

Master Degree in Astrophysics and Cosmology

# Wolf-Rayet – black hole binaries as progenitors of binary black holes

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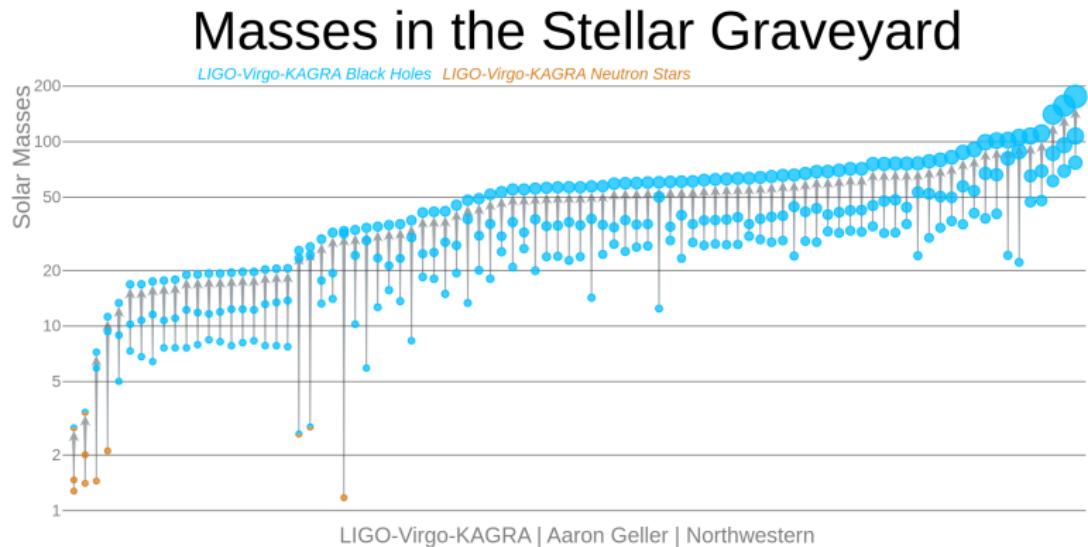
21<sup>st</sup> September 2022



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# Explaining gravitational wave detections

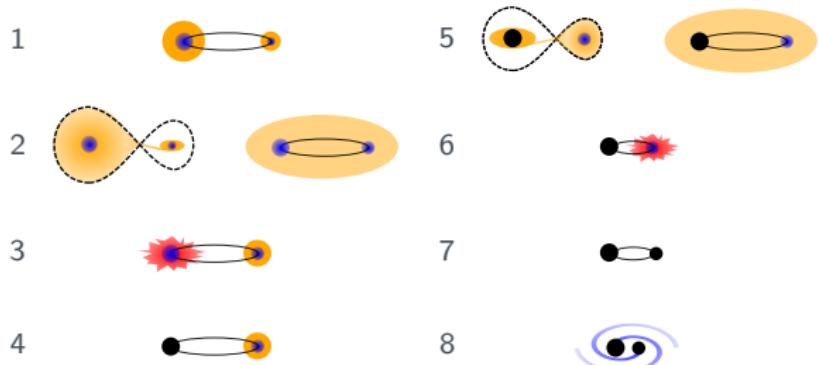
Which are the evolutionary channels of the  $\sim 90$  compact object binaries observed with gravitational wave detectors?



# Limited state-of-the-art models

## Probable evolution:

- 1 Isolated binary
- 2 Mass transfer (?)
- 3 Supernova
- 4 Black hole + star
- 5 Mass transfer
- 6 Supernova
- 7 Binary black hole (BBH)
- 8 Merging via GW emission



## Uncertainties:

- Mass transfer
- Core-collapse supernova
- Supernova kick

~ 80 merging BBHs detected...

...can we observe their progenitors?

# Wolf-Rayet – black hole binaries

**Time to merge only via  
GW emission**

## Wolf-Rayet stars:

- Strong stellar winds ( $\dot{M} \sim 10^4 - 10^5 M_{\odot} \text{ yr}^{-1}$ )
- Little or no H envelope → mass transfer product?
- $R_{\text{WR}} \sim R_{\odot}$  → allow close orbits  $a \gtrsim R_{\odot}$  → merging?

$$t_{\text{GW}}^* \sim 12 \text{ Gyr} \left( \frac{a}{20 R_{\odot}} \right)^4$$

*Peters 1964*

**Only 7 known Wolf-Rayet – black hole candidates**

Host galaxy	Name	$M_{\text{BH}}$ [ $M_{\odot}$ ]	$M_{\text{WR}}$ [ $M_{\odot}$ ]	$P$ [hours]	$t_{\text{GW}}^*$ [Gyr]
Milky Way	Cyg X-3	3-10	8-14	4.8	0.02
IC 10	IC10 X-1	-	17-35	34.9	3.5
NGC 300	NGC300 X-1	13-21	15-26	32.8	2.9
NGC 253	CXOU J004732.0-251722.1	-	-	14.5	0.3
Circinus	CG X-1	-	-	7.2	0.05
M101	M101 ULX-1	8-46	17-19	196.8	348
NGC 4490	CXOU J123030.3+413853	-	-	6.4	0.04

\*  $t_{\text{GW}}$  estimated with Peters 1964, assuming circular orbit and  $M_1 = M_2 = 10 M_{\odot}$

# Goals and methodology of the thesis

## Goals:

- 1 **Wolf-Rayet – black hole:** progenitors of merging BBHs at  $Z_{\odot}$ ?
- 2 **Cyg X-3:** case-study for evolution of merging BBHs at  $Z_{\odot}$

