Deep Learning

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- Research focusses on computational methods for text analysis, signal analysis, image analysis, and so forth

Deep learning algorithm does as well as dermatologists in identifying skin cancer

Date: January 25, 2017

Source: Stanford University

Summary: In hopes of creating better access to medical care, researchers have trained an algorithm to diagnose skin cancer.

Share:

RELATED TOPICS

Health & Medicine

- Skin Care
- Skin Cancer
- Psoriasis

Computers & Math

- Computer Programming
- Computers and Internet
- Artificial Intelligence

RELATED TERMS

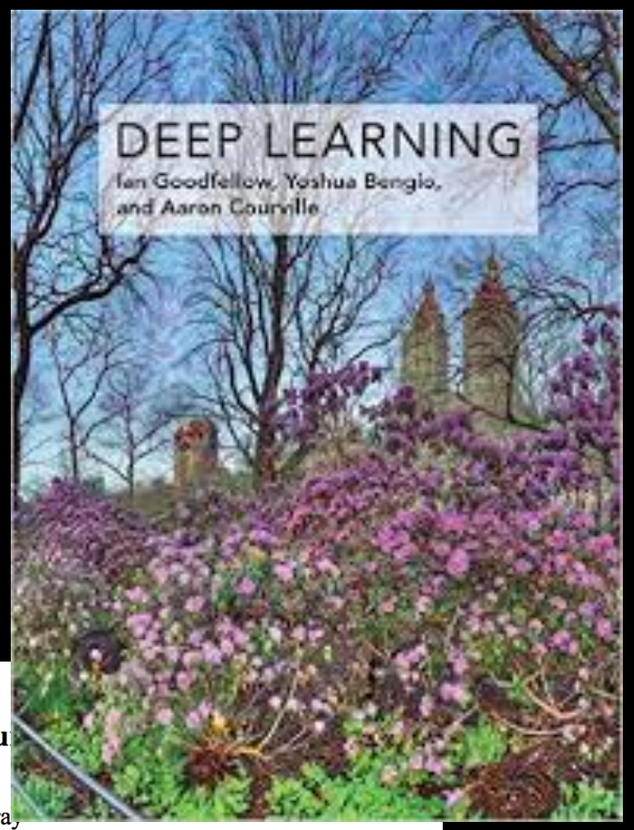
- Stem cell treatments

FULL STORY

A dermatologist using a dermatoscope, a type of handheld microscope, to look at skin. Computer scientists at Stanford have created an artificially intelligent diagnosis algorithm for skin cancer that matched the performance of board-certified

Literature

- http://www.deeplearningbook.org/
- arXiv server (https://arxiv.org/)



arXiv:1509.09308v2 [cs.NE] 10 Nov 2015

Fast Algorithms for Convolutional Neu

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Abstract

Deep convolutional neural networks take GPU days of compute time to train on large data sets. Pedestrian detection for self driving cars requires very low latency. Image recognition for mobile phones is constrained by limited processing resources. The success of convolutional neural networks in these situations is limited by how fast we can compute them. Conventional FFT based convolution is fast for large filters, but state of the art convolutional neural networks use small, 3×3 filters. We introduce a new class of fast algorithms for convolutional neural networks using Winograd's minimal filtering algorithms. The algorithms compute minimal complexity convolution over small tiles, which makes them fast with small filters and small batch sizes. We benchmark a GPU implementation of our algorithm with the VGG network and show state of the art throughput at batch sizes from 1 to 64.

1. Introduction

Deep convolutional neural networks (convnets) achieve state of the art results on image recognition problems [11][7]. The networks take several days of GPU time to train and require significant compute resources during classification as well. Larger data sets and models lead to better accuracy but also increase computation time. Therefore progress in deep neural networks is limited by how fast

cause they achieve better accuracy with fewer weights than shallow networks with larger filters [11, 7].

Therefore there is a strong need for fast convnet algorithms for small batch sizes and small filters. However conventional convnet libraries require large batch sizes and large filters for fast operation.

This paper introduces a new class of fast algorithms for convolutional neural networks based on the minimal filtering algorithms pioneered by Winograd [13]. The algorithms can reduce the arithmetic complexity of a convnet layer by up to a factor of 4 compared to direct convolution. Almost all of the arithmetic is performed by dense matrix multiplies of sufficient dimensions to be computed efficiently, even when the batch size is very small. The memory requirements are also light compared to the conventional FFT convolution algorithm. These factors make practical implementations possible. Our implementation for NVIDIA Maxwell GPUs achieves state of the art throughput for all batch sizes measured, from 1 to 64, while using at most 16MB of workspace memory.

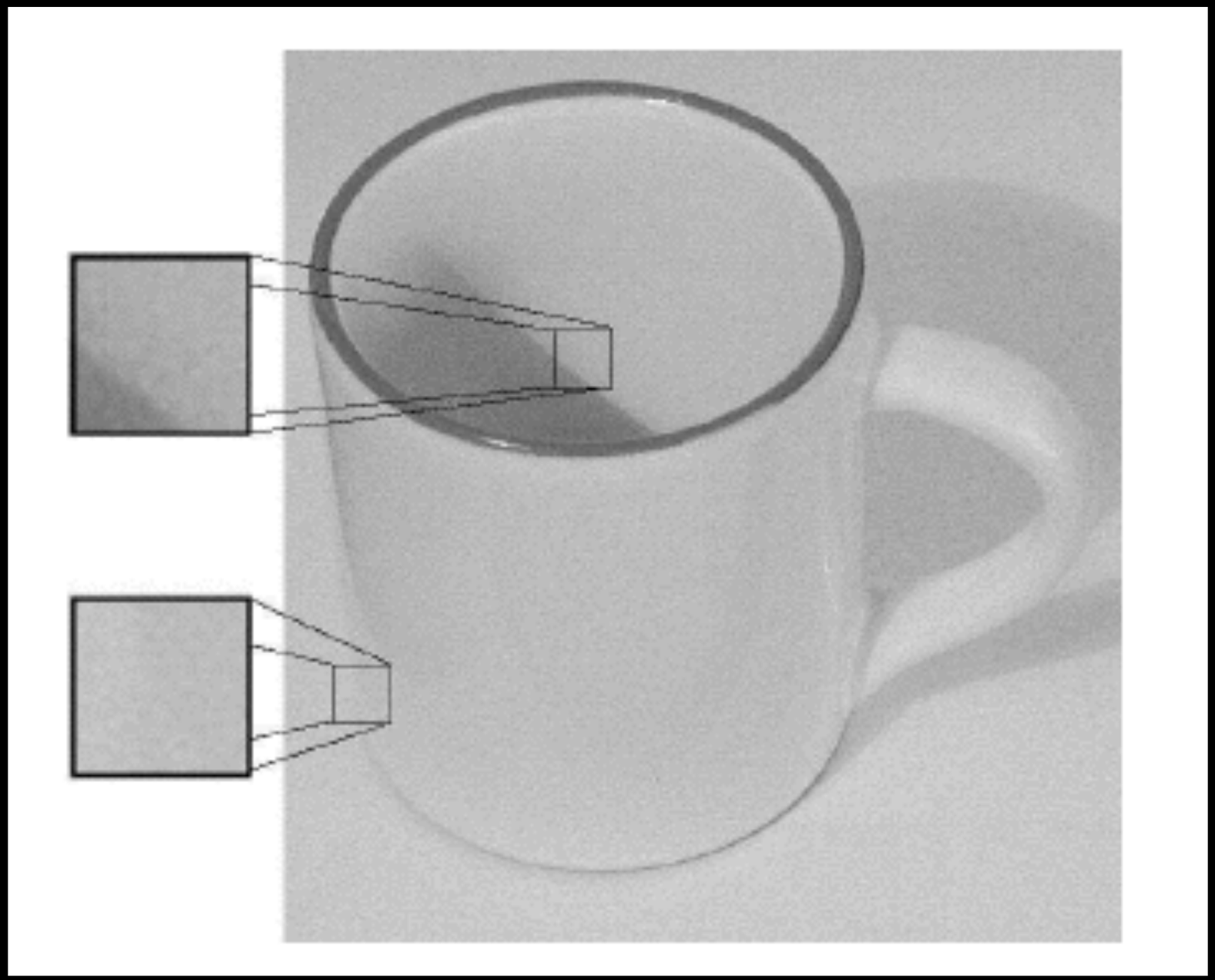
2. Related Work

The FFT and convolution theorem have been used to reduce the arithmetic complexity of convnet layers, first by Mathieu *et al.* [10], then refined by Visalache *et al.* [12], and then implemented in the NVIDIA cuDNN library [1].

Today

- Deep Learning essentials
- Acquiring intuition about convolutional neural networks
- Exploring deep neural networks
- Exploring convolution
- Exploring convolutional neural networks

Local Processing (visual “features”)



Filters

-1	0	+1
-2	0	+2
-1	0	+1

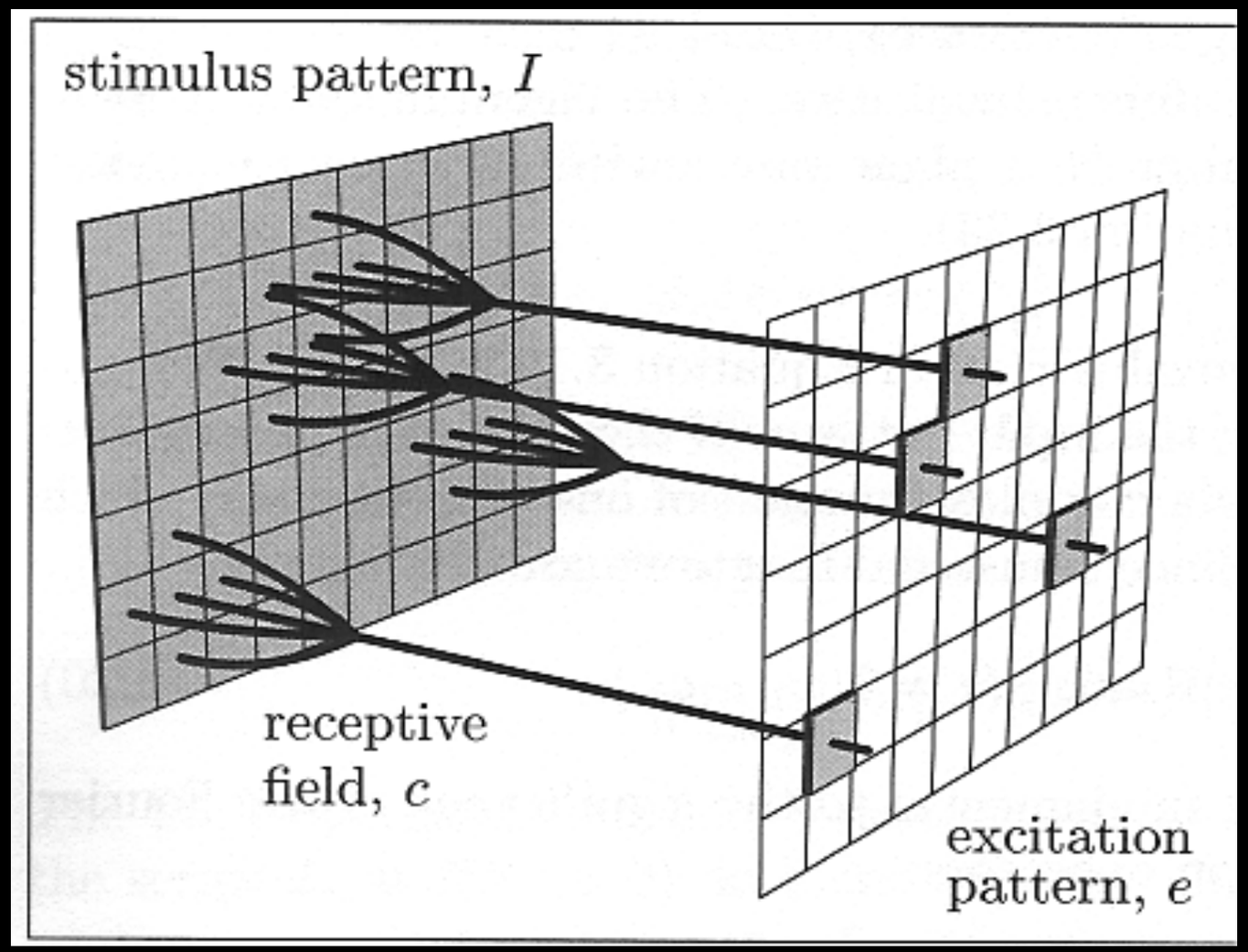
Gx

+1	+2	+1
0	0	0
-1	-2	-1

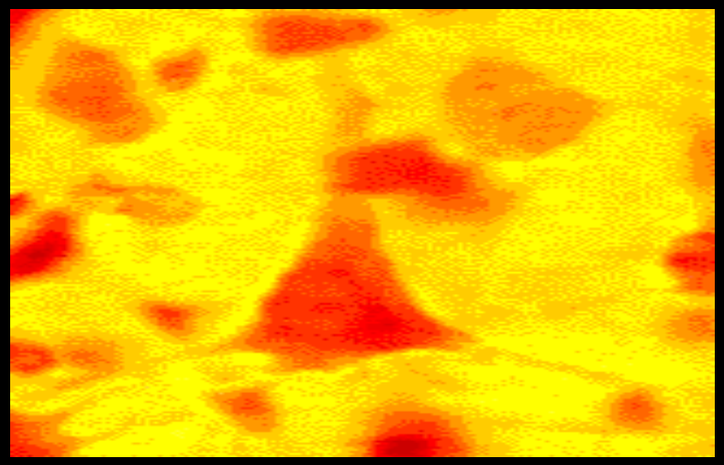
Gy

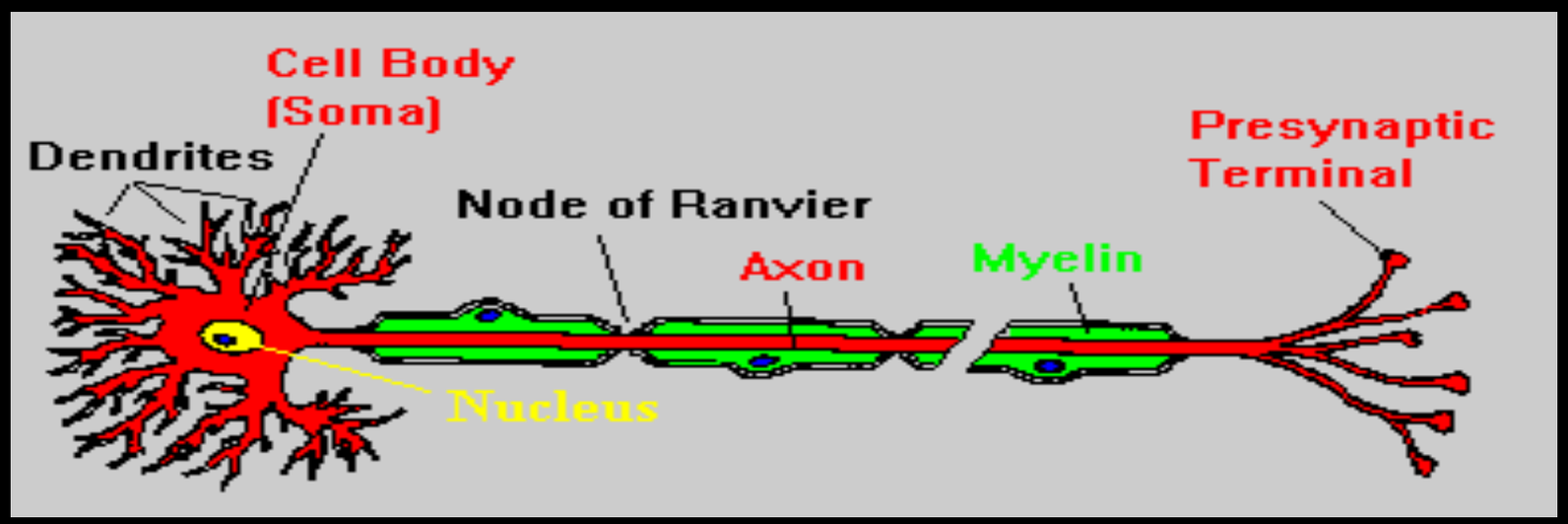
convolution

Filtering in Neural Networks

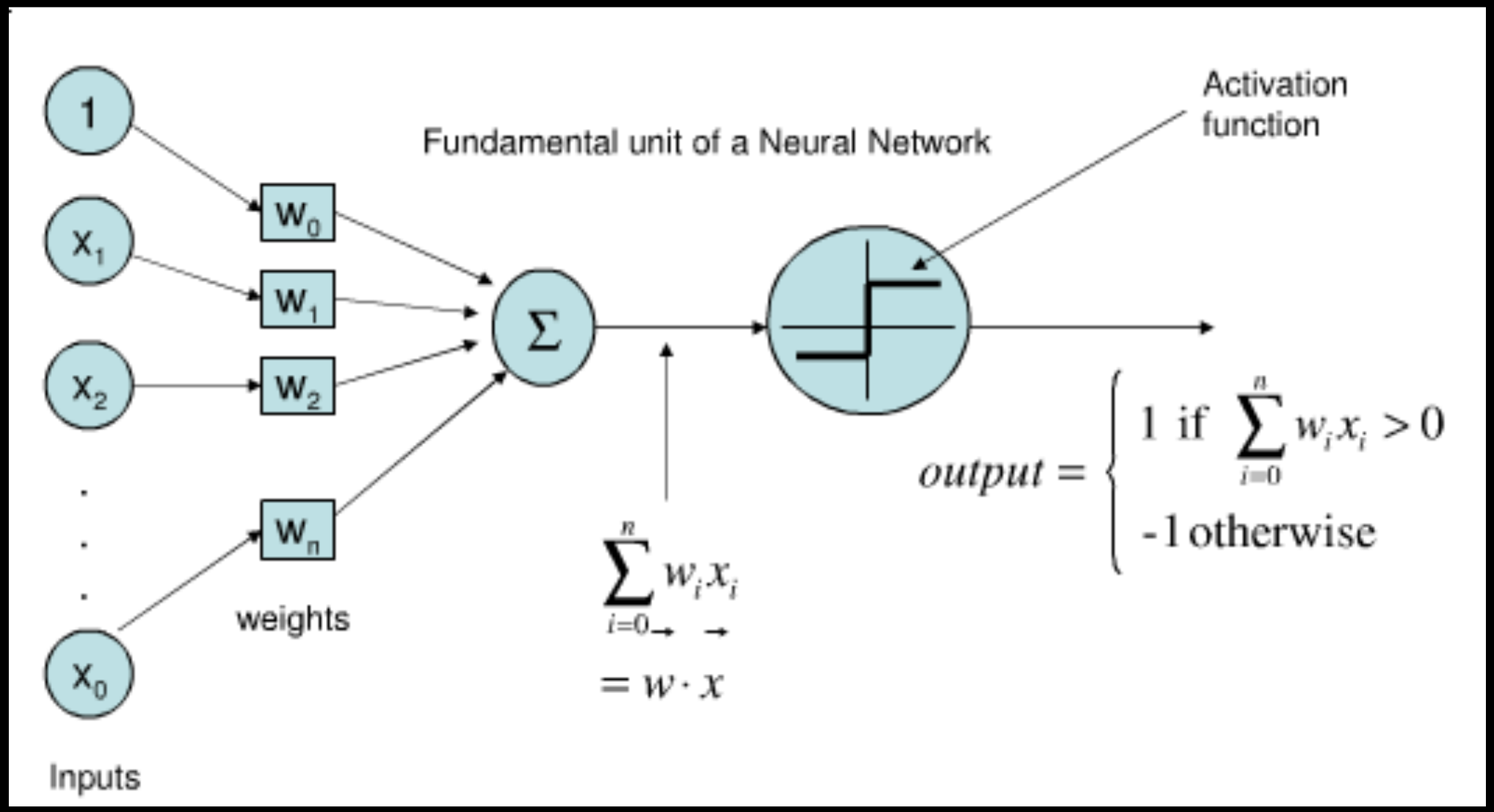


A brief history of neural networks



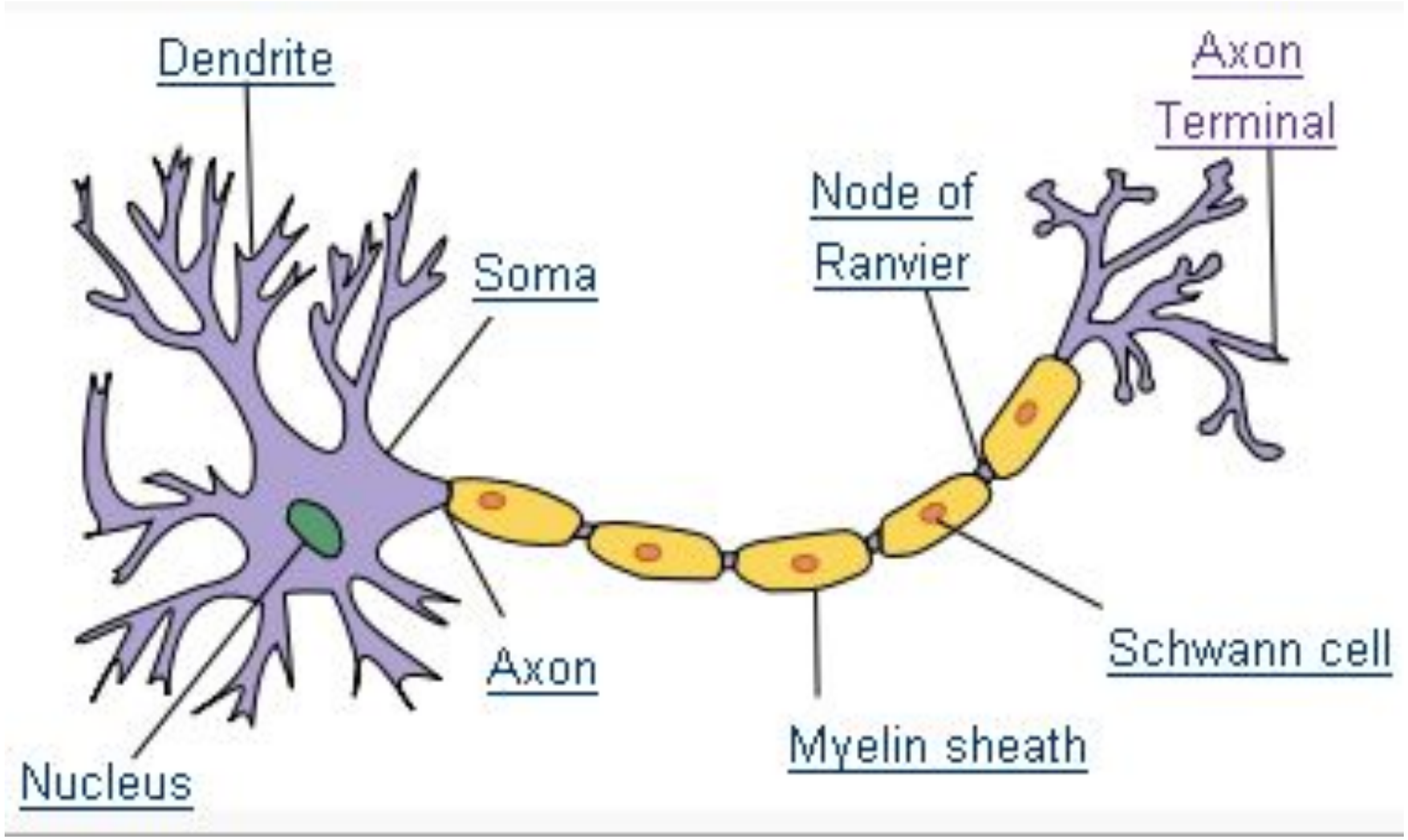


Perceptron (1957)

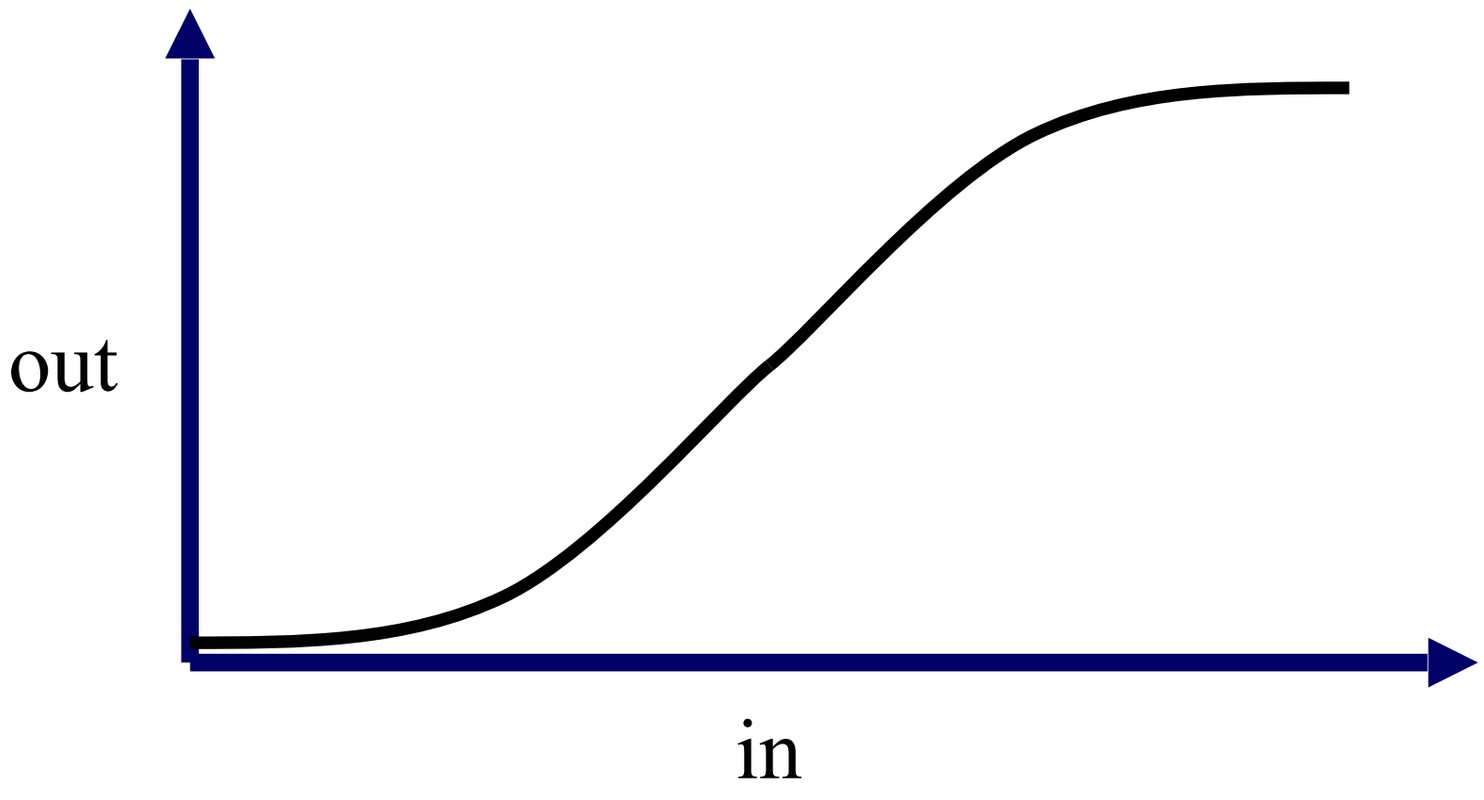


Automatically Learns Linear Mappings

Neurons, the building blocks of the brain

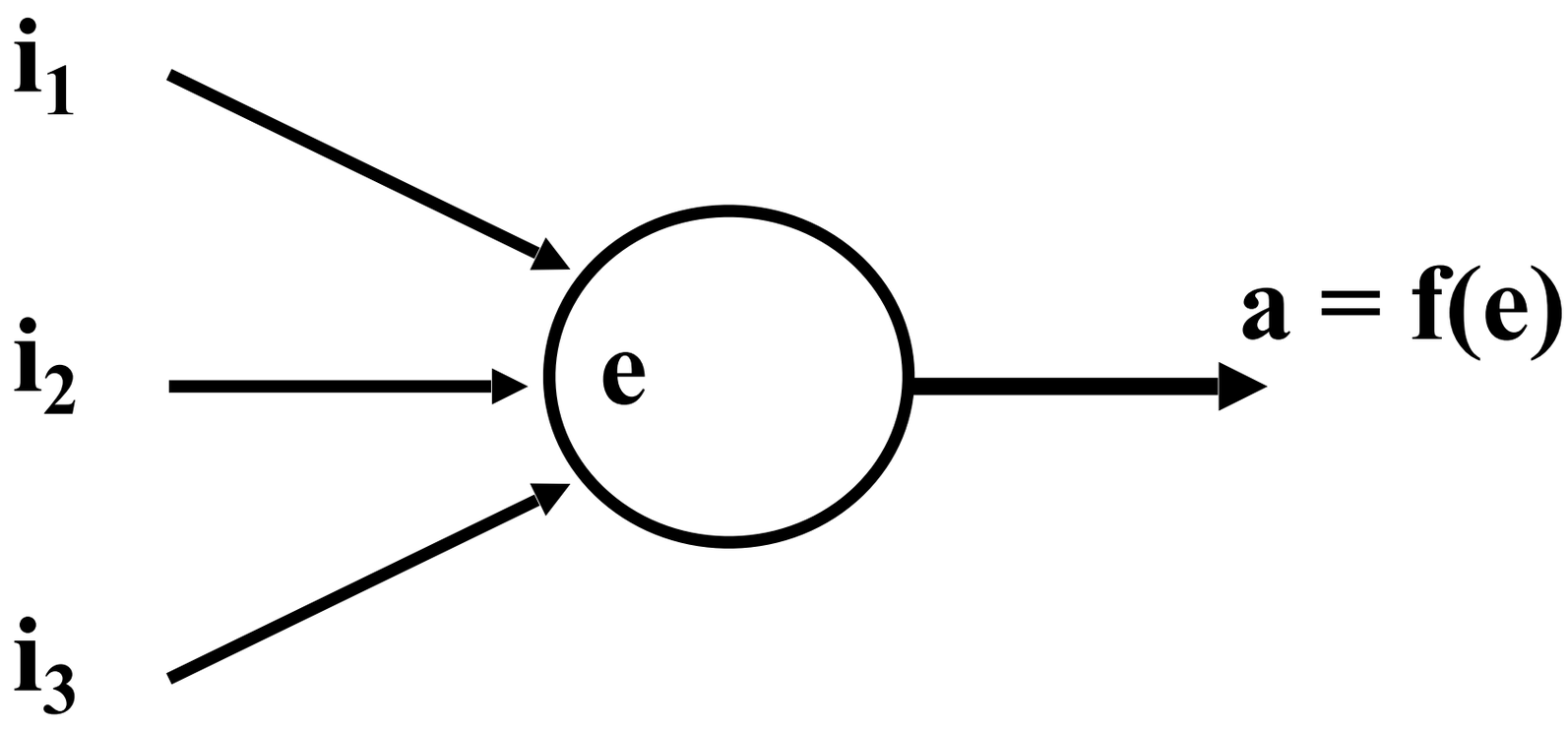


Neural activity



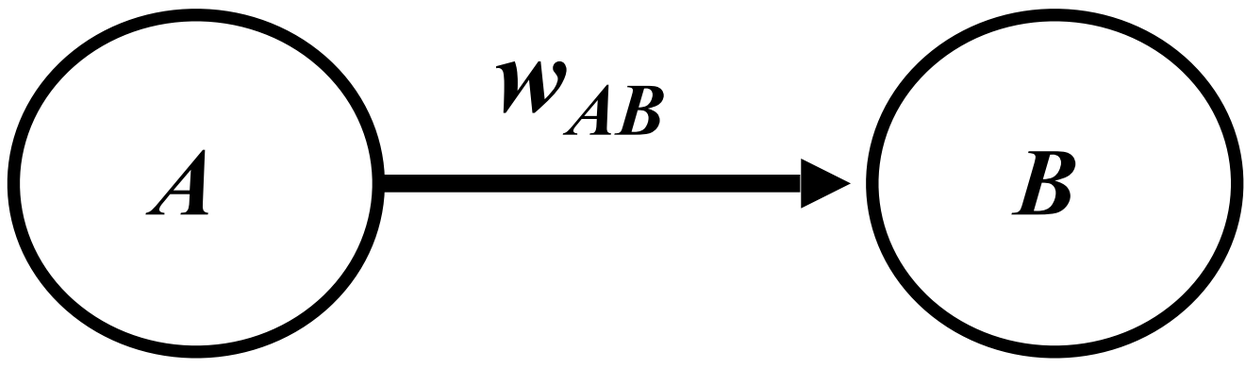
Artificial Neurons

- input (vectors)
- summation (excitation)
- output (activation)

