

Lecture 03:

Vanishing gradient, Memory in RNNs

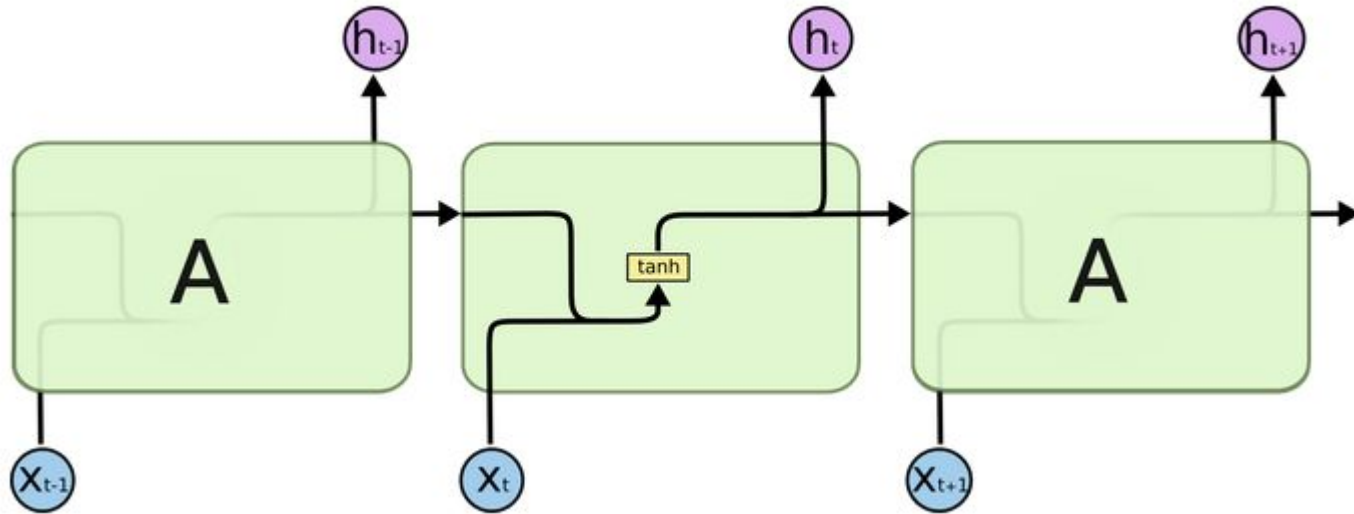
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MADE, Moscow

24.03.2021

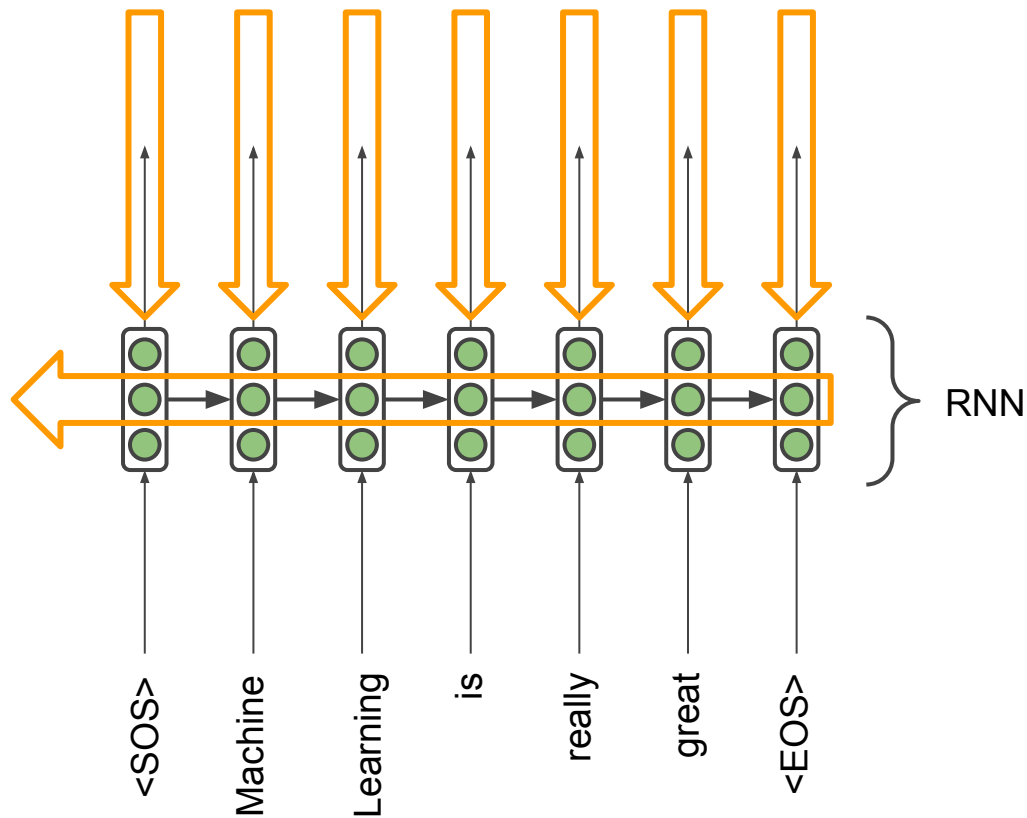
1. Recap: RNNs
2. LSTM overview
 - Gates in LSTM
3. RNNs as encoders for sequential data
4. Vanishing gradient problem
5. Exploding gradient problem
6. Q & A.

Vanilla RNN

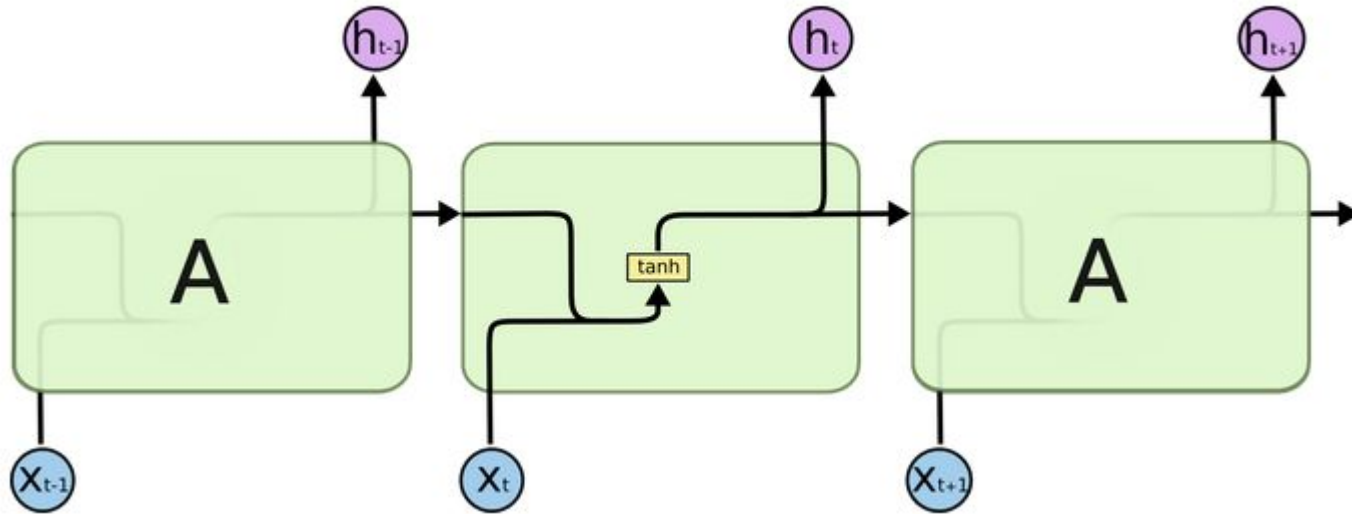


How to train it?