**Model-independent results? → 24 combinations of parameters**

## Methodology:

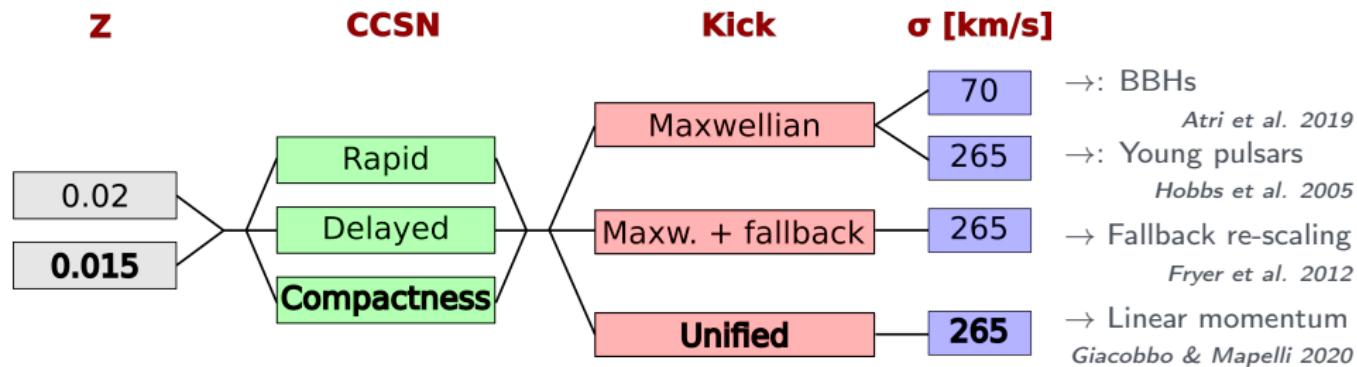
- I generated **24 sets of  $10^6$  binaries** → initial conditions representative of early-binaries observed in the Milky Way

*Sana et al. 2012, Moe & Di Stefano 2017*

- **Simulations with the population-synthesis code SEVN**  
*(Stellar EVolution for N-body simulations)*

*Spera et al. 2019, Costa et al. 2021, Iorio et al. in prep.*

# Parameter space in SEVN



## Core-collapse supernova (CCSN)

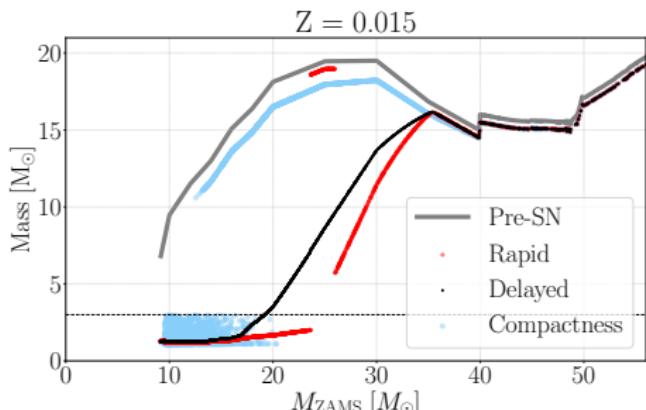
Preference for compact object masses:

- Light (Rapid/Delayed)

*Fryer et al. 2012*

- Heavy (Compactness)

*Mapelli et al. 2020*



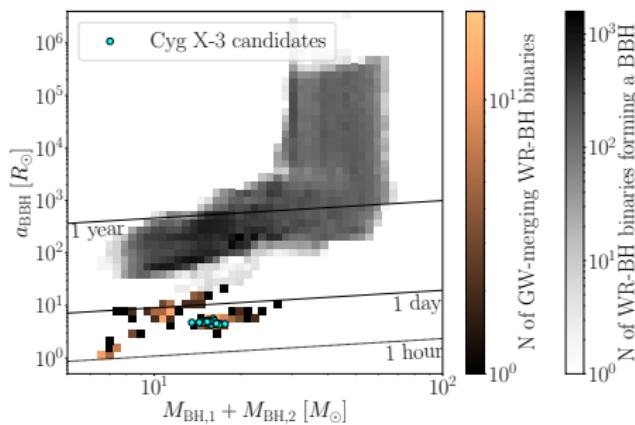
# Results: key progenitors at $Z_{\odot}$

## Main results:

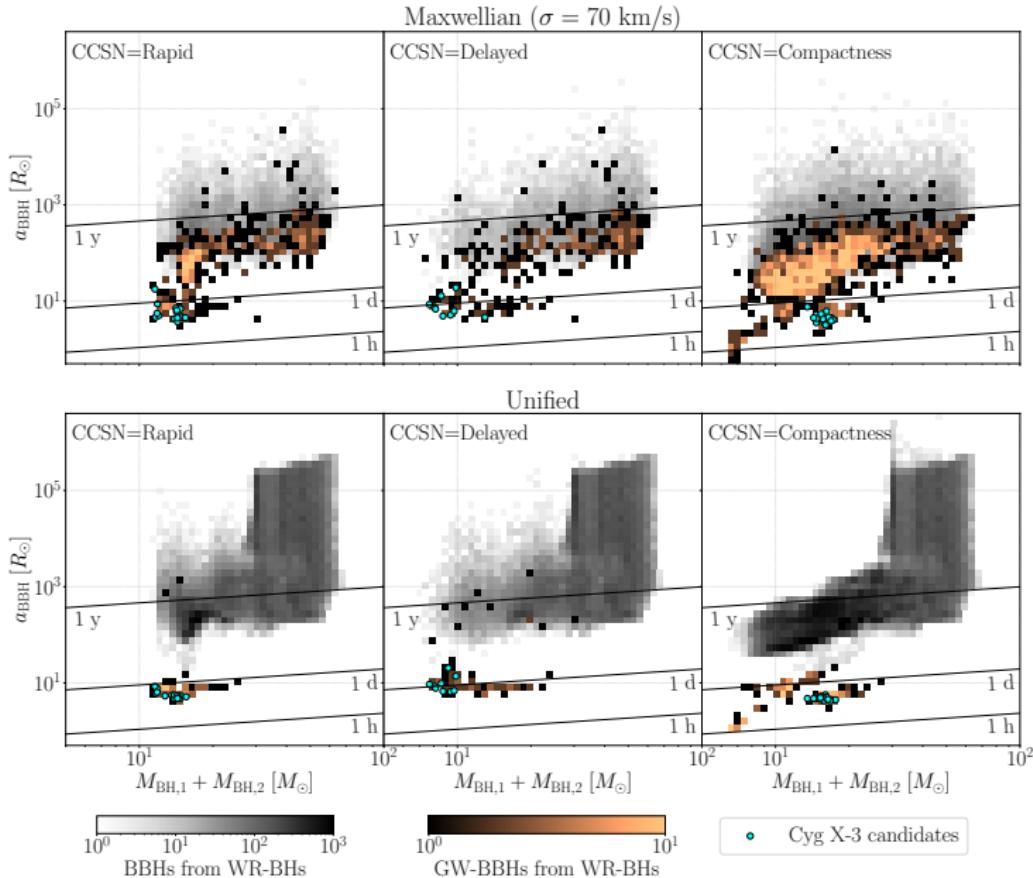
- 1 Wolf-Rayet – black hole: required for merging BBHs at  $Z_{\odot}$   
**( $\gtrsim 90\%$  probability)**
- 2 Cyg X-3: progenitor of merging BBHs  
**( $\gtrsim 75\%$  probability)**

