```
?- consult('crypto.pl').
   ../gv.pl compiled 0.00 sec, 12 clauses
   ../combosets.pl compiled 0.01 sec, 34 clauses
% crypto.pl compiled 0.02 sec, 63 clauses
true.
?- crypto(1,2,3,E).
E = ex(1, +, 2);
false.
?- crypto(1, 2, 3, E).
E = ex(1, +, 2)
Unknown action: , (h for help)
Action? ;
false.
?- crypto(1,2,3,E).
E = ex(1, +, 2);
false.
?- crypto(2,1,2,3,E).
E = ex(2, +, ex(2, -, 1));
E = ex(2, -, ex(1, -, 2));
E = ex(2, -, ex(1, -, 2));
E = ex(2, +, ex(2, -, 1));

E = ex(ex(2, +, 2), -, 1);
E = ex(ex(2, *, 2), -, 1) ;
false.
?- crypto(4,2,1,2,3,E).
E = ex(ex(4, +, 2), -, ex(1, +, 2));
E = ex(ex(4, +, 2), /, ex(1, *, 2));
E = ex(ex(4, +, 2), /, ex(2, /, 1)) ;
E = ex(ex(ex(4, +, 2), -, 2), -, 1);
E = ex(1, *, ex(ex(4, +, 2), /, 2)) ;
E = ex(ex(ex(4, +, 2), /, 2), /, 1);
E = ex(ex(1, *, ex(4, +, 2)), /, 2)
E = ex(ex(ex(4, +, 2), -, 1), -, 2)
E = ex(ex(ex(4, +, 2), /, 1), /, 2)
E = ex(ex(ex(4, *, 2), /, 2), -, 1)
E = ex(ex(4, -, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, -, 2)));
E = ex(ex(4, -, 2), +, ex(2, -, 1));
E = ex(2, +, ex(ex(4, -, 2), -, 1));
E = ex(ex(ex(4, -, 2), +, 2), -, 1) ;
E = ex(ex(2, +, ex(4, -, 2)), -, 1);
E = ex(ex(ex(4, -, 2), *, 2), -, 1);
E = ex(ex(2, *, ex(4, -, 2)), -, 1) ;
E = ex(ex(4, -, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, -, 2)));
E = ex(ex(4, -, 2), +, ex(2, -, 1));
E = ex(2, +, ex(ex(4, -, 2), -, 1));
E = ex(ex(2, -, 1), -, ex(2, -, 4));
E = ex(ex(2, -, ex(2, -, 4)), -, 1) ;
E = ex(2, -, ex(1, +, ex(2, -, 4)));
E = ex(ex(4, /, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, /, 2)));
E = ex(ex(4, /, 2), +, ex(2, -, 1));
E = ex(2, +, ex(ex(4, /, 2), -, 1));
E = ex(ex(ex(4, /, 2), +, 2), -, 1);
E = ex(ex(2, +, ex(4, /, 2)), -, 1);
E = ex(ex(ex(4, /, 2), *, 2), -, 1) ;
E = ex(ex(2, *, ex(4, /, 2)), -, 1);
```

```
E = ex(ex(4, /, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, /, 2)));
E = ex(ex(4, /, 2), +, ex(2, -, 1));
E = ex(2, +, ex(ex(4, /, 2), -, 1));
E = ex(ex(4, *, 1), -, ex(2, /, 2));
E = ex(ex(4, *, 1), -, ex(2, /, 2));
E = ex(ex(2, +, ex(4, *, 1)), /, 2);
E = ex(ex(2, +, ex(4, *, 1)), /, 2);
E = ex(ex(4, -, 1), +, ex(2, -, 2));
E = ex(ex(4, -, 1), -, ex(2, -, 2));
E = ex(ex(4, -, 1), +, ex(2, -, 2));
E = ex(ex(4, -, 1), -, ex(2, -, 2));
