

```

1 import numpy as np
2 import matplotlib.pyplot as plt
3 from scipy.integrate import odeint
4 import sys
5 import os
6
7 xmin = -1
8 ymin = -1
9 xmax = 1
10 ymax = 1
11
12 # Numerical integration
13 T = 100
14 t = np.linspace(0,T,T*100)
15
16 x1 = np.zeros(T)
17 y1 = x1.copy()
18 x1[0] = 0.01
19 y1[0] = 0.01
20
21 x2 = x1.copy()
22 y2 = x1.copy()
23 x2[0] = 0.4
24 y2[0] = 0.4
25
26 x3 = x1.copy()
27 y3 = x1.copy()
28
29 mu = 0.5
30 omega = 0.5
31 nu = 0.5
32 x3[0] = mu
33 y3[0] = mu
34
35 def dynamical_system1(xy, t):
36     x = xy[0]
37     y = xy[1]
38     dxdt_integration = (1/10)*x-y**3-x*y**2-x**2*y-y-x**3
39     dydt_integration = x+(1/10)*y+x*y**2+x**3-y**3-x**2*y
40     return [dxdt_integration, dydt_integration]
41
42 def dynamical_system2(rtheta, t):
43     r = rtheta[0]
44     drdt_integration = mu*r-r**3
45     dthetadt_integration = omega+nu*r**2
46     return [drdt_integration, dthetadt_integration]
47
48 x0y01 = [x1[0],y1[0]]
49 xy1 = odeint(dynamical_system1, x0y01, t)
50 x1 = xy1[:,0]
51 y1 = xy1[:,1]
52
53 x0y02 = [x2[0],y2[0]]
54 xy2 = odeint(dynamical_system1, x0y02, t)
55 x2 = xy2[:,0]
56 y2 = xy2[:,1]
57
58 r0theta0 = [mu**0.5,0]
59 rtheta = odeint(dynamical_system2, r0theta0, t)
60 r = rtheta[:,0]
61 theta = rtheta[:,1]
62 x3 = r*np.cos(theta)
63 y3 = r*np.sin(theta)
64
65 fig, ax = plt.subplots(figsize=(7,7))
66 ax.plot(x1, y1, '-', color='orange', linewidth=2, label='Trajectory going away from f.p. (sys. 2)')
67 ax.plot(x2, y2, '-', color='red', linewidth=2, label='Trajectory going towards f.p. (sys. 2)')
68 ax.plot(x3, y3, '-', color='blue', linewidth=2, label='Limit cycle (sys. 1)')
69 ax.set_title('$3.2b$')
70 ax.set_xlabel('x')
71 ax.set_ylabel('y')
72 ax.set_box_aspect(1)
73
74 plt.legend(loc="upper left")
75 plt.savefig('Dynamical systems/DS HW3/3.2/3.2b.png', bbox_inches='tight')

```

```
76 plt.show()
```