## In this parameter space:

- Results almost model-independent
- Cyg X-3 represents a sub-population of merging BBHs progenitors



# Probing the parameter space at Z=0.015



Natal kicks

Pure Maxwellian



merging BBHs

$a_{\text{BBH}} \lesssim 1000 R_\odot$



$t_{\text{GW}} \propto (1 - e^2)^{7/2}$

Peters 1964

Maxwellian  
rescaled for

- Compact object mass
- Ejecta mass

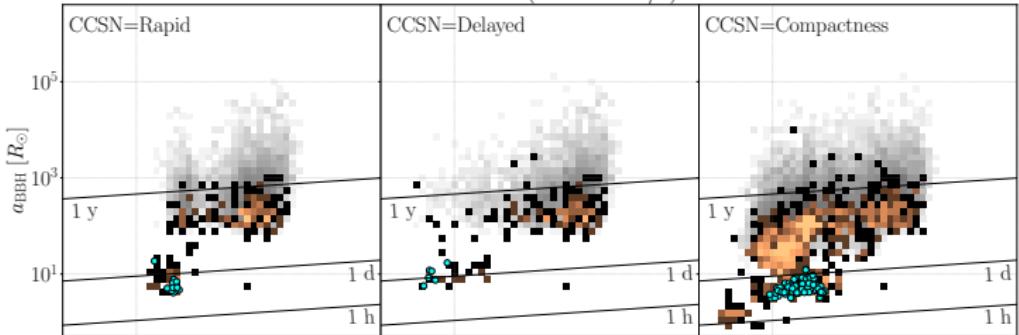


merging BBHs

$a_{\text{BBH}} \lesssim 20 R_\odot$

# Probing the parameter space at Z=0.02

Maxwellian ( $\sigma = 70 \text{ km/s}$ )



**Metallicity**

**Negligible effect**

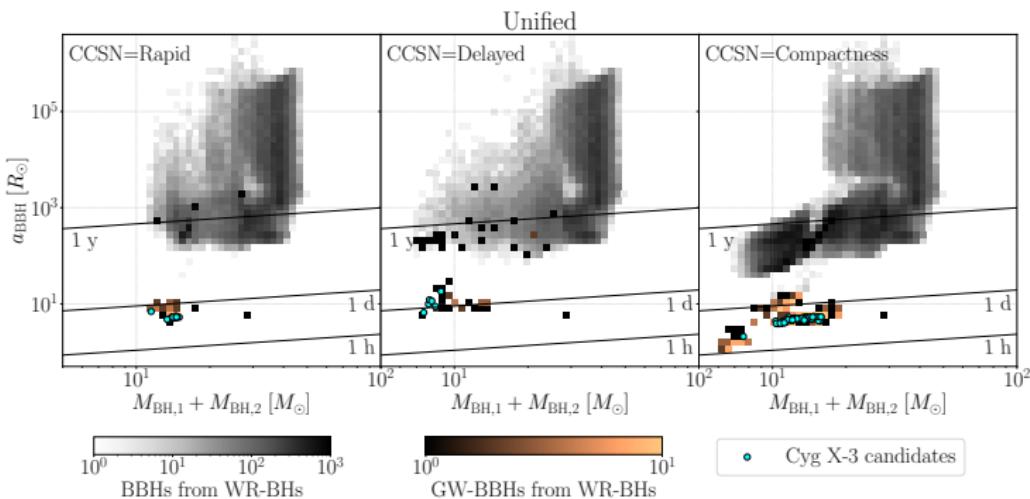


**Mass variation**



**Mass transfer selection**

**CCSN**

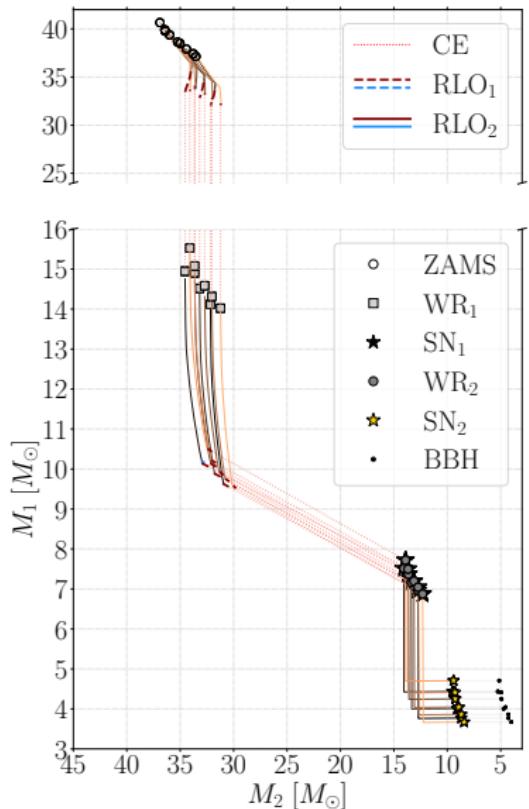
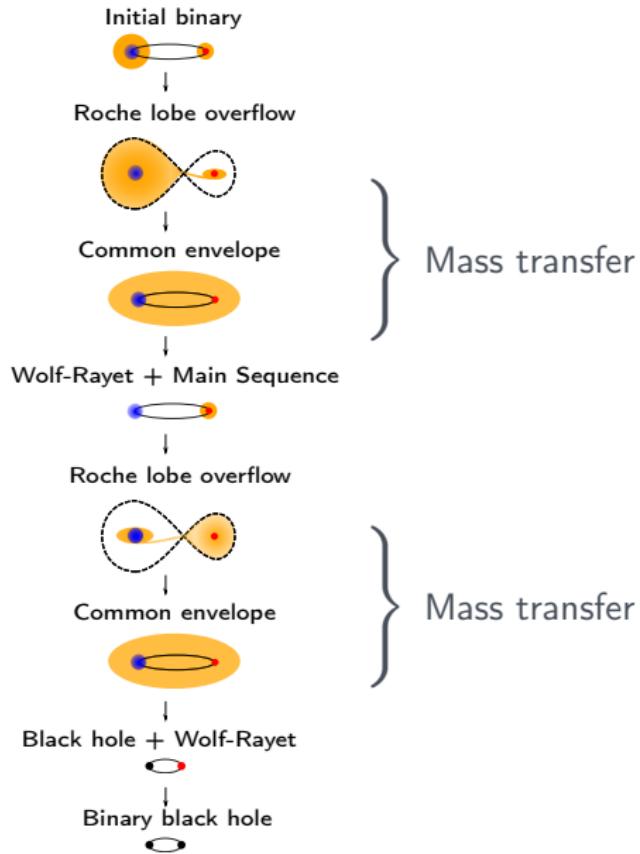