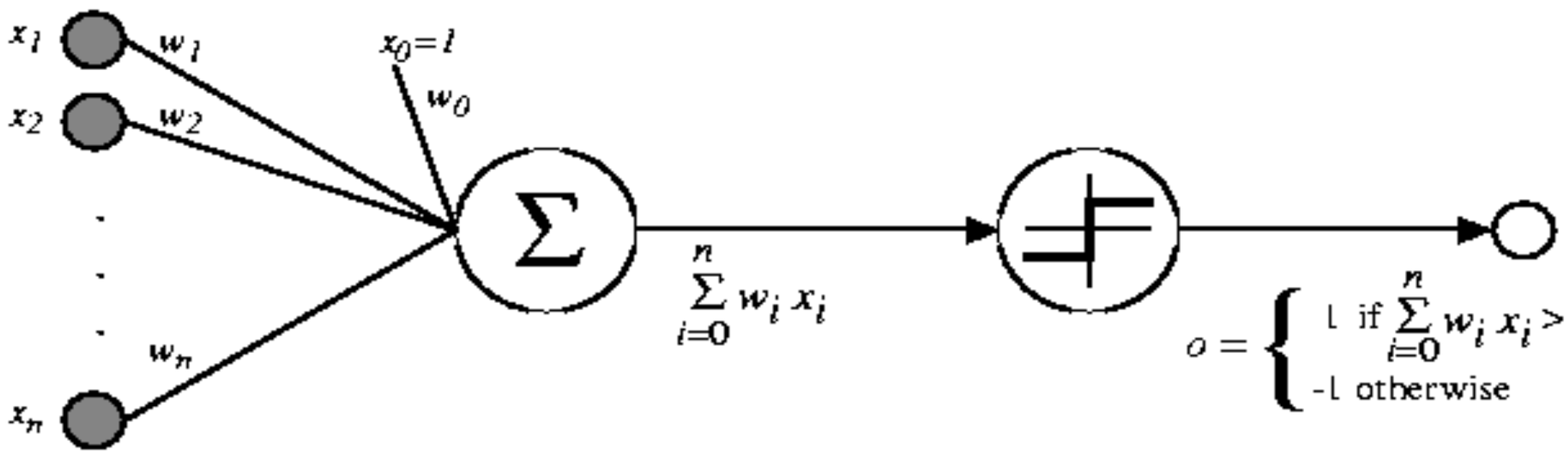


Artificial Connections (Synapses)

- w_{AB}
  - The weight of the connection from neuron *A* to neuron *B*



The Perceptron



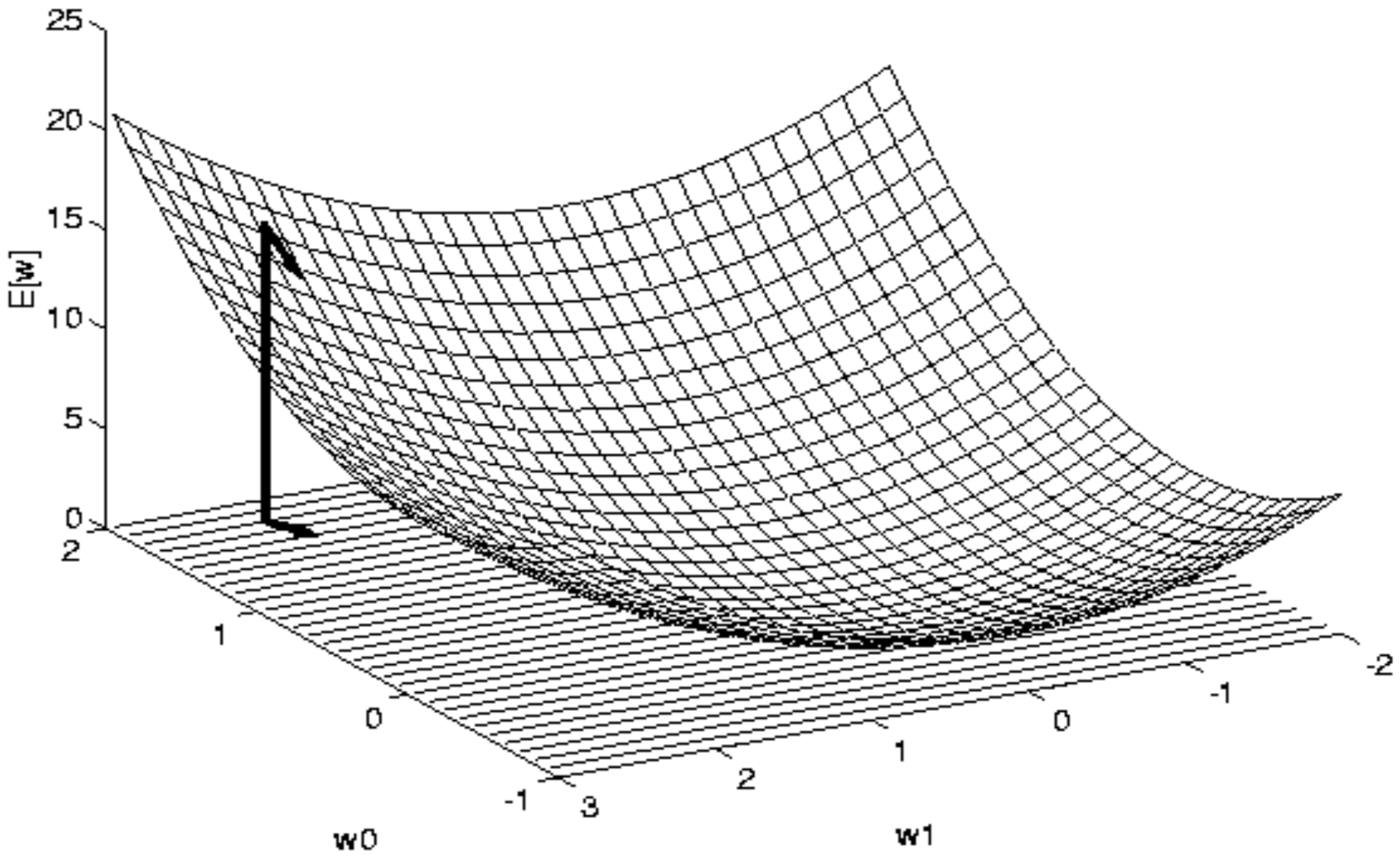
$$o(x_1, \ldots, x_n) = \begin{cases} 1 & \text{if } w_0 + w_1 x_1 + \cdots + w_n x_n > 0 \\ -1 & \text{otherwise.} \end{cases}$$

Learning in the Perceptron

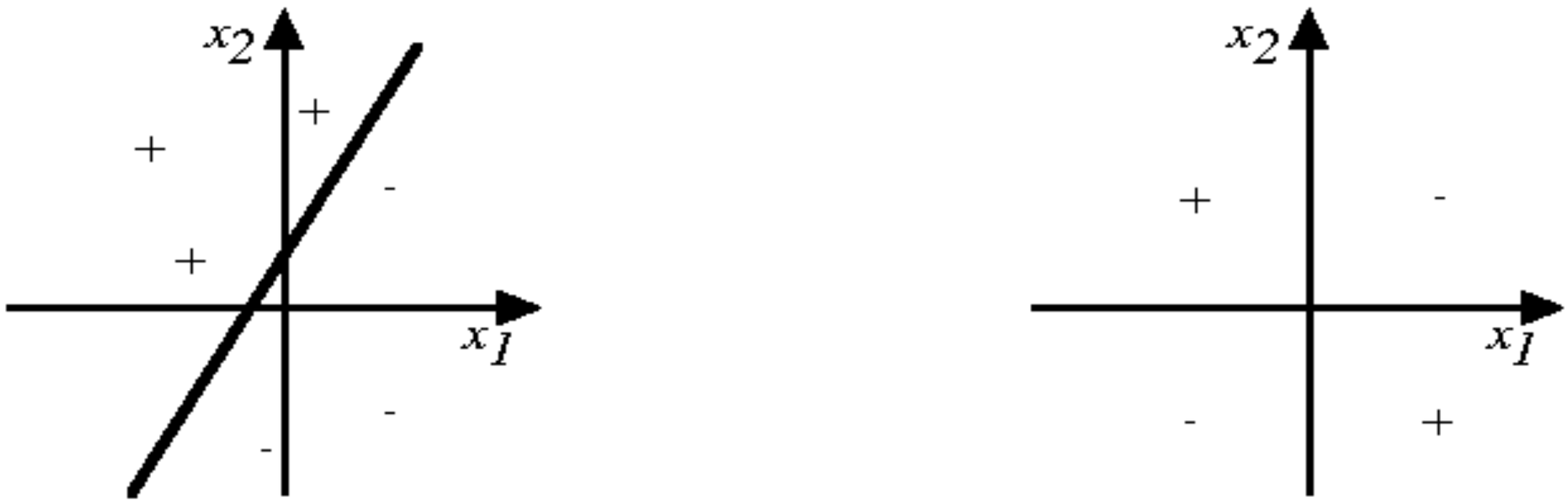
- Delta learning rule
  - the difference between the desired output ***t*** and the actual output ***o,*** given input ***x***
    weights are adjusted to minimise the difference

- Global error E
  - is a function of the differences between the desired (t) and actual (o) outputs

Gradient Descent



Can only learn linearly separable classification tasks

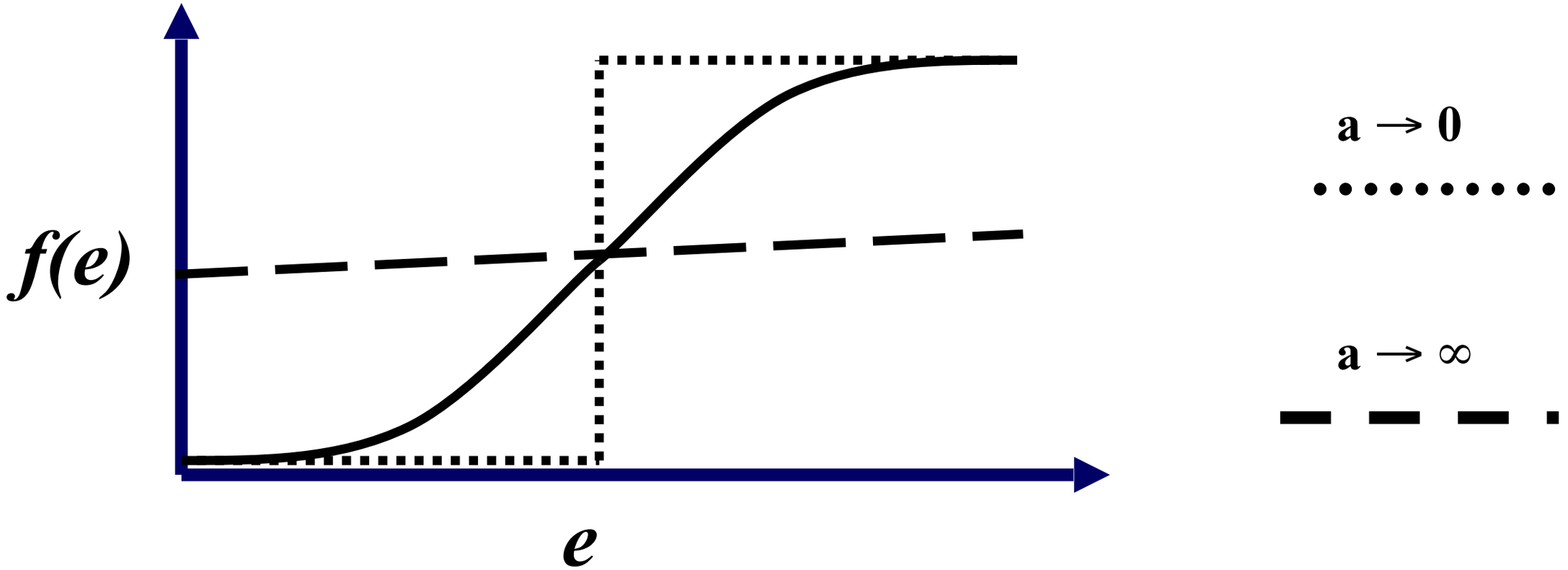


The history of the Perceptron

- Rosenblatt (1959)
- Minsky & Papert (1961)
- Rumelhart, McClelland & Hinton (1986)
- LeCun (1989), Hinton, LeCun (2016…)

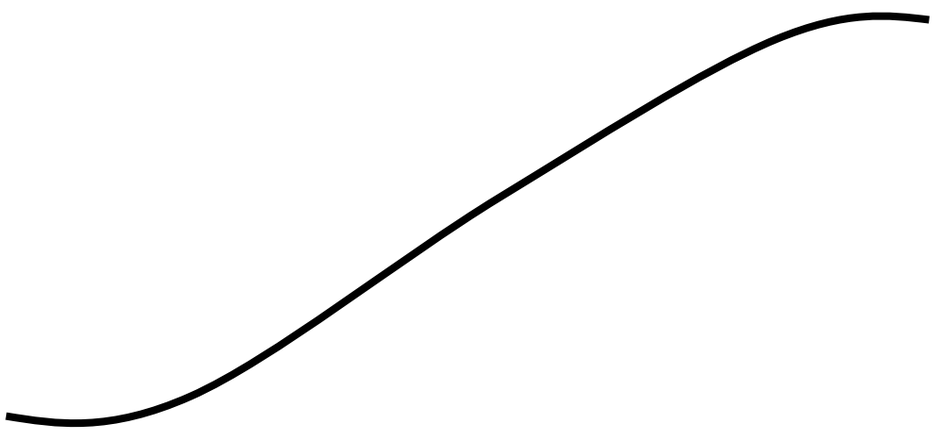
Sigmoid transfer (input-output) function

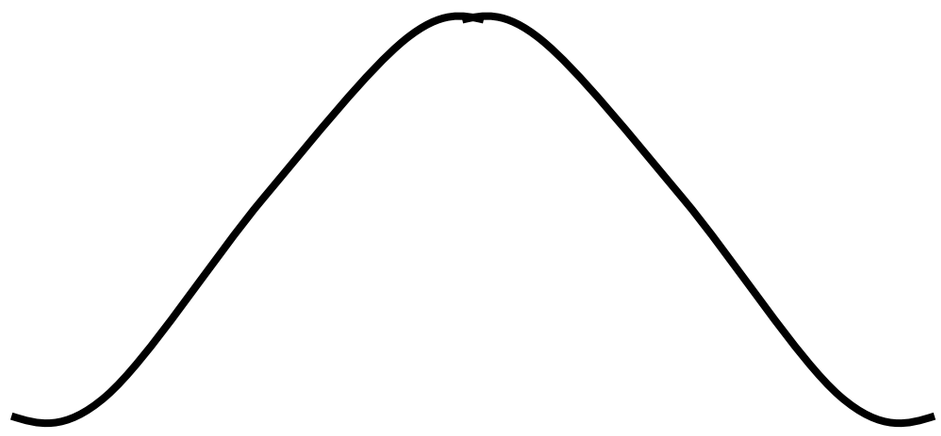
- nonlinear function: $$f(x) = \frac{1}{1 + e^{-x/a}}$$



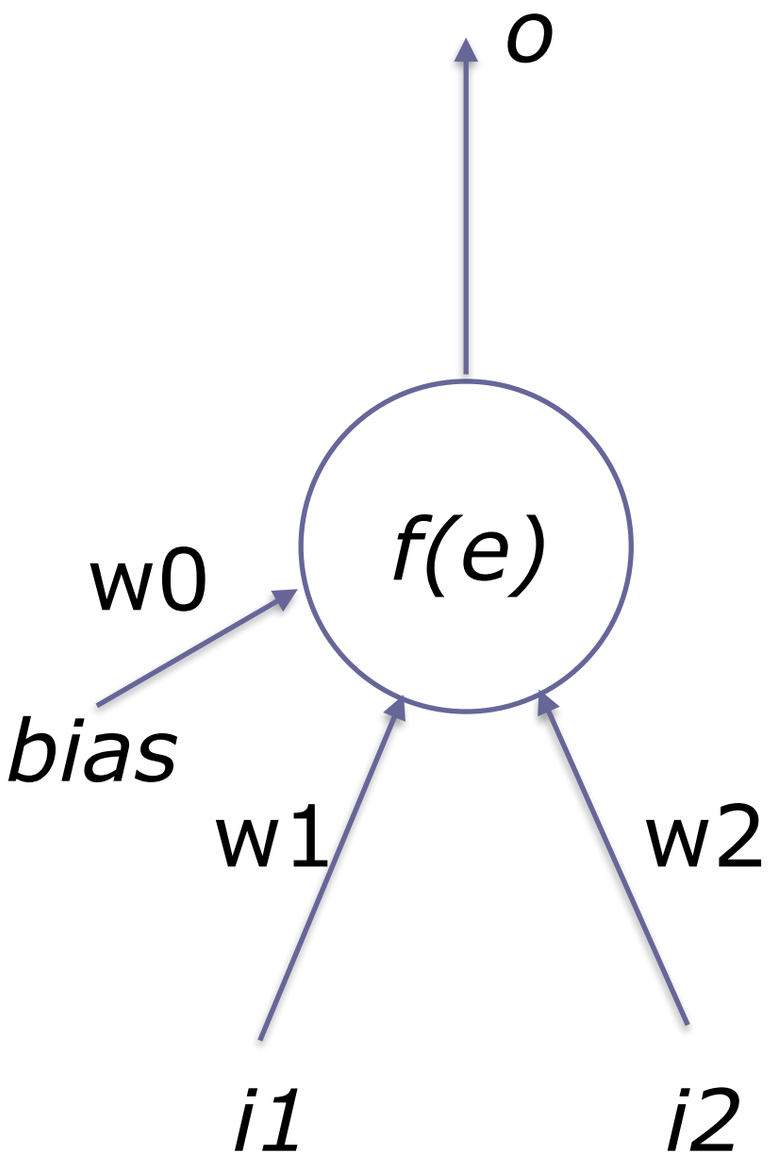
sigmoid transfer function

- May also be the **tanh** function (<-1,+1> instead of <0,1>)
- Derivative f’(x) = f(x) [1 – f(x)]





Perceptron



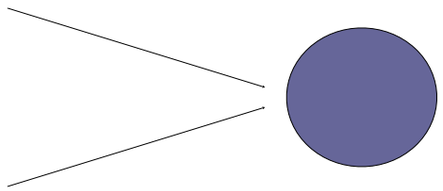
$$o = f\left(\sum_{i=0}^{I} w_i\, i_i\right) = f(e)$$

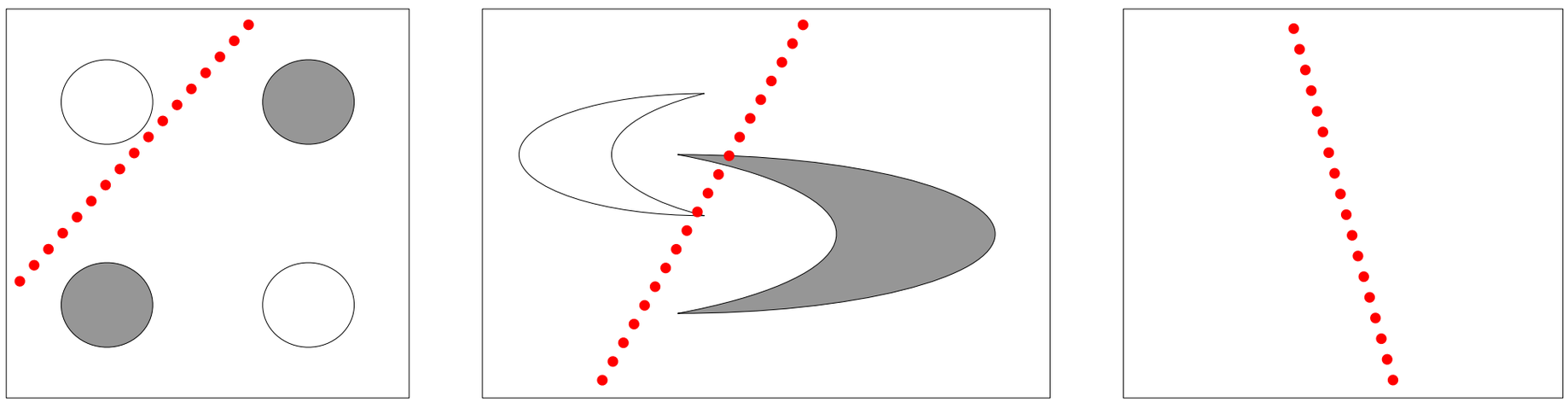
Derivation of the delta learning rule (for a sigmoid transfer function)

$$E = \sum_{p=1}^{P} \frac{1}{2}\left(t_p - o_p\right)^2$$

$$\Delta w_k = -\eta \frac{\partial E}{\partial w_k} = \eta \sum_{p=1}^{P} \left(t_p - o_p\right) f'\left(e_p\right) i_k = \eta \sum_{p=1}^{P} \sigma\, i_k$$

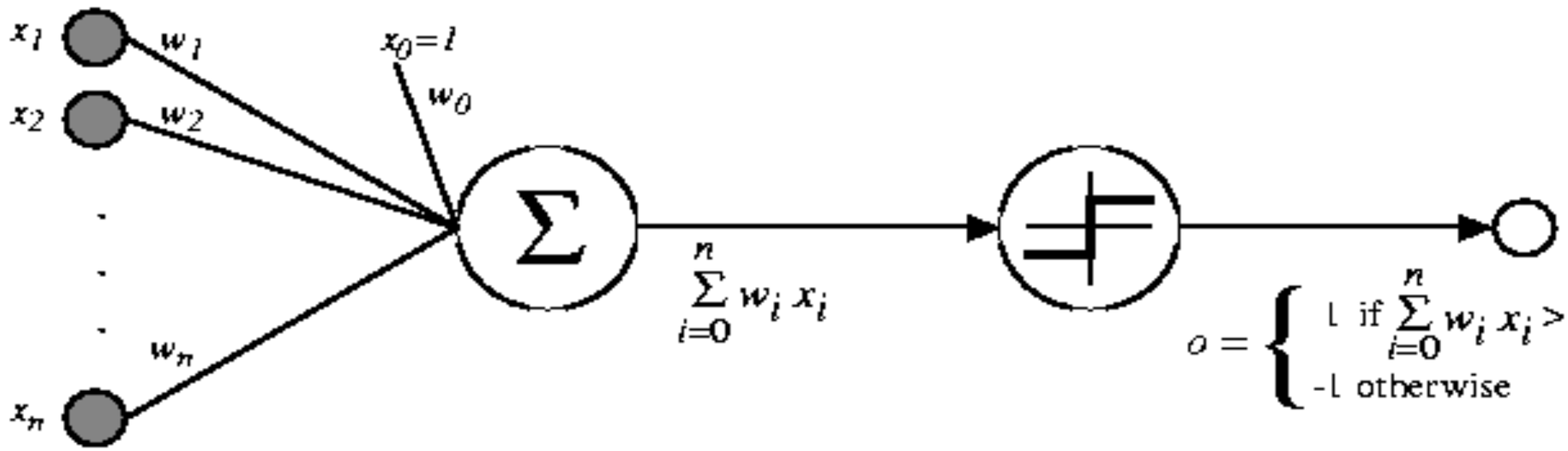
Decision boundaries of Perceptrons





Straight lines (surfaces), linear separable

Can you derive the equation of the decision boundary for a perceptron with 2 inputs (+ 1 bias input)?

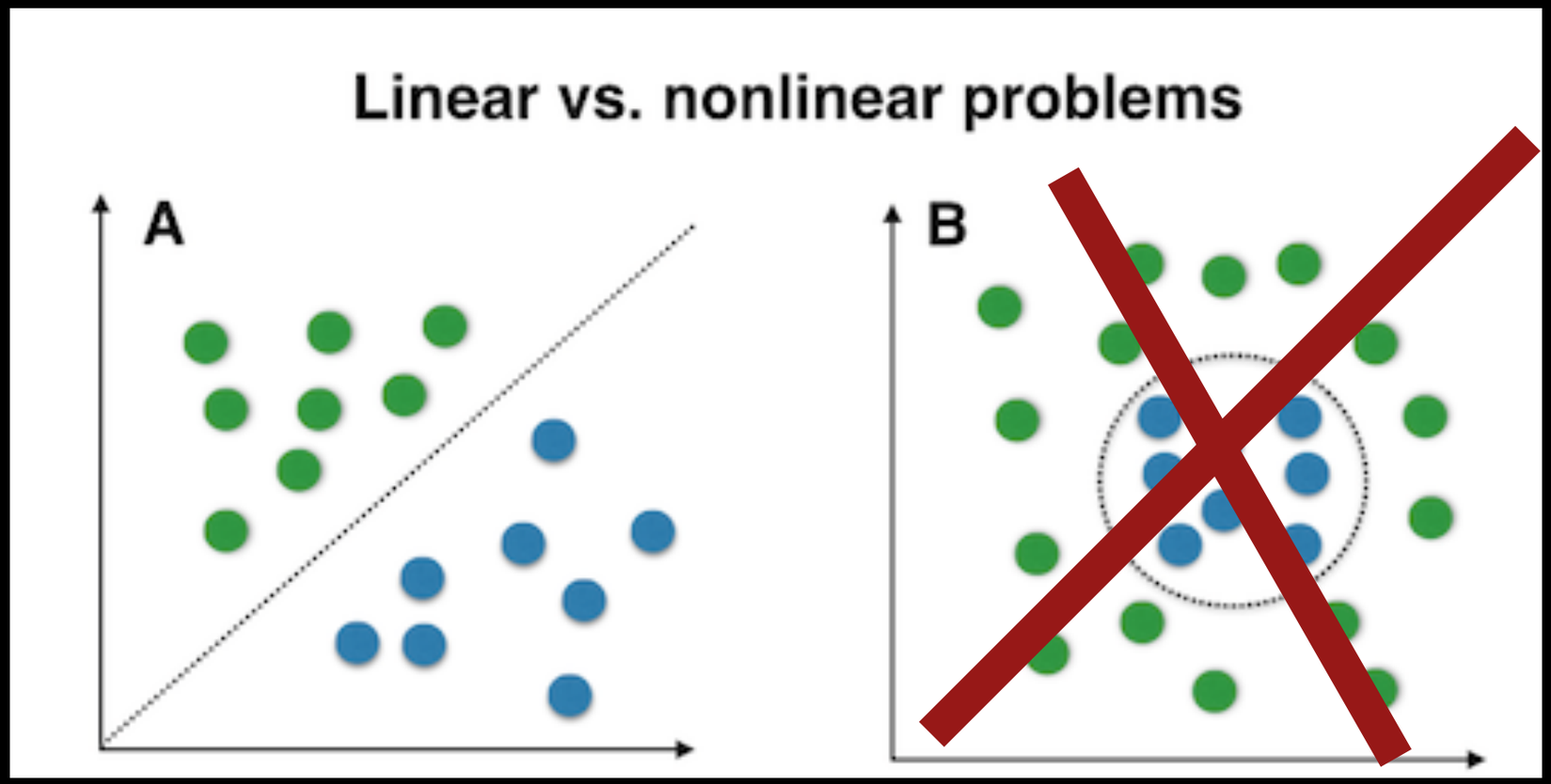


$$o(x_1, \ldots, x_n) = \begin{cases} 1 & \text{if } w_0 + w_1 x_1 + \cdots + w_n x_n > 0 \\ -1 & \text{otherwise.} \end{cases}$$

