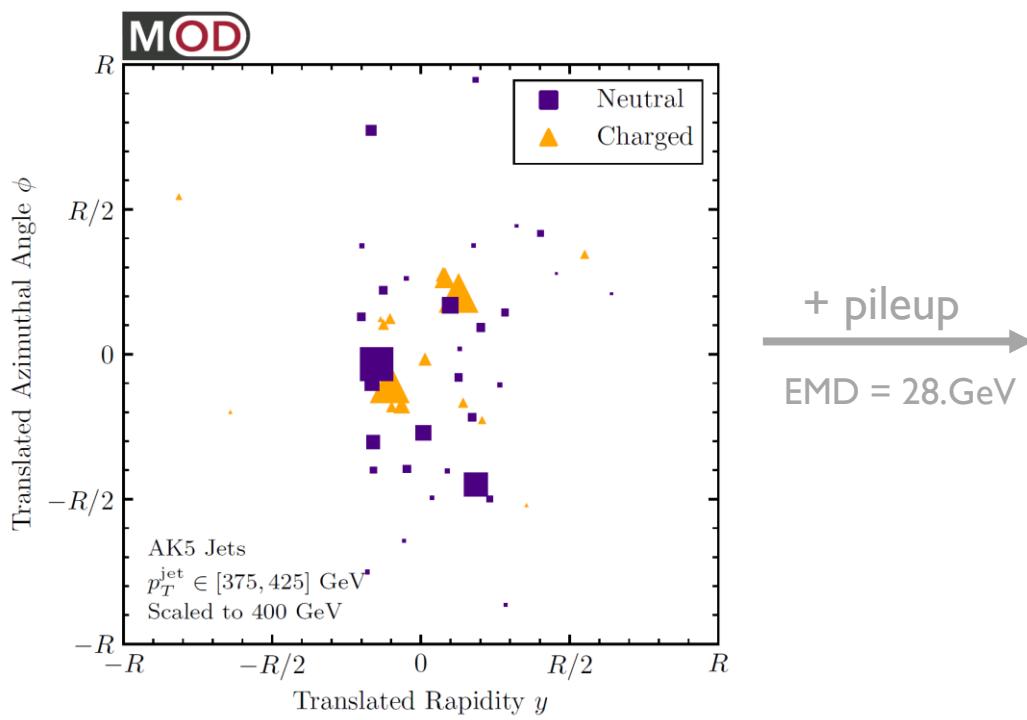
Quantifying event modifications: Pileup



Pileup Mitigation

Can use vertex information in CMS Open Data to find charged pileup particles.

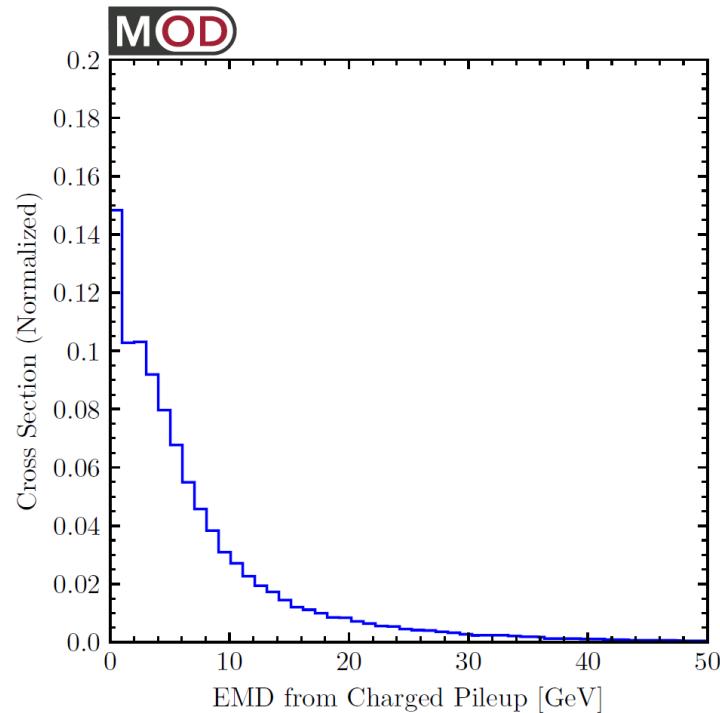
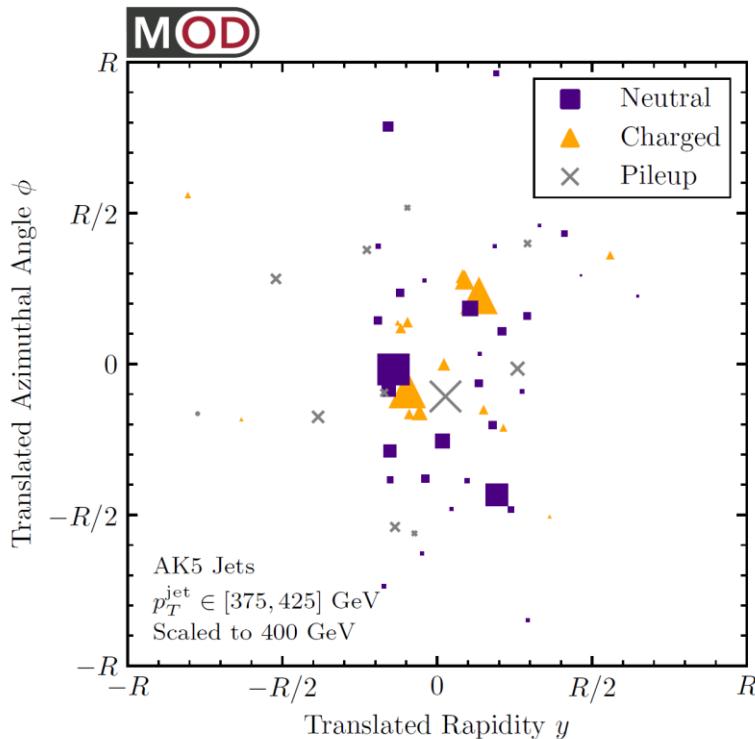
Allows us to study the effect of pileup on radiation pattern and observables.



Pileup Mitigation

Can use vertex information in CMS Open Data to find charged pileup particles.

Allows us to study the effect of pileup on radiation pattern and observables.



Quantify pileup mitigation performance with EMD (more in backup).

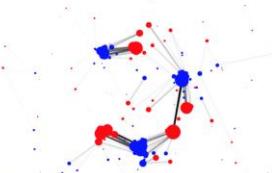
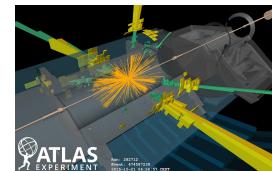
Optimize machine learning-based pileup mitigation methods to minimize EMD?

[\[Komiske, EMM, Nachman, Schwartz, 1707.08600\]](#)

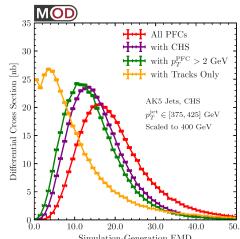
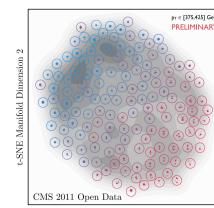
[\[Martinez, Cerri, Pierini, Spiropulu, Vlimant, 1810.07988\]](#)

Outline

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Part II Application



When are two jets similar?

When they have similar distributions of energy

The Energy Mover's Distance

Work to rearrange one event into another.

Movie Time

Visualize energy movement and jet formation.