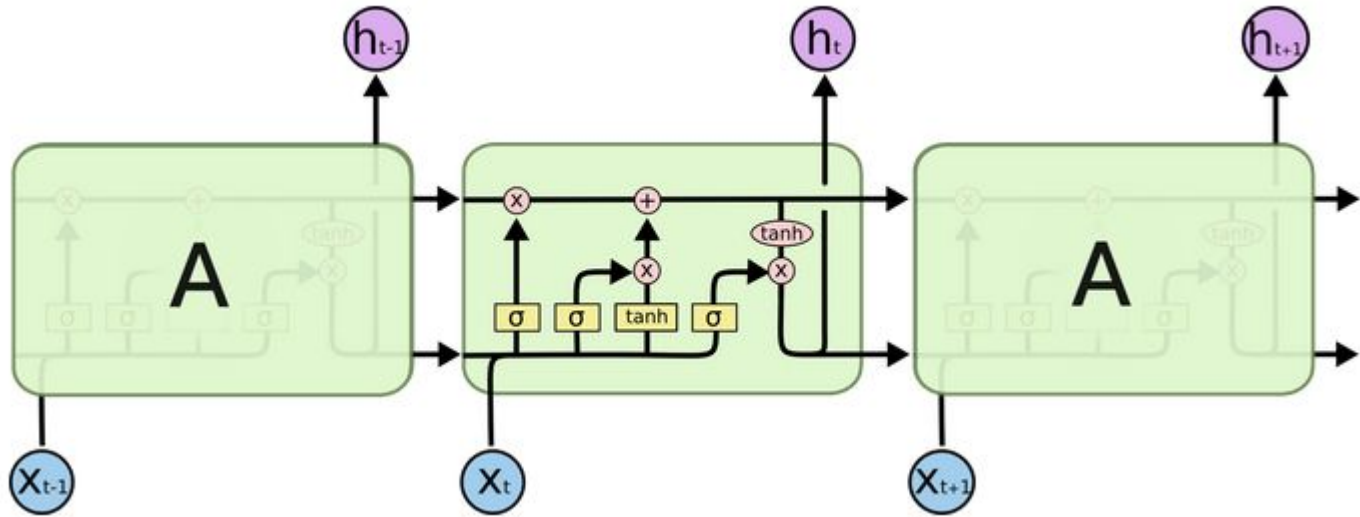
Loss
(e.g. Negative
log-likelihood)