• Cyg X-3 candidates

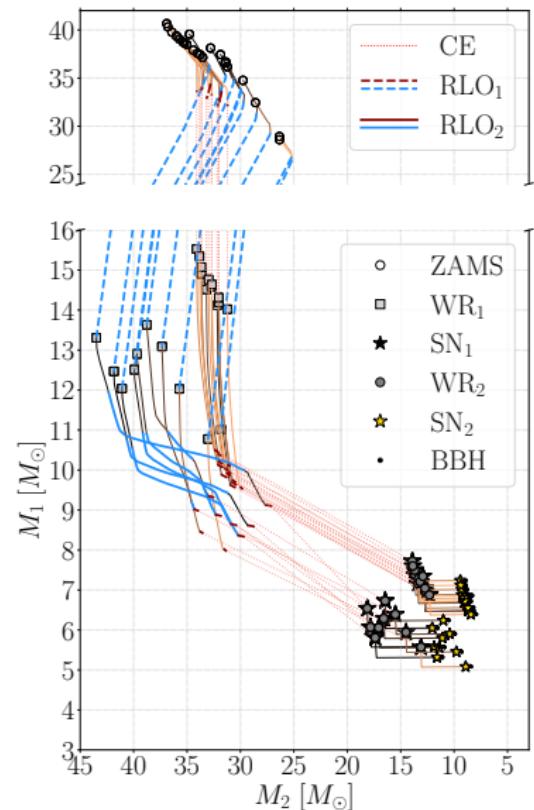
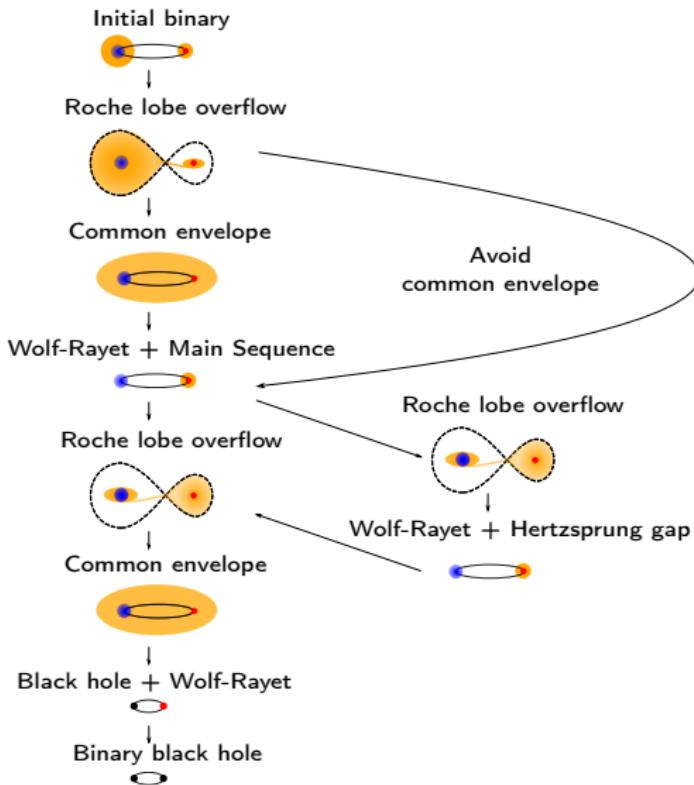
BBHs from WR-BHs

GW-BBHs from WR-BHs

# Delayed CCSN: 2 common envelope



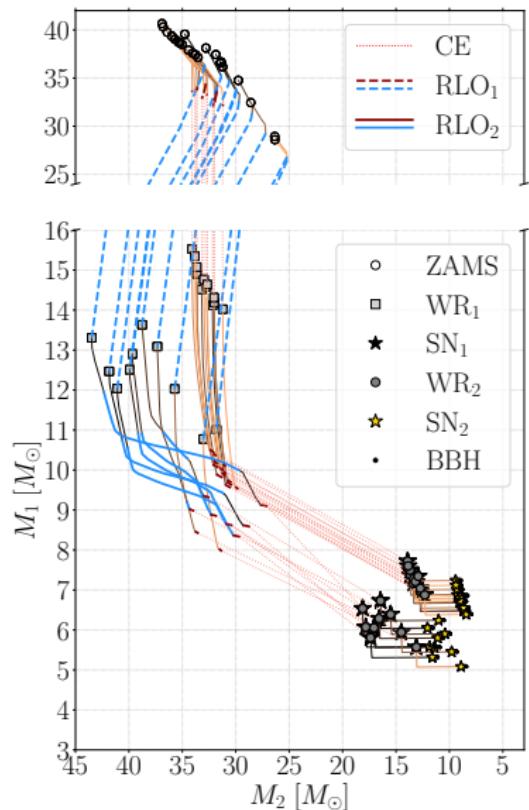
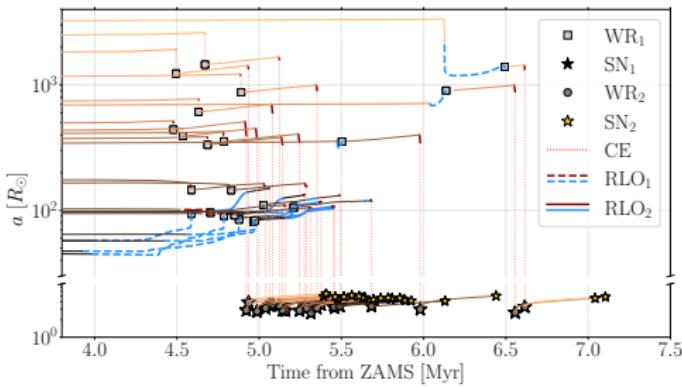
# Compactness CCSN: 2 or 3 mass transfer