Jets in CMS Open Data

A great resource for physics exploration

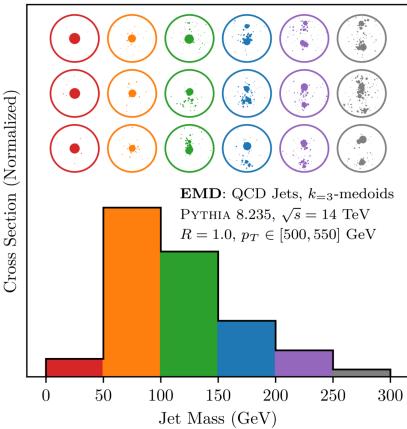
Exploring the Space of Jets

New ways to visualize and probe collider data

Quantifying Detector Effects

Robust bounds for pileup and detector effects

Going Beyond



Clustering sets of events

New observables through EMD geometry

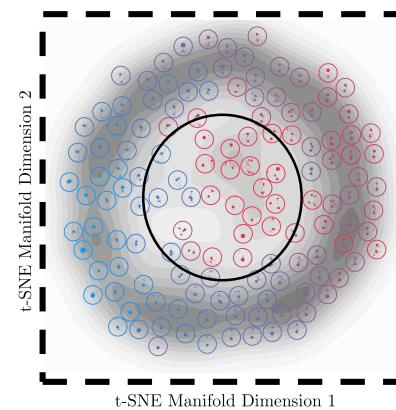
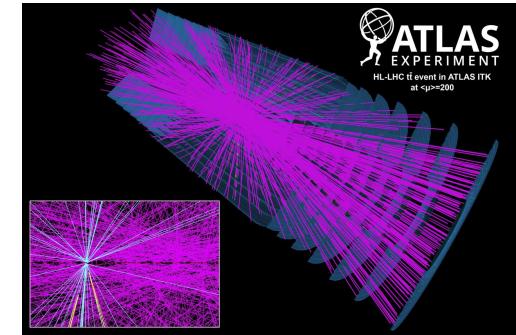
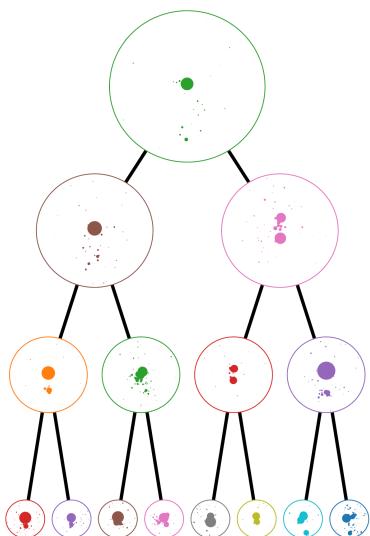
EMD for density estimation

“Event” mover’s distance between ensembles?

Model (in)dependent anomaly detection?

Train ML models to optimize EMD directly?

Include flavor information?



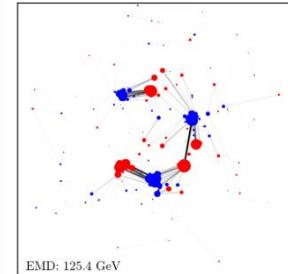
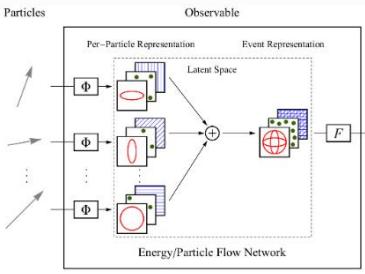
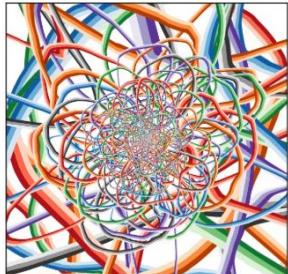
EnergyFlow

<https://energyflow.network>

pip install energyflow

Docs » Home

Welcome to EnergyFlow

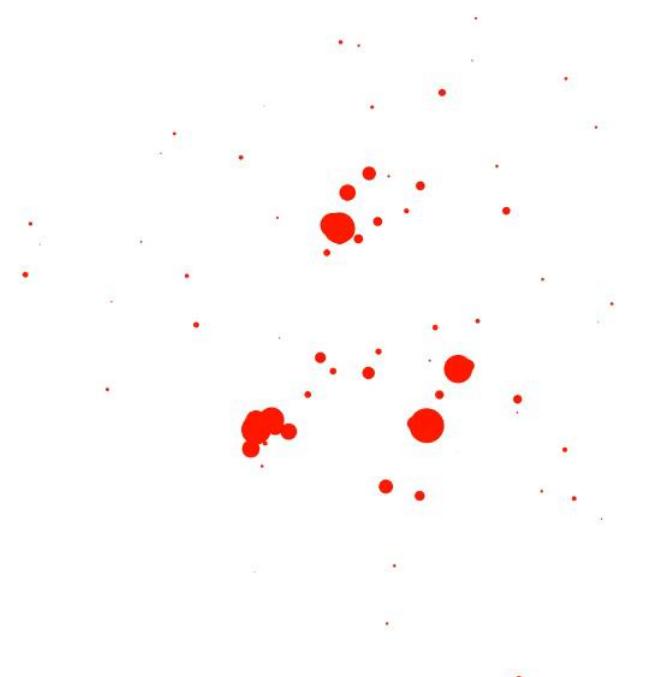


EnergyFlow is a Python package containing a suite of particle physics tools. Originally designed to compute Energy Flow Polynomials (EFPs), as of version [0.10.0](#) the package expanded to include implementations of Energy Flow Networks (EFNs) and Particle Flow Networks (PFNs). As of version [0.11.0](#), functions for facilitating the computation of the Energy Mover's Distance (EMD) on particle physics events are included. To summarize the main features:

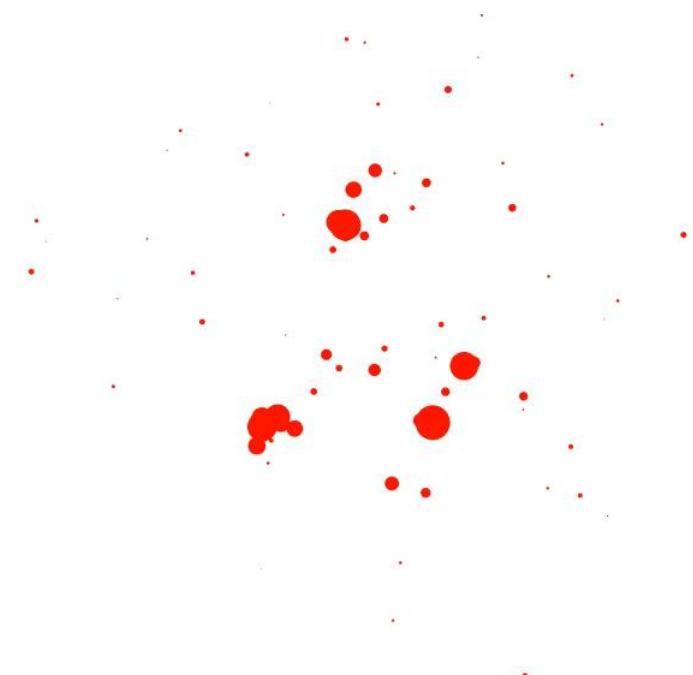
- **Energy Flow Polynomials:** EFPs are a collection of jet substructure observables which form a complete linear basis of IRC-safe observables. EnergyFlow provides tools to compute EFPs on events for several energy and angular measures as well as custom measures.
- **Energy Flow Networks:** EFNs are infrared- and collinear-safe models designed for learning from collider events as unordered, variable-length sets of particles. EnergyFlow contains customizable Keras implementations of EFNs.
- **Particle Flow Networks:** PFNs are general models designed for learning from collider events as