Exercises

https://github.com/ericpostma/ep
DEP-HO1.pdf
DEP-HO2.pdf
DEP-HO3.pdf

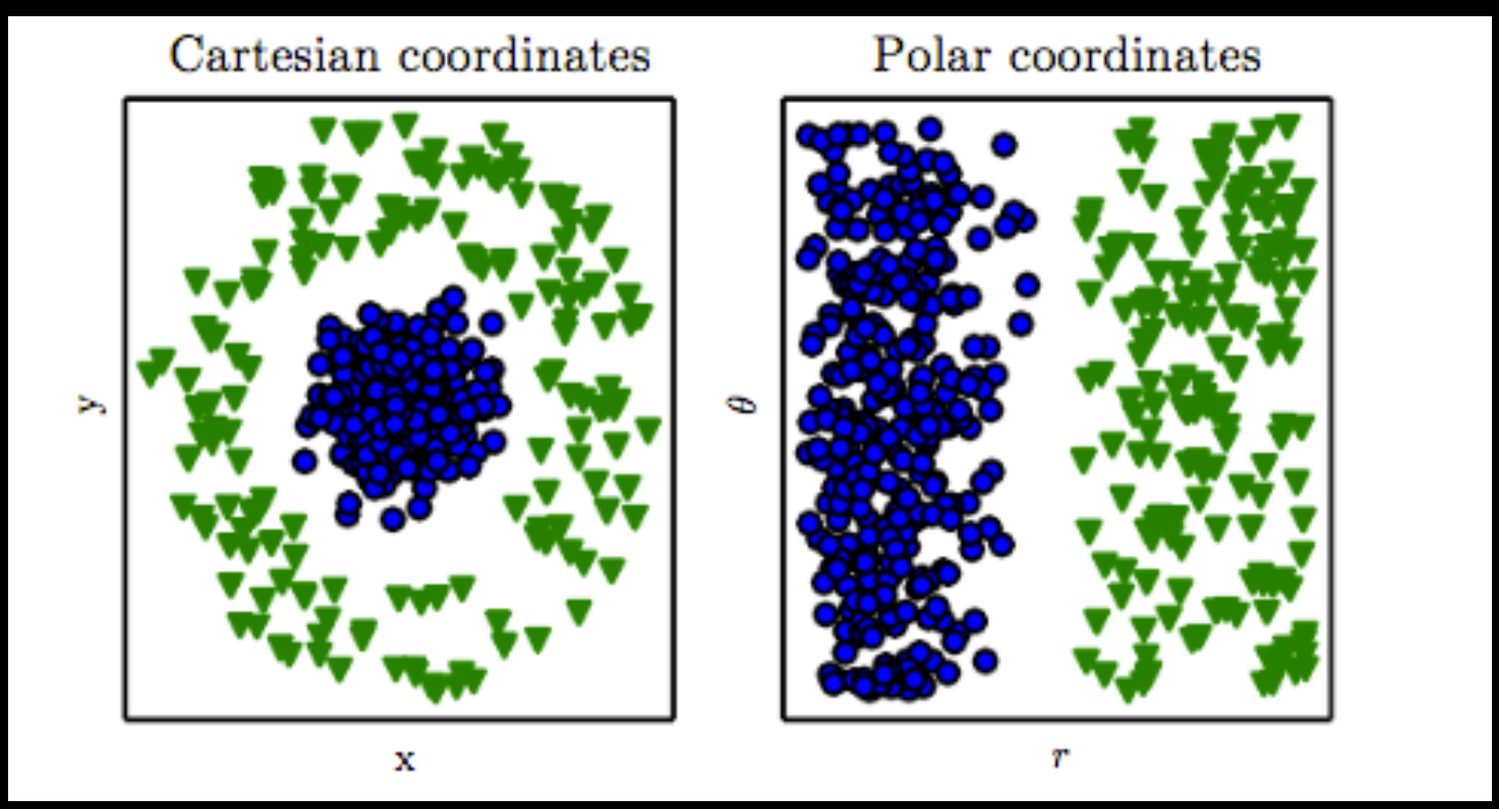
Linear separability



The importance of representation

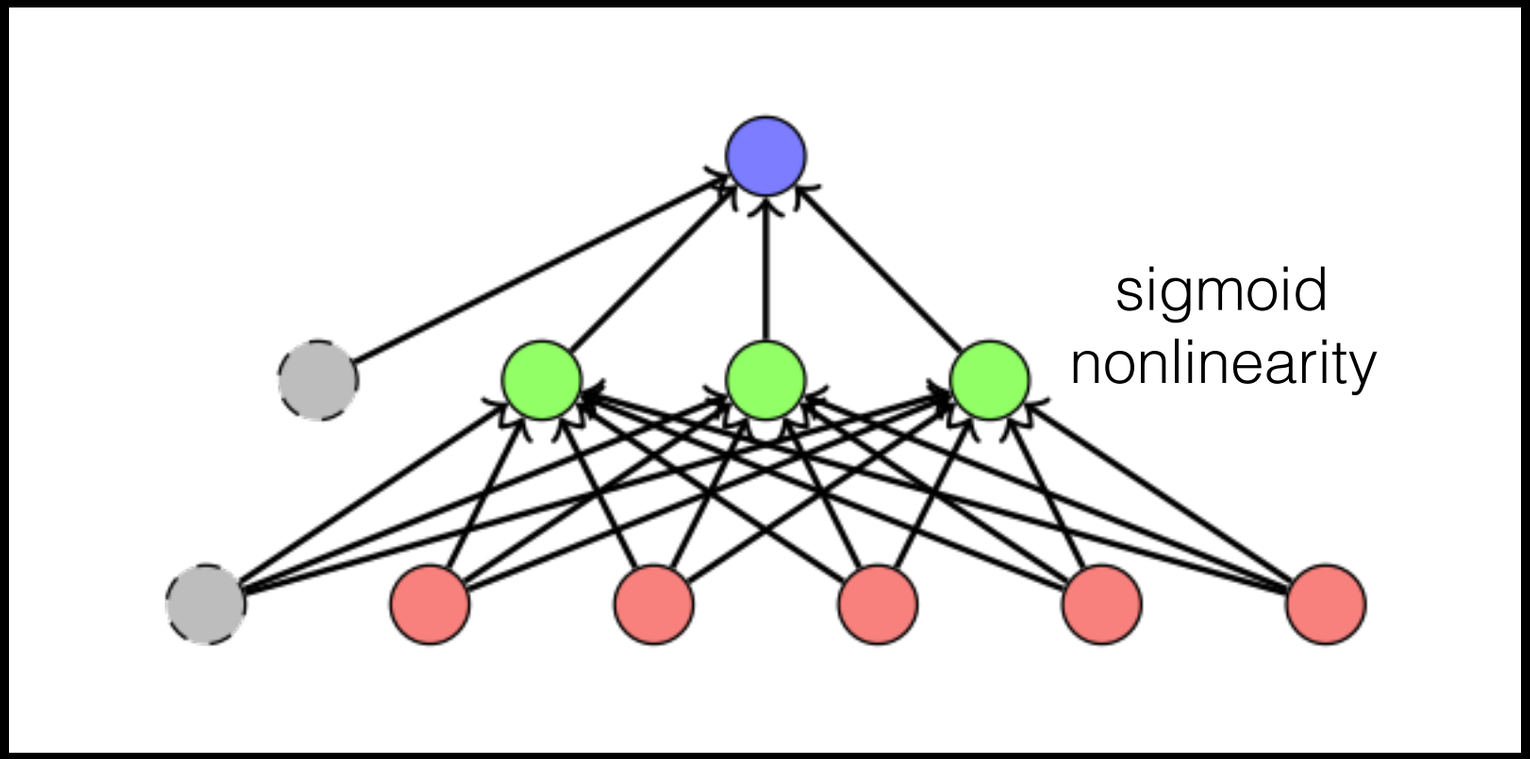
Perceptron can't classify this

Perceptron can classify this



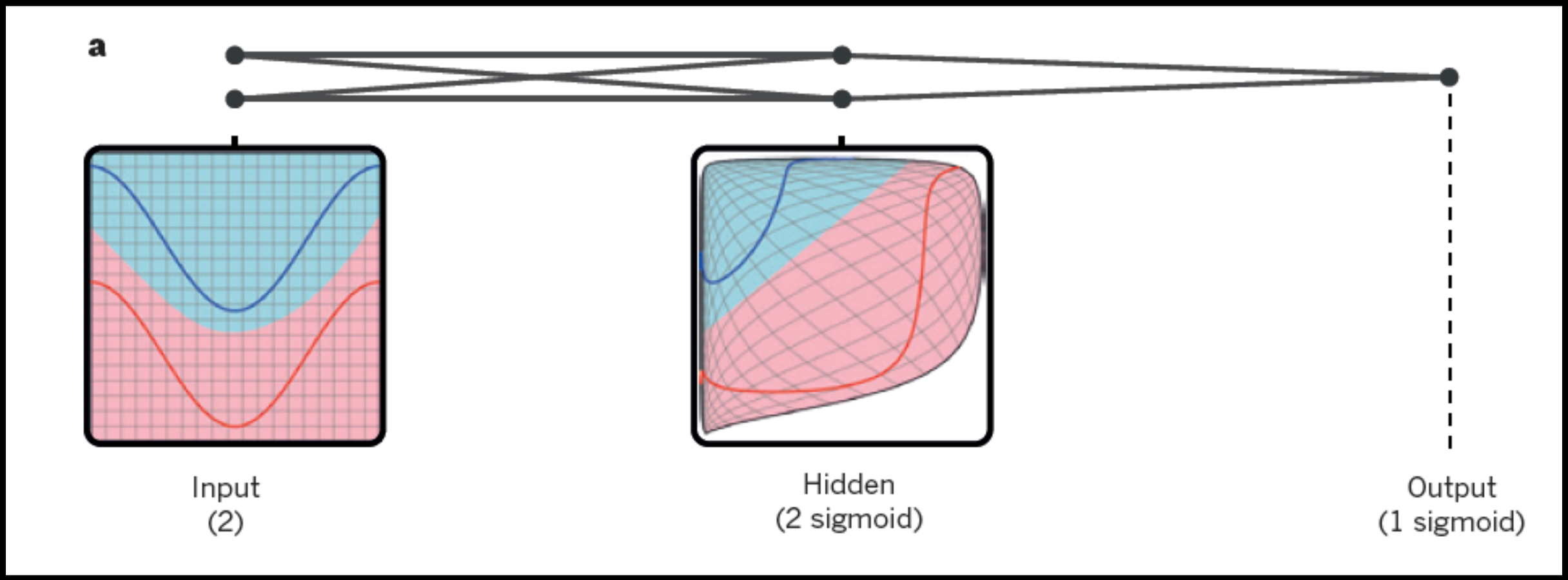
same task, different representation

Stacking Perceptrons



Main challenge (in the period 1960-1988):
How to automatically adapt the weights.

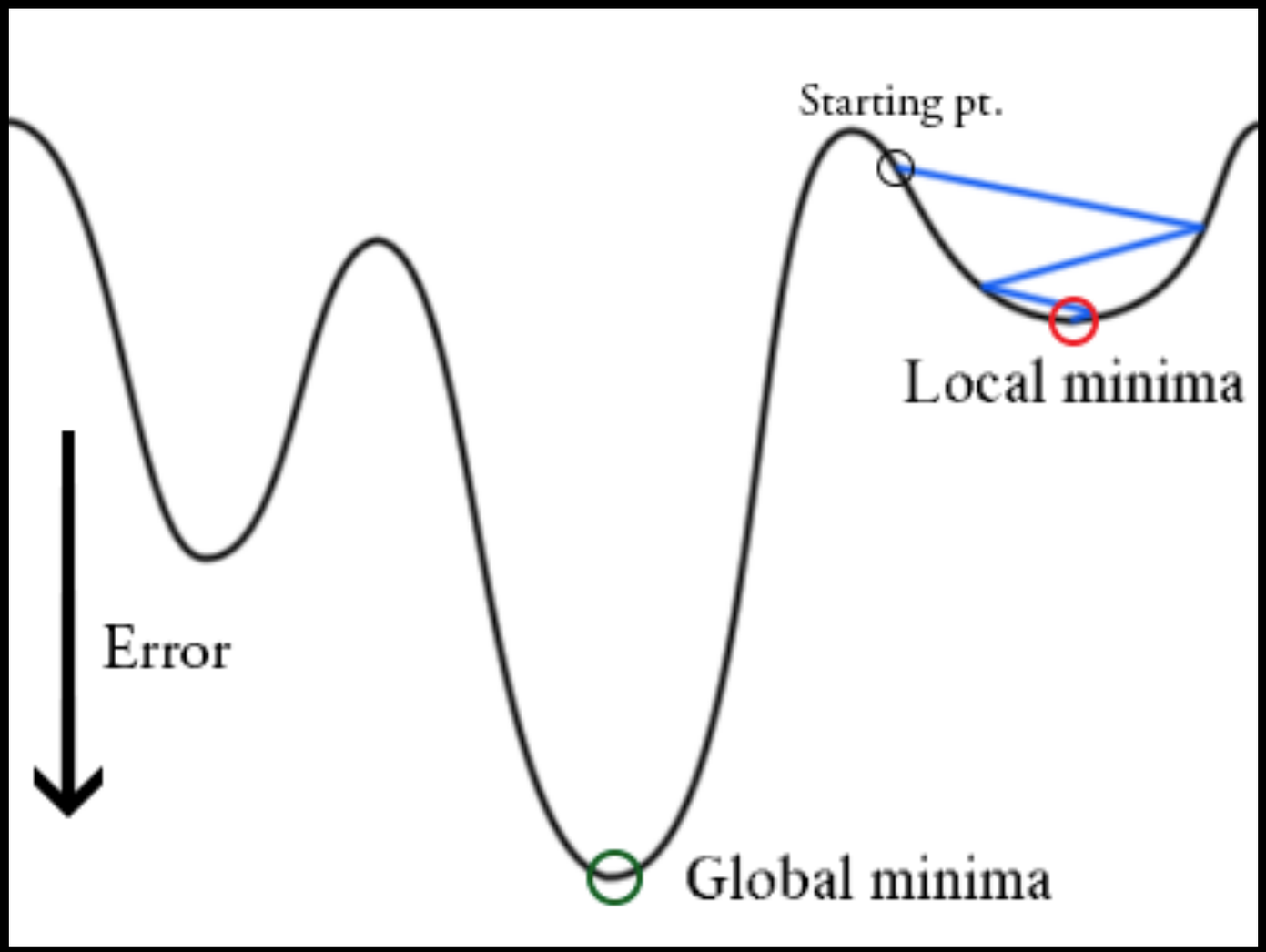
Multilayer Perceptron (1988)



Automatically Learns Non-Linear Mappings

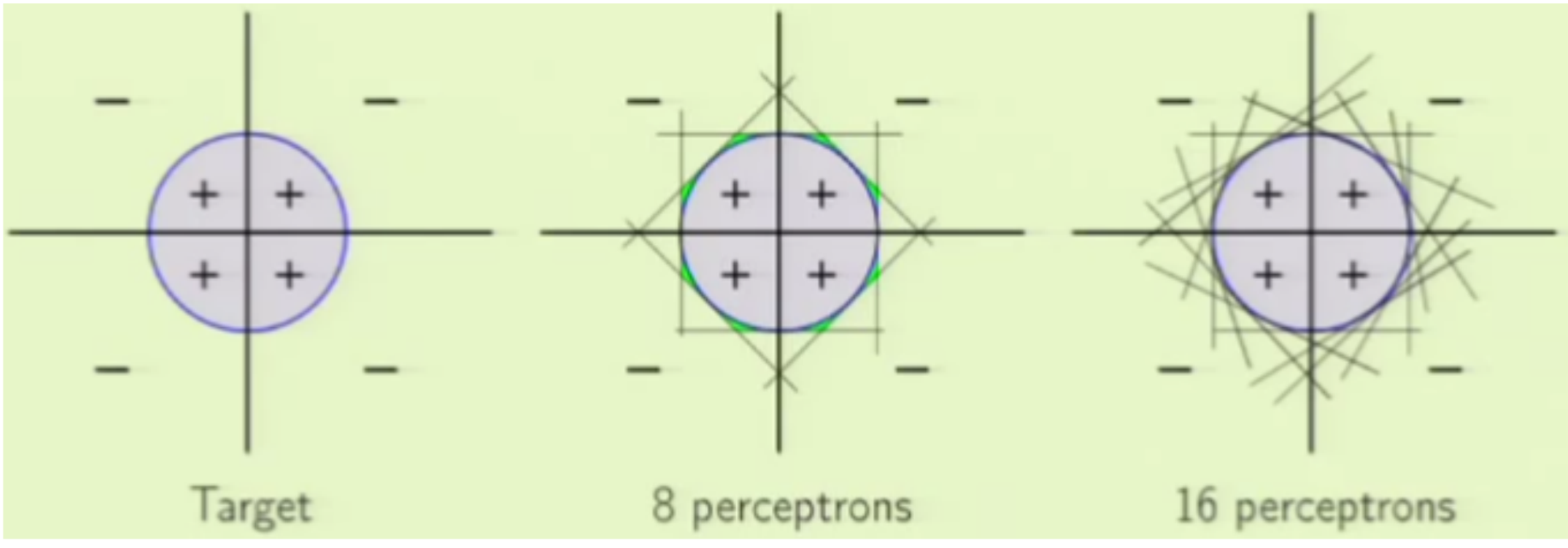
Gradient Descent

- Backpropagation (generalised delta rule)



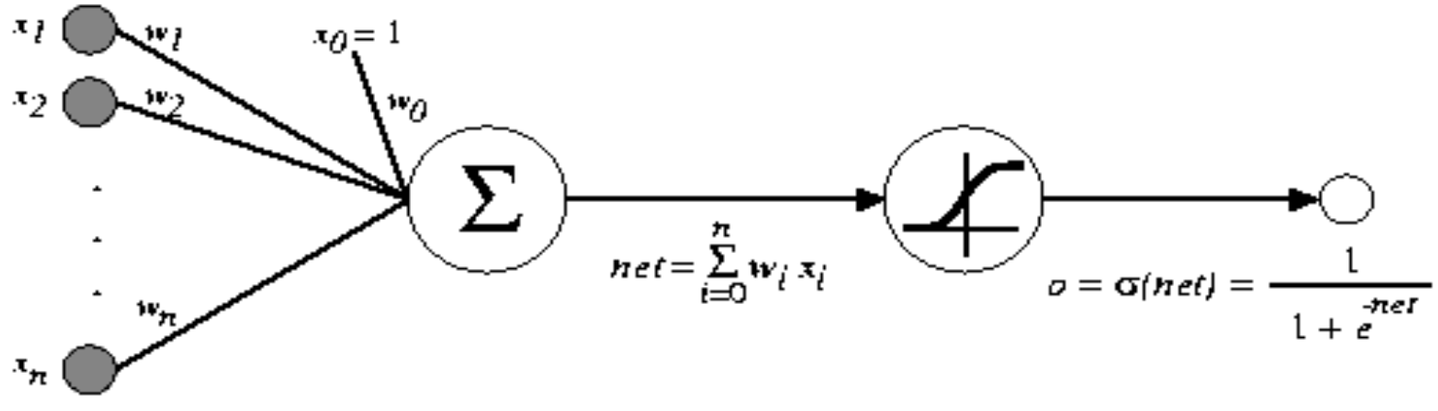
Coping with the limits of perceptrons

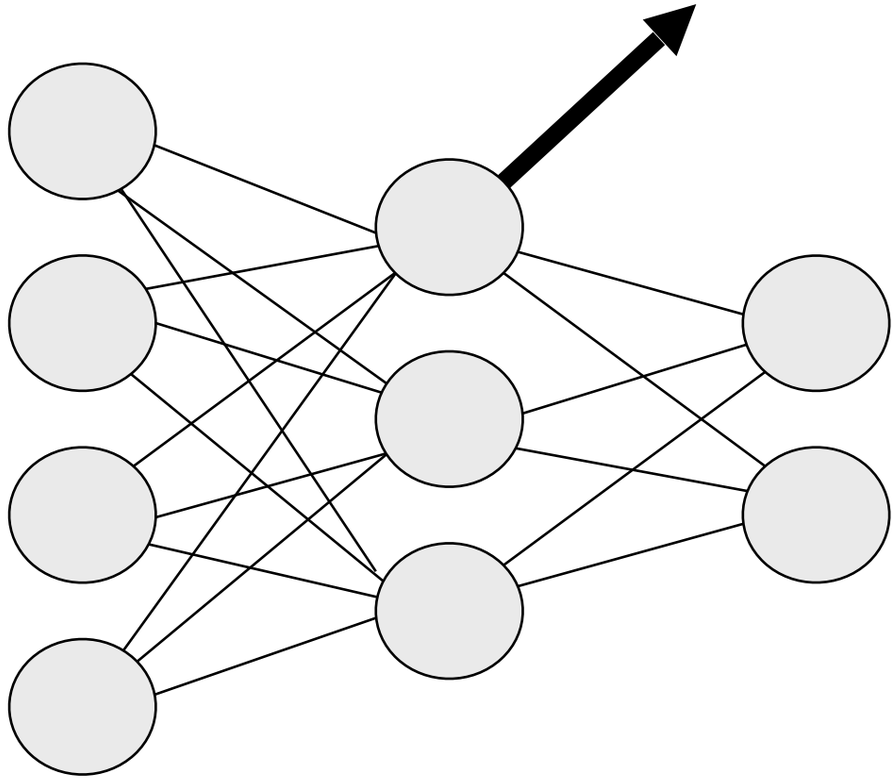
- Stacking perceptrons



what do these stacked perceptrons look like?

The Multilayer Perceptron





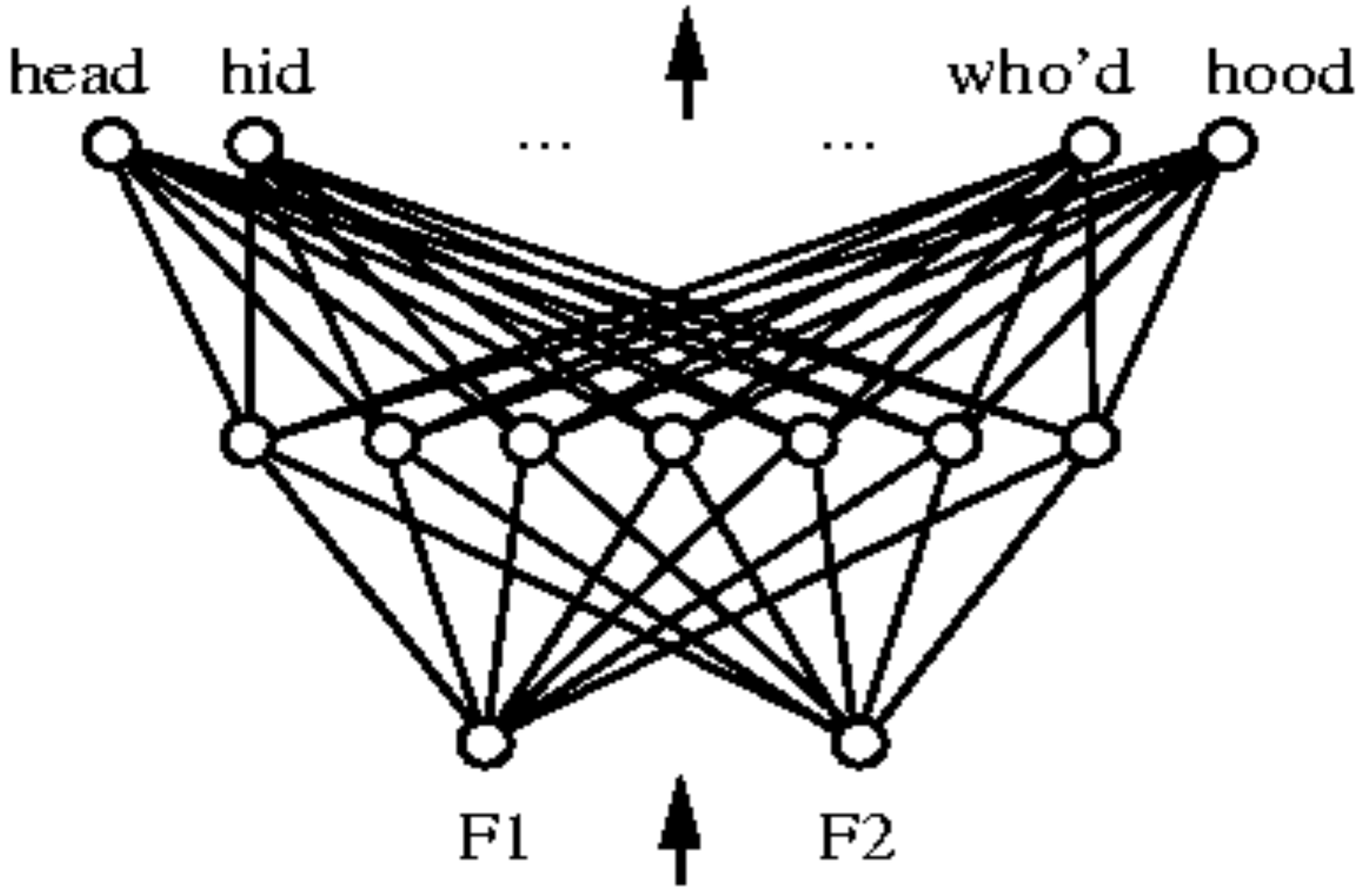
input hidden output

Training the MLP

- supervised learning
  - each training pattern: input I + desired output T
  - in each *epoch*: present all patterns
  - at each presentation: adapt weights
  - after many epochs convergence to a local minimum

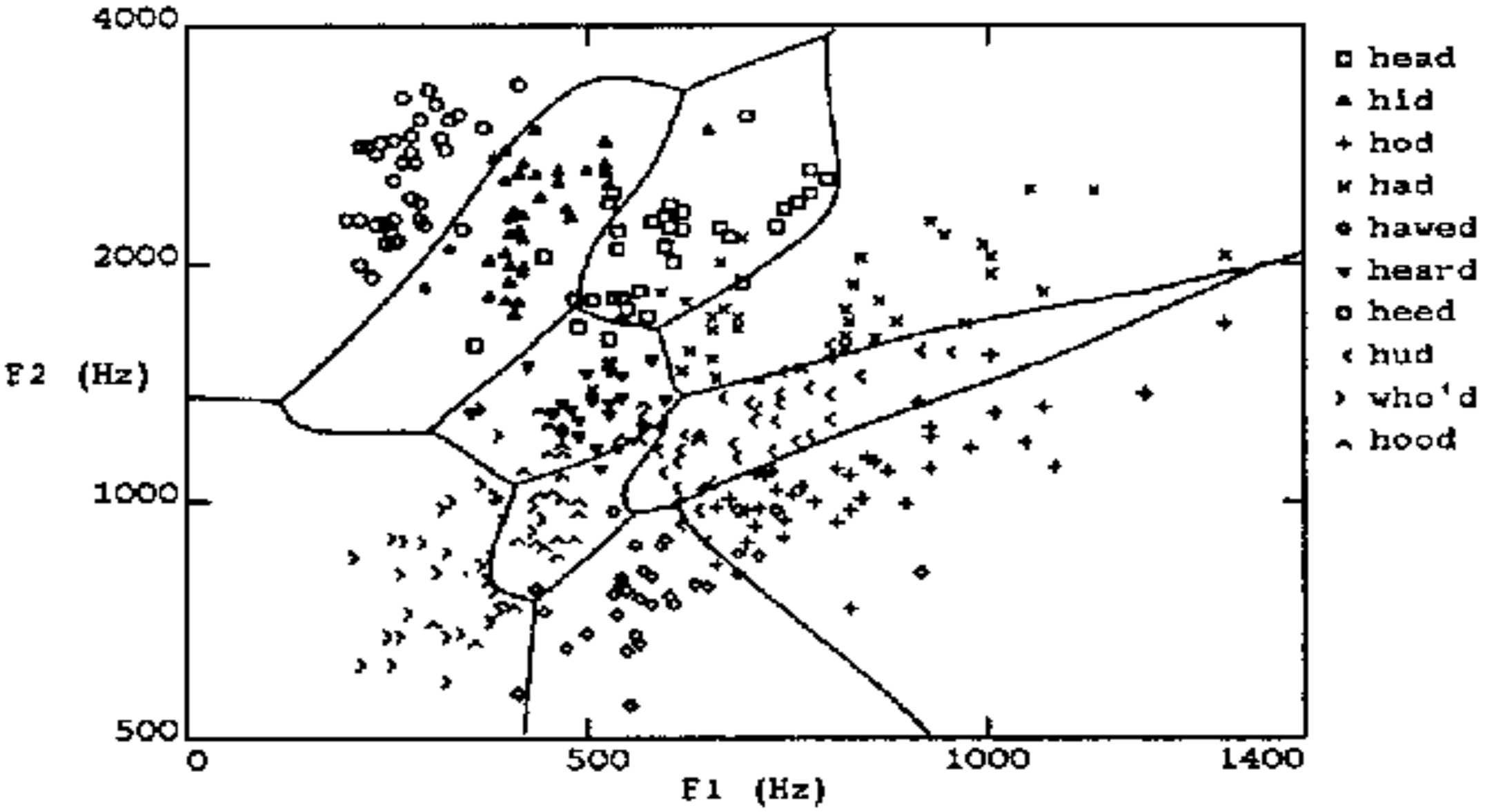
phoneme recognition with a MLP

Output: pronunciation

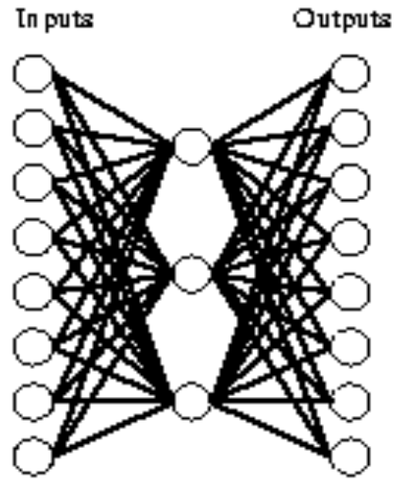


input: frequencies

Non-linear decision boundaries



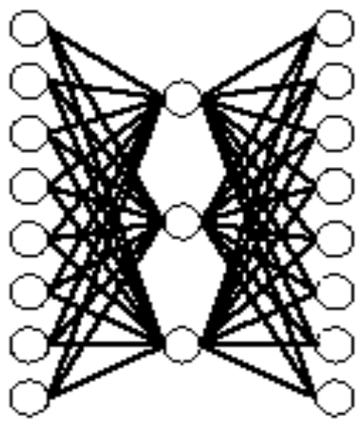
The *Autoencoder* *(Compression with an MLP)*



A target function:

Input		Output
10000000	$\rightarrow$	10000000
01000000	$\rightarrow$	01000000
00100000	$\rightarrow$	00100000
00010000	$\rightarrow$	00010000
00001000	$\rightarrow$	00001000
00000100	$\rightarrow$	00000100
00000010	$\rightarrow$	00000010
00000001	$\rightarrow$	00000001