# Cyg X-3 evolution and properties

## For the fiducial model:

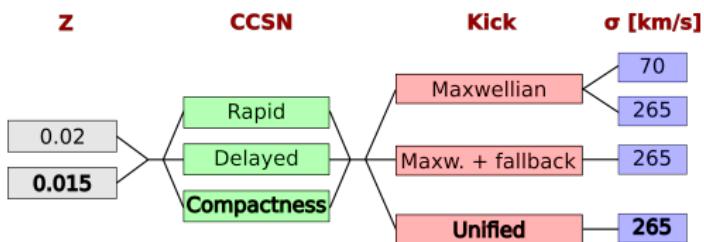
- $M_{\text{ZAMS},1,2} \sim 30 - 40 M_{\odot}$   
 $a_{\text{ZAMS}} \sim 50 - 3000 R_{\odot}$
- 2 or 3 mass transfer episodes  
**(1 common envelope needed)**
- Wolf-Rayet – black hole for  $\sim 0.5$  Myr
- **Wind-fed systems**
- BBHs merging in  $\sim 50 - 200$  Myr



# Conclusions

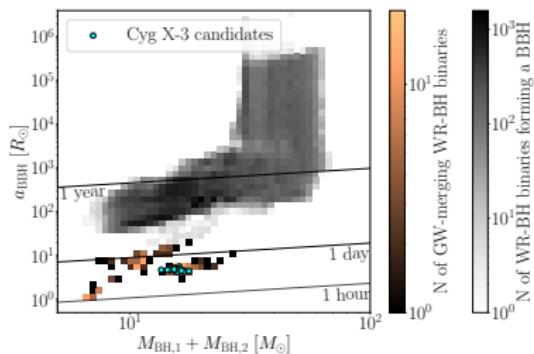
## Results (almost) model-independent:

- 1 Wolf-Rayet – black hole: necessary stage to form merging BBHs at  $Z_{\odot}$  ( $\gtrsim 90\%$  probability)
- 2 Cyg X-3: progenitor of merging BBHs ( $\gtrsim 75\%$  probability)



## Cyg X-3:

- Representative of a sub-population of merging BBHs progenitors
- 2 or 3 mass transfer (1 common envelope)



Wolf-Rayet – black hole observations → “Rosetta stone” for merging BBHs

**Thank you for the attention**

## **Additional slides**

# CCSN models in SEVN

## Rapid

$$M_{\text{proto}} = 1.0 M_{\odot}, \quad (15)$$

$$\begin{cases} M_{\text{fb}} = 0.2 M_{\odot} & M_{\text{CO}} < 2.5 M_{\odot} \\ M_{\text{fb}} = 0.286 M_{\text{CO}} - 0.514 M_{\odot} & 2.5 M_{\odot} \leq M_{\text{CO}} < 6.0 M_{\odot} \\ f_{\text{fb}} = 1.0 & 6.0 M_{\odot} \leq M_{\text{CO}} < 7.0 M_{\odot} \\ f_{\text{fb}} = a_1 M_{\text{CO}} + b_1 & 7.0 M_{\odot} \leq M_{\text{CO}} < 11.0 M_{\odot} \\ f_{\text{fb}} = 1.0 & M_{\text{CO}} \geq 11.0 M_{\odot} \end{cases} \quad (16)$$

with  $a_1 = 0.25 - (1.275/M - M_{\text{proto}})$ ,  $b_1 = -11a_1 + 1$ , and  $M_{\text{fb}} = f_{\text{fb}}(M - M_{\text{proto}})$  in the mass range for which  $f_{\text{fb}}$  is given.

The final baryonic mass of the remnant is then

$$M_{\text{rem,bar}} = M_{\text{proto}} + M_{\text{fb}} \quad (17)$$

## Delayed

$$\begin{cases} M_{\text{proto}} = 1.2 M_{\odot} & M_{\text{CO}} < 3.5 M_{\odot} \\ M_{\text{proto}} = 1.3 M_{\odot} & 3.5 M_{\odot} \leq M_{\text{CO}} < 6.0 M_{\odot} \\ M_{\text{proto}} = 1.4 M_{\odot} & 6.0 M_{\odot} \leq M_{\text{CO}} < 11.0 M_{\odot} \\ M_{\text{proto}} = 1.6 M_{\odot} & M_{\text{CO}} \geq 11.0 M_{\odot} \end{cases} \quad (18)$$

This assumes that the delay increases for more massive cores, causing more material to accrete onto the proto-NS during the explosion.

The amount of fallback is given by

$$\begin{cases} M_{\text{fb}} = 0.2 M_{\odot} & M_{\text{CO}} < 2.5 M_{\odot} \\ M_{\text{fb}} = 0.5 M_{\text{CO}} - 1.05 M_{\odot} & 2.5 M_{\odot} \leq M_{\text{CO}} < 3.5 M_{\odot} \\ f_{\text{fb}} = a_2 M_{\text{CO}} + b_2 & 3.5 M_{\odot} \leq M_{\text{CO}} < 11.0 M_{\odot} \\ f_{\text{fb}} = 1.0 & M_{\text{CO}} \geq 11.0 M_{\odot} \end{cases} \quad (19)$$

with  $a_2 = 0.133 - (0.093/M - M_{\text{proto}})$ ,  $b_2 = -11a_2 + 1$ , and  $M_{\text{fb}} = f_{\text{fb}}(M - M_{\text{proto}})$  in the mass range for which  $f_{\text{fb}}$  is given.