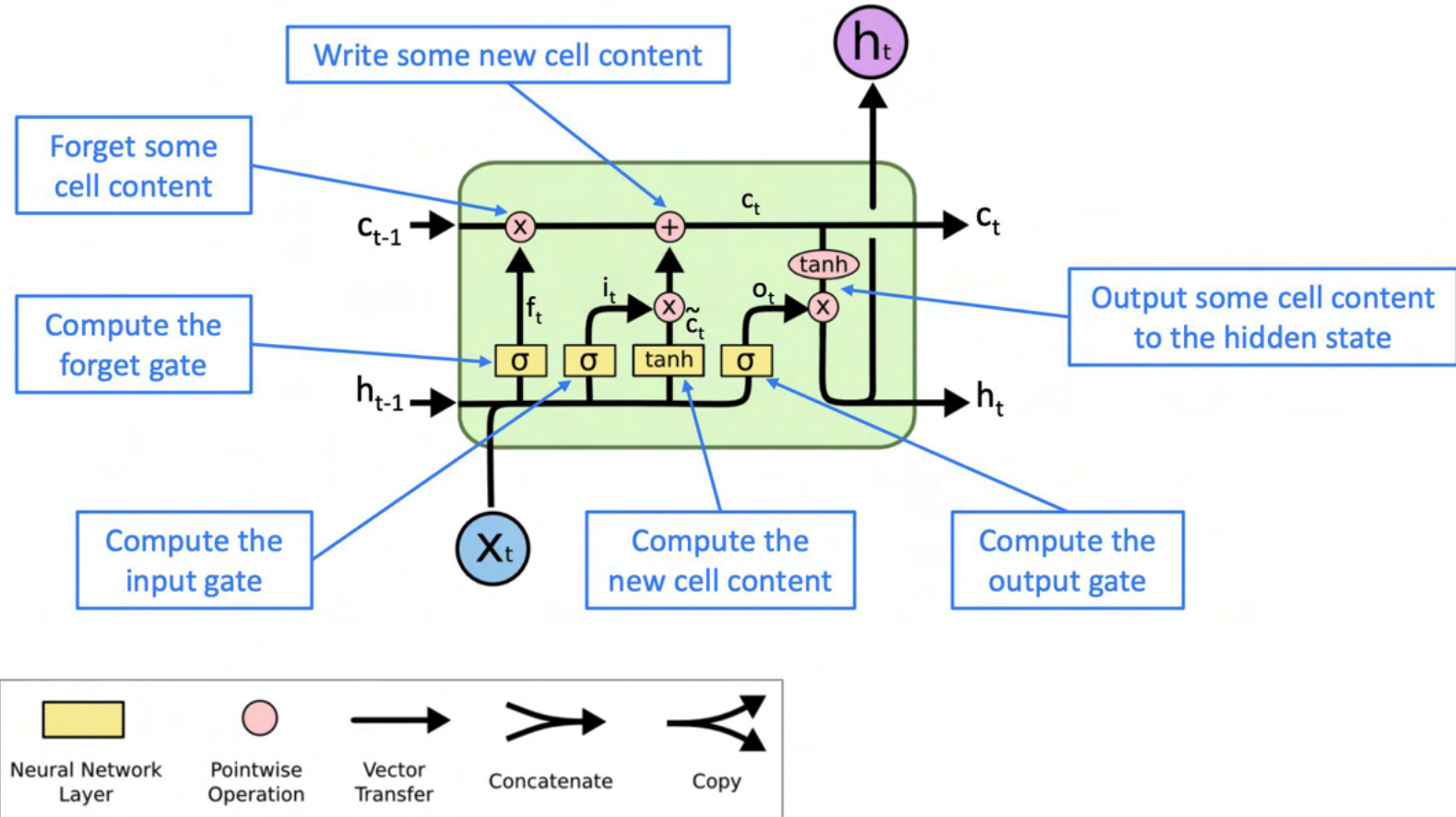
Vanilla RNN



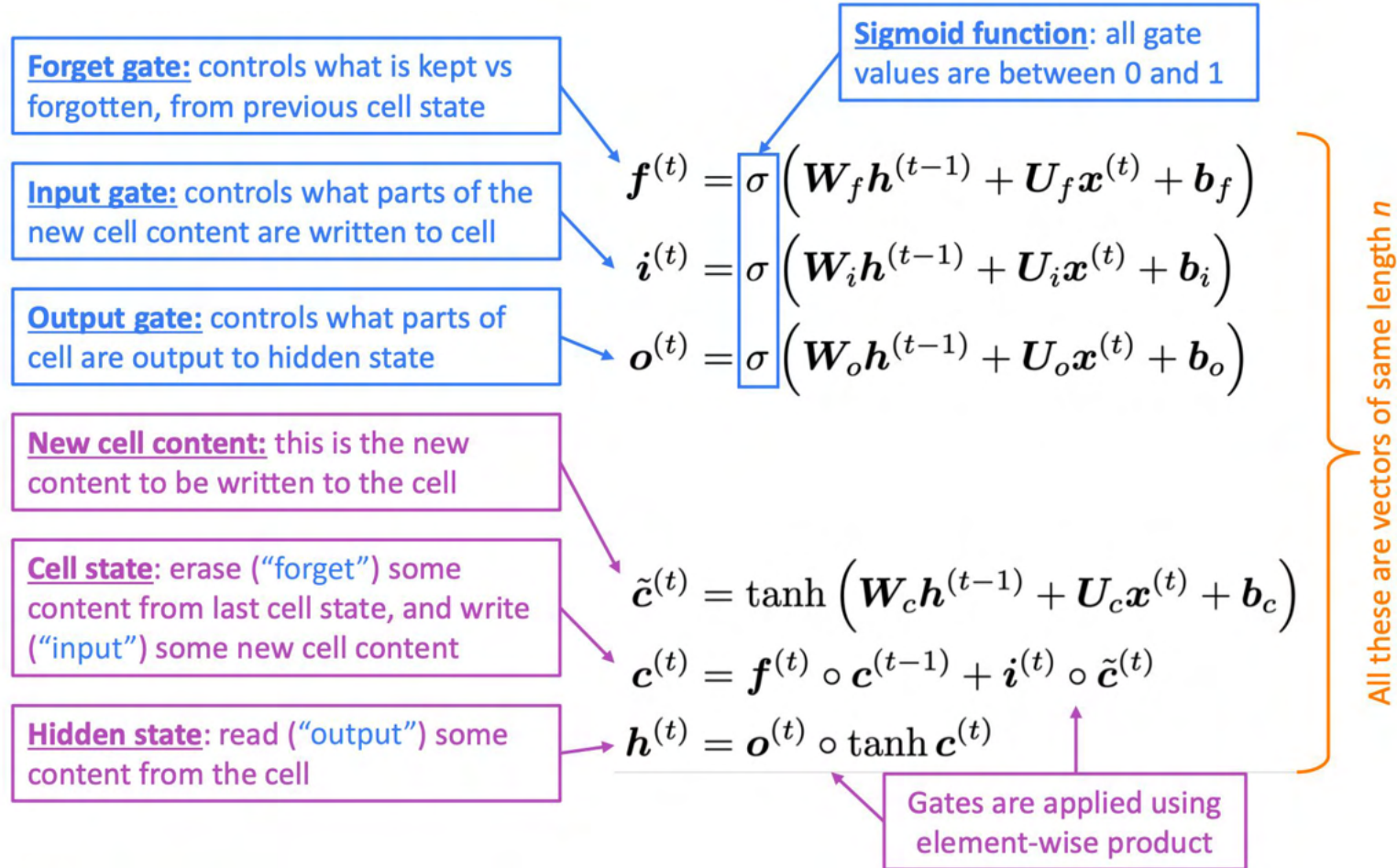
LSTM



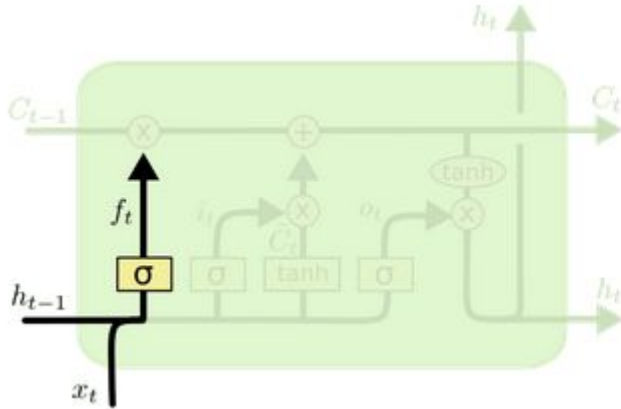
LSTM: quick overview



LSTM: quick overview

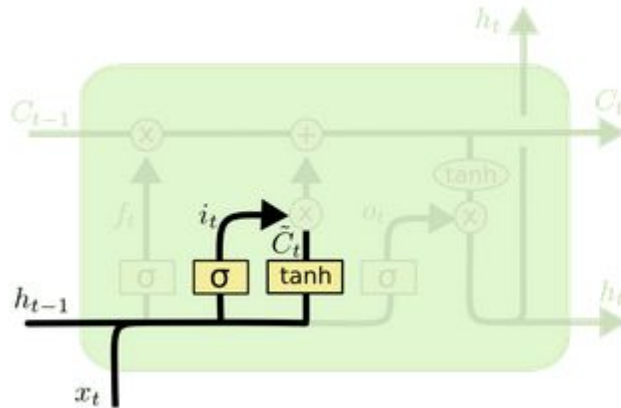


LSTM: quick overview



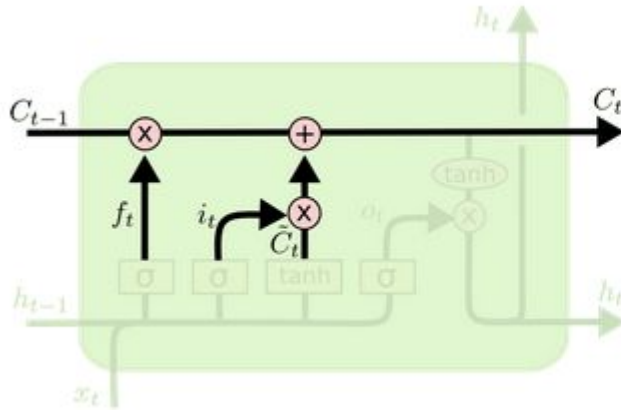
$$f_t = \sigma (W_f \cdot [h_{t-1}, x_t] + b_f)$$

LSTM: quick overview



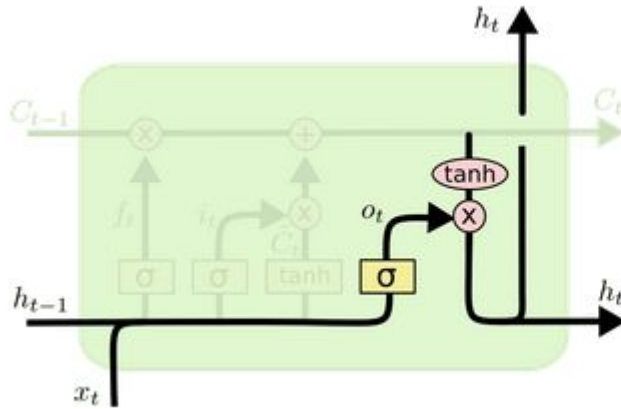
$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i)$$
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

LSTM: quick overview



$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

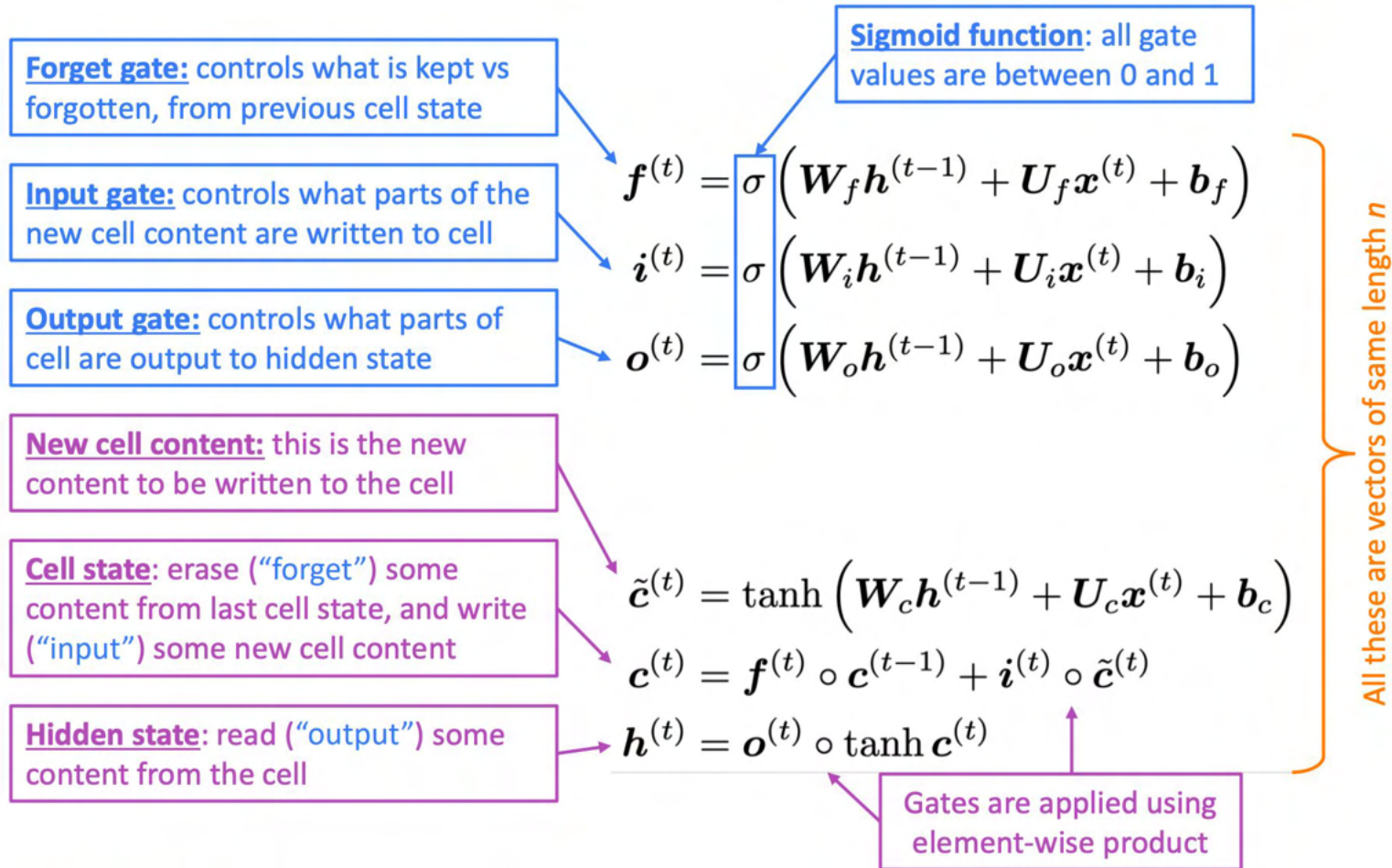
LSTM: quick overview



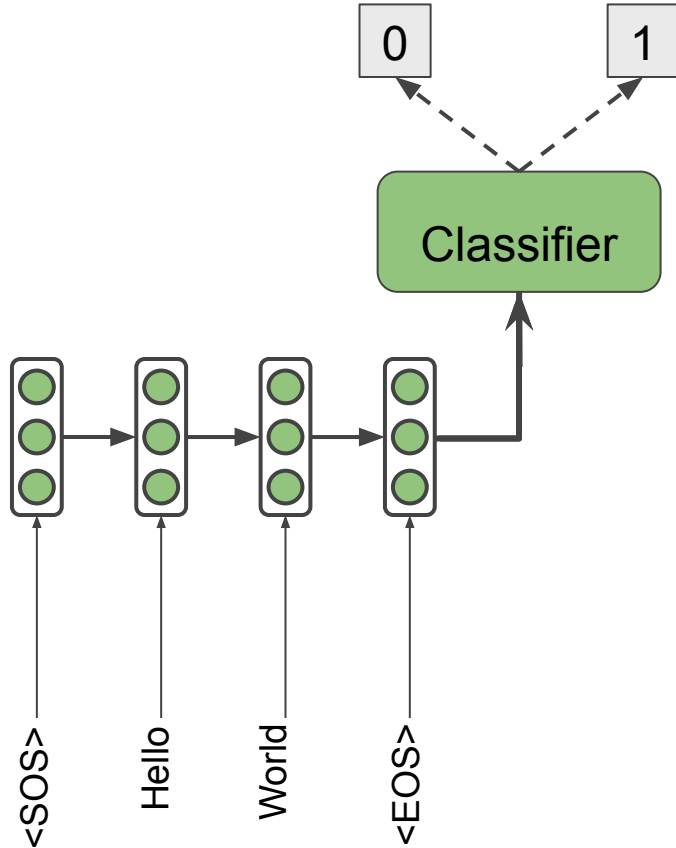
$$o_t = \sigma(W_o [h_{t-1}, x_t] + b_o)$$

$$h_t = o_t * \tanh(C_t)$$

LSTM: with formulas



RNN as encoder for sequential data



RNNs can be used to encode an input sequence in a fixed size vector.