The End

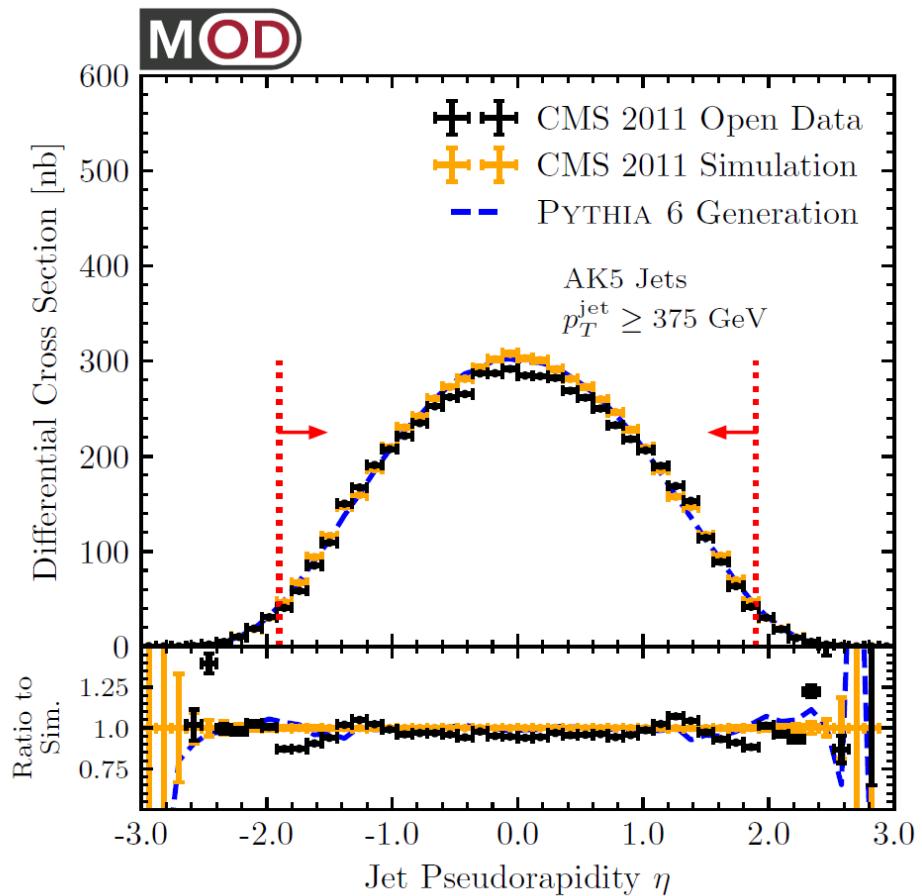
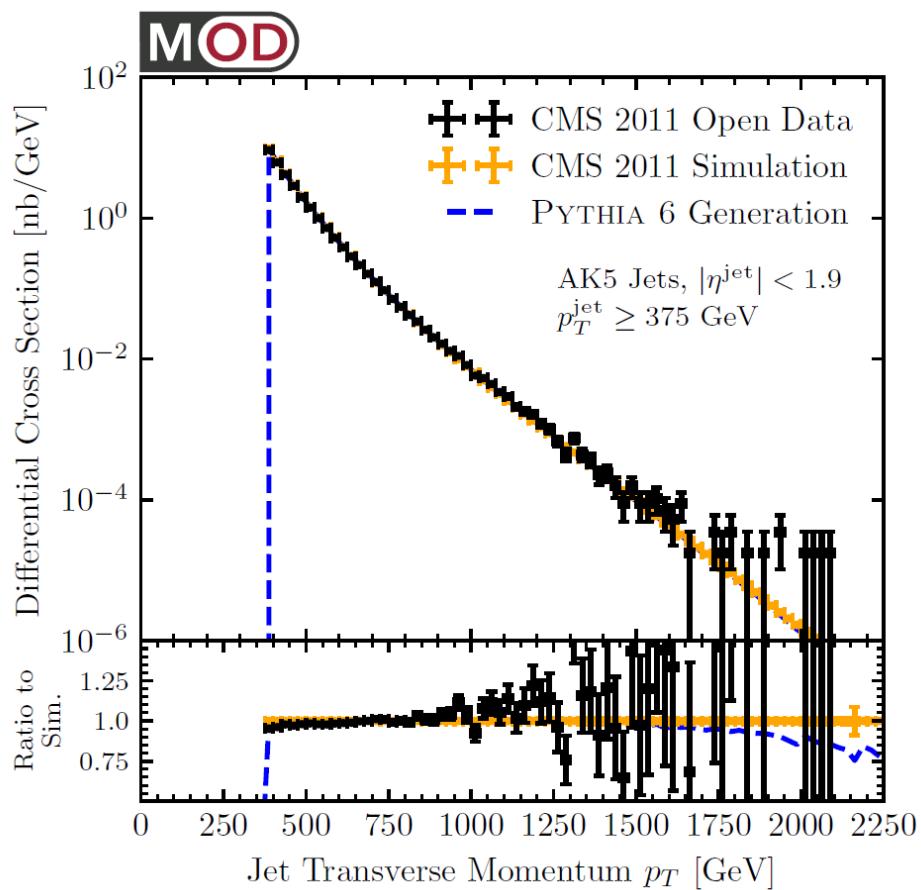
Thank you!



Extra Slides

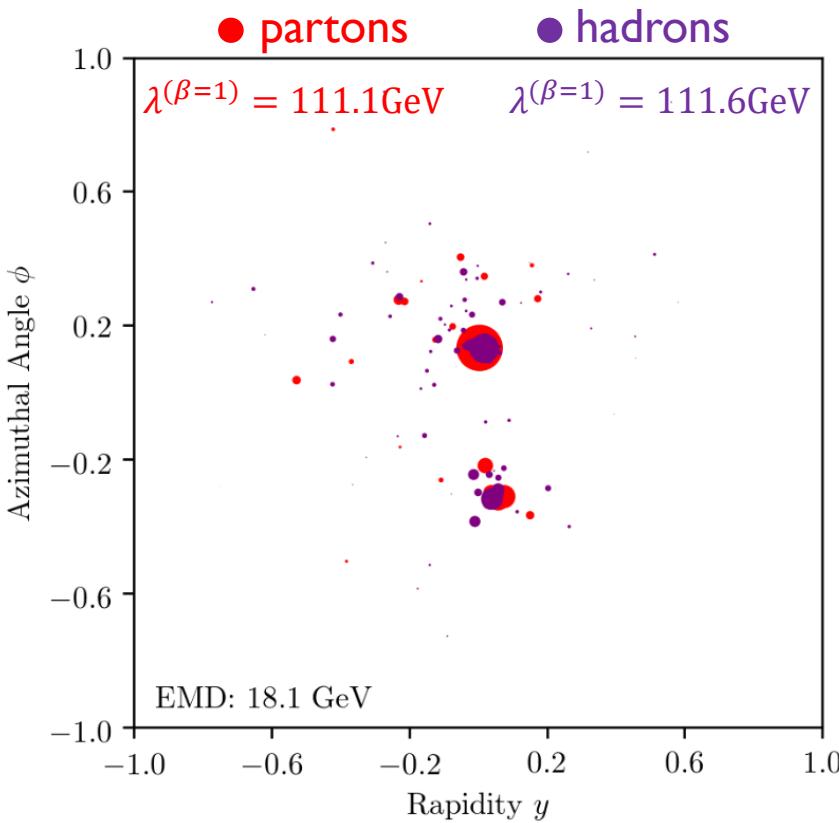


Jet Kinematic Distributions



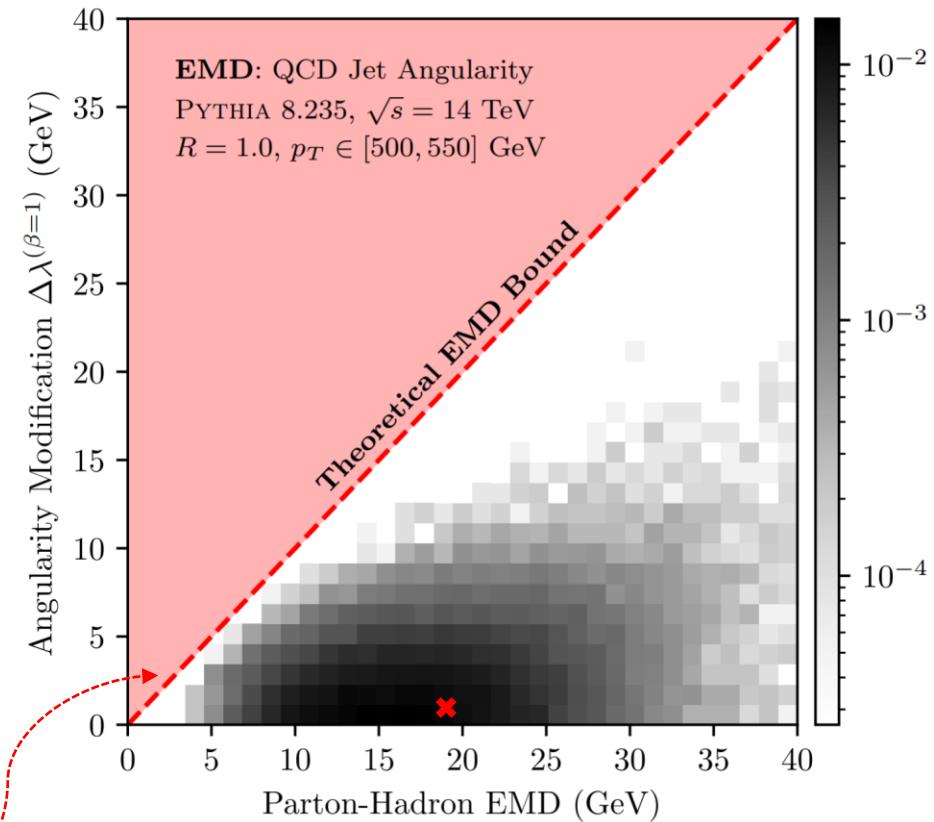
Quantifying event modifications: Hadronization