The final baryonic mass of the remnant is then

$$M_{\text{rem,bar}} = M_{\text{proto}} + M_{\text{fb}}, \quad (20)$$

Fryer et al. 2012

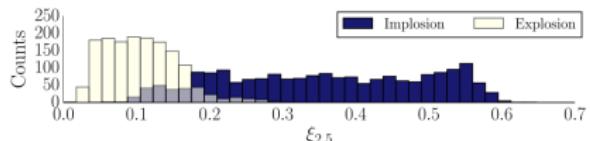
## Compactness

$$\xi_{2.5} = \frac{2.5}{R(2.5 M_{\odot})}$$

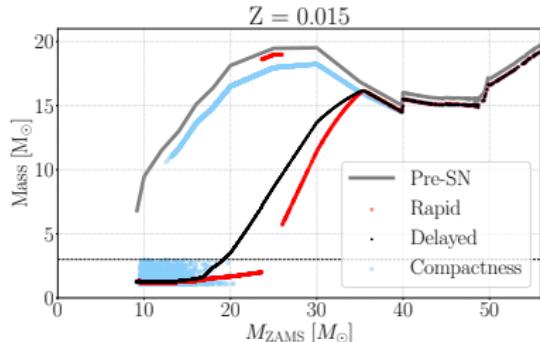
O'Connor et al. 2011

$$\xi_{2.5} = 0.55 - 1.1 \left( \frac{1 M_{\odot}}{M_{\text{CO}}} \right)$$

Mapelli et al. 2020



Sukhbold et al. 2016



# Kick models in SEVN

## Maxwellian

$$v = f_\sigma$$

- $\sigma = 70 \text{ km/s} \rightarrow \text{BBHs natal kicks}$

*Atri et al. 2019*

- $\sigma = 265 \text{ km/s} \rightarrow \text{young pulsars natal kicks}$

*Hobbs et al. 2005*

## Maxwellian (+ fallback)

$$v = f_\sigma (1 - f_{\text{fb}})$$

$$f_{\text{fb}} = M_{\text{fb}} / (M_{\text{rem}} - M_{\text{proto}}) \in [0, 1]$$

*Fryer et al. 2012*

## Unified

$$v = f_\sigma \frac{M_{\text{ej}}}{\langle M_{\text{ej}} \rangle} \frac{\langle M_{\text{NS}} \rangle}{M_{\text{rem}}}$$

$$M_{\text{ej}} = M_{\text{pre-SN}} - M_{\text{rem}}$$

with  $\langle M_{\text{NS}} \rangle \sim 1.30 M_\odot$     $\langle M_{\text{ej}} \rangle \sim 10.30 M_\odot$

*Giacobbo & Mapelli 2020*

# Mass transfer in SEVN



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Unstable Roche lobe overflow if  $q \geq q_{\text{crit}}$

Stellar phase	Burning	Condition	BSE phase	$q_{\text{crit}}$
Main sequence	H-core	$M_{\text{ZAMS}} \geq 0.7 M_{\odot}$	1	3.0
Hertzsprung-gap	H-shell	$f_{\text{conv}} < 0.33$	2	4.0
First giant branch	H-shell	$f_{\text{conv}} \geq 0.33$	3	Equation 1
Core He burning	He-core	$f_{\text{conv}} < 0.33$	4	3.0
Asymptotic giant branch	He-shell	$f_{\text{conv}} \geq 0.33$	5	Equation 1
Wolf-Rayet	He-core	$M_{\text{He}} > 0.979 M_{\odot}$	7	3.0
Wolf-Rayet	He-shell	$M_{\text{He}} > 0.979 M_{\odot}$	8	0.784

$$q_{\text{crit}} = 0.362 + \frac{1}{3 \left( 1 - \frac{M_{\text{He,d}}}{M_d} \right)}. \quad (1)$$

