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1 # Exercise 2.2 (d).
2 import numpy as np
3 import matplotlib.pyplot as plt
4
5 # Initialize lattice
6 lattice_size = 200
7 lattice = np.sign(np.random.rand(lattice_size,lattice_size) - 0.5)
8 new_lattice = lattice.copy()
9 ten_percent = int(lattice_size*lattice_size/10)
10
11 # Constants
12 J = 1
13 iterations = 1000
14 H_values = np.linspace(-0.05,0.05,50)
15 temperatures = np.array([1,2.269,5])
16 magnetization_array = np.zeros([len(H_values),len(temperatures)])
17
18 for temp_i in range(len(temperatures)):
19
20     T = temperatures[temp_i]
21     beta = 1/T
22     energy_step = 0
23
24     for H_i in H_values:
25
26         H = H_i
27         m = 0
28         lattice_copy = lattice.copy()
29
30         # MC loop
31         for time_step in range(iterations):
32
33             # Update randomly 10% of the cells
34             for update in range(ten_percent):
35
36                 i = np.random.randint(lattice_size)
37                 j = np.random.randint(lattice_size)
38
39                 M = 0
40
41                 # Due to boundaries
42                 if i > 0:
43                     M += lattice_copy[i-1,j]
44                 if i < lattice_size-1:
45                     M += lattice_copy[i+1,j]
46                 if j > 0:
47                     M += lattice_copy[i,j-1]
48                 if j < lattice_size-1:
49                     M += lattice_copy[i,j+1]
50
51                 E_plus = -H-J*M
52                 E_minus = H+J*M
53
54                 probb_plus = np.exp(-beta*E_plus) / (np.exp(-beta*E_plus) + np.exp(-
55                 beta*E_minus))
56                 rnd = np.random.rand()
57
58                 if rnd < probb_plus:
59                     new_lattice[i,j] = 1

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59         else:
60             new_lattice[i,j] = -1
61
62         lattice_copy = new_lattice.copy()
63
64         # Computing magnetization per unit volume to measure the state of the
magnetic property
65         m = lattice_copy.sum() / np.power(lattice_size, 2)
66         magnetization_array[energy_step,temp_i] = m
67         energy_step += 1
68
69         print(H_i)
70
71         print(temp_i)
72
73     coef_0 = np.polyfit(H_values,magnetization_array[:,0],1)
74     coef_1 = np.polyfit(H_values,magnetization_array[:,1],1)
75     coef_2 = np.polyfit(H_values,magnetization_array[:,2],1)
76
77     poly1d_0 = np.poly1d(coef_0)
78     poly1d_1 = np.poly1d(coef_1)
79     poly1d_2 = np.poly1d(coef_2)
80
81     x = np.array([0,0,0])
82     for i in range(len(temperatures)):
83         for j in range(len(H_values)):
84             x[i] += magnetization_array[j,i] / H_values[j]
85     x = x / len(H_values)
86     print(f'x = {x}')
87
88     plt.figure() # T = 1
89     plt.plot(H_values, magnetization_array[:,0], 'g', H_values, poly1d_0(H_values), '--
k')
90     plt.xlabel('Magnetic field, H')
91     plt.ylabel('Magnetization, m')
92     plt.legend(['Magnetic susceptibility','Linear regression'])
93     plt.savefig('22dt1.png', bbox_inches='tight')
94
95     plt.figure() # T = 2.269
96     plt.plot(H_values, magnetization_array[:,1], 'r', H_values, poly1d_1(H_values), '--
k')
97     plt.xlabel('Magnetic field, H')
98     plt.ylabel('Magnetization, m')
99     plt.legend(['Magnetic susceptibility','Linear regression'])
100    plt.savefig('22dtc.png', bbox_inches='tight')
101
102    plt.figure() # T = 5
103    plt.plot(H_values, magnetization_array[:,2], 'b', H_values, poly1d_2(H_values), '--
k')
104    plt.xlabel('Magnetic field, H')
105    plt.ylabel('Magnetization, m')
106    plt.legend(['Magnetic susceptibility','Linear regression'])
107    plt.savefig('22dt5.png', bbox_inches='tight')
108
109    # plt.legend(['T = 1', 'T = 2.269', 'T = 4'])
110    # plt.xlabel('Magnetic field, H')
111    # plt.ylabel('Magnetization, m')
112
113    plt.show()

```