$$\lambda^{(\beta=1)} = \sum_{i=1}^M E_i \theta_i$$

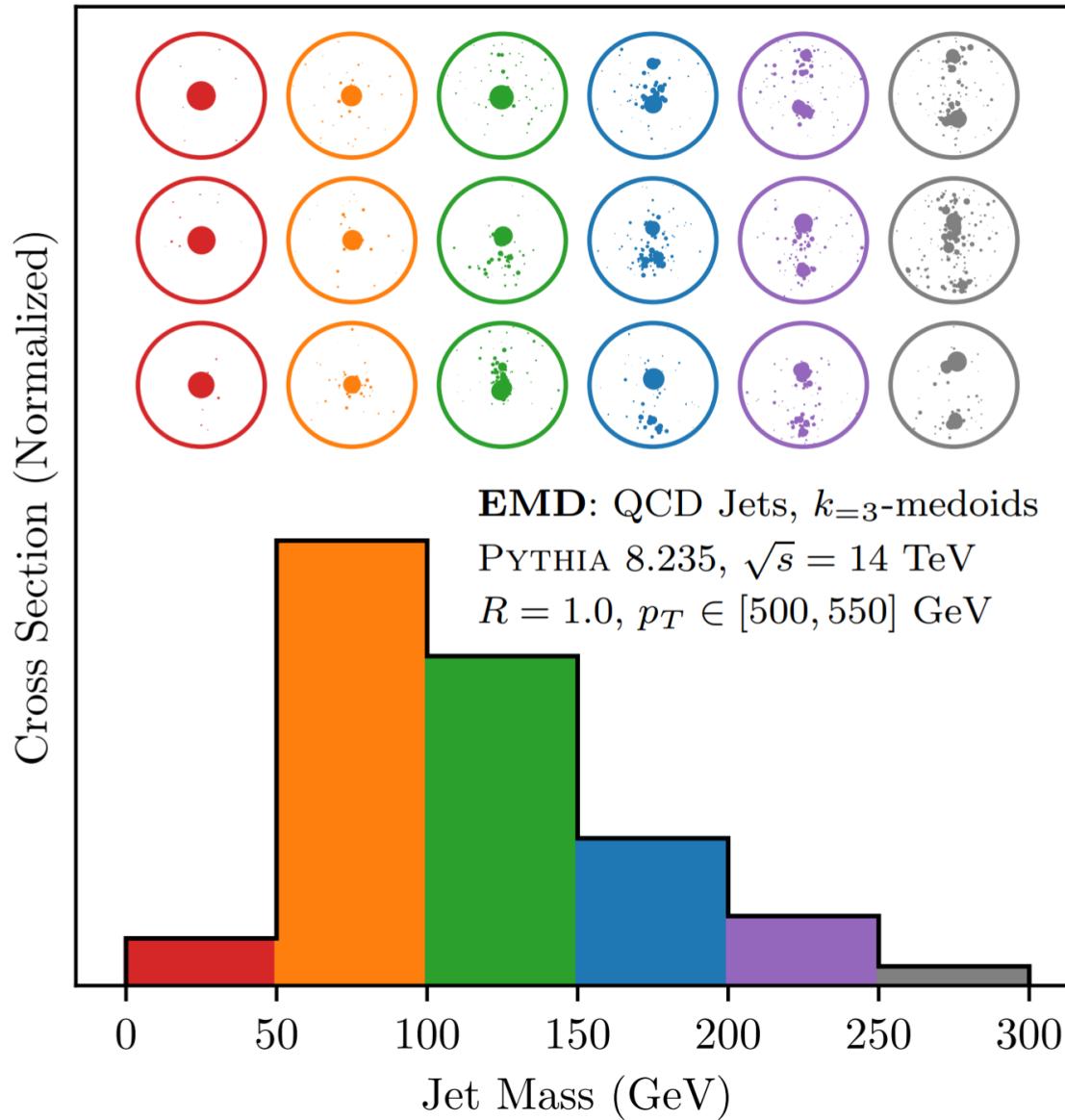


$$\begin{aligned}\mathcal{E} &= \mathcal{E}_{\text{partons}} \\ \mathcal{E}' &= \mathcal{E}_{\text{hadrons}}\end{aligned}$$

$$|\lambda^{(\beta=1)}(\mathcal{E}) - \lambda^{(\beta=1)}(\mathcal{E}')| \leq \text{EMD}(\mathcal{E}, \mathcal{E}')$$

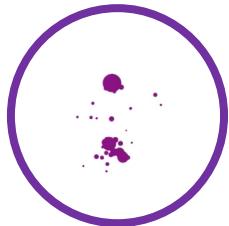


Exploring the Space of Events: k -medoids



Exploring the Space of Events: Jet Classification

Classify **W jets** vs. **QCD jets**



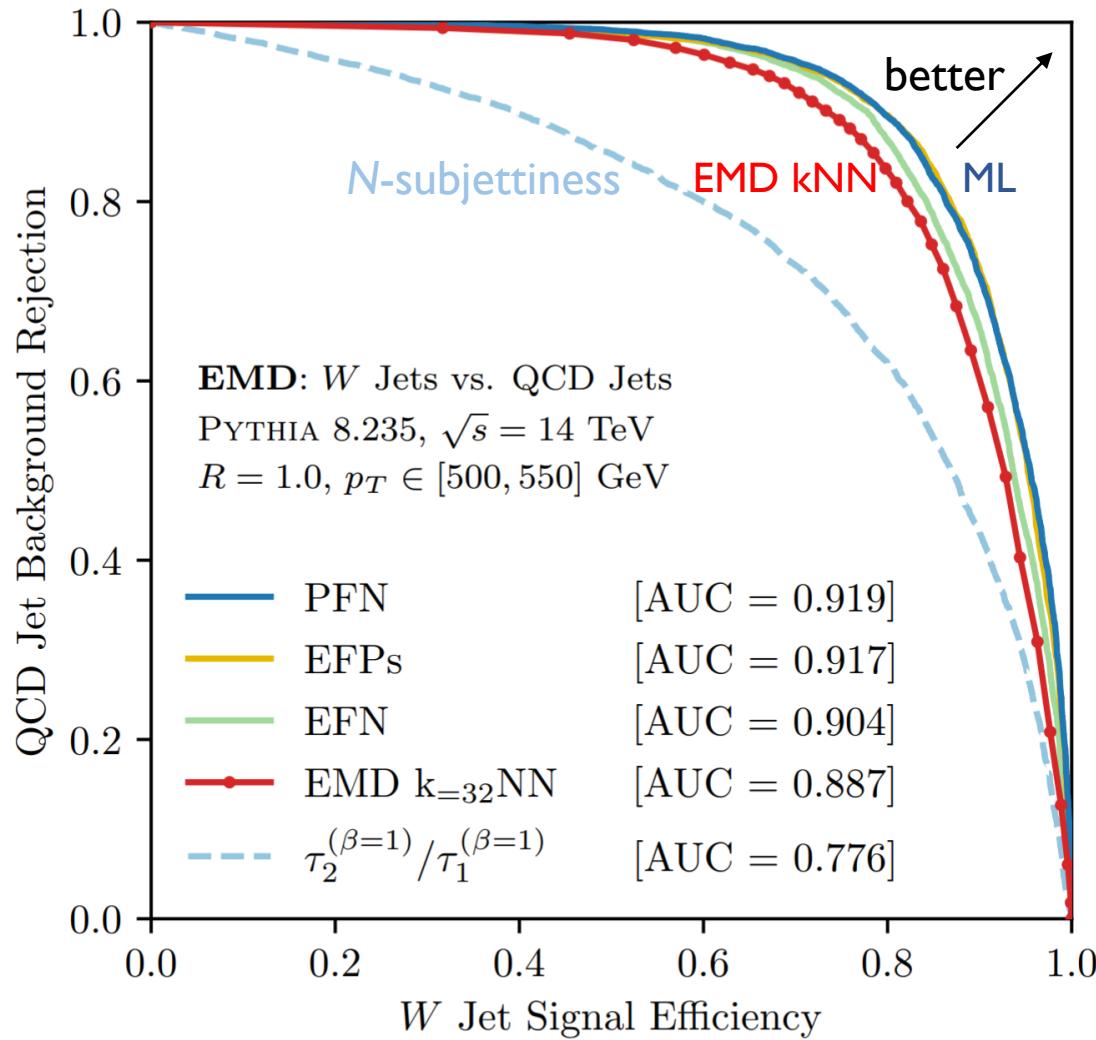
vs.