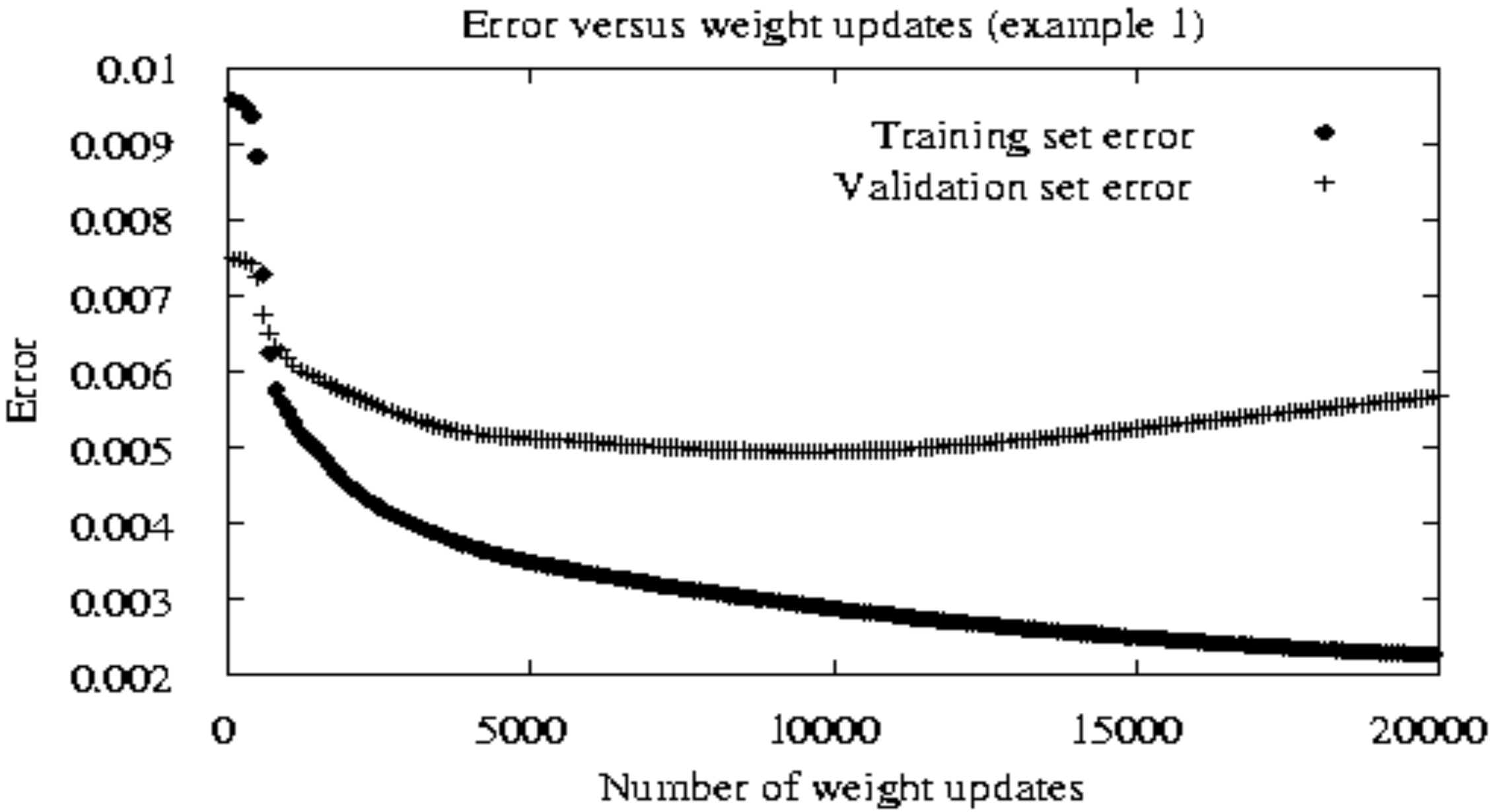
hidden representation



Learned hidden layer representation:

Input		Hidden Values				Output
10000000	→	.89	.04	.08	→	10000000
01000000	→	.01	.11	.88	→	01000000
00100000	→	.01	.97	.27	→	00100000
00010000	→	.99	.97	.71	→	00010000
00001000	→	.03	.05	.02	→	00001000
00000100	→	.22	.99	.99	→	00000100
00000010	→	.80	.01	.98	→	00000010
00000001	→	.60	.94	.01	→	00000001

Learning in the MLP



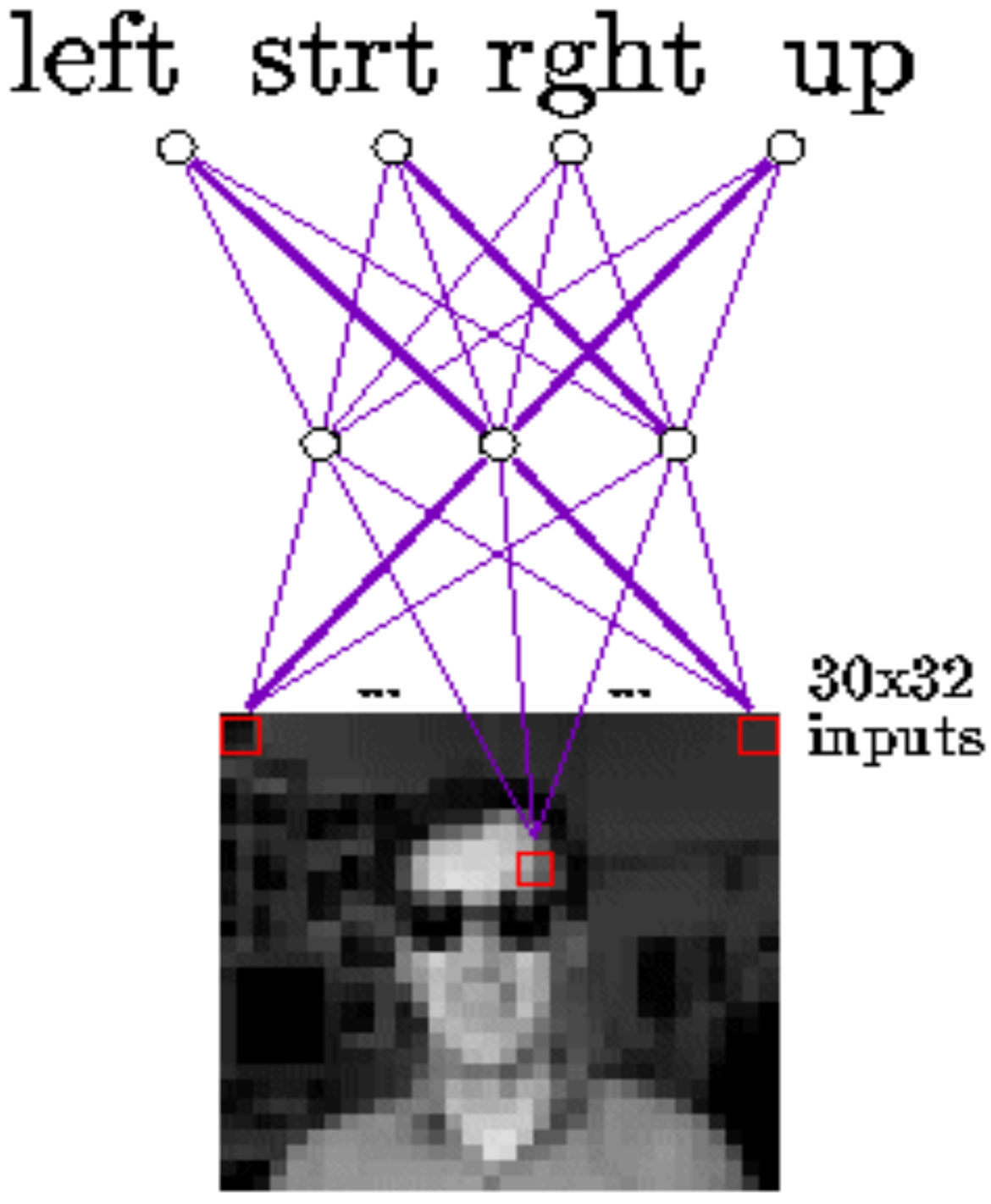
Preventing Overfitting

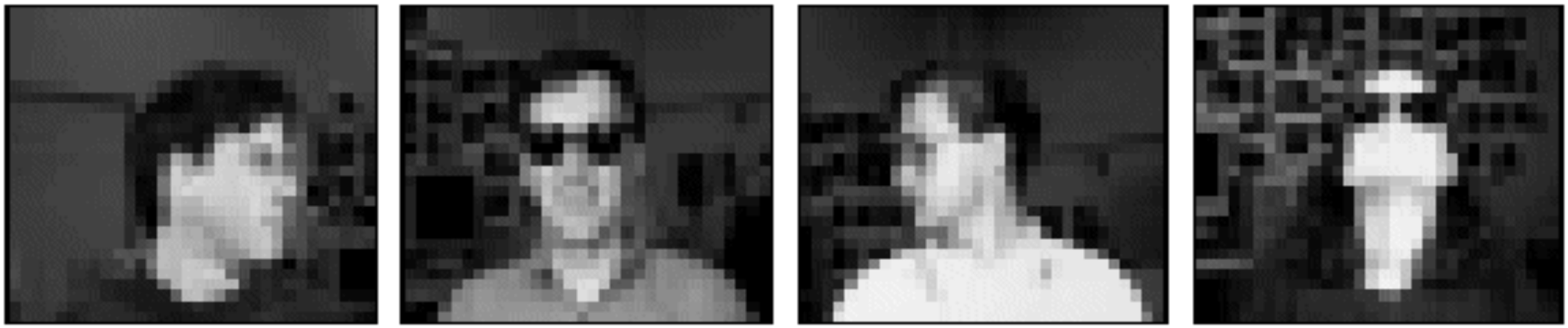
GENERALISATION

= performance on test set (unseen data)

- Early stopping
- Training, Validation and Test set
- *k*-fold cross validation
- Regularisation

Image Recognition with the MLP

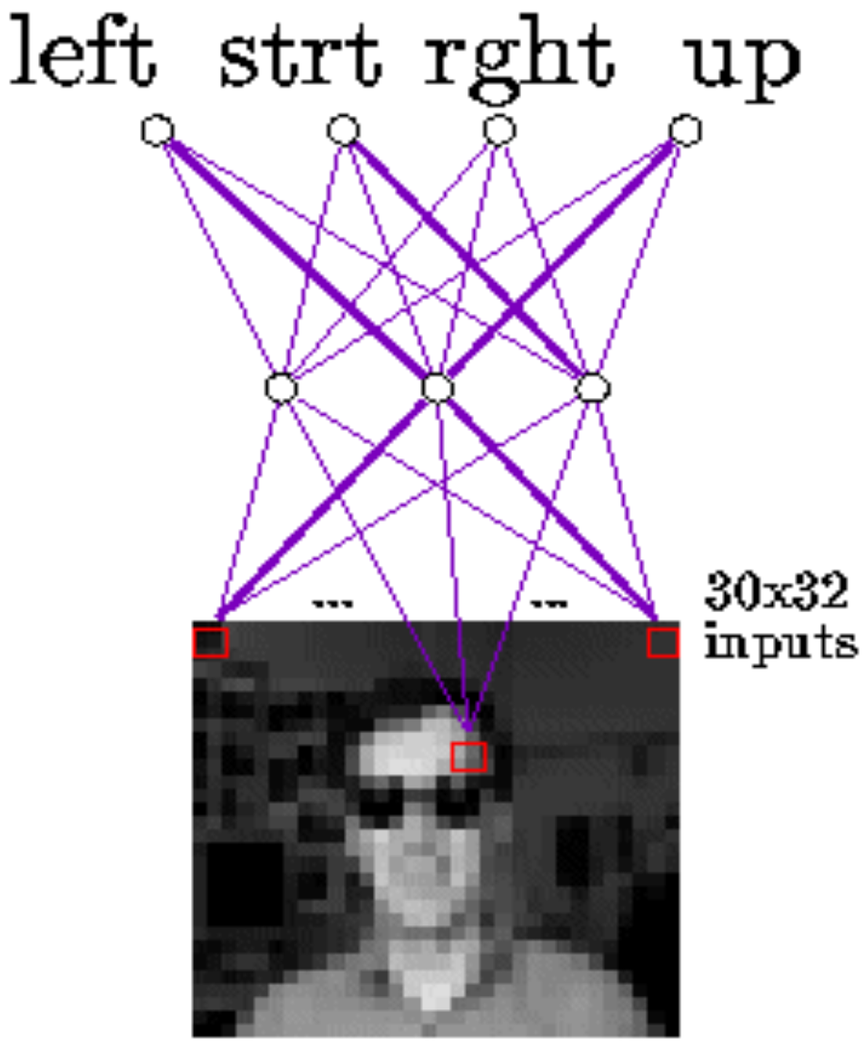


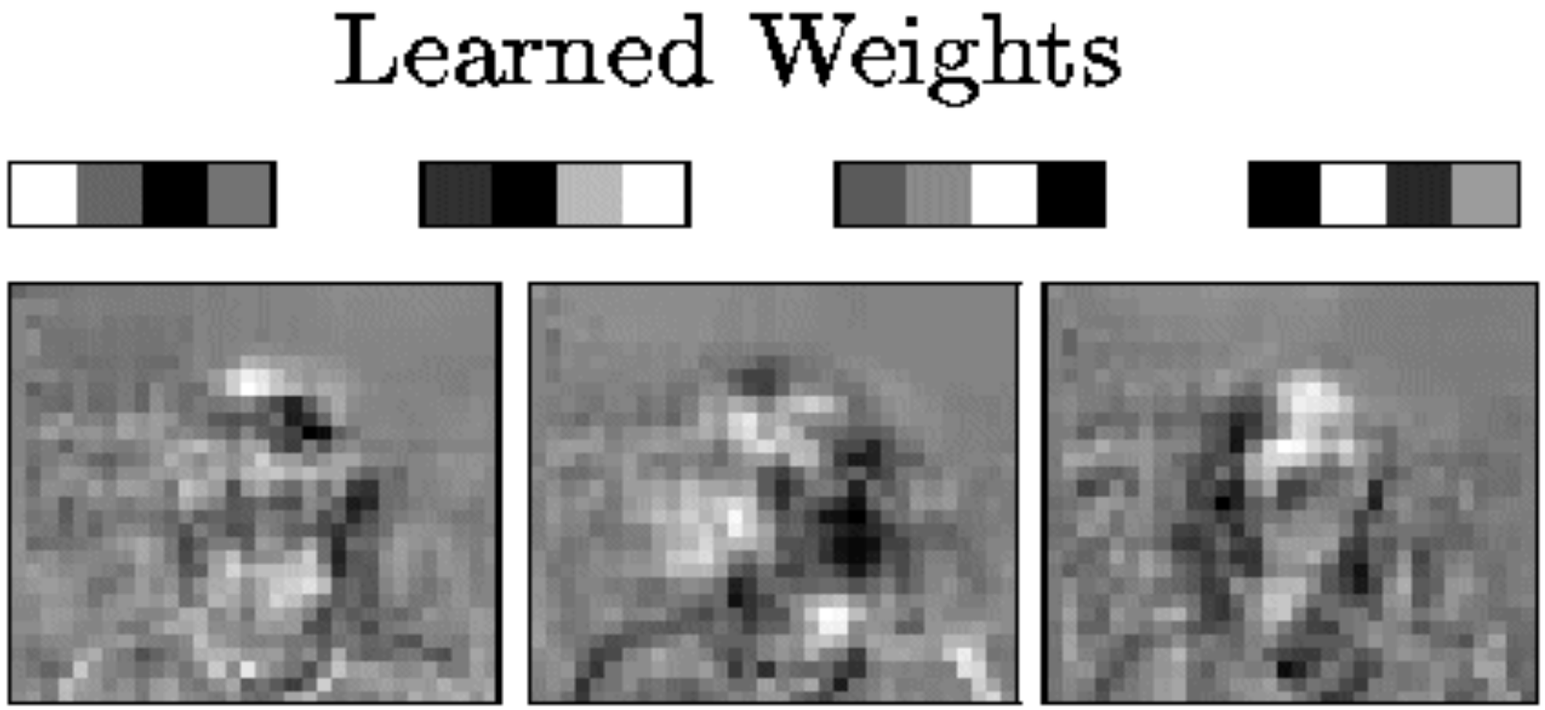


Typical input images

After training…

Hidden Representations





Questions

- The MLP consists of one (or more) hidden layers, i.e., hidden neurons with sigmoid transfer functions

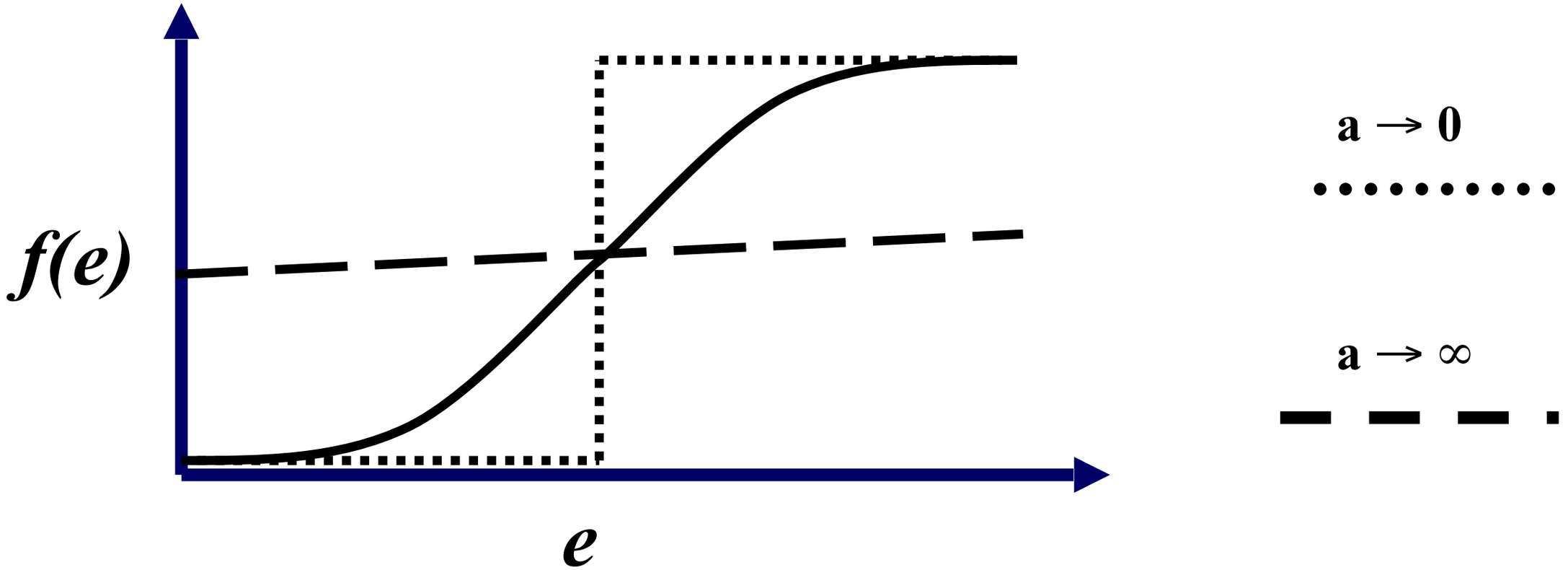
1. Can linear transfer functions be used? What would be the pro's and con's?

2. Can step transfer functions be used? What would be the pro's and con's?

RECAP PERCEPTRON...

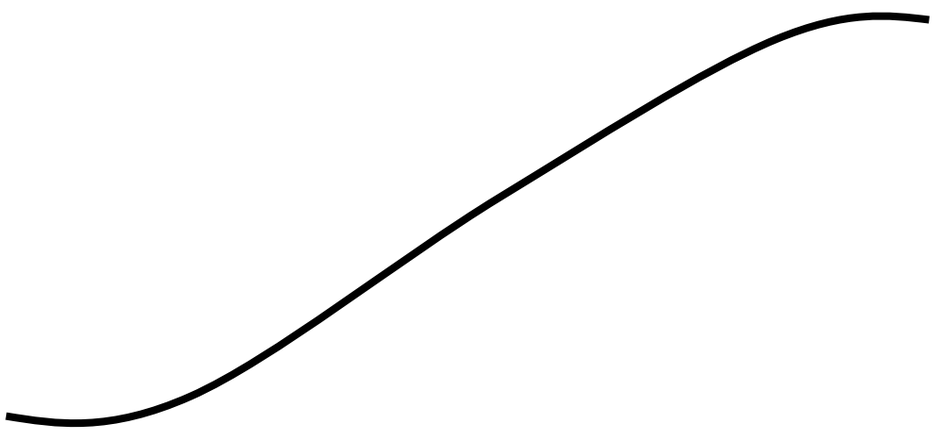
Sigmoid transfer (input-output) function

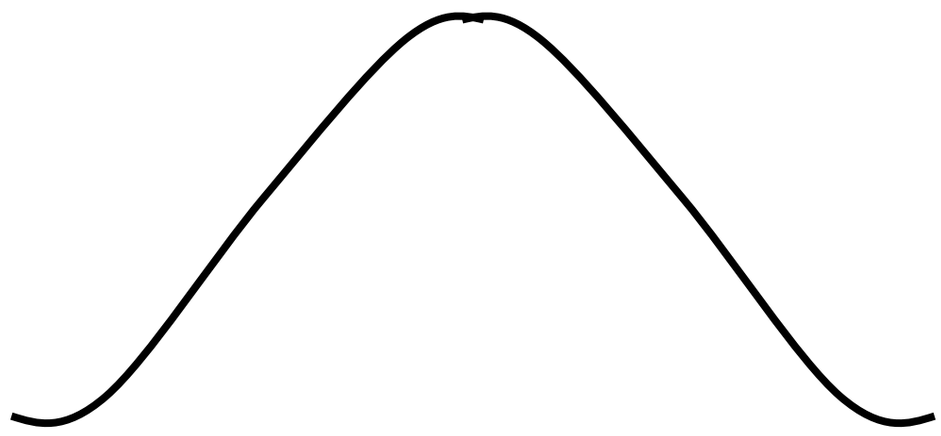
- nonlinear function: $$f(x) = \frac{1}{1 + e^{-x/a}}$$



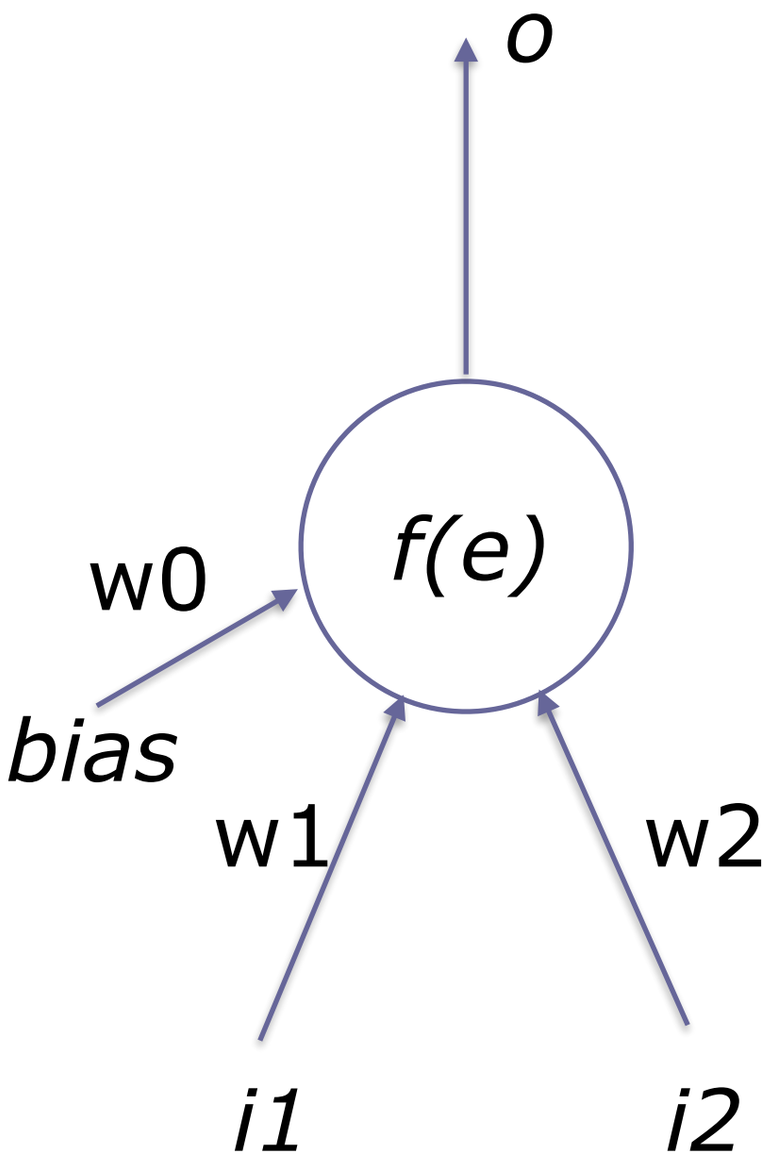
sigmoid transfer function

- May also be the **tanh** function (<-1,+1> instead of <0,1>)
- Derivative f’(x) = f(x) [1 – f(x)]





Perceptron



$$o = f\left(\sum_{i=0}^{I} w_i\, i_i\right) = f(e)$$

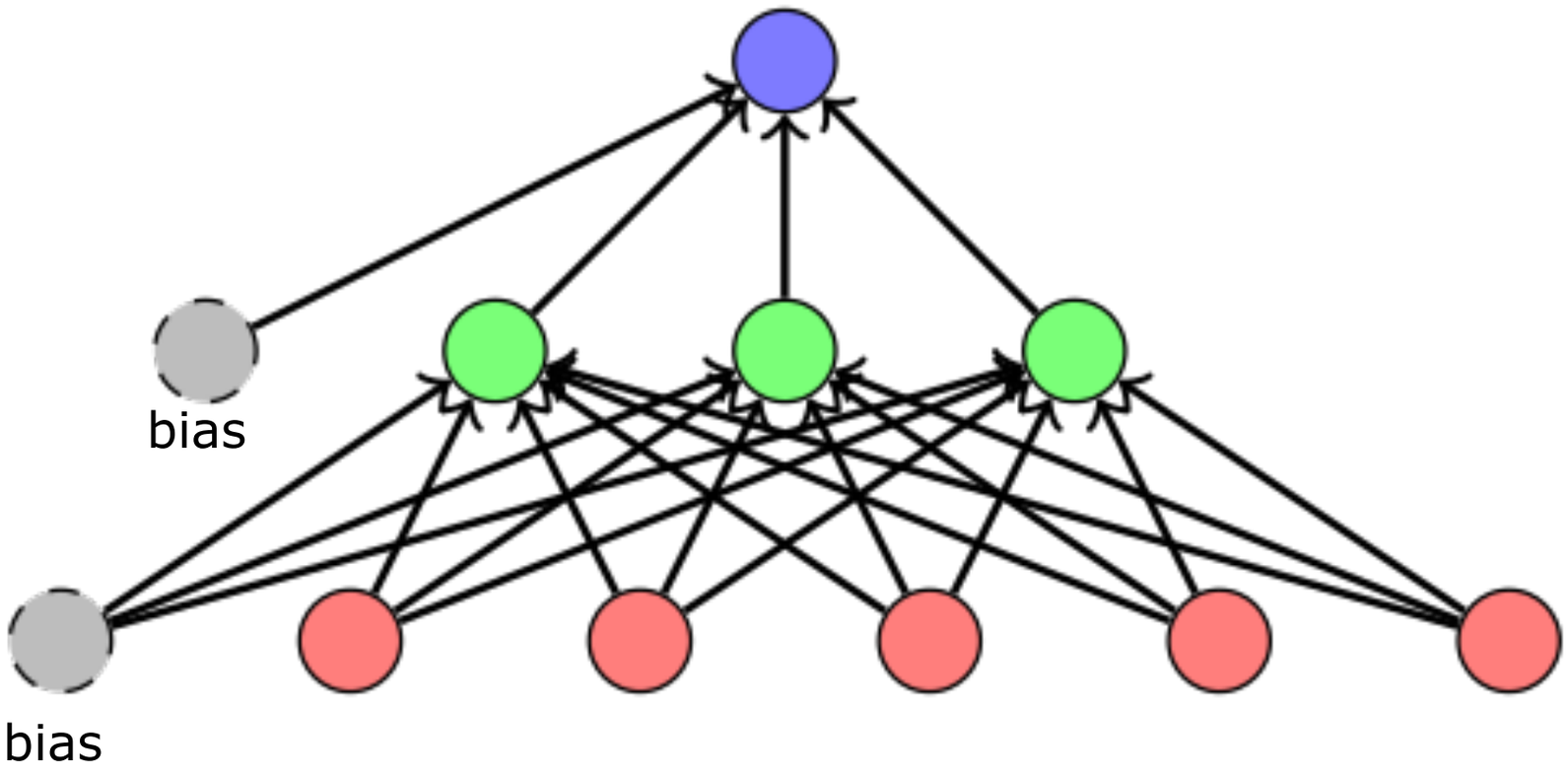
Derivation of the delta learning rule (for a sigmoid transfer function)

$$E = \sum_{p=1}^{P} \frac{1}{2}\left(t_p - o_p\right)^2$$

$$\Delta w_k = -\eta \frac{\partial E}{\partial w_k} = \eta \sum_{p=1}^{P} \left(t_p - o_p\right) f'\left(e_p\right) i_k = \eta \sum_{p=1}^{P} \delta\, i_k$$

Question

- How does the rate of weight change depend on the activation value of the neuron?