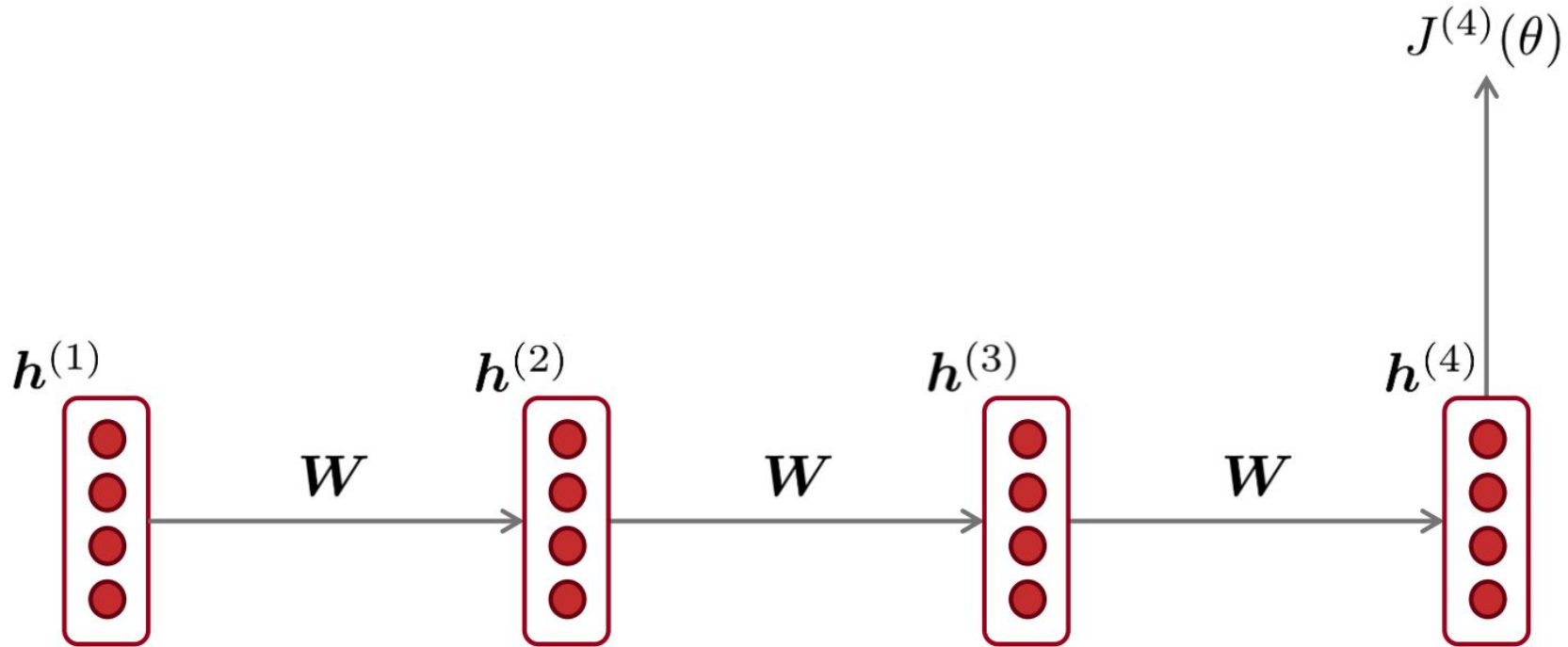
This vector can be treated as a representation of input sequence.

Example problem: PoS tagging

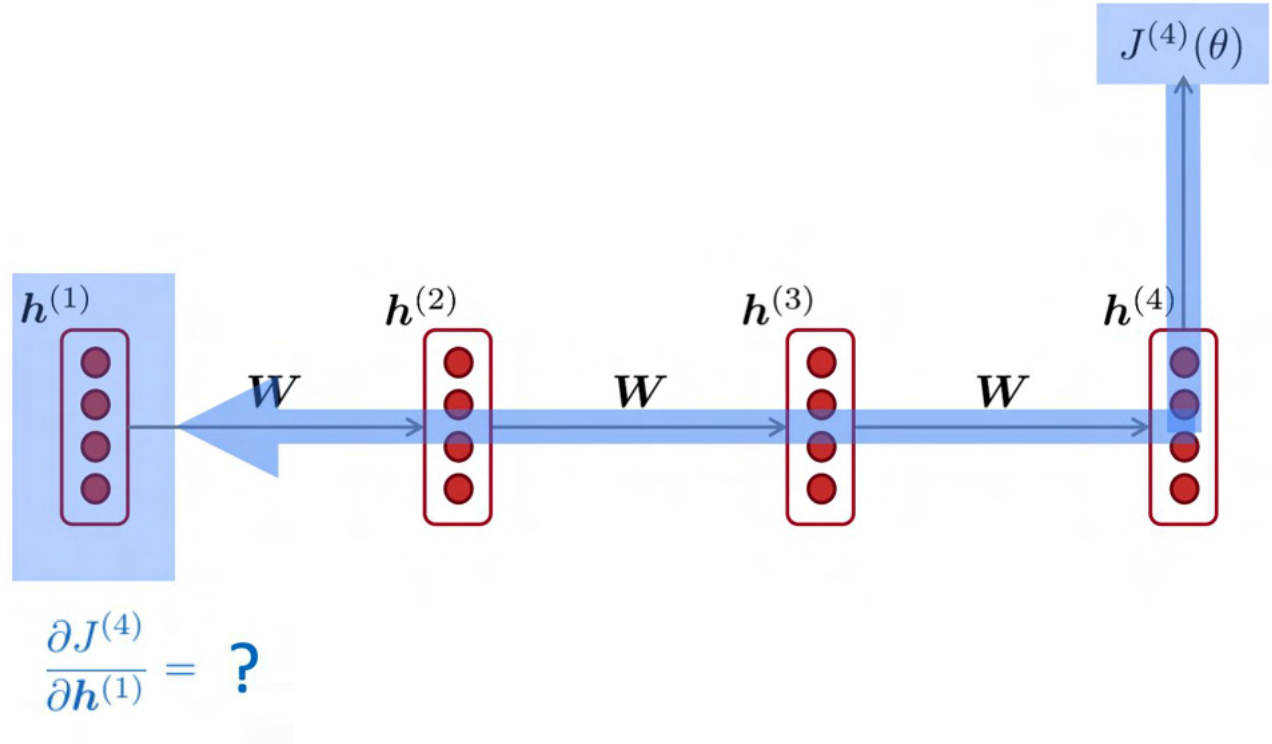
Pred. Tag	Actual Tag	Correct?	Token
PUNCT	PUNCT	✓	[
DET	DET	✓	this
NOUN	NOUN	✓	killing
ADP	ADP	✓	of
DET	DET	✓	a
ADJ	ADJ	✓	respected
NOUN	NOUN	✓	cleric
AUX	AUX	✓	will
AUX	AUX	✓	be
VERB	VERB	✓	causing
PRON	PRON	✓	us
NOUN	NOUN	✓	trouble
ADP	ADP	✓	for
NOUN	NOUN	✓	years
PART	PART	✓	to
VERB	VERB	✓	come
PUNCT	PUNCT	✓	.
PUNCT	PUNCT	✓]

- PoS tagging can be performed using
 - Rule-based taggers
 - Dynamic programming
 - Models based on CRF (Conditional Random Field)
 - Neural Networks
 - etc.