Look at a jet's nearest neighbors (kNN) to predict its class.

Optimal IRC-safe classifier with enough data.

Nearing performance of ML.



Exploring the Space of Events

Use EMD as a measure of event similarity

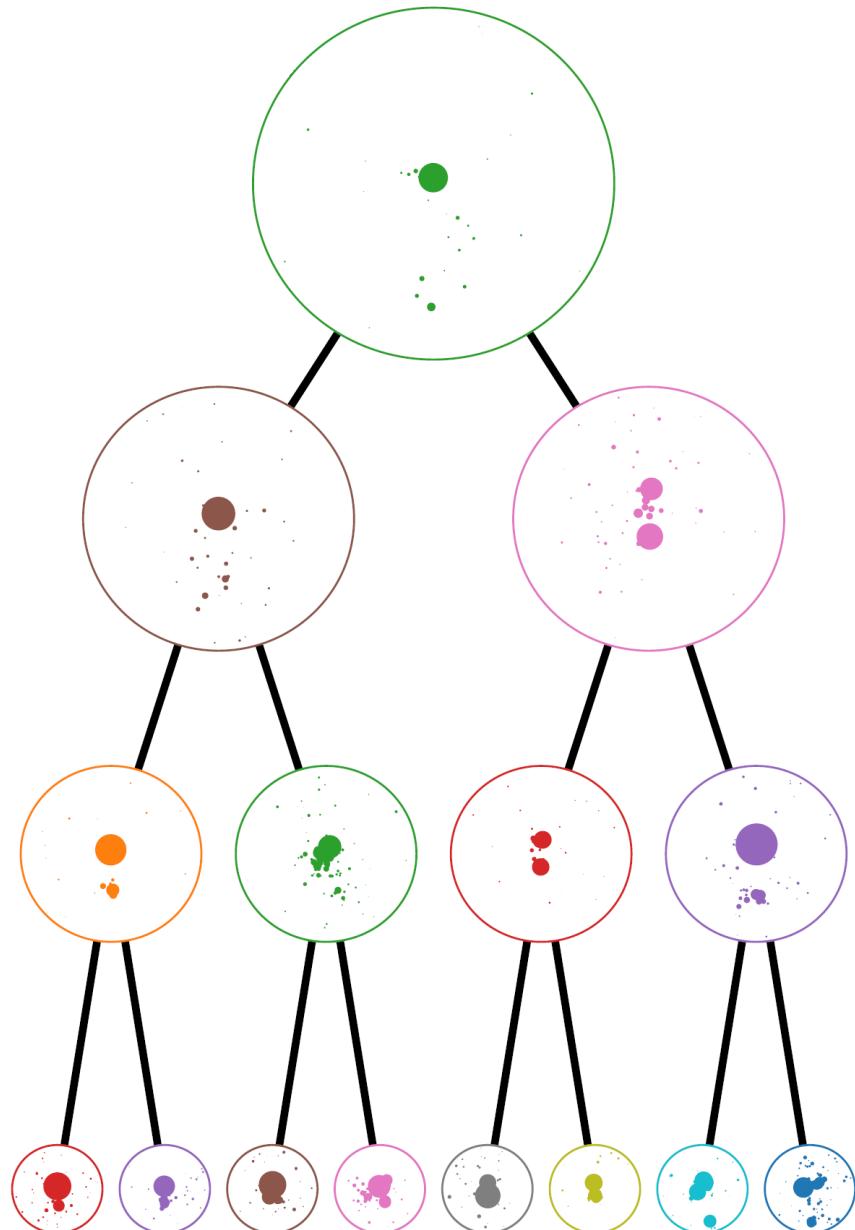
Unsupervised clustering algorithms can
be used to cluster events

Jets are clusters of particles
???? are clusters of jets

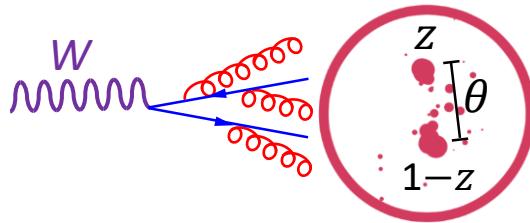
VP Tree: $O(\log(N))$ neighbor query time

Much more to explore.

Vantage Point (VP) Tree



Exploring the Space of Events: W jets



W jets are 2-pronged:

z : Energy Sharing of Prongs

θ : Angle between Prongs

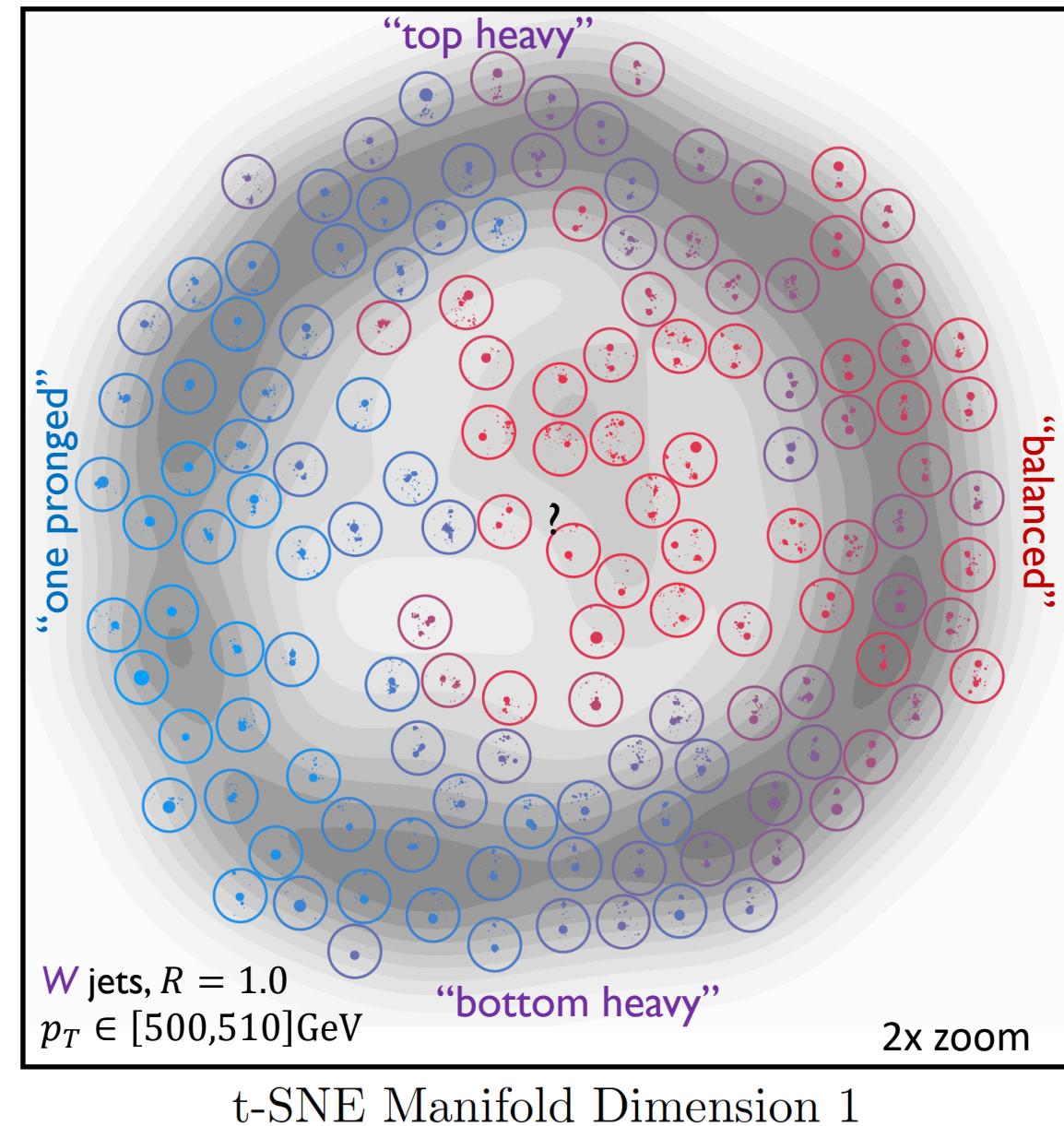
φ : Azimuthal orientation

Constrained by W mass:

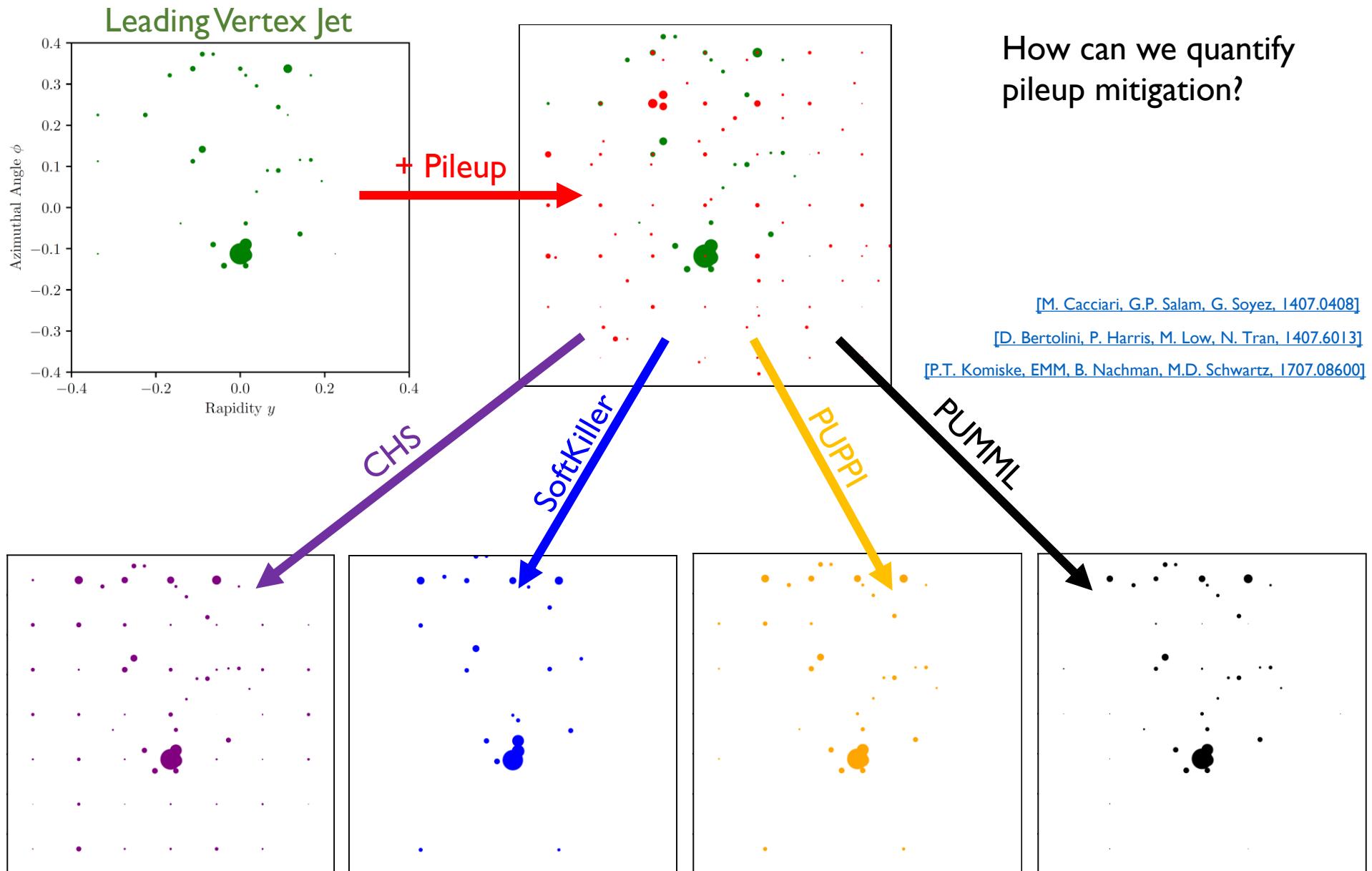
$$z(1-z)\theta^2 = \frac{p_{\mu J}^2}{p_T^2} = \frac{m_W^2}{p_T^2}$$

Hence we expect a **two-dimensional** space of W jets.

After φ rotation: **one-dimensional**

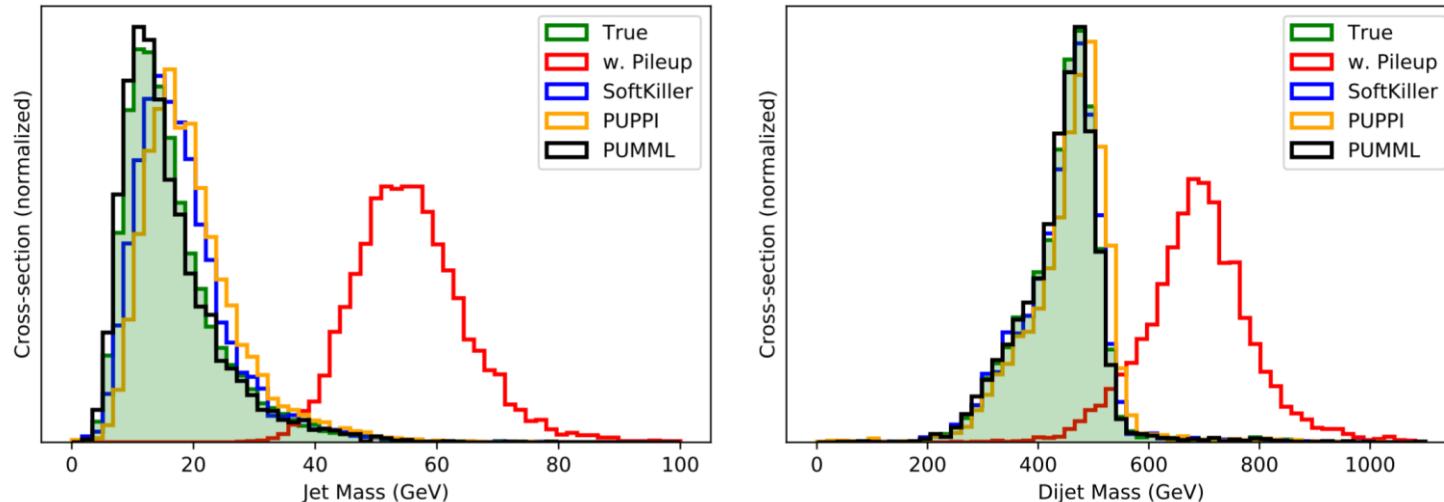


Quantifying event modifications: Pileup



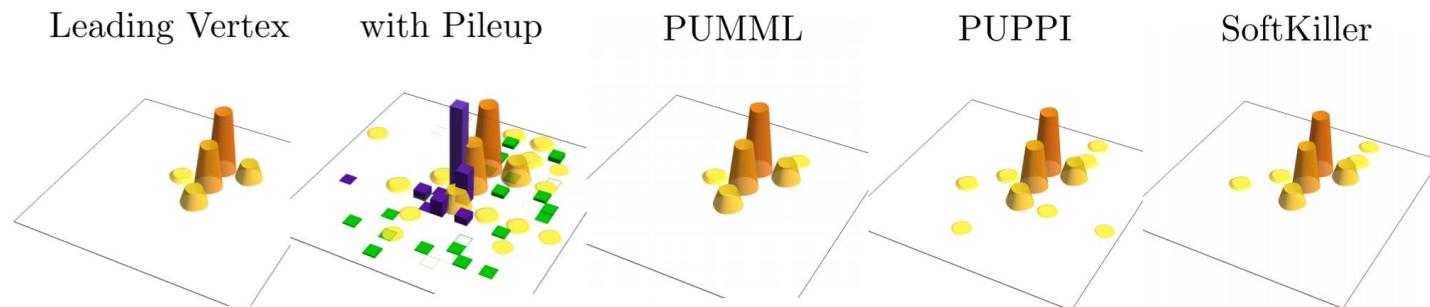
Quantifying event modifications: Pileup

Compare on a collection of observables?