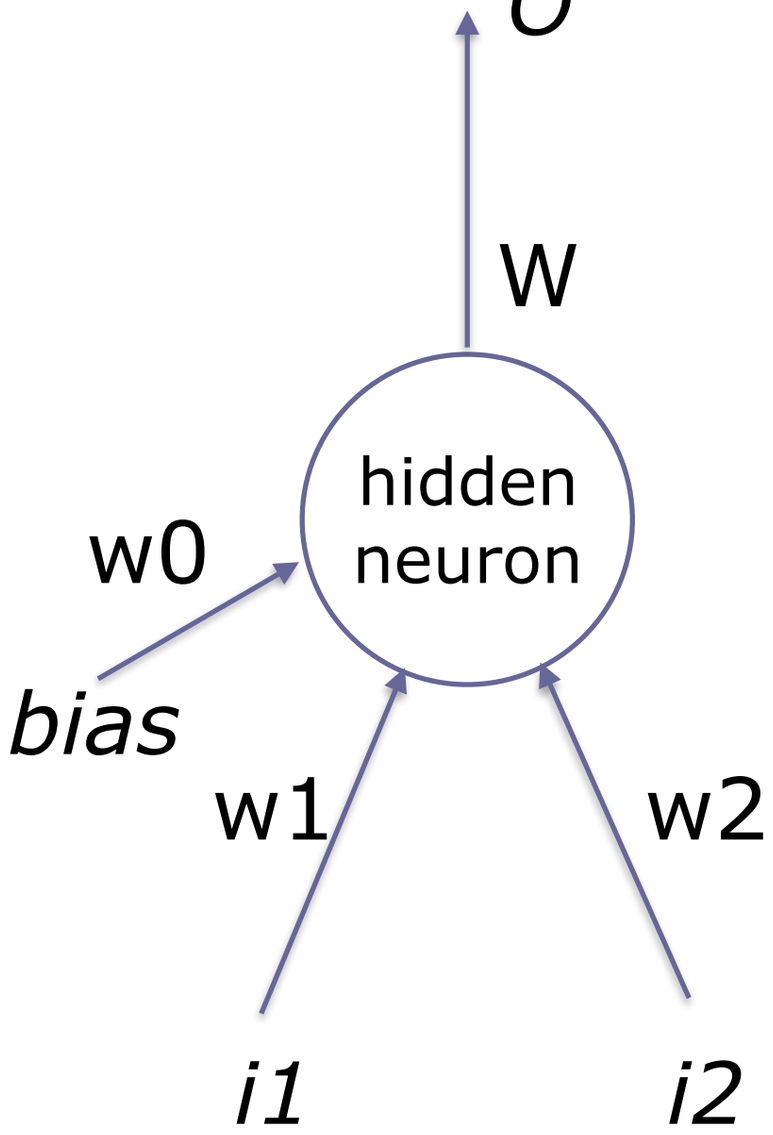


output neuron(s)

hidden neurons

inputs

Multilayer Perceptron



$$o_k = f\left(\sum_{j=0}^{H} W_{kj}\, h_j\right) = f(e_k)$$

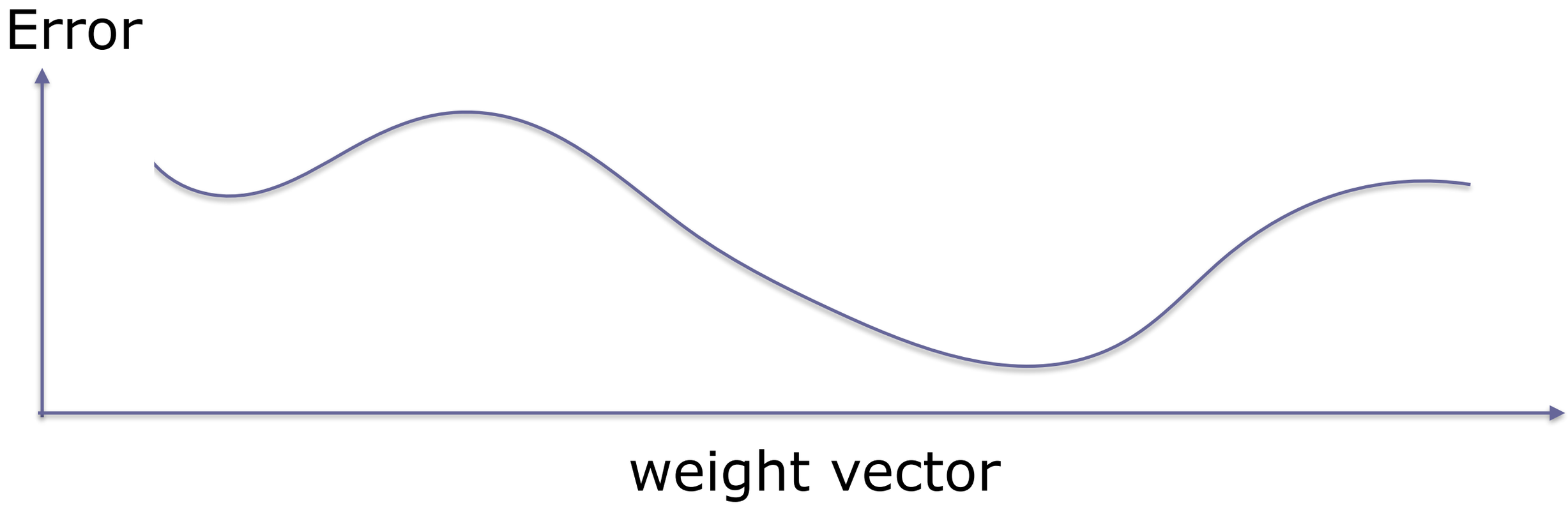
large W —> hidden to output weights

$$h_j = f\left(\sum_{i=0}^{I} w_{ji}\, i_i\right) = f(e_j)$$

small w —> input to hidden weights

Training the MLP

- Gradient Descent
- Error function is not convex
- Local minima



MLP with one hidden layer (mathematical equation)

O = number of output neurons
H = number of hidden neurons
I = number of inputs

$$o_k = f\left(\sum_{k=1,j=0}^{O,H} W_{kj}\, f\left(\sum_{j=1,i=0}^{H,I} w_{ji}\, i_i\right)\right)$$

output of k-th output neuron

hidden-to-output weights

input-to-hidden weights

Error function of MLP

$$E = \sum_{p=1,k=1}^{P,O} \frac{1}{2}\left(t_{pk} - o_{pk}\right)^2$$

$$E_{pk} = \frac{1}{2}\left(t_{pk} - o_{pk}\right)^2$$

$$E_{pk} = \frac{1}{2}\left(t_{pk} - f\left(\sum_{k=1,j=0}^{O,H} W_{kj}\, f\left(\sum_{j=1,i=0}^{H,I} w_{ji} i_{pi}\right)\right)\right)^2$$

Derivation of the generalised delta learning rule

(MLP with one hidden layer)

$$\Delta W_{kj} = -\eta \frac{\partial E}{\partial W_{kj}} = \eta \sum_{p=1}^{P} (t_{pk} - o_{pk}) f'(e_{pk}) h_{pj} = \eta \sum_{p=1}^{P} \delta_{pk} h_{pj}$$

the adaptation of the hidden to output weights is identica
to that of the perceptron weights (except for h <—> i)

Adaptation of input to hidden weights

- More complicated due to non-linearity of the hidden neuron transfer function

- Makes use of the chain rule

The chain rule may be written, in Leibniz's notation, in the following way. If a variable *z* depends on the variable *y*, which itself depends on the variable *x*, so that *y* and *z* are therefore dependent variables, then *z*, via the intermediate variable of *y*, depends on *x* as well. The chain rule then states,

$$\frac{dz}{dx} = \frac{dz}{dy} \cdot \frac{dy}{dx}.$$

https://en.wikipedia.org/wiki/Chain_rule

chain rule

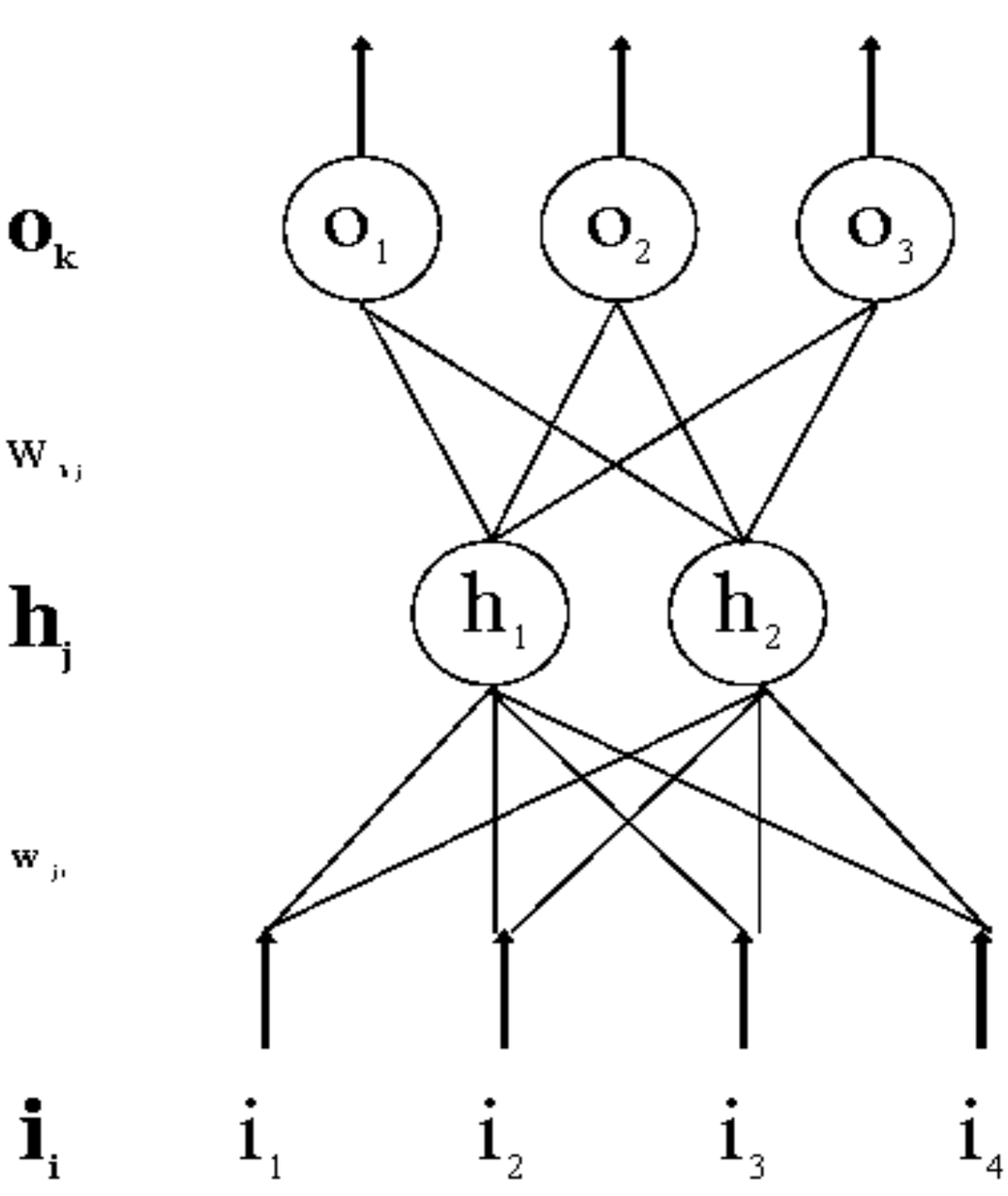
$$\Delta w_{ji} = -\eta \frac{\partial E}{\partial w_{ji}} = -\eta \frac{\partial E}{\partial h_{pj}} \frac{\partial h_{pj}}{\partial w_{ji}}$$

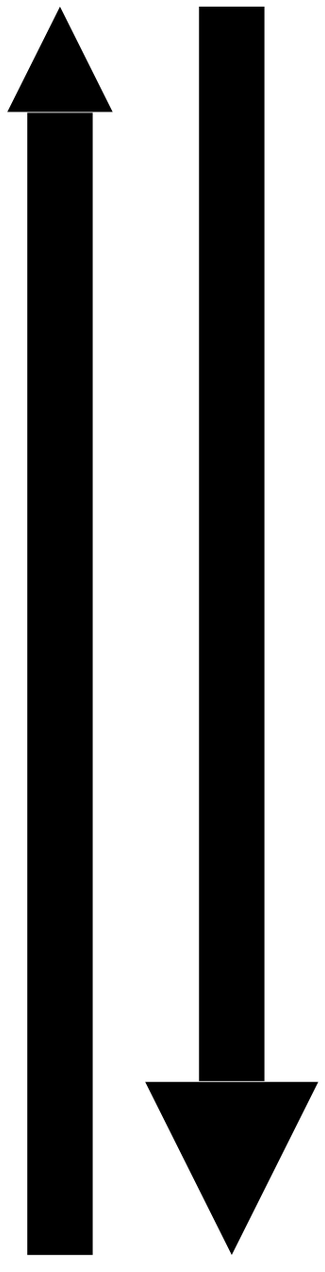
$$= \eta \sum_{p=1,k=1}^{P,H} (t_{pk} - o_{pk}) f'(e_{pk}) W_{kj} f'(e_{pj}) i_{pi}$$

$$= \eta \sum_{p=1,k=1}^{P,H} \delta_{pk} W_{kj} f'(e_{pj}) i_{pi}$$

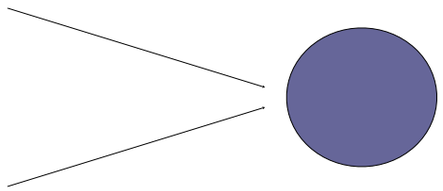
$$= \eta \sum_{p=1,k=1}^{P,H} \delta_{pj} i_{pi}$$

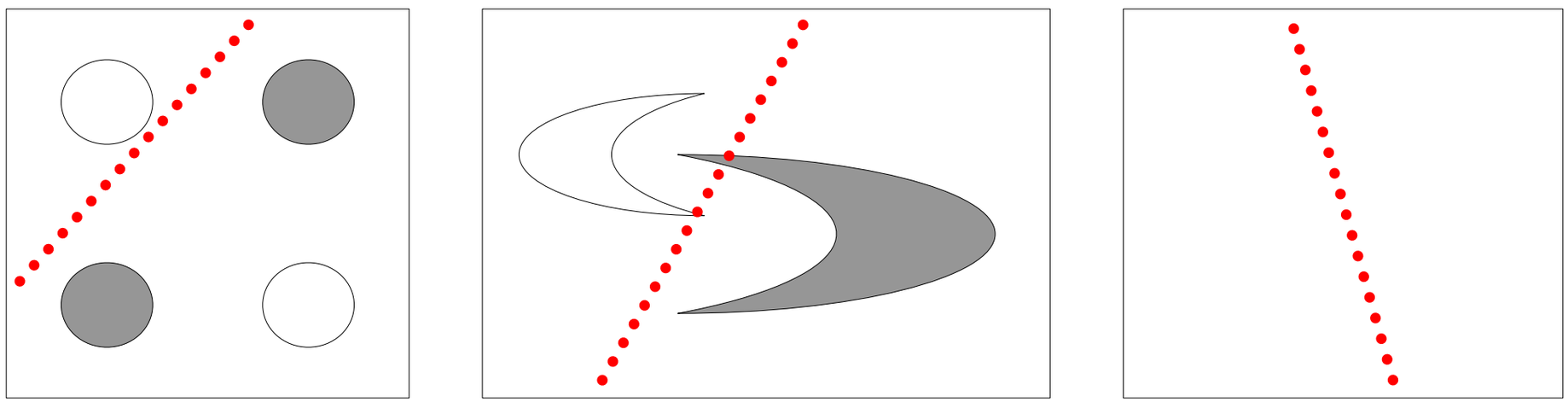
Forward and Backward Propagation





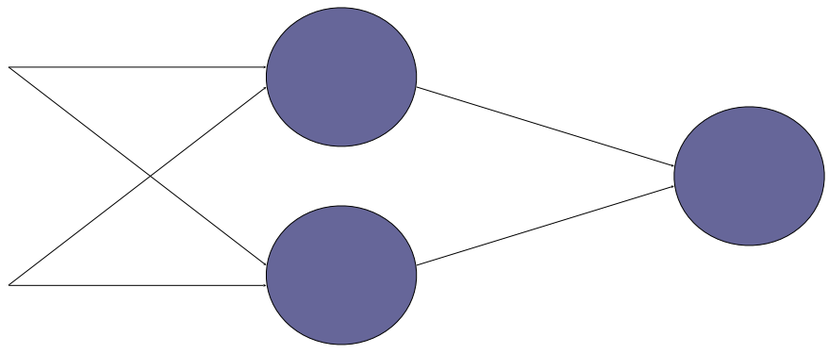
Decision boundaries of Perceptrons

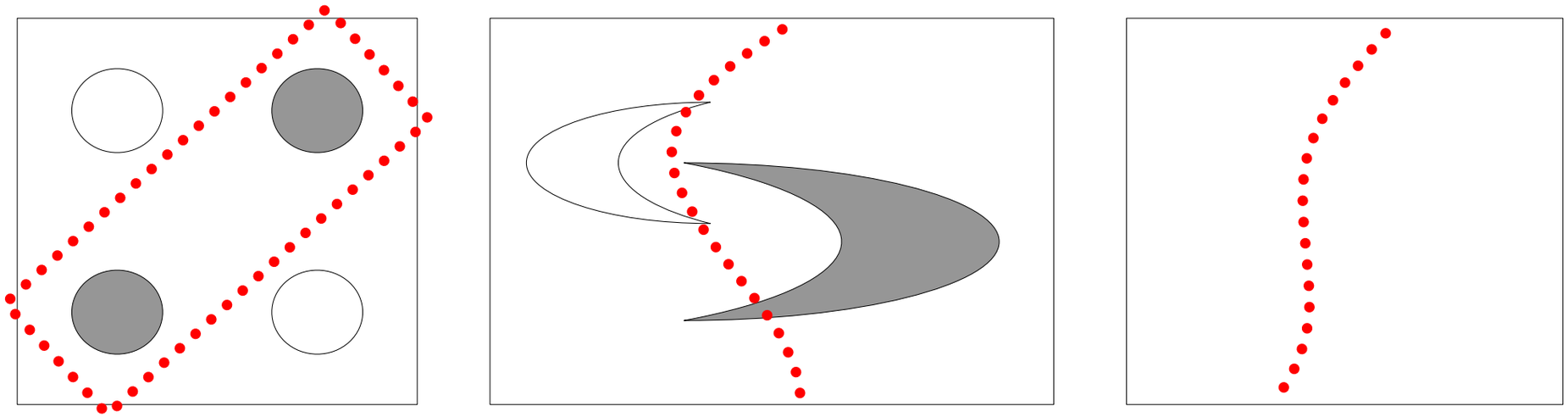




Straight lines (surfaces), linear separable

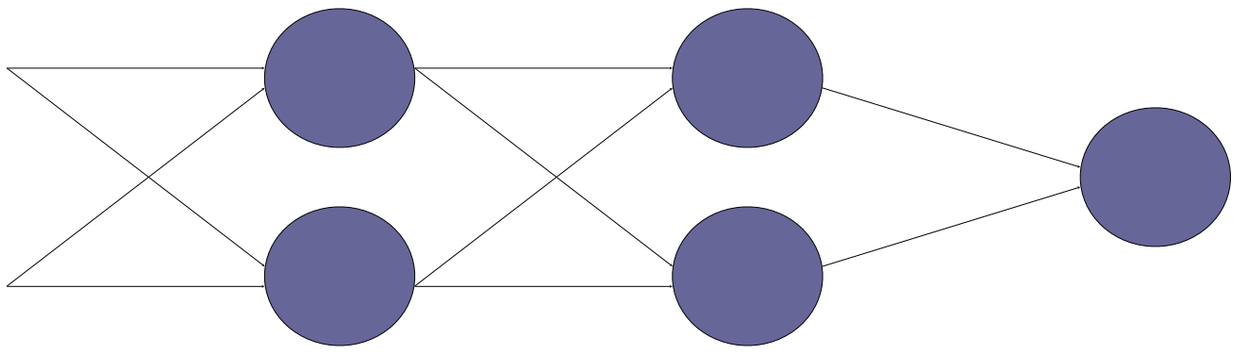
Decision boundaries of MLPs

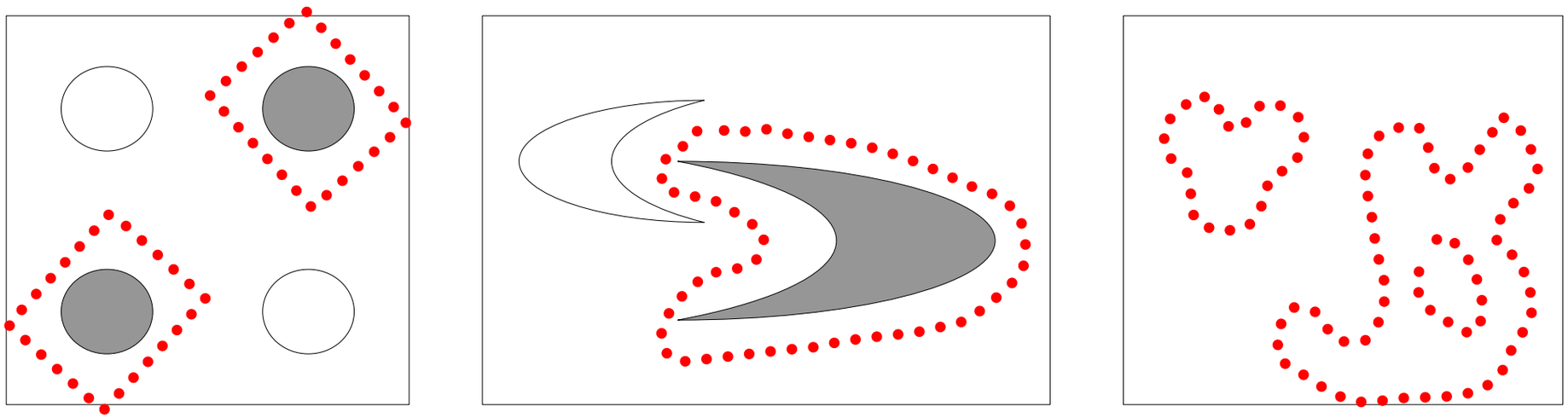




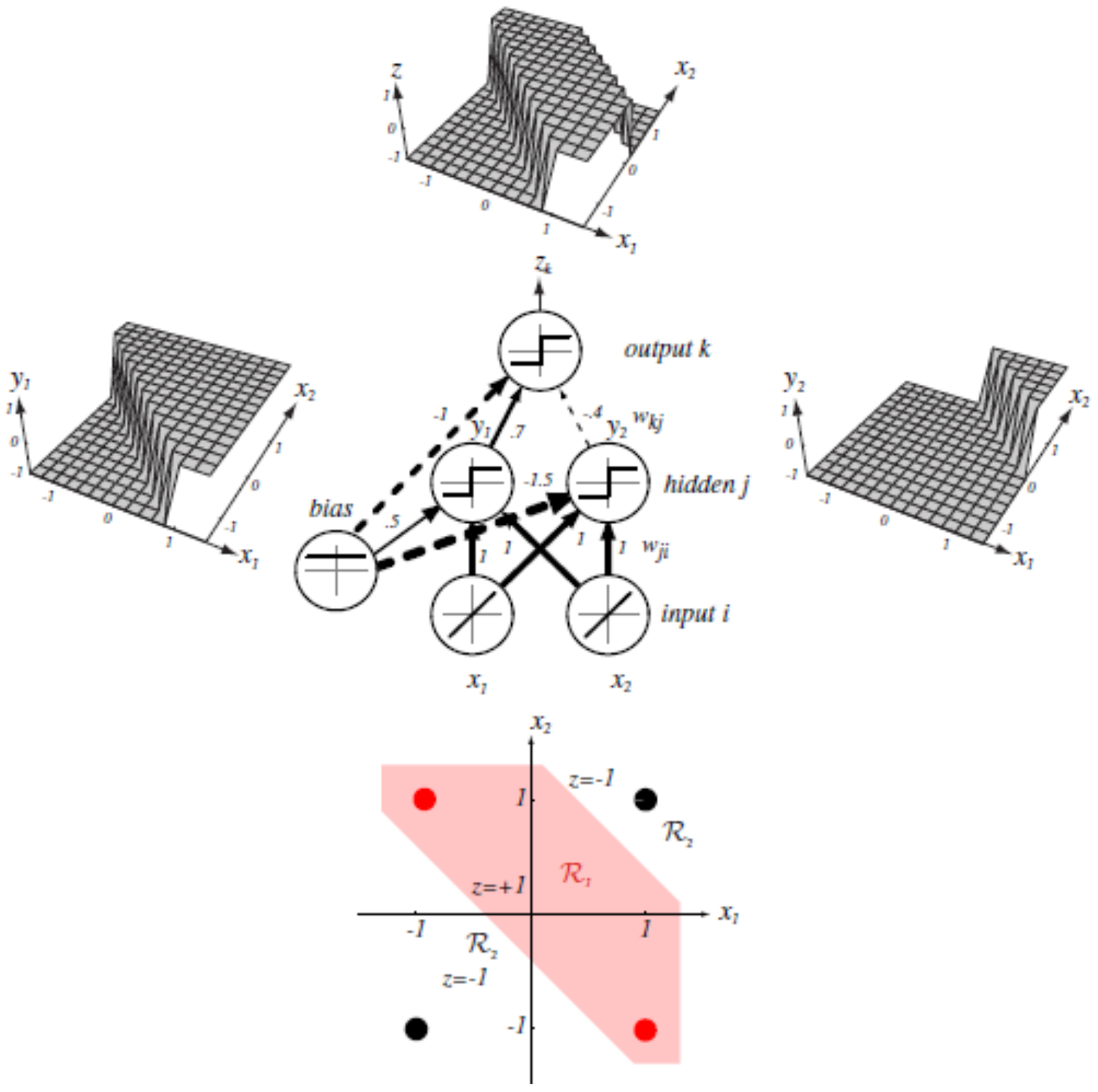
Convex areas (open or closed)

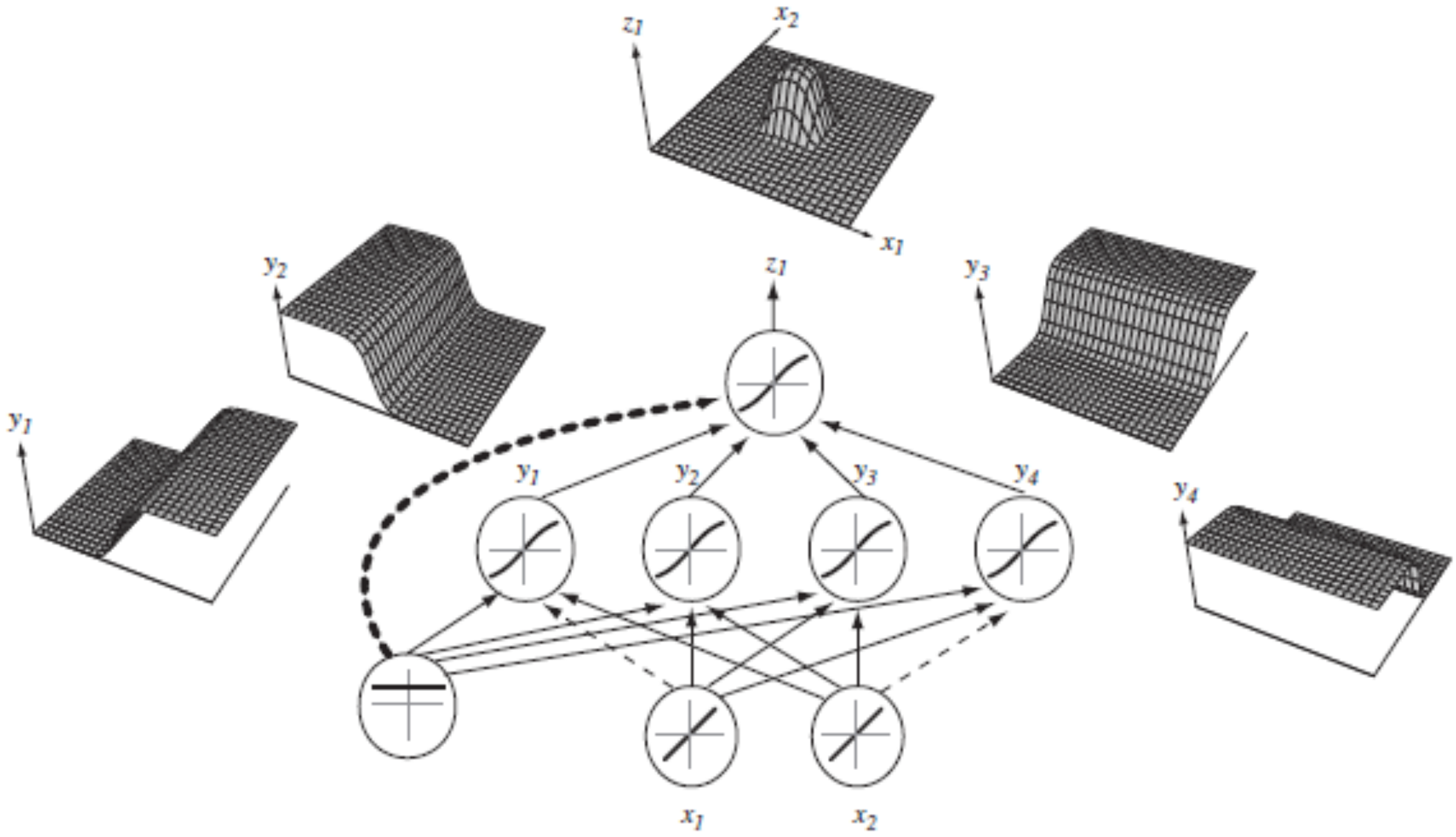
Decision boundaries of MLPs





Combinations of convex areas


z
x2
x1
y1
y2
output k
hidden j
input i
bias
wkj
wji
-1
.7
-.4
-1.5
.5
1
z=-1
z=+1
R1
R2

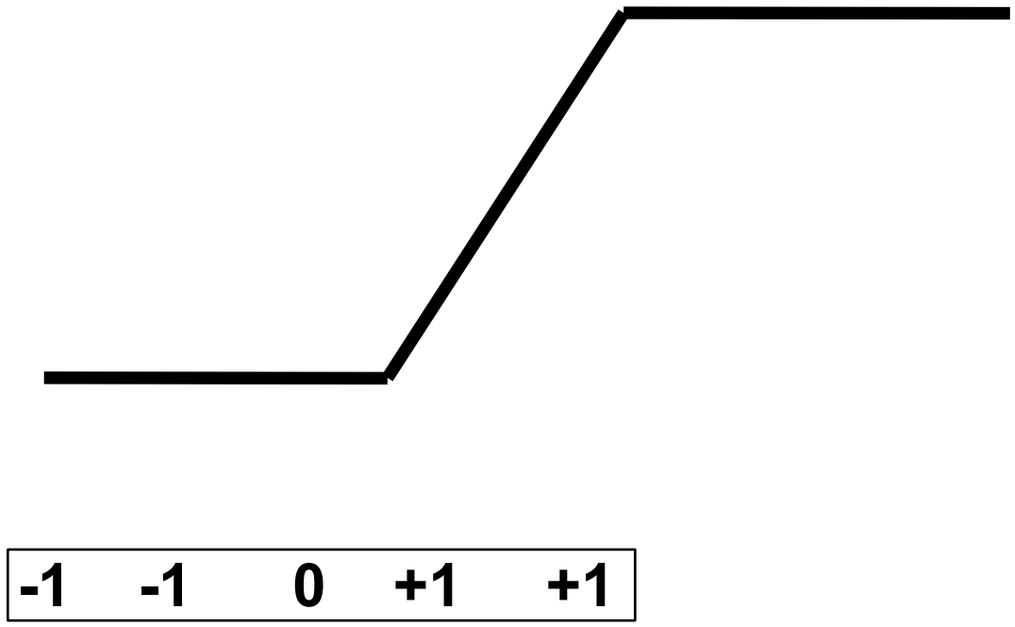


Soft thresholds (sigmoid functions) allow for smoother decision boundaries

Hands-on exercise 2

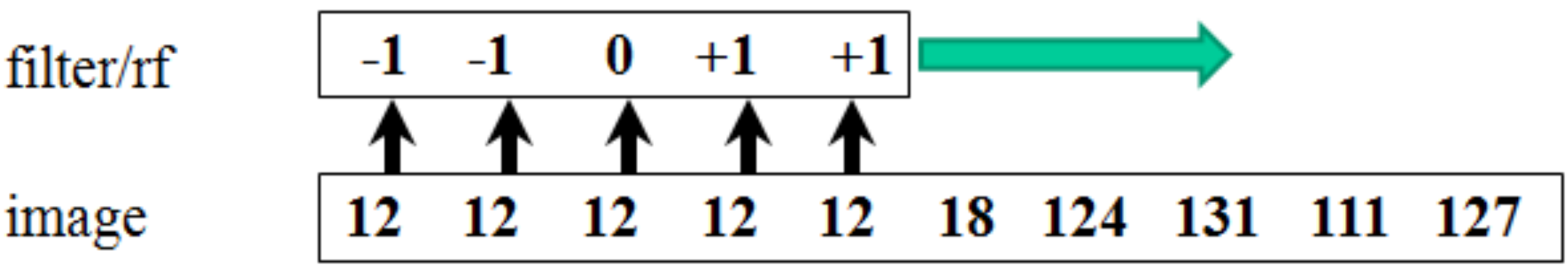
Receptive fields

- “Edge detector” (dark to light)

