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Application

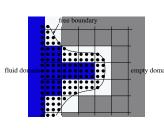








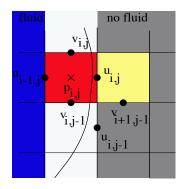
Theory



- the stress tensor: $\sigma = (-P + \lambda div\vec{u})I + 2\mu\delta$
- $P + \frac{2}{Re} \left(n_x n_x \frac{\partial u}{\partial x} + n_x n_y \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + n_y n_y \frac{\partial v}{\partial y} \right) = K\kappa$

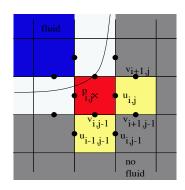
$$2n_{x}m_{x}\frac{\partial u}{\partial x}+(n_{x}m_{y}+n_{y}m_{x})\left(\frac{\partial u}{\partial y}+\frac{\partial v}{\partial x}\right)+2n_{y}m_{y}\frac{\partial v}{\partial y}=0$$

One empty neighbor



- free boundary lie almost parallel to the grid lines
- $n_y \& m_x = 0 \quad \| \quad n_x \& m_y = 0$
- $P = \frac{2}{Re} \frac{\partial u}{\partial x}$
- $\bullet \ \frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} = 0$
- using continuity equation

Two empty neighbors - common corner

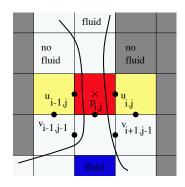


$$\bullet \ n_y = m_x = n_x = m_y$$

$$\bullet \ P = \pm \frac{1}{Re} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial x} \right)$$

$$\bullet \ \frac{\partial u}{\partial x} - \frac{\partial v}{\partial y} = 0$$

Two empty neighbors - opposite side



•
$$u_{i,i}^{new} = u_{i,i}^{old} + \delta t g_x$$

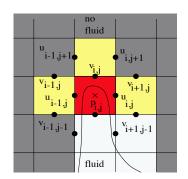
•
$$u_{i-1,j}^{new} = u_{i-1,j}^{old} + \delta t g_x$$

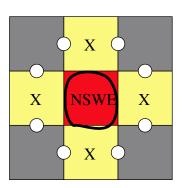
$$v_{i,j}^{new} = v_{i,j}^{old} + \delta t g_y$$

$$v_{i,j-1}^{new} = v_{i,j-1}^{old} + \delta t g_y$$

Free surface treatment

Three empty neighbors





Particle and ParticleTracer

- Particle(real x, real y, int type)
 Has some functions which can detect its position on the grid
- ParticleTracer(StaggeredGrid *grid)
 Has a vector of particles
 - void markCells()
 - void fillCell(int i, int j, int numParticles, int type)
 - void addRectangle(real x1, real y1, real x2, real y2, int type)
 - void addCircle(real x, real y, real r, int type)
 - void advanceParticles(real const dt)

Types and StaggeredGrid

- Types.hh:
 - flag EMPTY
- StaggeredGrid.cc:
 - int ppc_
 - bool isEmpty(const int x, const int y)
 - void setCellToEmpty(int x, int y)
 - void refreshEmpty()

FluidSimulator

- FluidSimulator.cc:
 - real rectX1_particle_, rectX2_particle_ , ...
 - real circR_particle_, circX_particle_, ...
 - void set_UVP_surface(int i, int j , const real &dt, bool compP)
 - void one_empty_neighbour(int i , int j , const real &dt, bool compP)
 - ...
 - four_empty_neighbour(int i , int j , const real &dt, bool compP)
 - void refreshEmpty()

Main while-loop

```
while (n <= nrOfTimeSteps)
    determineNextDT(safetyfac);
    particle tracer .markCells();
    set_UVP_surface(dt_, true);
    computeFG();
    composeRHS();
    solv().solve(grid_);
    updateVelocities();
    refreshBoundaries();
    set_UVP_surface(dt_, false);
    particle tracer_.advanceParticles(dt_); ...
                                  4 D > 4 A > 4 B > 4 B > ...
```

Examples

- The Breaking Dam Outflow
- The Breaking Dam Freeslip
- The Splash of a Liquid Drop

The Breaking Dam

```
imax = 50, imax = 20.
xlength = 10.0, ylength = 4.0,
tau = 0.5.
               delt = 0.04, t end = 5.0,
eps = 0.001,
            omg = 1.7
gamma = 0.5, itermax = 500,
GX = 0.0.
             GY = -1.0.
                             Re = 10.0.
UI = 0.0.
              VI = 0.0.
                             PI = 0.0.
ppc = 16,
wW = free.
              wE = out.
wS = free.
               wN = out
```

The Splash of a Liquid Drop

```
imax = 40.
               imax = 30.
xlength = 8.0,
              ylength = 6.0,
tau = 0.2.
               delt = 0.01, t end = 10.0,
eps = 0.001,
            omg = 1.7
gamma = 0.5, itermax = 500,
GX = 0.0.
              \mathsf{GY} = -1.0,
                              Re = 40.0.
UI = 0.0.
               VI = 0.0. PI = 0.0.
ppc = 16,
wW = free.
               wE = free.
wS = free.
               wN = out
```