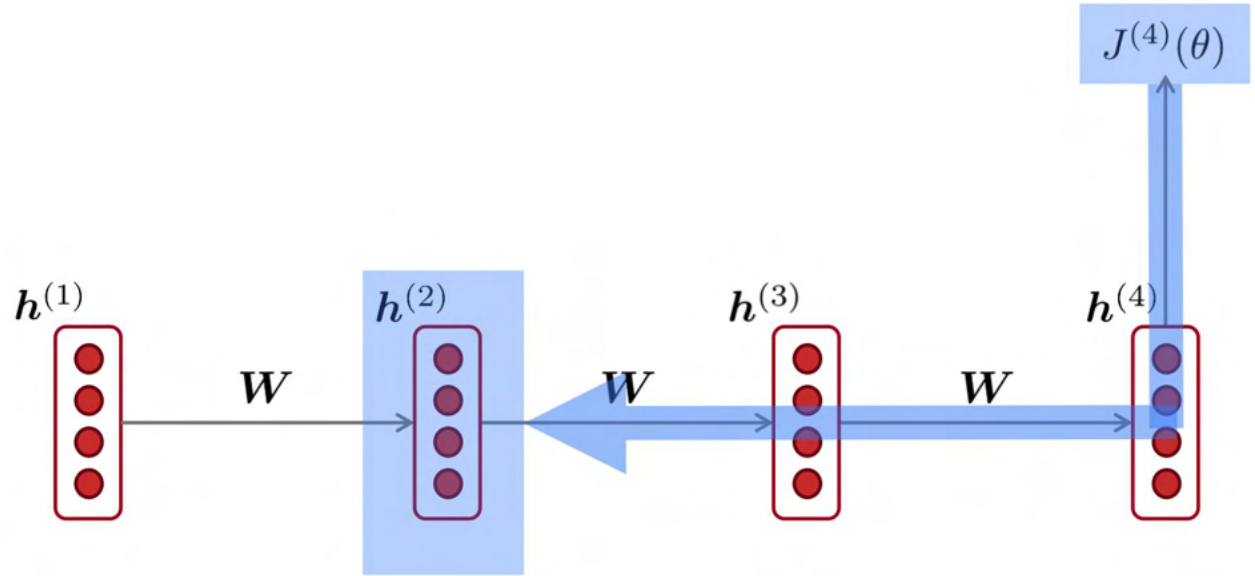
Vanishing gradient problem



Vanishing gradient problem



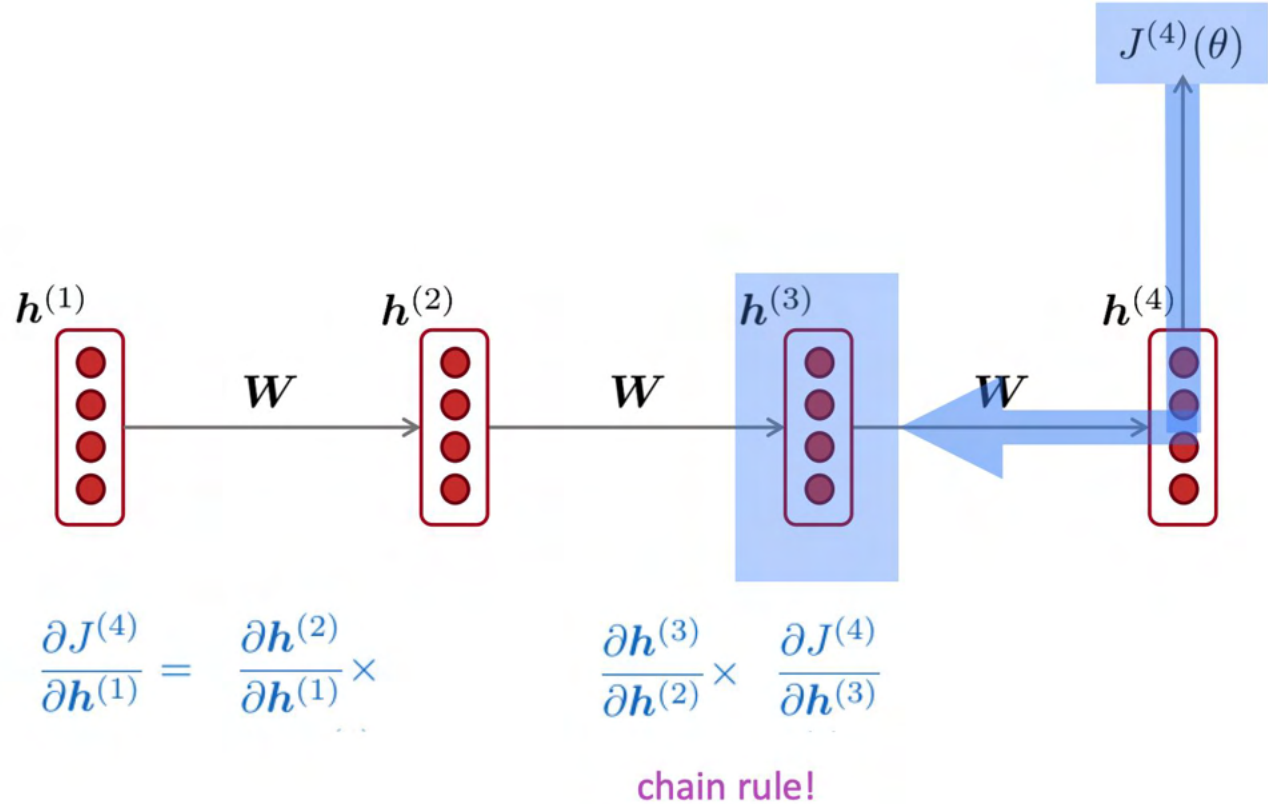
Vanishing gradient problem



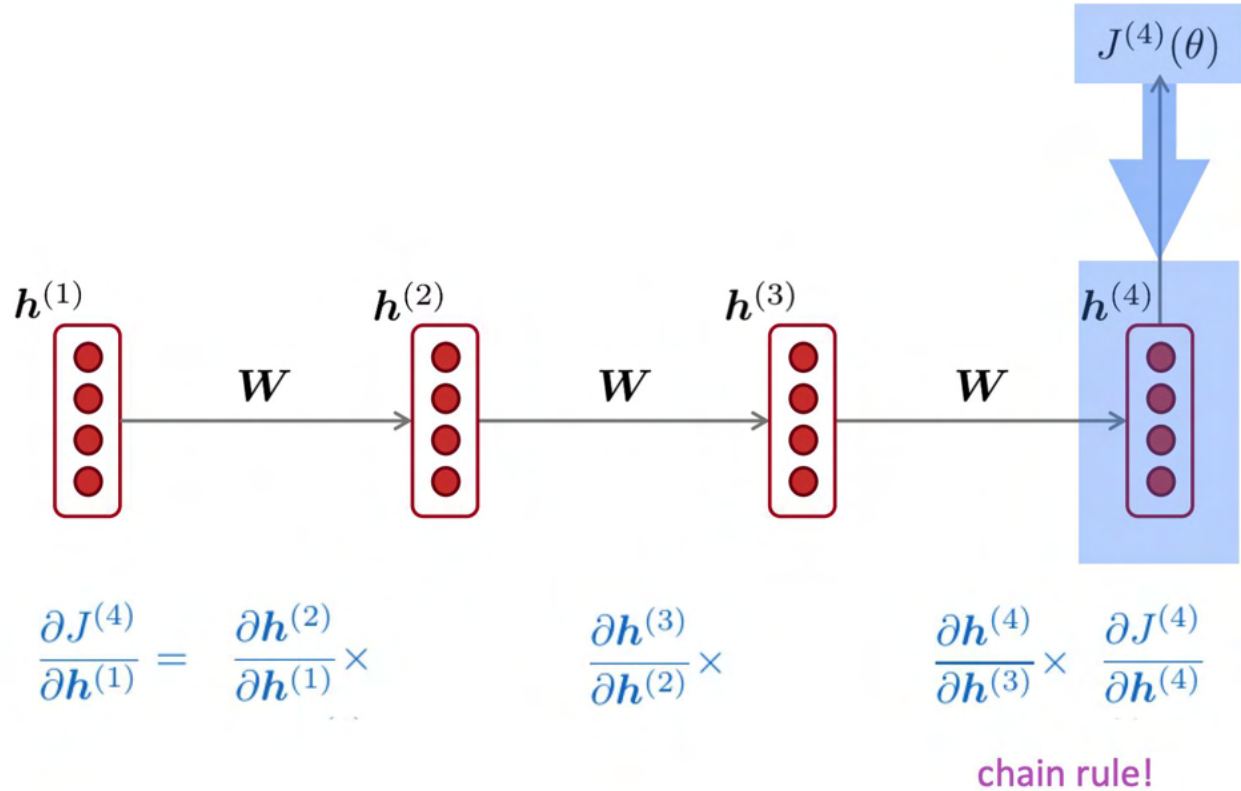
$$\frac{\partial J^{(4)}}{\partial h^{(1)}} = \frac{\partial h^{(2)}}{\partial h^{(1)}} \times \frac{\partial J^{(4)}}{\partial h^{(2)}}$$

chain rule!