E = ex(ex(4, -, 1), *, ex(2, /, 2))
E = ex(ex(4, -, 1), /, ex(2, /, 2));
E = ex(ex(4, -, 1), *, ex(2, /, 2));
E = ex(ex(4, -, 1), /, ex(2, /, 2))
E = ex(ex(2, +, ex(4, -, 1)), -, 2);
E = ex(ex(2, *, ex(4, -, 1)), /, 2);
E = ex(2, -, ex(2, -, ex(4, -, 1)));
E = ex(2, +, ex(ex(4, -, 1), -, 2));
E = ex(ex(2, +, ex(4, -, 1)), -, 2) ;
E = ex(ex(2, *, ex(4, -, 1)), /, 2) ;
E = ex(2, -, ex(2, -, ex(4, -, 1)));
E = ex(2, +, ex(ex(4, -, 1), -, 2));
E = ex(ex(2, -, 2), -, ex(1, -, 4));
E = ex(ex(2, -, 2), -, ex(1, -, 4));
E = ex(2, -, ex(2, +, ex(1, -, 4)))
E = ex(ex(2, -, ex(1, -, 4)), -, 2) ;
E = ex(2, -, ex(2, +, ex(1, -, 4)))
E = ex(ex(2, -, ex(1, -, 4)), -, 2) ;
E = ex(ex(4, /, 1), -, ex(2, /, 2));
E = ex(ex(4, /, 1), -, ex(2, /, 2));
E = ex(ex(2, +, ex(4, /, 1)), /, 2) ;
E = ex(ex(2, +, ex(4, /, 1)), /, 2);
E = ex(ex(4, +, 2), -, ex(2, +, 1));
E = ex(ex(4, +, 2), /, ex(2, *, 1));
E = ex(ex(4, +, 2), /, ex(2, /, 1))
E = ex(ex(1, *, ex(4, +, 2)), /, 2)
E = ex(ex(ex(4, +, 2), -, 1), -, 2)
E = ex(ex(ex(4, +, 2), /, 1), /, 2)
E = ex(ex(ex(4, +, 2), -, 2), -, 1) ;
E = ex(1, *, ex(ex(4, +, 2), /, 2));
E = ex(ex(ex(4, +, 2), /, 2), /, 1);
E = ex(ex(ex(4, *, 2), /, 2), -, 1);
E = ex(ex(4, -, 2), +, ex(2, -, 1));
E = ex(2, +, ex(ex(4, -, 2), -, 1));
E = ex(ex(4, -, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, -, 2)));
E = ex(ex(4, -, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, -, 2)));
E = ex(ex(4, -, 2), +, ex(2, -, 1));
E = ex(2, +, ex(ex(4, -, 2), -, 1));
E = ex(ex(ex(4, -, 2), +, 2), -, 1) ;
E = ex(ex(2, +, ex(4, -, 2)), -, 1);
E = ex(ex(ex(4, -, 2), *, 2), -, 1);
E = ex(ex(2, *, ex(4, -, 2)), -, 1);
E = ex(ex(2, -, 1), -, ex(2, -, 4));
E = ex(2, -, ex(1, +, ex(2, -, 4)));
E = ex(ex(2, -, ex(2, -, 4)), -, 1) ;
E = ex(ex(4, /, 2), +, ex(2, -, 1));
 = ex(2, +, ex(ex(4, /, 2), -, 1));
E = ex(ex(4, /, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, /, 2)));
```

```
E = ex(ex(4, /, 2), -, ex(1, -, 2));
E = ex(2, -, ex(1, -, ex(4, /, 2)));
E = ex(ex(4, /, 2), +, ex(2, -, 1));
E = ex(2, +, ex(ex(4, /, 2), -, 1));
E = ex(ex(ex(4, /, 2), +, 2), -, 1);
E = ex(ex(2, +, ex(4, /, 2)), -, 1);
E = ex(ex(ex(4, /, 2), *, 2), -, 1);
E = ex(ex(2, *, ex(4, /, 2)), -, 1) ;
E = ex(ex(4, +, 2), -, ex(2, +, 1));
E = ex(4, +, ex(2, -, ex(2, +, 1)));
