

Program 2 Report

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Pseudocode

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1. create an array graph, in which each element at index i is an
   array of Edge that are connected to device i. //used for finding
   edges connected a node
2. create array of Node resultGraph where each Node represents a
   device.
3. for each Node n in resultGraph:
    if n is the start node, assign to n Tstart
    else set n to Tfinal+1
    end if
4. Create a PriorityQueue queue, add start node to queue.
5. while queue is not empty:
    current <- first element from queue, remove current from
    queue.
    if current value is greater than Tfinal, no path, end
while.
    if current device is final destination, found a path, end
while.
    add current to Set visited.
    for each unvisited neighbors neighbor of device current
    from resultGraph
        e <- edge connecting current and neighbor
        otherDevice <- device id of neighbor
        if (value of current is less than or equal to
        timestamp of e
            and value of neighbor is greater than timestamp
        of e
```

```

        and timestamp of e is less than or equal to
Tfinal):
    set value of neighbor to timestamp of e
    add neighbor to queue based on its value
    add key otherDevice with value e to trackBack
map.
    end if
end for
end while
6. if not found any path, print "0". end
7. else if found a path:
    set key to destination device.
    while trackBack contain the key key
        get the edge e by key from trackBack, add e to list
trace at first index
        set key to the other device e is connected to
    end while
8. print list trace, containing edges each representing a
connection in path.

```

Time Complexity

The time complexity for this algorithm is $O(E + V)$, ignoring time for queueing and dequeuing operations and reconstructing the trace. Each visited node is added to the visited list so that they are evaluated exactly once. Moreover, we construct a backtrack map to find a node's parent when tracing back the path after we find a solution; this makes sure that edges are not reevaluated. We can ignore the time complexity for reconstructing our path after we found a path because it uses a map so that the time complexity of acquiring every parent is linear.

Proof of correctness

We denote the value of a node to the timestamp of that device in which it can broadcast the queried message. The nodes inside the priority queue is always reachable from start node during the given timeframe. In each of iteration of while loop, the node with the highest priority is evaluated first and added to the visited set. This ensures that the value of a visited node is never overridden by a smaller value later. If there is a path to end node within the given time, then we would find it. It is because the path must be a sequence with increasing timestamps, and we wouldn't miss any paths as we evaluate nodes with smaller timestamps first.