Vanishing gradient problem



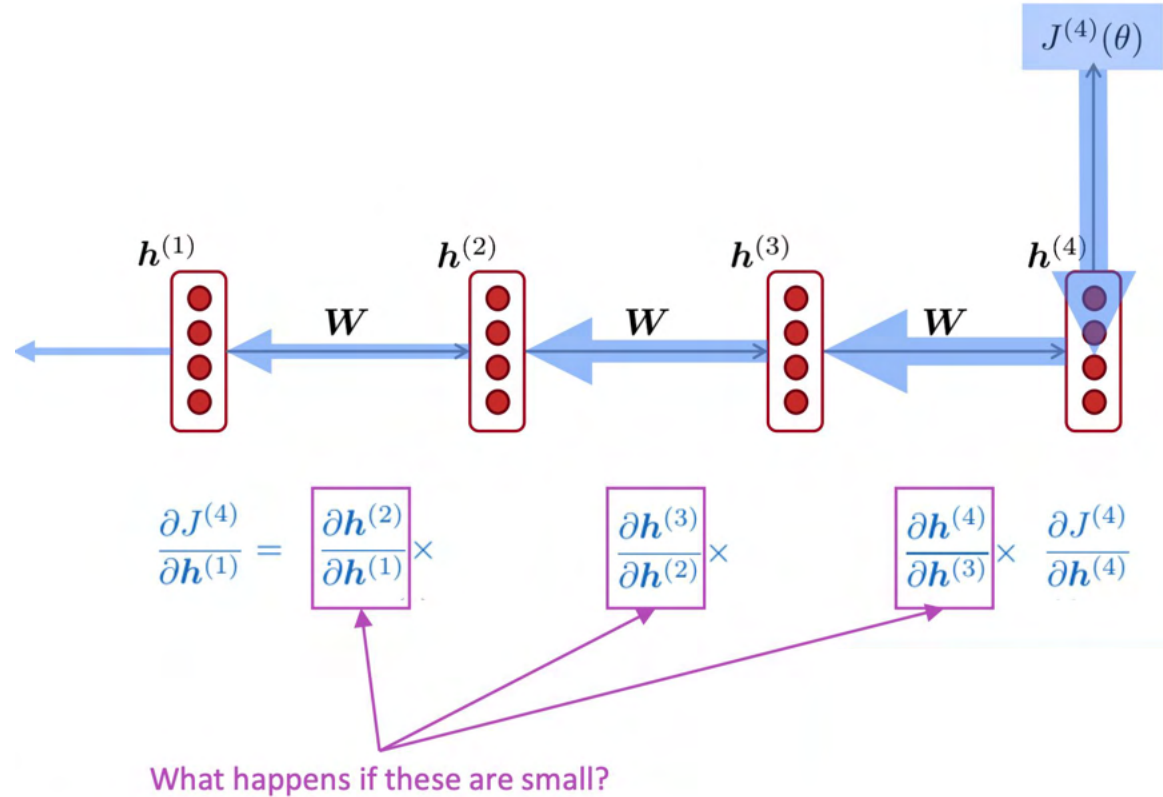
Vanishing gradient problem



Vanishing gradient problem

Vanishing gradient problem:

When the derivatives are small, the gradient signal gets smaller and smaller as it backpropagates further



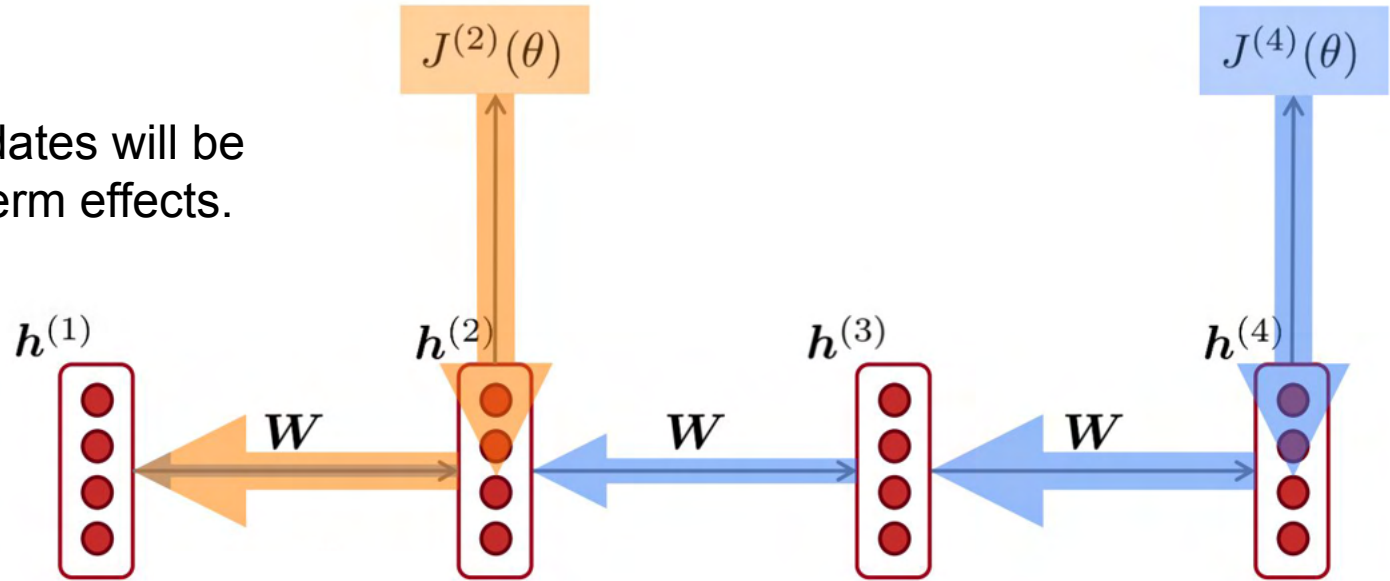
More info: "On the difficulty of training recurrent neural networks", Pascanu et al, 2013

<http://proceedings.mlr.press/v28/pascanu13.pdf>

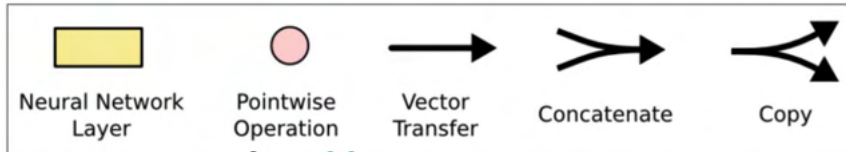
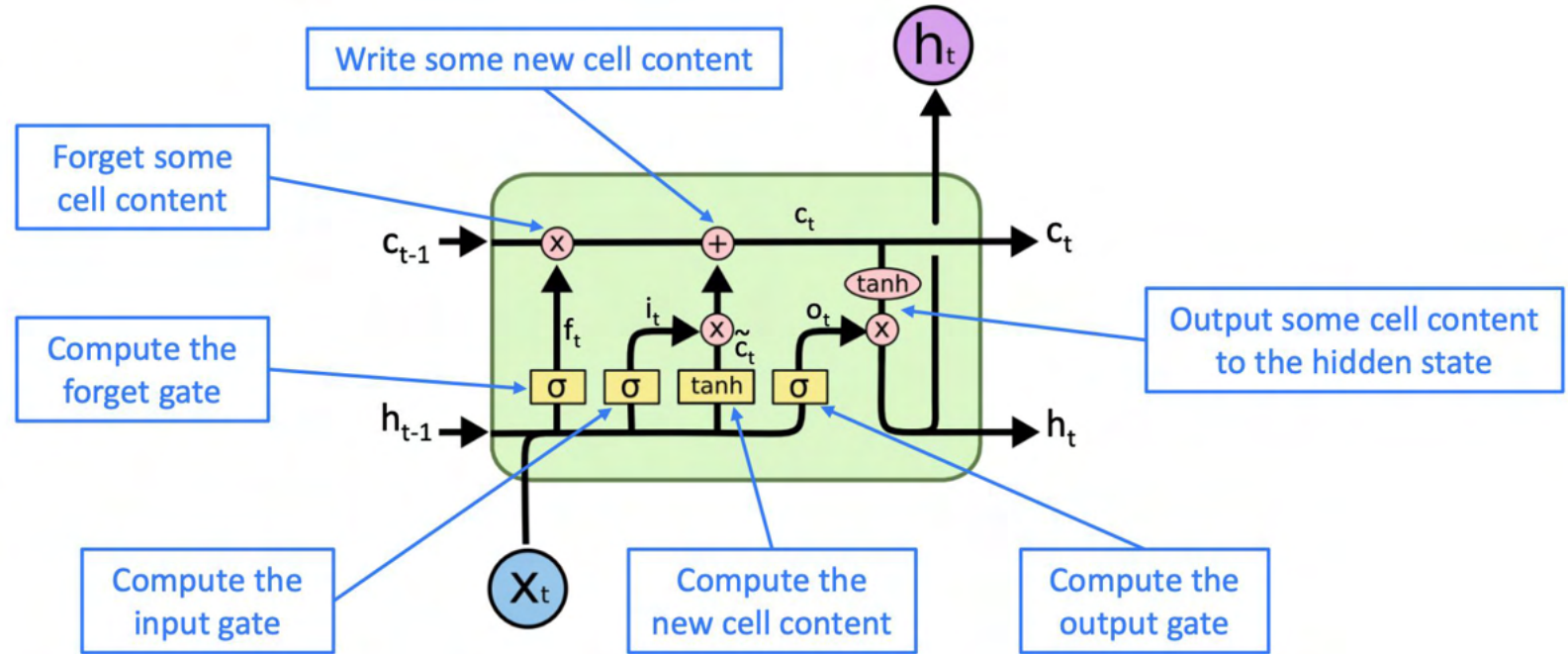
Vanishing gradient problem

Gradient signal from **far away** is lost because it's much smaller than from **close-by**.