E = ex(4, -, ex(ex(2, +, 1), -, 2));
E = ex(2, +, ex(4, -, ex(2, +, 1)));
E = ex(2, -, ex(ex(2, +, 1), -, 4))
E = ex(ex(4, +, 2), /, ex(2, *, 1));

E = ex(ex(4, +, ex(2, *, 1)), /, 2);
E = ex(4, -, ex(ex(2, *, 1), /, 2));
E = ex(4, -, ex(2, /, ex(2, *, 1)));
E = ex(4, -, ex(ex(2, *, 1), /, 2));
E = ex(4, -, ex(2, /, ex(2, *, 1)));
E = ex(ex(4, +, 2), /, ex(2, *, 1));
E = ex(ex(4, +, ex(2, *, 1)), /, 2);
E = ex(ex(2, -, 1), +, ex(4, -, 2));
E = ex(ex(2, -, 1), -, ex(2, -, 4));
E = ex(ex(2, -, 1), +, ex(4, /, 2));
E = ex(4, -, ex(2, -, ex(2, -, 1)));
E = ex(4, +, ex(ex(2, -, 1), -, 2));
E = ex(ex(4, +, ex(2, -, 1)), -, 2);
E = ex(ex(4, -, 2), -, ex(1, -, 2))
E = ex(ex(4, /, 2), -, ex(1, -, 2));
E = ex(4, -, ex(2, +, ex(1, -, 2)));
E = ex(ex(4, -, ex(1, -, 2)), -, 2);
E = ex(ex(4, +, 2), /, ex(2, /, 1));
E = ex(ex(4, +, ex(2, /, 1)), /, 2);
E = ex(4, -, ex(ex(2, /, 1), /, 2));
E = ex(4, -, ex(2, /, ex(2, /, 1)));
E = ex(4, -, ex(ex(2, /, 1), /, 2));
E = ex(4, -, ex(2, /, ex(2, /, 1)))
E = ex(ex(4, +, 2), /, ex(2, /, 1));
E = ex(ex(4, +, ex(2, /, 1)), /, 2);
E = ex(ex(2, -, 2), +, ex(4, -, 1))
E = ex(ex(4, -, 1), -, ex(2, -, 2));
E = ex(ex(2, -, 2), -, ex(1, -, 4));
E = ex(4, -, ex(1, +, ex(2, -, 2)));
E = ex(4, -, ex(1, -, ex(2, -, 2)));
E = ex(4, +, ex(ex(2, -, 2), -, 1));
E = ex(ex(4, +, ex(2, -, 2)), -, 1) ;
E = ex(ex(4, -, ex(2, -, 2)), -, 1) ;
E = ex(ex(2, -, 2), +, ex(4, -, 1));
E = ex(ex(4, -, 1), -, ex(2, -, 2));
E = ex(ex(2, -, 2), -, ex(1, -, 4));
E = ex(4, -, ex(1, +, ex(2, -, 2)));
E = ex(4, -, ex(1, -, ex(2, -, 2)));
E = ex(4, +, ex(ex(2, -, 2), -, 1));
E = ex(ex(4, +, ex(2, -, 2)), -, 1);
E = ex(ex(4, -, ex(2, -, 2)), -, 1);
E = ex(ex(4, *, 1), -, ex(2, /, 2));
E = ex(ex(4, *, ex(2, /, 2)), -, 1) ;
E = ex(ex(2, /, 2), *, ex(4, -, 1));
E = ex(1, *, ex(4, -, ex(2, /, 2)));

E = ex(ex(4, -, 1), /, ex(2, /, 2));
E = ex(ex(4, -, ex(2, /, 2)), /, 1);
E = ex(ex(4, /, 1), -, ex(2, /, 2));
E = ex(ex(4, /, ex(2, /, 2)), -, 1);
```

```
E = ex(4, -, ex(ex(2, /, 2), *, 1));
E = ex(4, -, ex(1, *, ex(2, /, 2)));
E = ex(4, -, ex(ex(2, /, 2), /, 1));
E = ex(4, -, ex(1, /, ex(2, /, 2)));
E = ex(4, -, ex(ex(2, /, 2), /, 1));
E = ex(4, -, ex(1, /, ex(2, /, 2)));
E = ex(ex(4, *, 1), -, ex(2, /, 2));
E = ex(ex(4, *, ex(2, /, 2)), -, 1) ;