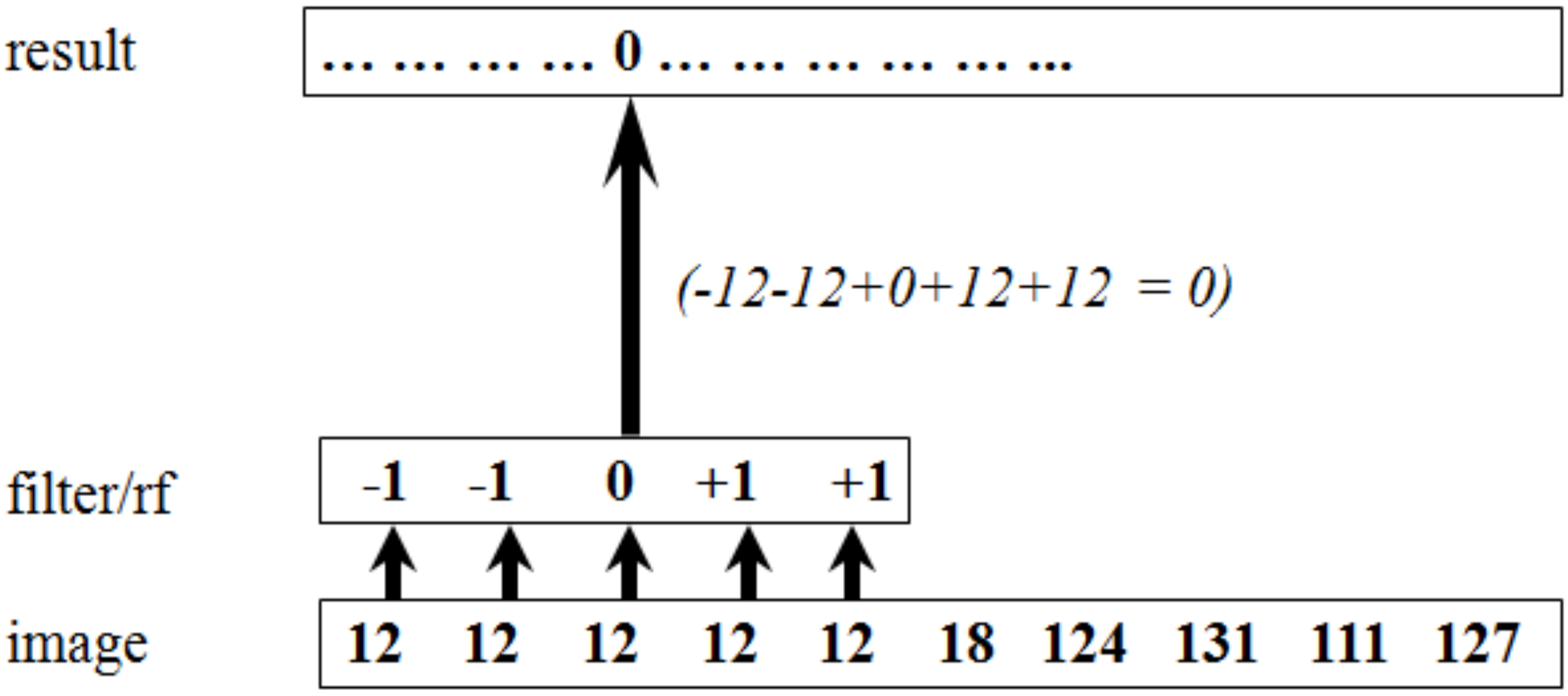


Filter/receptive field

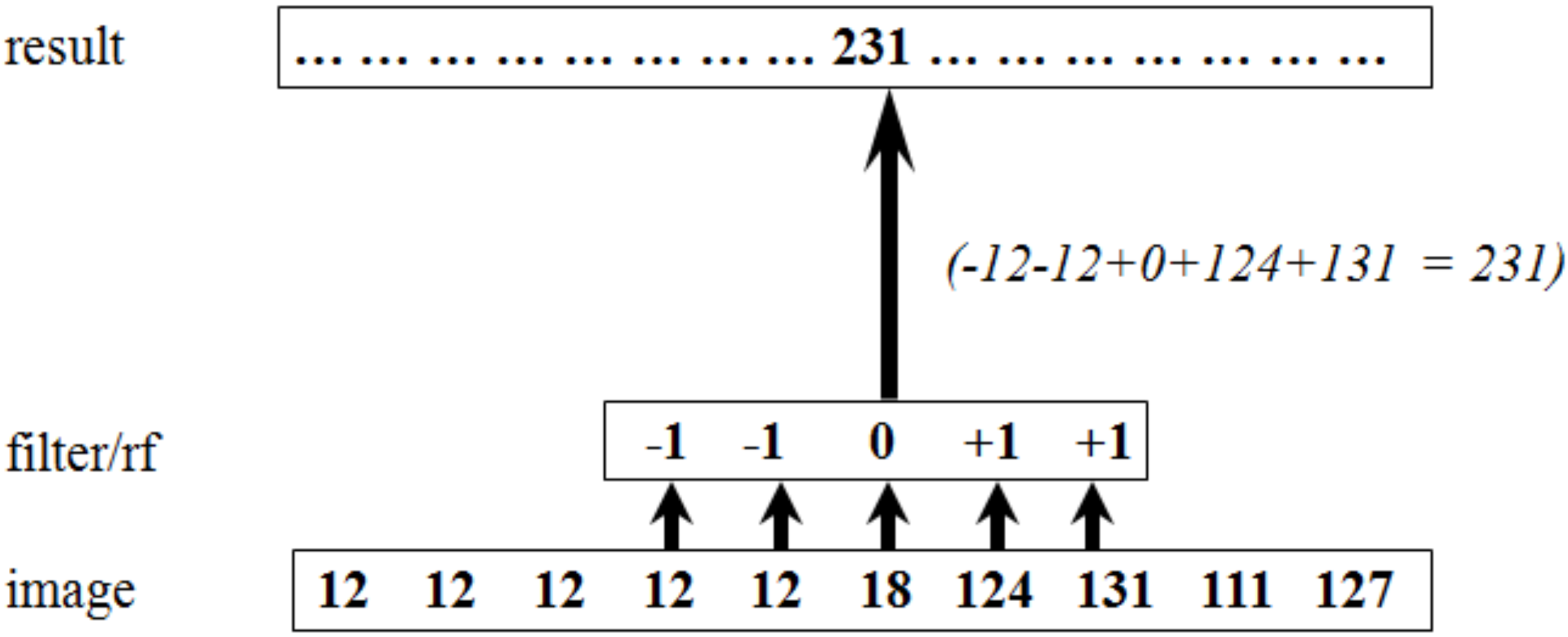
- A filter contains values (coefficients) each of which is multiplied with the corresponding pixel value in the image



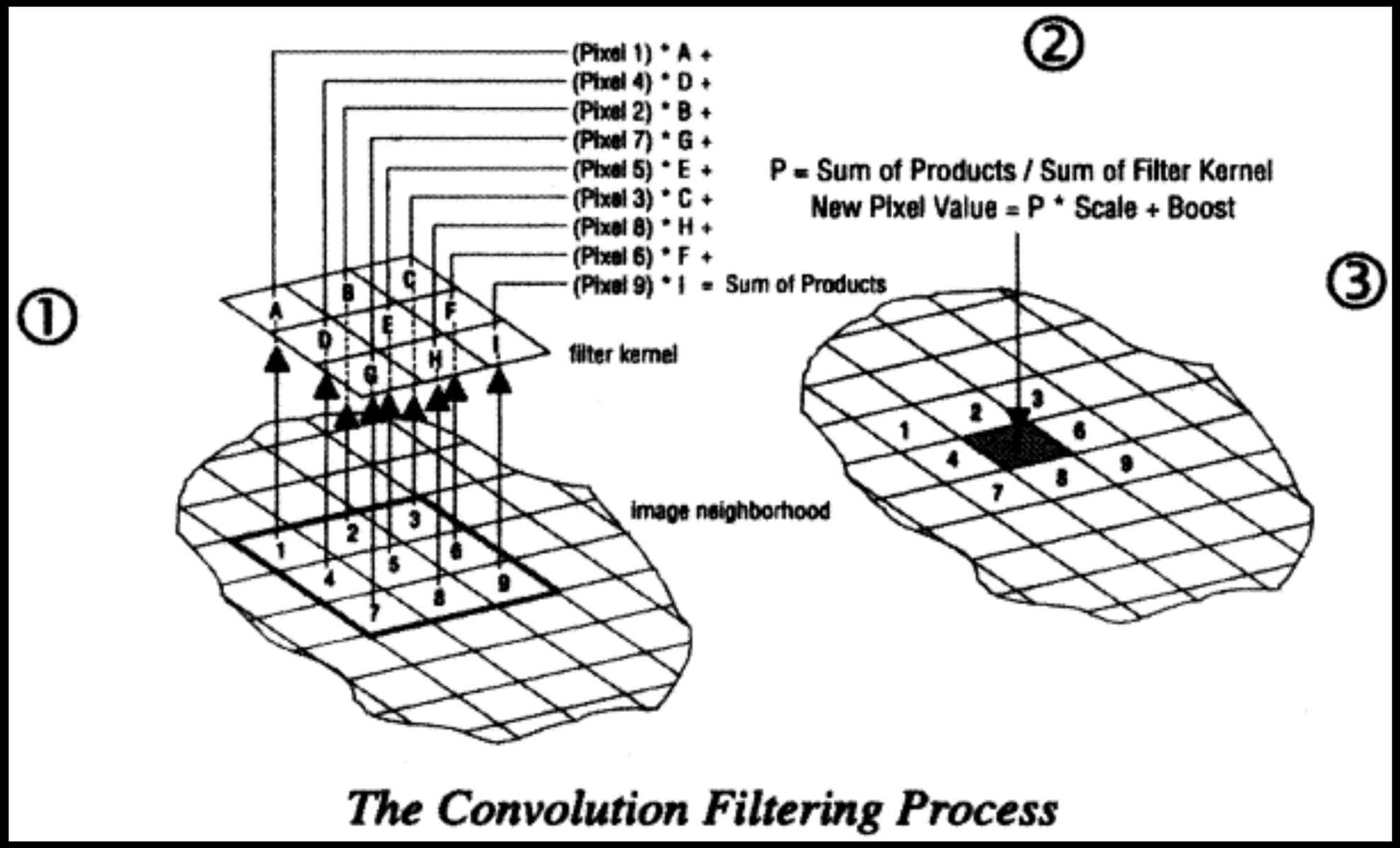
- Homogeneous image region: no edge detected



- Inhomogeneous image region: edge detected



Convolution



The Convolution Filtering Process

Computer Vision: Sobel edge detector

- Applies 2 filters (1 vertical and 1 horizontal)

-1	0	+1
-2	0	+2
-1	0	+1

Gx

+1	+2	+1
0	0	0
-1	-2	-1

Gy

Laplace edge detector

- Applies a 5 x 5 filter to each image location

-1	-1	-1	-1	-1
-1	-1	-1	-1	-1
-1	-1	24	-1	-1
-1	-1	-1	-1	-1
-1	-1	-1	-1	-1

Canny edge detector

1. Gaussian blurring

2. Sobel edge detector

Steps 3-6: tracing edges

$$\frac{1}{115}$$

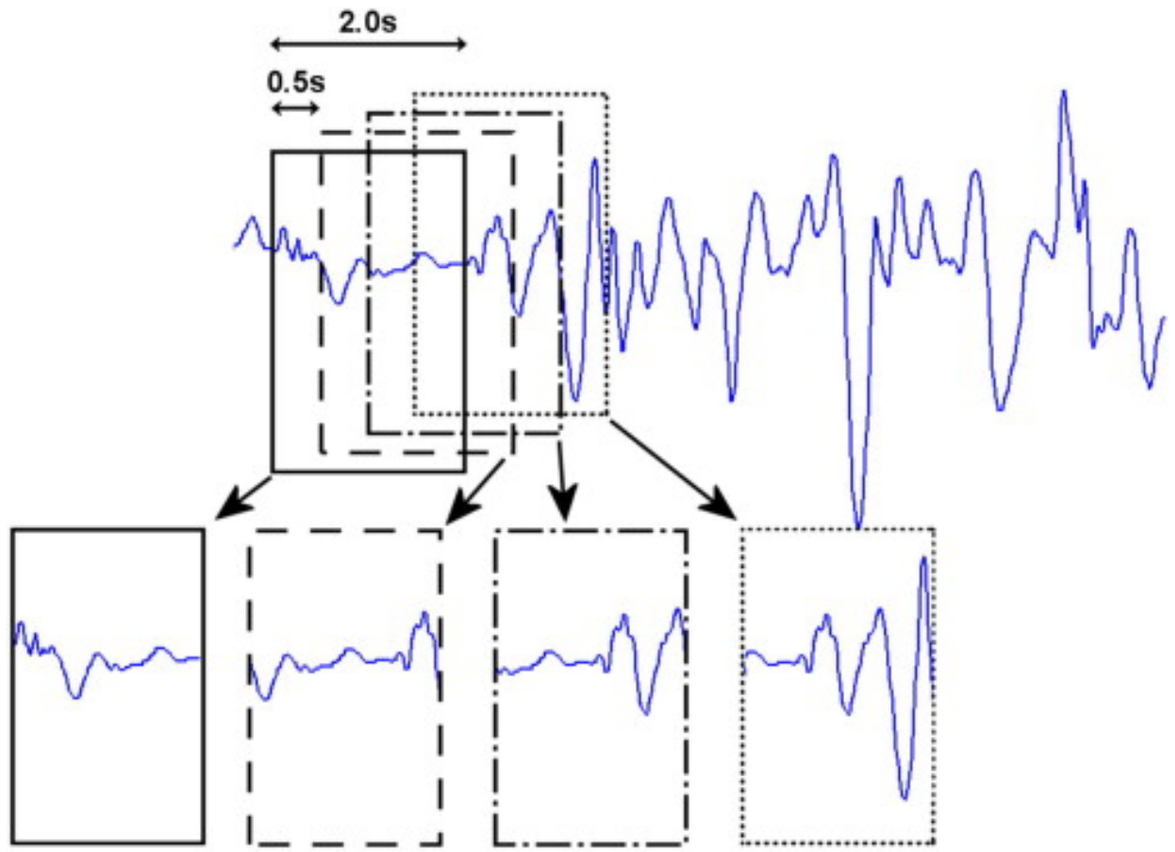
2	4	5	4	2
4	9	12	9	4
5	12	15	12	5
4	9	12	9	4
2	4	5	4	2

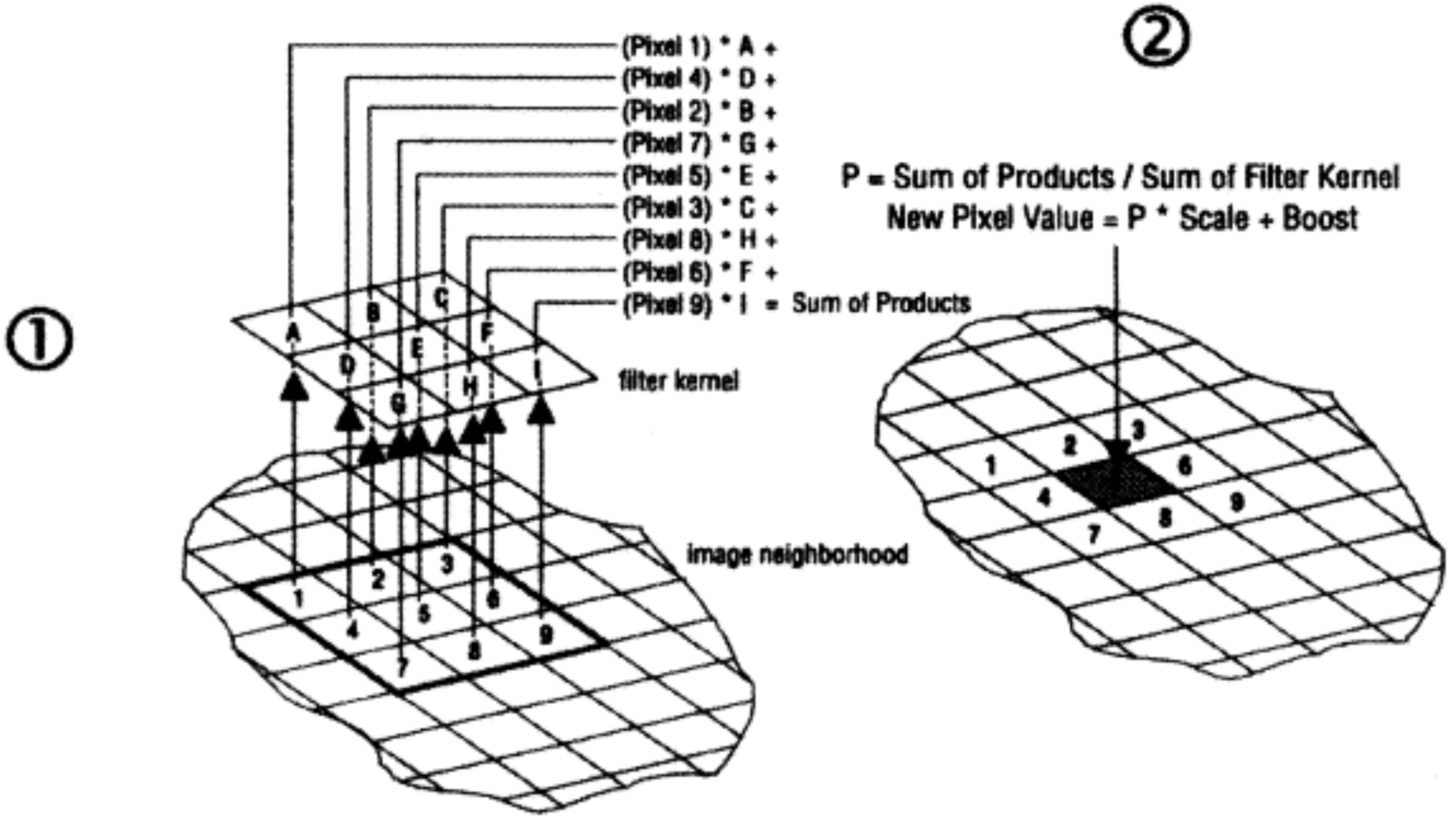
Figure 3 Discrete approximation to Gaussian function with σ=1.4

Filtering in the temporal or spatial (image) domain

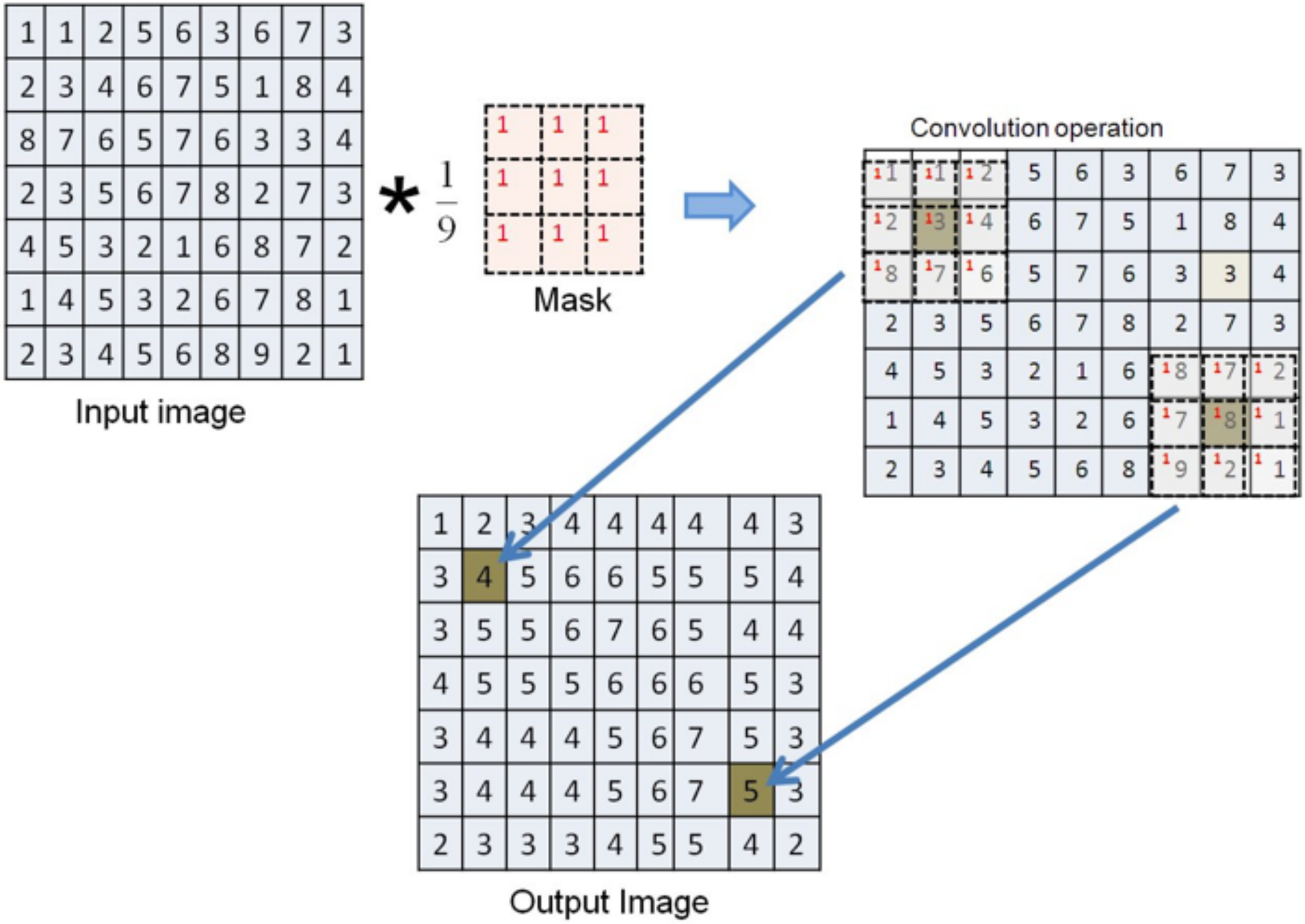
- Filtering can be done directly in the image domain by applying a filter (matrix of weights) to regions of the image

- This is the so-called “sliding window” method

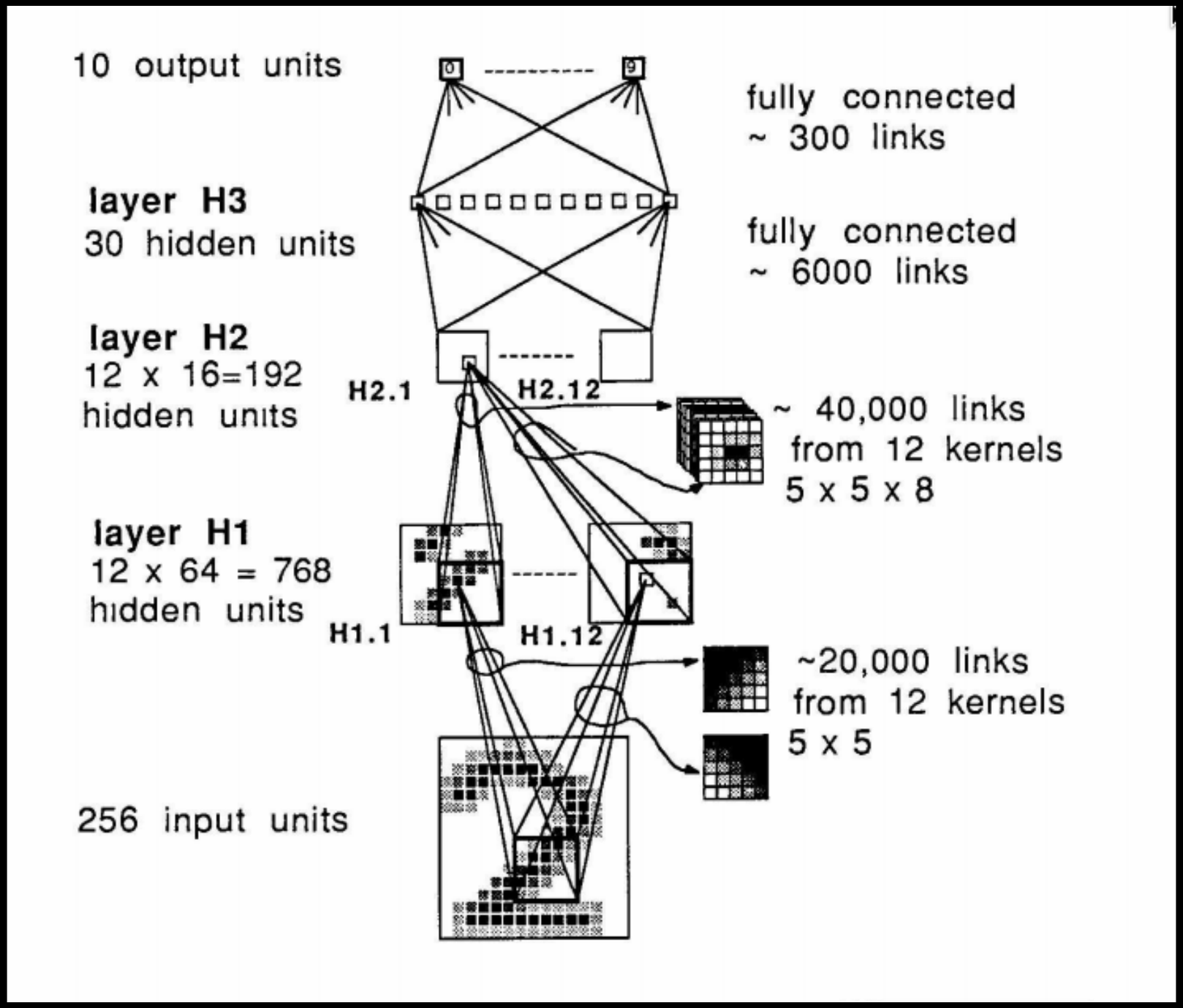




The Convolution Filtering Process


1 1 2 5 6 3 6 7 3
2 3 4 6 7 5 1 8 4
8 7 6 5 7 6 3 3 4
2 3 5 6 7 8 2 7 3
4 5 3 2 1 6 8 7 2
1 4 5 3 2 6 7 8 1
2 3 4 5 6 8 9 2 1
Input image
* 1/9
1 1 1
1 1 1
1 1 1
Mask
Convolution operation
1 2 3 4 4 4 4 4 3
3 4 5 6 6 5 5 5 4
3 5 5 6 7 6 5 4 4
4 5 5 5 6 6 6 5 3
3 4 4 4 5 6 7 5 3
3 4 4 4 5 6 7 5 3
2 3 3 3 4 5 5 4 2
Output Image

LeCun et al. (1989)



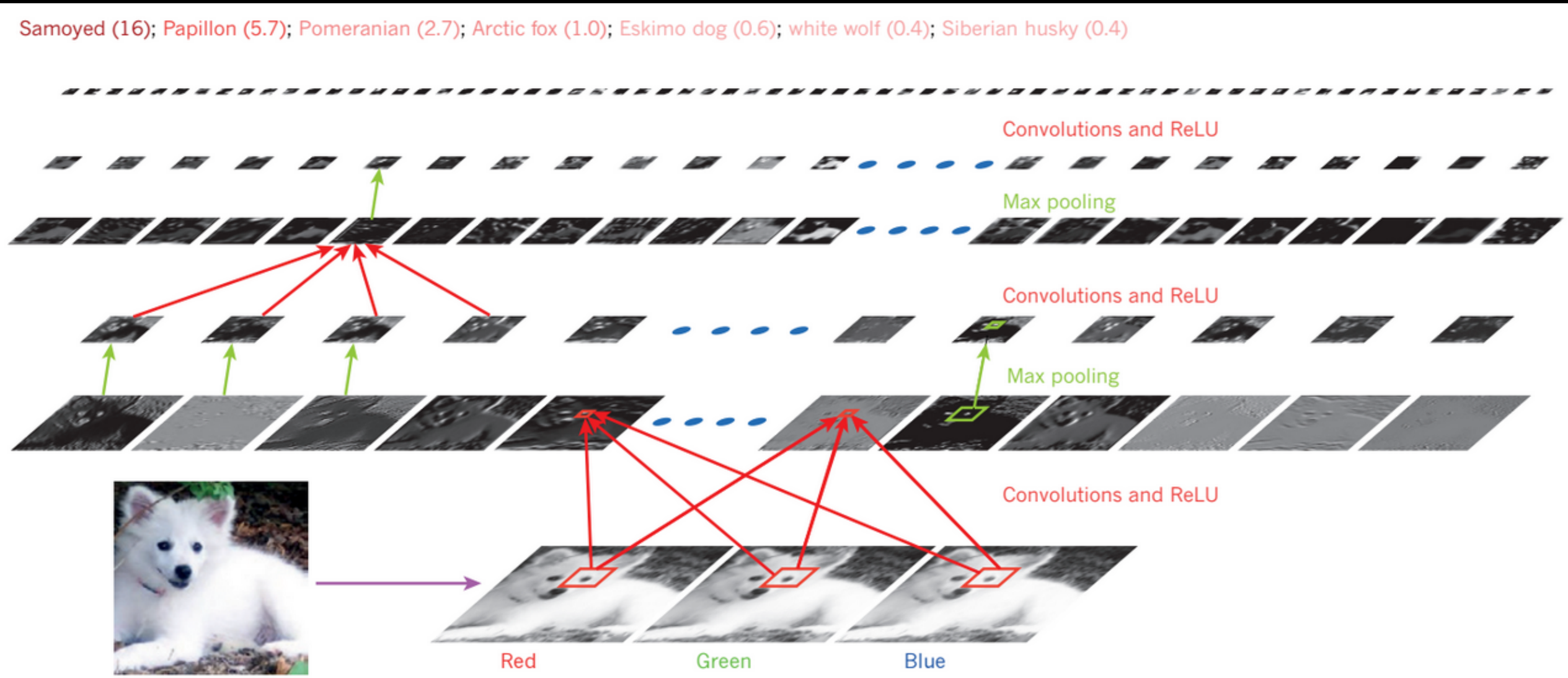
opinions1990-2012

- “It is very hard to train multilayer networks with more than 1 hidden layer”
- “This is a fundamental limit of multilayer perceptrons and (stochastic) gradient descent learning”

  Shift towards other machine learning methods (SVM, graphical models, …)