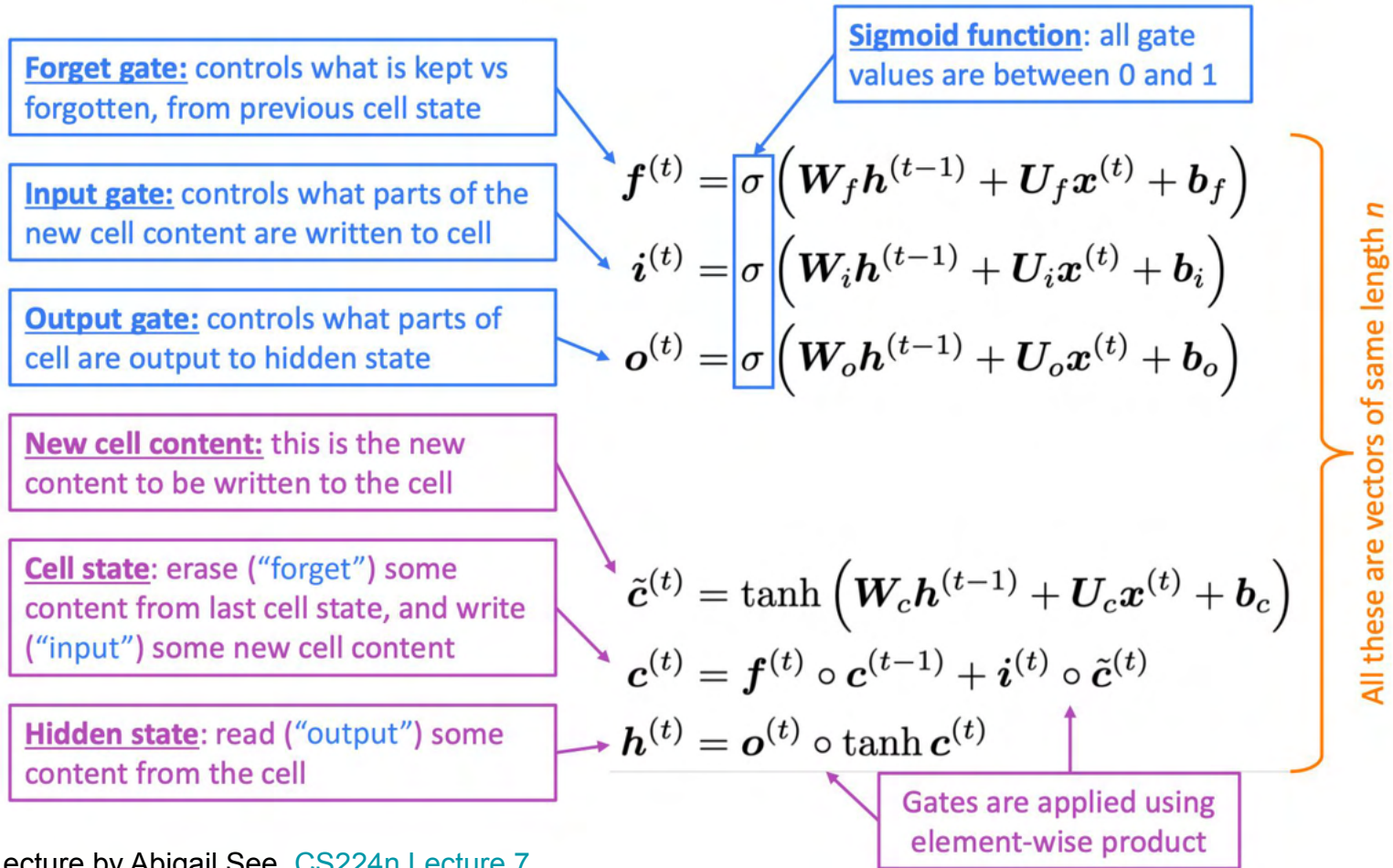
So model weights updates will be based only on short-term effects.



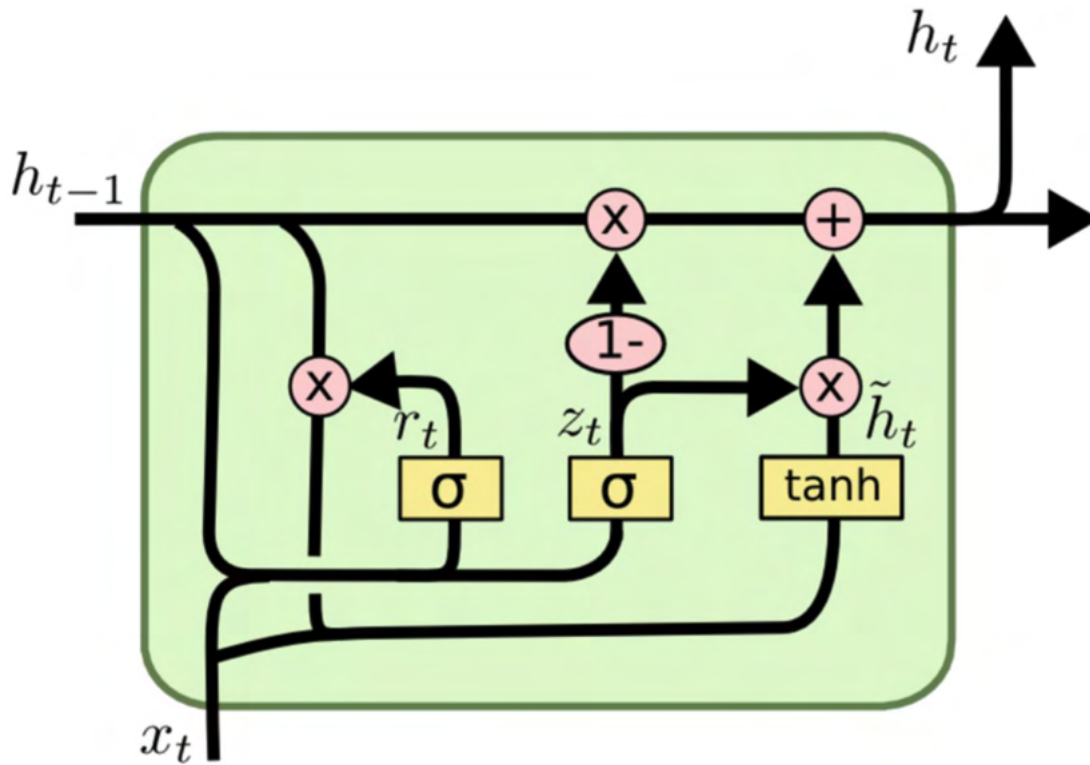
Vanishing gradient: LSTM



Vanishing gradient: LSTM



Vanishing gradient: GRU



Vanishing gradient: GRU

Update gate: controls what parts of hidden state are updated vs preserved

$$\mathbf{u}^{(t)} = \sigma \left(\mathbf{W}_u \mathbf{h}^{(t-1)} + \mathbf{U}_u \mathbf{x}^{(t)} + \mathbf{b}_u \right)$$

Reset gate: controls what parts of previous hidden state are used to compute new content

$$\mathbf{r}^{(t)} = \sigma \left(\mathbf{W}_r \mathbf{h}^{(t-1)} + \mathbf{U}_r \mathbf{x}^{(t)} + \mathbf{b}_r \right)$$

New hidden state content: reset gate selects useful parts of prev hidden state. Use this and current input to compute new hidden content.

$$\tilde{\mathbf{h}}^{(t)} = \tanh \left(\mathbf{W}_h (\mathbf{r}^{(t)} \circ \mathbf{h}^{(t-1)}) + \mathbf{U}_h \mathbf{x}^{(t)} + \mathbf{b}_h \right)$$

$$\mathbf{h}^{(t)} = (1 - \mathbf{u}^{(t)}) \circ \mathbf{h}^{(t-1)} + \mathbf{u}^{(t)} \circ \tilde{\mathbf{h}}^{(t)}$$

Hidden state: update gate simultaneously controls what is kept from previous hidden state, and what is updated to new hidden state content

How does this solve vanishing gradient?