E = ex(ex(2, /, 2), *, ex(4, -, 1));
E = ex(1, *, ex(4, -, ex(2, /, 2)));
E = ex(ex(4, -, 1), /, ex(2, /, 2));
E = ex(ex(4, -, ex(2, /, 2)), /, 1) ;
E = ex(ex(4, /, 1), -, ex(2, /, 2))
E = ex(ex(4, /, ex(2, /, 2)), -, 1)
E = ex(ex(4, *, 1), -, ex(2, /, 2))
E = ex(ex(4, *, ex(2, /, 2)), -, 1)
E = ex(ex(2, /, 2), *, ex(4, -, 1));
E = ex(1, *, ex(4, -, ex(2, /, 2)));
E = ex(ex(4, -, 1), /, ex(2, /, 2));
E = ex(ex(4, -, ex(2, /, 2)), /, 1);
E = ex(ex(4, /, 1), -, ex(2, /, 2));
E = ex(ex(4, /, ex(2, /, 2)), -, 1) ;
E = ex(4, -, ex(ex(2, /, 2), *, 1));
E = ex(4, -, ex(1, *, ex(2, /, 2)));
E = ex(4, -, ex(ex(2, /, 2), /, 1));

E = ex(4, -, ex(1, /, ex(2, /, 2)));
E = ex(4, -, ex(ex(2, /, 2), /, 1));

E = ex(4, -, ex(1, /, ex(2, /, 2)));
E = ex(ex(4, *, 1), -, ex(2, /, 2));
E = ex(ex(4, *, ex(2, /, 2)), -, 1) ;
E = ex(ex(2, /, 2), *, ex(4, -, 1));
E = ex(1, *, ex(4, -, ex(2, /, 2)));
E = ex(ex(4, -, 1), /, ex(2, /, 2));
E = ex(ex(4, -, ex(2, /, 2)), /, 1);
E = ex(ex(4, /, 1), -, ex(2, /, 2));
E = ex(ex(4, /, ex(2, /, 2)), -, 1) ;
E = ex(ex(4, +, 2), -, ex(1, +, 2))
E = ex(4, +, ex(2, -, ex(1, +, 2)))
E = ex(4, -, ex(ex(1, +, 2), -, 2))
E = ex(2, +, ex(4, -, ex(1, +, 2)))
E = ex(2, -, ex(ex(1, +, 2), -, 4));
E = ex(ex(4, +, 2), /, ex(1, *, 2));
E = ex(ex(4, +, ex(1, *, 2)), /, 2) ;
E = ex(4, -, ex(ex(1, *, 2), /, 2));
E = ex(4, -, ex(2, /, ex(1, *, 2)));
E = ex(4, -, ex(ex(1, *, 2), /, 2));
E = ex(4, -, ex(2, /, ex(1, *, 2)));
E = ex(ex(4, +, 2), /, ex(1, *, 2));
E = ex(ex(4, +, ex(1, *, 2)), /, 2);
E = ex(ex(4, -, 2), -, ex(1, -, 2))
E = ex(ex(4, /, 2), -, ex(1, -, 2))
E = ex(4, -, ex(2, +, ex(1, -, 2)))
E = ex(ex(4, -, ex(1, -, 2)), -, 2) ;
E = ex(ex(2, -, 1), +, ex(4, -, 2));
E = ex(ex(2, -, 1), -, ex(2, -, 4));
E = ex(ex(2, -, 1), +, ex(4, /, 2));
E = ex(4, -, ex(2, -, ex(2, -, 1)));
E = ex(4, +, ex(ex(2, -, 1), -, 2));
E = ex(ex(4, +, ex(2, -, 1)), -, 2);
E = ex(ex(4, +, 2), /, ex(2, /, 1));
E = ex(ex(4, +, ex(2, /, 1)), /, 2);
E = ex(4, -, ex(ex(2, /, 1), /, 2));
E = ex(4, -, ex(2, /, ex(2, /, 1)));
```

```
\begin{split} E &= \exp(4, -, \exp(\exp(2, /, 1), /, 2)) ; \\ E &= \exp(4, -, \exp(2, /, \exp(2, /, 1))) ; \\ E &= \exp(\exp(4, +, 2), /, \exp(2, /, 1)) ; \\ E &= \exp(\exp(4, +, \exp(2, /, 1)), /, 2) ; \\ false. \end{split}
```