*Hurley et al. 2002, Iorio et al. in prep.*

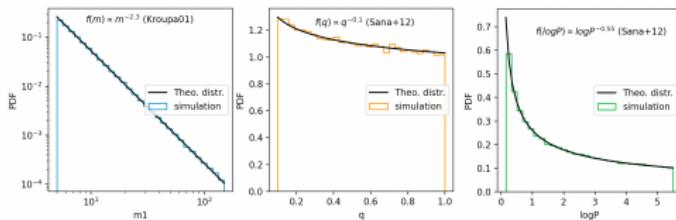
# Initial conditions with SEVN

## Primary masses

$$\xi(M_1) \propto M_1^{-2.3}$$

$$M_1 \in [10, 150] M_{\odot}$$

*Sana et al. 2012*



## Mass ratios

$$\xi(q) \propto q^{0.1}$$

$$q = M_2/M_1 \in [0.1, 1]$$

$$\xi(M_2) = \xi(M_1) \xi(q)$$

$$M_2 \in [1 M_{\odot}, M_1]$$

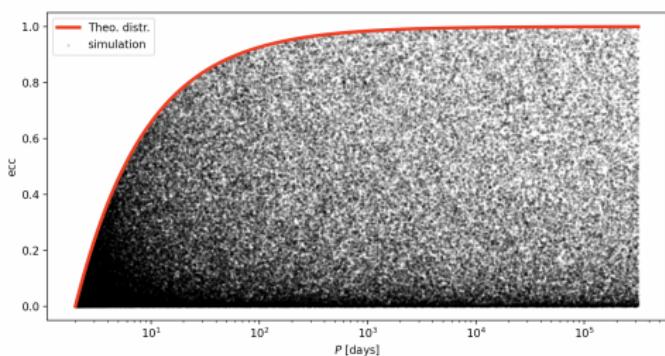
*Sana et al. 2012*

## Periods

$$\xi(\mathcal{P}) \propto \mathcal{P}^{-0.55}$$

$$\mathcal{P} = \log(P/\text{days}) \in [0.30, 5.5]$$

*Sana et al. 2012*



## Eccentricities

$$\xi(e(P)) \propto 1 - (P/\text{days})^{-2/3}$$

$$P \geq 2 \text{ days}$$

*Moe & Di Stefano 2017*

# Results (1)

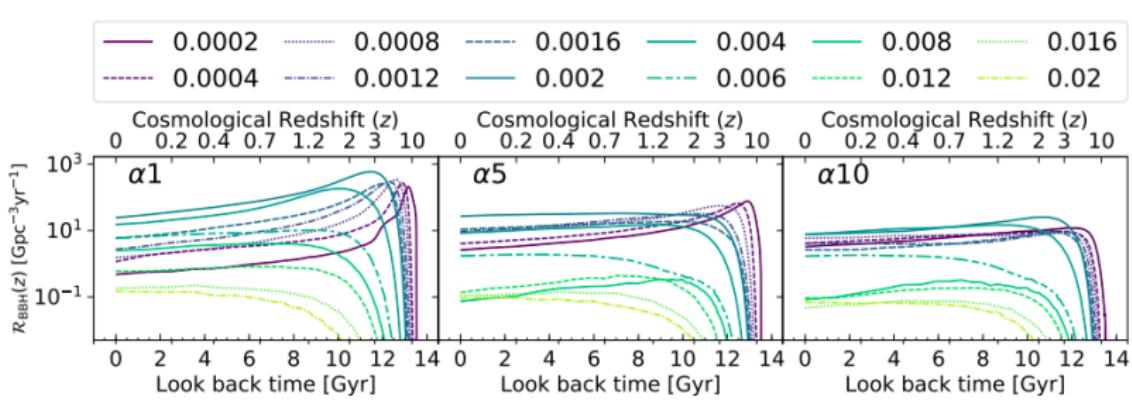
Metallicity CCSN model	$Z = 0.02$			$Z = 0.015$		
	Rap	Del	Com	Rap	Del	Com
Natal kick model		Maxwellian ( $\sigma = 70 \text{ km/s}$ )				
BBHs	5626	5248	18425	10350	7564	27740
after a WR–BH	100%	100%	100%	99%	99%	100%
GW–BBHs	207	171	949	418	282	1287
after a WR–BH	207	171	948	418	281	1285
Cyg X-3 candidates	14	8	76	16	10	18
becoming GW–BBHs	14	6	76	16	9	18
Natal kick model		Maxwellian ( $\sigma = 265 \text{ km/s}$ )				
BBHs	166	156	727	416	260	1420
after a WR–BH	100%	100%	100%	99%	99%	100%
GW–BBHs	34	21	221	101	67	392
after a WR–BH	34	21	221	101	67	392
Cyg X-3 candidates	4	2	29	6	4	7
becoming GW–BBHs	4	0	23	5	3	7

# Results (2)

Metallicity CCSN model	$Z = 0.02$			$Z = 0.015$		
	Rap	Del	Com	Rap	Del	Com
Natal kick model	Maxwellian + fallback					
BBHs	44307	35029	96557	55986	45701	109935
after a WR–BH	100%	100%	96%	92%	96%	94%
GW–BBHs	70	108	271	230	173	201
after a WR–BH	70	108	257	225	168	189
Cyg X-3 candidates	15	6	70	19	12	22
becoming GW–BBHs	15	5	70	19	9	22
Natal kick model	Unified					
BBHs	55655	46373	142613	71016	61257	157671
after a WR–BH	90%	95%	68%	87%	88%	69%
GW–BBHs	45	62	246	74	76	177
after a WR–BH	45	57	244	73	73	177
Cyg X-3 candidates	16	7	70	19	9	22
becoming GW–BBHs	16	6	70	19	9	22

