$$X \cdot \beta_1 = X'$$

$$X' \xrightarrow{\text{logistic}} p$$

$$\text{logistic}(x) = \frac{1}{1 + e^{-x}}$$

$$Y \sim \text{Bernoulli}(p)$$