Requires ad hoc choices of observables.

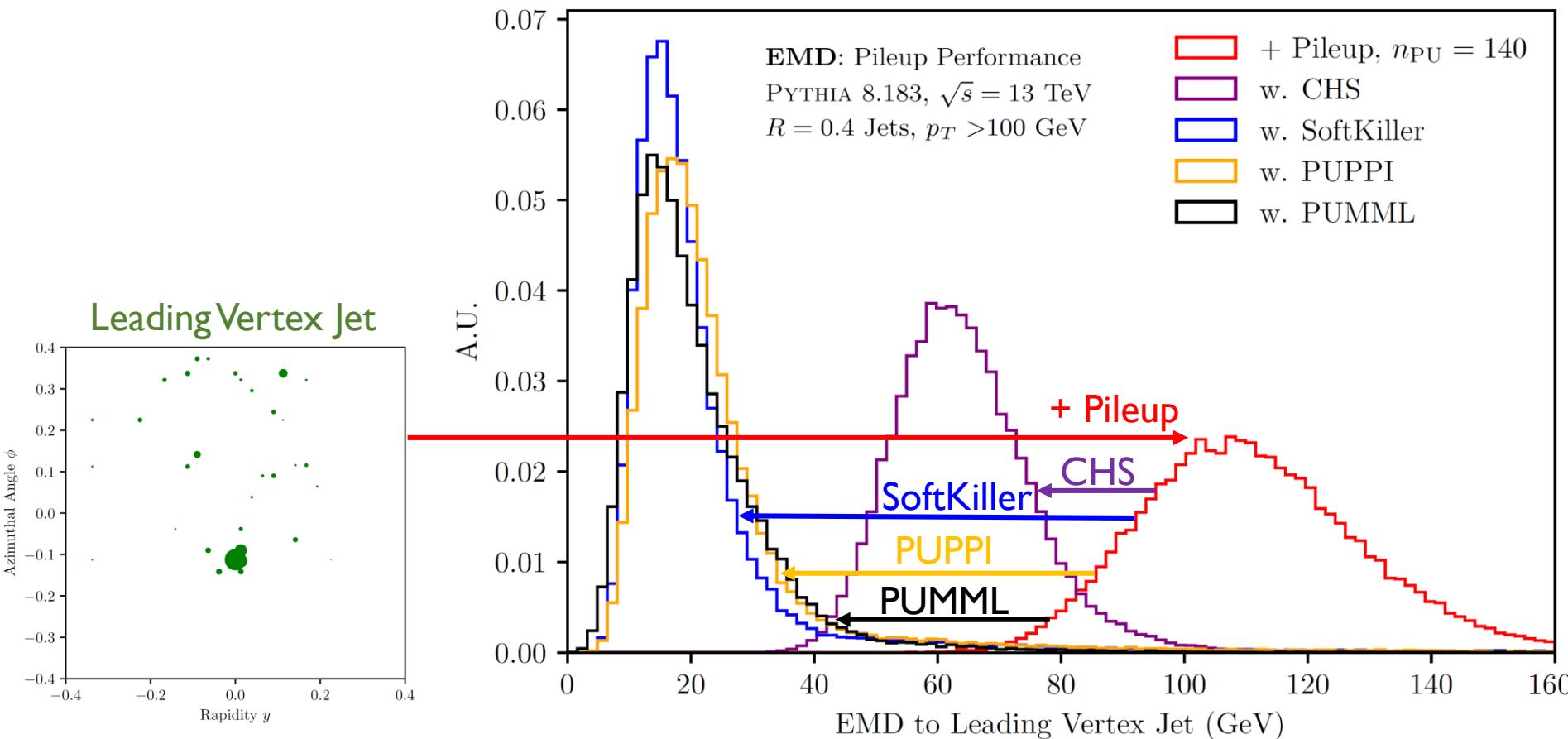
Compare calorimeter images pixel by pixel?



Discontinuous under physically-sensible single-pixel perturbations.
Undesirable behavior with increasing resolution.

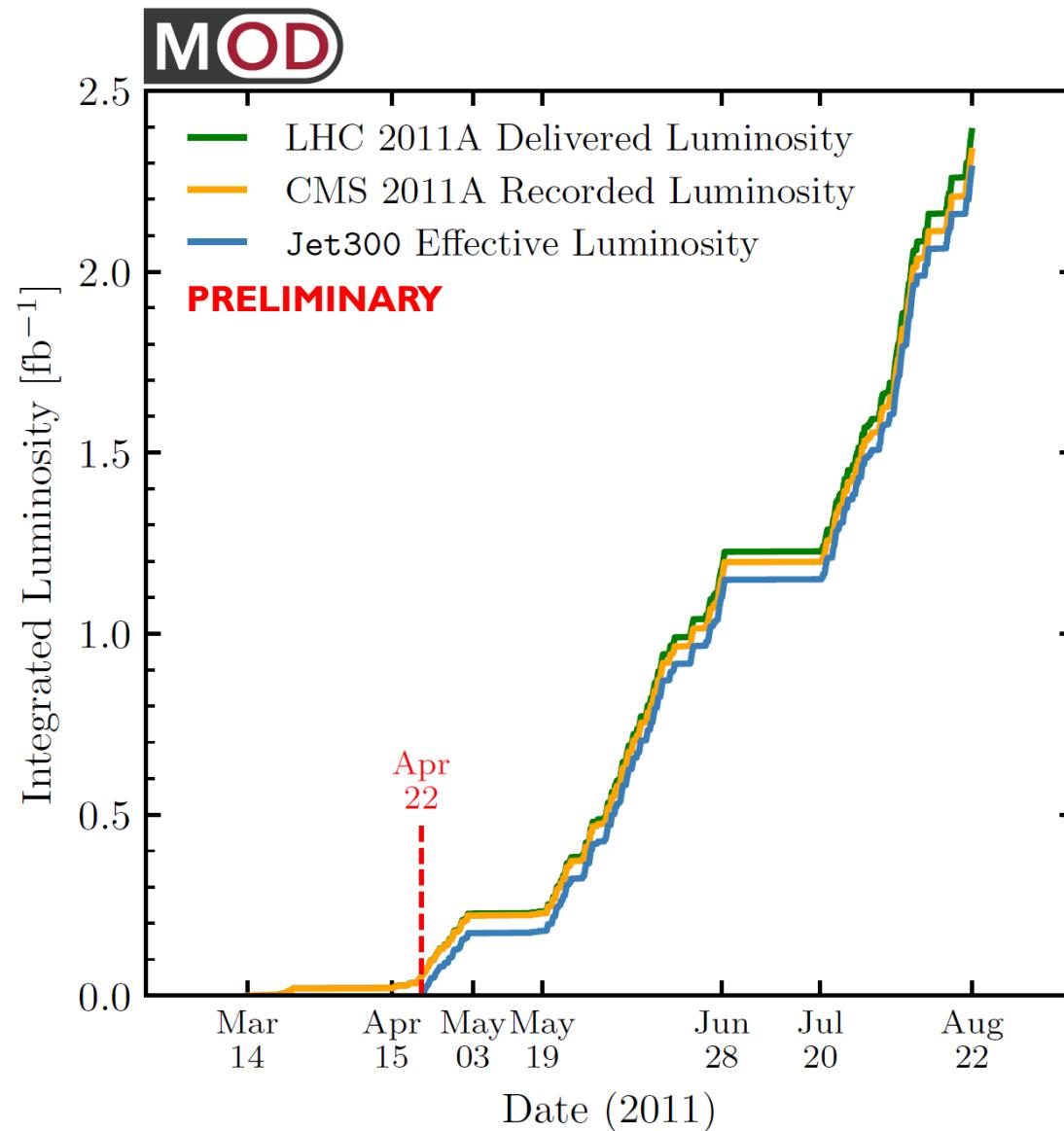
Quantifying event modifications: Pileup

Measure pileup mitigation performance with EMD!