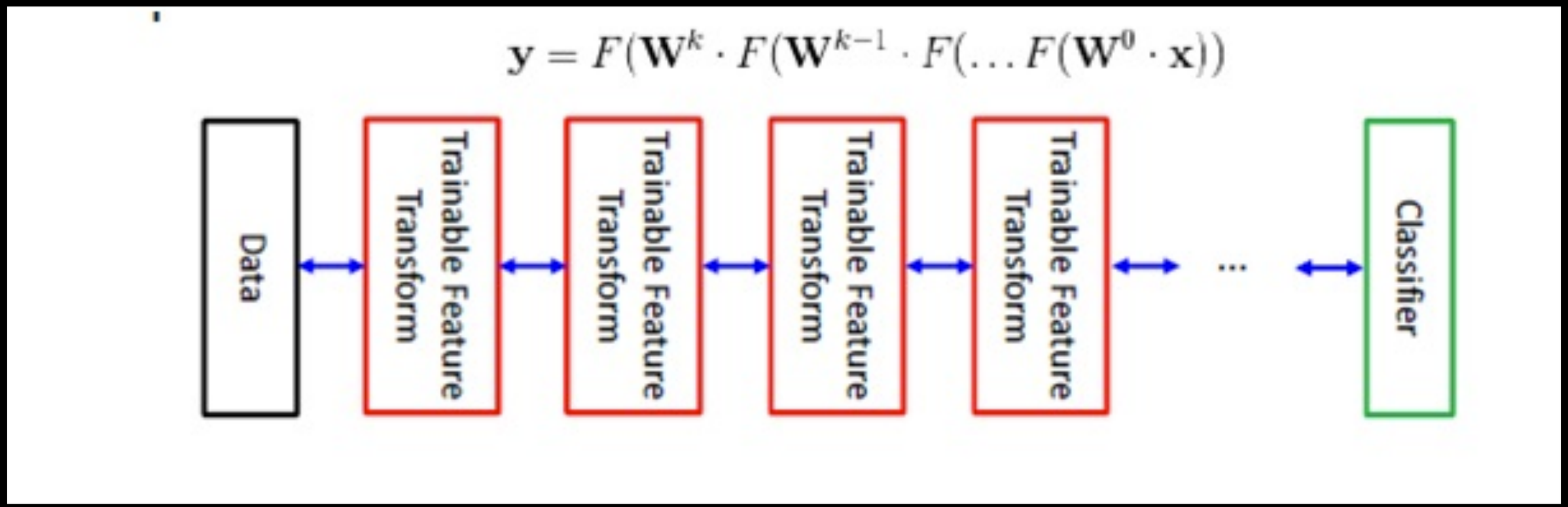
Deep Learning (2015)

Convolutional Neural Network (LeCun)



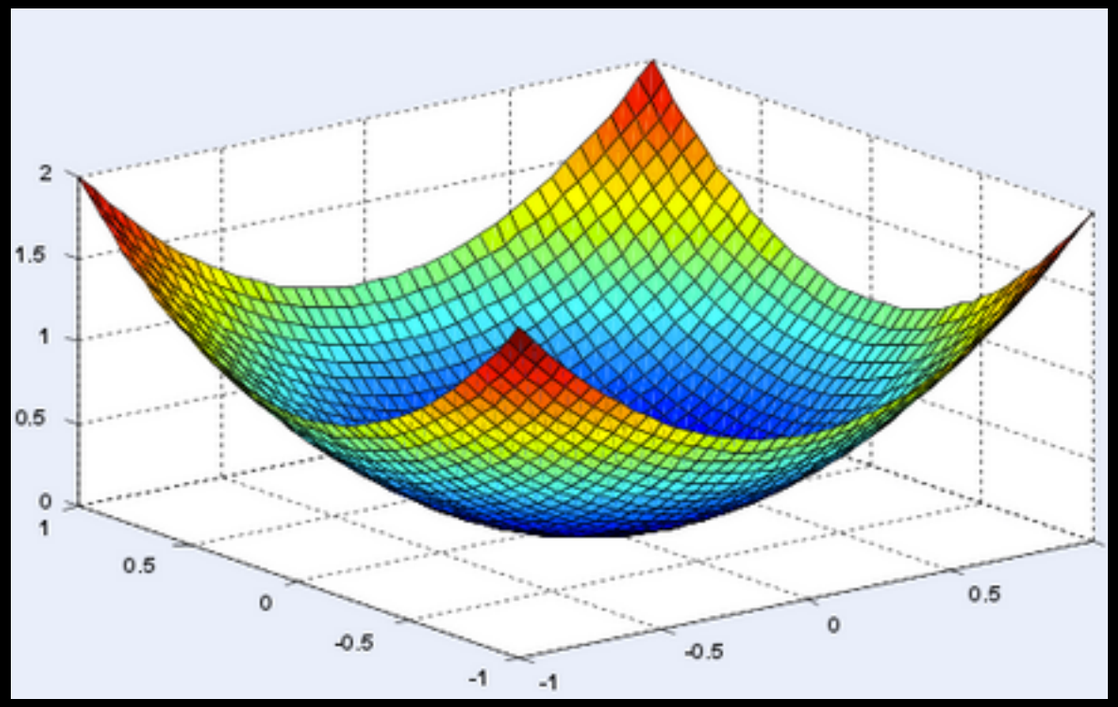
Automatically Learns Complex Non-Linear Mappings

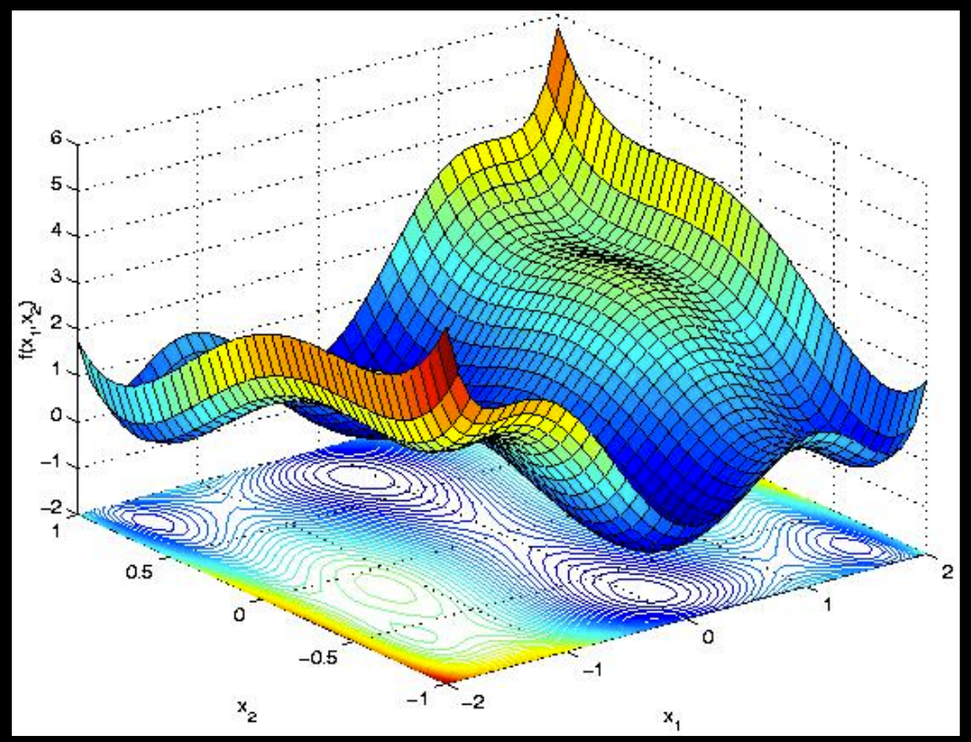
Stochastic Gradient Descent

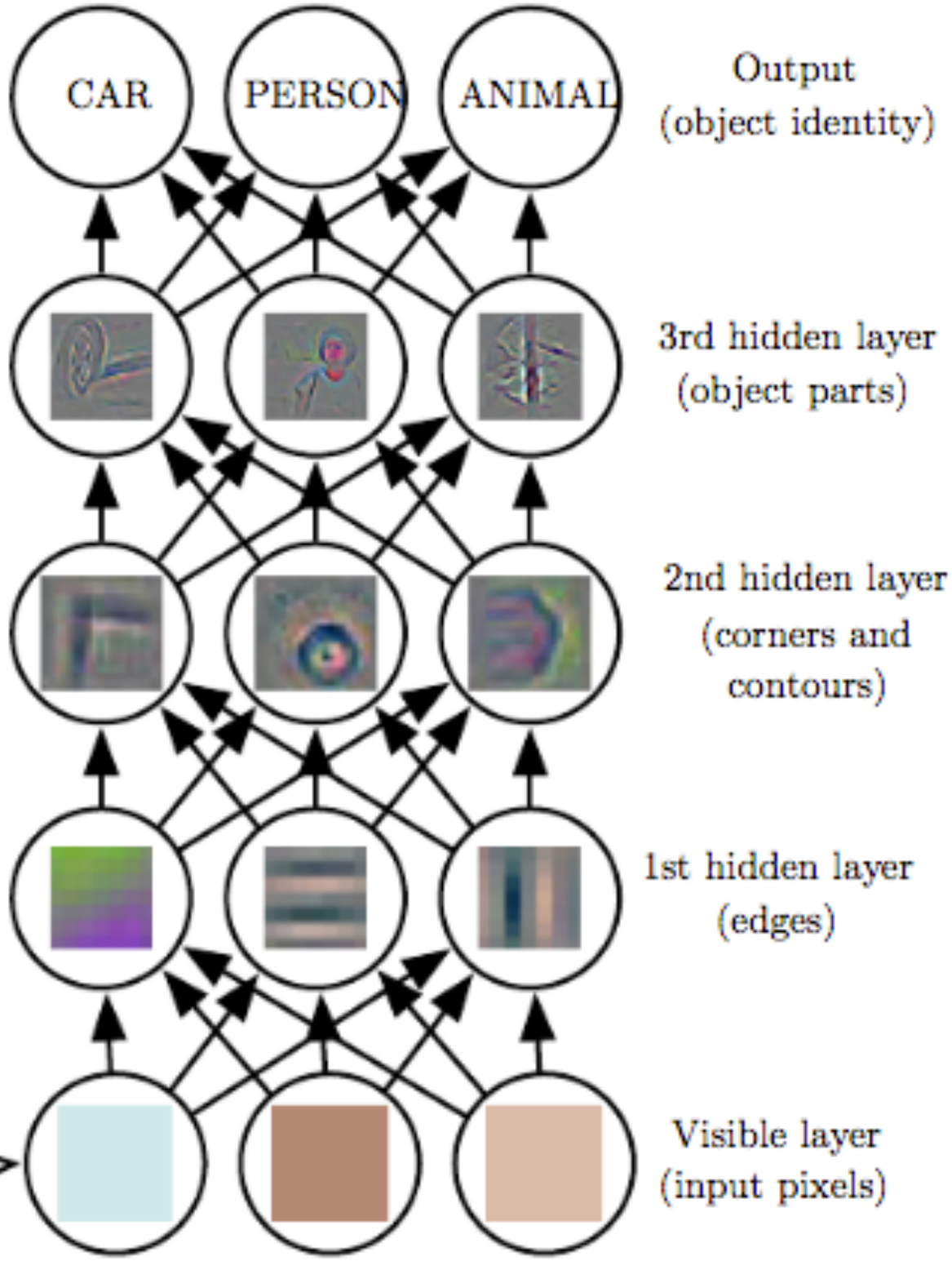


Training

- Training a Deep Convolutional Neural Network
- Non-convex optimisation problem
- Convex versus non-convex optimisation







http://www.deeplearningbook.org/

Biological Plausibility

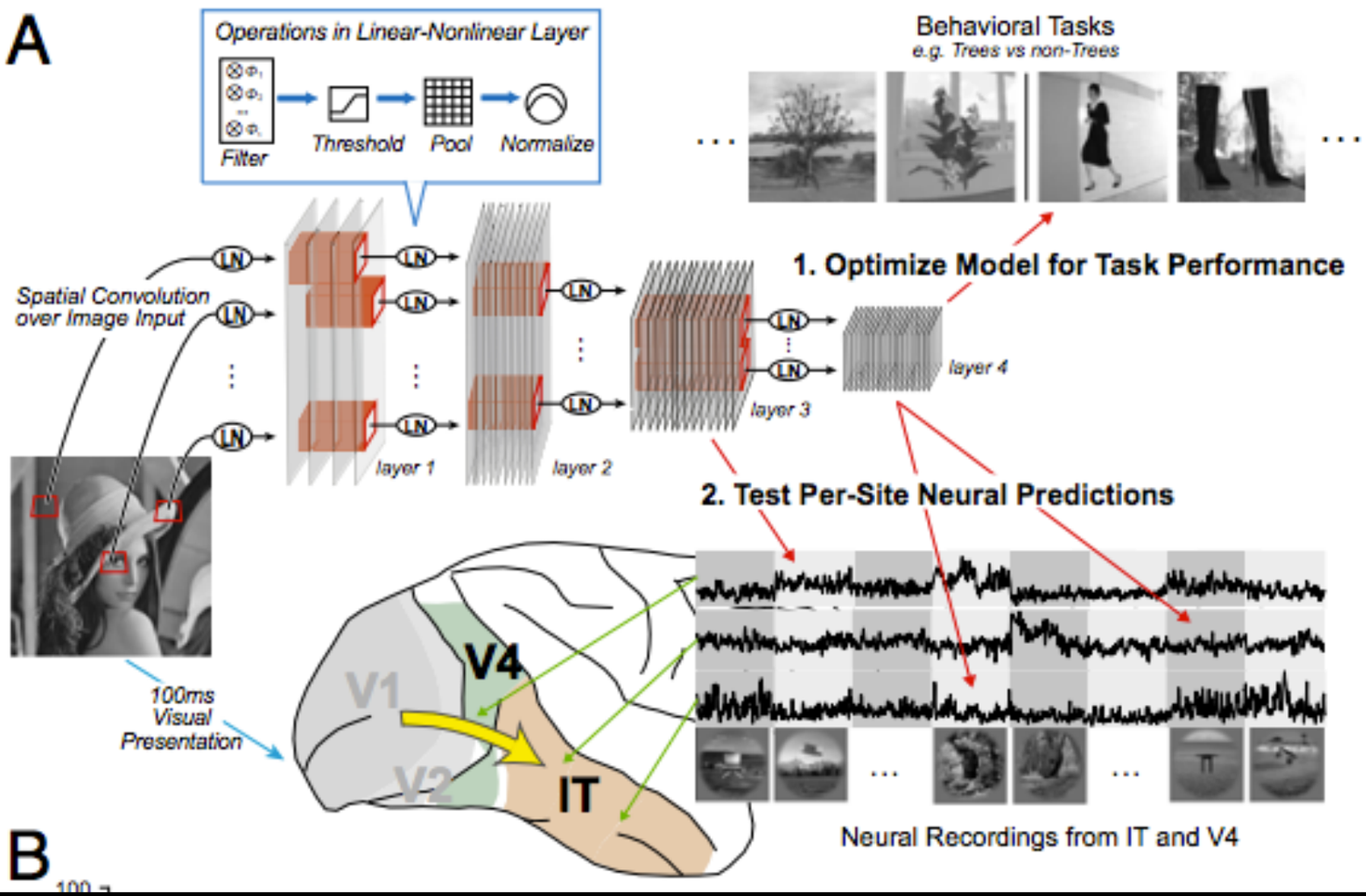
PNAS

Performance-optimized hierarchical models predict neural responses in higher visual cortex

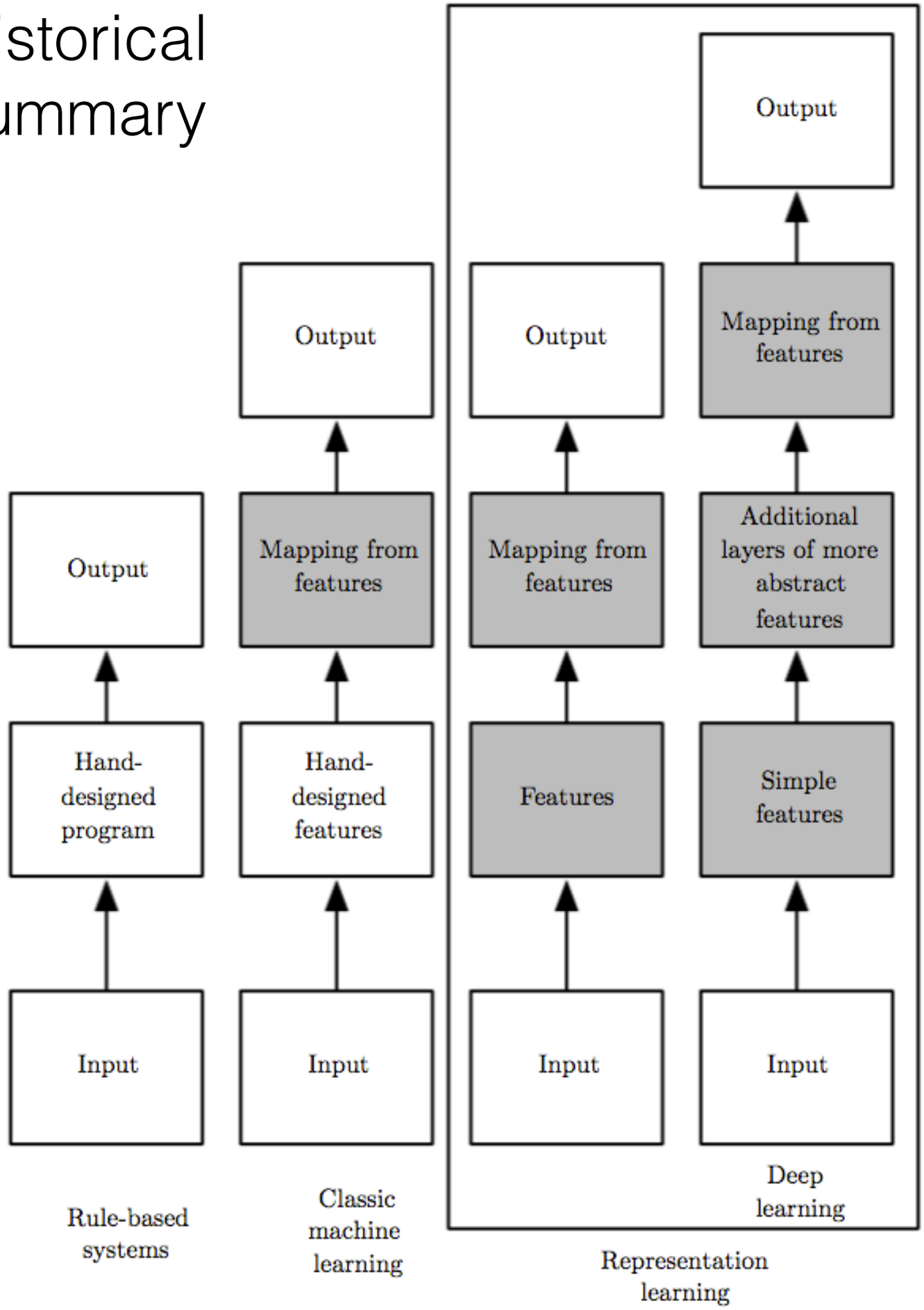
Daniel L. K. Yamins[a,1], Ha Hong[a,b,1], Charles F. Cadieu[a], Ethan A. Solomon[a], Darren Seibert[a], and James J. DiCarlo[a,2]

[a]Department of Brain and Cognitive Sciences and McGovern Institute for Brain Research, Massachusetts Institute of Technology, Cambridge, MA 02139; and [b]Harvard-MIT Division of Health Sciences and Technology, Institute for Medical Engineering and Science, Massachusetts Institute of Technology, Cambridge, MA 02139

Edited by Terrence J. Sejnowski, Salk Institute for Biological Studies, La Jolla, CA, and approved April 8, 2014 (received for review March 3, 2014)



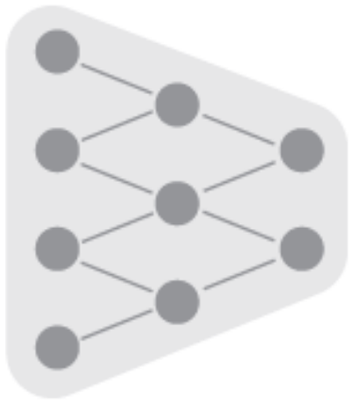
Historical summary



http://www.deeplearningbook.org/

Reading Images (FaceBook)

Vision
Deep CNN



Language
Generating RNN

A group of people shopping at an outdoor market.

There are many vegetables at the fruit stand.

A woman is throwing a **frisbee** in a park.

A **dog** is standing on a hardwood floor.

A **stop** sign is on a road with a mountain in the background

A group of **people** sitting on a boat in the water.

Applications of Deep Learning

(Feedforward networks, recurrent networks, reinforcement learning, …)

- Speech recognition/translation
- Image and object recognition
- Control tasks (playing video games)
- Language generation

COMPUTING NEWS

3 COMMENTS

Deep Learning Catches On in New Industries, from Fashion to Finance

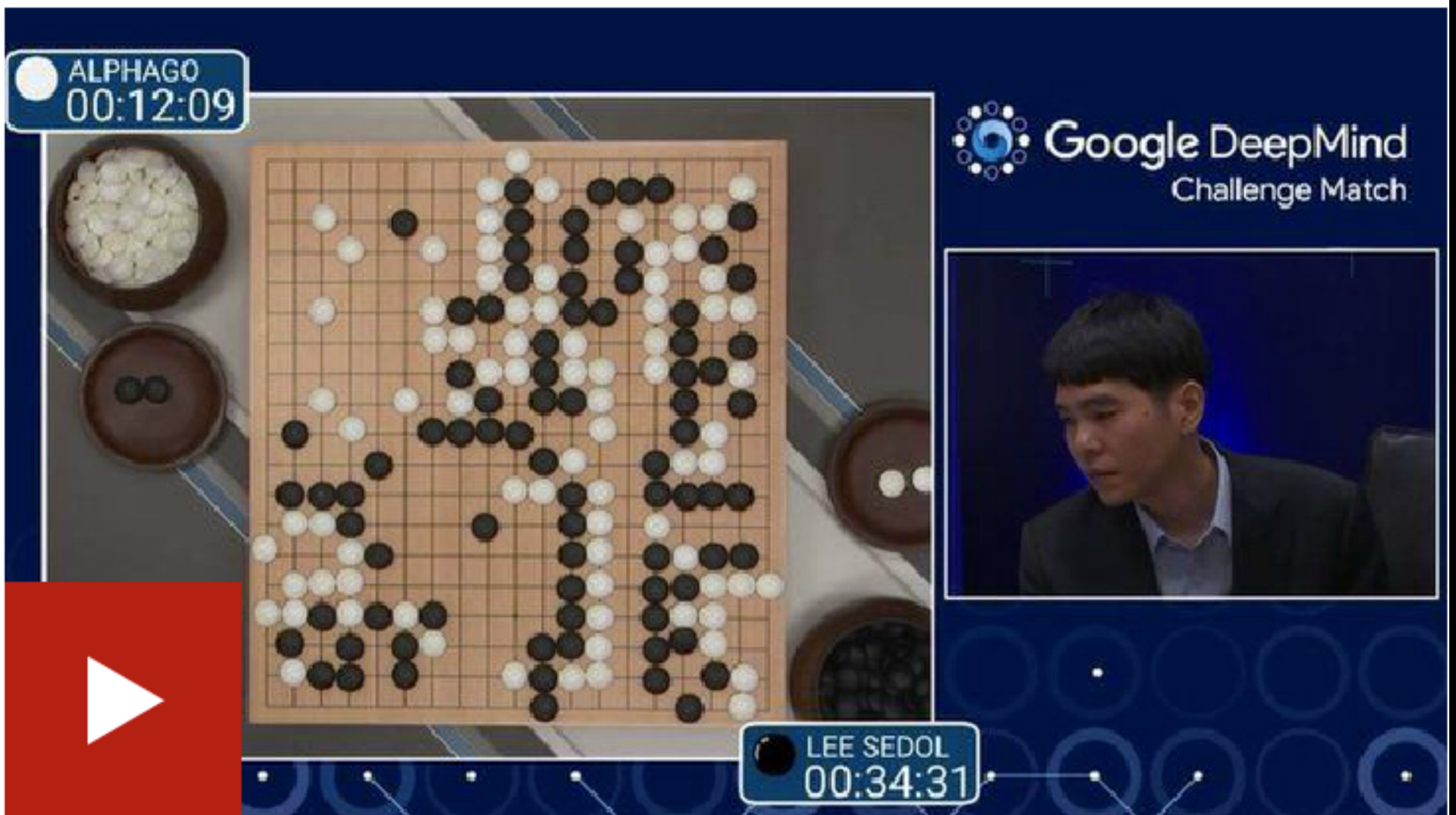
The machine-learning technique known as deep learning, which has shown impressive results in voice and image recognition, is finding new applications.

