

Free Surface Flows

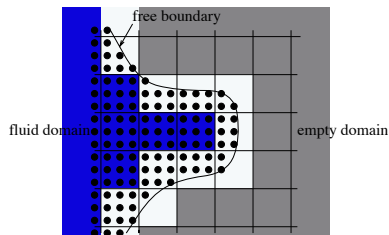
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[c]0.3



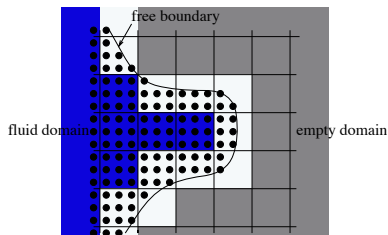
Theory



- the stress tensor:

$$\sigma = (-P + \lambda \operatorname{div} \vec{u})I + 2\mu \delta$$

Theory

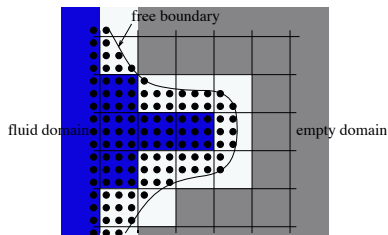


- the stress tensor:

$$\sigma = (-P + \lambda \operatorname{div} \vec{u})I + 2\mu \delta$$

- $P + \frac{2}{Re} \left(n_x n_x \frac{\partial u}{\partial x} + n_x n_y \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + n_y n_y \frac{\partial v}{\partial y} \right) = K \kappa$

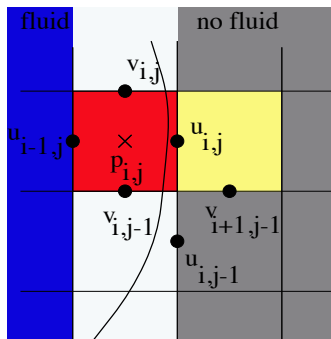
Theory



- the stress tensor:

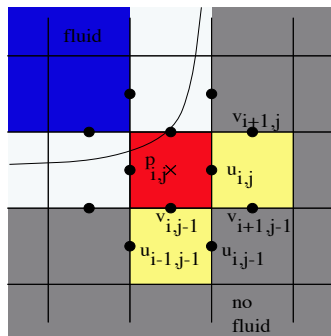
$$\sigma = (-P + \lambda \operatorname{div} \vec{u})I + 2\mu \delta$$
- $$P + \frac{2}{Re} \left(n_x n_x \frac{\partial u}{\partial x} + n_x n_y \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + n_y n_y \frac{\partial v}{\partial y} \right) = K \kappa$$
- $$2n_x m_x \frac{\partial u}{\partial x} + (n_x m_y + n_y m_x) \left(\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} \right) + 2n_y m_y \frac{\partial v}{\partial y} = 0$$

One empty neighbor



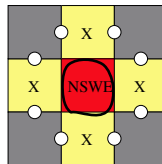
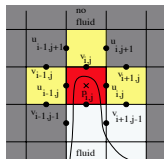
- free boundary lie almost parallel to the grid lines
- $n_y \& m_x = 0$ & $n_x \& m_y = 0$
- $P = \frac{2}{Re} \frac{\partial u}{\partial x}$
- $\frac{\partial u}{\partial y} + \frac{\partial v}{\partial x} = 0$
- using continuity equation

Two empty neighbor-common corner



- $n_y = m_x = n_x = m_y$
- $P = \pm \frac{1}{Re} \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial x} \right)$
- $\frac{\partial u}{\partial x} - \frac{\partial v}{\partial y} = 0$

Three empty neighbor



Particle and ParticleTracer

- **Particle(real x, real y, int type)**

Has some functions which can detect its position on the grid

- **ParticleTracer(StaggeredGrid *grid)**

Has a vector of particles

- **void markCells()**
- **void fillCell(int i, int j, int numParticles, int type)**
- **void addRectangle(real x1, real y1, real x2, real y2, int type)**
- **void addCircle(real x, real y, real r, int type)**
- **void advanceParticles(real const dt)**

Types and StaggeredGrid

- **Types.hh:**
 - **flag EMPTY**
- **StaggeredGrid.cc:**
 - **int ppc_**
 - **bool isEmpty(const int x, const int y)**
 - **void setCellToEmpty(int x, int y)**
 - **void refreshEmpty()**

FluidSimulator

- **FluidSimulator.cc:**

- **real rectX1_particle_, rectX2_particle_ , ...**
- **real circR_particle_, circX_particle_ , ...**
- **void set_UVP_surface(int i, int j , const real &dt, bool compP)**
- **void one_empty_neighbour(int i , int j , const real &dt, bool compP)**
- **...**
- **four_empty_neighbour(int i , int j , const real &dt, bool compP)**
- **void refreshEmpty()**

Main while-loop

```
while (n <= nrOfTimeSteps)
{
    ...
    determineNextDT(safetyfac_);
    particle_tracer_.markCells();
    set_UVP_surface(dt_, true);
    computeFG();
    composeRHS();
    solv().solve(grid_);
    updateVelocities();
    refreshBoundaries();
    set_UVP_surface(dt_, false);
    particle_tracer_.advanceParticles(dt_);
    ...
}
```

Examples

- The Breaking Dam - Outflow
- The Breaking Dam - Freeslip
- The Splash of a Liquid Drop

The Breaking Dam

```
imax = 50,      jmax = 20,  
xlength = 10.0, ylength = 4.0,  
tau = 0.5,      delt = 0.04,    t_end = 5.0,  
eps = 0.001,    omg = 1.7,  
gamma = 0.5,    itermax = 500,  
GX = 0.0,      GY = -1.0,      Re = 10.0,  
UI = 0.0,      VI = 0.0,      PI = 0.0,  
ppc=16,  
  
wW = free ,    wE=out ,  
wS = free ,    wN=out
```

The Splash of a Liquid Drop

```
imax = 40,      jmax = 30,  
xlength = 8.0,  ylength = 6.0,  
tau = 0.2,      delt = 0.01,    t_end = 10.0,  
eps = 0.001,    omg = 1.7,  
gamma = 0.5,    itermax = 500,  
GX = 0.0,       GY = -1.0,      Re = 40.0,  
UI = 0.0,       VI = 0.0,       PI = 0.0,  
ppc=16,  
  
wW = free ,     wE=free ,  
wS = free ,     wN=out
```