Guarantees performance on IRC safe observables.
Stable under physically-sensible perturbations.
Train to optimize EMD with machine learning?

Integrated Luminosity



Exploring the Space of Jets: Correlation Dimension

Sketch of leading log (one emission) calculation:

$$\dim_{q/g}(Q) = Q \frac{\partial}{\partial Q} \ln \sum_{i=1}^N \sum_{j=1}^N \Theta[\text{EMD}(\varepsilon_i, \varepsilon_j) < Q]$$

$$= Q \frac{\partial}{\partial Q} \ln \Pr [\text{EMD} < Q]$$

$$= Q \frac{\partial}{\partial Q} \ln \Pr [\lambda^{(\beta=1)} < Q; C_{q/g} \rightarrow 2 C_{q/g}]$$

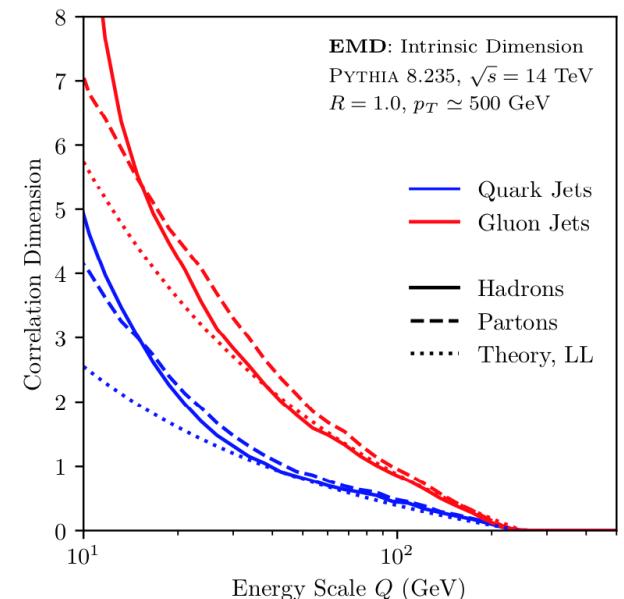
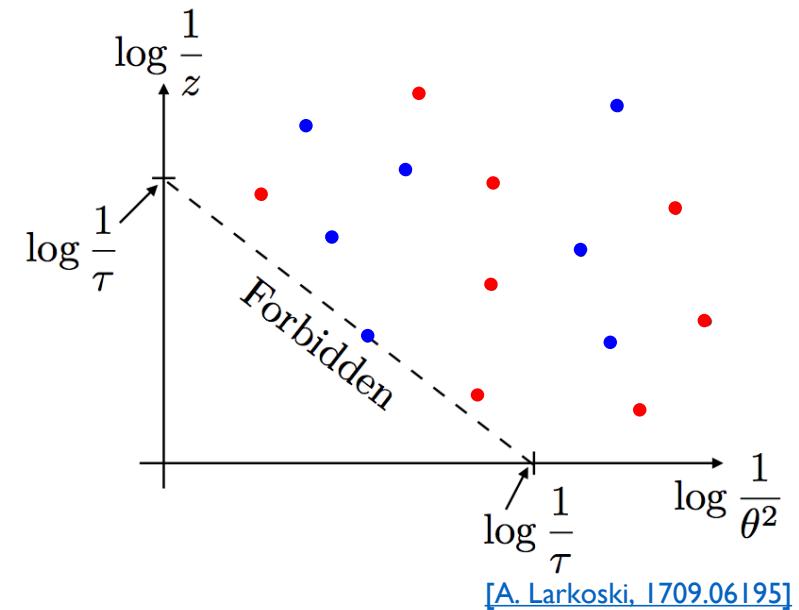
$$= Q \frac{\partial}{\partial Q} \ln \exp \left(- \frac{4\alpha_s C_{q/g}}{\pi} \ln^2 \frac{Q}{p_T/2} \right)$$

$$= - \frac{8\alpha_s C_{q/g}}{\pi} \ln \frac{Q}{p_T/2}$$

+ 1-loop running of α_s

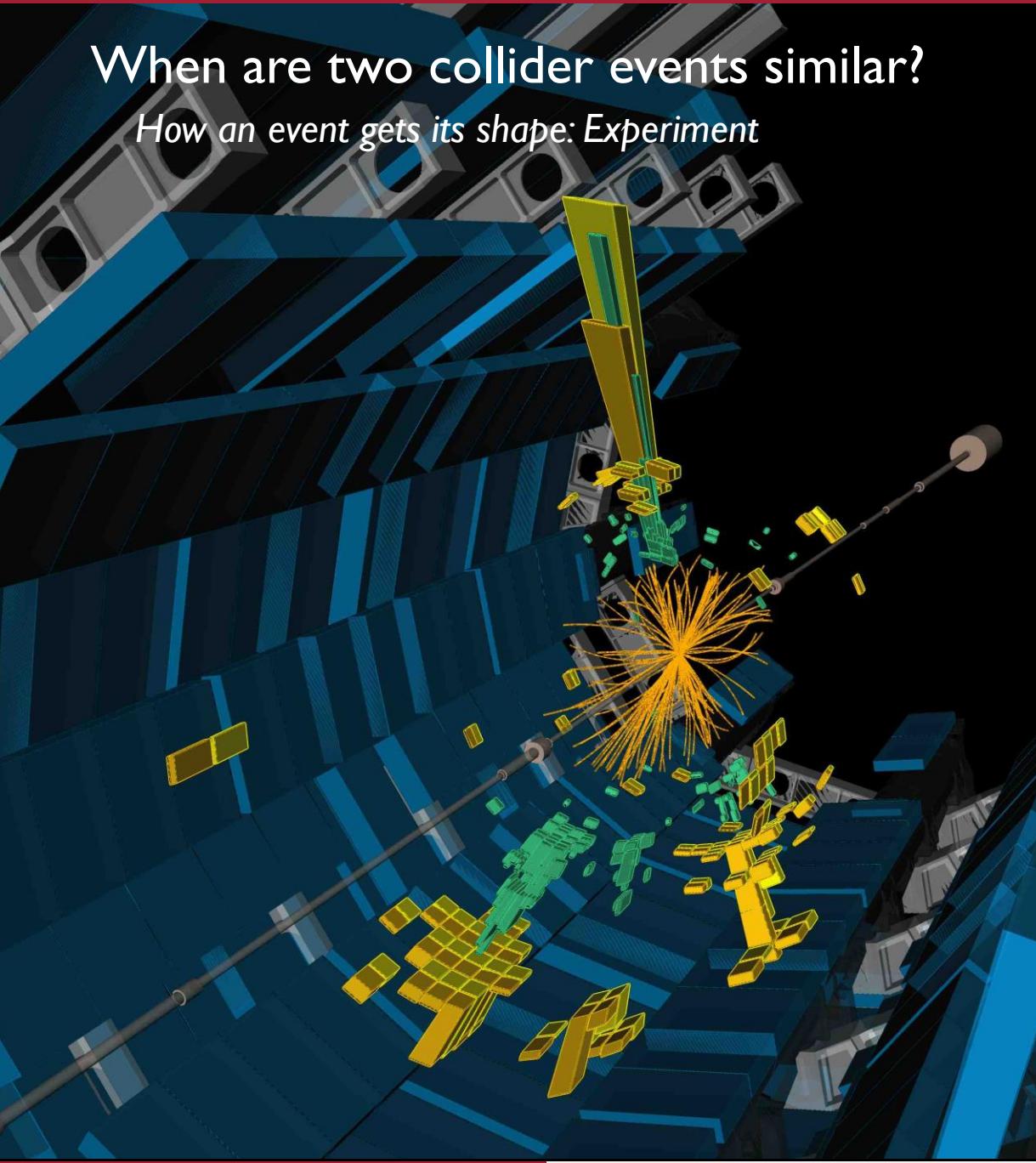
$$C_q = C_F = \frac{4}{3}$$

$$C_g = C_A = 3$$



When are two collider events similar?

How an event gets its shape: Experiment



tracker	ECAL	HCal	
			γ photon
			e^\pm electron
			μ^\pm muon
			π^\pm pion
			K^\pm kaon
			K_L^0 K-long
			p/\bar{p} proton
			n/\bar{n} neutron

Pileup Mitigation with PUMML