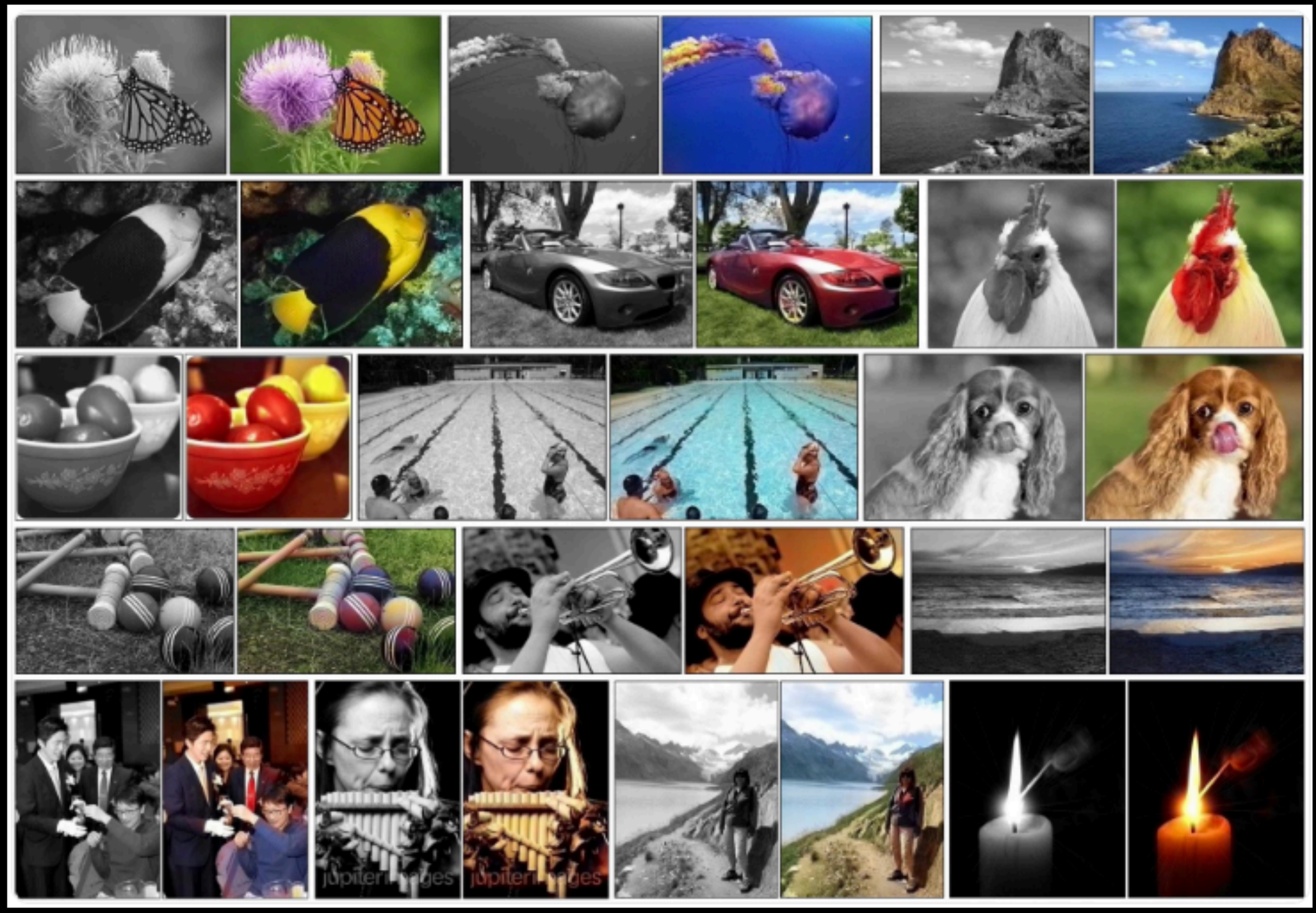
By Will Knight on May 31, 2015

Technology

Google's AI beats world Go champion in first of five matches

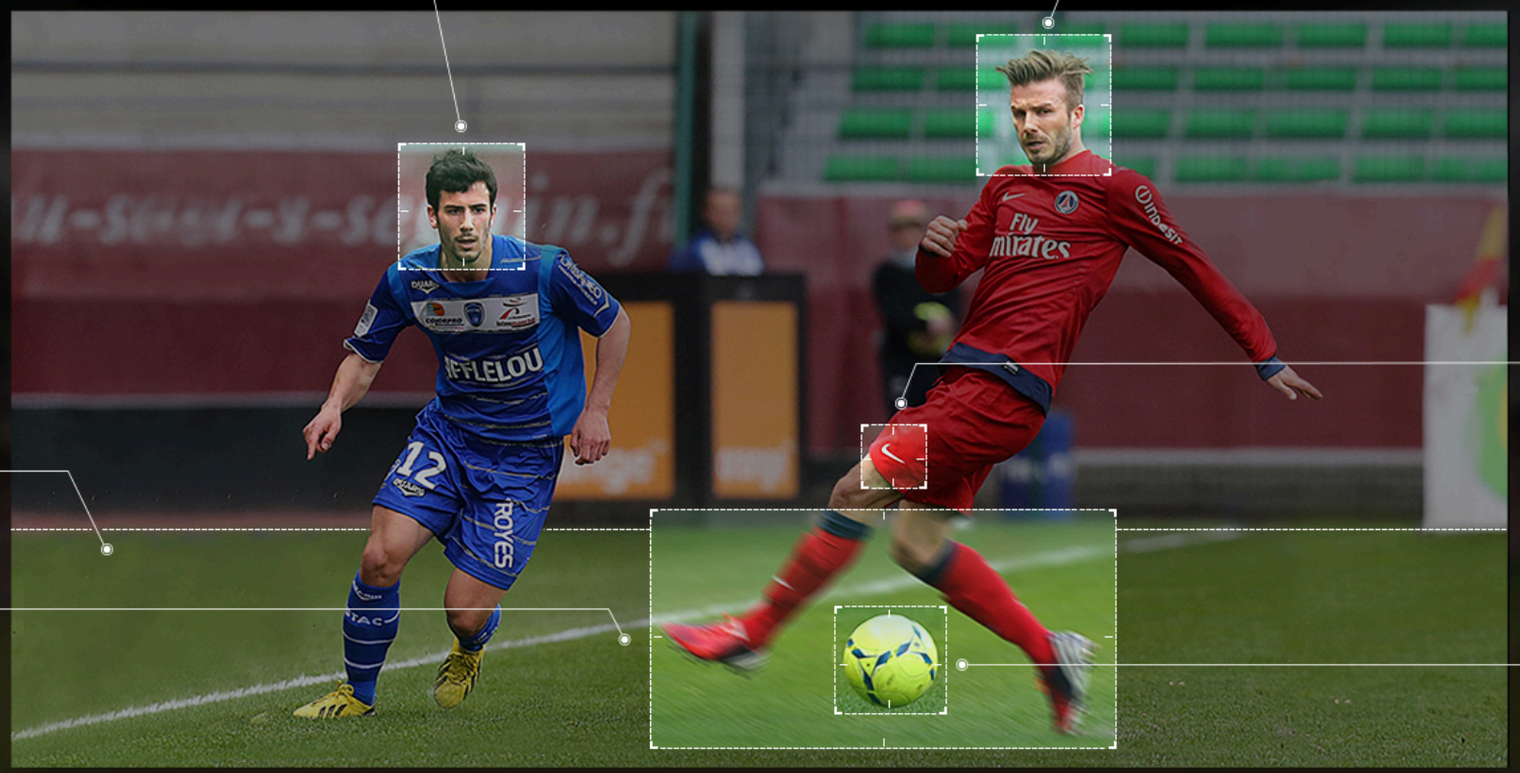
9 March 2016 | Technology



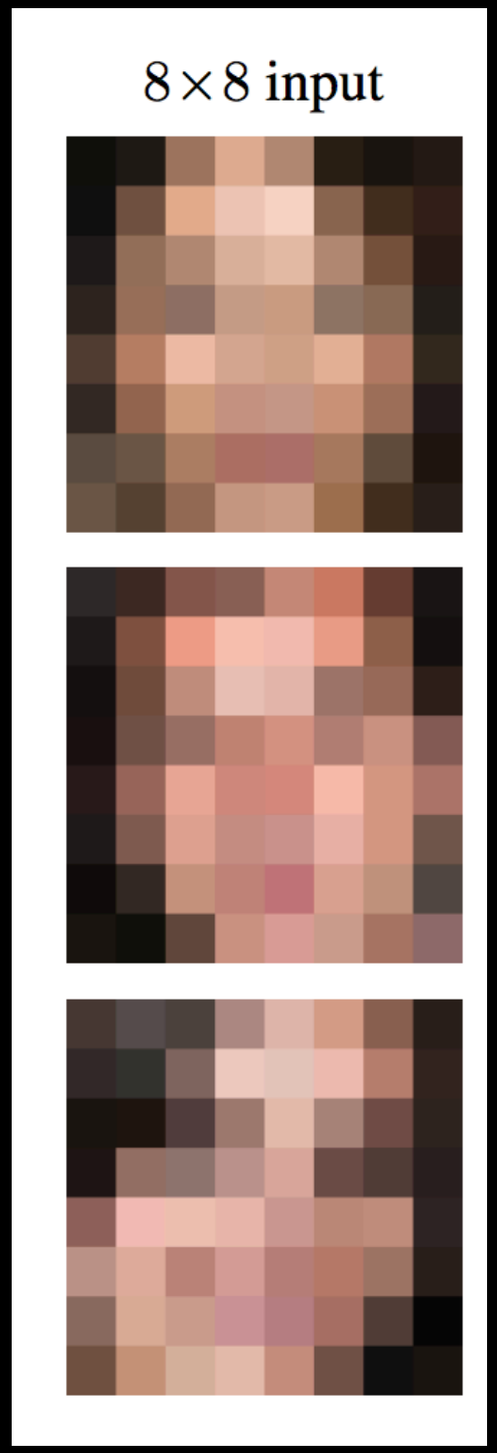


VDS

VIDEO DISCOVERY SERVICE



Dahl, Norouzi & Shlens (2017). Pixel Recursive Super Resolution. Google Brain



Brain reading

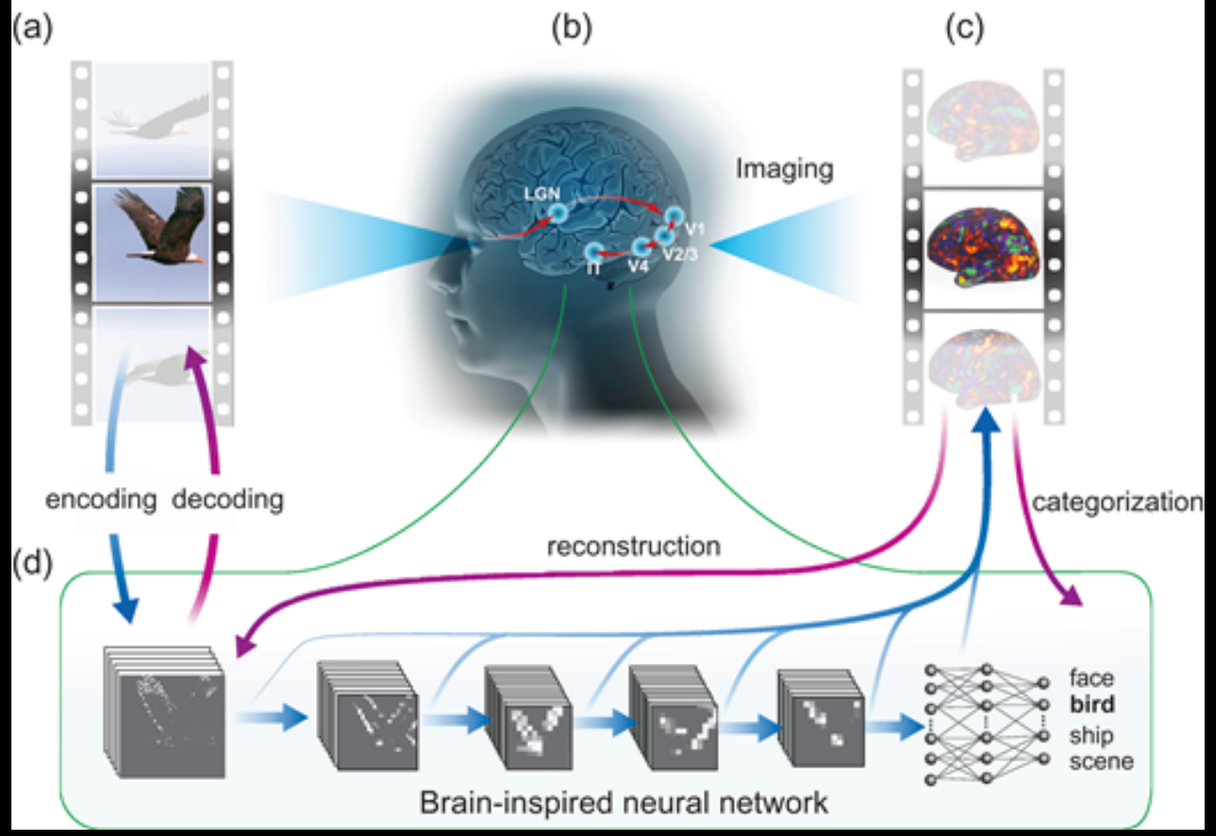
Neural Encoding and Decoding with Deep Learning for Dynamic Natural Vision

FREE

Haiguang Wen, Junxing Shi, Yizhen Zhang, Kun-Han Lu, Jiayue Cao, Zhongming Liu

Cerebral Cortex, https://doi.org/10.1093/cercor/bhx268

Published: 20 October 2017



Synthesizing Obama:
Learning Lip Sync from Audio

Supasorn Suwajanakorn
Steven M. Seitz
Ira Kemelmacher-Shlizerman

University of Washington

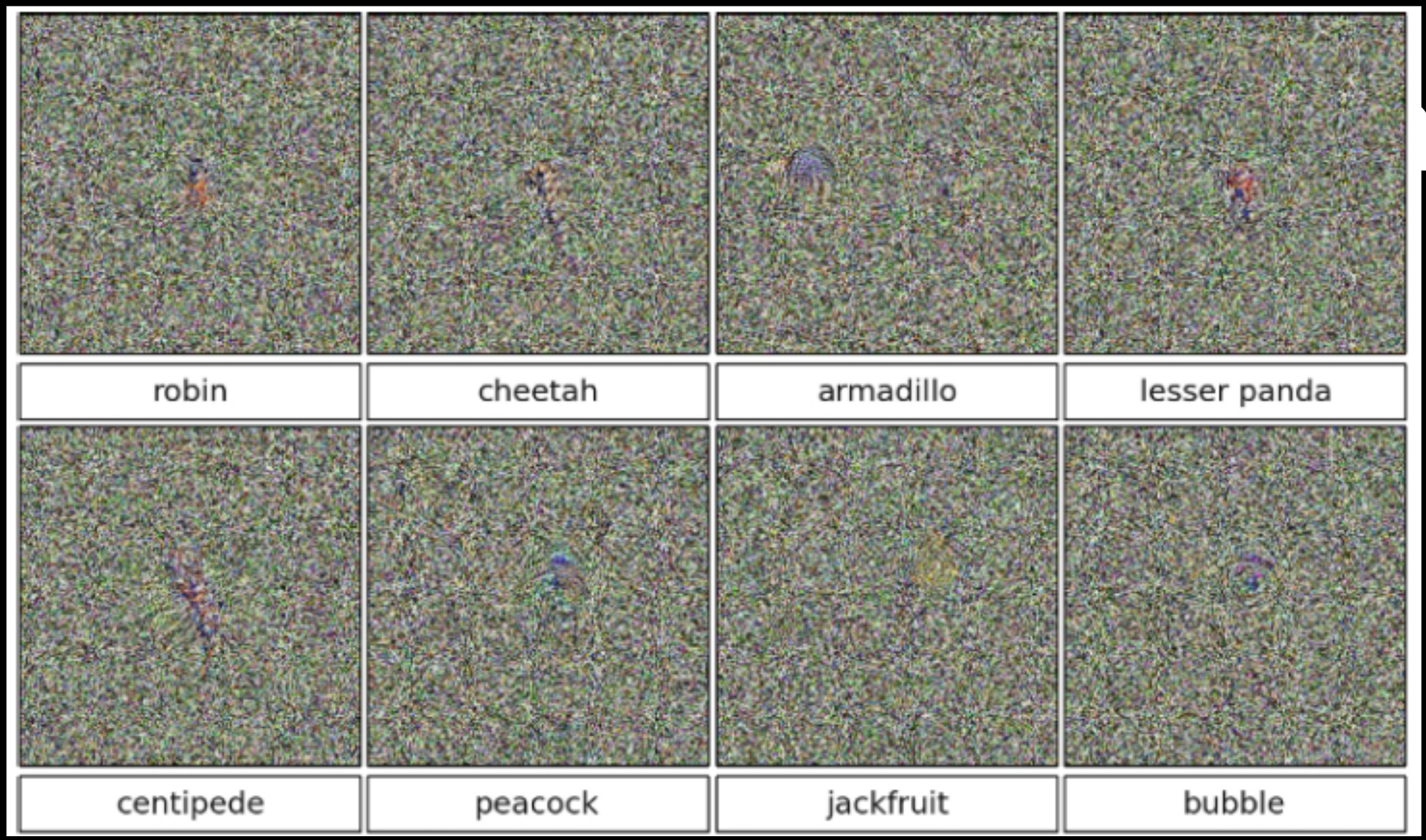
SIGGRAPH 2017
http://grail.cs.washington.edu/projects/AudioToObama/

Sensor-less tracking of human movements

Cao, Simon, Wei & Sheikh (2017).
CVPR

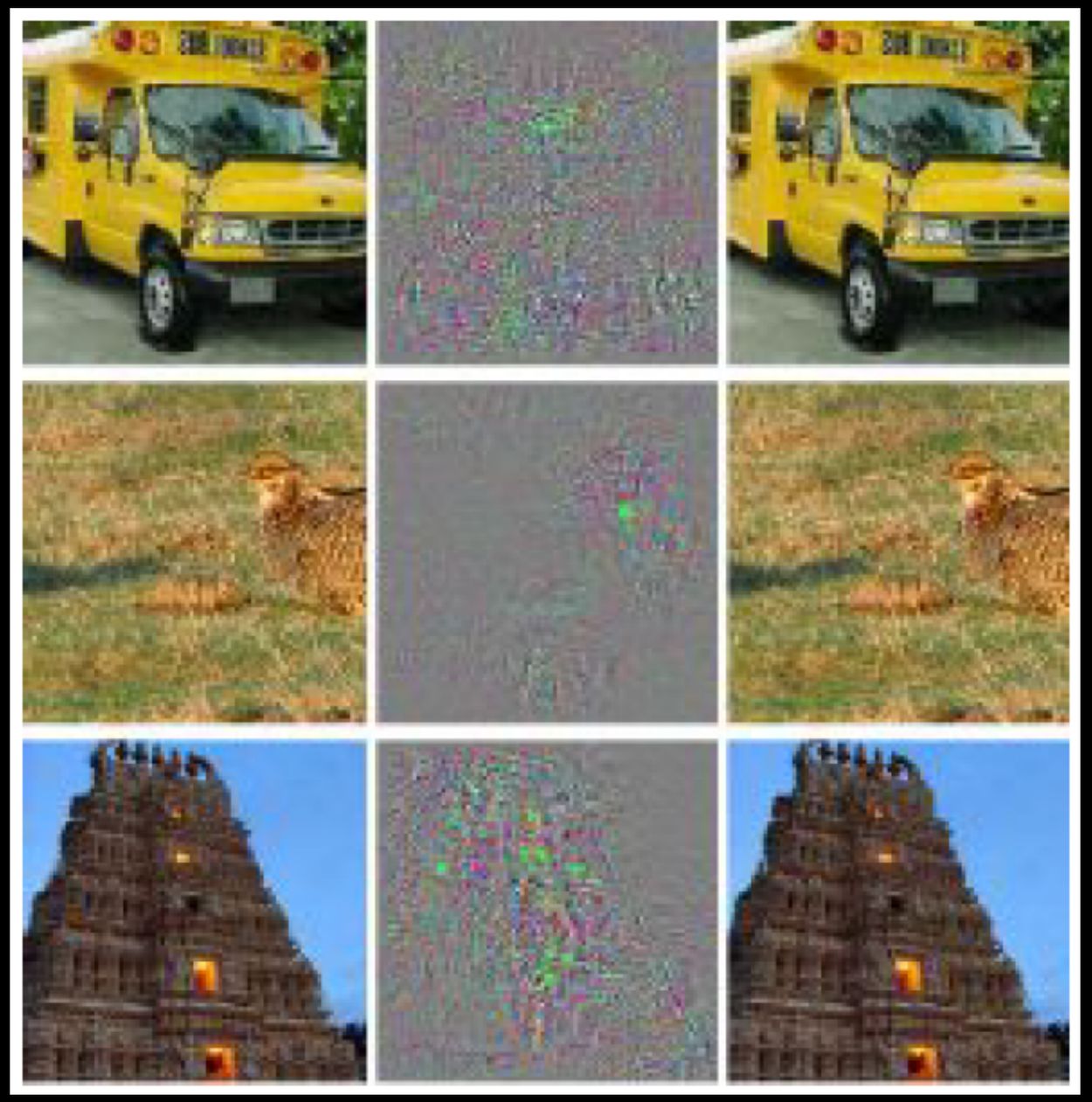
10.4 fps

Hands-on exercise 3



Nguyen, Yosinski & Clune (1994)

Deep Learning Flaws

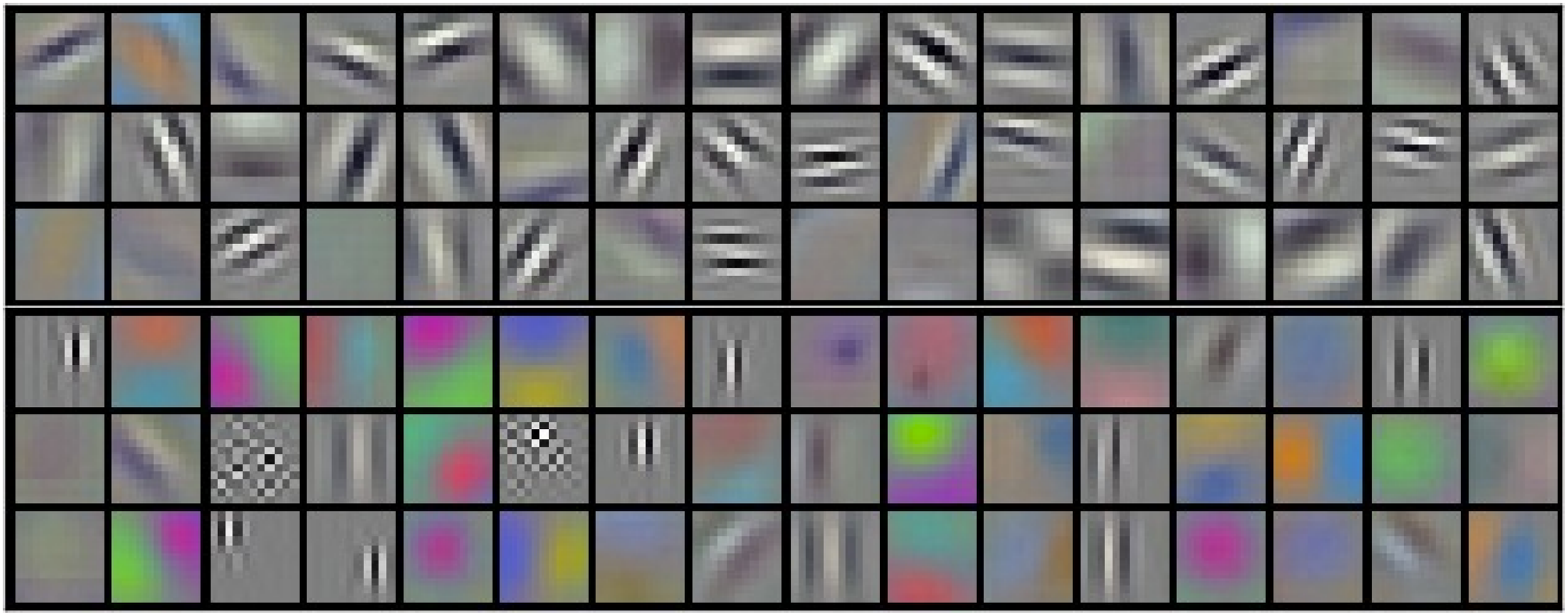


correctly classified

incorrectly classified

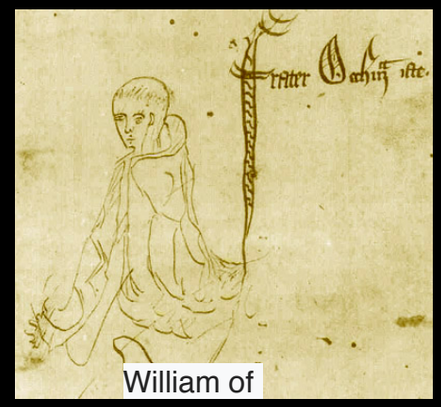
Szegedy et al. (2014)

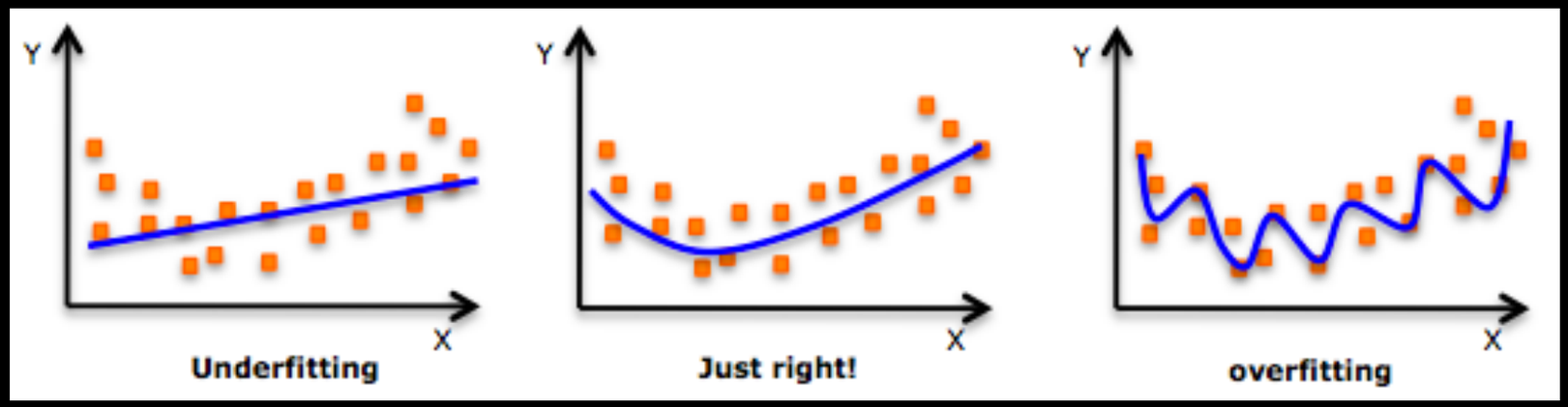
CNNs representations offer some transparency



I. Understanding the learning dynamics

- Golden rule of (good old) machine learning: *Occam's razor*
- Simple models generalise better (prevents overfitting)

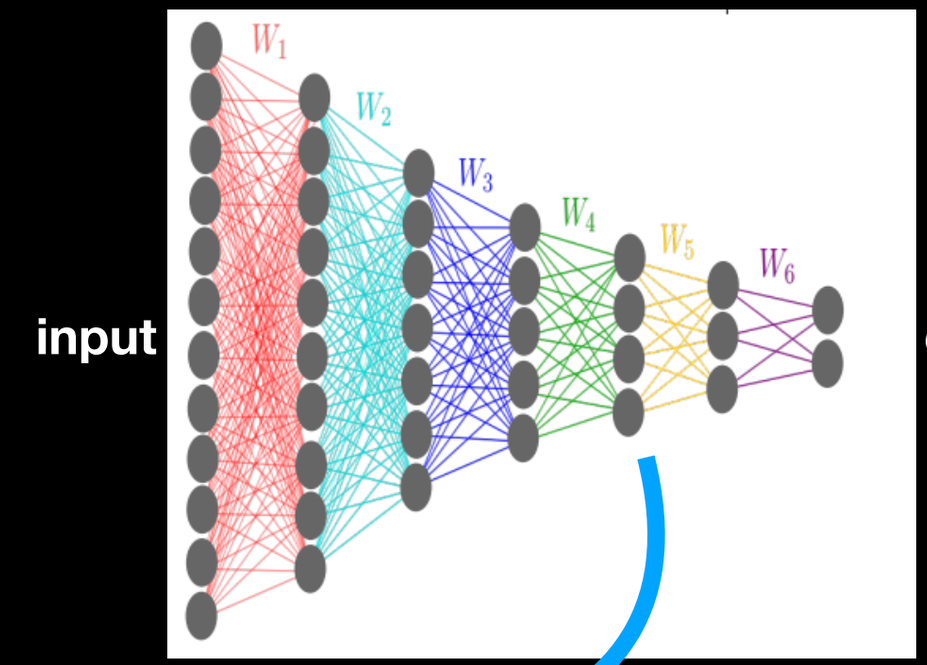


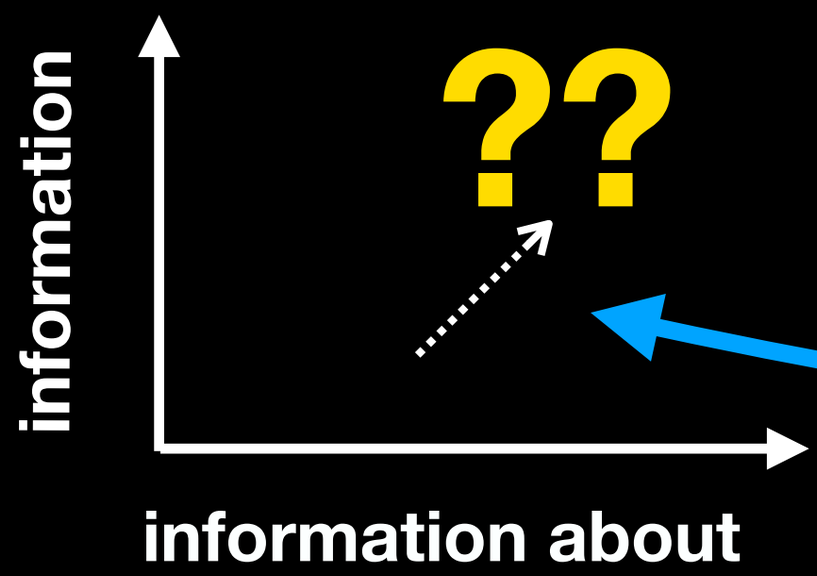


- What about the millions of parameters in Deep Learning models?

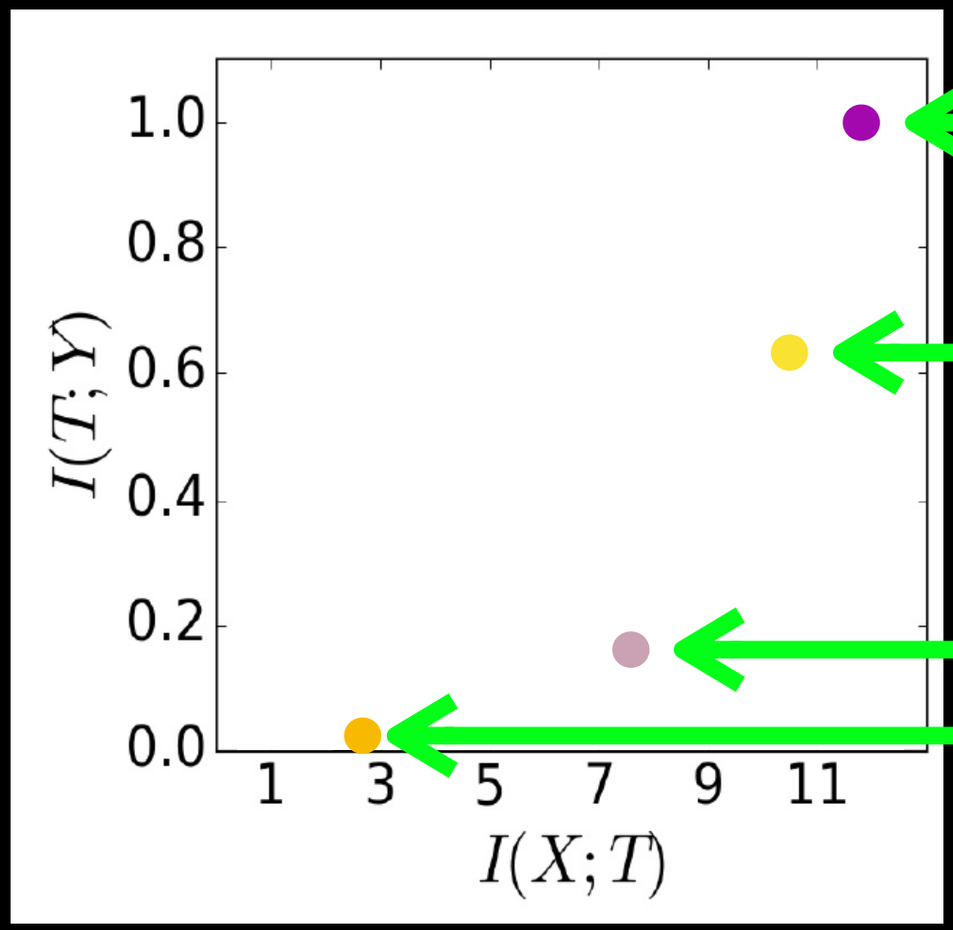
The information plane (Tishby)

- What does each layer “know” about the input and output?





The Information Plane



1st hidden layer

2nd hidden layer

3rd hidden layer

4th hidden layer

What information does T contain about output Y?

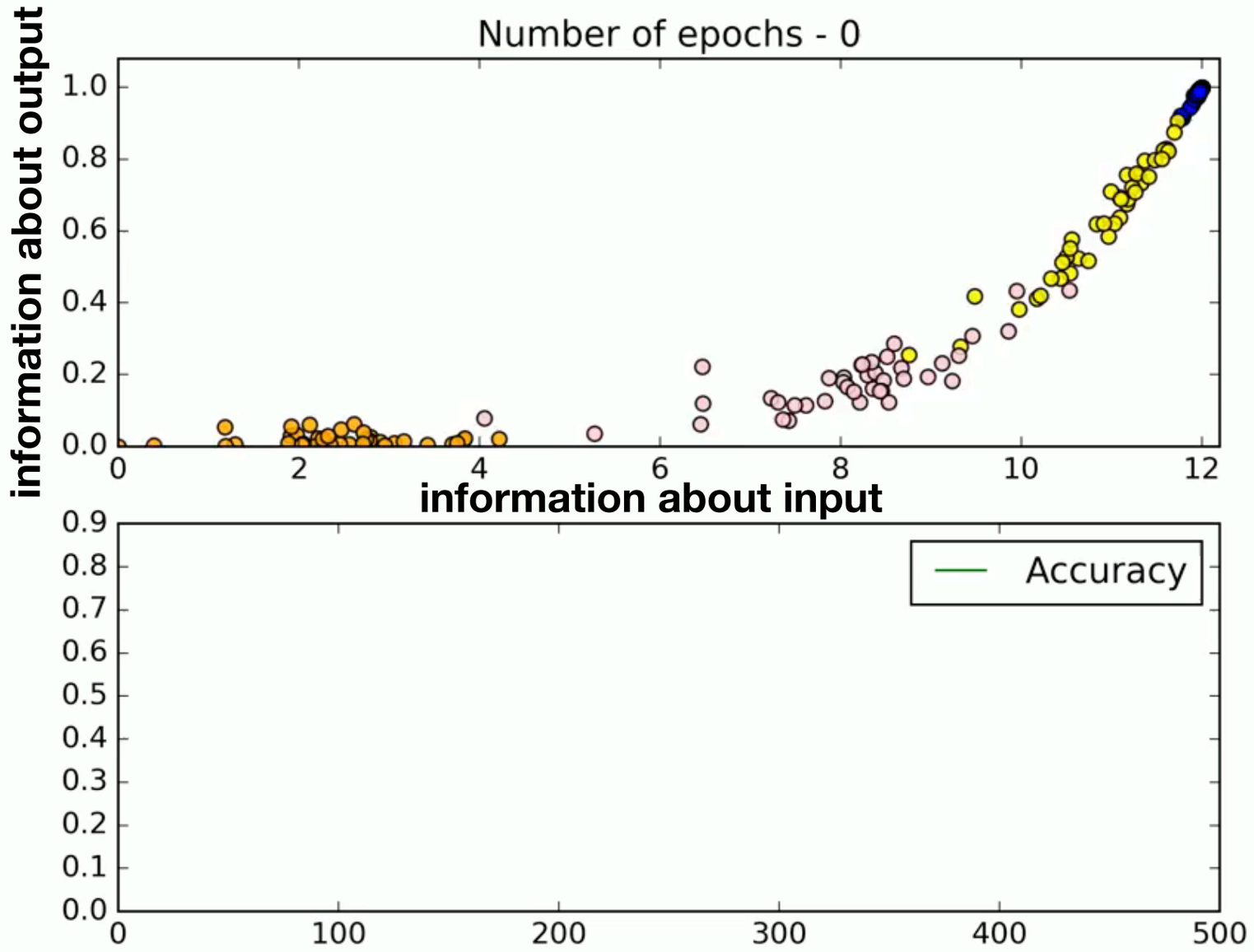
What information does T contain about input X?

We start to understand why and how deep learning works

- Two phases in learning dynamics:

1. Mapping input to output (fast)

2. Getting rid of noise (slow), compressing representations



(Schwartz-Ziv & Tishby, 2017