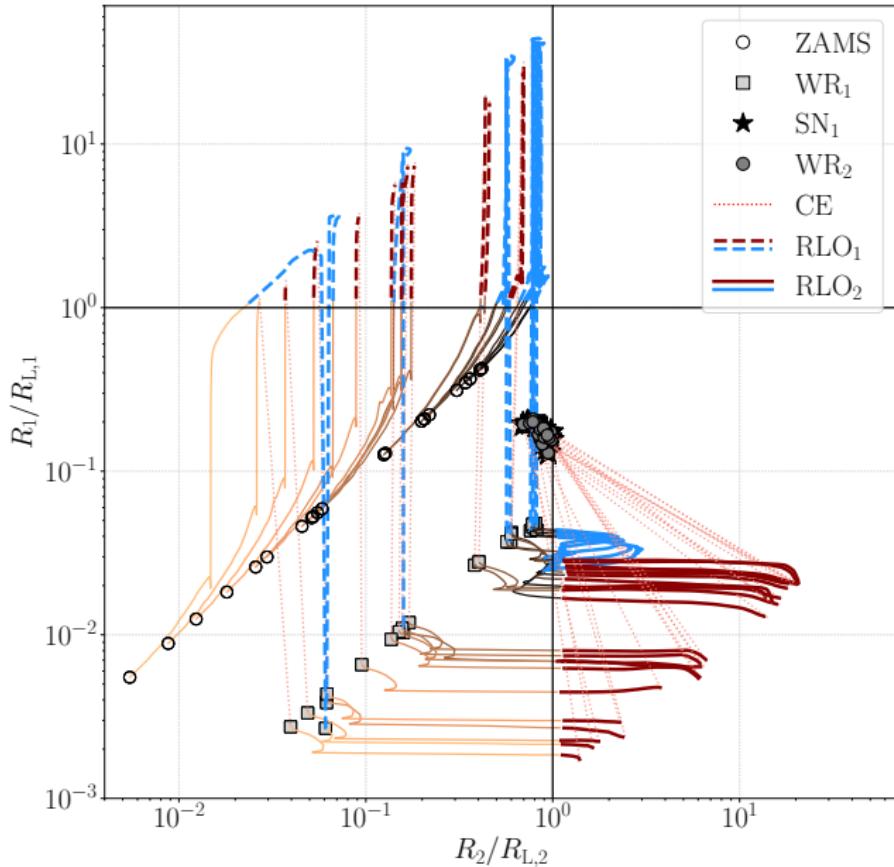
# Merger redshift and metallicity

~ 10% of today's BBH mergers have solar metallicity

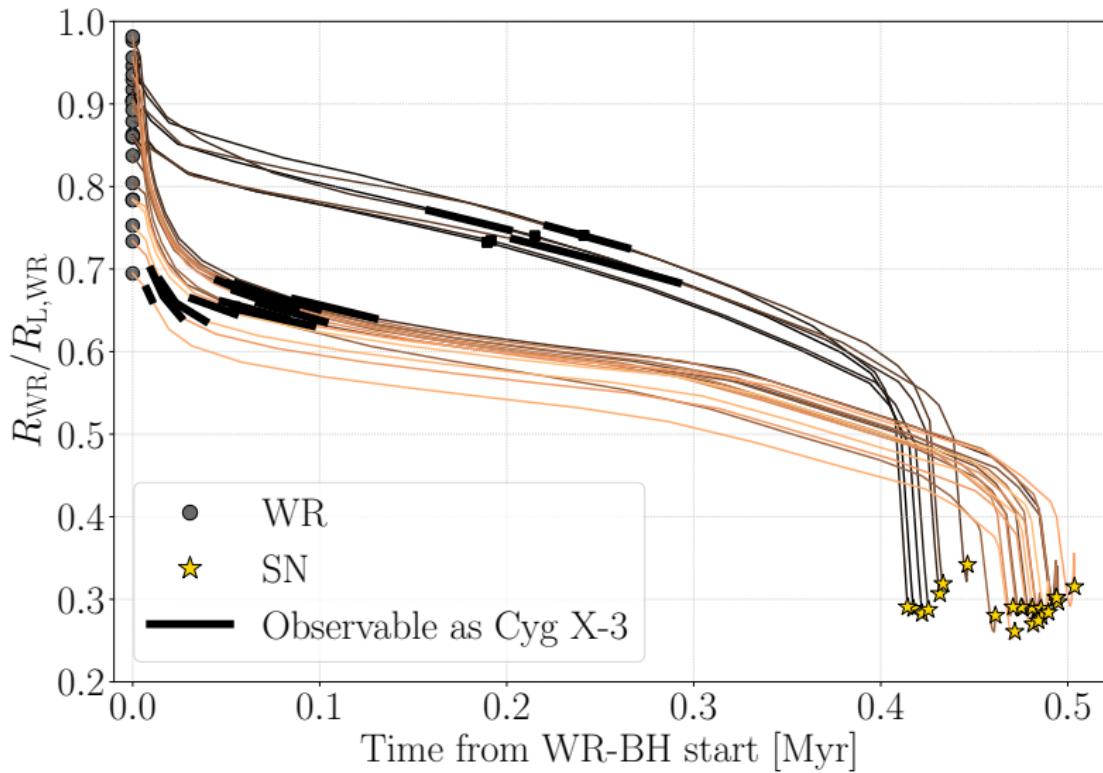


Santoliquido et al. 2021

## Fiducial evolution of Cyg X-3



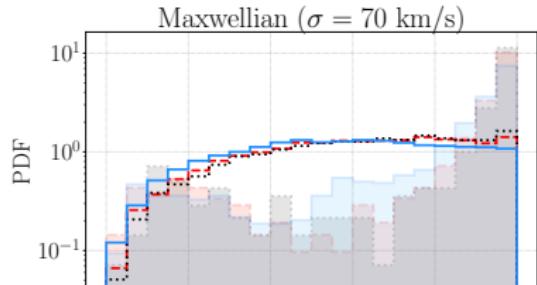
# Observability of Cyg X-3



# Influence of the parameter space

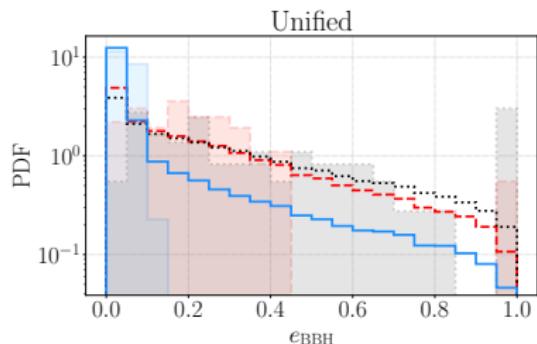
## Metallicity:

- Negligible impact ( $Z_{\odot}=0.02$  vs  $Z_{\odot}=0.015$ )
- $\neq$  number of systems,  $\approx$  probability



## Kick

- Strong kicks  $\rightarrow e_{\text{BBH}} \sim 1$  probable  
 $t_{\text{GW}} \propto (1 - e^2)^{7/2}$  *Peters 1964*
- Merging BBHs for  $a_{\text{BBH}} \lesssim 1000 R_{\odot}$



## Core-collapse supernova:

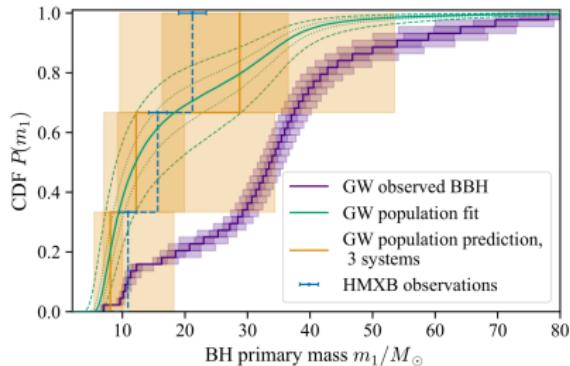
- Compact object mass and nature
- Selects mass transfer evolution



# X-ray binaries and possible tensions

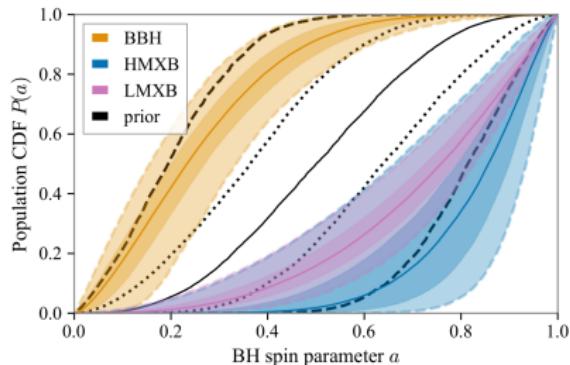
## High Mass X-ray binaries:

- accreting **black hole**
- **massive donor** ( $\gtrsim 5 M_{\odot}$ )



## Are progenitors of binary black holes?:

- Difficult to characterize (mass, spin)
- Compatible in the mass distribution
- **Tension in the spin distribution**



The debate is still open!

# SEVN speed