Like LSTM, GRU makes it easier to retain info long-term (e.g. by setting update gate to 0)

Vanishing gradient: LSTM vs GRU

- LSTM and GRU are both great
 - GRU is quicker to compute and has fewer parameters than LSTM
 - There is no conclusive evidence that one consistently performs better than the other
 - LSTM is a good default choice (especially if your data has particularly long dependencies, or you have lots of training data)

Rule of thumb: start with LSTM, but switch to GRU if you want something more efficient

Vanishing gradient in non-RNN

Vanishing gradient is present in **all** deep neural networks

- Due to chain rule / choice of nonlinearity function, gradient can become vanishingly small during backpropagation
- Lower levels are hard to train and are trained slower
- **Potential solution:**
direct (or skip-) connections
(just like in ResNet)

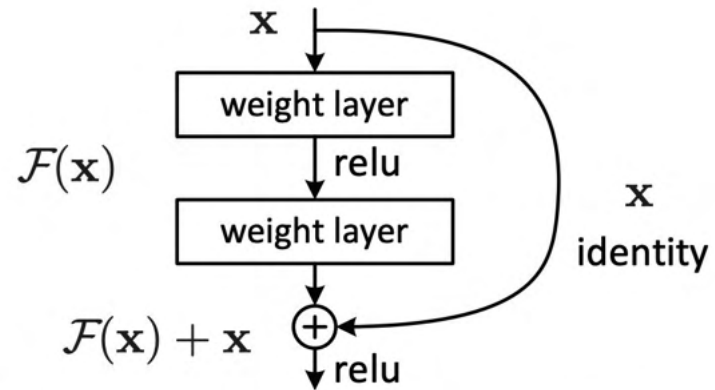
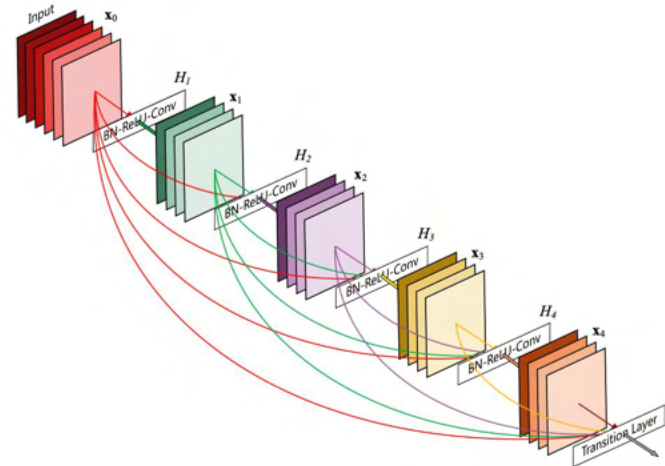


Figure 2. Residual learning: a building block.

Vanishing gradient in non-RNN

Vanishing gradient is present in **all** deep neural networks

- Due to chain rule / choice of nonlinearity function, gradient can become vanishingly small during backpropagation
- Lower levels are hard to train and are trained slower
- **Potential solution:**
dense connections
(just like in DenseNet)



Vanishing gradient in non-RNN

Vanishing gradient is present in **all** deep neural networks

- Due to chain rule / choice of nonlinearity function, gradient can become vanishingly small during backpropagation
- Lower levels are hard to train and are trained slower

Conclusion:

Though vanishing/exploding gradients are a general problem, RNNs are particularly unstable due to the repeated multiplication by the same weight matrix [Bengio et al, 1994]

Exploding gradient problem

- If the gradient becomes too big, then the SGD update step becomes too big: $\theta^{new} = \theta^{old} - \overbrace{\alpha}^{\text{learning rate}} \underbrace{\nabla_{\theta} J(\theta)}_{\text{gradient}}$
- This can cause bad updates: we take too large a step and reach a bad parameter configuration (with large loss)
- In the worst case, this will result in Inf or NaN in your network (then you have to restart training from an earlier checkpoint)

Exploding gradient solution

- Gradient clipping: if the norm of the gradient is greater than some threshold, scale it down before applying SGD update

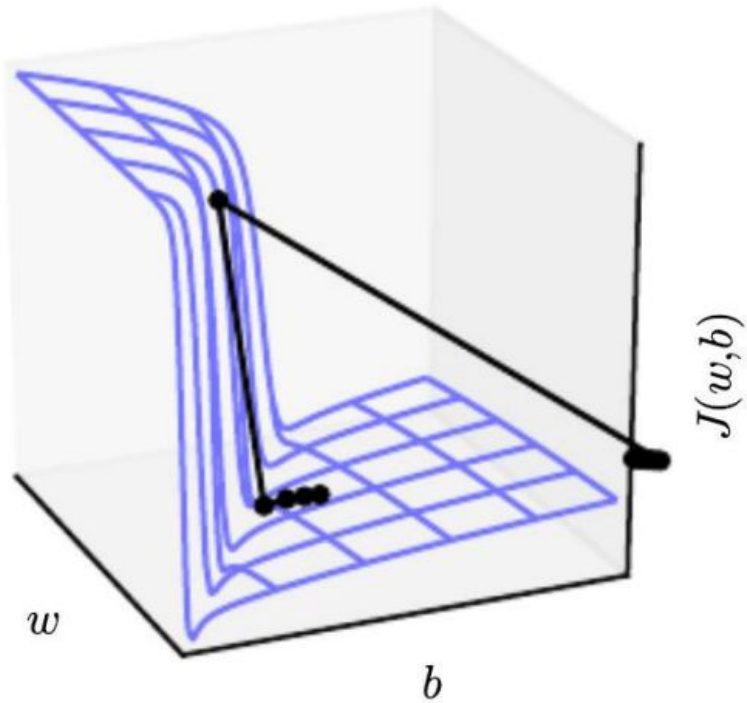
Algorithm 1 Pseudo-code for norm clipping

```
 $\hat{\mathbf{g}} \leftarrow \frac{\partial \mathcal{E}}{\partial \theta}$   
if  $\|\hat{\mathbf{g}}\| \geq threshold$  then  
     $\hat{\mathbf{g}} \leftarrow \frac{threshold}{\|\hat{\mathbf{g}}\|} \hat{\mathbf{g}}$   
end if
```

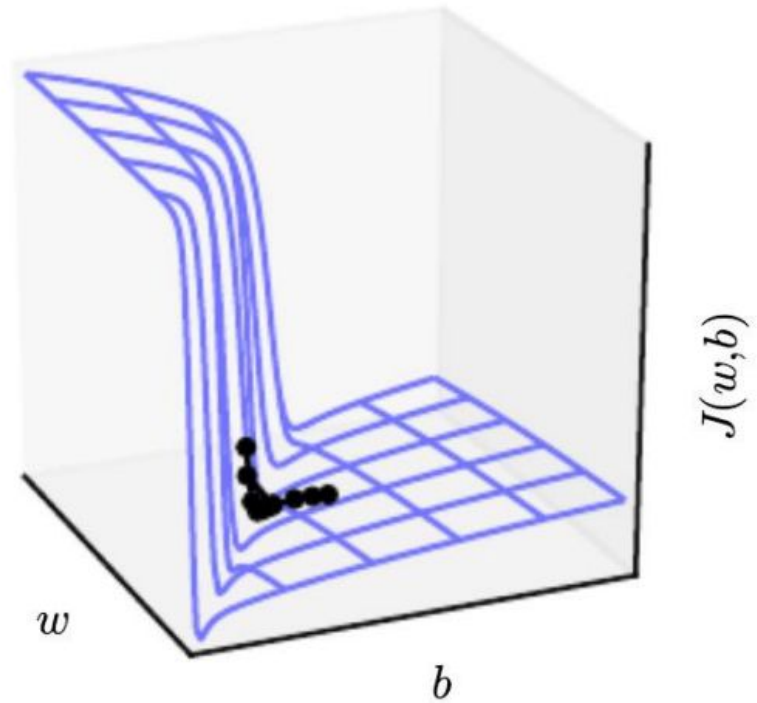
- Intuition: take a step in the same direction, but a smaller step

Exploding gradient solution

Without clipping



With clipping



- RNN is a great choice for data with sequential structure
- Multi-layer RNN can also be of great use
- **Rule of thumb:** start with LSTM, but switch to GRU if you want something more efficient

